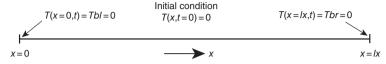
# Introduction to Finite Element Method TF4062

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### 1d Diffusion



#### Governing PDE

$$\frac{\partial T}{\partial t} = \kappa \frac{\partial^2 T}{\partial x^2} + H$$

Initial conditions:

$$T(x, t = 0) = 0 \ \forall x \in [0, L_x]$$

#### Boundary conditions:

$$T(x = 0, t) = 0$$
 and  $T(x = L_x, t) = 0$ 

## Discretized equations

$$\mathbf{L}\mathbf{T}^{n+1} = \mathbf{R}\mathbf{T}^n + \mathbf{F}$$

$$\mathbf{L} = rac{\mathbf{M}}{\Delta t} + \mathbf{K}$$

$$\mathbf{M} = \begin{bmatrix} \frac{\Delta x}{3} & \frac{\Delta x}{6} \\ \frac{\Delta x}{6} & \frac{\Delta x}{3} \end{bmatrix}$$

$$\mathbf{R} = rac{\mathbf{M}}{\Delta t}$$

## Stiffness matrix

$$\mathbf{K} = \kappa \begin{bmatrix} \frac{1}{\Delta x} & -\frac{1}{\Delta x} \\ -\frac{1}{\Delta x} & \frac{1}{\Delta x} \end{bmatrix}$$

## Load vector

$$\mathbf{F} = H \left[ \frac{\Delta x}{\frac{2}{\Delta x}} \right]$$

$$\mathbf{T} = \begin{bmatrix} T_1 \\ T_2 \end{bmatrix}$$

Sistem global (menggunakan matriks dan vektor global):

$$\tilde{\mathbf{L}}\tilde{\mathbf{T}}^{n+1} = \tilde{\mathbf{R}}\ \tilde{\mathbf{T}}^n + \tilde{\mathbf{F}} = \tilde{\mathbf{b}}$$