

CHAPTER No : 1

"BASIC CONCEPTS"

EXERCISE PROBLEMS

1.1 Unit ϵ_1 Notation

Q1) $i_s = 3[2\sin 3t - 1] A$

Sketch ϵ_1 label current signal versus t , and mark its dc component I_s & its ac component i_s .

$$i_s = 3(2\sin 3t - 1) A$$

$$i_s = 6\sin 3t - 3 A$$

$$i_s = -3 + 6\sin 3t A$$

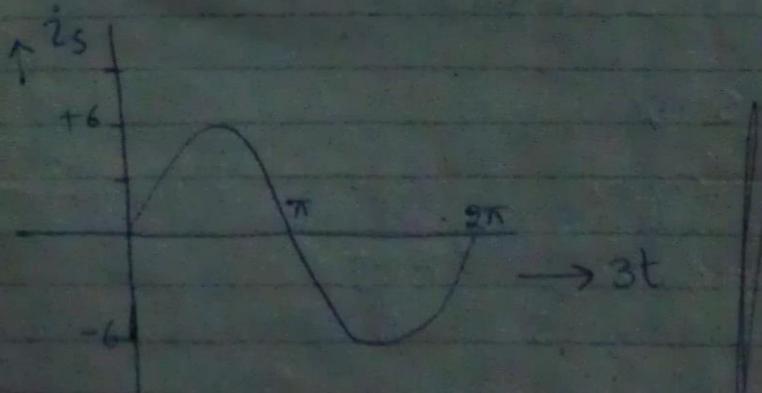
$$I_s \quad i_s$$

From here

$$I_s = -3 A \quad \text{dc component}$$

$$i_s = 6\sin 3t A \quad \text{a.c. component}$$

$$I_m = 6 A$$



Now,

After adding d.c.

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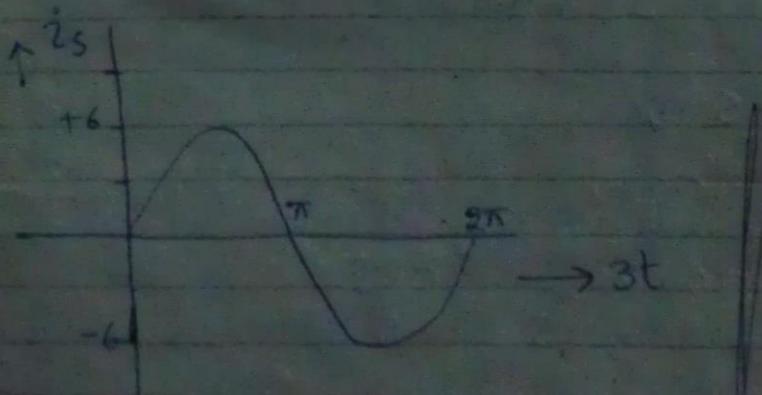
$$I_s \quad i_s$$

From here

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Now,

After adding d.c.

From H.

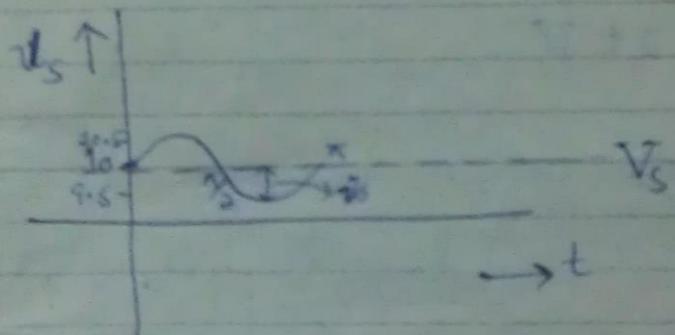
$$v_s = V_m \sin 2\pi f t$$

$$2\pi f = 2$$

$$f = \frac{2}{2\pi}$$

$$t = \frac{1}{\pi}$$

$$\Rightarrow T = \pi$$



b)

$$V_s = -3V$$

$$\begin{aligned} v_s &= V_s + v_s \\ &= -3 + 0.5 \sin 2t \end{aligned}$$

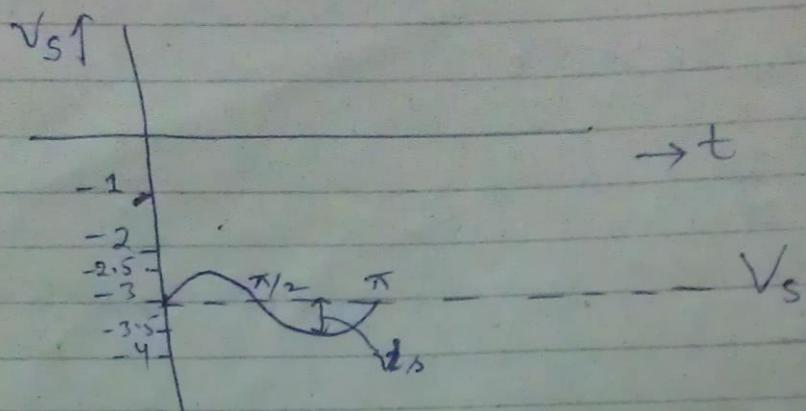
$$V_m = 0.5V$$

upper extreme is

$$V_s + V_m = -3 + 0.5 = -2.5$$

$$V_s - V_m = -3 - 0.5 = -3.5$$

$$T = \pi$$



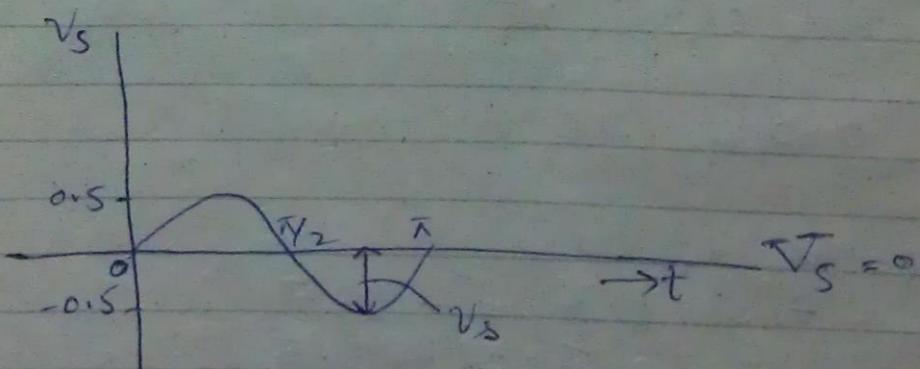
$$\text{c)} \quad V_s = 0 \\ V_s = 0.5 \sin 2t V$$

$$V_s = V_s + V_d \\ = 0 + 0.5 \sin 2t$$

$$V_m = 0.5$$

$$T = \pi$$

$$\text{upper extreme} = 0 + 0.5 = 0.5 \\ \text{lower extreme} = 0 - 0.5 = -0.5$$

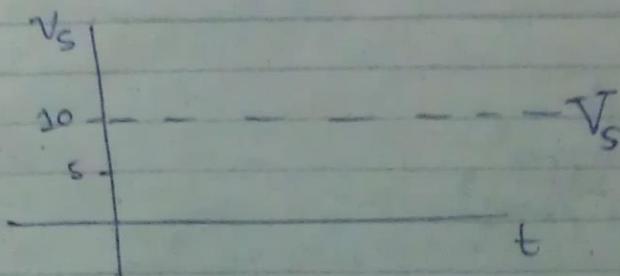


$$\underline{\underline{Q}} \quad V_s = 20V$$

$$v_s = 0$$

$$v_s = v_s + v_b$$

$$= 20 + 0$$



1.2) Electric Quantities:

Q3) Energy of electron = ?

$$\text{Energy} = VV$$

$$= (1.6 \times 10^{-19}) \times 12$$

$$\text{Energy} = 1.92 \times 10^{-18} \text{ J}$$

$$P = Vi$$

$$\frac{w}{t} = \frac{VQ}{t}$$

$$W = VQ$$

* Does energy of electron increase or decrease?

As electron is to have moved from +ve terminal of battery to -ve terminal. For it we have to do work. Electron absorbs this energy so, energy of electron increases.

* Does battery absorb or release energy?

As current in the battery flows from -ve to +ve terminal so, according to the sign conventions battery releases energy.

(Q4)

$$I = 1 \text{ A}$$

$$A = 1 \text{ mm}^2$$

$$N = 10^{23}/\text{cm}^3 \Rightarrow n = N/V$$

$$R = \frac{1 \times 10^{23}}{10^8} = 1 \times 10^{20}/\text{mm}^3$$

$$V_{av} = ?$$

$$V_{av} = \frac{I}{nAE}$$

$$= \frac{1}{1 \times 10^{20} \times 1 \times 10^{-6} \times 1.6 \times 10^{-19}}$$

$$= 62.5 \text{ mm/s}$$

$$V_{av} = 0.00625 \text{ mm/s}$$

(Q5)

$$V = 5t e^{-10^3 t}$$

a)

$$\dot{i} = ?$$

b) Find at which i is min & find t_{\min} .

$$i = \frac{dV}{dt}$$

$$i = 5t e^{-10^3 t}$$

$$\frac{di}{dt} = 5e^{-10^3 t} + 5t(-10^3) e^{-10^3 t}$$

$$i = 5e^{-10^3 t} \cdot (1 - 10^3 t)$$

For min. time we take derivative of i

$$\frac{d^2 i}{dt^2} = (-10^3) 5e^{-10^3 t} (1 - 10^3 t) + 5e^{-10^3 t} (-10^3)$$

$$\Rightarrow -5 \times 10^3 e^{-10^3 t} + 5 \times 10^6 t e^{-10^3 t} - 5e^{-10^3 t} \times 10^3 =$$

$$5 \times 10^3 e^{-10^3 t} (-1 + 10^3 t - 1) = 0$$

$$\frac{10^3 t}{t} = \frac{2}{10^3}$$

$$t = 2 \times 10^{-3} \text{ sec}$$

$$[t = 2 \text{ msec}]$$

$$i_{\min.} = 5e^{10^3 t} (1 - 10^3 t) \quad ; t = 2 \times 10^{-3}$$

$$= 5e^{-2} (1 - 2)$$

$$i_{\min.} = -5e^{-2} A = -0.676 A$$

Q6)

$$V = 12 V$$

$$I = 0.5 A$$

$$E = ?$$

$$V = ?$$

$$P = VI$$

$$P = 12 \times 0.5$$

$$P = 6W$$

$$\text{Energy} = P \times (t_2 - t_1)$$

$$W = 6 \times (3600 - 0)$$

$$= 21 \times 10^3 W$$

$$W = 21 \text{ KW}$$

$$Q = i \cdot (t_2 - t_1)$$

$$Q = 0.5 (3600 - 0)$$

$$Q = 1800 \text{ C}$$

Q7)

$$\text{Cost of energy} = 0.10/\text{KWh}$$

a) Cost of running 100-W TV for 8h/day for
a ~~year~~ = ?

$$E = P \times t$$

$$E = 100 \times (8 \times 7) \text{ h}$$

$$= 5600 \text{ Wh}$$

$$= 5.6 \text{ KWh}$$

$$\text{Cost for TV} = 0.1 \times 5.6$$

$$= 0.56$$

b) Cost of running 25W bulb continuously
for a year = ?

$$E = (25) \times (24 \times 365) \text{ h}$$

$$E = 219000 \text{ Wh}$$

$$E = 219 \text{ KWh}$$

$$\text{Cost of bulb} = 0.1 \times 219$$

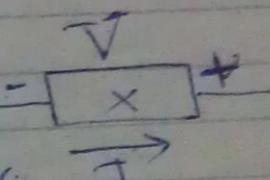
$$= 21.9$$

Q8) $I = 5e^{-20t} A$

$$V = 3I$$

$$V = 3 \times 5e^{-20t} = 15e^{-20t}$$

Find energy released or absorbed from $0 - 50\text{sec}$



Energy is releasing.

$$P = VI$$
$$= 15e^{-20t} \cdot 5e^{-20t}$$

$$P = 75e^{-20t} W$$

$$\begin{aligned}\text{Energy} &= \int_0^{50 \times 10^{-3}} 75e^{-20t} \cdot dt \\ &= \left[\frac{75e^{-20t}}{-20} \right]_0^{50 \times 10^{-3}} \\ &= -\frac{75}{20} [e^{-1} - 1] \\ &= \frac{75}{20} (1 - e^{-1}) \\ &= \frac{75}{20} \times 0.63\end{aligned}$$

Energy = 2.36 WSec or J

Q9) $V = 10e^{-5t}$

$$I = 3V$$

$$= 3 \times 10e^{-5t}$$

$$= 30e^{-5t}$$

$$W = ?$$

$$t = 0.1s \rightarrow 0.5s$$

$$P = VI$$

$$= 10e^{-5t} \times 30e^{-5t}$$

$$P = 300e^{-10t} \text{ W}$$

$$W = \int_{0.2}^{0.5} 300e^{-10t} dt$$

$$= 300 \left[\frac{e^{-10t}}{-10} \right]_{0.2}^{0.5}$$

$$= -\frac{300}{10} \left[e^{-10(0.5)} - e^{-10(0.2)} \right]$$

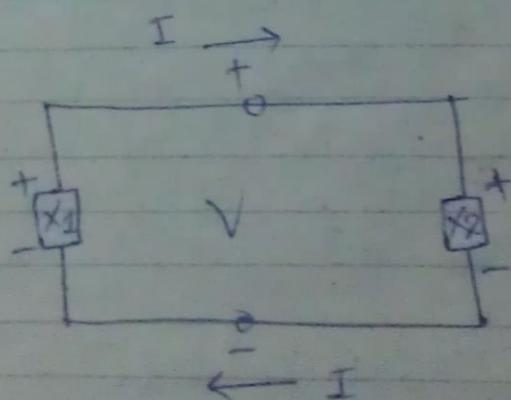
$$= -30 (e^{-5} - e^{-1})$$

$$= -30 \times (-0.36)$$

$$W = 10.8 \text{ J}$$

Energy is absorbing

Q10)



$$V = 10 \text{ V}$$

$$I = 2 \text{ A}$$

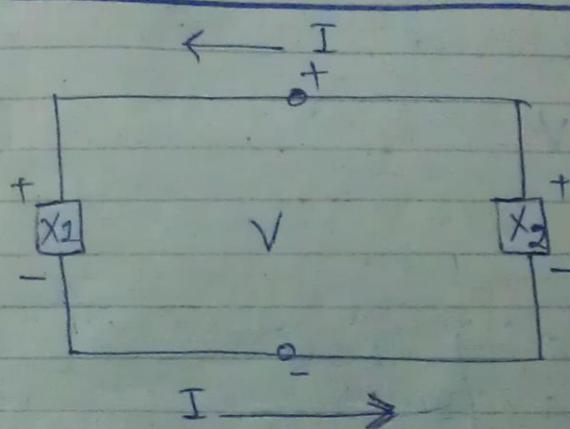
$$P = ?$$

X_1 is releasing power.
 X_2 is absorbing power.

$$\begin{aligned}
 P &= VI \\
 P &= 10 \times 2 \\
 P &= 20 \text{ W}
 \end{aligned}
 \quad \left| \begin{array}{l} X_1 \xrightarrow{\text{enter}} \text{from top} = \\ X_2 \xrightarrow{\text{enter}} \text{from bottom} \end{array} \right.$$

\therefore power released = \therefore power absorbed.

Q. 11)



Q. 12)

$$\begin{aligned}
 V &= 5 \text{ V} \\
 I &= -2 \text{ A}
 \end{aligned}$$

X_2 is releasing power
 X_1 is absorbing power.

$$\begin{aligned}
 P &= 5 \times (-2) \\
 P &= -10 \text{ W}
 \end{aligned}$$

Q. 13)

$$\begin{aligned}
 V &= 5 \text{ V} \\
 i &= 4 \text{ V}
 \end{aligned}$$

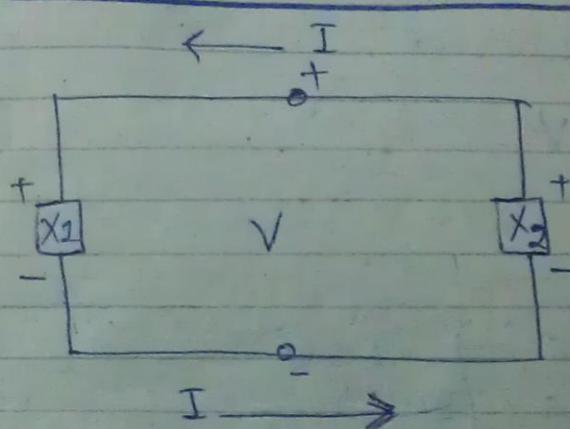
$$P = 20 \text{ W}$$

X_1 is releasing & X_2 is absorbing power.

$$\begin{aligned}
 P &= VI \\
 P &= 10 \times 2 \\
 P &= 20 \text{ W}
 \end{aligned}
 \quad \left| \begin{array}{l} X_1 \xrightarrow{\text{enter}} \text{from top} = \\ X_2 \xrightarrow{\text{enter}} \text{from bottom} \end{array} \right.$$

\therefore power released = \therefore power absorbed.

Q. 11)



Q. 12)

$$\begin{aligned}
 V &= 5 \text{ V} \\
 I &= -2 \text{ A}
 \end{aligned}$$

X_2 is releasing power
 X_1 is absorbing power.

$$\begin{aligned}
 P &= 5 \times (-2) \\
 P &= -10 \text{ W}
 \end{aligned}$$

Q. 13)

$$\begin{aligned}
 V &= 5 \text{ V} \\
 I &= 4 \text{ A}
 \end{aligned}$$

$$P = 20 \text{ W}$$

X_1 is releasing & X_2 is absorbing power.

$$\text{Q) } \begin{aligned} V &= -24 \text{ V} \\ i &= 5 \text{ A} \end{aligned}$$

$$P = -120 \text{ W}$$

x_2 is releasing ϵ , x_1 is absorbing power.

$$\text{d) } \begin{aligned} V &= -22 \text{ V} \\ i &= -2 \text{ A} \end{aligned}$$

$$P = 24 \text{ W}$$

x_1 is releasing power ϵ , x_2 is absorbing power.

$$\text{e) } \begin{aligned} V &= 0 \text{ V} \\ i &= 20 \text{ A} \\ P &= 0 \text{ W} \end{aligned}$$

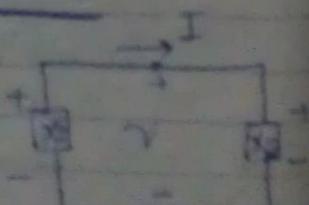
No power.

$$\text{f) } \begin{aligned} V &= 220 \text{ V} \\ i &= 0 \text{ A} \\ P &= 0 \text{ W} \end{aligned}$$

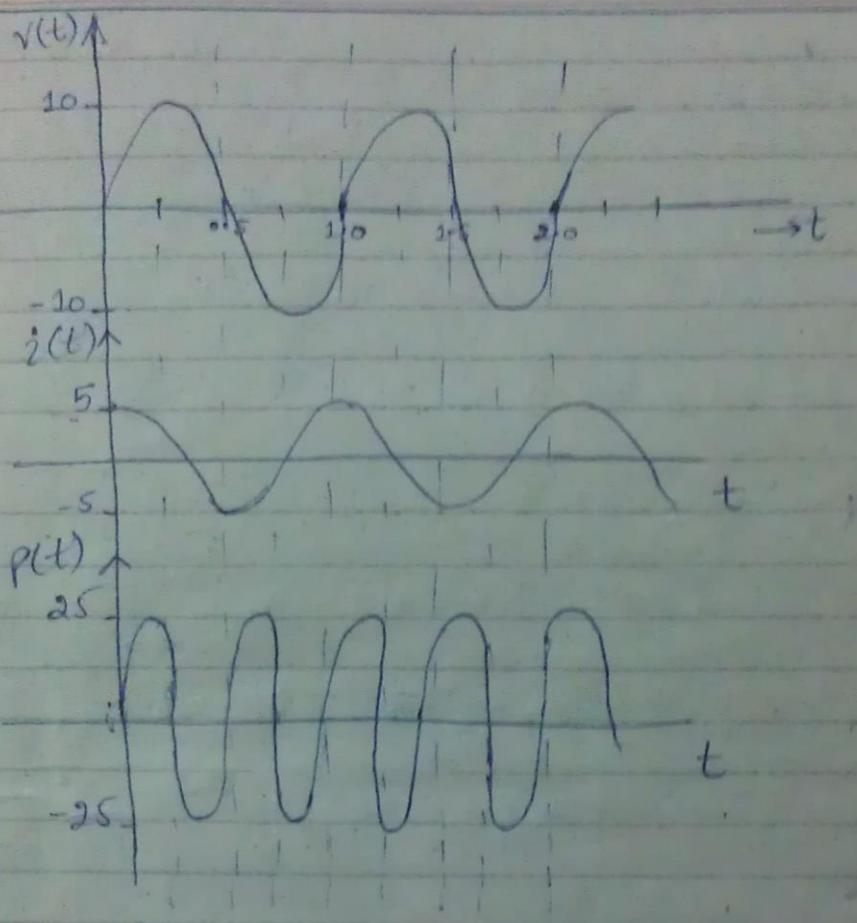
No power.

Q12)

$$\begin{aligned} V &= 10 \sin 2\pi 10^3 t \text{ V} \\ i &= 5 \cos 2\pi 10^3 t \text{ A} \end{aligned}$$



Plot V , i , ϵ , P versus t .



$$P = VI$$

$$P = 10 \sin 2\pi 10^3 t \cdot 5 \cos 2\pi 10^3 t$$

$$P = 50 \sin 2\pi 10^3 t \cdot \cos 2\pi 10^3 t = 25 \sin(2\pi 10^3 t)$$

$$P = 25 \sin 2\pi 2 \times 10^3 t \text{ Watt}$$

Power

From $0 \text{ ms} \rightarrow 0.25 \text{ ms}$

X_1 released $\rightarrow X_2$ absorbed

$0.25 \text{ ms} \rightarrow 0.5 \text{ ms}$

$X_2 \rightarrow X_1$

$0.5 \text{ ms} \rightarrow 0.75 \text{ ms}$

$X_1 \rightarrow X_2$

$0.75 \text{ ms} \rightarrow 1 \text{ ms}$

$X_2 \rightarrow X_1$

Q13)

$$v = 10 \sin 2\pi 10^3 t \text{ V}$$
$$i = 5 \sin (2\pi 10^3 t - \pi/4) \text{ A}$$

$$P = vi$$

$$= 10 \sin 2\pi 10^3 t \cdot 5 \sin (2\pi 10^3 t - \pi/4)$$

$$= 50 \sin(2\pi 10^3 t) \cdot \sin(2\pi 10^3 t - \pi/4)$$

$$= -25 \left[-2 \sin 2\pi 10^3 t \cdot \sin (2\pi 10^3 t - \pi/4) \right]$$

$$= -25 \left[-2 \sin \omega t \cdot \sin (\omega t - \pi/4) \right]_{\omega = 2\pi 10^3}$$

$$= -25 \left[\cos(\omega t + \omega t - \pi/4) - \cos(\omega t - \omega t + \pi/4) \right]$$

$$= -25 \left[\cos(2\omega t - \pi/4) - \cos(\pi/4) \right]$$

$$= -25 \cos(2\omega t - \pi/4) + 25 \cos \pi/4$$

$$P = 17.67 - 25 \cos(2 \cdot 2\pi 10^3 t - \pi/4)$$

$$\therefore P_s = 17.67 \text{ (offset)} \quad P_m = -25$$

$$P_s + P_m = 17.67 - 25 = -7.33$$

$$P_s - P_m = 17.67 + 25 = 42.67$$

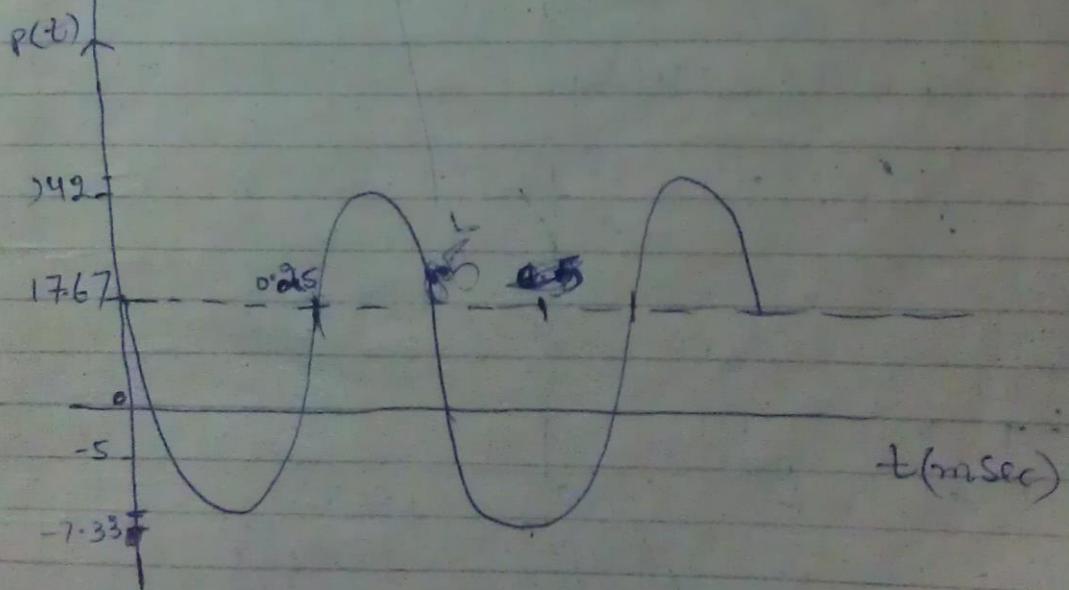
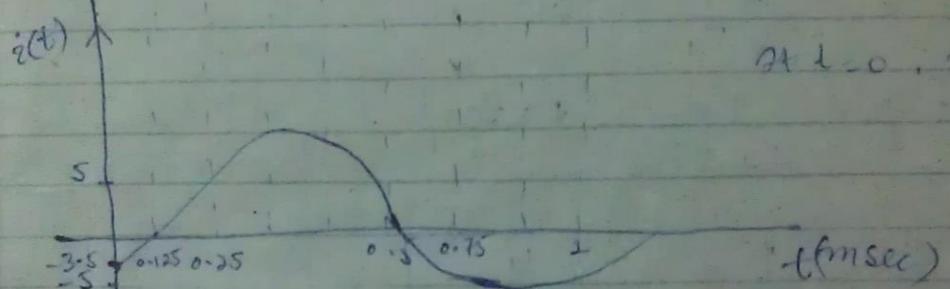
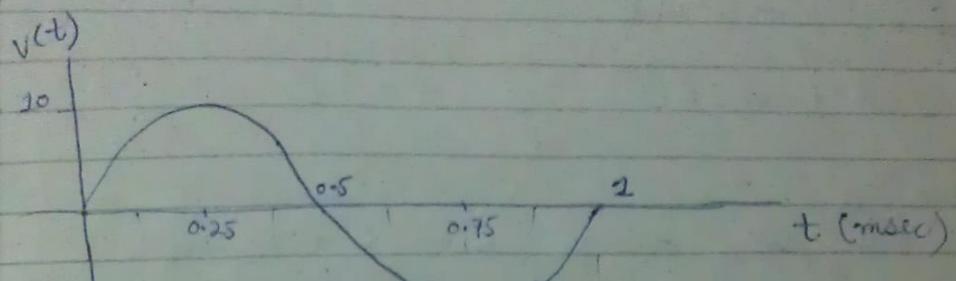
For v

$$V_m = 10 \text{ V} \quad f = 10^3 \text{ Hz}$$

$$\Rightarrow t = 1 \text{ ms}$$

For 2

$$i_m = 5 \text{ A} \quad t = 1 \text{ msec}$$



$$i = 0 \rightarrow 1 \text{ mA}$$

$$d = 25\%$$

$$f = 1 \text{ kHz}$$

$$f = 1 \times 10^3 \text{ Hz}$$

$$\Rightarrow t = 1 \text{ msec}$$

Net charge = ?

transferred b/w $t=0 \rightarrow t=5 \text{ msec}$

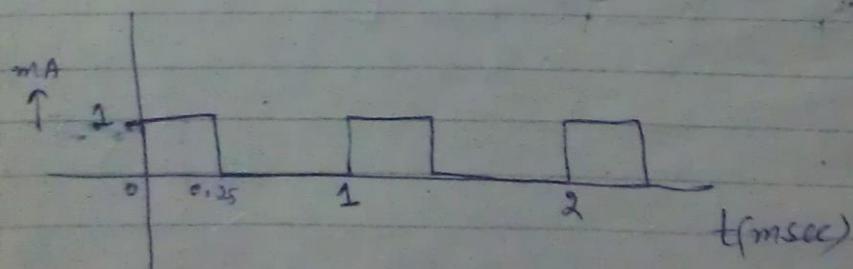
$$\text{Sol} \quad d = \frac{T_H}{T_L + T_H} \times 100\%$$

$$25\% = \frac{T_H}{T_H + T_L} \times 100\%$$

$$1 = \frac{T_H}{T_H + T_L} \times 4$$

$$T_H + T_L = 4T_H$$

$$\boxed{T_L = 3T_H}$$



From $0 \rightarrow 0.25 \text{ ms}$

$$V_1 = \int_0^{0.25 \times 10^{-3}} 1 \times 10^{-3} dt$$

$$= 0.25 \times 10^6 C$$

$$V_1 = 0.25 \mu C$$

From $0.25 \rightarrow 1 \text{ msec}$

$$V_2 = \int_{0.25 \times 10^{-3}}^{1 \times 10^{-3}} 0 dt$$

$$V_2 = 0 \mu C$$

$$V_o = V_1 + V_2$$

$$V_o = 0.25 \mu C$$

From $t=0 \rightarrow t=5 \text{ msec}$

$$V = (0.25 \mu C) \times 5 \times 10^{-3}$$

$$V = 1.25 \mu C$$

Q.25)

$$f = 1 \text{ kHz}$$

$$\text{upper extreme} = -5 \text{ mA}$$

$$\text{lower extreme} = 0 \text{ mA}$$

$$\Rightarrow X_s \neq X_m = 1.25 \text{ kHz}$$

$$V_s - X_m = 0 \text{ mA}$$

$$\Rightarrow \begin{aligned} I_s + I_m &= -5 \text{ mA} & \textcircled{1} \\ I_s - I_m &= 0 \text{ mA} & \textcircled{2} \end{aligned}$$

Adding $\textcircled{1}$ & $\textcircled{2}$

$$\begin{aligned} 2I_s &= -5 \\ I_s &= -2.5 \text{ mA} \end{aligned}$$

put in $\textcircled{1}$

$$I_m = 2.5 \text{ mA}$$

Now,

$$\begin{aligned} i_s &= I_s + i_m \\ &= I_s + I_m \sin 2\pi f t \end{aligned}$$

$$i_s = -2.5 \times 10^{-3} + 2.5 \times 10^{-3} \sin 2\pi 10^3 t \text{ (mA)}$$

b) $T = 1 \text{ ms} \Rightarrow f = 10^6 \text{ Hz}$

$$V_s + V_m = -10 \text{ V} \quad \textcircled{1}$$

$$V_s - V_m = -15 \text{ V} \quad \textcircled{2}$$

$\textcircled{1} + \textcircled{2}$

$$2V_s = -25$$

$$V_s = -12.5 \text{ V}$$

-12.5

$\textcircled{1} \Rightarrow V_m = 2.5 \text{ V}$

$$\begin{aligned} V_s &= V_s + V_m \sin 2\pi f t \\ &= -12.5 + 2.5 \sin 2\pi 10^6 t \end{aligned}$$

Q16)

$$V = 100 e^{-10^3 t} \text{ V}$$

t₁ = 0 and t₂ = 1 msec

$$V_{av} = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} V dt$$

$$V_{av} = \frac{1}{1 \times 10^{-3}} \int_0^{1 \times 10^{-3}} 100 e^{-10^3 t} dt$$

$$V_{av} = \frac{1}{1 \times 10^{-3}} \times \frac{100}{(-10^3)} \left[e^{-10^3 t} \right]_0^{1 \times 10^{-3}}$$

$$= -100 (e^{-1} - e^0)$$

$$V_{av} = 63.2 \text{ V}$$

b)

t₁ = 0 and t₂ = 2 msec

$$V_{av} = \frac{1}{2 \times 10^{-3}} \int_0^{2 \times 10^{-3}} 100 e^{-10^3 t} dt$$

$$= \frac{1}{2 \times 10^{-3}} \times \frac{100}{(-10^3)} \left[e^{-10^3 t} \right]_0^{2 \times 10^{-3}}$$

$$= -50 (e^{-2} - e^0)$$

$$= -50 (0.13 - 1)$$

$$V_{av} = 42.5 \text{ V}$$

$$\text{Q23) } V = 10 e^{10^3 t} \text{ V} \quad (1)$$

$$V_1 = 9 \text{ V} \quad V_2 = 1 \text{ V}$$

put $V_1 = 9 \text{ V}$ in (1)

$$9 = 10 e^{-10^3 t_1}$$

$$\ln \frac{9}{10} = -10^3 t_1$$

$$\ln \frac{9}{10} = -10^3 t_1$$

$$t_1 = -\frac{1}{10^3} \ln \frac{9}{10}$$

$$t_1 = 1.05 \times 10^{-3}$$

$$\Rightarrow t_1 = 0.1 \times 10^{-3} \text{ sec}$$

put $V_2 = 1 \text{ V}$ in (1)

$$1 = 10 e^{10^3 t_2}$$

$$\ln \frac{1}{10} = -10^3 t_2$$

$$t_2 = -\frac{1}{10^3} \ln \frac{1}{10}$$

$$\Rightarrow t_2 = 2.3 \times 10^{-3} \text{ sec}$$

$$V_{av} = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} 10 e^{10^3 t} dt$$

$$V_{av} = \frac{1}{2.3 \times 10^{-3} - 0.1 \times 10^{-3}} \times \frac{10}{10^3} \left[e^{10^3 t} \right]_{0.1 \times 10^{-3}}^{2.3 \times 10^{-3}}$$

$$V_{av} = \frac{1}{2 \cdot 2 \times 10^{-3}} \times \frac{20}{(-10^3)} \left[e^{-2 \cdot 3} - e^{0+1} \right]$$

$$= \frac{-10}{2 \cdot 2 \times 10^{-6}} \left[0.10 - 0.90 \right]$$

$$= -4.54 \times 10^6 (-0.8)$$

$$\underline{V_{av} = 3.63 \text{ V}}$$

Q18) $i = 20 (1 - e^{-500t}) \text{ mA}$

$t_1 = 1 \text{ msec}$ $t_2 = 3 \text{ msec}$
 $\dot{i}_{av} = ?$

$$\dot{i}_{av} = \frac{1}{3 \times 10^{-3} - 1 \times 10^{-3}} \int_{1 \times 10^{-3}}^{3 \times 10^{-3}} 20 (1 - e^{-500t}) dt$$

$$\dot{i}_{av} = \frac{1}{2 \times 10^{-3}} (20) \left[t - \frac{e^{-500t}}{-500} \right]_{1 \times 10^{-3}}^{3 \times 10^{-3}}$$

$$= \frac{20}{2 \times 10^{-3}} \left[(2 \times 10^{-3}) + \frac{1}{500} (e^{-1.5} - e^{-0.5}) \right]$$

$$= \frac{20}{2 \times 10^{-3}} \left[2 \times 10^{-3} + 4 \cdot 4 \times 10^{-9} - 1 \cdot 2 \times 10^{-3} \right]$$

$$= \frac{0.0248}{2 \times 10^{-3}}$$

$$\underline{\dot{i}_{av} = 12.4 \text{ mA}}$$

$$Q19) i = 100 (1 - e^{-500t}) \text{ mA} \quad \textcircled{1}$$

$$i_1 = 0 \text{ mA} \quad \text{&} \quad i_2 = 50 \text{ mA}$$

put $i_1 = 0 \text{ mA}$ in $\textcircled{1}$

$$0 = 100 (1 - e^{-500t_2}).$$

$$0 = 100 (1 - e^{-500t_2})$$

$$0 = 1 - e^{-500t_2}$$

$$1 = e^{500t_2}$$

$$\ln 1 = -500t_2$$

$$0 = -500t_2$$

$$t_2 = 0 \text{ msec}$$

Put $i_2 = 50 \text{ mA}$ in $\textcircled{1}$

$$50 = 100 (1 - e^{-500t_2})$$

$$\frac{1}{2} = 1 - e^{-500t_2}$$

$$e^{-500t_2} = \frac{1}{2}$$

$$-500t_2 = \ln \frac{1}{2}$$

$$t_2 = 1.3 \times 10^{-3}$$

$$\begin{aligned}
 \dot{i}_{av} &= \frac{1}{1.3 \times 10^{-3}} \int_0^{1.3 \times 10^{-3}} 100 (1 - e^{-500t}) dt \\
 &= \frac{100}{1.3 \times 10^{-3}} \left[t + \frac{e^{-500t}}{-500} \right]_0^{1.3 \times 10^{-3}} \\
 &= \frac{100}{1.3 \times 10^{-3}} \left[(1.3 \times 10^{-3}) + \frac{1}{500} (e^{-0.65} - e^0) \right] \\
 \dot{i}_{av} &= \frac{100}{1.3 \times 10^{-3}} (1.3 \times 10^{-3} + 1.04 \times 10^{-3} - 2 \times 10^{-3})
 \end{aligned}$$

$$\dot{i}_{av} = 26.15 \text{ mA}$$

Q20) Signal alternates b/w -1V & +2V
full cycle average = ?

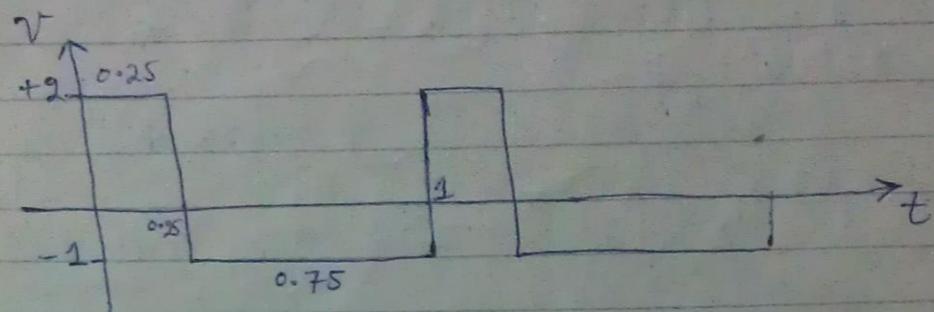
a) d = 25%.

$$d = \frac{T_H}{T_H + T_L} \times 100\%$$

$$25\% = \frac{T_H}{T_H + T_L} \times 100\%$$

$$T_H + T_L = 4T_H$$

$$T_L = 3T_H$$



$$V_{av} = \frac{1}{T} \left[\int_0^{0.25} 2 dt + \int_{0.25}^1 -1 dt \right]$$

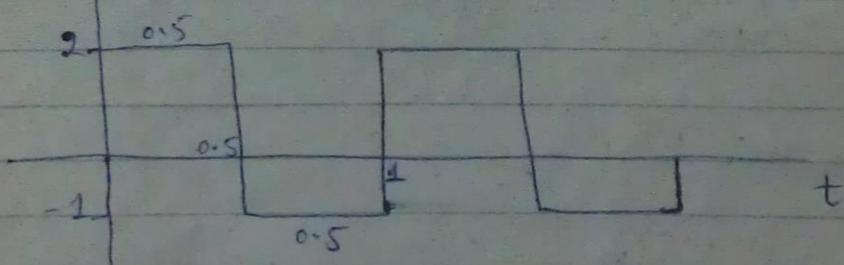
$$= 2 \times (0.5) + (-1)(0.75)$$

$V_{av} = -0.25V$

$$d = 50\%$$

$$50\% = \frac{T_H}{T_L + T_H} \times 100\%$$

$$\frac{T_H + T_L}{T_L} = \frac{2T_H}{T_H}$$



$$V_{av} = \frac{1}{T} \left[\int_0^{0.5} 2 dt + \int_{0.5}^1 -1 dt \right]$$

$$V_{avg} = 2 \times 0.5 + (-2)(0.5)$$

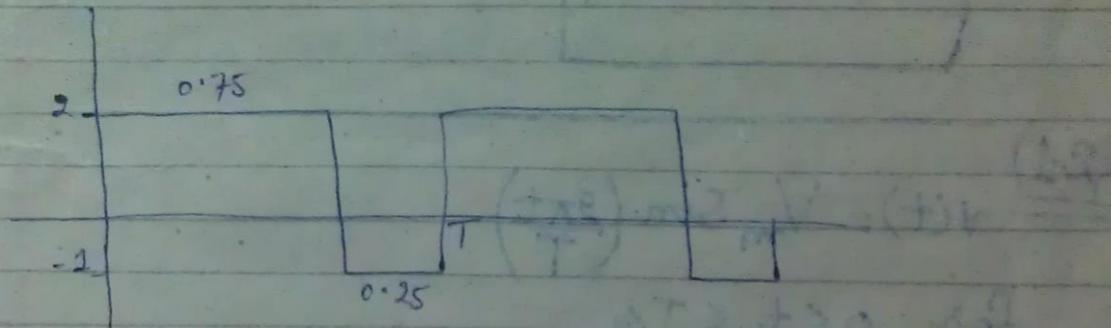
$$\boxed{V_{avg} = 0.5 V}$$

$$d = 75\%$$

$$75 = \frac{T_H}{T_L + T_H} \times 100$$

$$3T_H + 3T_L = 4T_H$$

$$T_H = 3T_L$$



$$V_{avg} = \frac{1}{4} \left[\int_0^{0.75} 2 dt + \int_{0.75}^1 -1 dt \right]$$

$$= 2 \times 0.75 + (-1) \times 0.25$$

$$\boxed{V_{avg} = 1.25 V}$$

② $V_{avg} = 0$, $d = ?$

$$0 = \frac{1}{T} \left[\int_0^T 2dt + \int_d^1 -1 dt \right]$$

$$0 = 2(d) + (-1)(1-d)$$

$$0 = 2d - 1 + d$$

$$0 = 3d - 1 \quad \therefore 2.5 \Rightarrow d$$

$$d = \frac{1}{3}$$

$$d = 0.33$$

$$d = 0.33 \times 100\%$$

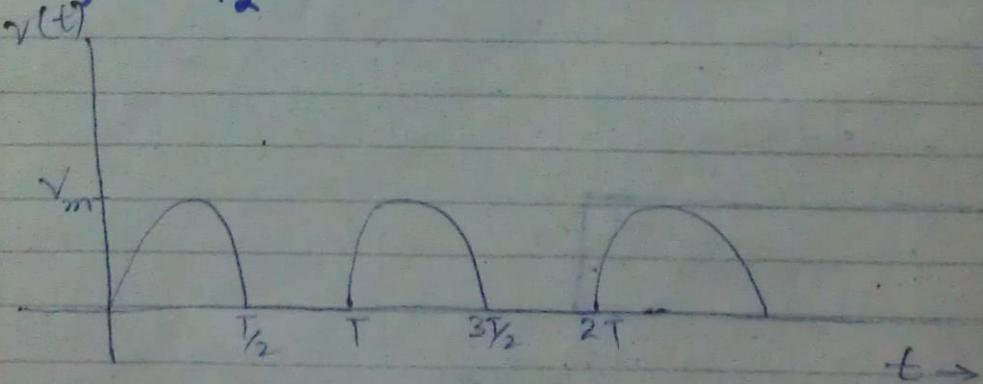
$$d = 33.3\%$$

Q21) $v(t) = V_m \sin\left(\frac{2\pi t}{T}\right)$

for $0 \leq t \leq T/2$

$$v(t) = 0$$

for $T/2 \leq t \leq T$



$$V_{av} = \frac{1}{T-0} \left[\int_0^{T/2} V_m \sin \frac{2\pi t}{T} dt + \int_{T/2}^T 0 dt \right]$$

$$\begin{aligned}
 V_{av} &= \frac{1}{T} V_m \left[-\cos \frac{2\pi f t}{T} \right]_0^{\frac{T}{2}} \\
 &= -\frac{1}{T} (V_m) \left(\frac{T}{2\pi} \right) \left[\cos \frac{2\pi}{T} \cdot \frac{T}{2} - \cos 0 \right] \\
 &= -\frac{V_m}{2\pi} (-1 - 1) \\
 &= -\frac{V_m}{2\pi} (-2)
 \end{aligned}$$

$V_{av} = \frac{V_m}{\pi}$

Q.22)

$$v(t) = 170 |\sin 120\pi t|$$
 $T = ?$
 $V_{av} = ?$

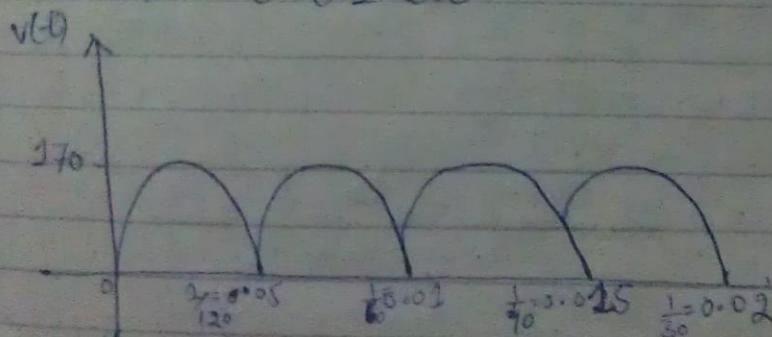
$V_m = 170$

$v(t) = 170 \sin 2\pi 60t$

$\Rightarrow f = 60 \text{ Hz}$

$T = \frac{1}{60}$

$T = 0.01 \text{ Sec}$



From graph
 $T = \frac{1}{120} \text{ sec}$

$$\begin{aligned}
 V_{av} &= \frac{1}{T} \int_0^{1/120} 170 (\sin 120\pi t) dt \\
 &= 120 \times 170 \left[-\frac{\cos 120\pi t}{120\pi} \right]_0^{1/120} \\
 &= -\frac{120 \times 170}{120 \times \pi} (\cos \pi - \cos 0) \\
 &= -\frac{170}{\pi} (-1 - 1)
 \end{aligned}$$

$$V_{av} = 108.28 \text{ V}$$

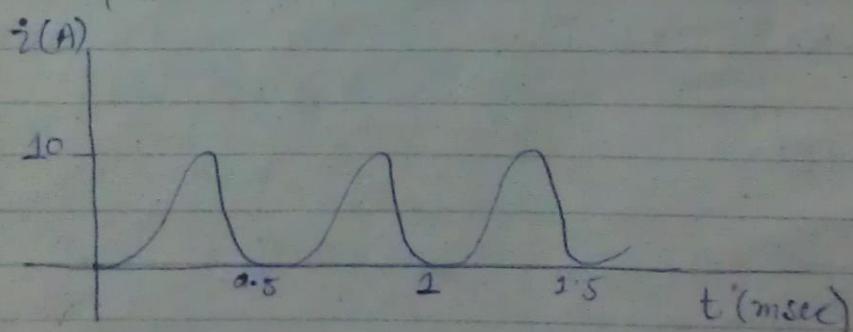
Q23)

$$i(t) = 10 \sin^2 2\pi 10^3 t \text{ A}$$

$$f = 10^3 \text{ Hz} \quad i_m = 10$$

$$T = 1 \times 10^{-3} \text{ sec}$$

$$T = 1 \text{ msec}$$



From graph
 $T = 0.5 \text{ msec}$

$$i_{av} = \frac{1}{0.5 \times 10^{-3} - 0} \int_0^{0.5 \times 10^{-3}} 10 \sin^2 2\pi 10^3 t dt$$

$$\begin{aligned}
 i_{av} &= \frac{10}{0.5 \times 10^{-3}} \int_0^{0.5 \times 10^{-3}} 1 - \cos \frac{4\pi \times 10^3 t}{2} dt \\
 &= \frac{10}{1 \times 10^{-3}} \int_0^{0.5 \times 10^{-3}} 1 - \cos 4\pi \times 10^3 t dt \\
 &= 1 \times 10^4 \left[t - \frac{\sin 4\pi \times 10^3 t}{4\pi \times 10^3} \right]_0^{0.5 \times 10^{-3}} \\
 &= 1 \times 10^4 \left[(0.5 \times 10^{-3}) - \left(\frac{\sin 2\pi}{4\pi \times 10^3} - \frac{\sin 0}{4\pi \times 10^3} \right) \right] \\
 &= 1 \times 10^4 (0.5 \times 10^{-3} - 0 + 0)
 \end{aligned}$$

$$i_{av} = 5 A$$

Q24)

$$v(t) = 4e^{-t} V$$

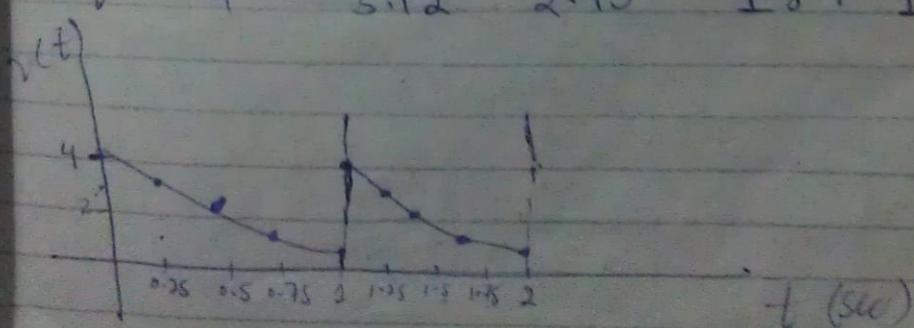
for $0 < t < 1 S$

$$v_{av} = ?$$

$$v(t \pm nT) = v(t)$$

$$T = 1 \text{ sec}$$

t	0	0.25	0.5	0.75	1
v	4	3.12	2.43	2.89	1.47



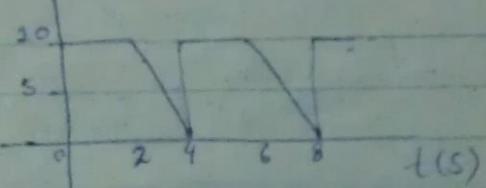
$$V_{AV} = \frac{1}{1-0} \int_0^1 4e^t dt$$

$$= 4 \left[\frac{e^{-t}}{-1} \right]_0^1$$

$$= -4 (e^1 - e^0)$$

$$V_{AV} = 2.52 V$$

Q25) $v(V)$



$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{10 - 5}{4 - 2} = 5$$

$$y = mt + c$$

$$y = -5t + 20$$

$$T = 4 \text{ sec}$$

$$V_{AV} = \frac{1}{4} \left[\int_0^2 10 dt + \int_2^4 20 - 5t dt \right]$$

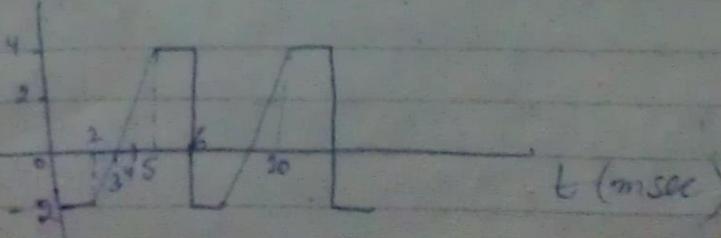
$$= \frac{1}{4} \left[10t \Big|_0^2 + \left[20t - \frac{5t^2}{2} \right] \Big|_2^4 \right] = 0$$

$$= \frac{1}{4} \left\{ 20 + 40 - [40 - 10] \right\}$$

$$= \frac{1}{4} (30)$$

$$V_{AV} = 7.5 V$$

Q26) $v(V)$



$$m = \frac{y_2 - y_1}{t_2 - t_1} = \frac{4 - (-2)}{5 - 2} = \frac{6}{3} = 2$$

$$y = mt + c$$

$$y = 2t - 6$$

to interval

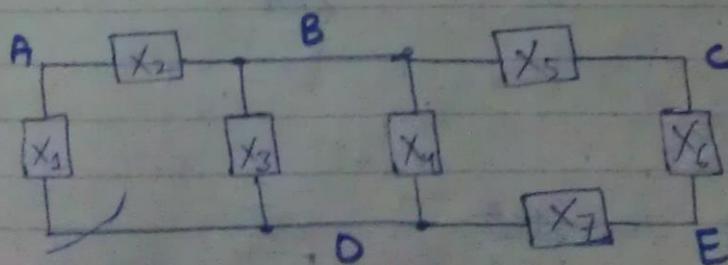
$V_{av} = ?$

$$T = 6 \text{ msec}$$

$$\begin{aligned} V_{av} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{1}{6 \times 10^{-3}} \left[\int_0^{2 \times 10^{-3}} -2 dt + \int_{2 \times 10^{-3}}^{5 \times 10^{-3}} (2 \times 10^3 t - 6) dt + \int_{5 \times 10^{-3}}^{6 \times 10^{-3}} 4 dt \right] \\ &= \frac{1}{6 \times 10^{-3}} \cdot \left[-2t \Big|_0^{2 \times 10^{-3}} + \left[\frac{3 \times 10^3 t^2}{2} - 6t \right] \Big|_{2 \times 10^{-3}}^{5 \times 10^{-3}} + \left[4t \right] \Big|_{5 \times 10^{-3}}^{6 \times 10^{-3}} \right] \\ &= \frac{1}{6 \times 10^{-3}} \left[-2 \times 2 \times 10^{-3} + \left\{ 10^3 (25 \times 10^{-3}) - 6 \times 5 \times 10^{-3} - 10^3 (4 \times 6 \times 10^{-3}) + (4 \times 6 \times 10^{-3} - 4 \times 5 \times 10^{-3}) \right\} \right] \\ &= \frac{1}{6 \times 10^{-3}} \left[-4 \times 10^{-3} + 25 \times 10^{-3} - 30 \times 10^{-3} - 4 \times 10^{-3} + 12 \times 10^{-3} + 24 \times 10^{-3} - 20 \times 10^{-3} \right] \\ &= \frac{3 \times 10^{-3}}{6 \times 10^{-3}} \end{aligned}$$

$$V_{av} = 0.5 \text{ V}$$

Q27)



A, B, C, D, E are Nodes.

Simple nodes: A, C, E

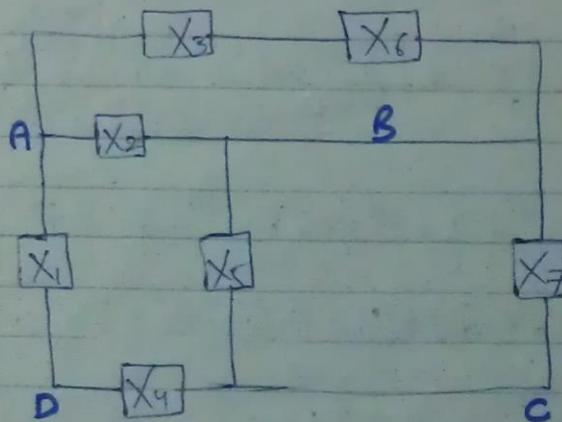
Meshes: $X_1X_2X_3$, X_3X_4 , $X_4X_5X_6X_7$

Loops: $X_1X_2X_4$, $X_3X_5X_6X_7$, $X_1X_2X_5X_6X_7$

In Series: X_1X_2 , $X_5X_6X_7$

In parallel: X_3X_4

Q28)



Nodes: A, B, C, D

Simple Nodes: D

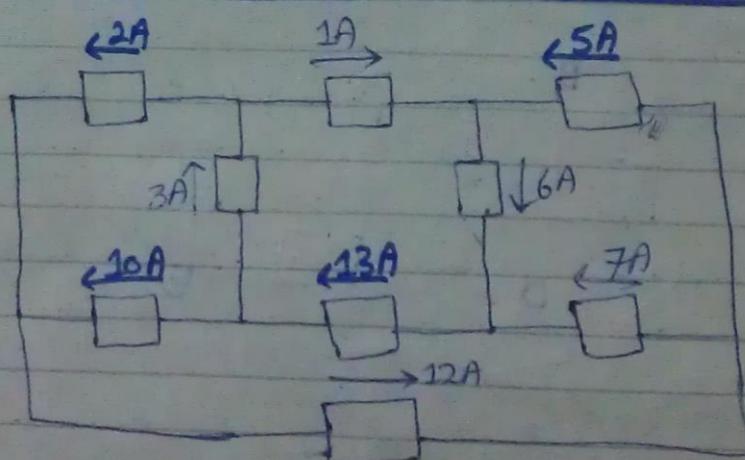
Meshes: $X_1X_2X_4X_5$, X_5X_7 , $X_9X_3X_6$

Loops: $X_1X_4X_3X_6X_7$, $X_1X_2X_4X_7$

In Series: X_3X_6 , $X_2X_5X_4$

In parallel: X_5X_7

Q29)



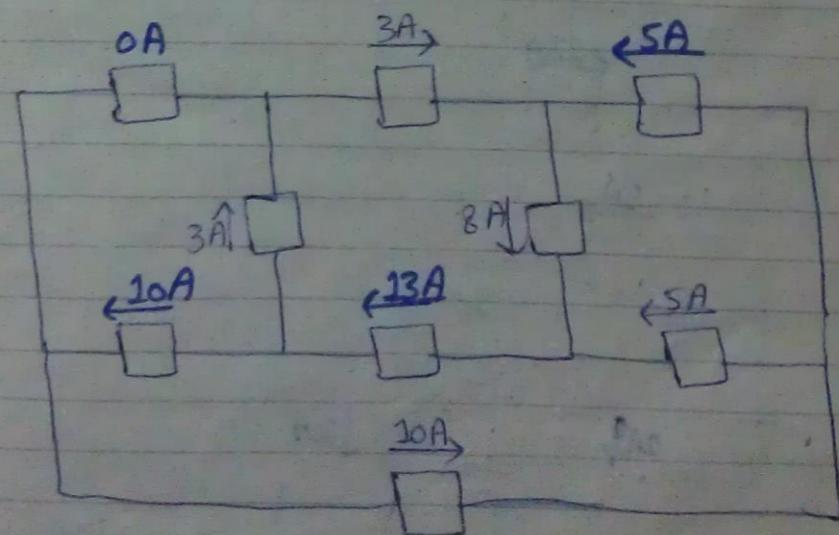
Q30) a)



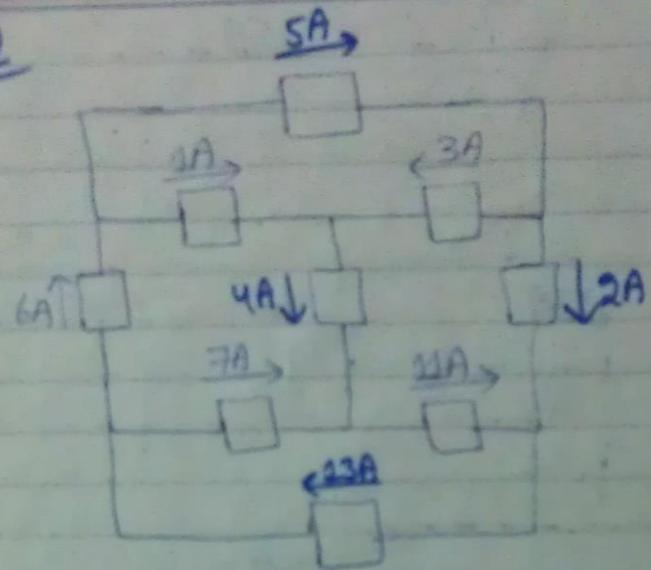
b)



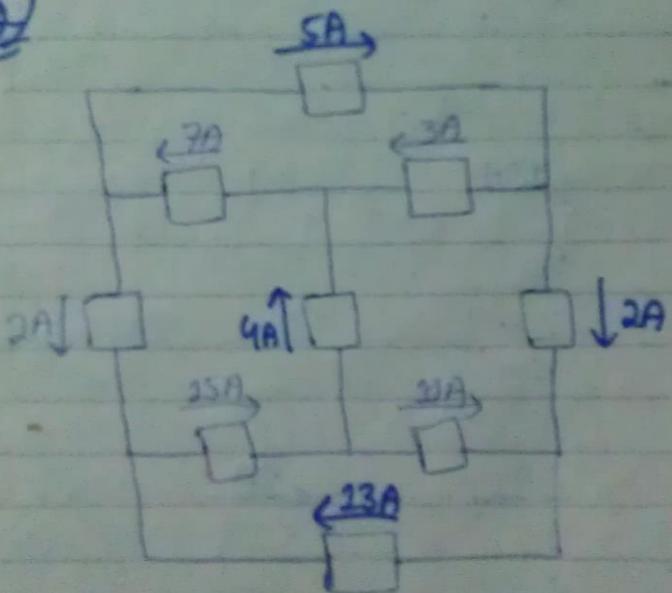
c)



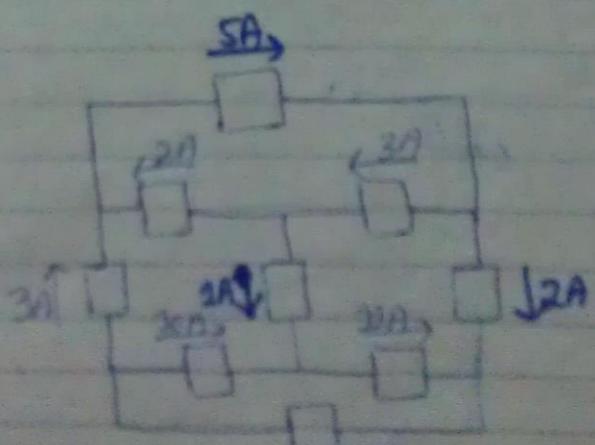
Q32)



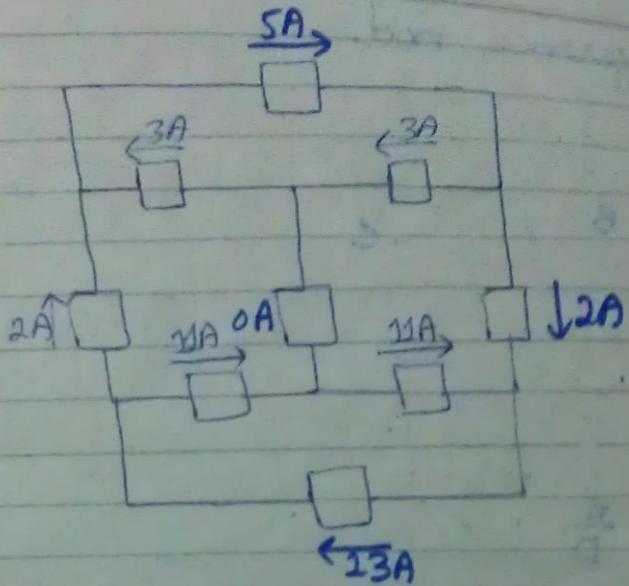
Q38)
a)



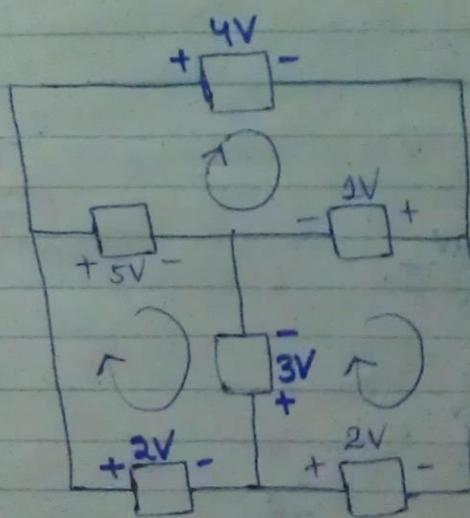
b)



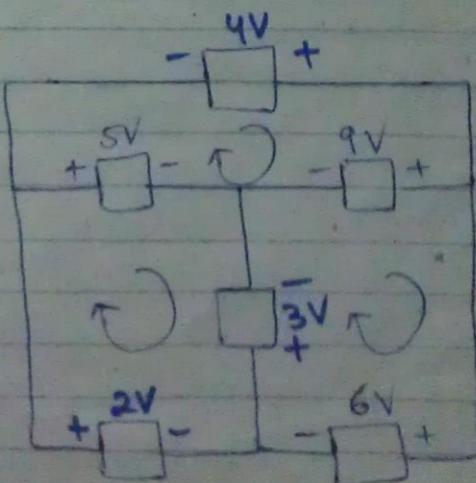
Q2



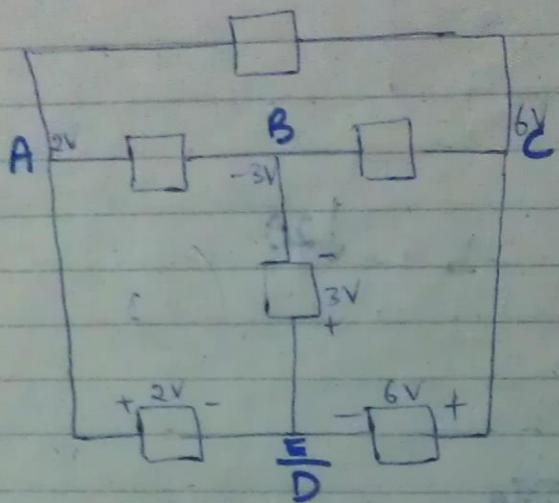
Q33)



Q34)
Q3

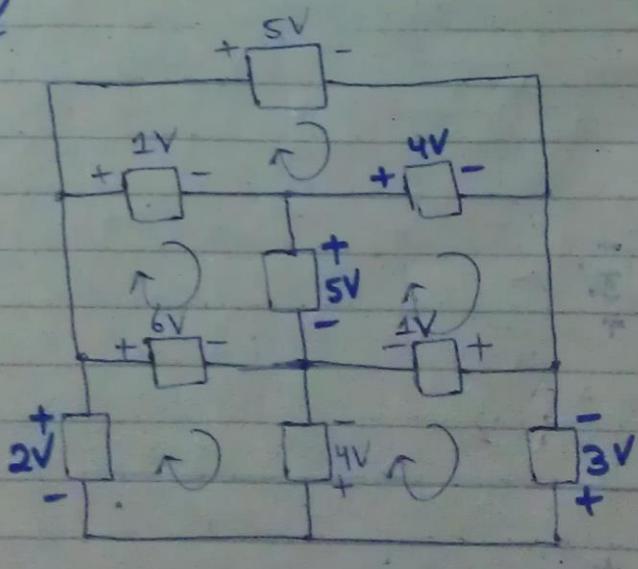


b) D is reference nod.



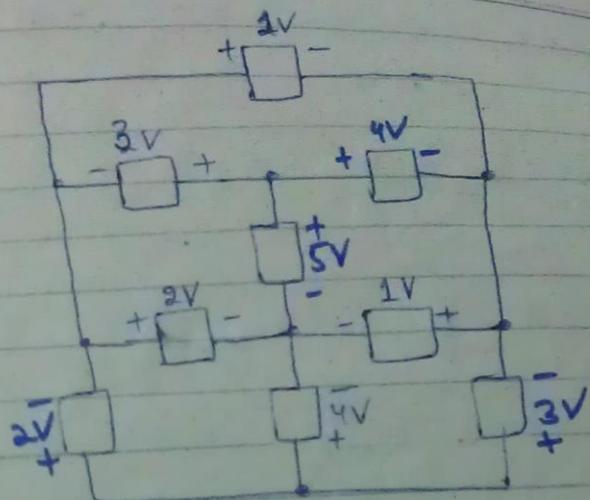
$$A = 2V, B = -3V, C = 6V$$

Q.35)

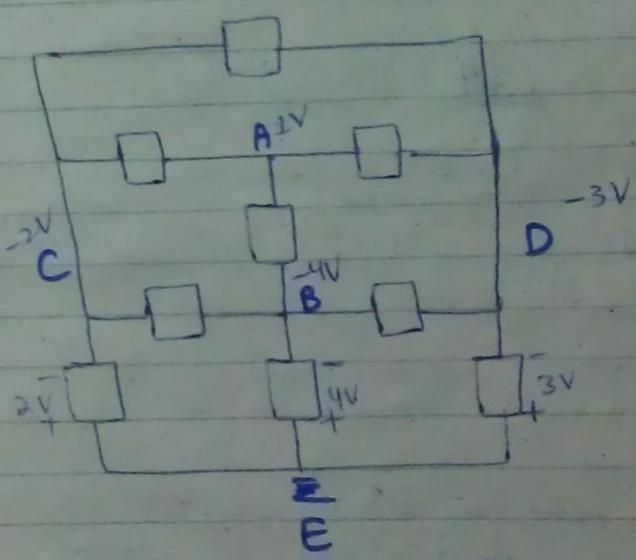


Q 36)

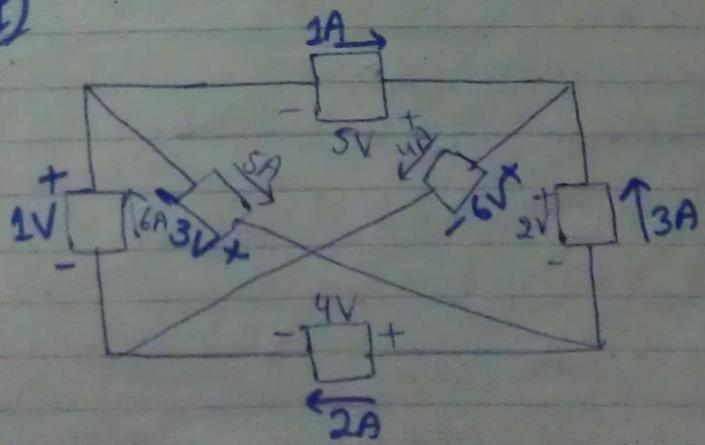
a)



b)



Q 37)

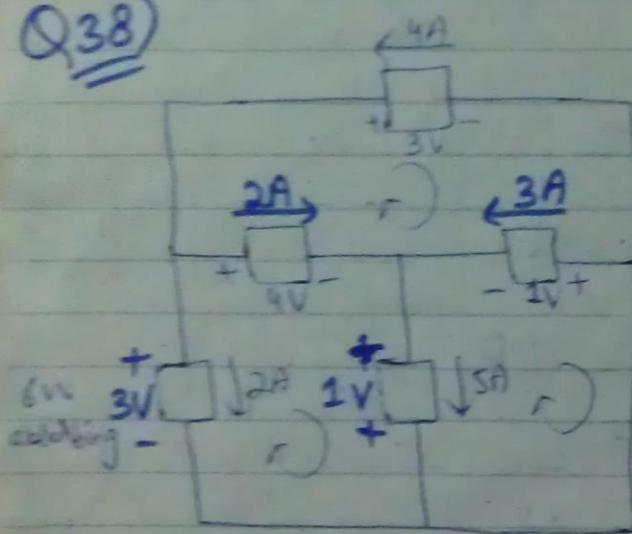


$$\text{power released} = 1 \times 5 + 2 \times 3 + 1 \times 6 + 3 \times 5 \\ = 32$$

$$\text{power absorbed} = 6 \times 4 + 4 \times 2 \\ = 32$$

Power released = power absorbed
 So, power is conserved.

Q38)

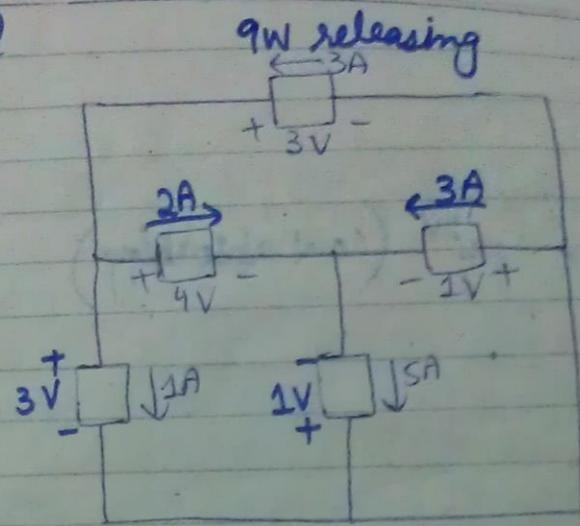


$$\text{power released} = 4 \times 3 + 8 \times 1 = 17$$

$$\text{power absorbed} = 3 \times 2 + 2 \times 4 + 3 \times 1 = 17$$

So, power is conserved

Q39)

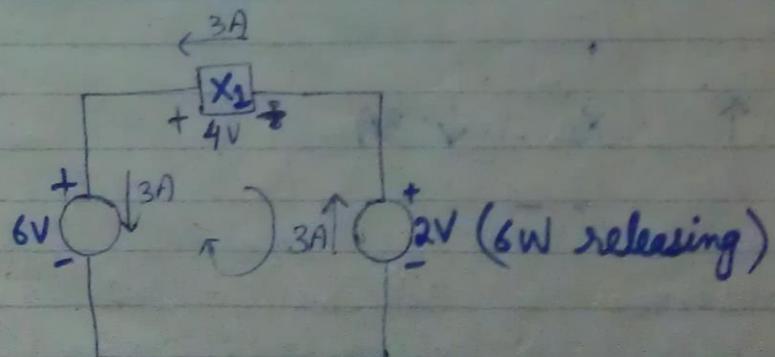


$$\text{Power released} = 3 \times 3 + 1 \times 5 = 14$$

$$\text{Power absorbed} = 2 \times 4 + 3 \times 1 + 1 \times 3 = 14$$

So, Power is conserved.

Q49)



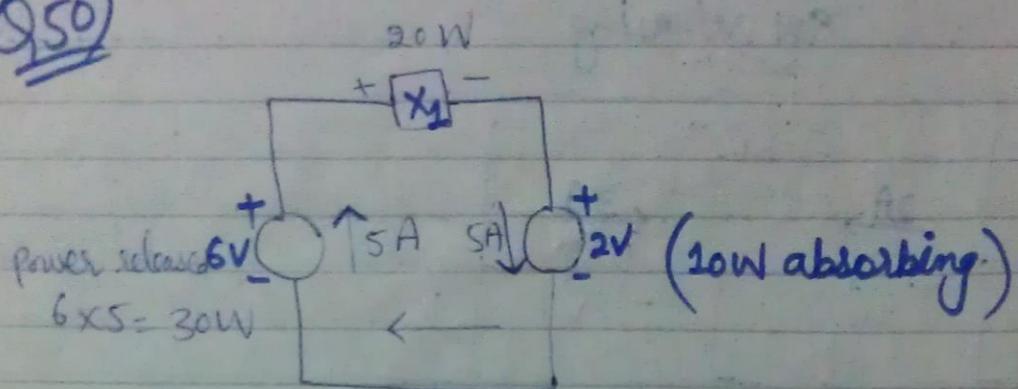
$$i = 3A \text{ (counter clockwise)}$$

b)

$$\text{Power absorbed by } 6V \text{ source} = 6 \times 3 = 18W$$

$$\text{Power released by } X_1 \text{ compound} = 4 \times 3 = 12W$$

Q50)



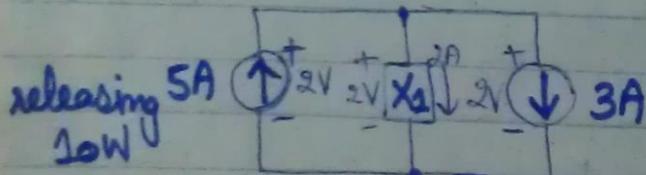
$$P = VI$$

$$10 = 2 \times I$$

$$I = 5\text{A}$$

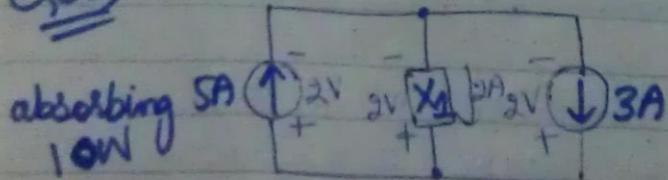
$$\begin{aligned}\text{Power released} &= VI \\ &= 6 \times 5 \\ &= 30\text{W}\end{aligned}$$

Q51)



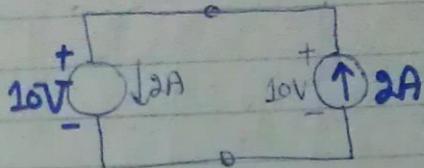
$$\begin{aligned}\text{Power absorbed by } 3\text{A source} &= 3 \times 2 = 6\text{W} \\ \text{Power absorbed by } X_1 \text{ compound} &= 2 \times 2 = 4\text{W}\end{aligned}$$

Q52)



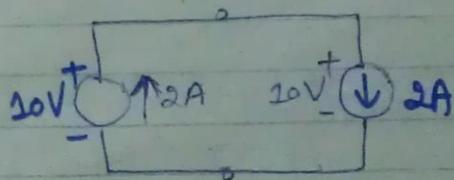
$$\begin{aligned}\text{Power released by } 3\text{A source} &= 3 \times 2 = 6\text{W} \\ \text{Power released by } X_1 \text{ compound} &= 2 \times 2 = 4\text{W}\end{aligned}$$

Q53)



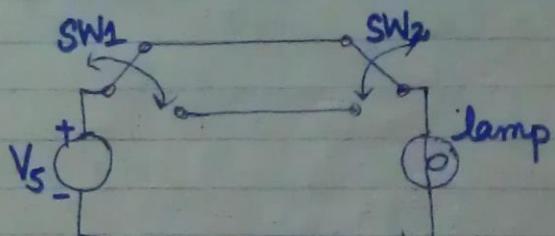
20W power is absorbed by 10V source.
20W power is released by 2A source.

b)



20W power is absorbed by 2A source.
20W power is released by 10V source.

Q54)



- i) The lamp will be off when switch 1 is on and switch 2 is off.
- ii) when SW1 is off and SW2 is on.

D)

- iii) The lamp will be on when SW1 is on & SW2 is on.
- iv) when SW1 is off and SW2 is off.