

Lab 5: Regression

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Regression with an indicator independent variable

First, let's practice the mechanics of running a regression in R. As you've seen, there are different ways to do this. For most applications, `lm()` is sufficient, but there may be situations in which you want to use the `estimatr` package. We will practice the syntax for both.

First, we need some data. Let's practice with `mtcars`.

```
car_data <- mtcars
```

Let's say that we are interested in exploring the relationship between transmission and fuel economy. Let's regress `mpg` onto `am`.

```
model_1 <- lm(car_data, formula = mpg ~ am)
```

```
summary(model_1)
```

```
##
## Call:
## lm(formula = mpg ~ am, data = car_data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.3923 -3.0923 -0.2974  3.2439  9.5077
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   17.147      1.125   15.247 1.13e-15 ***
## am              7.245      1.764    4.106 0.000285 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.902 on 30 degrees of freedom
## Multiple R-squared:  0.3598, Adjusted R-squared:  0.3385
## F-statistic: 16.86 on 1 and 30 DF,  p-value: 0.000285
```

We have a slope and intercept, but what do they mean? That depends on what form the independent variable takes and what the specific values represent. Let's check the documentation.

```
?mtcars
```

```
## starting httpd help server ... done
```

What values does `am` take in the data? What do those values represent?

YOUR ANSWER HERE

Now that we understand what the variable represents, let's interpret our results. One way we can do this, which is especially helpful when we have multiple independent variables is to think about the functional form (or "prediction equation") of our regression. In this case it would be something like:

$$\text{mpg} = b + mD_i$$

where $D_i = 0$ if the car has automatic transmission and $D_i = 1$ if it has a manual transmission.

As discussed in lecture, when we have a regression that is structured this way, the intercept is equal to the mean of the "untreated" category and the slope is the difference in means. Can you verify this?

YOUR CODE HERE

Extracting info from a regression

Notice that there is a lot more information stored in the object `model_1` than just the coefficients. For example, the fitted values and residuals. The fitted values are the Y_i generated for each observation by the model and the residuals are the difference between the fitted values and observed values.

If you take Linear Models in the winter quarter, you will talk in great detail about residuals and what they can tell you. For now just know that you can retrieve them from your model:

```
my_resid_1 <- model_1$residuals
```

Since we have the residuals and the fitted values, we should be able to recreate the original `mpg` column. See if you can recreate the `mpg` column and verify that they are the same.

YOUR CODE HERE

Adding a predictor

Let's think more critically about the regression we ran above. There's an apparent association between transmission type and miles per gallon. Do you have any concerns about this conclusion? This data is pretty old (1981 I believe), so automatic transmissions were less common and more expensive than today. Taking a quick glance at the data, it appears that some of the cars with the largest engines (by displacement) have automatic transmissions and some of cars with the smallest engines have manual transmissions. It is possible that engine size is a confounder, influencing both the choice of transmission (maybe car manufacturers wanted smoother shifting in their more powerful, expensive cars) and the fuel economy (bigger engines consume more fuel). So, let's incorporate engine size on fuel economy into the model.

To make the interpretation easier, let's create a new indicator variable called `sport` which takes on the value 1 if the displacement is greater than 250 cubic inches.

YOUR CODE HERE

Now, let's run the regression again, but include `sport`. Use `lm_robust()` from `estimatr` instead of `lm`.

YOUR CODE HERE

What happened to the intercept and coefficient on `am`? What does the coefficient on `sport` mean? What happened to the value of R^2 ?

Interaction terms

Let's suppose we hypothesize that manual transmission sports cars are less fuel efficient and manual transmission non-sports cars are more fuel efficient. We might think that in non-sports cars, manual transmissions are found on the cheapest models which also have the smallest engines and are lightest, leading to better fuel economy. For sports cars, maybe manual transmissions are primarily found in beefy American

muscle cars, which are less fuel efficient than their more refined automatic transmission equipped European counterparts. One way to get at this is to add an *interaction term*.

The way to add an interaction term to your model is by including the product of two independent variables. Again, let's use `lm_robust()`.

YOUR CODE HERE

Interpret the results. The functional form of this model is now:

$$\text{mpg} = 20.633 + 5.394(\text{am}) - 5.095(\text{sport}) - 5.532(\text{am})(\text{sport})$$

where `am` and `sport` are either 0 or 1. What does our model predict the fuel economy of an automatic sports car is? Automatic non-sports car? Manual sports car? Manual non-sports car?

Regression with continuous independent variables

So far, we've been working with indicator variables, which have coefficients that are easy to interpret. You're most likely to encounter these variables in experimental contexts. Unfortunately most social science research is not so neat or easy to interpret. Continuous variables are everywhere we look in the real world, and frequently find their way into our models.

Let's look back one of the plots we generated in Lab 1 using the UK coal data. If the code below doesn't work for you, you can save the csv locally (the data is in the course GitHub repo) and read it in.

```
data_path <- "https://raw.githubusercontent.com/aeggers/IntroQSS-F21/main/data/"

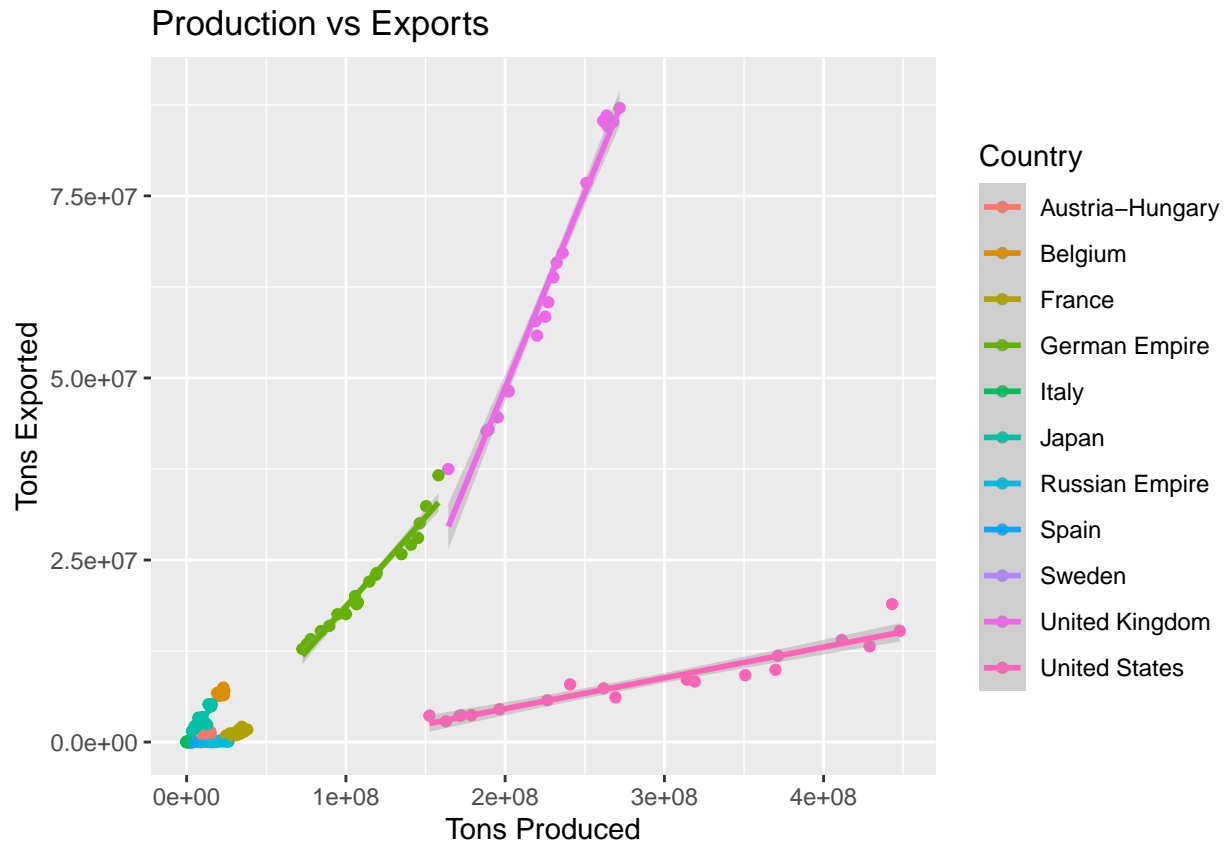
coal_data <- read_csv(str_c(data_path, "uk_coal_tables.csv"),
                      col_types = "cddddddd",
                      na = "N/A")
```

Remember this plot that we produced:

```
plot_1 <- ggplot(data = coal_data,
                 mapping = aes(x = Tons_Produced,
                               y = Tons_Exported,
                               color = Country)) +
  geom_point() +
  geom_smooth(method = "lm") +
  labs(x = "Tons Produced",
       y = "Tons Exported",
       title = "Production vs Exports")
```

plot_1

```
## `geom_smooth()` using formula 'y ~ x'
## Warning: Removed 2 rows containing non-finite values (stat_smooth).
## Warning: Removed 2 rows containing missing values (geom_point).
```



We colored by country because there seemed to be clusters of points that were behaving differently. Each line represents an OLS regression for a specific country. Use your data wrangling skills and the ggplot code above to find the slope and intercept of the regression for the United Kingdom.

YOUR CODE HERE

Interpret the results (remember that the independent variable is continuous). Does the intercept make sense? What does this tell us about this model's ability to generate out of sample predictions? Notice the R^2 value. Does it tell us anything about whether this is a "good" model?

Final project brainstorming

Brainstorm a regression you might want to add to your final project. What are the independent and dependent variables? Are they continuous or categorical? How would you interpret your regression coefficient?