

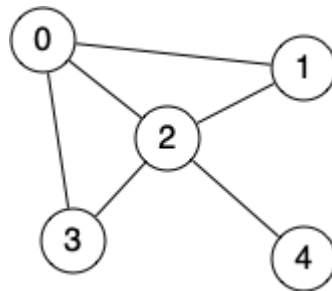
# Quiz 4

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Deadline	Friday, 03 July 2020 at 11:59PM
Latest Submission	Friday, 03 July 2020 at 11:01AM
Raw Mark	4.00/4.00 (100.00%)
Late Penalty	N/A
Final Mark	4.00/4.00 (100.00%)

## Question 1 (1 mark)

Consider the following graph



Which of the following gives a valid adjacency representation of this graph?

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(a)



	[0]	[1]	[2]	[3]	[4]
[0]	0	1	1	1	0
[1]	1	0	1	0	0
[2]	1	1	0	1	1
[3]	1	0	1	0	0
[4]	0	0	1	0	0

(b)



	[0]	[1]	[2]	[3]	[4]
[0]	1	1	0	1	0
[1]	1	1	1	0	0
[2]	1	1	1	1	1
[3]	1	0	1	1	0
[4]	0	0	1	0	1

(c)



	[0]	[1]	[2]	[3]	[4]
[0]	0	1	1	1	0
[1]	0	0	1	0	0
[2]	1	1	0	1	1
[3]	0	1	1	0	0
[4]	0	0	1	0	0

(d)	<div style="display: flex; align-items: center;"> <input type="radio"/> <table border="1" style="margin-left: 10px;"> <tr> <th></th> <th>[0]</th> <th>[1]</th> <th>[2]</th> <th>[3]</th> <th>[4]</th> </tr> <tr> <th>[0]</th> <td>0</td> <td>1</td> <td>1</td> <td>0</td> <td>0</td> </tr> <tr> <th>[1]</th> <td>0</td> <td>0</td> <td>1</td> <td>0</td> <td>0</td> </tr> <tr> <th>[2]</th> <td>1</td> <td>1</td> <td>0</td> <td>1</td> <td>1</td> </tr> <tr> <th>[3]</th> <td>1</td> <td>0</td> <td>1</td> <td>0</td> <td>0</td> </tr> <tr> <th>[4]</th> <td>0</td> <td>0</td> <td>1</td> <td>0</td> <td>0</td> </tr> </table> </div>		[0]	[1]	[2]	[3]	[4]	[0]	0	1	1	0	0	[1]	0	0	1	0	0	[2]	1	1	0	1	1	[3]	1	0	1	0	0	[4]	0	0	1	0	0
	[0]	[1]	[2]	[3]	[4]																																
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[2]	1	1	0	1	1																																
[3]	1	0	1	0	0																																
[4]	0	0	1	0	0																																
(e)	<div style="display: flex; align-items: center;"> <input type="radio"/> <div style="margin-left: 10px;">None of the above is correct</div> </div>																																				

✓ Your response was correct.

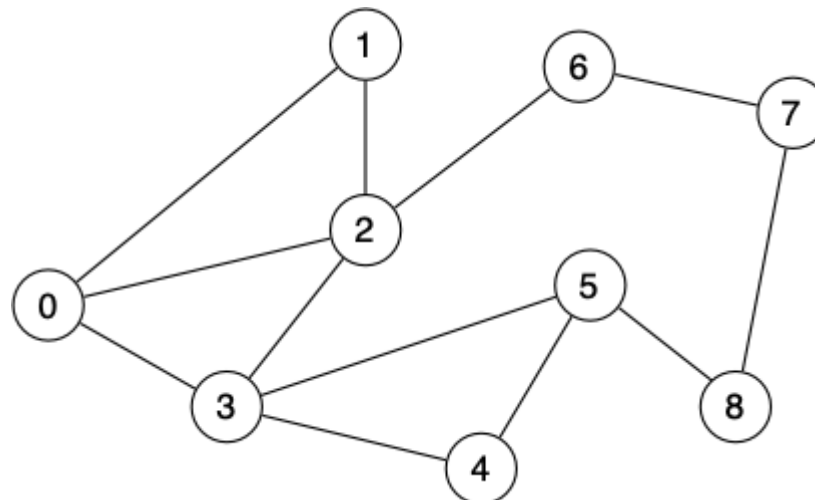
Mark: 1.00

The edges are not directed, so the matrix has to be symmetric.

Along each row  $[v]$ , it has a 1 value for edge incident on  $v$

### Question 2 (1 mark)

Consider the following graph



If we used a standard breadth-first search, starting from vertex 0, and giving priority to lower-numbered neighbours, which path would be discovered to reach vertex 8?

(a)	0-3-5-8
<input checked="" type="radio"/>	
(b)	0-3-4-5-8
<input type="radio"/>	
(c)	0-2-6-7-8
<input type="radio"/>	
(d)	0-1-2-3-4-5-8
<input type="radio"/>	
(e)	None of the above paths would be chosen
<input type="radio"/>	

✓ Your response was correct.

Mark: 1.00

Tracing the execution of the standard BFS path finding algorithm from slides and textbook ...

```
After visiting 0
queue: 1 2 3
visited: 0 0 0 0 -1 -1 -1 -1 -1

After visiting 1
queue: 2 3 (no non-visited edges)
visited: 0 0 0 0 -1 -1 -1 -1 -1

After visiting 2
queue: 3 6
visited: 0 0 0 0 -1 -1 2 -1 -1

After visiting 3
queue: 6 4 5
visited: 0 0 0 0 3 3 2 -1 -1

After visiting 6
queue: 4 5 7
visited: 0 0 0 0 3 3 2 7 -1

After visiting 4
queue: 5 7 (no non-visited edges)
visited: 0 0 0 0 3 3 2 7 -1

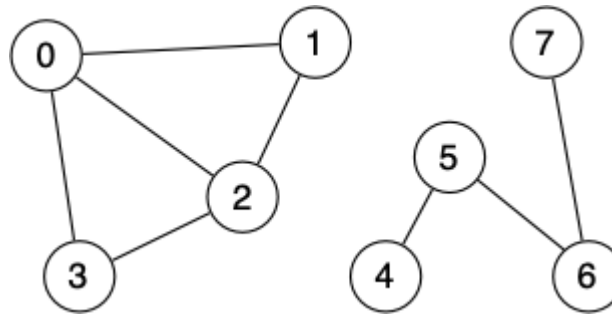
After visiting 5
queue: 7 8
visited: 0 0 0 0 3 3 2 7 5

After visiting 7
queue: 8 (no non-visited edges)
visited: 0 0 0 0 3 3 2 7 5

After visiting 8
queue: empty
found
trace path back : 8 5 3 0
```

**Question 3 (1 mark)**

Consider the following graph with two connected components



Which of the following actions would convert this into a graph with a single connected component?

You must choose *all* relevant actions to obtain full marks for this question. There is more than one valid action.

(a) <input checked="" type="checkbox"/>	add an edge between 0 and 5
(b) <input type="checkbox"/>	add an edge between 5 and 7
(c) <input checked="" type="checkbox"/>	add an edge between 2 and 4
(d) <input type="checkbox"/>	add an edge between 1 and 3
(e) <input checked="" type="checkbox"/>	add an edge between 0 and 6
(f) <input type="checkbox"/>	add an edge between 7 and 4

✓ Your response was correct.

Mark:  $\max(0.33 + 0.33 + 0.33, 0) = 1.00$

Any edge that joins a vertex from one component to a vertex in the other component is correct.

Joining edges *within* a component does not help.

**Question 4 (1 mark)**

How many edges are in a complete graph with N vertices?

(a) <input type="radio"/>	N-1
(b) <input type="radio"/>	N
(c) <input type="radio"/>	$\log_2 N$
(d) <input checked="" type="radio"/>	$N(N-1)/2$
(e) <input type="radio"/>	$N^2$

✓ Your response was correct.

Mark: 1.00

In a complete graph, every vertex is connected to every other vertex.

Each of the V vertices has (V-1) edges incident on it =>  $V(V-1)$  edges

Since each edge handles both (v,w) and (w,v), we divide by two =>  $V(V-1)/2$