

Exercise 5.1

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N = The set of natural numbers = $\{1, 2, 3, 4, \dots\}$

W = The set of whole numbers = $\{0, 1, 2, 3, 4, \dots\}$

Z = The set of all integers = $\{0, \pm 1, \pm 2, \pm 3, \dots\}$

E = The set of all even integers = $\{0, \pm 2, \pm 4, \dots\}$

O = The set of all odd integers = $\{\pm 1, \pm 3, \pm 5, \dots\}$

P = The set of prime numbers = $\{2, 3, 5, 7, 11, 13, 17, \dots\}$

Q = The set of all rational numbers = $\{x \mid x = \frac{m}{n}, \text{ where } m, n \in Z \text{ and } n \neq 0\}$

Q' = The set of all irrational numbers = $\{x \mid x \neq \frac{m}{n}, \text{ where } m, n \in Z \text{ and } n \neq 0\}$

R = The set of all real numbers = $Q \cup Q'$.

Q. 1: If $X = \{1, 4, 7, 9\}$ and $Y = \{2, 4, 5, 9\}$

Then find:

(i) $X \cup Y = \{1, 4, 7, 9\} \cup \{2, 4, 5, 9\}$
 $= \{1, 2, 4, 5, 7, 9\}$

(ii) $X \cap Y = \{1, 4, 7, 9\} \cap \{2, 4, 5, 9\}$
 $= \{4, 9\}$

(iii) $Y \cup X = \{2, 4, 5, 9\} \cup \{1, 4, 7, 9\}$
 $= \{1, 2, 4, 5, 7, 9\}$

(iv) $Y \cap X = \{2, 4, 5, 9\} \cap \{1, 4, 7, 9\}$
 $= \{4, 9\}$

Q. 2: If $X = \text{Set of prime numbers less than or equal to 17}$

and $Y = \text{Set of first 12 natural numbers, then find the following}$

$X = \{2, 3, 5, 7, 11, 13, 17\}$

$Y = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$

(i) $X \cup Y = \{2, 3, 5, 7, 11, 13, 17\} \cup \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$
 $= \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 17\}$
 $= Y \cup \{13, 17\}$

(ii) $X \cap Y = \{2, 3, 5, 7, 11, 13, 17\} \cap \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$
 $= \{2, 3, 5, 7, 11\}$

(iii) $Y \cup X = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\} \cup \{2, 3, 5, 7, 11, 13, 17\}$
 $= \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 17\}$
 $= Y \cup \{13, 17\}$

(iv) $Y \cap X = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\} \cap \{2, 3, 5, 7, 11, 13, 17\}$
 $= \{2, 3, 5, 7, 11\}$

Q. 3: If $X = \emptyset, Y = Z^+, T = O^+$, then find:

$$X = \{ \}$$

$$Y = \{1, 2, 3, 4, 5, \dots\}$$

$$T = \{1, 3, 5, \dots\}$$

$$\begin{aligned} \text{(i)} \quad X \cup Y &= \{ \} \cup \{1, 2, 3, 4, 5, \dots\} \\ &= \{1, 2, 3, 4, 5, \dots\} \\ &= Y \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad X \cup T &= \{ \} \cup \{1, 3, 5, \dots\} \\ &= \{1, 3, 5, \dots\} \\ &= T \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad Y \cup T &= \{1, 2, 3, 4, 5, \dots\} \cup \{1, 3, 5, \dots\} \\ &= \{1, 2, 3, 4, 5, \dots\} \\ &= Y \end{aligned}$$

$$\begin{aligned} \text{(iv)} \quad X \cap Y &= \{ \} \cap \{1, 2, 3, 4, 5, \dots\} \\ &= \{ \} \end{aligned}$$

$$\begin{aligned} \text{(v)} \quad X \cap T &= \{ \} \cap \{1, 3, 5, \dots\} \\ &= \{ \} \end{aligned}$$

$$\begin{aligned} \text{(vi)} \quad Y \cap T &= \{1, 2, 3, 4, 5, \dots\} \cap \{1, 3, 5, \dots\} \\ &= \{1, 3, 5, \dots\} \\ &= T \end{aligned}$$

Q. 4: If $U = \{x | x \in N \wedge 3 < x \leq 25\}$

$$X = \{x | x \text{ is prime} \wedge 8 < x < 25\}$$

$$\text{and } Y = \{x | x \in W \wedge 4 \leq x \leq 17\}$$

Find the value of:

So,

$$U = \{4, 5, 6, \dots, 25\}$$

$$X = \{11, 13, 17, 19, 23\}$$

$$Y = \{4, 5, 6, \dots, 17\}$$

$$\begin{aligned} \text{(i)} \quad (X \cup Y)' &= U - (X \cup Y) \\ &= \{4, 5, 6, \dots, 25\} - (\{11, 13, 17, 19, 23\} \cup \{4, 5, 6, \dots, 17\}) \\ &= \{4, 5, 6, \dots, 25\} - \{4, 5, 6, \dots, 17, 19, 23\} \\ &= \{18, 20, 21, 22, 24, 25\} \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad X' \cap Y' &= (U - X) \cap (U - Y) \\ &= (\{4, 5, 6, \dots, 25\} - \{11, 13, 17, 19, 23\}) \cap (\{4, 5, 6, \dots, 25\} - \{4, 5, 6, \dots, 17\}) \\ &= \{4, 5, 6, \dots, 10, 11, 12, 14, 15, 16, 18, 20, 21, 22, 24, 25\} \cap \{18, 19, 20, 21, 22, 23, 24, 25\} \\ &= \{18, 20, 21, 22, 24, 25\} \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad (X \cap Y)' &= U - (X \cap Y) \\ &= \{4, 5, 6, \dots, 25\} - (\{11, 13, 17, 19, 23\} \cap \{4, 5, 6, \dots, 17\}) \end{aligned}$$

$$= \{4, 5, 6, \dots, 25\} - \{11, 13, 17\}$$

$$= \{4, 5, 6, \dots, 10, 12, 14, 15, 16, 18, 19, 20, \dots, 25\}$$

(iv) $X' \cup Y'$

$$X' \cup Y' = (U - X) \cup (U - Y)$$

$$= (\{4, 5, 6, \dots, 25\} - \{11, 13, 17, 19, 23\}) \cup (\{4, 5, 6, \dots, 25\} - \{4, 5, 6, \dots, 17\})$$

$$= \{4, 5, 6, \dots, 10, 12, 14, 15, 16, 18, 20, 21, 22, 24, 25\} \cup \{18, 19, 20, 21, 22, 23, 24, 25\}$$

$$= \{4, 5, 6, \dots, 10, 12, 14, 15, 16, 18, 19, 20, \dots, 25\}$$

Q. 5: If $X = \{2, 4, 6, \dots, 20\}$ and $Y = \{4, 8, 12, \dots, 24\}$ then find the following:

(i) $X - Y = \{2, 4, 6, \dots, 20\} - \{4, 8, 12, \dots, 24\}$

$$= \{2, 6, 10, 14, 18\}$$

(ii) $Y - X = \{4, 8, 12, \dots, 24\} - \{2, 4, 6, \dots, 20\}$

$$= \{24\}$$

Q. 6: If $A = N$ and $B = W$ then find the following:

$$A = \{1, 2, 3, \dots\}$$

$$B = \{0, 1, 2, \dots\}$$

(i) $A - B = \{1, 2, 3, \dots\} - \{0, 1, 2, \dots\}$

$$= \{ \}$$

(ii) $B - A = \{0, 1, 2, \dots\} - \{1, 2, 3, \dots\}$

$$= \{0\}$$