

PDE

- ✚ To get all subject Notes: Just mail me at
Adi.CrazyGate2015@gmail.com
- ✚ After mailing within 2 minute you will get all subject note's
- ✚ I have a polite request to you if you will forward these note's to all your friend I will very thankful of yours
- ✚ If you want to all subject notes regarding GATE Chemical Engineering Please you can Join this group on Face book :
<https://www.facebook.com/groups/GateChemicals/>
- ✚ Very soon we will update you with well organized printed material & practice papers :

Thanks to all of You :

Sep 08/14

EconomicsTotal Capital Investment:-

It is a total investment required to start a project.

Consist of two types

- Fixed Capital Investment {
 - Manufacturing FC-I
 - Non-Manufacturing FC-I

Actually capital invested for start of plant
- Working Capital Investment
to fulfill plant worse condition.

* Fixed C.I :-

It is the capital needed to supply the necessary manufacturing and plant facilities and It is the actual money that is invested in the project.

→ Manufacturing fixed Capital:-

Money that is directly related to the ^{plant} ^{production} process operation.

ex → equipment, piping, electricity, raw material cost etc.
installation, manufacturing,

→ Non-Manufacturing fixed Capital:-

Money that is indirectly related to the process operation

ex → shops utilities, facilities for employees, construction overhead etc.
administrative office.
all office indirectly related
accounting office

* Working C.I :- money, that we keep with us for emergency purposes.

Capital necessary for the handling of emergency purposes.
ex → in case of strike.

** Depreciation :-

0	V_0	3L
1	V_1	2.4L
2	V_2	2.0L

> (0.6L) Depreciation.

These values are known as Book Value or Asset Value

n service life \rightarrow (10)
 $SO K \rightarrow$ scrap \rightarrow $V_s \neq 0$
 \rightarrow $SO K \rightarrow$ scrap \rightarrow $V_s = 0$

Book Value

It is the net present value of the equipment at the end of the year. It is represented by V_a . Which means yearly cost with net present value of the equipment at the end of the year 'a'

$$d_a = V_{a-1} - V_a$$

Depreciation
amt

Service Life:-

The period during which the use of the property is economically feasible is known as the service life. It is denoted by 'n'

Salvage/Scrap Value:-

Salvage is the net amt of money obtainable from the sale of used property over and above any charges involved in the removal and sale. (over & above charge is deinstallation)

Scrap is the value obtainable from the equipment is negligible then it is dismantled and sold as junk. The profit then obtained is known as the scrap value.

It is represented as V_s .

Salvage value $V_s \neq 0$
 Scrap " $V_s = 0$

Depreciation:-

Equipments, buildings, and other material objects comprising a manufacturing plant require an initial investment, which must be written off as an manufacturing expense. In order to write right

of this cost, ~~as~~ a decrease in value is assumed to occur throughout the usual life of the material. This decrease in value is designated as depreciation.

Reasons of depreciation.

Factors

Physical Depreciation

Technological Advances bcz improvement in technology value of previous technology depreciates

Economic changes value of dollar changes / change in currency

Methods of Calculating Depreciation :-

Do not consider the Time Value of Money :-

Consider the time Value of Money.

Don't consider Time Value

Consider Time Value

1> Straight line Method

2> Declining Balance Method

3> Double Declining Balance Method

4> Sum of the year Digits Method.

1> Sinking-Fund.

2> Present-Worth

Straight Line Method :-

Assumptions

1> Depreciation amt is same for the subsequent years.

$$d_1 = d_2 = d_3 = \dots = d_n$$

2> After the service life, the value may be salvage or scrap.

$$V_s \neq 0, \text{ \& } V_s = 0.$$

n = service life
or depreciation amt.

$$d = \frac{V_0 - V_s}{n}$$

V_0 = Value of equipment at the start of operation.

V_s = Value of equipment after service life.

$$V_1 = V_0 - d$$

$$V_2 = V_1 - d = V_0 - d - d = V_0 - 2d$$

$$V_3 = V_0 - 3d$$

$$V_n = V_0 - nd$$

V_n = book value of equipment after a year.

n = any year.

d = depreciation.

Q. The original value of an equipment is Rs 10,000. The salvage value is Rs 500, at the end of its useful life period of 5 yrs. What is the asset value in Rs, after 2 years by st. line method.

$$V_0 = \text{Original value} = 10000$$

$$V_s = \text{Salvage Value} = 500$$

$$n = \text{service life} = 5$$

$$d = \frac{10000 - 500}{5} = 1900$$

$$V_2 = 10000 - 2 \times 1900 = 6200$$

Declining Balance Method:- (Depreciation)

Assumptions:-

1) The depreciation amt for the subsequent yrs is not same.

$$d_1 \neq d_2 \neq d_3 \neq d_4 \dots \neq d_n$$

2) The %age fixed factor is same

$$\begin{array}{ll} V_0 & 10L \\ V_1 & 9L \\ V_2 & 8.1L \end{array}$$

$$f = 10\%$$

$$d_1 = 1L > 10\%$$

$$d_2 = 9000 > 10\%$$

depreciation is not same

fixed factor is same

3) It is applicable only for salvage value.

$$V_s \neq 0$$

$$d_1 = v_0 \times f$$

$$d_2 = v_1 \times f$$

$$\boxed{d_a = v_{a-1} \times f}$$

$$v_1 = v_0 - d_1$$

$$= v_0 - v_0 f = v_0 (1 - f)$$

$$v_2 = v_1 - d_2 = v_0 (1 - f) - v_1 f$$

$$= v_0 (1 - f)^2$$

$$\boxed{v_a = v_0 (1 - f)^a}$$

$$v_s = v_0 (1 - f)^n$$

$v_a = v_s$ Compensation
 $a = n$

$$\left(\frac{v_s}{v_0}\right)^{1/n} = (1 - f)$$

$$\boxed{f = 1 - \left(\frac{v_s}{v_0}\right)^{1/n}}$$

$v_s \geq 0$
then $f \neq 100\%$
 \therefore this method is not valid
for scrap value.
Equipment can't depreciate by 100%.

Q> above question by declining balance method, also calculate depreciation ant for second yr.

$$f = 1 - \left(\frac{500}{10000}\right)^{1/5}$$

$$= 0.450719$$

$$v_2 = 10000 (1 - f)^2$$

$$= 10000 \times 0.3017088$$

$$= 3017.088$$

$$d_2 = v_1 \times f$$

$$= v_0 (1 - f) \times f$$

$$= 2475.713$$

Double Declining Balance Method:-

Same as the declining balance Method but applicable for the case of scrap value.

$$d_n = V_{n-1} \times f$$

$$V_n = V_0(1-f)^n$$

$$f = \frac{2}{n} \text{ service life}$$

Q. Same question, $V_s = 0$, Calculate V_2, d_2

**
if it is salvage
go for declining
if it is scrap
go for double declining

$$f = \frac{2}{5} = 0.4$$

$$V_2 = V_0(1-f)^2$$

$$= 10000 \times 0.36$$

$$= 3600$$

$$d_2 = V_0(1-f) \times f$$

$$= 2400$$

**

If $V_s = 0$, then $f \neq 100\%$, we go for double declining.

Sum of the year digit Method:-

Assumptions:-

- ⇒ The depreciation amount is not same of the subsequent years.
 $d_1 \neq d_2 \neq d_3 \neq \dots \neq d_n$
- ⇒ % fixed factor is not same.
- ⇒ Applicable for salvage as well as scrap.

$$d_a = \frac{n-a+1}{\sum n} \{V_0 - V_s\}$$

$n = \text{service life}$

$$\sum n = \frac{n(n+1)}{2} \quad \text{sum of natural nos.}$$

$$V_1 = V_0 - d_1$$

$$V_2 = V_0 - d_1 - d_2$$

$$V_3 = V_0 - d_1 - d_2 - d_3$$

there is no shortcut
we have to find all
 $d_1, d_2, d_3 \dots$

Q) same quest $\Rightarrow V_2 = ?$ & $d_2 = ?$

$$\begin{aligned} d_2 &= \frac{5-2+1}{15} \{10000 - 500\} \quad \frac{5(6)^3}{2} \\ &= \frac{4}{15} \{9500\} \\ &= 2533.333 \end{aligned}$$

$$\begin{aligned} d_1 &= \frac{5-1+1}{15} \{9500\} \\ &= 0.333 \times 9500 \\ &= 3166.66 \end{aligned}$$

$$\begin{aligned} V_2 &= V_0 - d_1 - d_2 \\ &= 4300.00 \end{aligned}$$

Q) A piece of equipment originally costing Rs 40,000 was put into use 12 yrs ago. At the time the equipment was put into use, the service life was 20 yrs and the salvage value was assumed to be zero. On this basis a straight line depreciation fund was set up. The equipment can now be sold for Rs 10,000 and a more advanced model can be installed for Rs ~~55,000~~ 55,000. Assuming the depreciation fund is available for use. How much new capital must be supplied to make the purchase.

$$d = \frac{40000}{2.0}$$

$$= 20000$$

$$\text{depreciation amt in saving} = 12 \times 20000$$

$$= 240000$$

$$\text{after scaling total saving} = 240000 + 10000$$

$$= 340000$$

$$\text{new capital required} = 550000 - 340000$$

$$= 210000$$

PBT

$$\text{PBT} = \text{Profit before Tax} = \text{Income} - \text{Expense} \quad \text{after the start}$$

$$\text{TP} = \text{Taxable Profit} = \text{PBT} - \text{Depreciation}$$

before started plant
some part of P.C.
also used to save some
tax.

$$\text{PAT} = \text{Profit After Tax} = (1 - i) \text{TP}$$

↓
Tax rate

money which
an owner can use
for its own personal use.

$$\text{Expense} + \text{Depreciation} = \text{TFC}$$

Sep 09, 14

- Q.2) The investment for an asset cost Rs 100000, and the asset was assumed to have a service life of 12 yrs with 20000 salvage value. After the asset has been in use for 5 yrs the remaining service life and final salvage value are reestimated at 10 yrs and 10000 resp. Under this condition what is the depreciation cost during the 6th yrs of the total life if st. line depreciation is used.

$$V_0 = 10000$$

$$n = 12$$

$$V_s = 2000$$

$$a = 5$$

$$n_r = 10$$

$$V_{s_r} = 1000$$

depreciation after
5 yrs

$$d = \frac{10000 - 2000}{12}$$

$$= 666.66$$

depreciated value of
equipment,

$$V_a = V_0 - a d$$

$$= 6666.66$$

$$| a = 5$$

New estimate of
depreciated value.

$$d = \frac{6666.66 - 1000}{10}$$

$$= 566.66$$

Q. A property has an initial value of Rs 50,000, service life of 20 yrs. and final salvage value Rs 4000. It has been proposed to depreciate the property by tax book declining balance method. Would this method will be acceptable for income tax purposes in comparison to st. line method. If both are compared for initial 3 yrs of plant life.

$$V_0 = 50,000, \quad n = 20, \quad V_s = 4000$$

$$f = 1 - \left(\frac{V_s}{V_0}\right)^{1/n}$$

$$= 0.1186$$

$$V_3 = V_0 (1-f)^3$$

$$= 34,232.09$$

$$d_3 = V_2 \times f$$

$$= 4,606.8$$

st. line

$$st = d = 2300$$

$$(d_1 + d_2 + d_3) = 6900 \text{ ₹}$$

$$(d_1 + d_2 + d_3)_{DSM} = 15768 \text{ ₹}$$

DSM method is acceptable bcz we for more value we have to pay less tax

Q.2) The initial cost of the completely installed reactor is Rs 60000, $V_s = 10,000$. The total annual expenses for the plant is Rs 1,00,000. How many years of useful life should be estimated for the reactor if 12% of the total annual expenses for the plant are due to the cost for the reactor depreciation. S.L. method is used for depreciation purposes.

$$V_0 = 60000, V_s = 10,000$$

$$E_A = 1,00,000$$

$$n = ?$$

$$f.v. = 12\%$$

$$d = 12000$$

$$12000 = \frac{60000 - 10000}{n}$$

$$n = 4.16 \text{ yr}$$

Q.3) A person has a total income of 1 million/yr. and all expenses except depreciation amt are 6 lakh/yr. At the start of the 1st yr of operation. A composite account of all the depreciable items shows a value of 8,50,000. and the overall service life is estimated to be 20 yrs. The total V_s at the end of service life is estimated to be 50,000. 30% of all the profit before taxes must be paid but as income taxes. What would be the reduction in the income tax charges for the 1st yr of the operation. If sum of year digit method were used for

depreciation accounting instead of st. line method. $Am = 10,857$

$$TI = 1 \text{ million} = 100,000,000$$

$$Expense = 6,000,000$$

$$V_0 / \text{Composite Depreciation} = 8,500,000$$

$$n = 20$$

$$V_s = 50,000$$

$$PBT = I - E$$

$$= 4,000,000$$

$$\text{IFT paid} = \frac{30 \times 4,000,000}{100} = 1,200,000$$

Taxes is given applied over PBT, it is applied over TP

$$d_1 = \frac{20 \times 1 + 1}{1} \{ 1,000,000 - 50,000 \}$$

$$=$$

$$d_{SLM} = \frac{8,500,000 - 50,000}{20}$$

$$= 40,000$$

$$d_{SDM} = \frac{\frac{20}{20-1+1}}{\frac{20-1}{2}} \{ 8,500,000 - 50,000 \}$$

$$= 1,60,000, 76,190.476$$

$$30 (TP)_{SDM} = 4L - (d)_{SDM} = 3,23,809.32$$

$$30\% (TP)_{SDM} = 97,142.857$$

$$(TP)_{SLM} = 4L - (d)_{SLM} = 3,60,000$$

$$30\% (TP)_{SLM} = 108,000$$

Q.7 A plant has a service life of 7, $V_s = 30\%$ of initial value. For what min^m fixed % age factor will be the depreciation amt for the 2nd yr. calculated by DDBM, be equal to that calculated by the st. line method.

0.113

$$V_0 =$$

$$V_s = 30\% \text{ of } V_0$$

$$n = 7$$

$$d_2 = \frac{V_0 - 0.30V_0}{7}$$

$$V_2 = V_0 - 2 \left(\frac{V_0 - 0.30V_0}{7} \right)$$

$$f = 1 - \left(\frac{0.30V_0}{V_0} \right)^{1/n}$$

$$= 1 - 0.8419 = 0.1580$$

$$V_2 =$$

$$(d_2)_{\text{DBM}} = (d_2)_{\text{SLM}}$$

$$V_0 \times f = \frac{V_0 - V_s}{n}$$

$$V_0 (1-f) f = \frac{V_0 - 0.3V_0}{7}$$

$$f - f^2 = \left(\frac{0.7V_0}{7} \right) \frac{1}{V_0}$$

$$f - f^2 = 0.1$$

$$f^2 - f + 0.1 = 0$$

$$f = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(0.1)(1)}}{2 \cdot 1}$$

$$= \frac{1 \pm \sqrt{1 - 0.4}}{2}$$

$$= \frac{1 \pm 0.7745}{2}$$

$$= 0.112, 0.88725$$

minim value $f = 0.112$,

Interest:-

Interest:-

It is the money returned to the owner of the capital for the use of their capital. It is of two types.

1) Simple Interest:-

It requires compensation payment at a constant interest rate based on the original principle.

$$Z = Pin$$

$$S = P + Z = P + Pin = P(1 + in)$$

2) Compound

If payment is not made at the specified time interval then interest on interest will be there.

0
1
⋮
n-1

P
 $P(1+i)$

Pi
 $P(1+i)i$

$$S = P + Pi = P(1+i)$$

$$S = P(1+i) + P(1+i)i$$

$$= P(1+i)^2$$

$$S = P(1+i)^n$$

When the compounding is Annual, then

$$S = P(1+i)^n$$

i.e. effective interest rate compounded
annually

if compounding is not annual,

$$S = P\left(1 + \frac{r}{m}\right)^{mn}$$

r = nominal interest rate based on annual basis.

m = no. of intervals/year.

iss word r pehle r aur baad me m ki value hoti.

Q.7

6% compounded semi-annually.

r ← m

1.5% per quarter

$$r = 1.5 \times 4 = 6\%$$

Q.7

3% per quarter compounded quarterly

$$r = 3 \times 4 = 12\%$$

$$m = 4$$

Effective interest rate:—

It is defined as the actual annual return on the principal, u get after the 1 yr is more than the nominal interest rate bcz of the compounding effect at the end of a quarter, month, semi-annual period. This increased rate is known as effective interest rate.

$$1_{\text{eff}} = \left(1 + \frac{r}{m}\right)^m - 1$$

Q.7 It is desired to borrow 1000 to meet a financial obligation. The money can be borrowed from a loan agency at a monthly interest rate of 2%. Determine a total amount after 2 yrs when compounded monthly. Also calculate the effective interest rate.

$$P = 1000 \text{ ₹}$$

$$m = 12$$

$$n = 2$$

$$r = 0.02 \times 12 = 0.24\%$$

$$S = 1000 \left(1 + \frac{0.24}{12} \right)^{12 \times 2}$$

$$= 1040.43178 \approx 1608.437$$

$$\text{left} = \left(1 + \frac{r}{m} \right)^m - 1$$

$$= 0.2682$$

Continuous Compounding:-

When time period of compounding becomes extremely small or no. of intervals/year becomes extremely large. Then the interest is calculated by the help of continuous compounding.

$$S = P e^{rn} \quad \text{--- continuous}$$

$$\text{left} = e^x - 1$$

$$m \rightarrow \infty$$

$$t \rightarrow 0$$

per (min/hr)
compounding

Q.7 same questn.

$$S = P \cdot e^{rn} = 1000 (12)^{0.2 \times 2}$$

=

Annuity

$P \Rightarrow$ Present Value

$S \Rightarrow$ Future Value

Annuity:-

An annuity is a series of equal payment occurring at equal time intervals,

Equal Payment
Equal Intervals

! How much k baad
10,000, & 10,000.
! Ye mtlb koto k issue

as have loan

- ⇒ The payment of this type can be used to pay off a debt, accumulate a desired amt of capital, Receive a lumpsum of capital as in insurance plan and in the insurance plan.

Let Capital P represent uniform periodic payment made during n discrete period. such that the first payment being made at the end of the first year.

Future Value of annuity

future value of annuity

$$S = R(1+i)^{n-1} + R(1+i)^{n-2} + \dots + R(1+i) + R \quad (1)$$

$$S(1+i) = R(1+i)^n + R(1+i)^{n-1} + \dots + R(1+i) \quad (2)$$

$$S(1+i) - S = R(1+i)^n - R \quad (2)-(1)$$

$$S = \frac{R}{i} [(1+i)^n - 1]$$

to accumulate some money
debt to have some money.

$$S = P(1+i)^n$$

Present value of Annuity

$$P = \frac{R}{i} \left[\frac{(1+i)^n - 1}{(1+i)^n} \right]$$

debt to borrow some money
need to pay some money $\geq P$

Q7 It is desired to have 9000 ₹ available 12 yrs from now. If 5000 is available for investment. Then calculate the annual rate of compound interest.

$$S = 9000$$

$$n = 12$$

$$P = 5000$$

$$i = ?$$

$$S = P(1+i)^n$$

$$9000 = 5000(1+i)^{12}$$

$$1.8 = (1+i)^{12}$$

$$i = 0.05020$$

$$= 5.02\%$$

Q8 What will be the amt aft 10 yrs, if 2000 ₹ is deposited with a nominal interest rate of 6%. compounded semi-annually.

$$n = 10$$

$$S = ?$$

$$P = 2000$$

$$r = 6\%$$

$$m = 2$$

$$S = P \left(1 + \frac{r}{m}\right)^{mn}$$

$$= 3612.22 \text{ ₹}$$

Q9 A loan of Rs 2000 was made at 6% S.I per year for 4 yrs. at the end of this term, no interest had been paid and the loan was extended for 6 more years at a new effective compound interest rate of 8% / year. What is the total amt at the end of 10 yrs.

$$S = P + I, \quad I = 2000 \times 0.06 \times 4$$

$$= 480$$

$$S = 2480 = P_{\text{new}}$$

$$S = P_{\text{new}}(1+i)^n$$

Here we consider $n = 6$

$$= 2480(1+0.08)^6 = 3935.44$$

Q. > A person borrows Rs 50,000 at an effective interest rate of 10%. He wish to pay of the debt 5yrs by taking equal interval payment in each year. How much the each payment have to be?

$$P = 50,000$$

$$R = ?$$

$$P = \frac{R}{i} \frac{(1+i)^n - 1}{(1+i)^n}$$

$$50,000 = \frac{R}{0.1} \left(\frac{(1+0.1)^n - 1}{(1+0.1)^n} \right)$$

$$R = 13189.87 \text{ ₹}$$

Q. > An annuity due is being used to accumulate money with a effective compound interest rate of 8%, and Rs 1000 is deposited at the begining of ^{each} year. What will be the total amt of annuity due after 5 yrs.

$$R = 1000$$

$$i = 0.08$$

$$n = 5$$

This formula is used to Annuity due is used as payment is done at starting.

$$S = \frac{R}{i} [(1+i)^n - 1] (1+i)$$

$$= ₹ 866.60$$

$$S = 6335.929 ₹$$

Annuity = deposited end of yr.

Annuity due = deposited beginning of yr.

Present worth method :-

$$V_0 \leftarrow P = \frac{R}{i} \frac{(1+i)^n - 1}{(1+i)^n} \quad \text{Dep. amt.}$$

Present value is considered

Sinking fund Method

hypothetical method
abt all used any where.

$$S = \frac{R}{i} [(1+i)^n - 1]$$

\downarrow
 $V_0 - V_s$

Future value.
in some money req. to purchase

accumulate the money.

$$V_0 - V_a = \frac{R}{i} [(1+i)^n - 1]$$

$$V_0 - V_a = \frac{(V_0 - V_s)i}{i} \frac{[(1+i)^n - 1]}{[(1+i)^n - 1]}$$

$$V_a = V_0 - (V_0 - V_s) \frac{[(1+i)^n - 1]}{[(1+i)^n - 1]}$$

book value of equipment

Q. > A piece of equipment has an initial installed value of Rs 12000. It is estimated that its useful life period will be 10 yrs and V_s at the end of the useful life will be 2000. Depreciation will be charged by making equal charges each yr. 1st payment being made at the end of the 1st yr. The depreciation fund will be accumulated at an annual interest rate of 6%. At the end of the useful life, enough money must have been accumulated to account for the decrease in the equipment value. Determine the yearly

Cost due to depreciation?

$$V_0 = 12000, \quad n = 10, \quad V_s = 2000, \quad i = 0.06$$

$$S = \frac{R}{i} [(1+i)^n - 1]$$

$$12000 - 2000 = \frac{R}{0.06} [(1+0.06)^{10} - 1]$$

$$= 759.$$

$$\text{for 10 yrs} = 759 \times 10 = 7590.$$

★ These methods are better which don't consider time value of money.

Profitability

Methods of Profitability

Rate of return of Investment Method.

Net present Value Method

Discounted cash flow/Internal rate of return Method

Capitalized cost pay method.

Payout period method.

Rate of return of investment

It is defined as the ratio of profit to investment.

use to check pt

$$\frac{PBT}{FCI}, \quad \frac{PAT}{FCI}, \quad \frac{PBT}{TCI}, \quad \frac{PAT}{TCI}$$

Q. A plant requires an initial fixed capital of 9L and 1L of working capital. It is estimated that the annual income will be 8L, and the annual expenses including depreciation will be 5.20L, before IT. IT amounts to 34% of all pre-tax profits. Calculate the annual % return on total initial investment before income tax.

$$\frac{PBT}{TCI} = \frac{8L - 5.20L}{9L + 1L}$$

=

20.53%

Calculate the annual % return of F.C.I after income tax.

PAT

20.53%

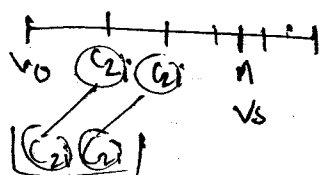
$$PAT = (1 - i) \times 2.8L$$

=

$$\frac{PAT}{F.C.I} = \frac{\quad}{9L}$$

ROR are pt values, and they are the pt values. ROR doesn't consider the \therefore they are not that accurate.

Capitalized Cost Method *allow more best*



$$S = \frac{R}{i} [(1+i)^n - 1]$$

$$V_0 - V_s = \frac{C_2 i}{i} [(1+i)^n - 1]$$

$$C_2 = \frac{V_0 - V_s}{(1+i)^n - 1}$$

$$C.C = V_0 + C_2$$

Perpetuity

Capitalised cost related to the investment represents the amt of money that must be available initially to purchase the equipment and simultaneously provide sufficient fund or interest accumulation to permit periodic replacement of the equipment.

Perpetuity - pay

Q.2. There are 3 tender m_1, m_2, m_3 . for m_1 service life is 10yr, initial value is 15 Lakhs, for 6 yrs - and initial value $15\frac{1}{2}$ L, 8yr, $M_3 \rightarrow 18\frac{1}{2}$ L.

Which is the best acc. to CC method if rate of interest is 10%.

	initial Value	Yr.
M_1	15	10
M_2	$15\frac{1}{2}$	6
M_3	$18\frac{1}{2}$	8

Q.3 Two pumps are under consideration for insulation.

1st one initial value 40000, $V_s = 3900$, 2nd initial value

50000, $V_s = 20,000$. Using the CC method find the common

life of the pumps. If both the pumps are equally economical.

[210%]

$$C_2 = \frac{V_0 - V_s}{(1+i)^n - 1}$$

=

$$\frac{40000 - 3900}{(1+0.10)^n - 1} = \frac{50000 - 20000}{(1+0.10)^n - 1}$$

$$40000 + \frac{36100}{1.1^n - 1} = \frac{30000}{1.1^n - 1} + 50000$$

$$\frac{36100}{1.1^n - 1} = \frac{30000 + 10000(1.1^n - 1)}{1.1^n - 1}$$

$$36100 - 30000 = (11000)^n - 10000$$

5>

Q> A H.E. with a negligible scrap value cost Rs 4000, and will have a useful life of 6yr. Another proposed H.E. of equivalent design capacity cost Rs 6800. But will have a useful life of 10yrs and a salvage value of 800. Assuming a rate of 8% per year. Determine which H.E. is cheaper.

1st one.

$$= \frac{4000}{(1+0.08)^6}$$

Q.7 A new storage tank can be purchased and ~~old~~ installed for Rs 10,000. This tank would last for 10 yrs. Another storage tank of capacity equivalent to the new tank is available and it has been proposed to repair the old tank instead of buying new 1. If the tank were repaired it would have useful life of 3 yrs before the same type of repairs would be needed again. neither tank have any scrap value. Money is worth 9% compounded annually. On the basis of equal capitalized cost for the two tanks. How much can be spent for repairing the existing tank.

New
 $V_0 = 10,000$
 $n = 10 \text{ yr}$
 $V_s = 0$

Old
 $n = 3 \text{ yrs}$
 $V_s = 0$

3414

$i = 0.09$

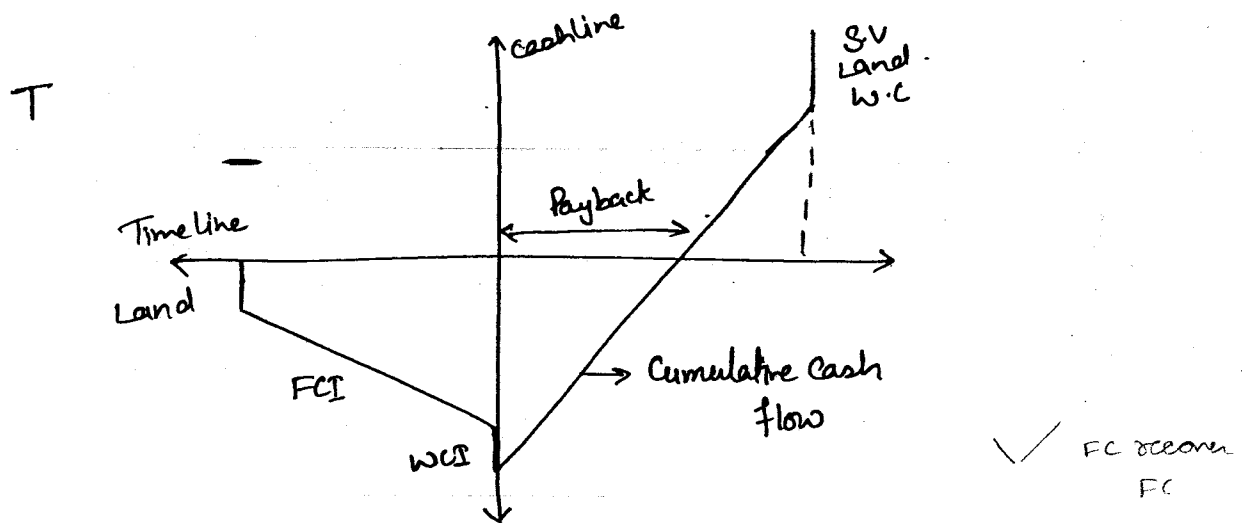
$$10000 + \frac{10000}{(1+0.09)^{10} - 1} = V_0 + \frac{V_0}{(1+0.09)^3 - 1}$$

$$17313.3433 =$$

Payout Period / Payback time

The total money ^{available} after the end of any year is called cash flow

PAT + Depreciation,



The minimum length of time theoretically necessary to recover the original depreciable capital investment in the form of cash flow to the project, is known as the payback time.

$$t = \frac{FCI}{CF} \text{ — Profit}$$

Net Present Value Method:-

Best method, accurate, tell abt whole plan.

The initial F.C. = 1L , W.C. = 10,000 , $N = 5$ yr , $V_s = 10,000$

Year	Predicted Cash Flow	Discounting Factor $C = 0.15$
0	1,10,000	
0-1	36,000	26100
1-2	31,000	23,420
2-3	36,000	23,700
3-4	40,000	22,900
4-5	43,000 + SV + W.C.	21,400
5		9000 + 5000

money get = 127500

Invest = 110000

NPV = 17500 > 0

FCI + W.C.

Internal rate of return.

The rate at which NPV is zero, is known as the internal rate of return.

$\approx 20.7\%$

max^m interest rate which should be borrowed to start a plant.

Q> F.C.I for a chemical plant is Rs 40 million with an estimated useful life of 6 yrs and a salvage value of 4 million. The rate of interest is 15%. Tax rate is 25%. In the first yr of operation the income from sales is Rs 20 million and the manufacturing expenses are 5 million. The plant is depreciated on a st. line basis.

i> calculate the ROR on investment.

$$ROR = \frac{PBT}{FCI} = \frac{I - E}{FC} = \frac{20 - 5}{40}$$

if it is not mentioned in the question we take PBT $= \frac{15}{40} = 0.375$

Q> for the same data the net present value in million at the start and at the end of the first yr of operation R.

$$NPV = \text{Total Discounted Cash flow (we earned)} - \text{total initial investment (we invest)}$$

$$NPV_{\text{start}} = 0 - 40 = -40 \text{ Million}$$

$$NPV_{1^{\text{st}} \text{ yr}} =$$

At the end of the first yr,

$$PBT = 20 - 5 \\ \approx 15 \text{ Million}$$

$$(I - E)$$

$$TP = 15 - 6 = 9M. \quad (PBT - \text{depreciat})$$

$$PAT = 0.75 \times 9M = 6.75M. \quad ((1-i)TP)$$

$$\text{Cash flow} = 6.75 + 6 = 12.75M \quad (PAT + \text{Deposi})$$

$$\boxed{NPV_{1st \text{ yr}} = 12.75 - 40 \\ = -27.25M}$$

$$(P = \frac{S}{(1+i)^t})$$

$$\text{Present value of Cash flow} = \frac{12.75}{(1+0.15)^1} = 11.08M$$

$$NPV_1 = 11.08 - 40 = -28.92$$

if cash flow remains same at each year calculate the payback t_{ym}.

$$t = \frac{FCI}{CF} \\ = \frac{40}{12.75} = 3.137$$

for same data, if we consider t_{ym} value of money, t = ?

if we consider t_{ym} t > .

$$\frac{12.75}{(1+i)} + \frac{12.75}{(1+i)^2} + \frac{12.75}{(1+i)^3} + \dots = 40$$

$$P = \frac{R}{i} \left[\frac{(1+i)^n - 1}{(1+i)^n} \right] \approx 40 \\ = \frac{12.75}{0.15} \left(\frac{1.15^n - 1}{1.15^n} \right) \approx 40 \\ = 85 \left(1 - \frac{1}{1.15^n} \right) \approx 40$$

$$1 - \frac{1}{1.15^n} = 0.4705$$

W.D.J

$$1.15^n = 1.888$$

$$n = 4.55$$

2. A process has a fixed capital of Rs 150 Lakh, WC of Rs 30 L and salvage value 0. Annual revenue from the sales are Rs 250 L manufacturing cost are Rs 145 L and the other expenses are 10% of revenue. Assume the project life span of 11 yr, tax life of 5 yr, and interest rate to be 10%. Tax rate is 40% & straight line depreciation i.e. 20%/year is applicable. Calculate the discounted value of the profit before tax, for the total plant life period.

$$F.C. = 150 \text{ L}, \text{ WC} = 30 \text{ L}, V_s = 0$$

$$n = 11 \text{ yrs}$$

$$MC = \frac{145 + 25}{1.10}$$

$$DN = 250 \quad 10\%$$

$$= 80$$

$$\begin{aligned} PBT &= I - E \\ &= 250 - 145 - 25 \\ &= 80 \text{ Lakh.} \end{aligned}$$

$$P = \frac{80 (1 + 0.1)^n - 1}{0.1 (1 + 0.1)^n} = 519.60 \approx 520 \text{ L.}$$

ii. The discounted value of depreciation benefit over the tax life is.
 Present value Saving tax, if we apply depreciation method.

$$PBT = 80 \text{ L}$$

$$40\% \text{ PAL} = 48 \text{ L}$$

$$\text{Tax Paid} = 32 \text{ L}$$

when depreciation applied,
TP = 50 L

$$PAT = 30 \text{ L}$$

$$\text{Tax paid} = 20 \text{ L}$$

$$\boxed{\text{Tax Saved} = 12 \text{ L}}$$

Present Value. $P = \frac{12}{0.1} \left[\frac{(1+0.1)^5 - 1}{(1+0.1)^5} \right]$

45.48

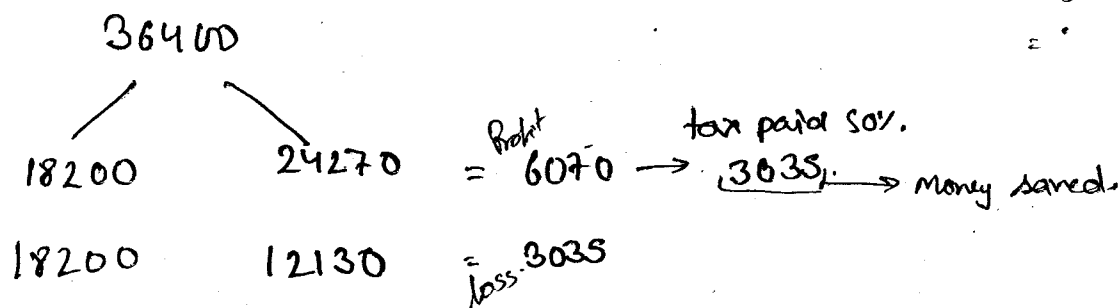
n25

$$= 45.48$$

F.C.I or initial investment.

Q.7 A company has a depreciable investment of Rs 36,400 which is depreciated in equal installment in 2 yr. Assume that the tax rate is 50% and the interest rate is 10%. The net present value of the tax that the company would have saved if it had depreciated $\frac{2}{3}$ rd of investment in the first yr and rest in the second yr is ?

$$\text{Ans } \frac{2}{3} \times 36400$$



amt of tax saved

$$P = \frac{3035}{1+i} - \left(\frac{3035}{(1+i)^2} \right)$$

$$= 250.826$$

Step before Plant
Payback
after
Break even pt.

(Retn)

Break even - point :-

Break even point is defined as the point where the total pmt cost equals total annual sale, Here total pmt cost means total annualised cost

$$PBT = I - E$$

$$TP = PBT - Dep$$

$$= I - E - Dep$$

$$0 = TP = I - (TAC)$$

$$\boxed{I = TAC} \quad (\text{Break even pt})$$

$$\text{Total Sale} \leftarrow \underbrace{x \cdot n}_{\substack{\downarrow \\ \text{selling price}}} = \underbrace{y \cdot n + \text{Fixed Cost}}_{\substack{\downarrow \\ \text{cost price} \quad \downarrow \\ \text{Depreciation}}} \text{Total cost}$$

Q1) The annual direct portion cost for a plant operating at 70% capacity are 2.80L. while the sum of annual fix charges and other expenses is 2L. What is the breakeven pt in units of prodⁿ per yr. If total annual sales are 5.60L and prod sales at Rs 40/unit.

$$n = \frac{560000}{40} \quad \frac{\text{Total Sale}}{\text{sell price.}}$$

$$= 14000$$

$$C.P. = \frac{280000}{14000} = 20 \text{ ₹}$$

$$40n = 20n + 2L$$

$$20n = 2L$$

$$n = 10,000 =$$

Q2) for some data, what were the annual Gross earning and the net profit of this plant at 100% capacity when the tax is required 15% of 1st 50000, 25% on 50000-70000 and 34% of above 75k. and 5% of the gross earning from 1L to 3.35L. Calculate?

When Capacity units.

70% 14000

100% $\frac{14000}{0.7}$

$$\text{Gross Annual Earning} = GAE = 40 \left(\frac{14000}{0.7} \right) - \left(20 \left(\frac{14000}{0.7} \right) + 2L \right)$$

$$= \underline{592000} \quad 2L$$

$$15\% \text{ on } 50000 = 7500$$

$$25\% \text{ on } 25000 = 6250$$

$$34\% \text{ on } 125000 = 42500$$

$$5\% \text{ of } 1\text{L} = 50,000$$

1. GAE = 22L.

1st tax is paid
once more than 1L

20 L =

$$\text{Tax paid} = 15\% \text{ of } (50000) + 25\% \text{ of } (25000) + 34\% \text{ of } (1.25\text{L}) \\ + 5\% \text{ of } (1\text{L})$$

$$= 61250$$

$$\text{Net Profit} = 2\text{L} - 61250$$

Alternative Investment:-

Design	1	2	3	4
Total Initial Installed cost	10,000	16,000	20,000	26,000
Operating Cost per year	100	100	100	100
Fixed charge (% of initial cost per year)	20	20	20	20
Value of heat saved	4100	6000	6900	8850

Owner demand min of 10% turnover.

$$\text{ROR}_1 = \frac{4100 - (100 + 2000)}{10000}$$

$$= 0.2 = 20\%$$

$$\text{ROR}_2 = \frac{6000 - (100 + 3200)}{16000} = 0.2437 = 24.37\%$$

(20% of 16000)
16.8%
~~24.37%~~

$$ROR_3 = \frac{6900 - (100 + \overset{4000}{\cancel{1000}})}{20000} \approx 0.14$$

$$ROR_4 = \frac{8850 - (100 + 5200)}{26000} \approx 0.1365 \approx 13.65\%$$

1 & 2

$$\frac{2700 - 2000}{16000 - 10000} = \frac{700}{6000} \approx 11.66\%$$

2 is good.

2 & 3

$$\frac{2800 - 2700}{20000 - 16000} = \frac{100}{4000} \approx 2.5\%$$

2 is good.

2 & 4

$$\frac{3550 - 2700}{26000 - 16000} = \frac{850}{10000} \approx 8.5\%$$

2 is good.

Sep 15, 14

Optimisation

1. Find the optimisation Variable? (x)
2. Identify the optimisation function? (f) Cost/profit

$$f = g(x)$$

$$3. \frac{df}{dx} = 0$$

Q. Obtain the optimal diameter of a cylindrical storage vessel of volume V . The curved shell cost $R_s C_s \text{ ₹/m}^2$ and the flat top-end bottom plate $R_s C_p \text{ ₹/m}^2$

Solⁿoptimisation variable = d optimisation function $f = 2\pi d^2 h = \dots$

$$A = 2\pi d^2 + 2\pi d h$$

$$\text{Total cost} = 2\pi d^2 C_p + 2\pi d h C_s$$

$$V = \pi d^2 h$$

$$h = \frac{V}{\pi d^2}$$

$$dTC = 2\pi d^2 C_p + 2\pi d \frac{V}{\pi d^2} C_s$$

$$= 2\pi \frac{d^2}{4} C_p + \frac{2V}{d} C_s$$

$$\frac{dTC}{dd} = \frac{2\pi C_p \cdot 2d}{4} + \frac{2(-1)V C_s}{d^2}$$

$$\frac{dTC}{dd} = \frac{\pi}{2} C_p - \frac{2V C_s}{d^2}$$

$$\pi C_p d = \frac{4V C_s}{d}$$

$$d = \left(\frac{4V C_s}{\pi C_p} \right)^{1/3}$$

2) A plant manufacture compressor at the rate of n units per day. The daily fixed charges are 20,000 ₹/daily. and the variable cost per compressor is $500 + 0.2N^{1.3}$ ₹/compressor. Selling Price per compressor is Rs 1000, ₹/compressor. The no. of compressor to be manufactured in order to maximise the daily profit is ?

$$F.C = 20000 \text{ ₹/daily.}$$

$$V.C = 500 + 0.2 N^{1.3} \text{ ₹/compressor.}$$

$$S.P = 1000 \text{ ₹/compressor}$$

No of units manufactured per day = N units/day.

$$\text{Profit} = P_e - E$$

$$= \left\{ 1000 \text{ ₹/compressor} \times N \frac{\text{compressor}}{\text{day}} \right\} - 20,000 - (500 + 0.2N^{1.3})N$$

$$P = N \times 1000 - 20000 - 500N - 0.2N^{2.3}$$

$$= 500N - 20,000 - 0.2N^{2.3}$$

$$\frac{dP}{dN} = 500 - 0.2 \times 2.3 N^{1.3}$$

$$= 500 - 0.46 N^{1.3}$$

$$500 = 0.46 N^{1.3}$$

$$N^{1.3} = 1086.956$$

2) A plant produces phenol. The V.C is Rs/tonn of phenol is related to the plant capacity, P (tonn/day) as $45000 + 5P$. The fixed charges are 1L/day. The SP of phenol is Rs 50,000/tonn. Find the optimal plant capacity for minimum cost per tonn/phenol.

$$VC = (45000 + SP) \text{ ₹/ton}$$

$$P = \text{ton/day}$$

$$SP = 50000 \text{ ₹/tonn}$$

$$FC = 10^5 \text{ ₹/day}$$

$$\text{Cost function} = VC + FC =$$

$$= (45000 + SP) + 10^5 \text{ ₹/day} \times \frac{1}{P} \frac{\text{day}}{\text{ton}}$$

$$= 45000 + SP + \frac{10^5}{P}$$

$$\frac{d(CF)}{dP} = 5 + \frac{10^5(-1)}{P^2}$$

$$= 5 - \frac{10^5}{P^2}$$

$$- \frac{2 \cdot 10^5}{P^3}$$

$$5 = \frac{10^5}{P^2}$$

$$P^2 = 20,000$$

$$P = \pm 141.42 \text{ tonn/day}$$

$$\text{Profit} = 50000 \text{ ₹/tonn} \cdot P (\text{ton/day})$$

$$- 10^5 - (45000 + SP) P$$

$$= 50000 P - 45000 P - SP^2 - 10^5$$

Find max^m daily profit

Q) Find the break even capacity.

$$50000 P = (45000 + SP + \frac{10^5}{P}) P$$

$$51641.4218 \text{ A}$$

$$\boxed{P = 20}$$

Q) Due to a 20% drop in the pelt & selling price, the pay back period of a new plant increased to 1.5 times that initiated estimated initially. Production cost & Production rate remains unchanged, if production CP is the the new SP is C_s . Then find the ratio of C_p by C_s

$$t = \frac{\text{FCI}}{CF} \cdot \frac{1}{\text{Profit}}$$

20%
 $CF = I - E$

$$t_1 = \frac{I}{SP - C_p}$$

$$t_1 = \frac{I}{X - C_p} \quad \text{--- (1)}$$

$$t_2 = \frac{I}{C_s - C_p} \quad \text{--- (2)}$$

$$t_2 = 1.5 t_1$$

$$1/2$$

$$\frac{t_1}{1.5 t_1} = \frac{\frac{I}{X - C_p}}{\frac{I}{C_s - C_p}}$$

$$X - 0.2X = C_s$$

$$0.8X = C_s$$

$$X = \frac{C_s}{0.8}$$

$$0.666 = \frac{C_s - C_p}{\frac{C_s}{0.8} - C_p} = \frac{(C_s - C_p) 0.8}{C_s - 0.8 C_p}$$

$$0.8333 (C_s - 0.8 C_p) = C_s - C_p$$

$$2 C_p = 0.666 C_s$$

$$\frac{C_p}{C_s} = 0.5 =$$

Q. A batch reactor produces 10^5 kg of a pdt. per year. The total batch time in hrs of the reactor is $k\sqrt{P_B}$ where P_B is, pdt/batch (kg) & k is $1.0 \text{ hr}/\sqrt{\text{kg}}$. The operating cost of the reactor is Rs 200/hr. The total annual fix charges are Rs $340 P_B$ and annual raw material cost is Rs 2 million. The optimum size in kg of each batch is.

$$t = k\sqrt{P_B} \quad \frac{\text{pdt}}{\text{batch (kg)}} \quad \left\{ \begin{array}{l} = P_B \\ T.P = 10^5 \text{ kg/yr} \\ t = 0.1 \frac{\text{hr}}{\sqrt{P_B}} \cdot P \end{array} \right.$$

$$\text{Op. Cost} = 200 \text{ ₹/hr}$$

Solⁿ

$$\text{Total prod}^n = 10^5 \text{ kg/yr}$$

$$t_B = k\sqrt{P_B} \text{ hr}$$

$$P_B = \frac{\text{kg of Pdt}}{\text{Batch}}$$

$$\text{Op Cost} = 200 \text{ ₹/hr}$$

$$\text{Fixed charges} = 340 P_B \text{ ₹/yr}$$

$$\text{Raw Material Cost} = 2 \times 10^6 \text{ ₹/yr.}$$

$$T.C = 340 P_B + 2 \times 10^6 + 200 \text{ ₹/hr} \times 1.0 \sqrt{P_B} \times \frac{10^5 \text{ kg/yr}}{P_B \text{ kg/batch}}$$

$$= 340 P_B + 2 \times 10^6 + 2 \times 10^7 \frac{1}{\sqrt{P_B}}$$

$$= 340 + 2 \times 10^7 \left(-\frac{1}{2}\right) \frac{1}{(P_B)^{3/2}}$$

$$340 = \frac{10^7}{(P_B)^{3/2}}$$

$$(P_B)^{3/2} = \frac{10^7}{340}$$

$$P_B = 952.82 \frac{\text{kg of Pdt}}{\text{Batch}}$$

$$\frac{d(T.C)}{dP_B} = 340 + 200 \text{ ₹/hr} \cdot 0.1 \frac{1}{\sqrt{P_B}}$$

$$= 340 + 20 \left(-\frac{1}{2\sqrt{P_B}}\right)$$

$$340 = \frac{100}{\sqrt{P_B}} \times 10^5$$

$$\sqrt{P_B} = \frac{100}{340}$$

$$P_B = 8.65 \times 10^{-4}$$

$$184390.88$$

Cost Index : — $\frac{\text{cost}}{\text{area} \times \text{cost}}$

It is an index value which relates the cost of equipment at a certain tym, w.r.t the cost of equipment at certain basic tym

Marshall & Swift

$$\frac{(\text{Cost of the Equipment})_{Y_1}}{(\text{Cost of the Equipment})_{Y_2}} = \frac{\text{Cost Index of Year } Y_1}{\text{" " " " } Y_2}$$

Q) The cost of a distillation tower in the year 2000 is Rs x find the cost of the distillation column in year 2004 if the cost index for the year 2000 & 2004 are 480 & 520 resp.

$$\frac{x}{y} = \frac{480}{520}$$

$$x = 0.92 y$$

$$y = 1.08 x$$

Cost Capacity Rule / Six-tenth Rule : —

year cost.
Capacity

$$\frac{(\text{Cost of the Equipment})_{Y_1}}{(\text{" " " " } Y_2)} = \left(\frac{\text{Capacity } C_1}{\text{Capacity } C_2} \right)^{6/10}$$

Q) The cost of a drum dryer is 2 million ₹, what is the cost of the drum dryer with double the surface area.

$$\frac{2}{x} = \left(\frac{1}{2} \right)^{6/10}$$

$$x = 3 \text{ million ₹}$$

Q. Purchase of H.E of 20m^2 area was $5,00,000 \text{ ₹}$ in 2006. What will be the estimated cost of a similar H.E of 50m^2 area in yr 2013. The cost index 2006 & 2013 are 430.2 & 512.6

$$\frac{5,00,000}{n} = \frac{430.2}{512.6} = \frac{20}{50}$$

$$n = 22$$

5L — 2006 — 20m^2

cost — 2013 — 20m^2

5,95,769.40 — 2013 — 20m^2

cost — 2013 — 50m^2

10,45,00,000

Lang Multiplication Factor :-

Type of Plant	Factor for fixed solid Capital Investment	Factor for T.C.I
Solid Processing Plant	3.9	4.6
Solid-Fluid Processing Plant	4.1	4.9
Fluid-Processing Plant	4.8	5.7

Q.7 For a solid processing plant, the delivered equipment cost is 10L ₹. Using Lang multiplication factor approximate the fixed capital & total capital

FCI

or = Factor \times Delivered Equipment Cost.

TCI

$$F.C.I = 3.9 \times 10L$$

$$= 39L$$

$$T.C.I = 4.6 \times 10L$$

$$= 46L.$$

Q.8 The heat integration is planned in a process plant at an investment of Rs 2 million. This would result in net energy saving of 20 GJ/year. If the nominal rate of interest is 15% and the plant life is 3yr. Then the break even cost of energy in Rs/GJ is?

$$R = \frac{P i (1+i)^n}{(1+i)^n - 1} = n \frac{\text{₹}}{\text{GJ}} \times \frac{20 \text{ GJ}}{\text{yr.}}$$

Design of cylindrical & Spherical Vessels:—

Cylindrical & spherical vessels may be the thin wall or thick wall vessels, depending upon the opr. temp & press. range.

The thin wall vessels are those vessels in which thickness to diameter ratio is less than 0.1

Let a cylindrical vessel of length L , diameter d & thickness t is subjected to an internal pressure P . This will cause ~~cause~~ Two type Longitudinal stress (σ_L) and tangential stress (σ_θ)

$$\sigma_L = \frac{PD}{4t} \quad , \quad \sigma_\theta = \frac{PD}{2t}$$

$$\boxed{\sigma_\theta = 2\sigma_L}$$

For spherical vessel,

$$\sigma_L = \frac{PD}{4t} \quad , \quad \sigma_\theta = \frac{PD}{4t}$$

$$\boxed{\sigma_L = \sigma_\theta}$$

for conical vessel,

$$\sigma_L = \frac{Pr}{2t \cos \alpha} \quad \sigma_\theta = \frac{Pr}{t \cos \alpha}$$

$$\boxed{\sigma_\theta = 2\sigma_L}$$

Bcz of the shape of the sphere, it undergoes minimum stress and therefore the minm absolute stress value.

$$\sigma_{min} = \frac{PD}{4t}$$

The calculation of thickness for cylindrical vessel.

$$t = \frac{PD_o}{2fJ + P}$$

P = Design Pressure, which is 5% more than the maxm operating pressure of the vessel.

D_o = Outer dia or nominal dia.

f = Maxm allowable stress value, that a material can handle.

J = Joint efficiency factor,

general value of $J = 0.85$.

t = Calculated wall thickness.

$$= t + C \cdot A$$

The actual wall thickness equals to calculated wall thickness plus corrosion allowance. CA is generally 2mm

Standard Wall thickness

The next integer to the actual wall thickness

Q → A process vessel is to be designed for the maxm operating pressure of 500 kN/m^2 . The vessel has the nominal dia has 1.2 m . The maxm allowable stress value 118 MN/m^2 . What will std. plate thickness to fabricate the cylindrical vessel.

5% more press = S_{25} (5, 7, 9, 11)

$$t = \frac{500 \times 1.2}{2 \times 118 \times 10^3 \times 0.85 + 500}$$

6

$$P = \frac{2ft}{D_o - t}$$

For spherical Vessel:—

$$t = \frac{PD_o}{4f + P}$$

$$P = \frac{4ft}{D_o - t}$$

Q → if a spherical vessel having the same dia & thickness is fabricated with the same quality steel. What max int. press. the sphere will withstand safely.

$t = 5$

$$= \frac{4 \times 118 \times 0.85 \times 5}{1.2 - 5}$$

$$P = 1.6$$

Heads & Closures

Heads of cylindrical vessels are to be closed before putting them into operation. This is done by means of heads & closures.

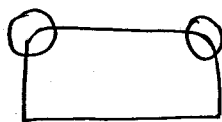
Flat heads:-

Generally used for man holes in low pressure vessels.

They can also be used as closures for small diameter vessels under low pressure.

Flanged only heads:-

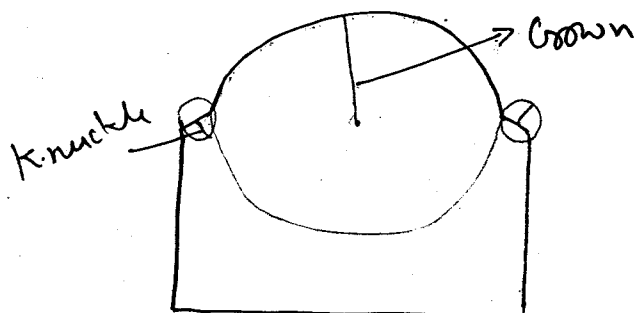
It is a type of flat head in which gradual change in shape at the corner is there.



This head is used to close the ends of horizontal storage vessel at atm. pressure.

Flanged Shallow Dished & Flanged Standard Dished:-

These two are also known as torispherical head.



If the crown radius is greater than the shell outside diameter the head is known as Flanged Shallow dished.

The crown radius is equal to or less than the shell outside diameter the head is known as Flanged standard Dished.

For designing pt of view,

$$\frac{r_k}{r_c} \geq 0.6$$

These types of heads are used for vertical process vessel for low pressure.

Ellipsoidal head:-

For this case

$$r_k = r_c$$

Cheapest

They are used for the vertical process vessel operating at high pressures and they are most economical heads available for vessel under high pressure.

Hemi-spherical head:-



For a given thickness, this type of head is the strongest among all.

This is the most expensive head and widely use for high pressure vessel.

Conical head or Reducers

They are used as bottoms for evaporators, crystallizers etc. Advantage lies in the fact they allow accumulation & removal of solids from such equipment.

They provide a smooth transition b/w two parts of different dia in cylindrical process vessel.

Supports for Process Vessel

A process vessel is usually supported in a vertical or in horizontal position depending upon the process requirement.

Distillation column is supported in vertical position.

Heat Exchanger " " " horizontal "

For vertical vessel the common supports are.

1) Skirt Support $\begin{cases} \rightarrow \text{cylindrical} \\ \rightarrow \text{conical} \end{cases}$

2) Lug Support / Bracket

3) Leg Support.

4) Ring Support

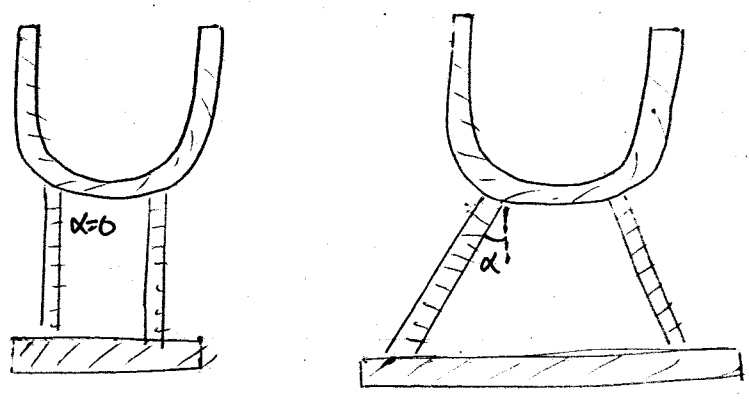
For horizontal vessel the common supports are

1) Saddle Support

2) Ring "

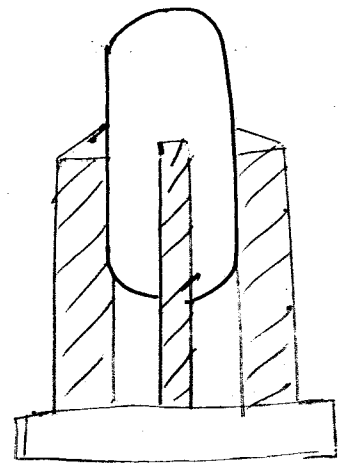
3) Leg "

Skirt Support



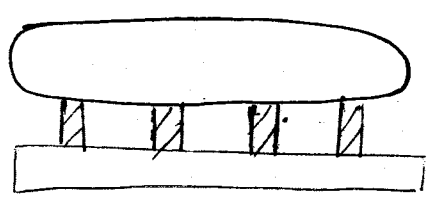
These support are found to be most suitable for taller vessel and they are also useful for the vessels subjected to major loading

Lug Support or Bracket Support.



They are used to support vertical vessels having smaller height or the vessels which are subjected to minor loading

Saddle Support



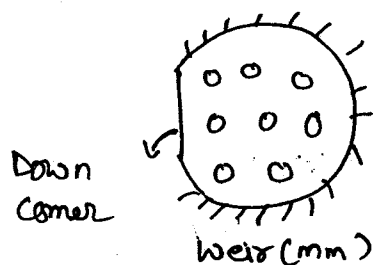
They are used for generally thick wall vessel, the no. saddle should be 3 or more, for thin walled vessels the saddles are provided at the points near the ends of vessels.

Contactors:-

They are basically plate or tray contactors.

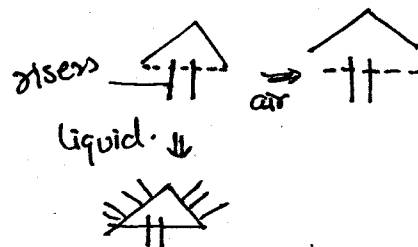
Cross flow plates are the most common type of plate contactor used in the distillation column. They are of 3 types:-

i) Sieve tray:-



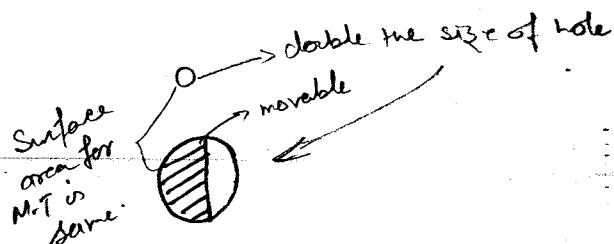
The simplest type of cross flow plates are the sieve plates. The vapour passes up through the perforations and the liquid is retained on the plate by the vapour flow,

ii) Bubble Cap:-



These are the plates in which the vapour passes up through ~~perforations~~ short pipes called as risers, covered by a movable cap. The use of cap ensure that a level of liquid is maintained on the tray at all vapour flow rates.

Valve tray:—



Valve plates are essentially the sieve plates with large dia. holes covered by moveable flaps which lifts as the vapour flow increases. As the area for the vapour flow varies wid the flow rate the whole valve plates can operate at wider range of flow rate as compared to sieve plates.

Summary:—

The sieve plates are the cheapest and least prone to falling fouling and are satisfactory for most applications. The moving valve plates should be considered when vapour flow rate vary. Their cost is more than the sieve but they have increased performance. The bubble cap should only be used where very low vapour rates have to be handled as they are the most expensive and most prone to fouling.

Packing Vs Tray

The plate columns can be designed to handle a wider range of liquid-gas flow rates than packed column as the packed column are not suitable or very low liquid rate.

The efficiency of a plate can be predicted wid more accuracy in comparison to packing.

In the tray column it is easy to make provision for the withdrawal of side stream.

Petroleum refinery, different section of distillation column

It is easier to make a provision for cooling and cleaning at different section.

For the corrosive liquid packed column are used, bez packing is cheaper than the tray.

For the liquids containing some solid particles, it is easier to make provision for cleaning in plate column.

The pressure drop is lower for the packing than the plates.

Packed column are most suitable for handling foaming system, bez there is a continuous contact system in the packing in comparison to plate columns, in which there is discrete contact system.

The packed columns are favourable for small diameter vessels in which it is difficult to make provision for the tray.

Pumps & Compressor: —

Centrifugal pump & Reciprocating pump.

Selection of pump based on the criteria of total head & total flow rate.

Specific speed of the centrifugal pump & based on the sp. speed selection of pump.

Pressure drop in a pipe line.

Net positive suction head / Cavitation.

Storage & transport.

→ gases
→ liquids.