Exercise 6.2

Q.1 Simplify each of the following as a rational expression.

(i)
$$\frac{x^2 - x - 6}{x^2 - 9} + \frac{x^2 + 2x - 24}{x^2 - x - 12}$$
Solution:
$$\frac{x^2 - x - 6}{x^2 - 9} + \frac{x^2 + 2x - 24}{x^2 - x - 12}$$

$$= \frac{x^2 - x - 6}{x^2 - 9} + \frac{x^2 + 2x - 24}{x^2 - x - 12}$$

$$= \frac{x^2 - 3x + 2x - 6}{(x)^2 - (3)^2} + \frac{x^2 + 6x - 4x - 24}{x^2 - x - 12}$$

$$= \frac{x(x - 3) + 2(x - 3)}{(x - 3)(x + 3)} + \frac{x(x + 6) - 4(x + 6)}{x(x - 4) + 3(x - 4)}$$

$$= \frac{(x - 3)(x + 2)}{(x - 3)(x + 3)} + \frac{(x + 6)(x - 4)}{(x - 4)(x + 3)}$$

$$= \frac{(x + 2)}{(x + 3)} + \frac{(x + 6)}{(x + 3)}$$

$$= \frac{x + 2 + x + 6}{x + 3}$$

$$= \frac{2(x + 4)}{x + 3}$$

Q.2
$$\left[\frac{x+1}{x-1} - \frac{x-1}{x+1} - \frac{4x}{x^2+1}\right] + \frac{4x}{x^4-1}$$
Solution:
$$\left[\frac{x+1}{x-1} - \frac{x-1}{x+1} - \frac{4x}{x^2+1}\right] + \frac{4x}{x^4-1}$$

$$= \left[\frac{x+1}{x-1} - \frac{x-1}{x+1} - \frac{4x}{x^2+1}\right] + \frac{4x}{x^4-1}$$

$$= \left[\frac{(x+1)^2 - (x-1)^2}{(x-1)(x+1)} - \frac{4x}{x^2+1}\right] + \frac{4x}{x^4-1}$$

$$= \left[\frac{x^2 + 2x + 1 - (x^2 + 1 - 2x)}{(x-1)(x+1)} - \frac{4x}{x^2+1}\right] + \frac{4x}{x^4-1}$$

$$= \left[\frac{x^2 + 2x + 1 - x^2 + 1 + 2x}{x^2 - 1} - \frac{4x}{x^2 + 1} \right] + \left[\frac{4x}{x^4 - 1} \right]$$

$$= \left[\frac{4x}{x^2 - 1} - \frac{4x}{x^2 + 1} \right] + \frac{4x}{x^4 - 1}$$

$$= \left[\frac{4x(x^2 + 1) - 4x(x^2 - 1)}{(x^2 - 1)(x^2 + 1)} \right] + \frac{4x}{x^4 - 1}$$

$$= \left[\frac{4x^3 + 4x - 4x^3 + 4x}{x^4 - 1} \right] + \frac{4x}{x^4 - 1}$$

$$= \frac{8x}{x^4 - 1} + \frac{4x}{x^4 - 1}$$

$$= \frac{8x + 4x}{x^4 - 1}$$

$$= \frac{12x}{x^4 - 1}$$

Q.3
$$\frac{1}{x^2 - 8x + 15} + \frac{1}{x^2 - 4x + 3} - \frac{2}{x^2 - 6x + 5}$$
Solution:
$$\frac{1}{x^2 - 8x + 15} + \frac{1}{x^2 - 4x + 3} - \frac{2}{x^2 - 6x + 5}$$

$$= \frac{1}{x^2 - 8x + 15} + \frac{1}{x^2 - 4x + 3} - \frac{2}{x^2 - 6x + 5}$$

$$= \frac{1}{x^2 - 3x - 5x + 15} + \frac{1}{x^2 - 3x - 1x + 3} - \frac{2}{x^2 - 5x - x + 5}$$

$$= \frac{1}{x(x - 3) - 5(x - 3)} + \frac{1}{x(x - 3) - 1(x - 3)} - \frac{2}{x(x - 5) - 1(x - 5)}$$

$$= \frac{1}{(x - 3)(x - 5)} + \frac{1}{(x - 3)(x - 1)} - \frac{2}{(x - 5)(x - 1)}$$

$$= \frac{(x - 1) + (x - 5) - 2(x - 3)}{(x - 3)(x - 5)(x - 1)}$$

$$= \frac{(x - 1) + (x - 5) - 2(x + 6)}{(x - 3)(x - 5)(x - 1)}$$

$$= \frac{0}{(x - 3)(x - 5)(x - 1)}$$

Q.4
$$\frac{(x+2)(x+3)}{x^2-9} + \frac{(x+2)(2x^2-32)}{(x-4)(x^2-x-6)}$$
Solution:
$$\frac{(x+2)(x+3)}{x^2-9} + \frac{(x+2)(2x^2-32)}{(x-4)(x^2-x-6)}$$

$$= \frac{(x+2)(x+3)}{x^2-9} + \frac{(x+2)(2x^2-32)}{(x-4)(x^2-x-6)}$$

$$= \frac{(x+2)(x+3)}{(x)^2-(3)^2} + \frac{(x+2)\left[2(x^2-16)\right]}{(x-4)(x^2-3x+2x-6)}$$

$$= \frac{(x+2)(x+3)}{(x-3)(x+3)} + \frac{(x+2)\left[2(x)^2-(4)^2\right]}{(x-4)\left[x(x-3)+2(x-3)\right]}$$

$$= \frac{(x+2)}{(x-3)} + \frac{(x+2)\left[2(x+4)(x-4)\right]}{(x-4)(x-3)(x+2)}$$

$$= \frac{(x+2)}{(x-3)} + \frac{2(x+4)}{(x-3)}$$

$$= \frac{x+2}{x-3} + \frac{2x+8}{x-3}$$

$$= \frac{x+2+2x+8}{x-3}$$

$$= \frac{3x+10}{3x+10}$$

free ilm.

Q.5 =
$$\frac{x+3}{2x^2+9x+9} + \frac{1}{2(2x-3)} - \frac{4x}{4x^2-9}$$

Solution: = $\frac{x+3}{2x^2+9x+9} + \frac{1}{2(2x-3)} - \frac{4x}{4x^2-9}$
= $\frac{x+3}{2x^2+9x+9} + \frac{1}{2(2x-3)} - \frac{4x}{4x^2-9}$
= $\frac{x+3}{2x^2+6x+3x+9} + \frac{1}{2(2x-3)} - \frac{4x}{(2x)^2-(3)^2}$
= $\frac{x+3}{2x(x+3)+3(x+3)} + \frac{1}{2(2x-3)} - \frac{4x}{(2x-3)(2x+3)}$
= $\frac{(x+3)}{(x+3)(2x+3)} + \frac{1}{2(2x-3)} - \frac{4x}{(2x-3)(2x+3)}$
= $\frac{1}{2x+3} + \frac{1}{2(2x-3)} - \frac{4x}{(2x-3)(2x+3)}$
= $\frac{1}{2x+3} + \frac{1}{2(2x-3)} - \frac{4x}{(2x-3)(2x+3)}$
= $\frac{2(2x-3)+(2x+3)-4x\times2}{2(2x-3)(2x+3)}$
= $\frac{4x-6+2x+3-8x}{2(2x-3)(2x+3)}$

$$= \frac{-2x-3}{2(2x-3)(2x+3)}$$

$$= \frac{-1(2x+3)}{2(2x-3)(2x+3)}$$

$$= \frac{-1}{2(2x-3)}$$

Q.6
$$A - \frac{1}{A}$$
, Where $A = \frac{a+1}{a-1}$
Solution: $A - \frac{1}{A}$, Where $A = \frac{a+1}{a-1}$
 $= A - \frac{1}{A} = ?$

$$= \frac{a+1}{a-1} \cdot \frac{a-1}{a+1}$$

$$= \frac{(a+1)^2 - (a-1)^2}{(a-1)(a+1)}$$

$$= \frac{a^2 + 2a + 1 - (a^2 - 2a + 1)}{a^2 - 1}$$

$$= \frac{a^2 + 2a + 1 - a^2 + 2a + 1}{a^2 - 1}$$

$$= \frac{4a}{a^2 - 1}$$

Q.7
$$\left[\frac{x-1}{x-2} + \frac{2}{2-x}\right] - \left[\frac{x+1}{x+2} + \frac{4}{4-x^2}\right]$$
Solution:
$$\left[\frac{x-1}{x-2} + \frac{2}{2-x}\right] - \left[\frac{x+1}{x+2} + \frac{4}{4-x^2}\right]$$

$$= \left[\frac{x-1}{x-2} + \frac{2}{2-x}\right] - \left[\frac{x+1}{x+2} + \frac{4}{4-x^2}\right]$$

$$= \left[\frac{x-1}{x-2} + \frac{2}{-x+2}\right] - \left[\frac{x+1}{x+2} + \frac{4}{-x^2+4}\right]$$

$$= \left[\frac{x-1}{x-2} - \frac{2}{x-2}\right] - \left[\frac{x+1}{x+2} + \frac{4}{-(x^2-4)}\right]$$

$$= \left[\frac{x-1}{x-2} - \frac{2}{x-2}\right] - \left[\frac{x+1}{x+2} + \frac{4}{-(x^2-4)}\right]$$

$$= \left[\frac{x-1-2}{x-2}\right] - \left[\frac{x+1}{x+2} - \frac{4}{(x+2)(x-2)}\right]$$

$$= \frac{(x-3)}{(x-2)} - \frac{(x+1)(x-2)-4}{(x+2)(x-2)}$$

$$= \frac{x-3}{x-2} - \frac{x^2 - x - 2 - 4}{(x+2)(x-2)}$$

$$= \frac{x-3}{x-2} - \frac{x^2 - x - 6}{(x-2)(x+2)}$$

$$= \frac{x-3}{x-2} - \frac{x^2 - 3x + 2x - 6}{(x-2)(x+2)}$$

$$= \frac{x-3}{x-2} - \frac{x(x-3)2(x-3)}{(x-2)(x+2)}$$

$$= \frac{x-3}{x-2} - \frac{(x-3)(x+2)}{(x-2)(x+2)}$$

$$= \frac{x-3}{x-2} - \frac{(x-3)(x+2)}{(x-2)(x+2)}$$

$$= \frac{x-3}{x-2} - \frac{x-3}{(x-2)(x+2)}$$
O Ans.



free ilm.

Q.8 What rational number should be subtracted from

$$= \frac{2x^2 + 2x - 7}{x^2 + x - 6} \text{ to get } \frac{x - 1}{x - 2}$$

Solution: let required rational number be P(x)

According to condition

$$\frac{2x^2 + 2x - 7}{x^2 + x - 6} - P(x) = \frac{x - 1}{x - 2}$$

$$P(x) = \frac{2x^2 + 2x - 7}{x^2 + x - 6} - \frac{x - 1}{x - 2}$$

$$= \frac{2x^2 + 2x - 7}{x^2 + 3x - 2x - 6} - \frac{x - 1}{x - 2}$$

$$= \frac{2x^2 + 2x - 7}{x(x + 3) - 2(x + 3)} - \frac{x - 1}{x - 2}$$

$$= \frac{2x^2 + 2x - 7}{(x + 3)(x - 2)} - \frac{x - 1}{x - 2}$$

$$= \frac{2x^2 + 2x - 7}{(x + 3)(x - 2)} - \frac{x - 1}{(x + 3)(x - 2)}$$

$$= \frac{2x^2 + 2x - 7 - (x - 1)(x + 3)}{(x + 3)(x - 2)}$$

$$= \frac{2x^2 + 2x - 7 - x^2 - 2x + 3}{(x+3)(x-2)}$$

$$= \frac{x^2 - 4}{(x+3)(x-2)}$$

$$= \frac{x^2 - 2^2}{(x+3)(x-2)}$$

$$= \frac{(x+2)(x-2)}{(x+3)(x-2)}$$

$$= \frac{x+2}{x+3}$$

Q.9 =
$$\frac{x^2 + x - 6}{x^2 - x - 6} \times \frac{x^2 - 4}{x^2 - 9}$$

Q.10
$$\frac{x^3 - 8}{x^2 - 4} \times \frac{x^2 + 6x + 8}{x^2 - 2x + 1}$$
Solution:
$$\frac{x^3 - 8}{x^2 - 4} \times \frac{x^2 + 6x + 8}{x^2 - 2x + 1}$$

$$= \frac{x^3 - 8}{x^2 - 4} \times \frac{x^2 + 6x + 8}{x^2 - 2x + 1}$$

$$= \frac{(x)^3 - (2)^3}{(x^2) - (2)^2} \times \frac{x^2 + 4x + 2x + 8}{x^2 - x - x + 1}$$

$$= \frac{(x - 2)(x^2 + 2x + 4)}{(x - 2)(x + 2)} \times \frac{x(x + 4) + 2(x + 4)}{x(x - 1) - 1(x - 1)}$$

$$= \frac{x^2 + 2x + 4}{(x + 2)} \times \frac{(x + 4)(x + 2)}{(x - 1)(x - 1)}$$

$$= \frac{(x^2 + 2x + 4)(x + 4)}{(x - 1)^2}$$

Q.11
$$\frac{x^4 - 8x}{2x^2 + 5x - 3} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x^2 - 2x}$$
Solution:
$$\frac{x^4 - 8x}{2x^2 + 5x - 3} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x^2 - 2x}$$

$$= \frac{x^4 - 8x}{2x^2 + 5x - 3} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x^2 - 2x}$$

$$= \frac{x(x^3 - 8)}{2x^2 + 6x - x - 3} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x(x - 2)}$$

$$= \frac{x[(x)^3 - (2)^3]}{2x(x + 3) - 1(x + 3)} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x(x - 2)}$$

$$= \frac{x(x^2)(x^2 + 2x + 4)}{(2x - 1)(x + 3)} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x(x - 2)}$$

$$= \frac{x(x^2)(x^2 + 2x + 4)}{(2x - 1)(x + 3)} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x(x - 2)}$$

$$= 1 \text{ Ans}$$

Q.12
$$\frac{2y^2 + 7y - 4}{3y^2 - 13y + 4} \div \frac{4y^2 - 1}{6y^2 + y - 1}$$
Solution:
$$\frac{2y^2 + 7y - 4}{3y^2 - 13y + 4} \div \frac{4y^2 - 1}{6y^2 + y - 1}$$

$$= \frac{2y^2 + 7y - 4}{3y^2 - 13y + 4} \div \frac{4y^2 - 1}{6y^2 + y - 1}$$

$$= \frac{2y^2 + 8y - 1y - 4}{3y^2 - 12y - y + 4} \div \frac{(2y)^2 - (1)^2}{6y^2 + 3y - 2y - 1}$$

$$= \frac{2y(y + 4) - 1(y + 4)}{3y(y - 4) - 1(y - 4)} \div \frac{(2y - 1)(2y + 1)}{3y(2y + 1) - 1(2y + 1)}$$

$$= \frac{(y + 4)(2y - 1)}{(3y - 1)(y - 4)} \div \frac{(2y - 1)(2y + 1)}{(3y - 1)(2y + 1)}$$

$$= \frac{(y + 4)(2y - 1)}{(3y - 1)(y - 4)} \times \frac{(3y - 1)}{(2y - 1)}$$

$$= \frac{(y + 4)(2y - 1)}{(3y - 1)(y - 4)} \times \frac{(3y - 1)}{(2y - 1)}$$

$$= \frac{y + 4}{y - 4}$$

Q.13
$$\left[\frac{x^2 + y^2}{x^2 - y^2} - \frac{x^2 - y^2}{x^2 + y^2} \right] \div \left[\frac{x + y}{x - y} - \frac{x - y}{x + y} \right]$$
Solution:
$$\left[\frac{x^2 + y^2}{x^2 - y^2} - \frac{x^2 - y^2}{x^2 + y^2} \right] \div \left[\frac{x + y}{x - y} - \frac{x - y}{x + y} \right]$$

$$= \left[\frac{x^2 + y^2}{x^2 - y^2} - \frac{x^2 - y^2}{x^2 + y^2} \right] \div \left[\frac{x + y}{x - y} - \frac{x - y}{x + y} \right]$$

$$= \left[\frac{(x^2 + y^2)^2 - (x^2 - y^2)^2}{(x^2 - y^2)(x^2 + y^2)} \right] \div \left[\frac{(x + y)^2 - (x - y)^2}{(x - y)(x + y)} \right]$$

$$= \left[\frac{(x^4 + 2x^2y^2 + y^4) - (x^4 - 2x^2y^2 + y^4)}{(x^2 - y^2)(x^2 + y^2)} \right] \div \left[\frac{(x^2 + 2xy + y^2) - (x^2 - 2xy + y^2)}{x^2 - y^2} \right]$$

$$= \left[\frac{x^4 + 2x^2y^2 + y^4 - x^4 + 2x^2y^2 - y^4}{(x^2 - y^2)(x^2 + y^2)} \right] \div \left[\frac{x^4 + 2xy + y^2 - x^4 + 2xy - y^2}{x^2 - y^2} \right]$$

$$= \left[\frac{4x^2y^2}{(x^2 - y^2)(x^2 + y^2)} \right] \div \left[\frac{4xy}{x^2 - y^2} \right]$$

$$= \frac{4x^2y^2}{(x^2 - y^2)(x^2 + y^2)} \times \frac{x^2 - y^2}{4xy}$$

$$= \frac{4x^2y^2}{(x^2 - y^2)(x^2 + y^2)} \times \frac{x^2 - y^2}{4xy}$$

$$= \frac{4x^2y^2}{(x^2 - y^2)(x^2 + y^2)} \times \frac{x^2 - y^2}{4xy}$$

$$=\frac{xy}{x^2+y^2}$$
 Ans

Report any mistake?

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