



# Workshop 3

COMP90051 Machine Learning  
Semester 1, 2021

# Learning outcomes

At the end of this workshop you should:

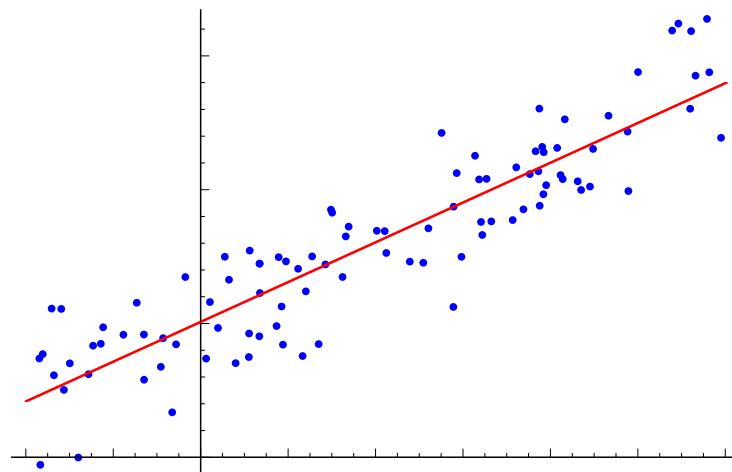
- be able to implement **linear regression** using numerical linear algebra functions
- be familiar with the **scikit-learn interface** for linear regression
- be able to implement **polynomial regression**
- be able to explain the **benefits/drawbacks** of linear regression versus polynomial regression

# Quick review: linear regression

Assume the response  $y$  is a *linear* function of the features  $\mathbf{x} = [x_1, \dots, x_m]^T$ :

$$y = w_0 + \sum_{i=1}^m w_i \cdot x_i$$

Write this more compactly as  $y = \mathbf{x}^T \mathbf{w}$  by redefining  $\mathbf{x} = [x_0, x_1, \dots, x_m]^T$  with  $x_0 = 1$  and defining  $\mathbf{w} = [w_0, \dots, w_m]^T$



**Question:** How do we choose the weights?

# Quick review: linear regression

## Decision theoretic view

Make decision that minimises the empirical risk

$$\hat{R} = \frac{1}{n} \sum_{i=1}^n L(y_i, \hat{y}_i)$$

and choose the square loss  
 $L(y, \hat{y}) = (\hat{y} - y)^2$ .

Optimal decision for  $\mathbf{w}$   
minimises the sum-squared error.

## Probabilistic view

Assume

$$y|\mathbf{x}, \mathbf{w} \sim \mathcal{N}(\mathbf{x}^T \mathbf{w}; \sigma^2)$$

Can write down the likelihood for the observations

$$\begin{aligned} L(\mathbf{w}|\mathbf{X}, \mathbf{Y}) \\ = \prod_{i=1}^n p(y_i|\mathbf{x}_i, \mathbf{w}, \sigma) \end{aligned}$$

MLE for  $\mathbf{w}$  minimises the sum-squared error.

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