

SSY281 - Model Predictive Control

MA2_09

Lucas Rath

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Question 1 *Describe the closed-loop stability properties of an infinite-time LQ controller and a finite-time LQ controller in receding horizon.*

If the pair (A, B) is controllable and $Q, R \geq 0$, then the solution to the infinite horizon LQ control problem gives a stable closed-loop system.

On the other hand, stability of the closed-loop system is not guaranteed for the finite-time LQ controller in receding horizon since it is based on optimality over a finite horizon (optimality does not guarantee stability)

Question 2 *How can stability of a finite-time LQ controller in receding horizon be enforced?*

It is possible to enforce stability of a finite-time LQ controller in receding horizon by increasing the time-horizon to infinity. In practice, it can be increased until the solution converges to the solution of the infinite case.

Question 3 *Explain the main advantage of a DP solution of a finite-time LQ problem vs. the batch solution.*

Regardless of which version of the receding horizon controller we choose the two solutions are of course identical, however, the DP solution might be less computational expensive. Mainly, if the time-horizon is long enough, then the controller gain may converge to a constant value.