# Joint Modeling of Topics, Citations, and Topical Authority in Academic Corpora

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# Research Overview

#### Introduction



Michael I. Jordan

**Citation Indices** 

**Citations: 122,672** 

h-index: 138

Reinforcement Learning

2.76

Statistical Inference

10.29

Image Processing

0.14

Information Retrieval

0.10

Measure topical authority of academic researchers

#### Proposed Model

- Latent Topical-Authority Indexing (LTAI)
  - A Bayesian probabilistic model that discovers topic-specific authority of scholars
  - Uses paper contents and citation networks

#### Key Idea

Paper written by authors of high topical authority values by papers

High probability of being cited by papers of similar topic



Topic	RL	Statistical Inference	Image Processing	IR
Authority	2.76	10.29	0.14	0.10

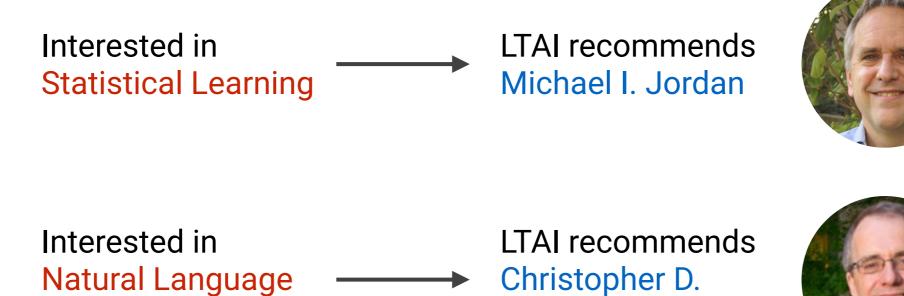
highly cited

less cited

#### Possible Applications

**Processing** 

- Recommending fine-grained authoritative researcher
  - ex ) Newly entering graduate student



Manning

- Finding academic papers from given topical interests
- Discovering research topics from academic corpus

### LTAI: Input & Output

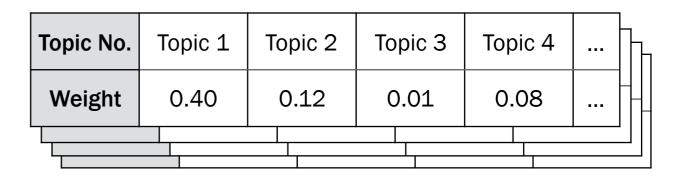
- Input
  - Paper content (text)
  - Authorship (author-paper link)
  - Citation network (paper-paper link)

- Output
  - Academic Topics (global)
  - Topic distribution (per paper)
  - Topical authority (per author)

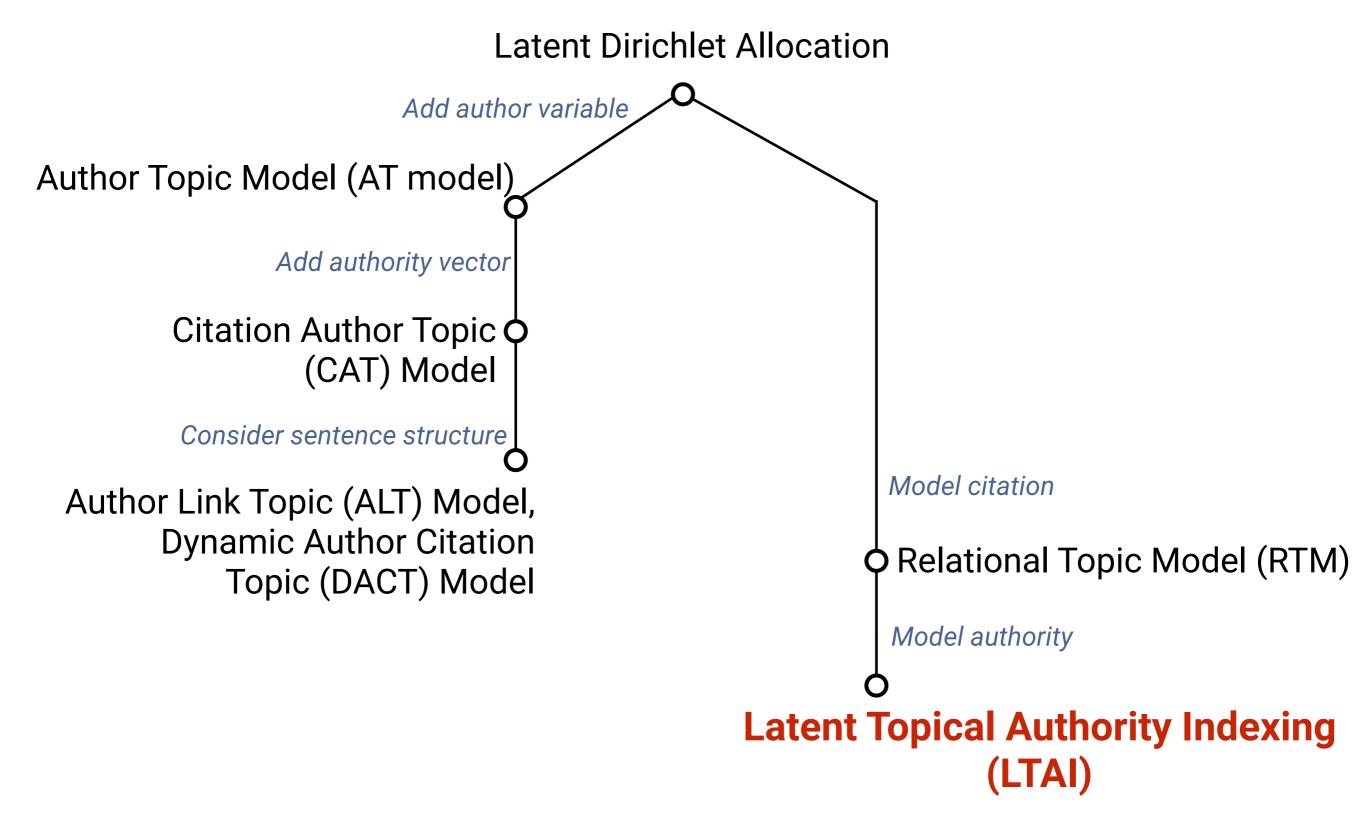
Topic No.	Hand-Tagged Labels	Top Frequent Words
Topic 1	Information Retrieval	information user document text retrieval web system content collection using
Topic 2	Image Processing	image object visual motion recognition model feature shape vision face
Topic 3	Distributed System	distributed system protocol group failure message fault recovery process asynchronous
Topic 4	Database	query database data transaction system rule view processing paper relational
	•••	

#### **Global Academic Topics**

Topic No.	Topic 1	Topic 2	Topic 3	Topic 4	    
Authority	3.82	9.58	1.27	0.32	

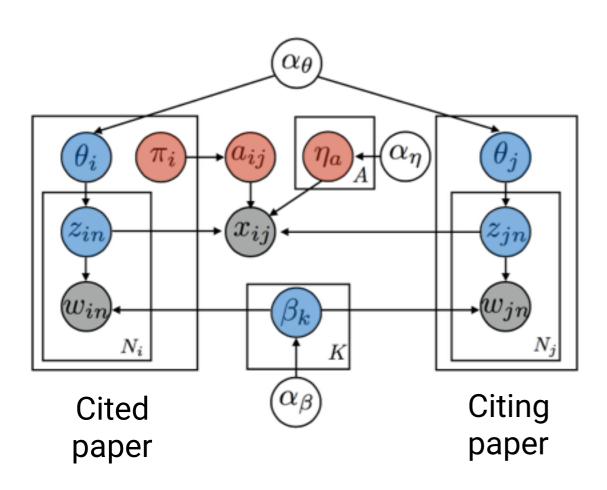


#### Related Work



# Model Description

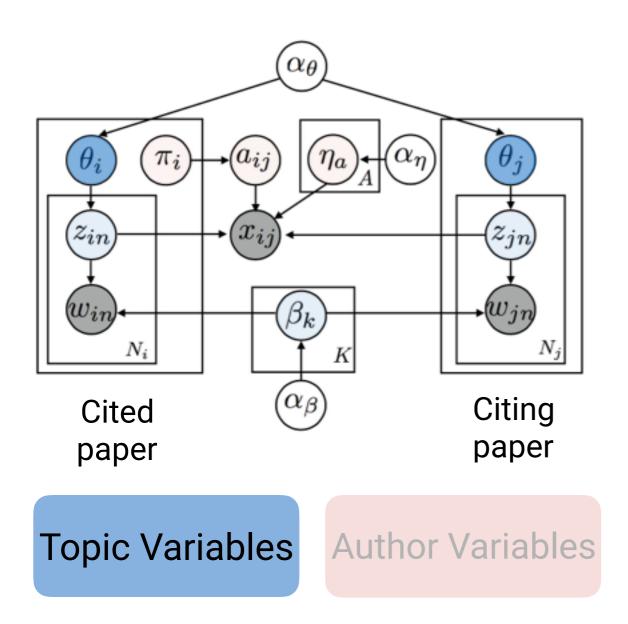
### Model Description: Full Graphical Model



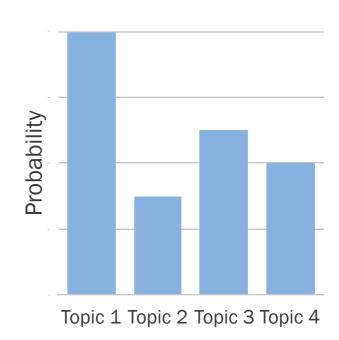
Topic Variables

**Author Variables** 

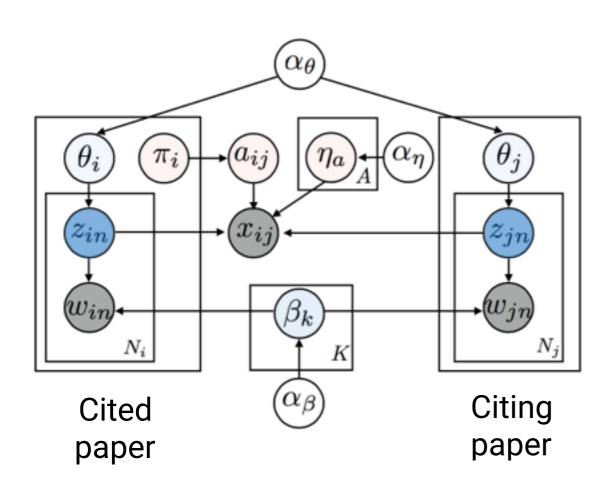
### Model Description: Topic Variables



- θ Document-Topic distributionK (# topics)-dimensional vector
- z Per-word topic indicator variable
- $\beta_k$  Topic-Word distribution V (vocab. size)-dimensional vector



### Model Description: Topic Variables

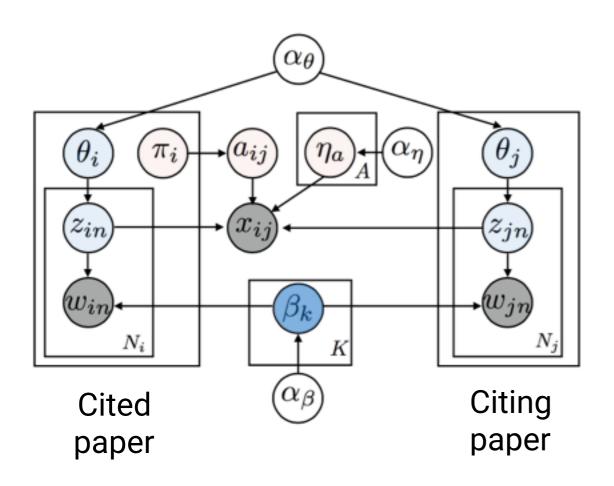


- θ Document-Topic distributionK (# topics)-dimensional vector
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- $\beta_k$  Topic-Word distribution V (vocab. size)-dimensional vector

**Topic Variables** 

**Author Variables** 

#### Model Description: Topic Variables



**Topic Variables** 

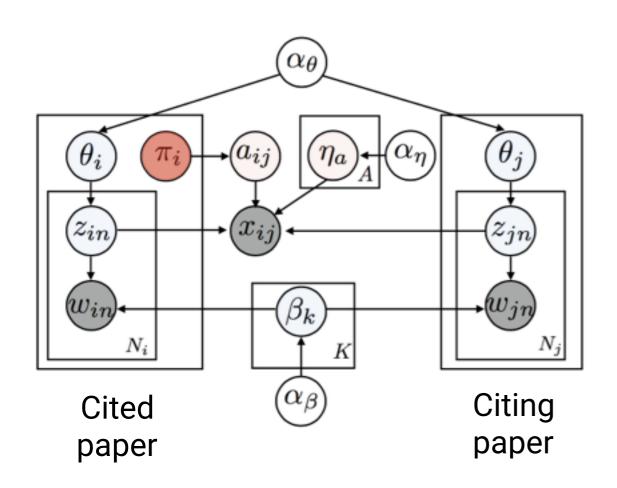
**Author Variables** 

- θ Document-Topic distributionK (# topics)-dimensional vector
- z Per-word topic indicator variable
- $\beta_k$  Topic-Word distribution V (vocab. size)-dimensional vector

Topic 1	Topic 2
machine	image
0.05	0.07
learning	pattern
0.04	0.02
probability 0.02	recognition 0.02
distribution	pixel
0.01	0.01
•••	

• • •

### Model Description: Author Variables



Topic Variables

**Author Variables** 

 $\pi_i$  Mixture weight over authors of publication i

Given to each cited paper

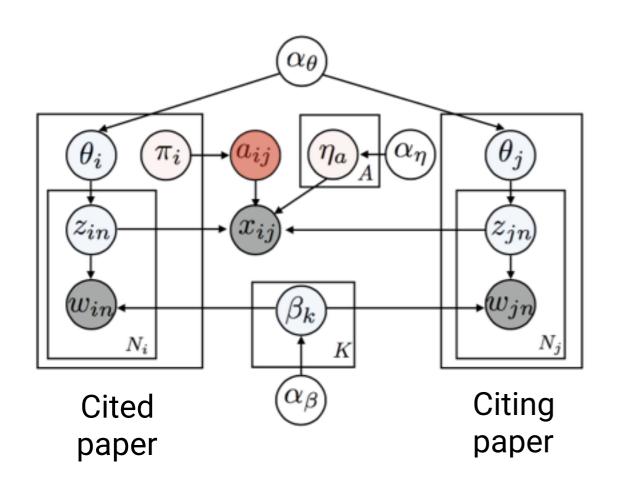
 $a_{ij}$  Selected author for cited paper i regarding citing paper j

depends on the mixture weight  $\pi_i$ 

 $\eta_a$  Authority variable

Given to each author K-dimensional vector

### Model Description: Author Variables



Topic Variables

**Author Variables** 

 $\pi_i$  Mixture weight over authors of publication i

Given to each cited paper

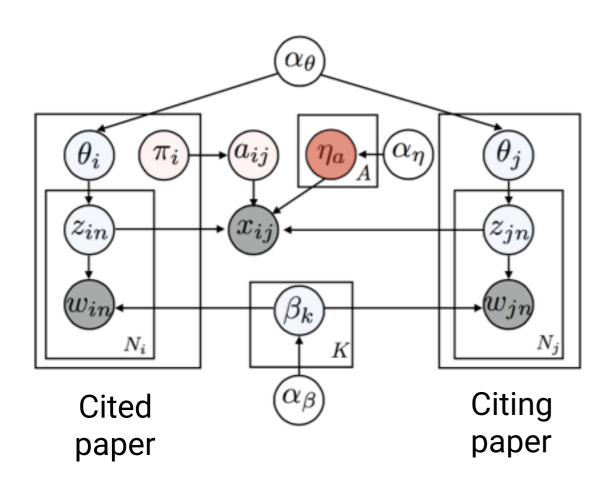
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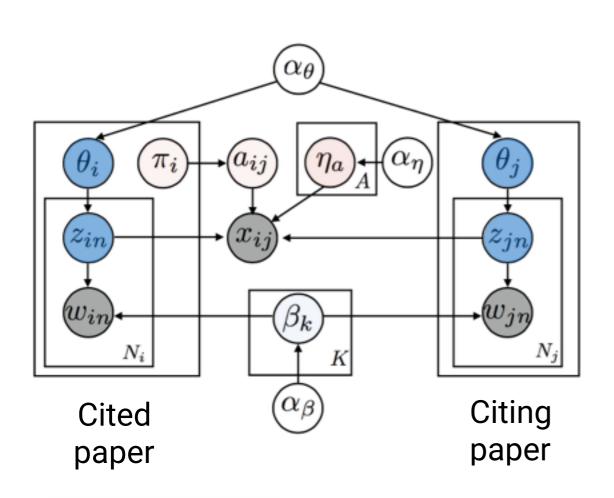
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depends on the mixture weight  $\pi_i$ 

 $\eta_a$  Authority variable

Given to each author K-dimensional vector

#### **Model Description: Citation Modeling**



$$p(x_{ij} = 1) =$$

$$p(i \leftarrow j = 1) \propto$$

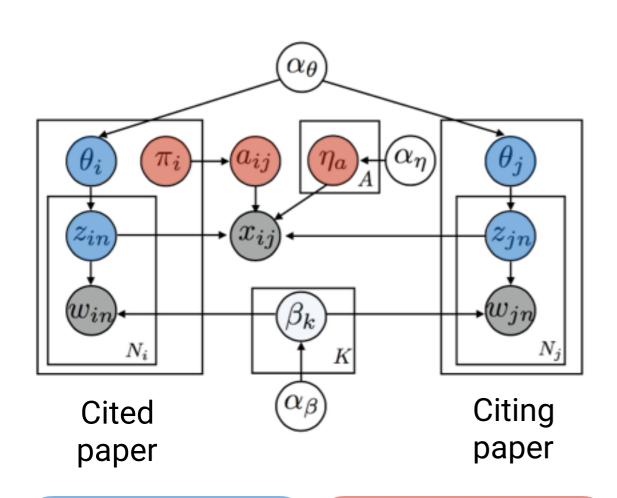
$$\overline{z_i}^{\intercal}\overline{z_j}$$

**Topic Similarity for Citation** 

Topic Variables

**Author Variables** 

#### **Model Description: Citation Modeling**



$$p(x_{ij} = 1) =$$

$$p(i \leftarrow j = 1) \propto$$

$$\overline{z_i}^{\mathsf{T}}\overline{z_j}$$

**Topic Similarity for Citation** 

Topic Variables

**Author Variables** 

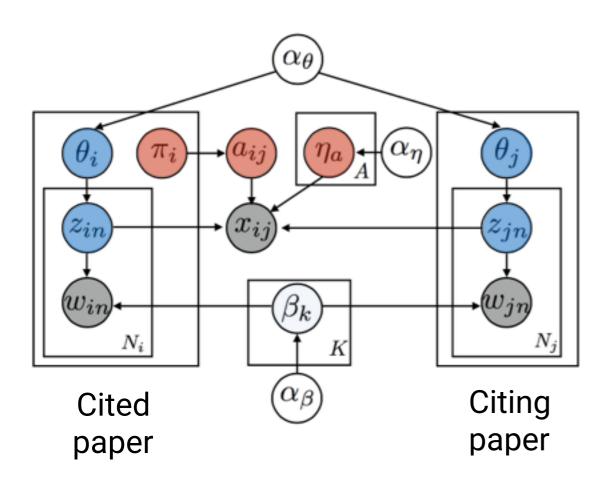
$$\overline{z_i}^{\mathsf{T}} diag(\eta_{a_{i\leftarrow j}}) \overline{z_j}$$

Adding Authority Variable

#### Model Description: Generative Process

- 1. For each topic  $k \in \{1, 2, ..., K\}$ , draw topic distribution  $\beta_k \sim \text{Dirichlet}(\alpha_\beta)$
- 2. For each document  $i \in \{1, 2, ..., D\}$ :
  - (a) Draw topic proportion:  $\theta_i \sim \text{Dirichlet}(\alpha_{\theta})$
  - (b) For each word token:  $n \in \{1, 2, ..., N_i\}$ :
    - i. Draw topic assignment:  $z_{in} \sim Mult(\theta_d)$
    - ii.Draw word token:  $w_{in} \sim Mult(\beta_{z_{in}})$
- 3. For each author a and topic k:
  - (a) Draw authority index of author a:  $\eta_{ak} \sim \mathcal{N}(0, \bar{\alpha_{\eta}}^{1}I)$
- 4. For each ordered document pair *i* and *j*:
  - (a) Draw influence proportion parameter: ~ Dirichlet(  $\pi_i$  )
  - (b) Draw one author from a set of authors of cited document  $i: a_{i \leftarrow j} \sim Mult(\pi_{i \leftarrow j})$
  - (c) Draw link from document j to document i:  $x_{i \leftarrow j} \sim \mathcal{N}(\overline{z_i}^\intercal diag(\eta_{a_{i \leftarrow j}}) \overline{z_j}, c_{i \leftarrow j}^{-1})$

#### **Model Inference**



Topic Variables

**Author Variables** 

#### Topic Variables

- Tracking exact posterior distribution: Infeasible
- Stochastic Variational Inference
  - Create approximate posterior distribution

#### Author Variables

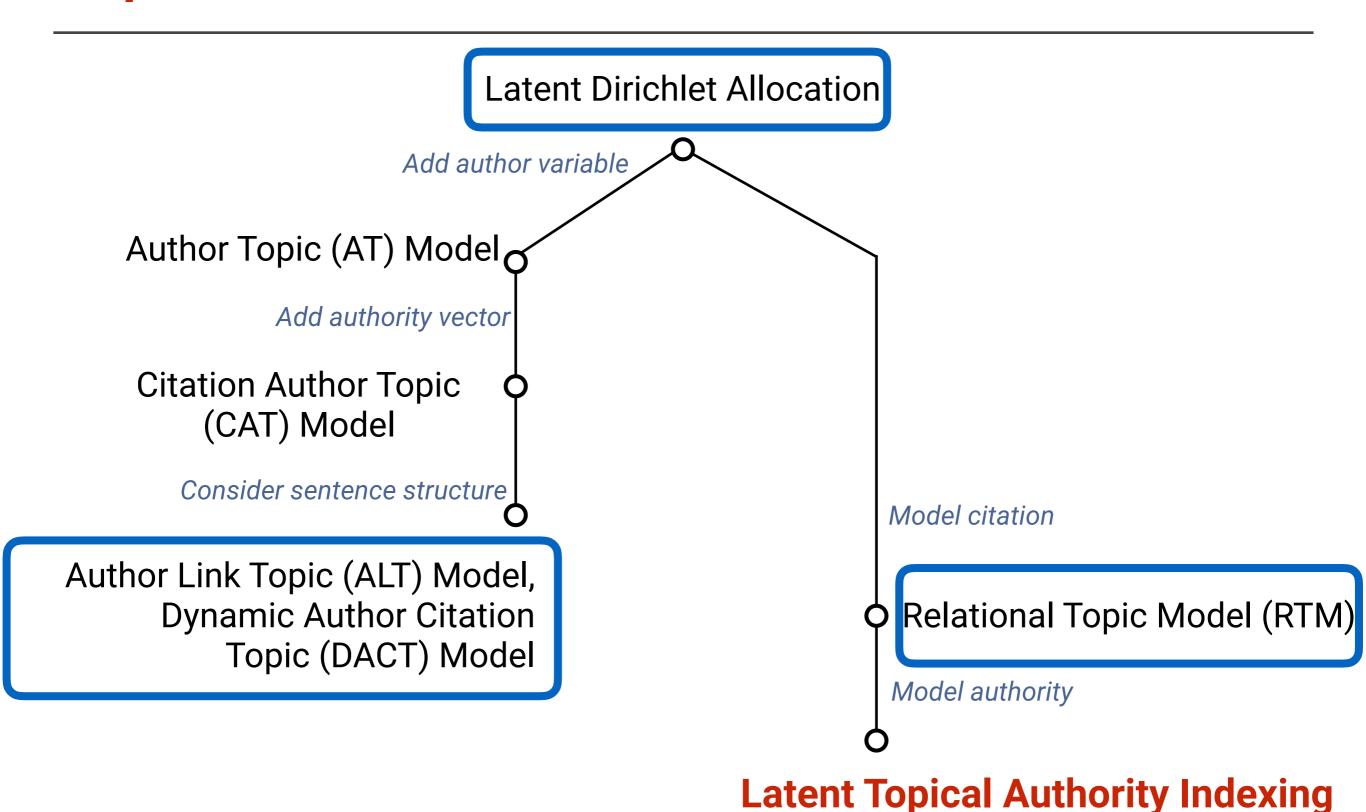
- EM approach
  - Fix topic variables
  - Take gradient of the model likelihood with respect to eta
  - Fix eta and reassign values with respect to pi
  - Subsample the negative links

# Experiments

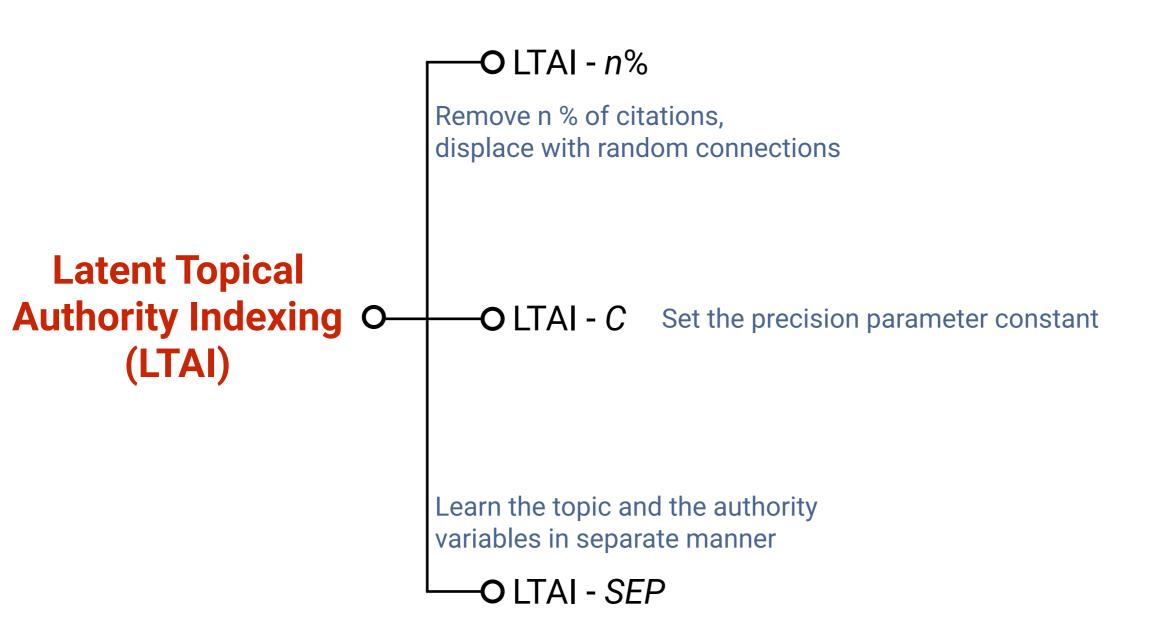
# **Experiments: Dataset**

	# Tokens	# Docs	# Authors	Avg. citation / Doc	Avg. citation /Author
CORA	17,059	13,147	12,111	3.46	12.17
arXiv-Physics	49,807	27,770	10,950	12.70	67.93
PNAS	39,664	31,054	9,862	1.57	13.18
Citeseer	21,223	4,255	6,384	1.24	4.38

#### **Experiments: Related Models**



#### **Experiments: Related Models**



### **Experiments: Model Comparison**

	Unified Model	Authority	Using cited contents	No sentence structure required
RTM	0	X	0	0
ALTM	0	0	X	0
DACTM	0	0	X	X
LTAI-n%	0	0	0	0
LTAI-C	0	0	O	0
LTAI-SEP	X	Ο	О	O
LTAI	0	0	0	0

#### **Experiments: Evaluation Metric**

Mean Reciprocal Rank (MRR) = 1/(harmonic rank)

$$MRR = \frac{1}{|Q|} \sum_{i=1}^{|Q|} \frac{1}{rank_i}$$

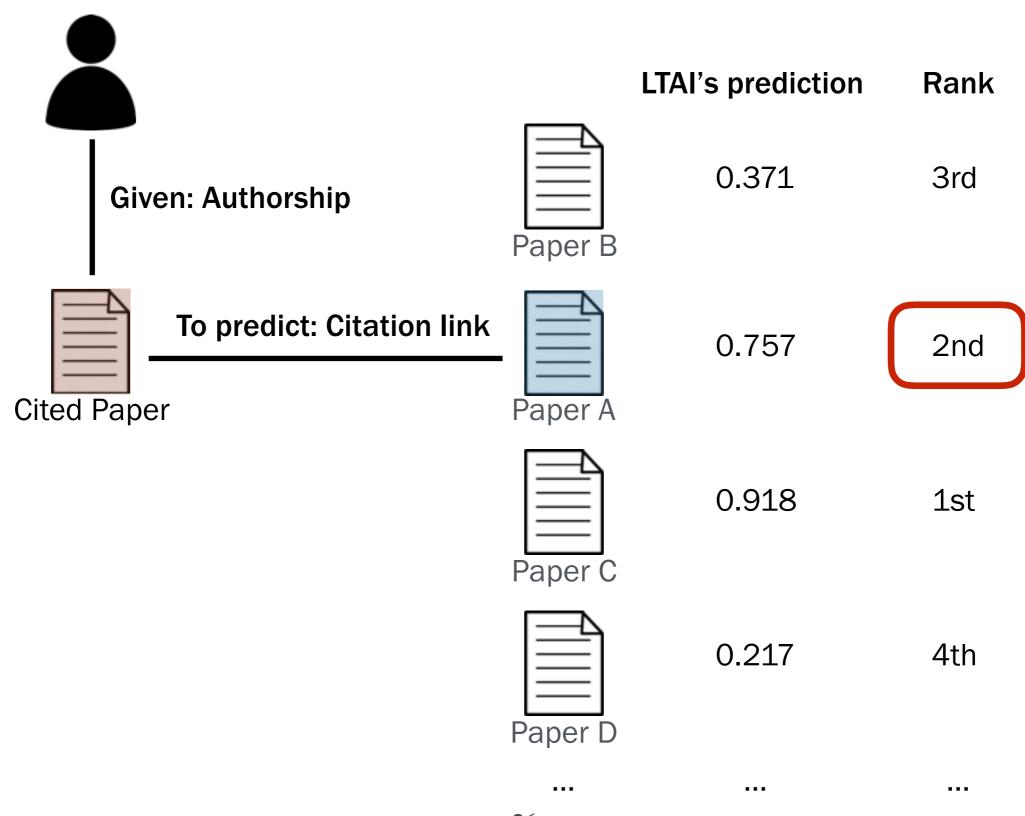
For author, citation prediction

Word predictive probability

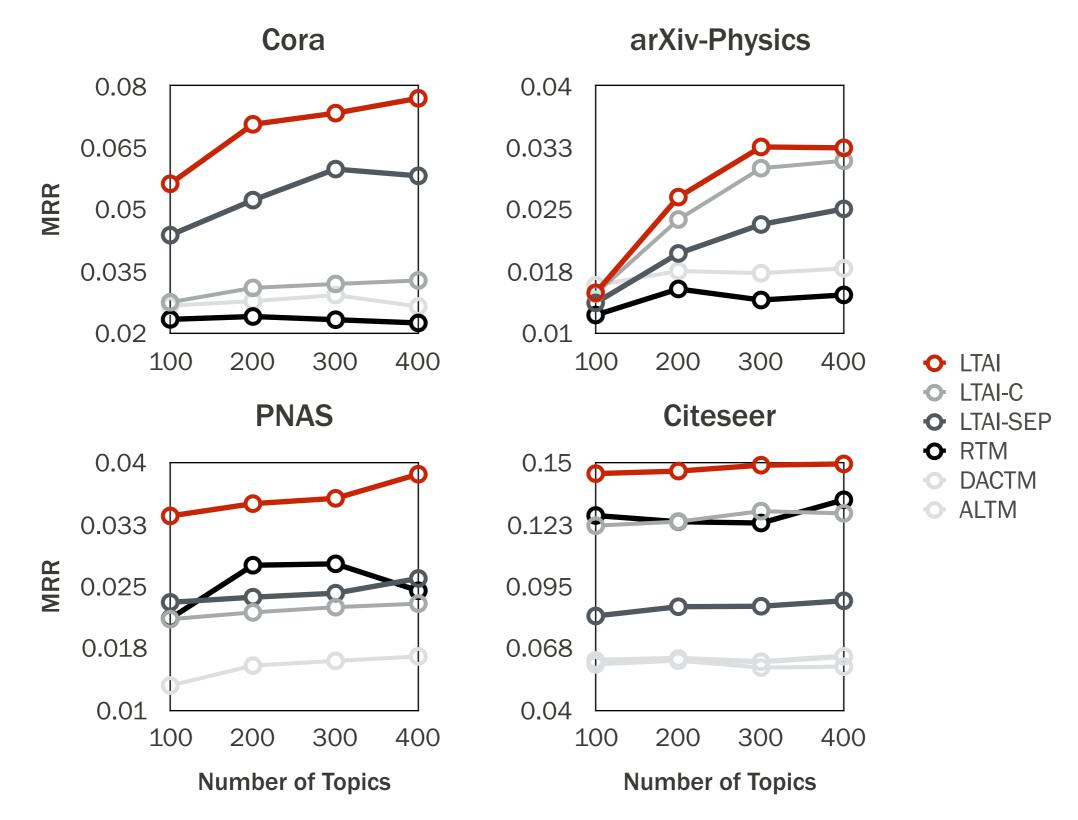
$$p(w_{new}|\mathcal{D}_{train}, w_{obs}) = \sum_{k=1}^{K} \mathbb{E}_q[\theta_k] \mathbb{E}_q[\beta_{k,w_{new}}]$$

For word prediction

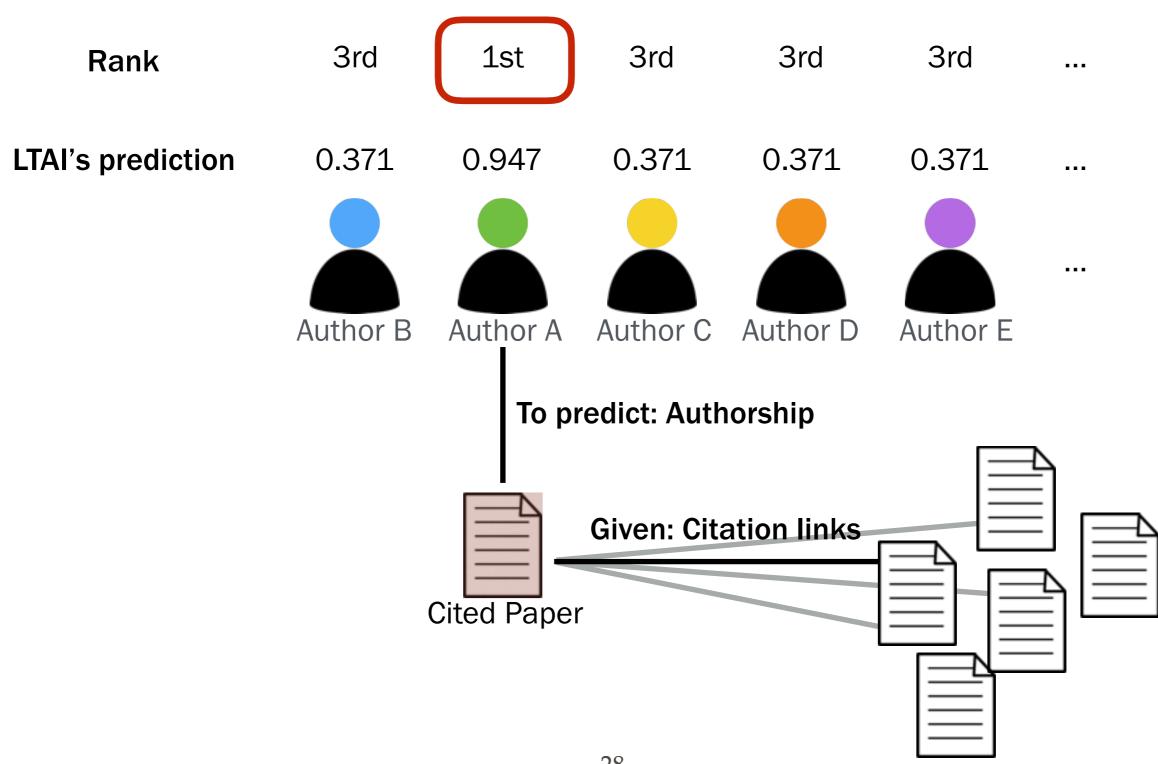
### **Experiments: Citation Prediction**



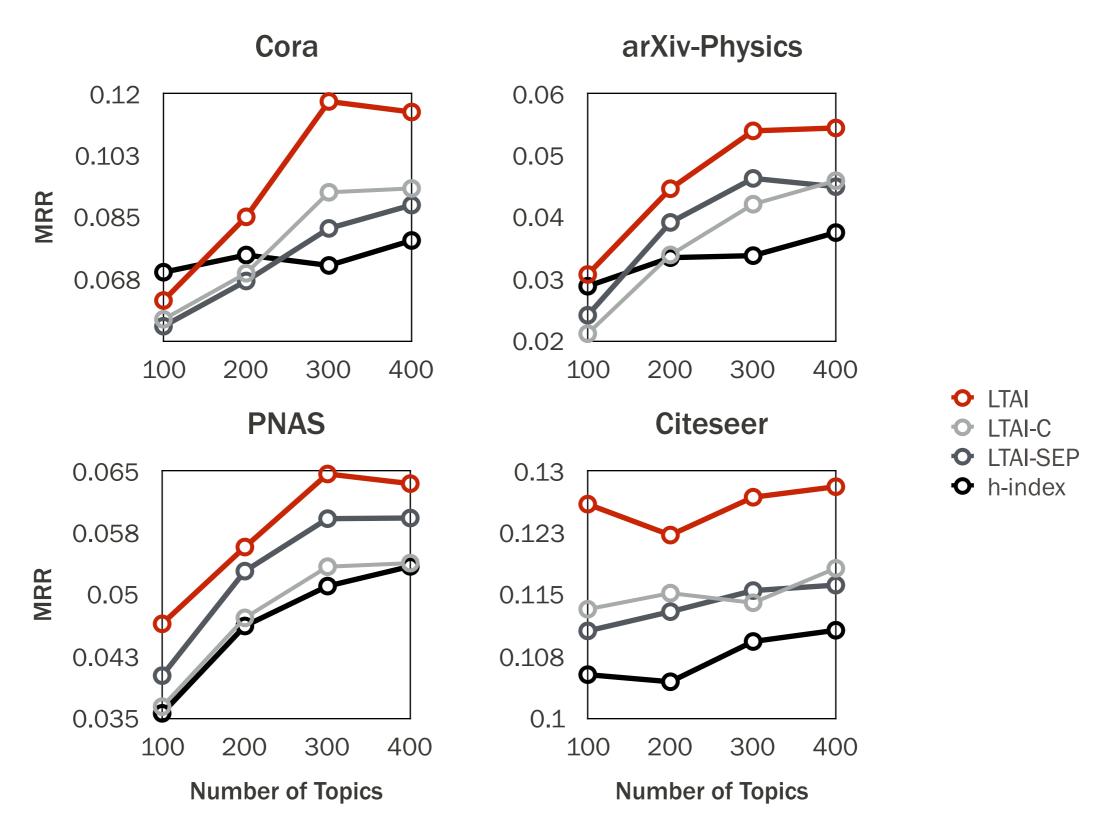
#### **Experimental Results: Citation Prediction**



#### **Experiments: Author Prediction**



#### **Experimental Results: Author Prediction**



#### **Experimental Results: Word Prediction**

#### Log Predictive Probability

	LTAI	LTAI-10%	LTAI-20%	LTAI-30%	LDA
CORA	-7.624	-7.672	-7.711	-7.754	-7.740
arXiv-Physics	-7.724	-7.744	-7.761	-7.813	-7.805
PNAS	-8.214	-8.262	-8.298	-8.321	-8.280
Citeseer	-7.808	-7.850	-7.863	-7.875	-7.866

# Qualitative Analysis

# Qualitative Analysis

T 27: approximation, intelligence, artificial, correlation, support, recognition, model, representation

Author	Authority Score of T27	h-index	# cite	# papers
M Jordan	9.85	9	245	28
F Girosi	4.76	4	117	13
T Poggio	4.67	6	176	28
M Jones	2.83	7	135	20

Lists famous researchers with their topical authority score,
 h-index, number of citations, and number of papers

#### Qualitative Analysis: Researcher with Focused Research Domain

T 27: approximation, intelligence, artificial, correlation, support, recognition, model, representation

Author	Authority Score of T27	h-index	# cite	# papers
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- High concentration on statistical learning
  - Training support vector machines: an application to face detection
  - An improved training algorithm for support vector machines
  - Regularization theory and neural networks architectures
- Relatively low number of h-index, #cite, #papers, but high topical authority score

#### Qualitative Analysis: Researcher with Broader Research Domain

T 27: approximation, intelligence, artificial, correlation, support, recognition, model, representation

Author	Authority Score of T27	h-index	# cite	# papers
M Jordan	9.85	9	245	28
F Girosi	4.76	4	117	13
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- Has broader academic interest than Federico Girosi:
   Statistical learning + computer vision
  - Face recognition: Features versus templates
  - Hierarchical models of object recognition in cortex
  - Example-based learning for view-based human face detection
- Coauthored all papers written by Federico Girosi

#### Qualitative Analysis: Researcher with Different Research Domain

T 27: approximation, intelligence, artificial, correlation, support, recognition, model, representation

Author	Authority Score of T27	h-index	# cite	# papers
M Jordan	9.85	9	245	28
F Girosi	4.76	4	117	13
T Poggio	4.67	6	176	28
M Jones	2.83	7	135	20

- Research interests:
  - Programming language design, implementation, and application
- Main topic extracted by LTAI:
  - Language, type, programming, higher order
- Algorithms and inference techniques often used in the paper

#### Qualitative Analysis: Researcher with Different Research Domain

T 27: approximation, intelligence, artificial, correlation, support, recognition, model, representation

Author	Authority Score of T27	h-index	# cite	# papers
M Jordan	9.85	0	245	28
F Girosi	4.76	4	117	13
T Poggio	4.67	6	176	28
M Jones	2.83	7	135	20

- Research ir
  - Programn
- Main topic
  - Language
- Algorithms

The efficiency of a parallel implementation of the conjugate gradient method preconditioned by an incomplete Cholesky factorization can vary dramatically depending on the column ordering chosen. One method to minimize the number of major parallel steps is to choose an ordering based on a coloring of the symmetric graph representing the nonzero adjacency structure of the matrix. In this paper, we compare the performance of the preconditioned conjugate gradient method using these coloring orderings with a number of standard orderings on matrices arising from applications in structural engineering. Because optimal colorings for these systems may not be a priori known, we employ several graph coloring heuristics to obtain consistent colorings. Based on lower bounds obtained from the local structure of these systems, we find that the colorings determined by these heuristics are nearly optimal.

oplication

the paper

#### Conclusion

- LTAI models topical authority of academic researchers
  - Input: Text data, link data (authorship, citation)
  - Output: Research topic, topic distribution (paper), topical authority (author)
- LTAI outperforms related citation models
  - 3 Experiments: Predicting citation/authorship links and words
- LTAI's possible applications
  - Finding authoritative researchers from given topical interests
  - Finding academic papers from given topical interests
  - Discovering research topics from academic corpus

#### References

- 1. D. M. Blei, A. Y. Ng, and M. I. Jordan. Latent dirichlet allocation. JMLR, 2003.
- 2. J. Chang and D. M. Blei. Relational topic models for document networks. In AISTATS, 2010.
- 3. M. Rosen-Zvi, T. Griffiths, M. Steyvers, and P. Smyth. The author-topic model for authors and documents. In UAI, 2004.
- 4. Y. Tu, N. Johri, D. Roth, and J. Hockenmaier. Citation author topic model in expert search. In ICCL, 2010.
- 5. Liu, A. Niculescu-Mizil, and W. Gryc. Topic-link Ida: joint models of topic and author community. In ICML, 2009.

#### Appendix: Variational Inference

Variational distributions over the topic-related latent variables

$$q(\theta, \beta, z) = \prod_{i} q(\theta_i) \prod_{N_i} q(z_{in}) \prod_{k} q(\beta_k)$$

where

$$q(z_{in}) = \text{Multinomial}(z_{in}|\phi_{in})$$
  
 $q(\theta_i) = \text{Dirichlet}(\theta_i|\gamma_i)$   
 $q(\beta_k) = \text{Dirichlet}(\phi_k|\lambda_k).$ 

Then ELBO of log-likelihood of the variational distribution becomes

$$\mathcal{L}_{[q]} = \mathbb{E}_{q} \left[ \sum_{k} \log p(\beta_{k} | \alpha_{\beta}) + \sum_{i} \log p(\theta_{i} | \alpha_{\theta}) \right]$$
$$+ \sum_{i} \sum_{N_{i}} \log p(z_{in} | \theta_{d}) + \log p(w_{in} | \beta_{z_{in}})$$
$$+ \sum_{i,j} \log p(x_{ij} | z_{i}, z_{j}, \pi_{i}) \right] - \mathcal{H}[q],$$

#### Appendix: Variational Inference

Taking gradient w.r.t gamma and lambda leads to

$$\gamma_{ik} = \alpha_{\theta} + \sum_{N_i} \phi_{ink}$$
 and  $\lambda_{kw} = \alpha_{\beta} + \sum_{i} \sum_{N_i} \phi_{ink} \delta(w_{in} = w)$ 

Taking gradient w.r.t. phi leads to

$$\phi_{ink} \propto \exp\left\{\frac{\sum_{j} \partial \mathbb{E}_{q}[\log p(x_{ij}|\bar{z}_{i},\bar{z}_{j},\pi_{i},\eta)]}{\partial \phi_{ink}} + \frac{\sum_{j} \partial \mathbb{E}_{q}[\log p(x_{ji}|\bar{z}_{j},\bar{z}_{i},\pi_{j},\eta)]}{\partial \phi_{ink}} + \mathbb{E}_{q}[\log \theta_{ik}] + \mathbb{E}_{q}[\log \beta_{kw_{in}}]\right\}$$

Where

$$\mathbb{E}_{q}[\log p(x_{ij}|\bar{z}_{i},\bar{z}_{j},\pi_{i},\eta)]$$

$$= \mathbb{E}_{q}[\log \sum_{a \in A_{i}} p(a_{ij} = a|\pi_{i})p(x_{ij}|\bar{z}_{i},\bar{z}_{j},\eta_{a})]$$

$$\geq \sum_{a \in A_{i}} p(a_{ij} = a|\pi_{i})\mathbb{E}_{q}[\log p(x_{ij}|\bar{z}_{i},\bar{z}_{j},\eta_{a})]$$

using Jensen's inequality and

### Appendix: Variational Inference

$$\mathbb{E}_q[\log p(x_{ij}|\bar{z}_i,\bar{z}_j,\eta_a)] = \mathcal{N}(x_{ij}|\bar{\phi}_i^{\top} \operatorname{diag}(\eta_a)\bar{\phi}_j,c_{ij})$$

by first-order Taylor expansion.

Thus,

$$\begin{split} & \frac{\sum_{j} \partial \mathbb{E}_{q}[\log p(x_{ij}|\bar{z_{i}},\bar{z_{j}},\pi_{i},\eta)]}{\partial \phi_{ink}} \\ & \approx \sum_{j} \frac{\bar{\phi}_{jk} c_{ij}}{N_{i}} \sum_{a \in A_{i}} \eta_{ak}(x_{ij} - \bar{\phi}_{i}^{\top} \mathrm{diag}(\eta_{a}) \bar{\phi}_{j}) p(a_{ij} = a|\pi_{i}) \end{split}$$