Exercise 1.2

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Q. 1: Solve the following equations using quadratic formula.

(i)
$$2 - x^{2} = 7x$$

$$-x^{2} - 7x + 2 = 0$$

$$a = -1, b = -7, c = 2$$

$$x = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$$

$$x = \frac{-(-7) \pm \sqrt{(-7)^{2} - 4(-1)(2)}}{2(-1)}$$

$$x = \frac{7 \pm \sqrt{49 + 8}}{-2}$$

$$x = \frac{7 \pm \sqrt{57}}{-2}$$
S.S = $\left\{\frac{7 \pm \sqrt{57}}{-2}\right\}$

(ii)
$$5x^2 + 8x + 1 = 0$$

 $a = 5$, $b = 8$, $c = 1$
 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
 $x = \frac{-(8) \pm \sqrt{(8)^2 - 4(5)(1)}}{2(5)}$
 $x = \frac{-8 \pm \sqrt{64 - 20}}{10}$
 $x = \frac{-8 \pm \sqrt{44}}{10}$
 $x = \frac{-8 \pm \sqrt{4 \times 11}}{10}$
 $x = \frac{-8 \pm 2\sqrt{11}}{10}$
 $x = \frac{2(-4 \pm \sqrt{11})}{10}$
 $x = \frac{-4 \pm \sqrt{11}}{5}$

S.S =
$$\left\{\frac{-4\pm\sqrt{11}}{5}\right\}$$

(iii) $\sqrt{3}x^2 + x = 4\sqrt{3}$
 $\sqrt{3}x^2 + x - 4\sqrt{3} = 0$
 $a = \sqrt{3}$, $b = 1$, $c = -4\sqrt{3}$
 $x = \frac{-b\pm\sqrt{b^2-4ac}}{2a}$
 $x = \frac{-(1)\pm\sqrt{(1)^2-4(\sqrt{3})(-4\sqrt{3})}}{2(\sqrt{3})}$
 $x = \frac{-1\pm\sqrt{1+16(\sqrt{3})^2}}{2\sqrt{3}}$
 $x = \frac{-1\pm\sqrt{1+16(3)}}{2\sqrt{3}}$

$$x = \frac{-1 \pm \sqrt{1+48}}{2\sqrt{3}}$$

$$x = \frac{-1 \pm \sqrt{49}}{2\sqrt{3}}$$

$$x = \frac{-1 \pm 7}{2\sqrt{3}}$$

$$x = \frac{-1+7}{2\sqrt{3}}$$

$$x = \frac{6}{2\sqrt{3}}$$

$$x = \frac{3}{\sqrt{3}}$$

and

and

$$x = \frac{-1-7}{2\sqrt{3}}$$

$$x = \frac{-8}{2\sqrt{3}}$$

$$x = \frac{-4}{\sqrt{3}}$$

$$x = \frac{6}{2\sqrt{3}}$$

$$=\frac{6}{2\sqrt{3}}$$

$$\chi = \frac{-8}{2\sqrt{3}}$$

$$x = \frac{3}{\sqrt{3}}$$

$$\frac{3}{\sqrt{2}}$$
 and

$$\boldsymbol{x}$$

$$x = \frac{-4}{\sqrt{3}}$$

$$= \frac{3}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} \qquad \text{and} \qquad$$

 \boldsymbol{x}

$$= \frac{-4}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$= \frac{3\sqrt{3}}{\left(\sqrt{3}\right)^2} \qquad \text{and}$$
$$= \frac{3\sqrt{3}}{3} \qquad \text{and}$$

$$=\frac{3\sqrt{3}}{3}$$

$$x = \frac{-4\sqrt{3}}{(\sqrt{3})^2}$$

$$x = \frac{-4\sqrt{3}}{3}$$

(iv)

$$x = \sqrt{3}$$
 and

$$x = \frac{-4\sqrt{3}}{3}$$

$$S.S = \left\{ \sqrt{3}, \frac{-4\sqrt{3}}{3} \right\}$$

$$4x^2 - 14 = 3x$$

$$4x^2 - 3x - 14 = 0$$

$$a = 4$$
, $b = -3$, $c = -14$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-3)\pm\sqrt{(-3)^2-4(4)(-14)}}{2(4)}$$

$$x = \frac{3 \pm \sqrt{9 + 224}}{8}$$

$$=\frac{3\pm\sqrt{233}}{8}$$

$$=$$
 $\left\{\frac{3\pm\sqrt{233}}{233}\right\}$

(v)
$$6x^2 - 3 - 7x = 0$$

$$6x^2 - 7x - 3 = 0$$

$$= -7$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$=\frac{-(-7)\pm\sqrt{(-7)^2-4(6)(-3)}}{2(6)}$$

$$x = \frac{7 \pm \sqrt{49 + 72}}{12}$$

$$x = \frac{7 \pm \sqrt{121}}{12}$$

$$x = \frac{7 \pm 11}{12}$$

$$=\frac{7+11}{12}$$

and

$$x = \frac{7-11}{12}$$

$$\boldsymbol{x}$$

X

$$=\frac{18}{12}$$

$$x = \frac{-4}{12}$$

$$x = \frac{3}{2}$$
 and $x = \frac{-1}{3}$
S.S = $\left\{\frac{3}{2}, \frac{-1}{3}\right\}$

(vi)
$$3x^2 + 8x + 2 = 0$$

a = 3, b = 8, c = 2

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(8) \pm \sqrt{(8)^2 - 4(3)(2)}}{2(3)}$$

$$x = \frac{-8 \pm \sqrt{64 - 24}}{6}$$

$$x = \frac{-8 \pm \sqrt{40}}{6}$$

$$x = \frac{-8 \pm \sqrt{4 \times 10}}{6}$$

$$x = \frac{-8 \pm 2\sqrt{10}}{6}$$

$$x = \frac{2(-4 \pm \sqrt{10})}{6}$$

$$x = \frac{-4 \pm \sqrt{10}}{3}$$

$$x = \frac{-4 + \sqrt{10}}{3}$$
and
$$x$$
S.S = $\left\{ \frac{-4 + \sqrt{10}}{3}, \frac{-4 - \sqrt{10}}{3} \right\}$

S.S =
$$\left\{ \frac{-4+\sqrt{10}}{3}, \frac{-4-\sqrt{10}}{3} \right\}$$

(vii) $\frac{3}{x-6} - \frac{4}{x-5} = 1$
 $\frac{3(x-5)-4(x-6)}{(x-6)(x-5)} = 1$

$$\frac{3x-15-4x+24}{x^2-6x-5x+30} = 1$$

$$\frac{-x+9}{x^2-11x+30} = 1$$

$$-x + 9 = x^2 - 11x + 30$$
$$= x^2 - 11x + 30 + x - 9$$

$$0 = x^2 - 10x + 21$$

a = 1, b = -10, c = 21

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(1)(21)}}{2(1)}$$

$$x = \frac{10 \pm \sqrt{100 - 84}}{2}$$

$$x = \frac{10 \pm \sqrt{16}}{2}$$

$$x = \frac{10\pm 4}{2}$$

$$x = \frac{10+4}{2}$$
 and $x = \frac{10-4}{2}$
 $x = \frac{14}{2}$ and $x = \frac{6}{2}$

S.S =
$$\{7,3\}$$

(viii) $\frac{x+2}{x-1} - \frac{4-x}{2x} = 2\frac{1}{3}$
 $\frac{2x(x+2)-(4-x)(x-1)}{2x(x-1)} = \frac{7}{3}$
 $\frac{(2x^2+4x)-(4x-4-x^2+x)}{2x^2-2x} = \frac{7}{3}$
 $\frac{(2x^2+4x)-(5x-4-x^2)}{2x^2-2x} = \frac{7}{3}$
 $\frac{2x^2+4x-5x+4+x^2}{2x^2-2x} = \frac{7}{3}$
 $\frac{3x^2-x+4}{2x^2-2x} = \frac{7}{3}$
 $3(3x^2-x+4) = 7(2x^2-2x)$
 $9x^2-3x+12 = 14x^2-14x$
 $9x^2-3x+12-14x^2+14x = 0$
 $-5x^2+11x+12 = 0$

$$a = -5, \qquad b = 11, \qquad c = 12$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(11) \pm \sqrt{(11)^2 - 4(-5)(12)}}{2(-5)}$$

$$x = \frac{-11 \pm \sqrt{361}}{-10}$$

$$x = \frac{-11 \pm 19}{-10}$$

$$x = \frac{-11 \pm 19}{-10}$$

$$x = \frac{8}{-10} \qquad \text{and} \qquad x = \frac{-30}{-10}$$

$$x = \frac{-30}{-10}$$

$$x = \frac{-30}{-10}$$

$$x = \frac{-4}{-10} \qquad \text{and} \qquad x = 3$$

S.S =
$$\left\{\frac{-4}{5}, 3\right\}$$

(ix) $\frac{a}{x-b} + \frac{b}{x-a} = 2$
 $\frac{a(x-a)+b(x-b)}{(x-a)(x-b)} = 2$
 $\frac{ax-a^2+bx-b^2}{x^2-bx-ax+ab} = 2$
 $\frac{ax+bx-a^2-b^2}{x^2-ax-bx+ab} = 2$
 $ax + bx - a^2 - b^2 = 2(x^2 - ax - bx + ab)$
 $ax + bx - a^2 - b^2 = 2x^2 - 2ax - 2bx + 2ab$
 $0 = 2x^2 - 2ax - 2bx + 2ab - ax - bx + a^2 + b^2$
 $0 = 2x^2 - 3ax - 3bx + 2ab + a^2 + b^2$
 $0 = 2x^2 - 3(a+b)x + 2ab + a^2 + b^2$

a = 2, b = -3(a + b), c =
$$a^2 + b^2 + 2ab$$

$$x = \frac{-b \pm \sqrt{(b)^2 - 4ac}}{2a}$$

$$x = \frac{-(-3(a+b)) \pm \sqrt{(-3(a+b))^2 - 4(2)(a^2 + b^2 + 2ab)}}{2(2)}$$

$$x = \frac{3a + 3b \pm \sqrt{9(a+b)^2 - 8(a+b)^2}}{4}$$

$$x = \frac{3a + 3b \pm \sqrt{(a+b)^2}}{4}$$

$$x = \frac{3a + 3b \pm \sqrt{(a+b)^2}}{4}$$

$$x = \frac{3a+3b+(a+b)}{4}$$
 and $x = \frac{3a+3b-(a+b)}{4}$
 $x = \frac{3a+3b+a+b}{4}$ and $x = \frac{3a+3b-a-b}{4}$
 $x = \frac{4a+4b}{4}$ and $x = \frac{2a+2b}{4}$
 $x = \frac{4(a+b)}{4}$ and $x = \frac{2(a+b)}{4}$
 $x = a+b$ and $x = \frac{a+b}{2}$
S.S = $\left\{a+b, \frac{a+b}{2}\right\}$

a = -l, b =
$$(2l + m)$$
, c = $-(l + m)$

$$x = \frac{-b \pm \sqrt{(b)^2 - 4ac}}{2a}$$

$$x = \frac{-(2l+m) \pm \sqrt{(2l+m)^2 - 4(-l)(-(l+m))}}{2(-l)}$$

$$x = \frac{-(2l+m) \pm \sqrt{4l^2 + m^2 + 4lm - 4l^2 - 4lm}}{2(-l)}$$

$$x = \frac{-2l}{x}$$

$$x = \frac{-(2l+m)\pm\sqrt{m^2}}{-2l}$$

$$x = \frac{-(2l+m)\pm m}{-2l}$$

 $-(l+m)-lx^2+(2l+m)x$

 $-lx^2 + (2l + m)x - (l + m)$

(x)

$$x = \frac{-(2l+m)\pm\sqrt{4l^2+m^2+4lm-4l^2-4lm}}{-2l}$$

$$x = \frac{-(2l+m)\pm\sqrt{m^2}}{-2l}$$

$$x = \frac{-(2l+m)\pm m}{-2l}$$

$$x = \frac{-2l-m+m}{-2l} \quad \text{and} \quad x = \frac{-2l-m-m}{-2l}$$

$$x = \frac{-2l}{-2l} \quad \text{and} \quad x = \frac{-2l-2m}{-2l}$$

$$x = 1 \quad \text{and} \quad x = \frac{-2(l+m)}{-2l}$$

S.S =
$$\left\{1, \frac{l+m}{l}\right\}$$