

```

% Options for packages loaded elsewhere

\PassOptionsToPackage{unicode}{hyperref}

\PassOptionsToPackage{hyphens}{url}

%

\documentclass[

]{article}

\usepackage{lmodern}

\usepackage{amsmath}

\usepackage{ifxetex,ifluatex}

\ifnum 0\ifxetex 1\fi\ifluatex 1\fi=0 % if pdftex

  \usepackage[T1]{fontenc}

  \usepackage[utf8]{inputenc}

  \usepackage{textcomp} % provide euro and other symbols

  \usepackage{amssymb}

\else % if luatex or xetex

  \usepackage{unicode-math}

  \defaultfontfeatures{Scale=MatchLowercase}

  \defaultfontfeatures[\rmfamily]{Ligatures=TeX,Scale=1}

\fi

% Use upquote if available, for straight quotes in verbatim environments

\IfFileExists{upquote.sty}{\usepackage{upquote}}{}

\IfFileExists{microtype.sty}{% use microtype if available

  \usepackage{microtype}

  \UseMicrotypeSet[protrusion]{basicmath} % disable protrusion for tt fonts

}{}

\makeatletter

\@ifundefined{KOMAClassName}{% if non-KOMA class

  \IfFileExists{parskip.sty}{%

    \usepackage{parskip}

```

```

}{% else

\setlength{\parindent}{0pt}

\setlength{\parskip}{6pt plus 2pt minus 1pt}}

}{% if KOMA class

\KOMAOptions{parskip=half}}

\makeatother

\usepackage{xcolor}

\ifFileExists{xurl.sty}{\usepackage{xurl}}{} % add URL line breaks if available

\ifFileExists{bookmark.sty}{\usepackage{bookmark}}{\usepackage{hyperref}}

\hypersetup{

pdftitle={Lab 1},

pdfauthor={Hanlin Wang},

hidelinks,

pdfcreator={LaTeX via pandoc}}

\urlstyle{same} % disable monospaced font for URLs

\usepackage[margin=1in]{geometry}

\usepackage{color}

\usepackage{fancyvrb}

\newcommand{\VerbBar}{}

\newcommand{\VERB}{\Verb[commandchars=\\\{\}]}

\DefineVerbatimEnvironment{Highlighting}{Verbatim}{commandchars=\\\{\}}

% Add ',fontsize=\small' for more characters per line

\usepackage{framed}

\definecolor{shadecolor}{RGB}{248,248,248}

\newenvironment{Shaded}{\begin{snugshade}}{\end{snugshade}}

\newcommand{\AlertTok}[1]{\textcolor{rgb}{0.94,0.16,0.16}{\textbf{#1}}}

\newcommand{\AnnotationTok}[1]{\textcolor{rgb}{0.56,0.35,0.01}{\textbf{\textit{#1}}}}

\newcommand{\AttributeTok}[1]{\textcolor{rgb}{0.77,0.63,0.00}{\textbf{#1}}}

\newcommand{\BaseNTok}[1]{\textcolor{rgb}{0.00,0.00,0.81}{\textbf{#1}}}

```

```

\newcommand{\BuiltInTok}[1]{#1}

\newcommand{\CharTok}[1]{\textcolor{rgb}{0.31,0.60,0.02}{#1}}

\newcommand{\CommentTok}[1]{\textcolor{rgb}{0.56,0.35,0.01}{\textit{#1}}}

\newcommand{\CommentVarTok}[1]{\textcolor{rgb}{0.56,0.35,0.01}{\textbf{\textit{#1}}}}

\newcommand{\ConstantTok}[1]{\textcolor{rgb}{0.00,0.00,0.00}{#1}}

\newcommand{\ControlFlowTok}[1]{\textcolor{rgb}{0.13,0.29,0.53}{\textbf{#1}}}

\newcommand{\DataTypeTok}[1]{\textcolor{rgb}{0.13,0.29,0.53}{#1}}

\newcommand{\DecValTok}[1]{\textcolor{rgb}{0.00,0.00,0.81}{#1}}

\newcommand{\DocumentationTok}[1]{\textcolor{rgb}{0.56,0.35,0.01}{\textbf{\textit{#1}}}}

\newcommand{\ErrorTok}[1]{\textcolor{rgb}{0.64,0.00,0.00}{\textbf{#1}}}

\newcommand{\ExtensionTok}[1]{#1}

\newcommand{\FloatTok}[1]{\textcolor{rgb}{0.00,0.00,0.81}{#1}}

\newcommand{\FunctionTok}[1]{\textcolor{rgb}{0.00,0.00,0.00}{#1}}

\newcommand{\ImportTok}[1]{#1}

\newcommand{\InformationTok}[1]{\textcolor{rgb}{0.56,0.35,0.01}{\textbf{\textit{#1}}}}

\newcommand{\KeywordTok}[1]{\textcolor{rgb}{0.13,0.29,0.53}{\textbf{#1}}}

\newcommand{\NormalTok}[1]{#1}

\newcommand{\OperatorTok}[1]{\textcolor{rgb}{0.81,0.36,0.00}{\textbf{#1}}}

\newcommand{\OtherTok}[1]{\textcolor{rgb}{0.56,0.35,0.01}{#1}}

\newcommand{\PreprocessorTok}[1]{\textcolor{rgb}{0.56,0.35,0.01}{\textit{#1}}}

\newcommand{\RegionMarkerTok}[1]{#1}

\newcommand{\SpecialCharTok}[1]{\textcolor{rgb}{0.00,0.00,0.00}{#1}}

\newcommand{\SpecialStringTok}[1]{\textcolor{rgb}{0.31,0.60,0.02}{#1}}

\newcommand{\StringTok}[1]{\textcolor{rgb}{0.31,0.60,0.02}{#1}}

\newcommand{\VariableTok}[1]{\textcolor{rgb}{0.00,0.00,0.00}{#1}}

\newcommand{\VerbatimStringTok}[1]{\textcolor{rgb}{0.31,0.60,0.02}{#1}}

\newcommand{\WarningTok}[1]{\textcolor{rgb}{0.56,0.35,0.01}{\textbf{\textit{#1}}}}

\usepackage{graphicx}

\makeatletter

```

```

\def\maxwidth{\ifdim\Gin@nat@width>\linewidth\linewidth\else\Gin@nat@width\fi}
\def\maxheight{\ifdim\Gin@nat@height>\textheight\textheight\else\Gin@nat@height\fi}
\makeatother

% Scale images if necessary, so that they will not overflow the page
% margins by default, and it is still possible to overwrite the defaults
% using explicit options in \includegraphics[width, height, ...]{}
\setkeys{Gin}{width=\maxwidth,height=\maxheight,keepaspectratio}
% Set default figure placement to htbp
\makeatletter
\def\fps@figure{htbp}
\makeatother
\setlength{\emergencystretch}{3em} % prevent overfull lines
\providecommand{\tightlist}{%
  \setlength{\itemsep}{0pt}\setlength{\parskip}{0pt}}
\setcounter{secnumdepth}{-\maxdimen} % remove section numbering
\ifluatex
  \usepackage{selnolig} % disable illegal ligatures
\fi

\title{Lab 1}
\author{Hanlin Wang}
\date{11:59PM February 18, 2021}

\begin{document}
\maketitle

```

You should have RStudio installed to edit this file. You will write code in places marked ``TO-DO'' to complete the problems. Some of this will be a pure programming assignment. The tools for the solutions to these

problems can be found in the class practice lectures. I want you to use the methods I taught you, not for you to google and come up with whatever works. You won't learn that way.

To ``hand in" the homework, you should compile or publish this file into a PDF that includes output of your code. Once it's done, push by the deadline to your repository in a directory called ``labs".

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Print out the numerical constant pi with ten digits after the decimal point using the internal constant `\texttt{pi}`.

```
\end{itemize}
```

```
\begin{Shaded}
```

```
\begin{Highlighting}[]
```

```
\FunctionTok{options}\NormalTok{{}\AttributeTok{digits=}\DecValTok{11}\NormalTok{{}}
```

```
\NormalTok{pi}
```

```
\end{Highlighting}
```

```
\end{Shaded}
```

```
\begin{verbatim}
```

```
## [1] 3.1415926536
```

```
\end{verbatim}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Sum up the first 103 terms of the series $1 + 1/2 + 1/4 + 1/8 +$

\ldots

$$\sum_{k=0}^{102} \frac{1}{2^k}$$

[1] 2

Find the product of the first 37 terms in the sequence $1/3, 1/6, 1/9$

\ldots

$$\prod_{k=1}^{37} \frac{1}{3^k}$$

\begin{verbatim}

[1] 1.613528728e-61

\end{verbatim}

\begin{Shaded}

\begin{Highlighting}[]

\FunctionTok{prod}\NormalTok{{}}\DecValTok{1}

\SpecialCharTok{/}\NormalTok{{}}\FunctionTok{seq}\NormalTok{{}}\AttributeTok{from =}

\DecValTok{3}\NormalTok{, }\AttributeTok{by =} \DecValTok{3}\NormalTok{, }\AttributeTok{length.out
= } \DecValTok{37}\NormalTok{}}\end{Highlighting}

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

[1] 1.613528728e-61

\end{verbatim}

\begin{itemize}

\tightlist

\item

Find the product of the first 387 terms of

$1 \cdot \frac{1}{2} \cdot \frac{1}{4} \cdot \frac{1}{8} \cdot \dots$

\end{itemize}

\begin{Shaded}

\begin{Highlighting}[]

\FunctionTok{prod}\NormalTok{{}}\DecValTok{1} \SpecialCharTok{/}\NormalTok{{}}\DecValTok{2}

\SpecialCharTok{^}\NormalTok{{}}\DecValTok{0}\SpecialCharTok{:} \DecValTok{386}\NormalTok{}}\end{Highlighting}

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

[1] 0

\end{verbatim}

\begin{Shaded}

\begin{Highlighting}[]

\FunctionTok{prod}\NormalTok{{}\DecValTok{1}

\SpecialCharTok{/}\NormalTok{{}\FunctionTok{seq}\NormalTok{{}\AttributeTok{from =}

\DecValTok{2}\NormalTok{, }\AttributeTok{by =} \DecValTok{3}\NormalTok{, }\AttributeTok{length.out

=} \DecValTok{387}\NormalTok{ })}}

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

[1] 0

\end{verbatim}

\begin{Shaded}

\begin{Highlighting}[]

\NormalTok{.Machine}\SpecialCharTok{\$}\NormalTok{double.xmin}

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

[1] 2.2250738585e-308

\end{verbatim}

Is this answer \emph{exactly} correct? It's not correct because the
answer numerically underflow

\#TO-DO

\begin{itemize}

\tightlist

\item

Figure out a means to express the answer more exactly. Not compute exactly, but express more exactly.

\end{itemize}

\begin{Shaded}

\begin{Highlighting}[]

\SpecialCharTok{{-}}\FunctionTok{log}\NormalTok{{}}\DecValTok{2}\NormalTok{{}}\SpecialCharTok{*}\FunctionTok{sum}\NormalTok{((}\DecValTok{0}\SpecialCharTok{:} \DecValTok{386}\NormalTok{)}

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

[1] -51771.856063

\end{verbatim}

\begin{itemize}

\tightlist

\item

Create the sequence $x = \{-\infty, 20, 18, \dots, -20\}$.

\end{itemize}

\begin{Shaded}

\begin{Highlighting}[]

```

\NormalTok{X }\OtherTok{\textless{}\{-}}
\FunctionTok{c}\NormalTok{({}\ConstantTok{Inf}\NormalTok{,{ }\FunctionTok{seq}\NormalTok{({}\Attribut
eTok{from =}\DecValTok{20}\NormalTok{,{ }\AttributeTok{to =}
\SpecialCharTok{\-}}\DecValTok{20}\NormalTok{,{ }\AttributeTok{by =}
\SpecialCharTok{\-}}\DecValTok{2}\NormalTok{({})}

\NormalTok{X}

\end{Highlighting}

\end{Shaded}

```

```

\begin{verbatim}

## [1] Inf 20 18 16 14 12 10 8 6 4 2 0 -2 -4 -6 -8 -10 -12 -14
## [20] -16 -18 -20

\end{verbatim}

```

Create the sequence

```

\texttt{x\ =\ {[}\log\_3(Inf),\ log\_3(100),\ log\_3(98),\ ...\ log\_3(-20){]}}.

```

```

\begin{Shaded}

\begin{Highlighting}[]

\NormalTok{X }\OtherTok{\textless{}\{-}}
\FunctionTok{c}\NormalTok{({}\ConstantTok{Inf}\NormalTok{,{ }\FunctionTok{seq}\NormalTok{({}\Attribut
eTok{from =}\DecValTok{100}\NormalTok{,{ }\AttributeTok{to =}
\SpecialCharTok{\-}}\DecValTok{20}\NormalTok{,{ }\AttributeTok{by =}
\SpecialCharTok{\-}}\DecValTok{2}\NormalTok{({})}

\NormalTok{X }\OtherTok{=} \FunctionTok{log}\NormalTok{({X, }\AttributeTok{base =}
\DecValTok{3}\NormalTok{({})}

\end{Highlighting}

\end{Shaded}

```

```

\begin{verbatim}

## Warning: NaNs produced

\end{verbatim}

```

Comment on the appropriateness of the non-numeric values.

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Create a vector of booleans where the entry is true if

x_i is positive and finite.

```
\end{itemize}
```

```
\begin{Shaded}
```

```
\begin{Highlighting}[]
```

```
\NormalTok{Y } \OtherTok{=} \FunctionTok{is.nan} \NormalTok{(X) } \SpecialCharTok{\&}
```

```
\FunctionTok{is.finite} \NormalTok{(X) } \SpecialCharTok{\&} \NormalTok{ X } \SpecialCharTok{\textgreater} \\ \DecValTok{0}
```

```
\end{Highlighting}
```

```
\end{Shaded}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Locate the indices of the non-real numbers in this vector. Hint: use

the \texttt{which} function. Don't hesitate to use the documentation

via $\texttt{?which}$.

```
\end{itemize}
```

```
\begin{Shaded}
```

```
\begin{Highlighting}[]
```

```
\NormalTok{?which}
```

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

starting httpd help server ... done

\end{verbatim}

\begin{Shaded}

\begin{Highlighting}[]

\FunctionTok{which}\NormalTok{{Y}}\SpecialCharTok{==}\ConstantTok{FALSE}\NormalTok{{}}

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

[1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25

[26] 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50

[51] 51 52 53 54 55 56 57 58 59 60 61 62

\end{verbatim}

\begin{itemize}

\tightlist

\item

Locate the indices of the infinite quantities in this vector.

\end{itemize}

\begin{Shaded}

\begin{Highlighting}[]

\FunctionTok{which}\NormalTok{{}}\FunctionTok{is.infinite}\NormalTok{{X}}}

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

[1] 1 52

\end{verbatim}

\begin{itemize}

\tightlist

\item

Locate the indices of the min and max in this vector. Hint: use the

\texttt{which.min} and \texttt{which.max} functions.

\end{itemize}

\begin{Shaded}

\begin{Highlighting}[]

\FunctionTok{which.min}\NormalTok{(X)}

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

[1] 52

\end{verbatim}

\begin{Shaded}

\begin{Highlighting}[]

\FunctionTok{which.max}\NormalTok{(X)}

\end{Highlighting}

\end{Shaded}

```
\begin{verbatim}
```

```
## [1] 1
```

```
\end{verbatim}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Count the number of unique values in `\texttt{x}`.

```
\end{itemize}
```

```
\begin{Shaded}
```

```
\begin{Highlighting}[]
```

```
\FunctionTok{length}\NormalTok{({})\FunctionTok{unique}\NormalTok{({X})}
```

```
\end{Highlighting}
```

```
\end{Shaded}
```

```
\begin{verbatim}
```

```
## [1] 53
```

```
\end{verbatim}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Cast `\texttt{x}` to a factor. Do the number of levels make sense?

```
\end{itemize}
```

```
\begin{Shaded}
```

```
\begin{Highlighting}[]
```

```
\FunctionTok{as.factor}\NormalTok{({X})}
```

\end{Highlighting}

\end{Shaded}

\begin{verbatim}

```
## [1] Inf          4.19180654857877 4.1734172518943 4.15464876785729
## [5] 4.13548512895119 4.11590933734319 4.09590327428938 4.07544759935851
## [9] 4.05452163806914 4.03310325630434 4.01116871959141 3.98869253500376
## [13] 3.96564727304425 3.94200336638929 3.91772888178973 3.89278926071437
## [17] 3.86714702345081 3.84076143030548 3.81358809221559 3.78557852142874
## [21] 3.75667961082847 3.72683302786084 3.69597450568212 3.66403300987579
## [25] 3.63092975357146 3.59657702661571 3.56087679500731 3.52371901428583
## [29] 3.48497958377173 3.44451784578705 3.40217350273288 3.3577627814323
## [33] 3.31107361281783 3.26185950714291 3.20983167673402 3.15464876785729
## [37] 3.09590327428938 3.03310325630434 2.96564727304425 2.89278926071437
## [41] 2.8135880922156 2.72683302786084 2.63092975357146 2.52371901428583
## [45] 2.40217350273288 2.26185950714291 2.09590327428938 1.89278926071437
## [49] 1.63092975357146 1.26185950714291 0.630929753571457 -Inf
## [53] NaN          NaN          NaN          NaN
## [57] NaN          NaN          NaN          NaN
## [61] NaN          NaN
## 53 Levels: -Inf 0.630929753571457 1.26185950714291 ... NaN
```

\end{verbatim}

\begin{itemize}

\tightlist

\item

Cast `\texttt{x}` to integers. What do we learn about R's infinity
representation in the integer data type?

\end{itemize}

```

\begin{Shaded}
\begin{Highlighting}[]
\FunctionTok{as.integer}\NormalTok{{(X)}}
\end{Highlighting}
\end{Shaded}

```

```

\begin{verbatim}
## Warning: NAs introduced by coercion to integer range
\end{verbatim}

```

```

\begin{verbatim}
## [1] NA 4 4 4 4 4 4 4 4 4 4 3 3 3 3 3 3 3 3 3 3 3 3
## [26] 3 3 3 3 3 3 3 3 3 3 3 3 2 2 2 2 2 2 2 2 1 1 1
## [51] 0 NA NA NA NA NA NA NA NA NA NA NA NA NA
\end{verbatim}

```

```

\begin{itemize}
\tightlist
\item
  Use \texttt{x} to create a new vector \texttt{y} containing only the
  real numbers in x.
\end{itemize}

```

```

\begin{Shaded}
\begin{Highlighting}[]
\NormalTok{y }\OtherTok{=}\NormalTok{ X[(!\SpecialCharTok{!})\NormalTok{ }\FunctionTok{is.infinite}\NormalTok{ }\SpecialCharTok{\&}}
\FunctionTok{is.nan}\NormalTok{ }\SpecialCharTok{\&}\NormalTok{ X }\SpecialCharTok{\textless{}}
\DecValTok{0}\NormalTok{ )}]

```


\NormalTok{y}
\end{Highlighting}
\end{Shaded}

\begin{verbatim}
[1] Inf 4.19180654858 4.17341725189 4.15464876786 4.13548512895
[6] 4.11590933734 4.09590327429 4.07544759936 4.05452163807 4.03310325630
[11] 4.01116871959 3.98869253500 3.96564727304 3.94200336639 3.91772888179
[16] 3.89278926071 3.86714702345 3.84076143031 3.81358809222 3.78557852143
[21] 3.75667961083 3.72683302786 3.69597450568 3.66403300988 3.63092975357
[26] 3.59657702662 3.56087679501 3.52371901429 3.48497958377 3.44451784579
[31] 3.40217350273 3.35776278143 3.31107361282 3.26185950714 3.20983167673
[36] 3.15464876786 3.09590327429 3.03310325630 2.96564727304 2.89278926071
[41] 2.81358809222 2.72683302786 2.63092975357 2.52371901429 2.40217350273
[46] 2.26185950714 2.09590327429 1.89278926071 1.63092975357 1.26185950714
[51] 0.63092975357 -Inf NaN NaN NaN
[56] NaN NaN NaN NaN NaN
[61] NaN NaN
\end{verbatim}

\begin{itemize}
\tightlist
\item
Use the left rectangle method to numerically integrate x^2 from 0
to 1 with rectangle width size $1e-6$.
\end{itemize}

\begin{Shaded}
\begin{Highlighting}[]

```

\FunctionTok{sum}\NormalTok{{}}\FunctionTok{seq}\NormalTok{{}}\AttributeTok{from =}
\DecValTok{0}\NormalTok{, }\AttributeTok{to =} \DecValTok{1}\SpecialCharTok{{-}}
\FloatTok{1e{-}6}\NormalTok{, }\AttributeTok{by =}
\FloatTok{1e{-}6}\NormalTok{) }\SpecialCharTok{^}} \DecValTok{2} \SpecialCharTok{*}
\FloatTok{1e{-}6}\NormalTok{}}

```

```

\end{Highlighting}

```

```

\end{Shaded}

```

```

\begin{verbatim}

```

```

## [1] 0.3333328333

```

```

\end{verbatim}

```

```

\begin{itemize}

```

```

\tightlist

```

```

\item

```

Calculate the average of 100 realizations of standard Bernoullis in
one line using the `\texttt{sample}` function.

```

\end{itemize}

```

```

\begin{Shaded}

```

```

\begin{Highlighting}[]

```

```

\FunctionTok{sample}\NormalTok{{( }\FunctionTok{c}\NormalTok{{}}\DecValTok{0}\NormalTok{,}\DecValT
ok{1}\NormalTok{), }\AttributeTok{size =} \DecValTok{500}\NormalTok{, }\AttributeTok{replace =}
\ConstantTok{TRUE}\NormalTok{}}

```

```

\end{Highlighting}

```

```

\end{Shaded}

```

```

\begin{verbatim}

```

```

## [1] 1 0 0 0 0 1 0 0 1 0 0 1 0 0 0 1 1 1 1 0 0 1 0 1 1 0 1 0 0 0 1 1 1 1 0 0

```

```

## [38] 0 0 0 1 1 0 1 1 0 0 0 1 0 1 1 1 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 1 0 1 1 1 0

```

```

## [75] 1 0 1 1 1 1 1 0 0 0 0 1 0 0 0 1 0 0 1 1 1 1 1 1 1 0 0 1 1 1 0 0 0 0 1 0 0

```

```

## [112] 1 0 0 0 1 1 0 0 0 0 0 0 0 1 1 1 0 0 1 1 1 1 1 0 0 1 1 0 0 0 0 0 1 1 0 0
## [149] 0 0 1 0 1 0 1 0 0 0 0 1 1 1 1 0 1 0 1 1 0 0 1 1 0 1 0 0 0 1 0 0 0 0 0 0 1
## [186] 1 0 0 0 0 1 1 0 1 1 1 0 1 0 0 1 0 0 1 0 0 1 0 0 1 1 1 1 0 1 0 1 0 0 1 0 1
## [223] 0 1 1 1 1 1 0 0 1 0 1 1 1 1 0 0 1 1 1 1 1 0 1 1 1 1 0 1 1 0 0 1 0 0 0 0 0
## [260] 0 1 0 0 1 0 0 1 0 0 0 0 0 0 1 1 0 1 1 1 0 0 0 0 1 0 1 1 1 0 0 1 1 1 0 1 1 1
## [297] 0 0 0 0 0 1 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 1 0 1 1 0 1 0 0 0 1 1 0 1 0 1 1
## [334] 0 0 1 1 0 1 0 0 0 1 1 1 1 0 1 0 0 0 0 1 0 1 1 0 1 0 1 1 0 0 0 1 1 0 1 0 1
## [371] 0 1 0 0 0 0 0 1 1 1 1 1 1 1 1 0 1 1 0 0 1 1 0 1 1 1 0 1 1 1 1 0 1 0 0 1 1
## [408] 1 1 0 0 1 0 1 1 0 0 1 0 0 0 0 1 1 0 0 0 1 1 0 0 1 0 1 0 1 0 1 1 0 0 1 1 1
## [445] 0 1 0 0 0 0 0 1 1 1 0 1 1 0 1 0 1 0 0 0 1 0 0 0 1 1 0 0 0 0 0 1 1 1 0 0 1
## [482] 1 1 0 0 1 0 1 1 1 1 1 1 1 0 1 0 1 0 0

```

\end{verbatim}

\begin{itemize}

\tightlist

\item

Calculate the average of 500 realizations of Bernoullis with $p = 0.9$

in one line using the `\texttt{sample}` and `\texttt{mean}` functions.

\end{itemize}

\begin{Shaded}

\begin{Highlighting}[]

```

\FunctionTok{mean}\NormalTok{{}\FunctionTok{sample}\NormalTok{{( }\FunctionTok{c}\NormalTok{{}\Dec
ecValTok{0}\NormalTok{,}\DecValTok{1}\NormalTok{)}, }\AttributeTok{size =}
\DecValTok{100}\NormalTok{, }\AttributeTok{replace =}
\ConstantTok{TRUE}\NormalTok{, }\AttributeTok{prob =}
\FunctionTok{c}\NormalTok{{}\FloatTok{0.9}\NormalTok{, }\FloatTok{0.1}\NormalTok{)}}}

```

\end{Highlighting}

\end{Shaded}

```
\begin{verbatim}
```

```
## [1] 0.06
```

```
\end{verbatim}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Calculate the average of 1000 realizations of Bernoullis with $p = 0.9$

in one line using `\texttt{rbinom}`.

```
\end{itemize}
```

```
\begin{Shaded}
```

```
\begin{Highlighting}[]
```

```
\NormalTok{?rbinom}
```

```
\FunctionTok{mean}\NormalTok{({}\FunctionTok{rbinom}\NormalTok{({}\AttributeTok{n =}
\DecValTok{1000}\NormalTok{, }\AttributeTok{size =} \DecValTok{1}\NormalTok{, }\AttributeTok{prob
=}\FloatTok{0.9}\NormalTok{)})}
```

```
\end{Highlighting}
```

```
\end{Shaded}
```

```
\begin{verbatim}
```

```
## [1] 0.912
```

```
\end{verbatim}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

In class we considered a variable `\texttt{x_3}` which measured

“criminality”. We imagined $L = 4$ levels “none”, “infraction”,

``misdemeanor" and ``felony". Create a variable `\texttt{x_3}` here with 100 random elements (equally probable). Create it as a nominal (i.e.~unordered) factor.

`\end{itemize}`

`\begin{Shaded}`

`\begin{Highlighting}[]`

`\NormalTok{X_3 }\OtherTok{=}`

`\FunctionTok{as.factor}\NormalTok{{}\FunctionTok{sample}\NormalTok{{}\FunctionTok{c}\NormalTok{{}\StringTok{"none"}\NormalTok{{, }\StringTok{"infraction"}\NormalTok{{, }\StringTok{"misdemeanor"}\NormalTok{{, }\StringTok{"felony"}\NormalTok{{}, }\AttributeTok{size =}\DecValTok{100}\NormalTok{{, }\AttributeTok{replace =}\ConstantTok{TRUE}\NormalTok{{}}}`

`\NormalTok{X_3}`

`\end{Highlighting}`

`\end{Shaded}`

`\begin{verbatim}`

[1] misdemeanor felony infraction none misdemeanor felony

[7] misdemeanor infraction misdemeanor felony misdemeanor felony

[13] none misdemeanor infraction infraction felony felony

[19] infraction infraction felony felony none none

[25] felony misdemeanor infraction none none felony

[31] felony misdemeanor felony infraction none felony

[37] infraction felony infraction felony felony infraction

[43] misdemeanor misdemeanor infraction infraction felony misdemeanor

[49] felony felony infraction misdemeanor none felony

[55] misdemeanor infraction felony none misdemeanor felony

[61] misdemeanor misdemeanor infraction felony felony felony

[67] none felony misdemeanor none none none

[73] misdemeanor felony none misdemeanor infraction none

```
## [79] felony   misdemeanor none      misdemeanor misdemeanor none
## [85] none      none      misdemeanor felony   none      felony
## [91] none      misdemeanor infraction none      infraction felony
## [97] felony   misdemeanor none      none
## Levels: felony infraction misdemeanor none
\end{verbatim}
```

```
\begin{itemize}
\tightlist
\item
  Use \texttt{x\_3} to create \texttt{x\_3\_bin}, a binary feature where
  0 is no crime and 1 is any crime.
\end{itemize}
```

```
\begin{Shaded}
\begin{Highlighting}[]
\NormalTok{X\_3\_bin }\OtherTok{=}\NormalTok{ X\_3 }\SpecialCharTok{!=} \StringTok{"none"}
\end{Highlighting}
\end{Shaded}
```

```
\begin{itemize}
\tightlist
\item
  Use \texttt{x\_3} to create \texttt{x\_3\_ord}, an ordered factor
  variable. Ensure the proper ordinal ordering.
\end{itemize}
```

```
\begin{Shaded}
\begin{Highlighting}[]
```

```

\FunctionTok{factor}\NormalTok{{(X\_3, }\AttributeTok{levels =}
\FunctionTok{c}\NormalTok{{}\StringTok{"none"}\NormalTok{, }\StringTok{"infraction"}\NormalTok{, }\S
tringTok{"misdemeanor"}\NormalTok{, }\StringTok{"felony"}\NormalTok{, }\AttributeTok{order =}
\ConstantTok{TRUE}\NormalTok{}}

```

```

\end{Highlighting}

```

```

\end{Shaded}

```

```

\begin{verbatim}

```

```

## [1] misdemeanor felony    infraction none      misdemeanor felony
## [7] misdemeanor infraction misdemeanor felony    misdemeanor felony
## [13] none      misdemeanor infraction infraction felony    felony
## [19] infraction infraction felony    felony    none      none
## [25] felony    misdemeanor infraction none      none      felony
## [31] felony    misdemeanor felony    infraction none      felony
## [37] infraction felony    infraction felony    felony    infraction
## [43] misdemeanor misdemeanor infraction infraction felony    misdemeanor
## [49] felony    felony    infraction misdemeanor none      felony
## [55] misdemeanor infraction felony    none      misdemeanor felony
## [61] misdemeanor misdemeanor infraction felony    felony    felony
## [67] none      felony    misdemeanor none      none      none
## [73] misdemeanor felony    none      misdemeanor infraction none
## [79] felony    misdemeanor none      misdemeanor misdemeanor none
## [85] none      none      misdemeanor felony    none      felony
## [91] none      misdemeanor infraction none      infraction felony
## [97] felony    misdemeanor none      none

## Levels: none < infraction < misdemeanor < felony

```

```

\end{verbatim}

```

```

\begin{Shaded}

```

```

\begin{Highlighting}[]

```

`\NormalTok{?factor}`

`\end{Highlighting}`

`\end{Shaded}`

`\begin{itemize}`

`\tightlist`

`\item`

Convert this variable into three binary variables without any
information loss and put them into a data matrix.

`\end{itemize}`

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`\begin{Highlighting}[]`

`\CommentTok{\#TO{-}DO}`

`\end{Highlighting}`

`\end{Shaded}`

`\begin{itemize}`

`\tightlist`

`\item`

What should the sum of each row be (in English)?

`\end{itemize}`

`\#TO-DO`

Verify that.

`\begin{Shaded}`

`\begin{Highlighting}[]`

`\CommentTok{\#TO{-}DO}`

`\end{Highlighting}`

`\end{Shaded}`

`\begin{itemize}`

`\tightlist`

`\item`

How should the column sum look (in English)?

`\end{itemize}`

`\#TO-DO`

Verify that.

`\begin{Shaded}`

`\begin{Highlighting}[]`

`\CommentTok{\#TO{-}DO}`

`\end{Highlighting}`

`\end{Shaded}`

`\begin{itemize}`

`\tightlist`

`\item`

Generate a matrix with 100 rows where the first column is realization from a normal with mean 17 and variance 38, the second column is uniform between -10 and 10, the third column is poisson with mean 6, the fourth column is exponential with lambda of 9, the fifth column is binomial with $n = 20$ and $p = 0.12$ and the sixth column is a binary variable with exactly 24% 1's dispersed randomly. Name the rows the

entries of the `\texttt{fake_first_names}` vector.

`\end{itemize}`

`\begin{Shaded}`

`\begin{Highlighting}[]`

`\NormalTok{fake_first_names } \OtherTok{=} \FunctionTok{c} \NormalTok{({}`

`\StringTok{"Sophia"} \NormalTok{, } \StringTok{"Emma"} \NormalTok{, } \StringTok{"Olivia"} \NormalTok{, }
 \StringTok{"Ava"} \NormalTok{, } \StringTok{"Mia"} \NormalTok{, } \StringTok{"Isabella"} \NormalTok{, } \St
 ringTok{"Riley"} \NormalTok{, }`

`\StringTok{"Aria"} \NormalTok{, } \StringTok{"Zoe"} \NormalTok{, } \StringTok{"Charlotte"} \NormalTok{, }
 StringTok{"Lily"} \NormalTok{, } \StringTok{"Layla"} \NormalTok{, } \StringTok{"Amelia"} \NormalTok{, } \Stri
 ngTok{"Emily"} \NormalTok{, }`

`\StringTok{"Madelyn"} \NormalTok{, } \StringTok{"Aubrey"} \NormalTok{, } \StringTok{"Adalyn"} \NormalTok{
 ok, } \StringTok{"Madison"} \NormalTok{, } \StringTok{"Chloe"} \NormalTok{, } \StringTok{"Harper"} \Norma
 lTok, }`

`\StringTok{"Abigail"} \NormalTok{, } \StringTok{"Aaliyah"} \NormalTok{, } \StringTok{"Avery"} \NormalTok{,
 } \StringTok{"Evelyn"} \NormalTok{, } \StringTok{"Kaylee"} \NormalTok{, } \StringTok{"Ella"} \NormalTok{, } \\
 StringTok{"Ellie"} \NormalTok{, }`

`\StringTok{"Scarlett"} \NormalTok{, } \StringTok{"Arianna"} \NormalTok{, } \StringTok{"Hailey"} \NormalTok{To
 k, } \StringTok{"Nora"} \NormalTok{, } \StringTok{"Addison"} \NormalTok{, } \StringTok{"Brooklyn"} \Norma
 lTok, }`

`\StringTok{"Hannah"} \NormalTok{, } \StringTok{"Mila"} \NormalTok{, } \StringTok{"Leah"} \NormalTok{, }
 StringTok{"Elizabeth"} \NormalTok{, } \StringTok{"Sarah"} \NormalTok{, } \StringTok{"Eliana"} \NormalTok{,
 } \StringTok{"Mackenzie"} \NormalTok{, }`

`\StringTok{"Peyton"} \NormalTok{, } \StringTok{"Maria"} \NormalTok{, } \StringTok{"Grace"} \NormalTok{, }
 } \StringTok{"Adeline"} \NormalTok{, } \StringTok{"Elena"} \NormalTok{, } \StringTok{"Anna"} \NormalTok{, }
 } \StringTok{"Victoria"} \NormalTok{, }`

`\StringTok{"Camilla"} \NormalTok{, } \StringTok{"Lillian"} \NormalTok{, } \StringTok{"Natalie"} \NormalTok{}`

, \StringTok{"Jackson"}\NormalTok{, }\StringTok{"Aiden"}\NormalTok{, }\StringTok{"Lucas"}\NormalTok{

\StringTok{"Liam"}\NormalTok{, }\StringTok{"Noah"}\NormalTok{, }\StringTok{"Ethan"}\NormalTok{, }\StringTok{"Mason"}\NormalTok{, }\StringTok{"Caden"}\NormalTok{, }\StringTok{"Oliver"}\NormalTok{, }\StringTok{"Elijah"}\NormalTok{, }

\StringTok{"Grayson"}\NormalTok{, }\StringTok{"Jacob"}\NormalTok{, }\StringTok{"Michael"}\NormalTok{, }\StringTok{"Benjamin"}\NormalTok{, }\StringTok{"Carter"}\NormalTok{, }\StringTok{"James"}\NormalTok{, }

\StringTok{"Jayden"}\NormalTok{, }\StringTok{"Logan"}\NormalTok{, }\StringTok{"Alexander"}\NormalTok{, }\StringTok{"Caleb"}\NormalTok{, }\StringTok{"Ryan"}\NormalTok{, }\StringTok{"Luke"}\NormalTok{, }\StringTok{"Daniel"}\NormalTok{, }

\StringTok{"Jack"}\NormalTok{, }\StringTok{"William"}\NormalTok{, }\StringTok{"Owen"}\NormalTok{, }\StringTok{"Gabriel"}\NormalTok{, }\StringTok{"Matthew"}\NormalTok{, }\StringTok{"Connor"}\NormalTok{, }\StringTok{"Jayce"}\NormalTok{, }

\StringTok{"Isaac"}\NormalTok{, }\StringTok{"Sebastian"}\NormalTok{, }\StringTok{"Henry"}\NormalTok{, }\StringTok{"Muhammad"}\NormalTok{, }\StringTok{"Cameron"}\NormalTok{, }\StringTok{"Wyatt"}\NormalTok{, }

\StringTok{"Dylan"}\NormalTok{, }\StringTok{"Nathan"}\NormalTok{, }\StringTok{"Nicholas"}\NormalTok{, }\StringTok{"Julian"}\NormalTok{, }\StringTok{"Eli"}\NormalTok{, }\StringTok{"Levi"}\NormalTok{, }\StringTok{"Isaiah"}\NormalTok{, }

\StringTok{"Landon"}\NormalTok{, }\StringTok{"David"}\NormalTok{, }\StringTok{"Christian"}\NormalTok{, }\StringTok{"Andrew"}\NormalTok{, }\StringTok{"Brayden"}\NormalTok{, }\StringTok{"John"}\NormalTok{, }

\StringTok{"Lincoln"}

\NormalTok{}}

\end{Highlighting}

\end{Shaded}

\begin{itemize}

\tightlist

\item

Create a data frame of the same data as above except make the binary variable a factor ``DOMESTIC" vs ``FOREIGN" for 0 and 1 respectively. Use RStudio's \texttt{View} function to ensure this worked as desired.

\end{itemize}

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\end{Highlighting}

\end{Shaded}

\begin{itemize}

\tightlist

\item

Print out a table of the binary variable. Then print out the proportions of ``DOMESTIC" vs ``FOREIGN".

\end{itemize}

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\end{Highlighting}

\end{Shaded}

Print out a summary of the whole dataframe.

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\CommentTok{\#TO{-}DO}
\end{Highlighting}
\end{Shaded}

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```

\begin{itemize}
\tightlist
\item
  Let  $n = 50$ . Create a  $n \times n$  matrix  $R$  of exactly
  50% entries 0's, 25% 1's 25% 2's. These values should be in random
  locations.
\end{itemize}

```

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\end{Highlighting}
\end{Shaded}

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```

\begin{itemize}
\tightlist
\item
  Randomly punch holes (i.e.  $\sim \text{NA}$ ) values in this matrix so that
  an each entry is missing with probability 30%.
\end{itemize}

```

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\end{Highlighting}
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```
\begin{itemize}
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\tightlist
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\item
```

Sort the rows in matrix `\texttt{R}` by the largest row sum to lowest.

Be careful about the NA's!

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\end{itemize}
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\CommentTok{\#TO{-}DO}
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\end{Highlighting}
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\end{Shaded}
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```
\begin{itemize}
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\tightlist
```

```
\item
```

We will now learn the `\texttt{apply}` function. This is a handy function that saves writing for loops which should be eschewed in R.

Use the apply function to compute a vector whose entries are the standard deviation of each row. Use the apply function to compute a vector whose entries are the standard deviation of each column. Be careful about the NA's! This should be one line.

```
\end{itemize}
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\begin{Highlighting}[]
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\CommentTok{\#TO{-}DO}
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\end{Highlighting}
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\begin{itemize}
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\tightlist
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\item
```

Use the `\texttt{apply}` function to compute a vector whose entries are the count of entries that are 1 or 2 in each column. This should be one line.

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\end{itemize}
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\begin{Highlighting}[]
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\CommentTok{\#TO{-}DO}
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\end{Highlighting}
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\end{Shaded}
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\begin{itemize}
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\tightlist
```

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\item
```

Use the `\texttt{split}` function to create a list whose keys are the column number and values are the vector of the columns. Look at the last example in the documentation `\texttt{?split}`.

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\end{itemize}
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\end{Highlighting}
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\end{Shaded}
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\begin{itemize}
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\tightlist
```

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\item
```

In one statement, use the `\texttt{lapply}` function to create a list whose keys are the column number and values are themselves a list with keys: `"min"` whose value is the minimum of the column, `"max"` whose value is the maximum of the column, `"pct_missing"` is the proportion of missingness in the column and `"first_NA"` whose value is the row number of the first time the NA appears.

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\end{itemize}
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\CommentTok{\#TO{-}DO}
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\end{Highlighting}
```

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\end{Shaded}
```

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\begin{itemize}
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\tightlist
```

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\item
```

Set a seed and then create a vector `\texttt{v}` consisting of a sample of 1,000 iid normal realizations with mean -10 and variance 100.

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\end{itemize}
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```
\begin{Highlighting}[]
```



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\CommentTok{\#TO{-}DO}
```

```
\end{Highlighting}
```

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\end{Shaded}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Repeat this exercise by resetting the seed to ensure you obtain the same results.

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\end{itemize}
```

```
\begin{Shaded}
```

```
\begin{Highlighting}[]
```

```
\CommentTok{\#TO{-}DO}
```

```
\end{Highlighting}
```

```
\end{Shaded}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Find the average of \texttt{v} and the standard error of \texttt{v} .

```
\end{itemize}
```

```
\begin{Shaded}
```

```
\begin{Highlighting}[]
```

```
\CommentTok{\#TO{-}DO}
```

```
\end{Highlighting}
```

```
\end{Shaded}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

Find the 5\%ile of v and use the $qnorm$ function to compute what it theoretically should be. Is the estimate about what is expected by theory?

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\end{itemize}
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\begin{Shaded}
```

```
\begin{Highlighting}[]
```

```
\CommentTok{\#TO{-}DO}
```

```
\end{Highlighting}
```

```
\end{Shaded}
```

```
\begin{itemize}
```

```
\tightlist
```

```
\item
```

What is the percentile of v that corresponds to the value 0?

What should it be theoretically? Is the estimate about what is expected by theory?

```
\end{itemize}
```

```
\begin{Shaded}
```

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\begin{Highlighting}[]
```

```
\CommentTok{\#TO{-}DO}
```

```
\end{Highlighting}
```

```
\end{Shaded}
```

\end{document}