

The following exercises provide more exposure to Scheme.

1. Implement fully the Complex Number representation we discussed in class. In particular, besides the function `real_part`, `complex_part` and `make_complex` we defined in class, you should implement the following definitions. Whereever you see a parameter with **num** in it, we are assuming it is a complex number.

`(complex num)` implements the operation $\overline{x + yi}$ from the handout.

`(abs num)` implements the operation $|x + yi|$ from the handout.

`(equal? num1 num2)` returns `#t` if `num1` and `num2` represent the same complex number and returns `#f` otherwise.

`(plus num1 num2)` implements the operation $(x_1 + y_1i) + (x_2 + y_2i)$ from the handout.

`(minus num1 num2)` implements the operation $(x_1 + y_1i) - (x_2 + y_2i)$ from the handout.

`(prod num1 num2)` implements the operation $(x_1 + y_1i) \times (x_2 + y_2i)$ from the handout.

`(quotient num1 num2)` implements the operation $\frac{x_1 + y_1i}{x_2 + y_2i}$ from the handout.

2. Define a function `permutation?` that takes as parameters two lists, `list1` and `list2` and returns `#t` if the lists are permutations of one another, and returns `#f` otherwise. Thus

`(permutation? '(1 3 2) '(3 1 2))` would return `#t`

`(permutation? '(1 3 2) '(1 2))` would return `#f`

`(permutation? '(1 3 3) '(1 3 2))` would return `#f`

`(permutation? '(1 3 2) '(1 2 3 a))` would return `#f`

Note that `(permutation? '() '())` would return `#t`.

You may assume as known any functions we defined in class or in an assignment, so you do not have to redefine these.

3. We can represent a binary tree in Scheme as follows:

- `()` will represent the empty tree; otherwise
- Each node of a binary tree non-empty tree will be of the form `(atom list1 list2)`, where `atom` represents the nodes value and `list1` and `list2` are lists (possibly empty) representing the left and right subtrees respectively; for example

`(a (b ()) (c () ())) (d () (e (f () ()) ()))`

- a. Define a function `tree?` that accepts a list as an argument and returns `#t` if the list is a tree and `#f` otherwise.
- b. Define a function `preorder` that accepts a tree as a parameter and returns a list containing the node values of the tree based on a preorder traversal. When applied to the above tree, `preorder` would return the list `(a b c d e f)`
- c. Same as b. except give an `inorder` traversal. When applied to the above tree, `inorder` would return the list `(b c a d f e)`
- d. Same as b. and c. except give a `postorder` traversal. When applied to the above tree, `postorder` would return the list `(c b f e d a)`