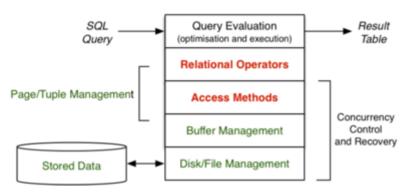
Implementing Relational Operators

Implementation of relational operations in DBMS:



... Implementing Relational Operators

2/72

1/72

So far, have considered file structures ...

- heap file ... tuples added to any page which has space
- sorted file ... tuples arranged in file in key order
- hash file ... tuples placed in pages using hash function

with relational algebra operations ...

- scanning (e.g. select * from R)
- sorting (e.g. select * from R order by x)
- projection (e.g. select x,y from R)
- selection (e.g. select * from R where Cond)

and now ...

- indexes ... search trees based on pages/keys
- signatures ... bit-strings which "summarize" tuples

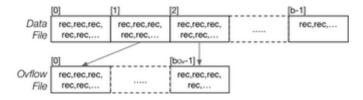
... Implementing Relational Operators

3/72

File/query Parameters ...

- r tuples of size R, b pages of size B, c tuples per page
- Rel.k attribute in where clause, b_q answer pages for query q
- b_{OV} overflow pages, average overflow chain length OV

File structures ...



When showing the cost of operations ...

- for queries, simply count number of pages read
- for updates, use n_r and n_w to distinguish reads/writes

When comparing two methods for same query

• ignore the cost of writing the result (same for both)

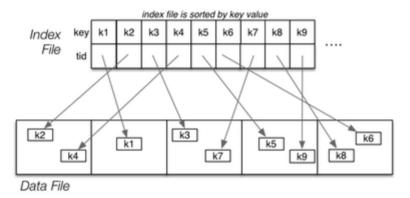
In counting reads and writes, assume minimal buffering

- each request page() causes a read
- each release page() causes a write (if page is dirty)

Indexing

Indexing 6/72

An index is a file of (keyVal,tupleID) pairs, e.g.



Indexes 7/72

A 1-d index is based on the value of a single attribute A.

Some possible properties of A:

- may be used to sort data file (or may be sorted on some other field)
- values may be unique (or there may be multiple instances)

Taxonomy of index types, based on properties of index attribute:

primary index on unique field, may be sorted on A

clustering index on non-unique field, file sorted on A

secondary file not sorted on A

A given table may have indexes on several attributes.

... Indexes 8/72

Indexes themselves may be structured in several ways:

dense every tuple is referenced by an entry in the index file

sparse only some tuples are referenced by index file entries

single-level tuples are accessed directly from the index file

multi-level may need to access several index pages to reach tuple

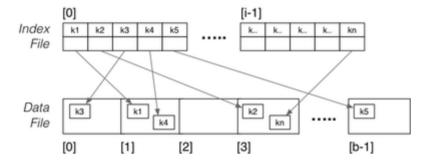
Index file has total i pages (where typically $i \ll b$)

Index file has page capacity c_i (where typically $c_i \gg c$)

Dense index: $i = ceil(r/c_i)$ Sparse index: $i = ceil(b/c_i)$

Dense Primary Index

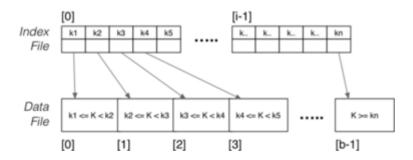
9/72



Data file unsorted; one index entry for each tuple

Sparse Primary Index

10/72



Data file sorted; one index entry for each page

Exercise 1: Index Storage Overheads

11/72

Consider a relation with the following storage parameters:

- B = 8192, R = 128, r = 100000
- header in data pages: 256 bytes
- · key is integer, data file is sorted on key
- index entries (keyVal,tupleID): 8 bytes

header in index pages: 32 bytes

How many pages are needed to hold a dense index?

How many pages are needed to hold a sparse index?

Selection with Primary Index

12/72

For one queries:

```
ix = binary search index for entry with key K
if nothing found { return NotFound }
b = getPage(pageOf(ix.tid))
t = getTuple(b,offsetOf(ix.tid))
    -- may require reading overflow pages
return t
```

Worst case: read logoi index pages + read 1+Ov data pages.

Thus, $Cost_{one,prim} = log_2 i + 1 + Ov$

Assume: index pages are same size as data pages ⇒ same reading cost

... Selection with Primary Index

13/72

For range queries on primary key:

- · use index search to find lower bound
- · read index sequentially until reach upper bound
- accumulate set of buckets to be examined
- · examine each bucket in turn to check for matches

For pmr queries involving primary key:

• search as if performing one query.

For gueries not involving primary key, index gives no help.

... Selection with Primary Index

14/72

Method for range queries (when data file is not sorted)

Overview:

tid = insert tuple into page P at position p find location for new entry in index file insert new index entry (k,tid) into index file

Problem: order of index entries must be maintained

- need to avoid overflow pages in index
- either reorganise index file or mark entries

Reogranisation requires, on average, read/write half of index file:

$$Cost_{insert,prim} = (log_2i)_r + i/2.(1_r + 1_w) + (1 + Ov)_r + (1 + \delta)_w$$

Deletion with Primary Index

16/72

Overview:

find tuple using index
mark tuple as deleted
delete index entry for tuple

If we delete index entries by marking ...

•
$$Cost_{delete,prim} = (log_2 i)_r + (1 + Ov)_r + 1_W + 1_W$$

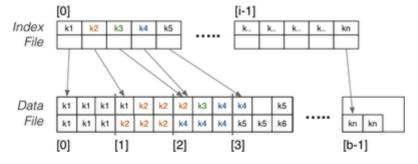
If we delete index entry by index file reorganisation ...

•
$$Cost_{delete,prim} = (log_2 i)_r + (1 + Ov)_r + i/2.(1_r + 1_w) + 1_w$$

Clustering Index

17/72

Data file sorted; one index entry for each key value



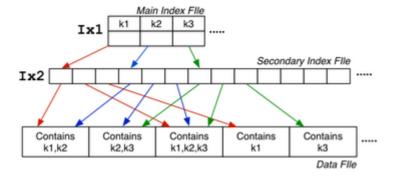
Cost penalty: maintaining both index and data file as sorted

(Note: can't mark index entry for value X until all X tuples are deleted)

Secondary Index

18/72

Data file not sorted; want one index entry for each key value



 $Cost_{pmr} = (log_2i_{ix1} + a_{ix2} + b_q.(1 + Ov))$

Multi-level Indexes

Above Secondary Index used two index files to speed up search

- by keeping the initial index search relatively quick
- Ix1 small (depends on number of unique key values)
- Ix2 larger (depends on amount of repetition of keys)
- typically, $b_{Ix1} \ll b_{Ix2}$

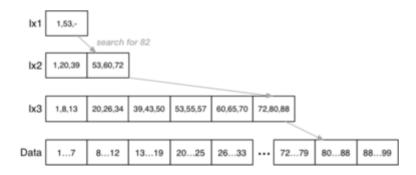
Could improve further by

- making Ix1 sparse, since Ix2 is guaranteed to be ordered
- in this case, $b_{Ix1} = ceil(b_{Ix2} / c_i)$
- if Ix1 becomes too large, add Ix3 and make Ix2 sparse
- if data file ordered on key, could make Ix3 sparse

Ultimately, reduce top-level of index hierarchy to one page.

... Multi-level Indexes 20/72

Example data file with three-levels of index:



Assume: not primary key, c = 100, $c_i = 3$

Select with Multi-level Index

21/72

For one query on indexed key field:

```
xpid = top level index page
for level = 1 to d {
   read index entry xpid
   search index page for J'th entry
      where index[J].key <= K < index[J+1].key
   if (J == -1) { return NotFound }
   xpid = index[J].page</pre>
```

pid = xpid // pid is data page index search page pid and its overflow pages

 $Cost_{one,mli} = (d + 1 + Ov)_r$

(Note that $d = ceil(log_{C_i}r)$ and c_i is large because index entries are small)

22/72 **B-Trees**

B-trees are MSTs with the properties:

- they are updated so as to remain balanced
- each node has at least (n-1)/2 entries in it
- each tree node occupies an entire disk page

B-tree insertion and deletion methods

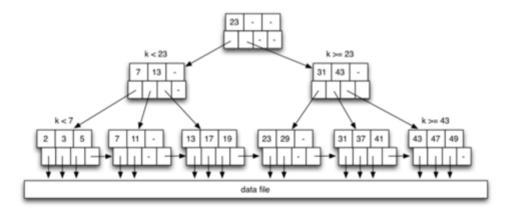
- · are moderately complicated to describe
- · can be implemented very efficiently

Advantages of B-trees over general MSTs

- better storage utilisation (around 2/3 full)
- better worst case performance (shallower)

23/72 ... B-Trees

Example B-tree (depth=3, n=3) (actually B+ tree)



(Note: in DBs, nodes are pages \Rightarrow large branching factor, e.g. n=500)

24/72 **B-Tree Depth**

Depth depends on effective branching factor (i.e. how full nodes are).

Simulation studies show typical B-tree nodes are 69% full.

Gives load $L_i = 0.69 \times c_i$ and depth of tree ~ ceil($\log_{L_i} r$).

Example: c_i =128, L_i =88

Level #nodes		#keys	
root	1	87	

1	88	7656
2	7744	673728
3	681472	59288064

Note: c_i is generally larger than 128 for a real B-tree.

Insertion into B-Trees

25/72

Overview of the method:

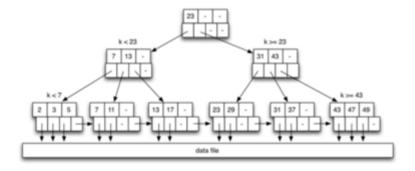
- 1. find leaf node and position in node where entry would be stored
- 2. if node is not full, insert entry into appropriate spot
- 3. if node is full, split node into two half-full nodes and promote middle element to parent
- 4. if parent full, split and promote upwards
- 5. if reach root, and root is full, make new root upwards

Note: if duplicates not allowed and key exists, may stop after step 1.

Example: B-tree Insertion

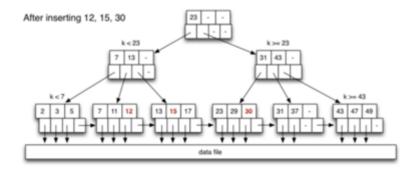
26/72

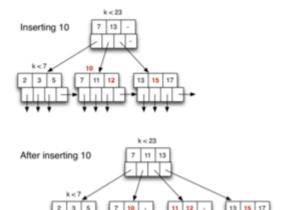
Starting from this tree:



insert the following keys in the given order 12 15 30 10

... Example: B-tree Insertion





B-Tree Insertion Cost

29/72

Insertion cost = Cost_{treeSearch} + Cost_{treeInsert} + Cost_{dataInsert}

Best case: write one page (most of time)

- traverse from root to leaf
- read/write data page, write updated leaf

 $Cost_{insert} = D_r + 1_W + 1_r + 1_W$

Common case: 3 node writes (rearrange 2 leaves + parent)

- traverse from root to leaf, holding nodes in buffer
- read/write data page
- update/write leaf, parent and sibling

 $Cost_{insert} = D_r + 3_W + 1_r + 1_W$

... B-Tree Insertion Cost 30/72

Worst case: 2D-1 node writes (propagate to root)

- traverse from root to leaf, holding nodes in buffers
- read/write data page
- update/write leaf, parent and sibling
- repeat previous step D-1 times

 $Cost_{insert} = D_r + 3D_W + 1_r + 1_W$ (naive method)

 $Cost_{insert} = D_r + (2D-1)_W + 1_r + 1_W$ (optimised method)

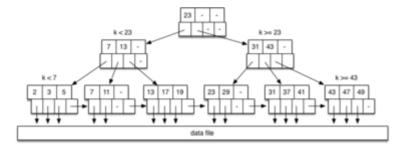
Selection with B-Trees

31/72

For one queries:

```
N = B-tree root node
while (N is not a leaf node)
   N = scanToFindChild(N,K)
tid = scanToFindEntry(N,K)
access tuple T using tid
```

 $Cost_{one} = (D + 1)_r$

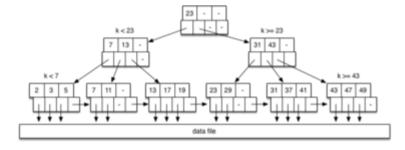


... Selection with B-Trees 32/72

For range queries (assume sorted on index attribute):

```
search index to find leaf node for Lo
for each leaf node entry until Hi found {
          access tuple T using tid from entry
}
```

 $Cost_{range} = (D + b_i + b_q)_r$



B-trees in PostgreSQL

33/72

PostgreSQL implements ≅ Lehman/Yao-style B-trees

• variant that works effectively in high-concurrency environments.

B-tree implementation: backend/access/nbtree

- **README** ... comprehensive description of methods
- nbtree.c ... interface functions (for iterators)
- nbtsearch.c ... traverse index to find key value
- nbtinsert.c ... add new entry to B-tree index

Notes:

- stores all instances of equal keys (dense index)
- avoids splitting by scanning right if key = max(key) in page
- common insert case: new key is max(key) overall; handled efficiently

... B-trees in PostgreSQL

34/72

Changes for PostgreSQL v12

- indexes smaller
 - o for composite keys, only store first attribute
 - o index entries are smaller, so ci larger, so tree shallower
- include TID in index key
 - o duplicate index entries are stored in "table order"

To explore indexes in more detail:

- \di+ IndexName
- select * from bt_page_items(IndexName,BlockNo)

... B-trees in PostgreSQL 35/72

Interface functions for B-trees

```
// build Btree index on relation
Datum btbuild(rel,index,...)
// insert index entry into Btree
Datum btinsert(rel, key, tupleid, index,...)
// start scan on Btree index
Datum btbeginscan(rel, key, scandesc,...)
// get next tuple in a scan
Datum btgettuple(scandesc, scandir,...)
// close down a scan
Datum btendscan(scandesc)
```

N-dimensional Selection

N-dimensional Queries

Have looked at one-dimensional queries, e.g.

```
select * from R where a = K
select * from R where a between Lo and Hi
```

and heaps, hashing, indexing as ways of efficient implementation.

Now consider techniques for efficient multi-dimensional queries.

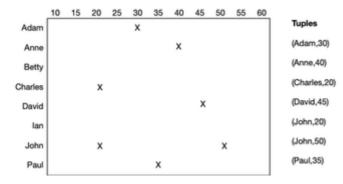
Compared to 1-d queries, multi-dimensional queries

- typically produce fewer results
- require us to consider more information
- require more effort to produce results

38/72 **Tuple Space**

It is possible to view tuples as points in an Nd space.

Consider the relation Person(name, age) and its tuple-space.



Operations for Nd Select

N-dimensional select queries = condition on ≥1 attributes.

• pmr = partial-match retrieval (equality tests), e.g.

```
select * from Person
where name = 'John' and age = 50;
```

• space = tuple-space queries (range tests), e.g.

```
select * from Person where 20 \le age \le 50 and 'Charles' \le name \le 'John'
```

N-d Selection via Heaps

40/72

Heap files can handle pmr or space using standard method:

```
// select * from R where C
r = openRelation("R",READ);
for (p = 0; p < nPages(r); p++) {
    buf = getPage(file(r), p);
    for (i = 0; i < nTuples(buf); i++) {
        t = getTuple(buf,i);
        if (matches(t,C))
            add t to result set
    }
}
Costpmr = Costspace = b</pre>
```

N-d Selection via Multiple Indexes

41/72

DBMSs already support building multiple indexes on a table.

Which indexes to build depends on which queries are asked.

```
create table R (a int, b int, c int);
create index Rax on R (a);
create index Rbx on R (b);
create index Rcx on R (c);
create index Rabx on R (a,b);
create index Racx on R (a,c);
create index Rbcx on R (b,c);
create index Rallx on R (a,b,c);
```

But more indexes ⇒ space + update overheads.

N-d Queries and Indexes

42/72

Generalised view of pmr and space queries:

```
select * from R where a_1 op_1 C_1 and ... and a_n op_n C_n
```

pmr : all op; are equality tests. space : some op; are range tests.

Possible approaches to handling such queries ...

... N-d Queries and Indexes 43/72

If using just one of several indexes, which one to use?

```
select * from R where a_1 op<sub>1</sub> C_1 and ... and a_n op<sub>n</sub> C_n
```

The one with best selectivity for a_i op C_i (i.e. fewest matches)

Factors determining selectivity of ai opi Ci

- assume uniform distribution of values in dom(a_i)
- · equality test on primary key gives at most one match
- equality test on larger dom(a_i) ⇒ less matches
- range test over large part of dom(a_i) ⇒ many matches

... N-d Queries and Indexes 44/72

Implementing selection using one of several indices:

```
// Query: select * from R where a_1op_1C_1 and ... and a_nop_nC_n // choose a_i with best selectivity

TupleIDs = IndexLookup(R, a_i, op_i, C_i)

// gives { tid_1, tid_2, ...} for tuples satisfying a_iop_iC_i

PageIDs = { }

foreach tid in TupleIDs

{ PageIDs = PageIDs \cup {pageOf(tid)} }

// PageIDs = a set of b_{q_{ix}} page numbers

...

Cost = Cost<sub>index</sub> + b_{q_{ix}} (some pages do not contain answers, b_{q_{ix}} > b_q)
```

DBMSs typically maintain statistics to assist with determining selectivity

... N-d Queries and Indexes 45/72

Implementing selection using multiple indices:

```
// Query: select * from R where a_1op_1C_1 and ... and a_nop_nC_n
// assumes an index on at least a_i
TupleIDs = IndexLookup(R, a_1, op_1, C_1)
foreach attribute a_i with an index {
		tids = IndexLookup(R, a_i, op_i, C_i)
		TupleIDs = TupleIDs \cap tids
}
PageIDs = { }
foreach tid in TupleIDs
		{ PageIDs = PageIDs $\mathcal{U}$ {pageOf(tid)} } }
// PageIDs = a set of b_q page numbers
...

Cost = k.Costindex + b_q (assuming indexes on k of n attrs)
```

Exercise 2: One vs Multiple Indices

Consider a relation with r = 100,000, B = 4096, defined as:

```
create table Students (
   id     integer primary key,
   name     char(10), -- simplified
   gender   char(1), -- 'm','f','?'
   birthday char(5) -- 'MM-DD'
);
```

Assumptions:

- data file is not ordered on any attribute
- has a dense B-tree index on each attribute
- 96 bytes of header in each data/index page

For Students(id, name, gender, birthday) ...

- · calculate the size of the data file and each index
- · describe the selectivity of each attribute

Now consider a query on this relation:

```
select * from Students
where name='John' and birthday='04-01'
```

- estimate the cost of answering using name index
- estimate the cost of answering using birthday index
- · estimate the cost of answering using both indices

Bitmap Indexes 48/72

Alternative index structure, focussing on sets of tuples:

		Data File	
	Part#	Colour	Price
[0]	P7	red	\$2.50
[1]	P1	green	\$3.50
[2]	P9	blue	\$4.10
[3]	P4	blue	\$7.00
[4]	P5	red	\$5.20
[5]	P5	red	\$2.50

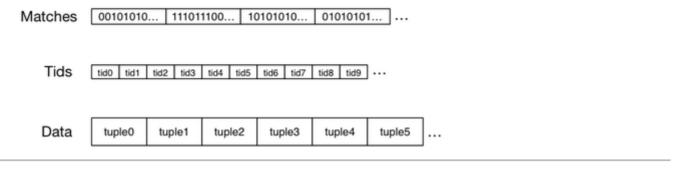


Colour Index

Index contains bit-strings of r bits, one for each value/range

... Bitmap Indexes 49/72

Also useful to have a file of tids, one for each tuple:



50/72 ... Bitmap Indexes

Answering queries using bitmap index:

```
Matches = AllOnes(r)
foreach attribute A with index {
   // select i<sup>th</sup> bit-string for attribute A
   // based on value associated with A in WHERE
  Matches = Matches & Bitmaps[A][i]
// Matches contains 1-bit for each matching tuple
foreach i in 0..r-1 {
   if (Matches[i] == 0) continue;
   Pages = Pages U {pageOf(Tids[i])}
foreach pid in Pages {
   P = getPage(pid)
   extract matching tuples from P
```

Exercise 3: Bitmap Index

Using the following file structure:

		Data File	
	Part#	Colour	Price
[0]	P7	red	\$2.50
[1]	P1	green	\$3.50
[2]	P9	blue	\$4.10
[3]	P4	blue	\$7.00
[4]	P5	red	\$5.20
[5]	P5	red	\$2.50



Show how the following queries would be answered:

```
select * from Parts
where colour='red' and price < 4.00
select * from Parts
where colour='green' or colour ='blue'
```

52/72 ... Bitmap Indexes

Storage costs for bitmap indexes:

- one bitmap for each value/range for each indexed attribute
- each bitmap has length ceil(r/8) bytes
- e.g. with 50K records and 8KB pages, bitmap fits in one page

Query execution costs for bitmap indexes:

- read one bitmap for each indexed attribute in query
- perform bitwise AND on bitmaps (in memory)
- read pages containing matching tuples

Note: bitmaps could index pages rather than tuples (shorter bitmaps)

Hashing for N-d Selection

Hashing and *pmr* 54/72

For a pmr query like

select * from R where $a_1 = C_1$ and ... and $a_n = C_n$

- if one a; is the hash key, query is very efficient
- if no ai is the hash key, need to use linear scan

Can be alleviated using multi-attribute hashing (mah)

- form a composite hash value involving all attributes
- at query time, some components of composite hash are known (allows us to limit the number of data pages which need to be checked)

MA.hashing works in conjunction with any dynamic hash scheme.

... Hashing and *pmr* 55/72

Multi-attribute hashing parameters:

- file size = $b = 2^d$ pages \Rightarrow use d-bit hash values
- relation has n attributes: a₁, a₂, ...a_n
- attribute ai has hash function hi
- attribute a; contributes d; bits (to the combined hash value)
- total bits $d = \sum_{i=1}^{n} d_i$
- a choice vector (cv) specifies for all k ...
 bit j from h_i(a_i) contributes bit k in combined hash value

MA. Hashing Example

56/72

Consider relation Deposit (branch, acctNo, name, amount)

Assume a small data file with 8 main data pages (plus overflows).

Hash parameters: d=3 $d_1=1$ $d_2=1$ $d_3=1$ $d_4=0$

Note that we ignore the amount attribute ($d_4=0$)

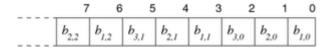
Assumes that nobody will want to ask queries like

select * from Deposit where amount=533

Choice vector is designed taking expected queries into account.

... MA. Hashing Example

Choice vector:



This choice vector tells us:

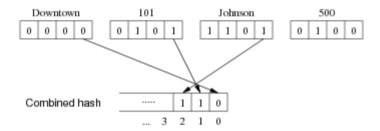
- bit 0 in hash comes from bit 0 of hash₁(a₁) (b_{1.0})
- bit 1 in hash comes from bit 0 of hash₂(a₂) (b_{2.0})
- bit 2 in hash comes from bit 0 of hash3(a3) (b3.0)
- bit 3 in hash comes from bit 1 of hash₁(a₁) (b_{1,1})
- etc. etc. (up to as many bits of hashing as required, e.g. 32)

... MA.Hashing Example 58/72

Consider the tuple:

branch	acctNo	name	amount
Downtown	101	Johnston	512

Hash value (page address) is computed by:



MA. Hashing Hash Functions

59/72

Auxiliary definitions:

```
#define MaxHashSize 32
typedef unsigned int HashVal;

// extracts i'th bit from hash value
#define bit(i,h) (((h) & (1 << (i))) >> (i))

// choice vector elems
typedef struct { int attr, int bit } CVelem;
typedef CVelem ChoiceVec[MaxHashSize];

// hash function for individual attributes
HashVal hash_any(char *val) { ... }
```

... MA. Hashing Hash Functions

60/72

Produce combined d-bit hash value for tuple t:

```
HashVal hash(Tuple t, ChoiceVec cv, int d)
{
    HashVal h[nAttr(t)+1]; // hash for each attr
    HashVal res = 0, oneBit;
    int i, a, b;
```

```
for (i = 1; i <= nAttr(t); i++)
    h[i] = hash_any(attrVal(t,i));
for (i = 0; i < d; i++) {
    a = cv[i].attr;
    b = cv[i].bit;
    oneBit = bit(b, h[a]);
    res = res | (oneBit << i);
}
return res;</pre>
```

Exercise 4: Multi-attribute Hashing

61/72

Compute the hash value for the tuple

```
('John Smith', 'BSc(CompSci)',1990,99.5)
```

where d=6, $d_1=3$, $d_2=2$, $d_3=1$, and

- $cv = \langle (1,0), (1,1), (2,0), (3,0), (1,2), (2,1), (3,1), (1,3), ... \rangle$
- hash₁('John Smith') = ...0101010110110100
- hash₂('BSc(CompSci)') = ...10111111101101111
- $hash_3(1990) = ...0001001011000000$

Queries with MA.Hashing

62/72

In a partial match query:

- values of some attributes are known
- values of other attributes are unknown

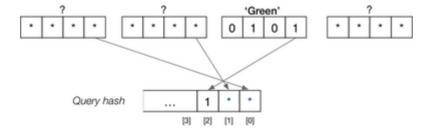
E.g.

```
select amount
from Deposit
where branch = 'Brighton' and name = 'Green'
for which we use the shorthand (Brighton, ?, Green, ?)
```

... Queries with MA.Hashing

63/72

Consider query: select amount from Deposit where name='Green'



Matching tuples must be in pages: 100, 101, 110, 111.

Exercise 5: Partial hash values in MAH

```
d=6, b=2<sup>6</sup>, CV = <(0,0),(0,1),(1,0),(2,0),(1,1),(0,2), ...>
hash (a) = ...00101101001101
hash (b) = ...00101101001101
```

• hash (c) = ...00101101001101

What are the query hashes for each of the following:

• (a,b,c), (?,b,c), (a,?,?), (?,?,?)

MA. Hashing Query Algorithm

65/72

```
// Builds the partial hash value (e.g. 10*0*1)
// Treats query like tuple with some attr values missing
nstars = 0;
for each attribute i in query Q {
   if (hasValue(Q,i)) {
      set d[i] bits in composite hash
            using choice vector and hash(Q,i)
   } else {
      set d[i] *'s in composite hash
            using choice vector
        nstars += d[i]
   }
}
```

... MA. Hashing Query Algorithm

66/72

```
// Use the partial hash to find candidate pages
r = openRelation("R",READ);
for (i = 0; i < 2<sup>nstars</sup>; i++) {
    P = composite hash
    replace *'s in P
        using i and choice vector
    Buf = readPage(file(r), P);
    for each tuple T in Buf {
        if (T satisfies pmr query)
            add T to results
    }
}
```

Exercise 6: Representing Stars

67/72

Our hash values are bit-strings (e.g. 100101110101)

MA.Hashing introduces a third value (* = unknown)

How could we represent "bit"-strings like 1011*1*0**010?

Exercise 7: MA.Hashing Query Cost

68/72

Consider R(x,y,z) using multi-attribute hashing where

$$d = 9$$
 $d_X = 5$ $d_V = 3$ $d_Z = 1$

How many buckets are accessed in answering each query?

```
1. select * from R where x = 4 and y = 2 and z = 1
2. select * from R where x = 5 and y = 3
3. select * from R where y = 99
4. select * from R where z = 23
5. select * from R where x > 5
```

Query Cost for MA. Hashing

69/72

Multi-attribute hashing handles a range of query types, e.g.

```
select * from R where a=1 select * from R where d=2 select * from R where b=3 and c=4 select * from R where a=5 and b=6 and c=7
```

A relation with n attributes has 2ⁿ different query types.

Different query types have different costs (different no. of *'s)

```
Cost(Q) = 2^{S} where s = \Sigma_{i \in Q} d_{i} (alternatively Cost(Q) = \Pi_{i \in Q} 2^{d_{i}})
```

Query distribution gives probability p_Q of asking each query type Q.

... Query Cost for MA.Hashing

70/72

Min query cost occurs when all attributes are used in query

 $Min\ Cost_{pmr} = 1$

Max query cost occurs when no attributes are specified

$$Max\ Cost_{pmr} = 2^d = b$$

Average cost is given by weighted sum over all query types:

$$Avg\ Cost_{pmr} = \Sigma_Q p_Q \Pi_{i \notin Q} 2^{d_i}$$

Aim to minimise the weighted average query cost over possible query types

Optimising MA.Hashing Cost

71/72

For a given application, useful to minimise Cost_{pmr}.

Can be achieved by choosing appropriate values for d_i (cv)

Heuristics:

- distribution of query types (more bits to frequently used attributes)
- size of attribute domain (≤ #bits to represent all values in domain)
- discriminatory power (more bits to highly discriminating attributes)

Trade-off: making Q_i more efficient makes Q_k less efficient.

This is a combinatorial optimisation problem (solve via standard optimisation techniques e.g. simulated annealing)

Exercise 8: MA.Hashing Design

Consider relation Person(name, gender, age) ...

p_Q	Query Type Q
0.5	select name from Person where gender=X and age=Y
0.25	select age from Person where name=X
0.25	select name from Person where gender=X

Assume that all other query types have $p_Q=0$.

Design a choice vector to minimise average selection cost.

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