

## Purpose

This document extends the analysis of spatial autocorrelation from the document titled `Testing_spatial_subsampling.Rmd` to the statistical analysis of spatial correlations with semivariograms. Instead of just visually assessing the spatial autocorrelation in the reconstructions, we can fit empirical variograms to the reconstructions at each time step for each taxon.

## Semivariances

First, I used the `semivariogram` function from the `gstat` package to fit spherical, exponential, and Gaussian variograms to each taxon at each time period. This function returns the semivariances of the relative abundances, as well as the sill, nugget, and range parameter estimates. The range is an estimate of how far away the grid cells need to be to be considered independent. The ratio of nugget:sill is an indicator of the strength of spatial dependence in the relative abundance, with high ratio (>75%) indicative of low spatial dependence.

Since I replaced the x-y distances with cell number, the distance and range can be interpreted as number of cells in the following analysis.

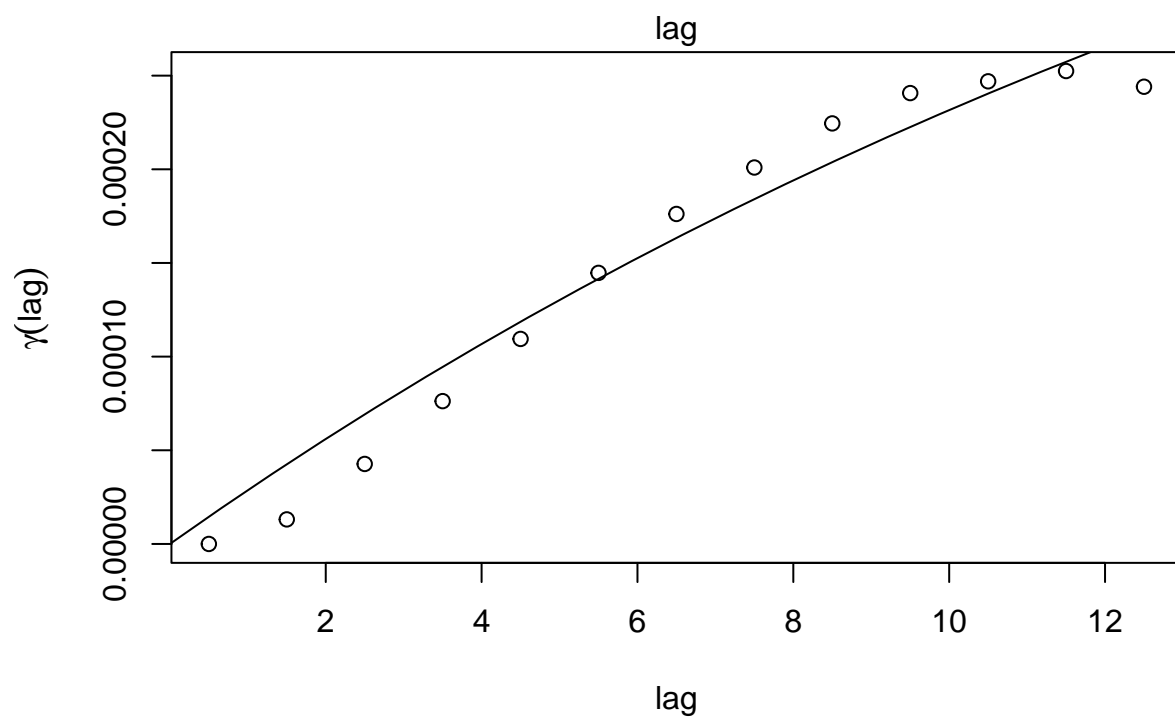
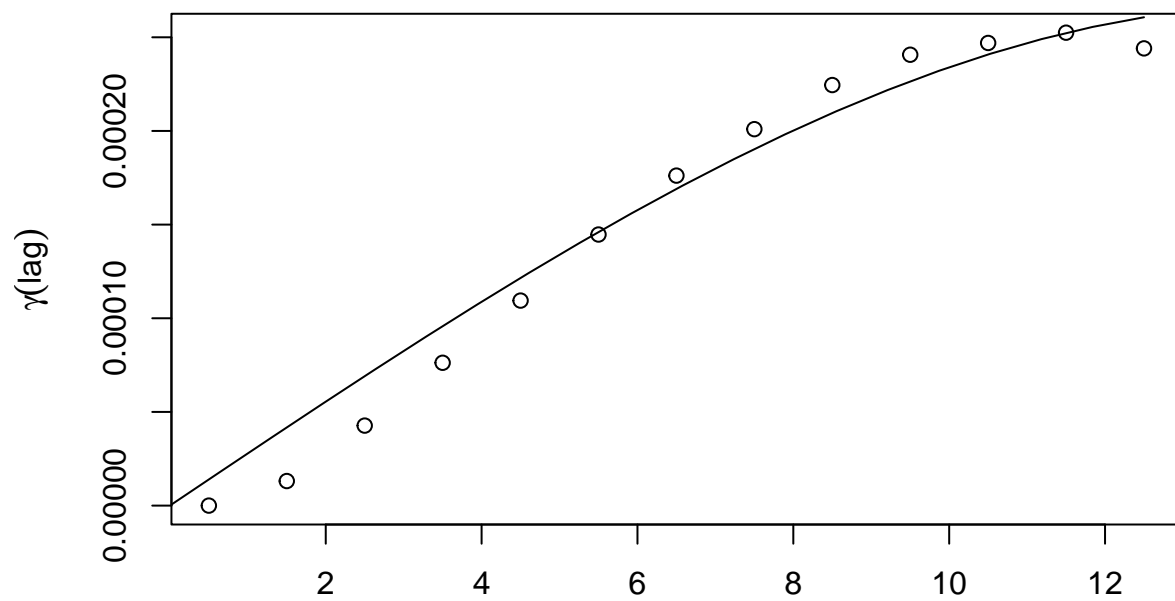
My expectation is that of these three options, the Gaussian variogram will be the best fit because this is the closest to the nugget used for model fitting, but the actual nugget is an inverse power law kernel, which I believe is the same as the powered exponential kernel.

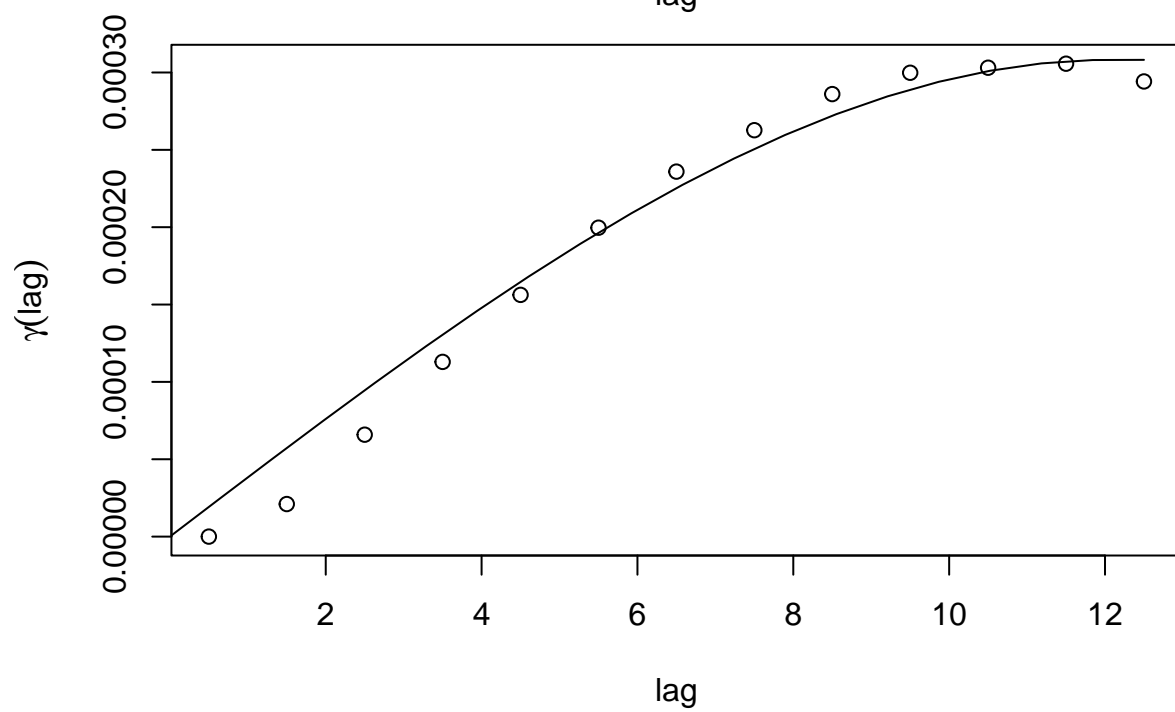
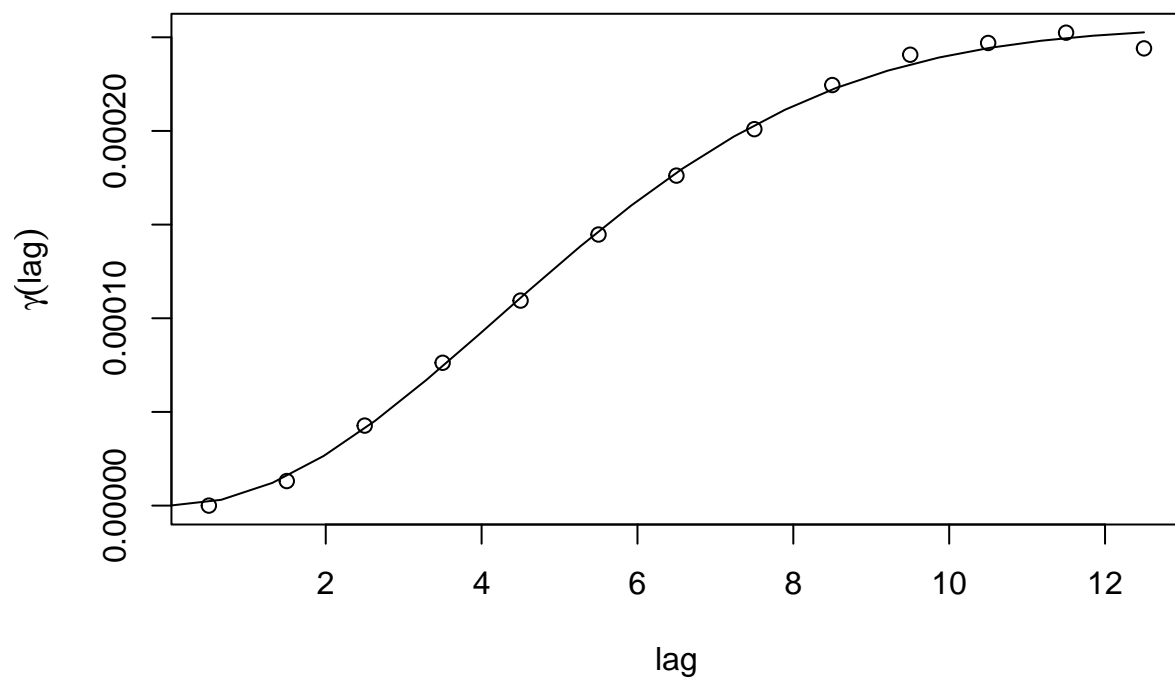
```
ash_spherical_params <- matrix(, nrow = length(time), ncol = 4)
ash_exponential_params <- matrix(, nrow = length(time), ncol = 4)
ash_gaussian_params <- matrix(, nrow = length(time), ncol = 4)

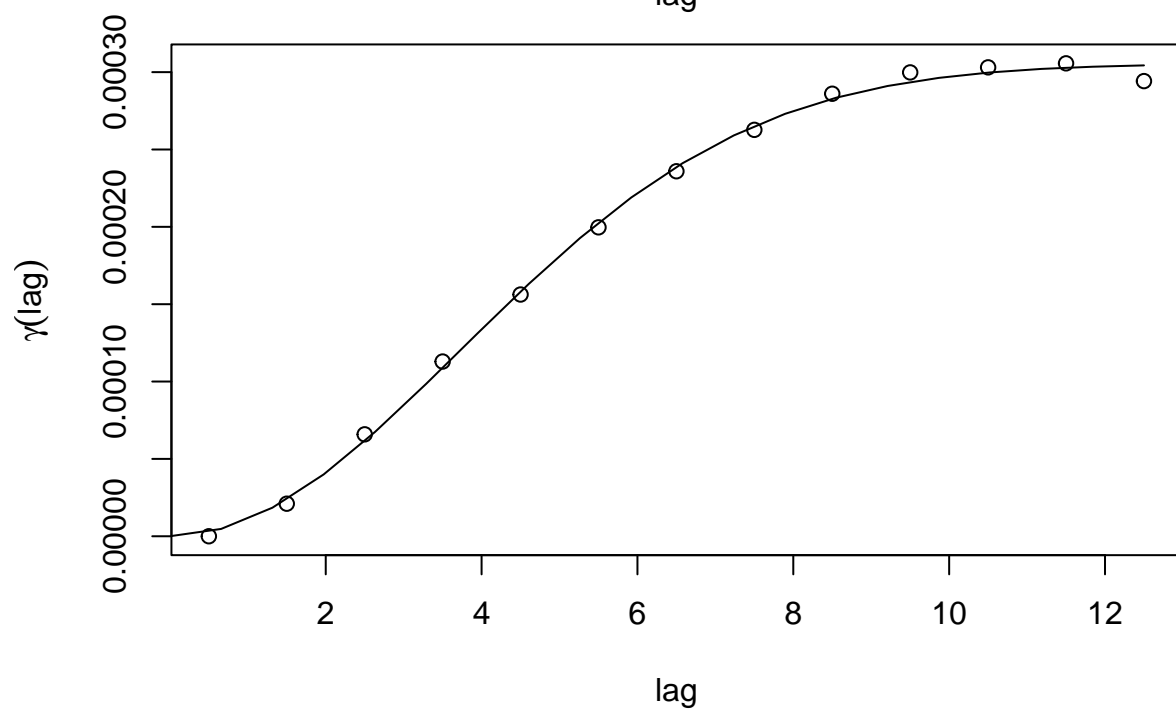
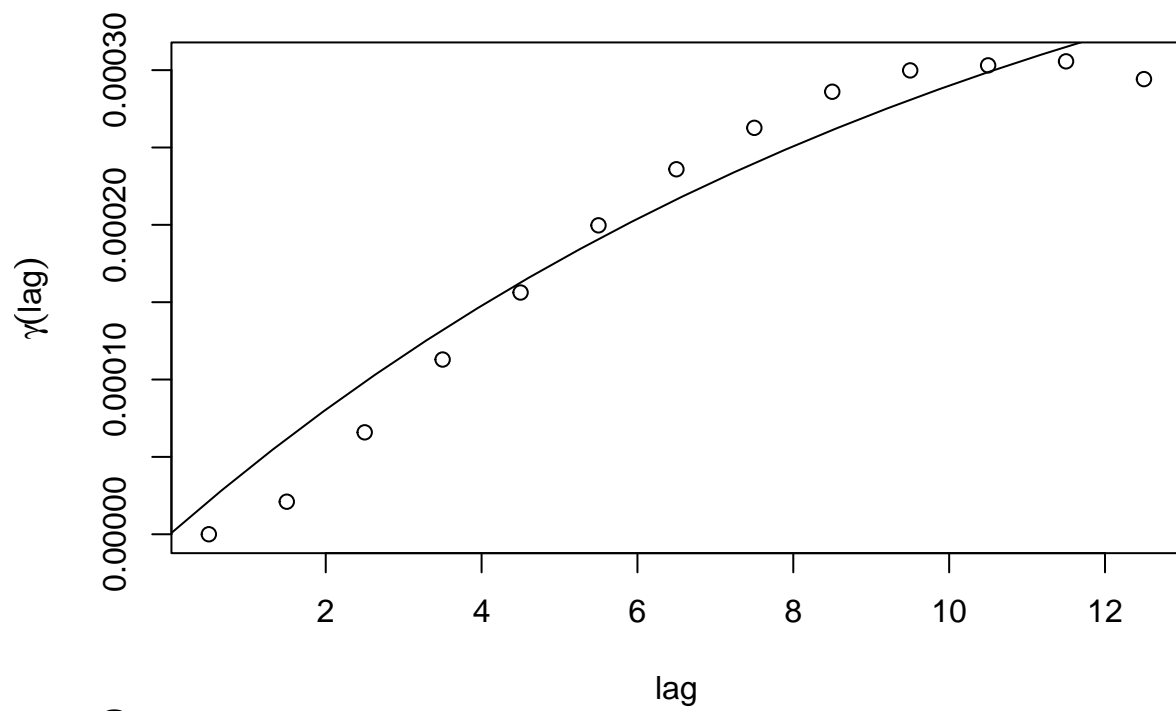
for(i in 1:length(time)){
  t <- time[i]
  sub <- dplyr::filter(ash_melt,
                      time == t,
                      !is.na(ash))
  sv <- geostats::semivariogram(x = sub$x, y = sub$y, z = sub$ash,
                              model = 'spherical')
  ash_spherical_params[i,1] <- t
  ash_spherical_params[i,2:4] <- sv$snr

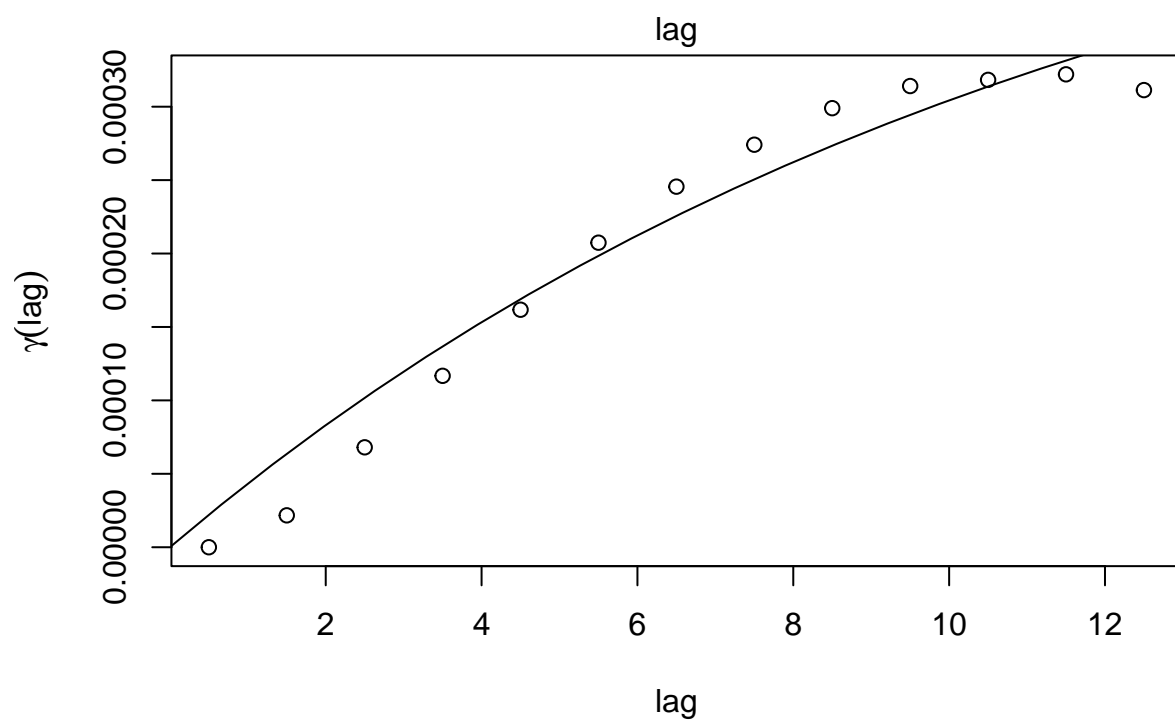
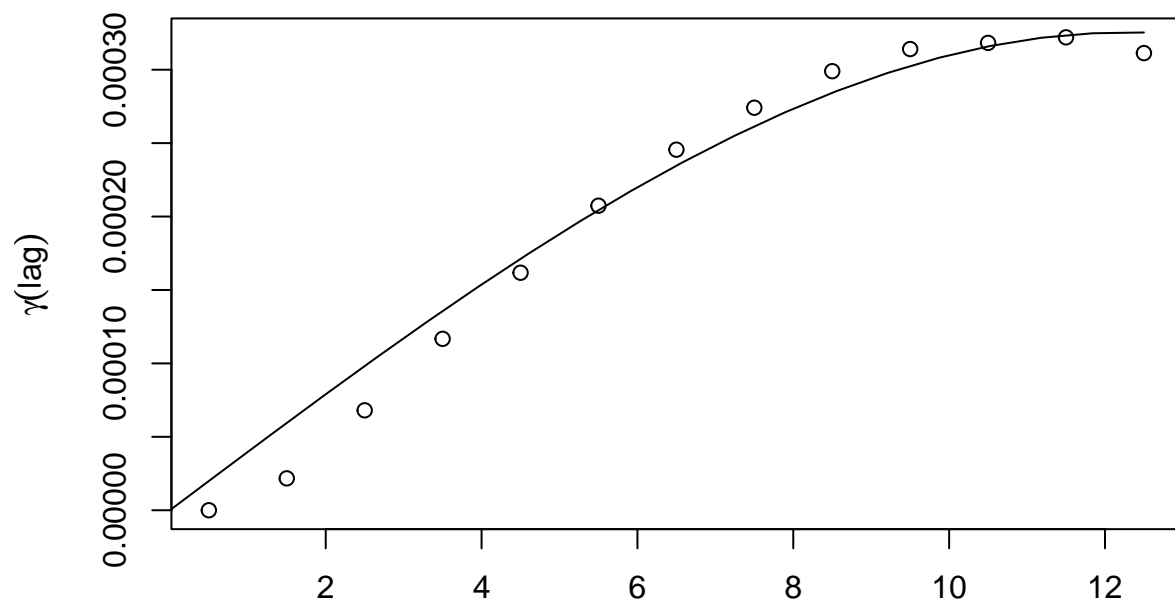
  sv <- geostats::semivariogram(x = sub$x, y = sub$y, z = sub$ash,
                              model = 'exponential')
  ash_exponential_params[i,1] <- t
  ash_exponential_params[i,2:4] <- sv$snr

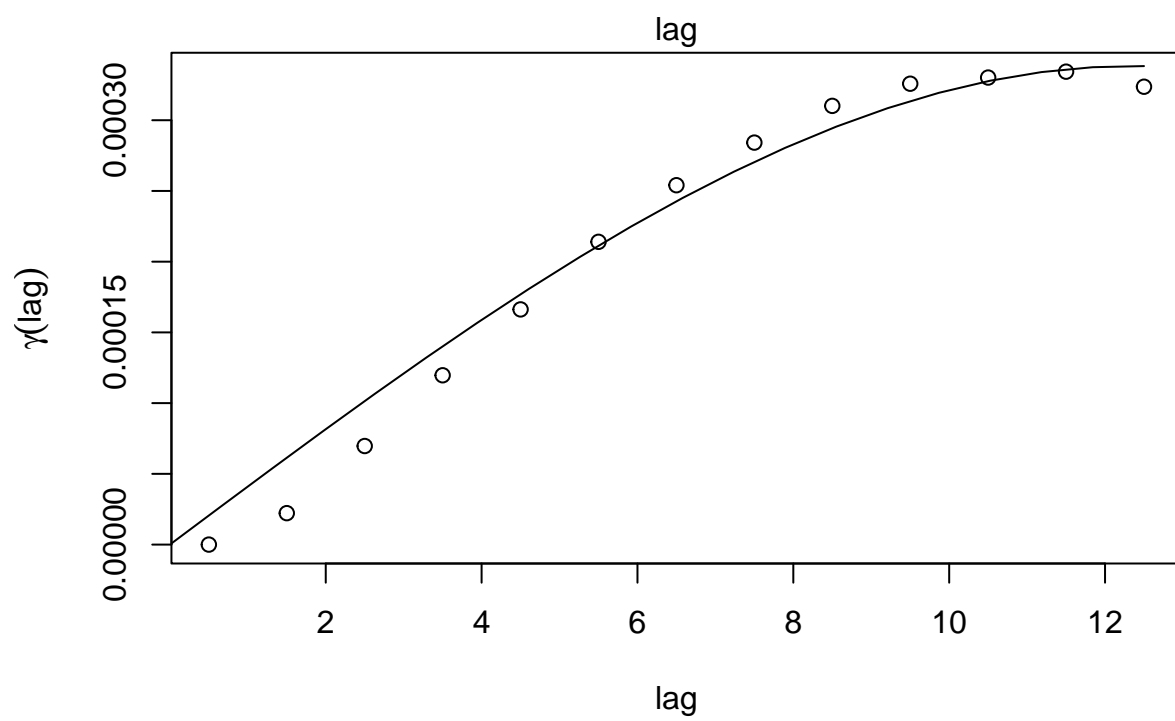
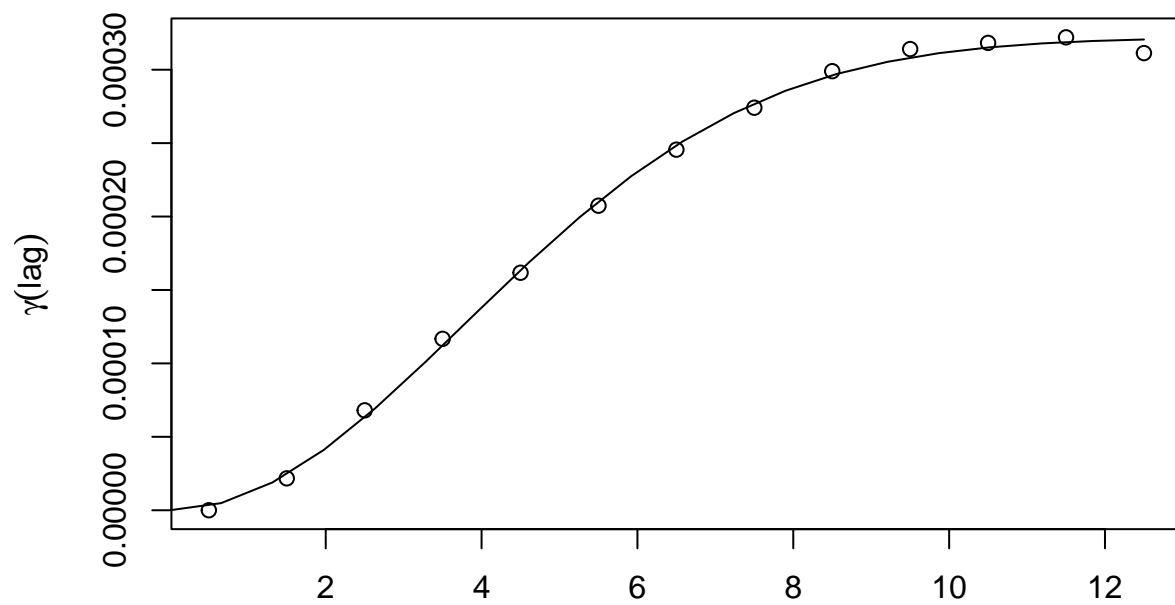
  sv <- geostats::semivariogram(x = sub$x, y = sub$y, z = sub$ash,
                              model = 'gaussian')
  ash_gaussian_params[i,1] <- t
  ash_gaussian_params[i,2:4] <- sv$snr
}
```

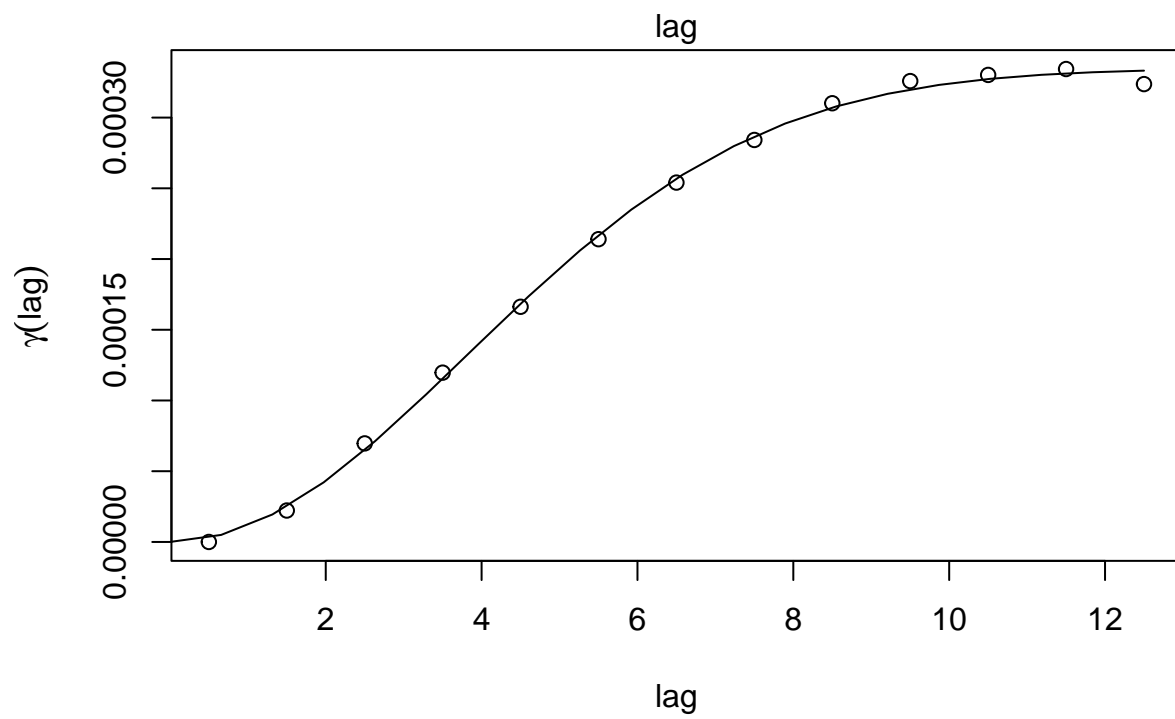
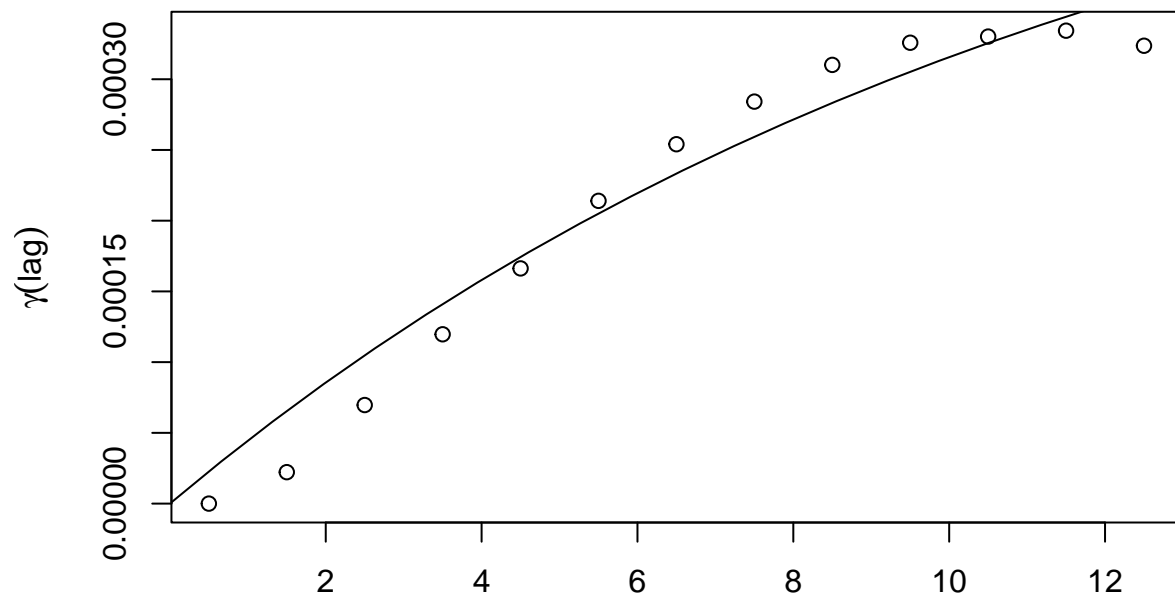


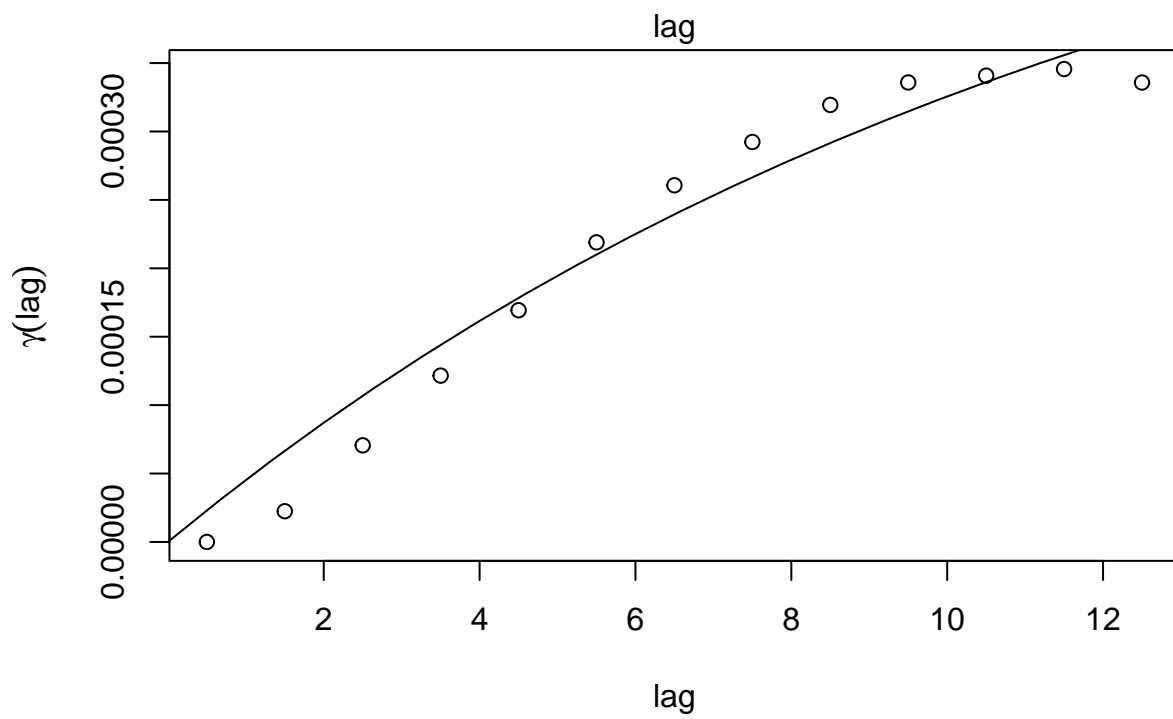
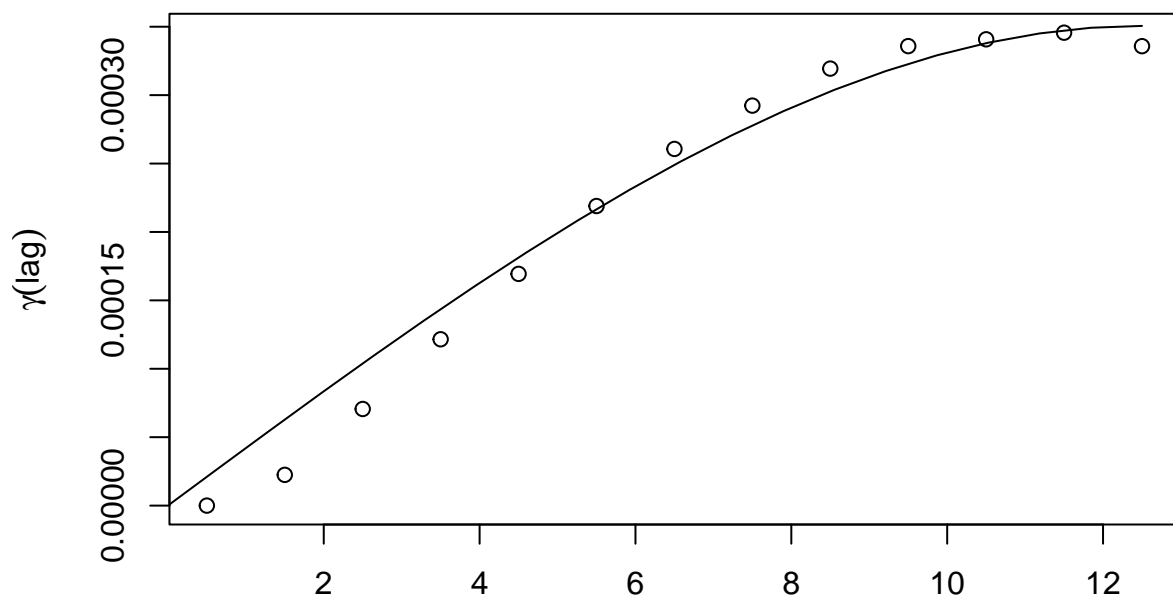




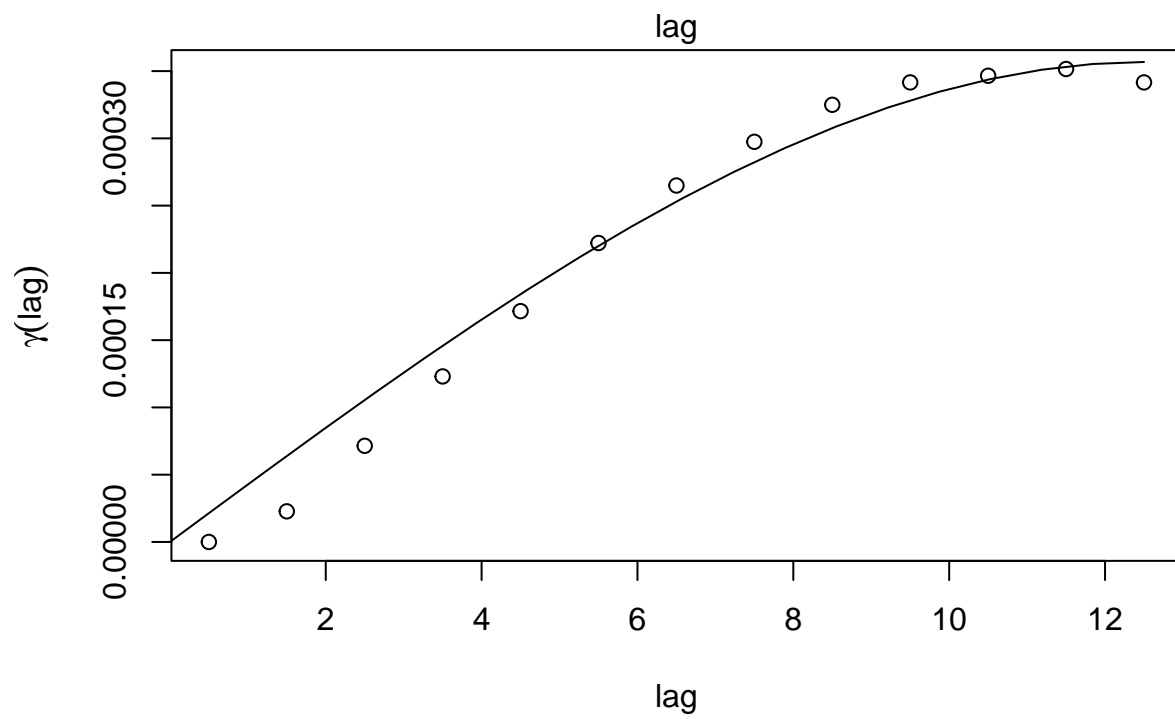
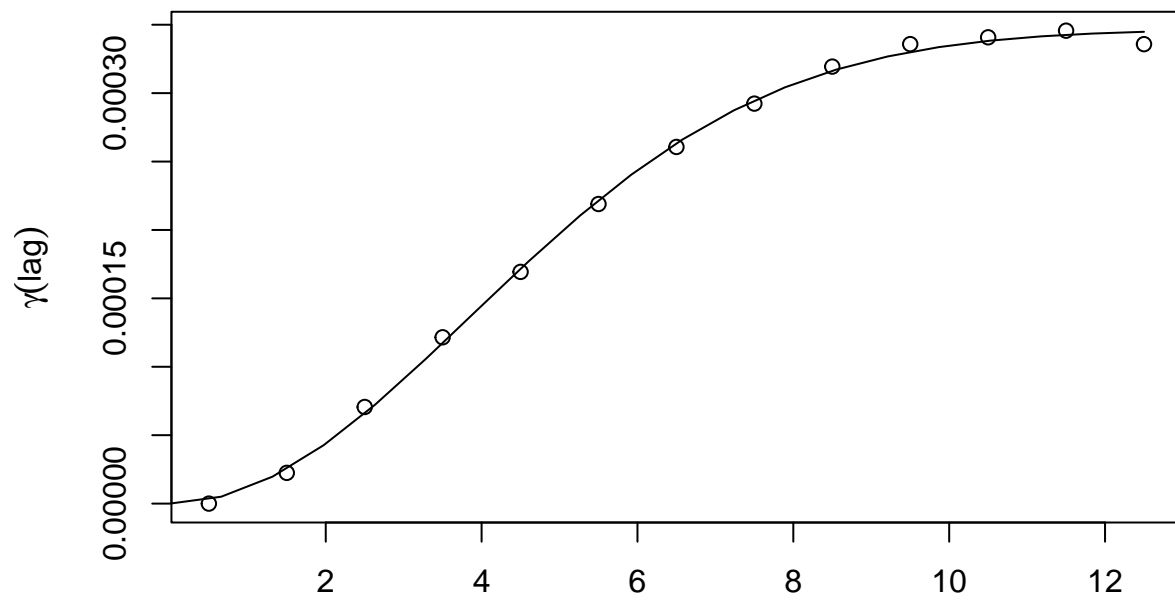


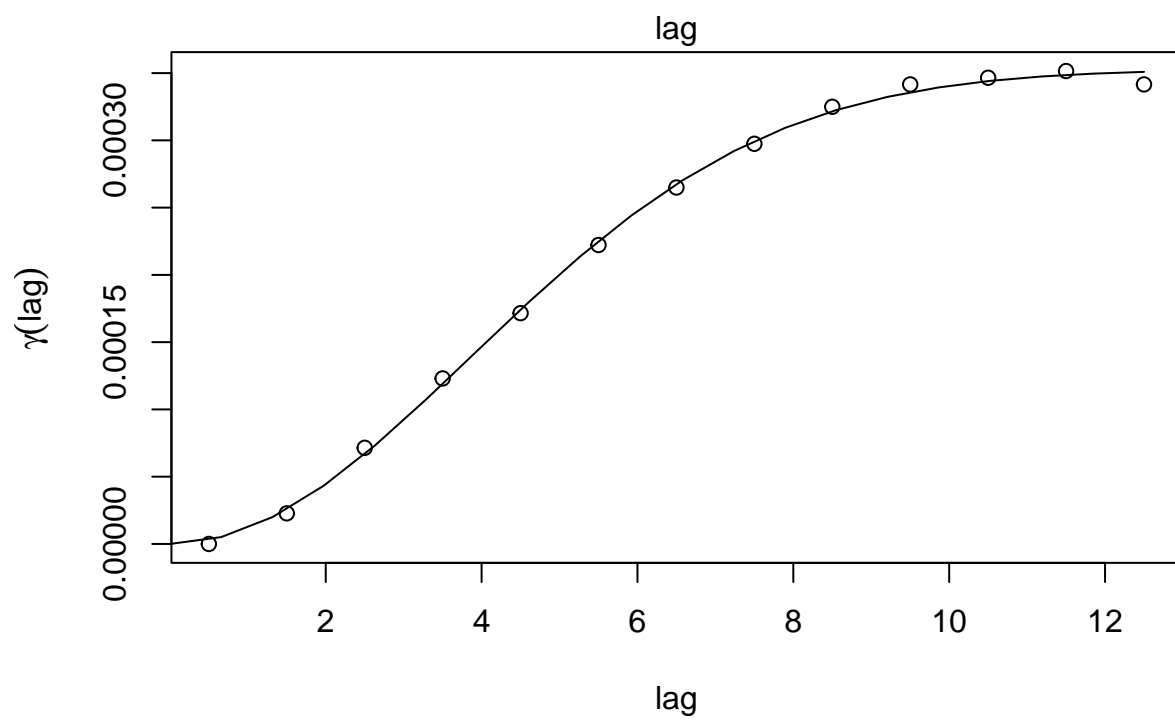
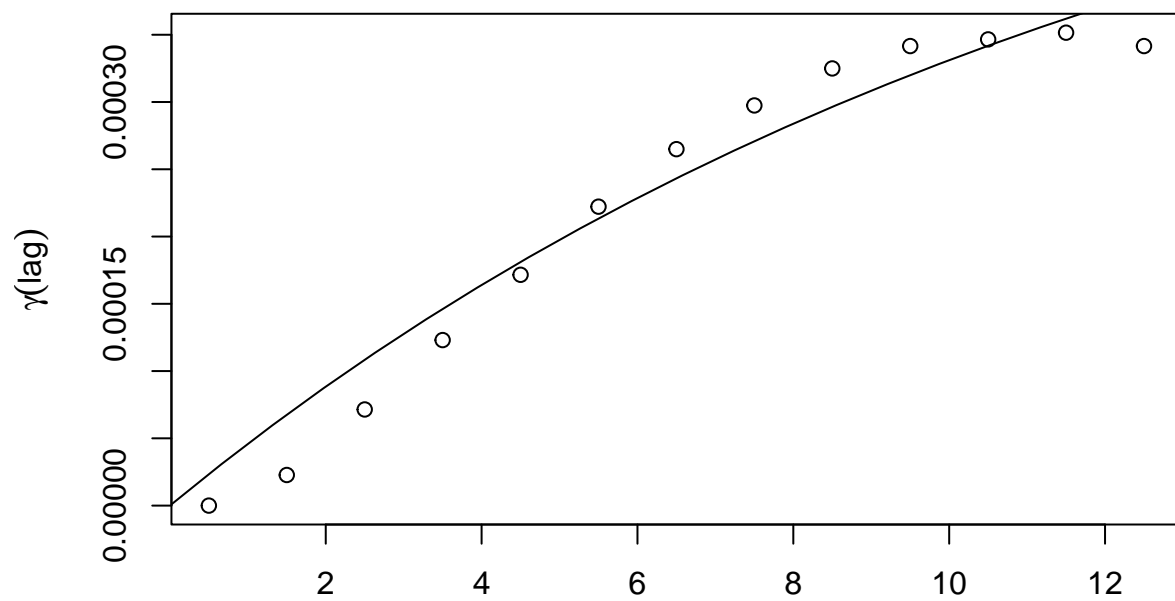


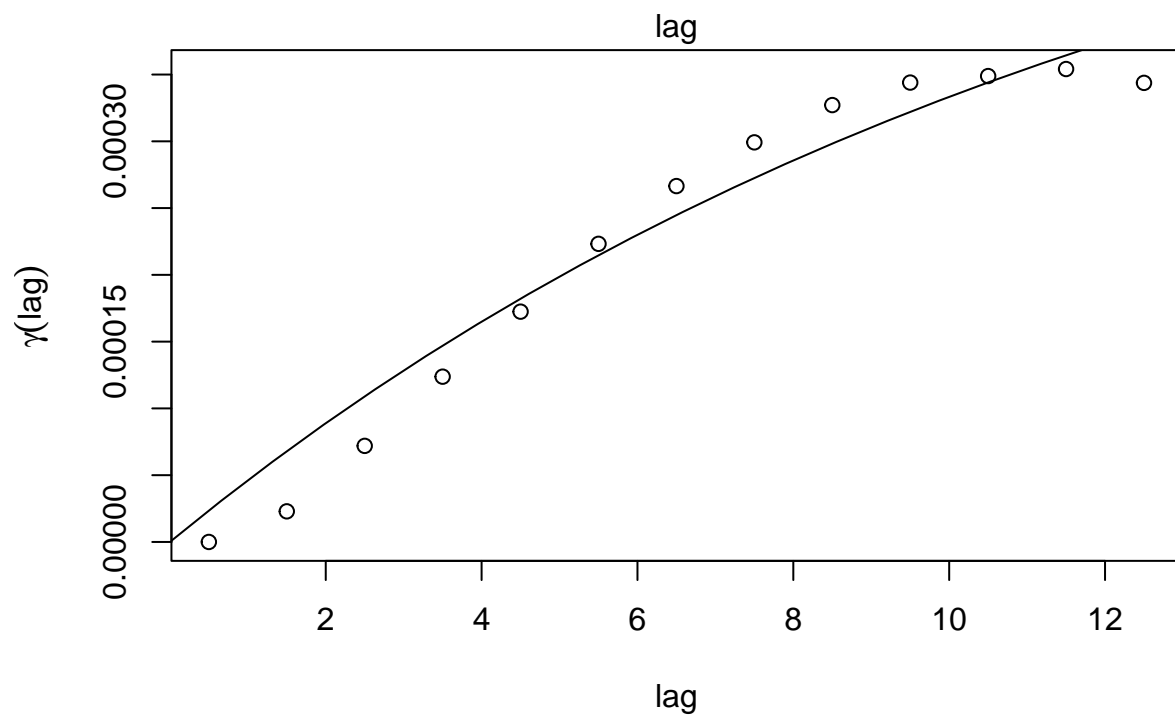
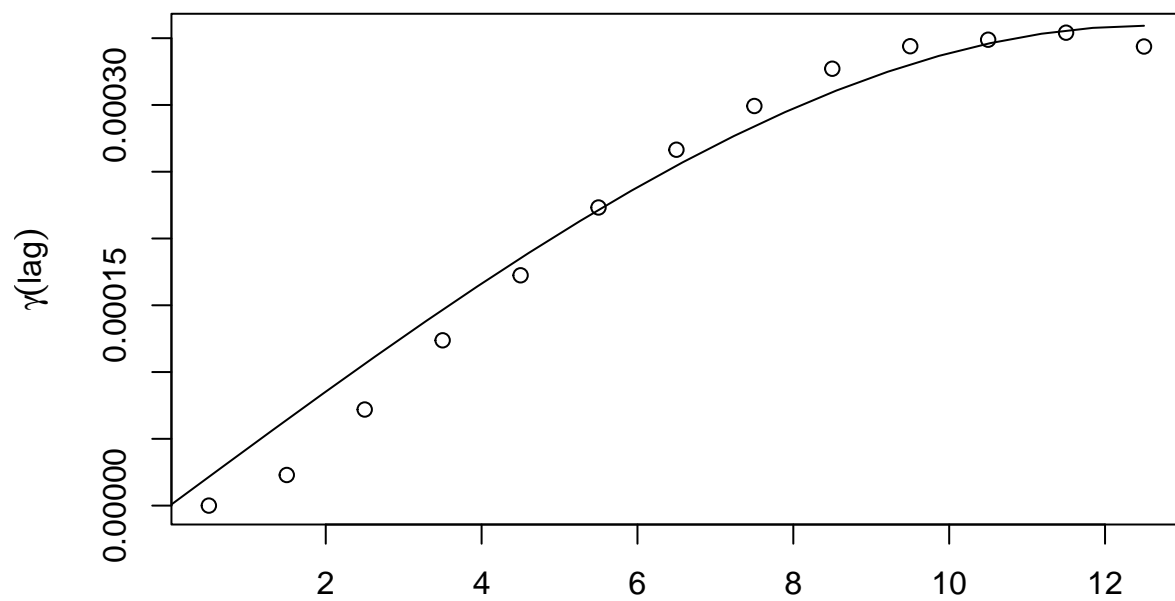


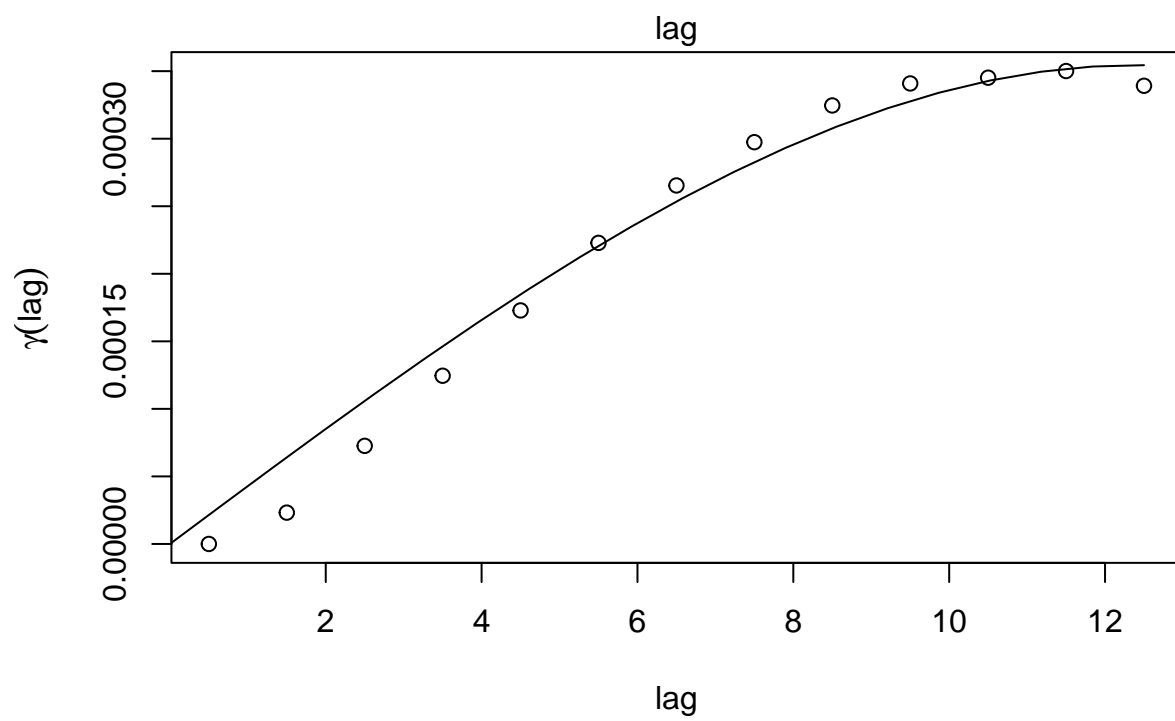
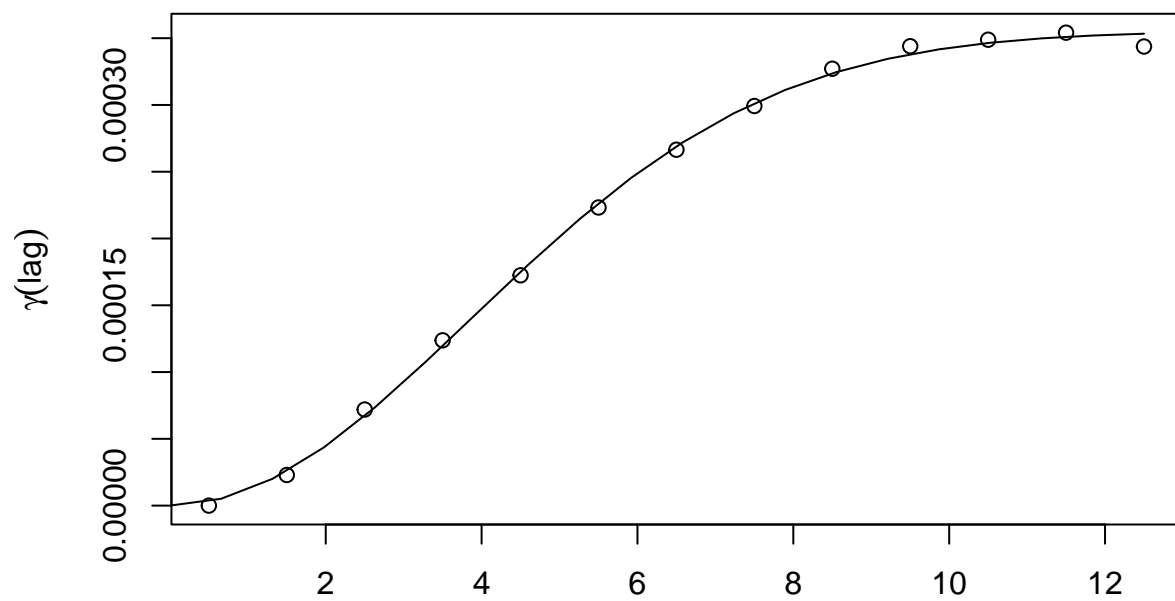


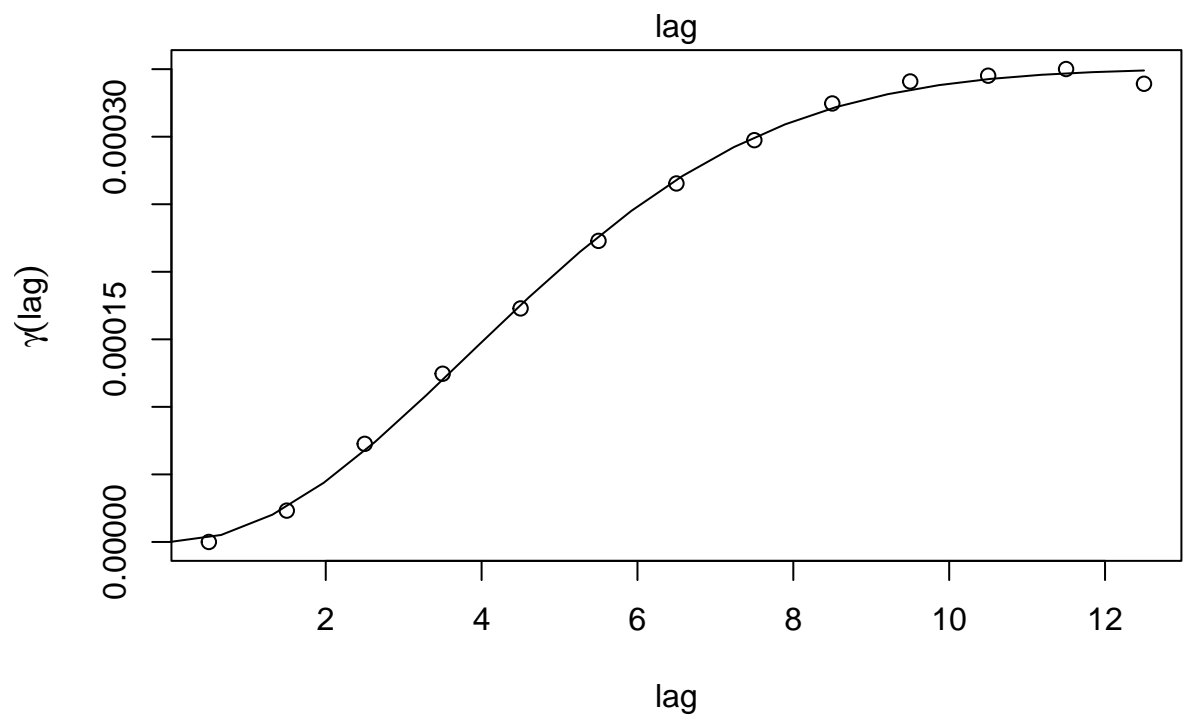
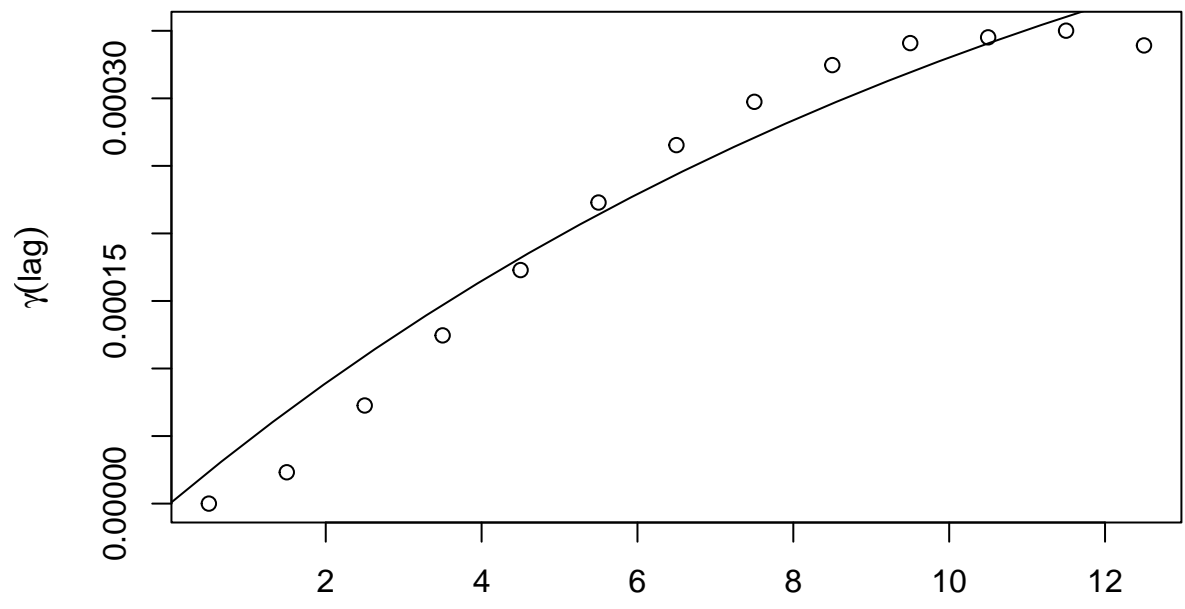


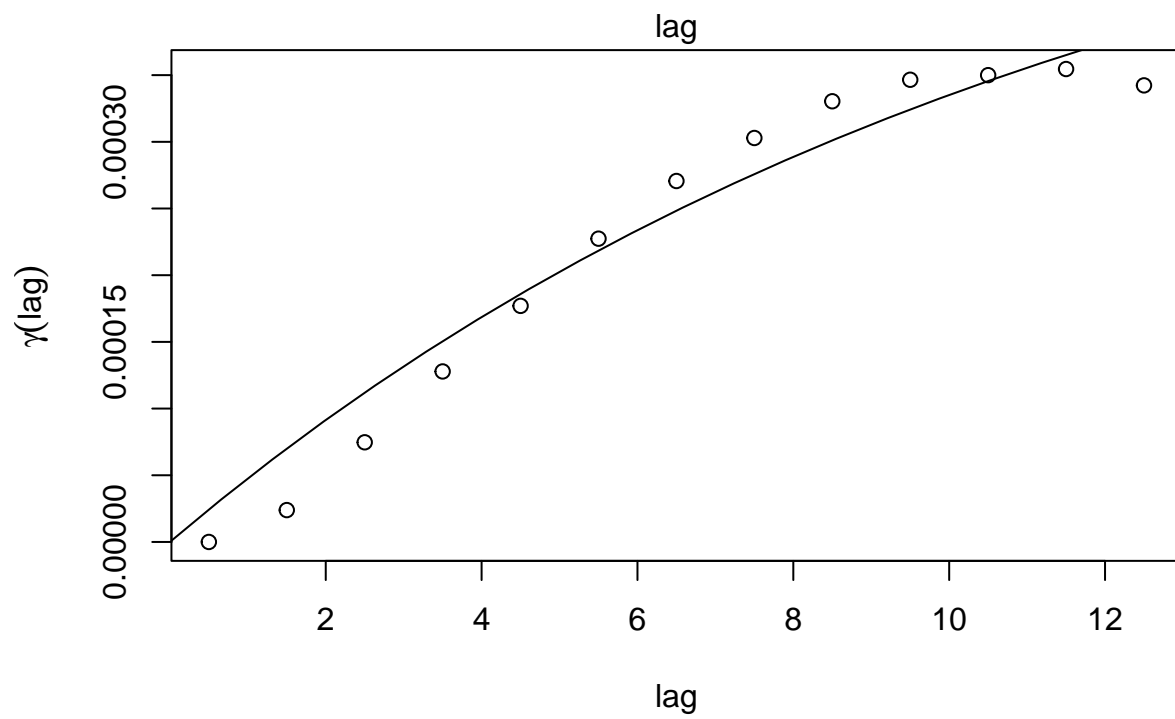
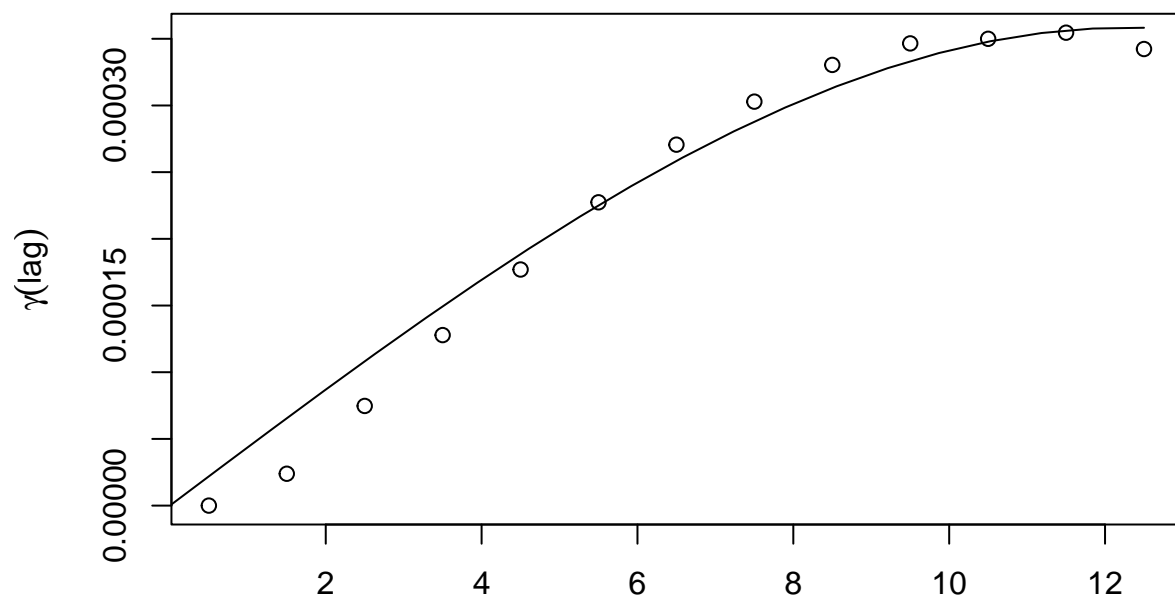


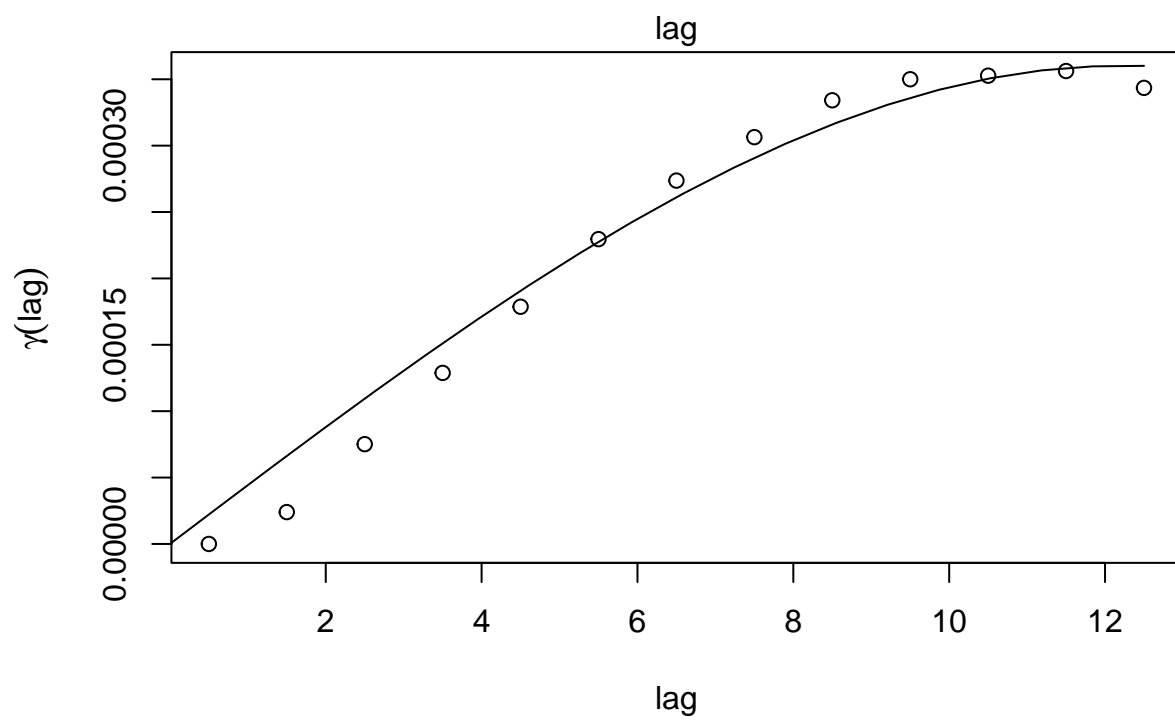
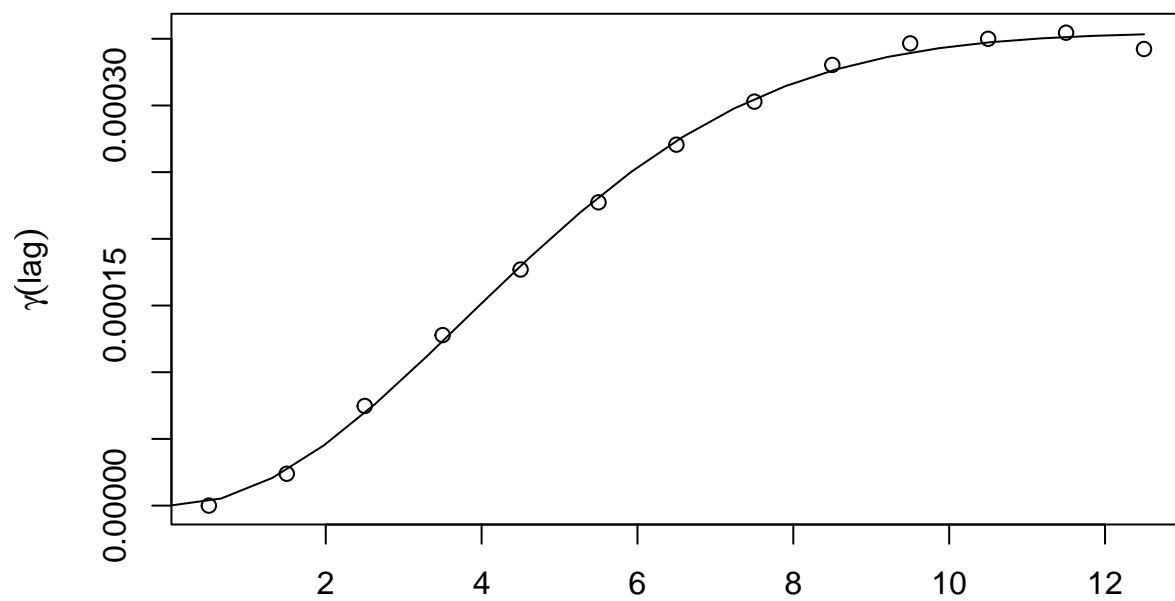


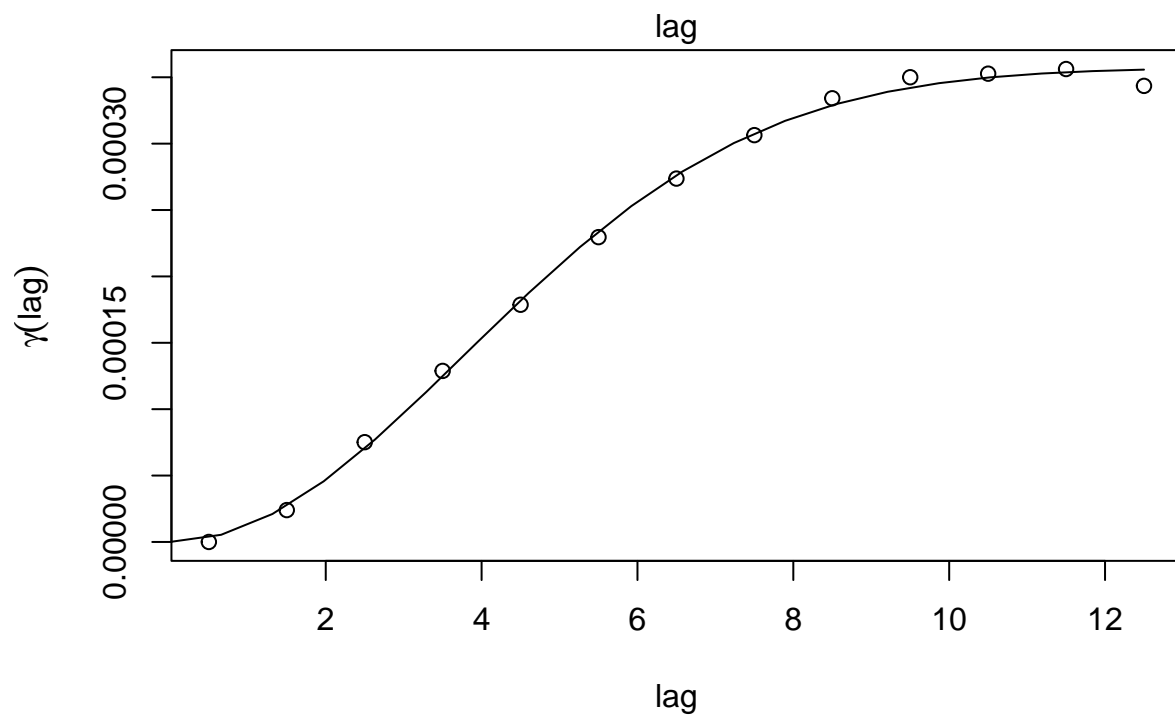
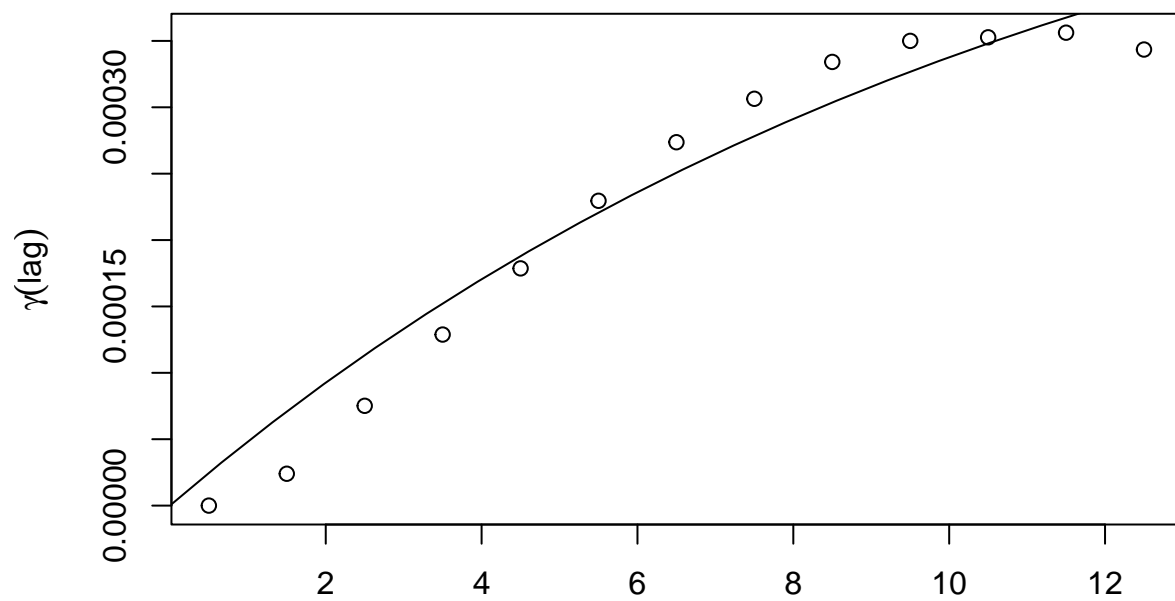




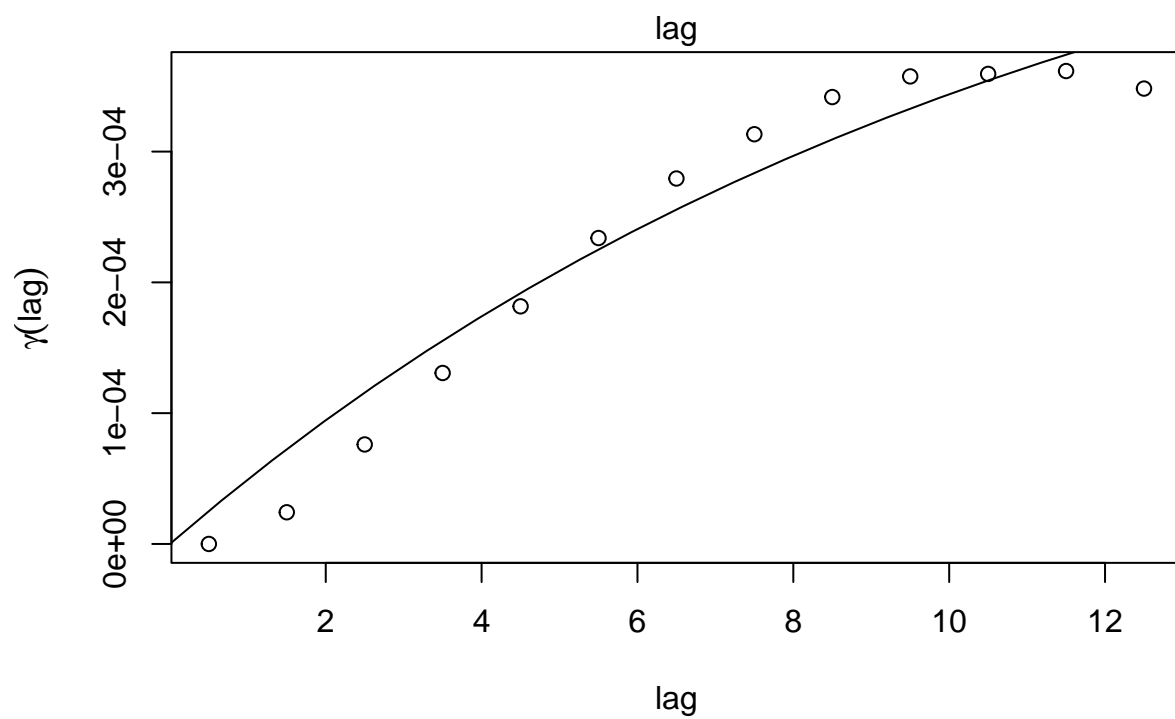
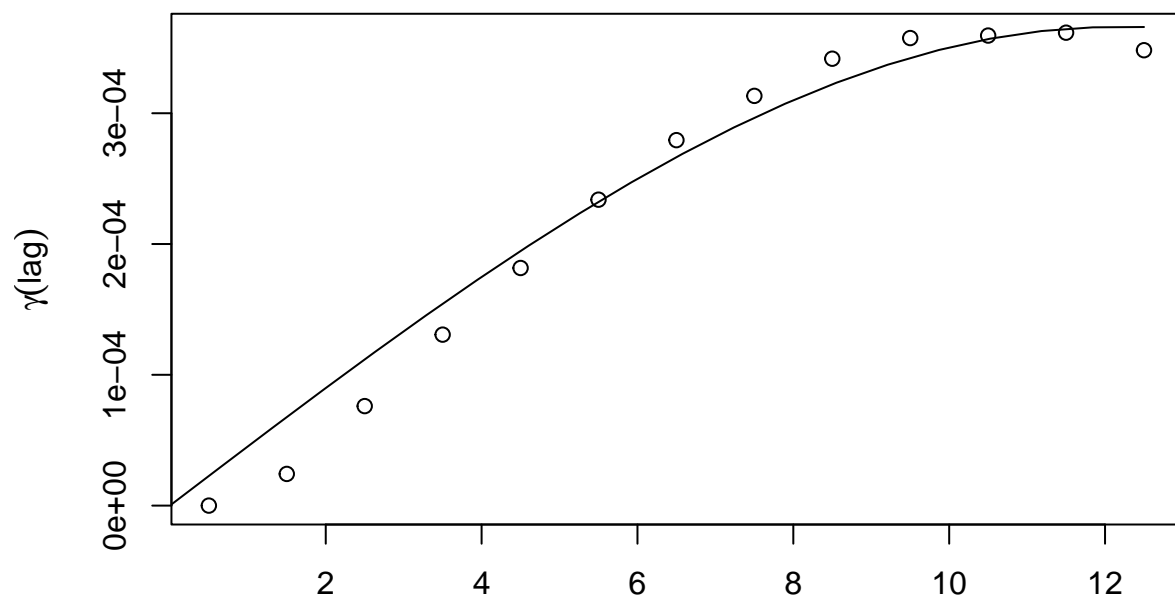


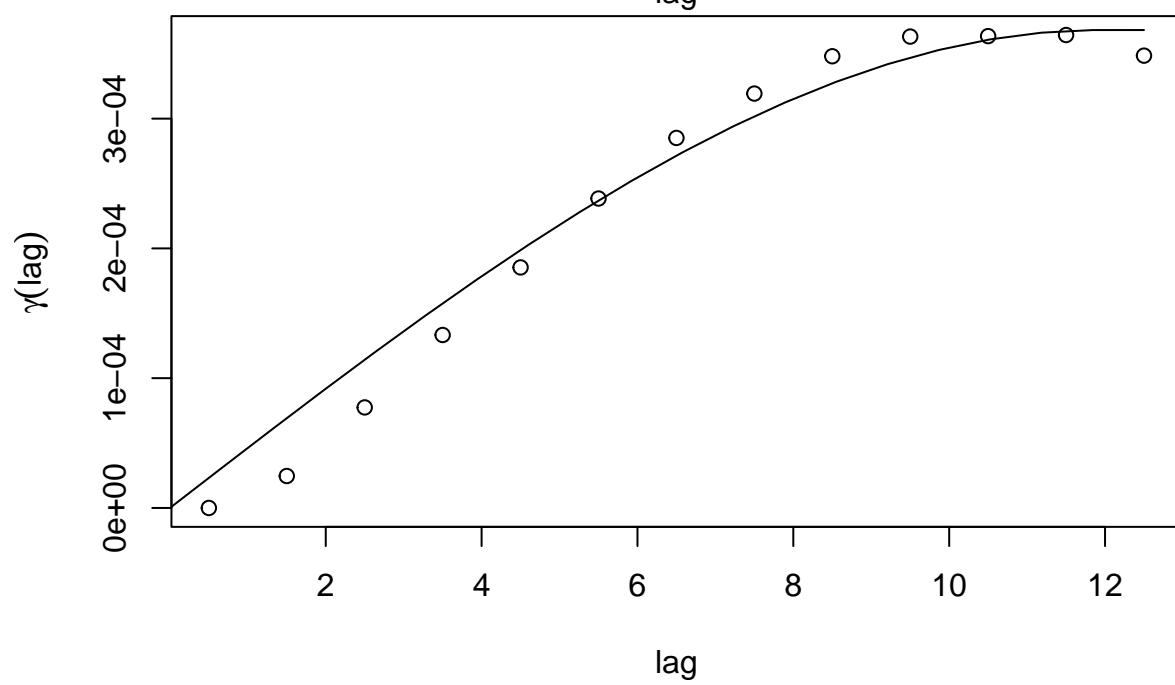
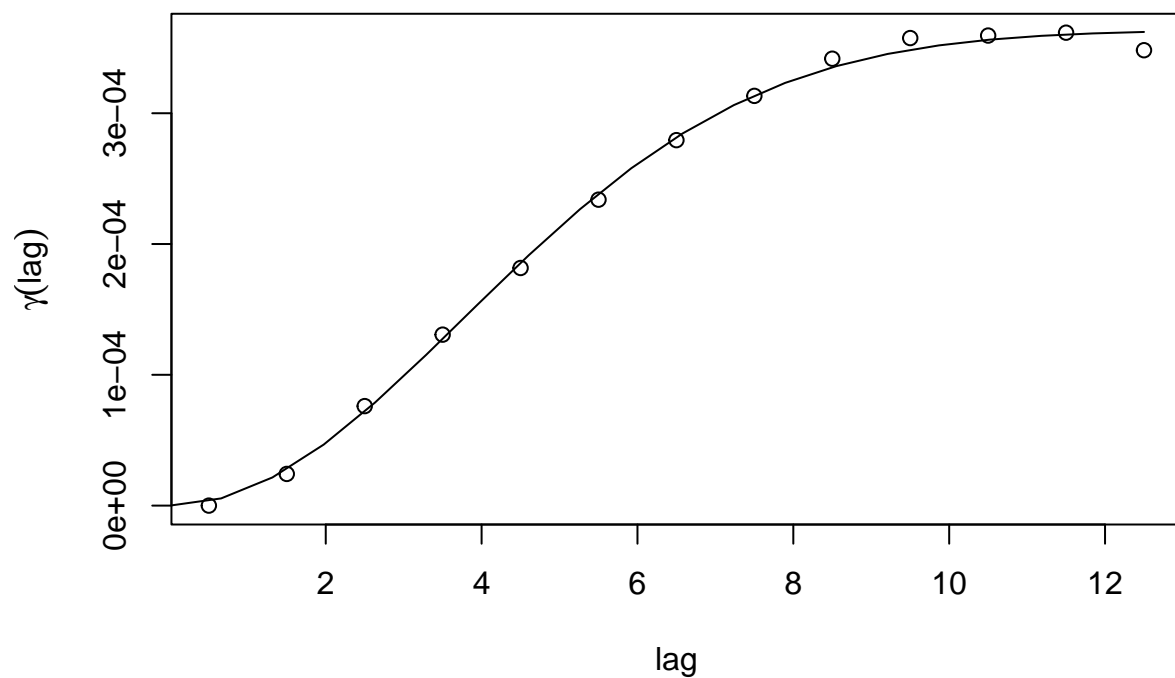


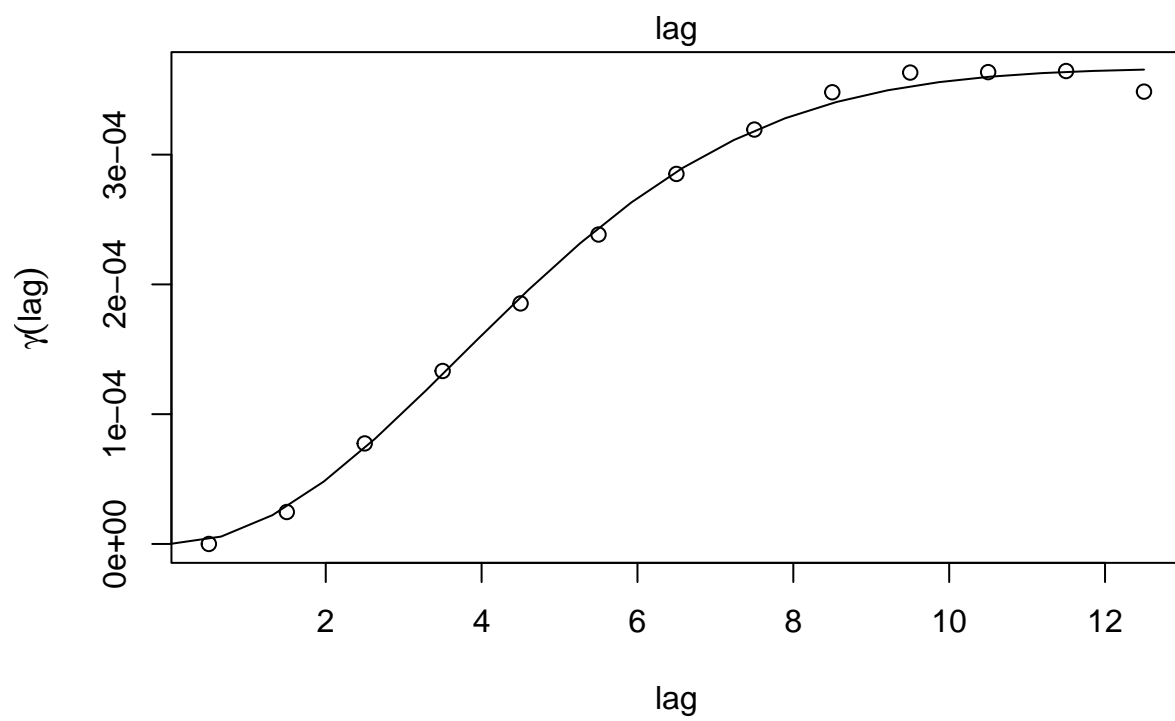
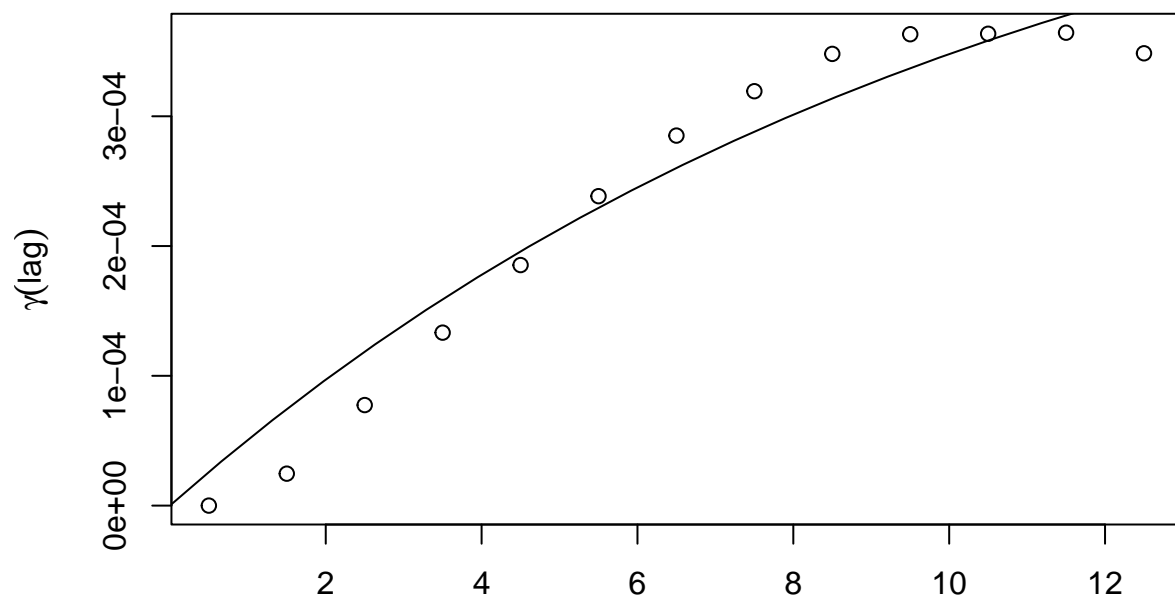


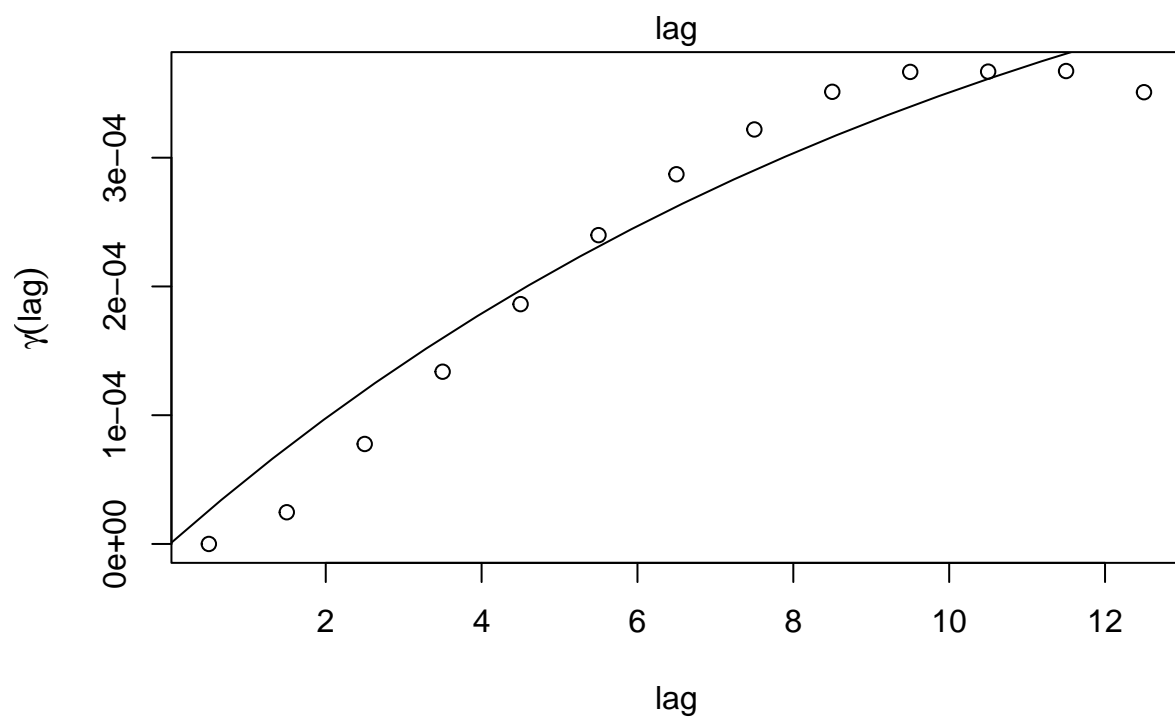
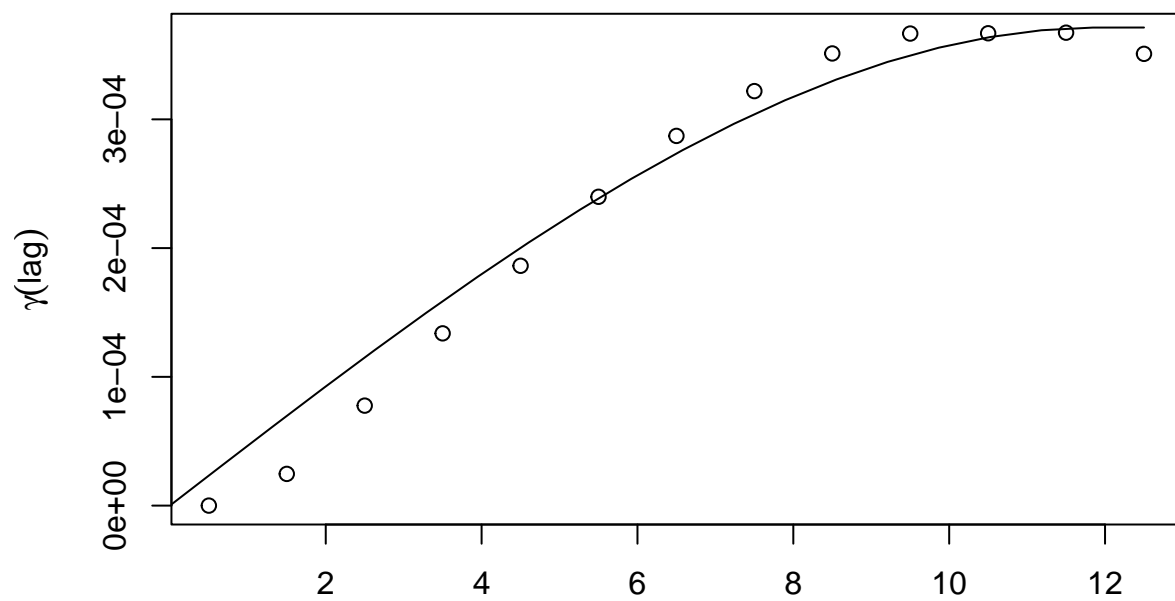


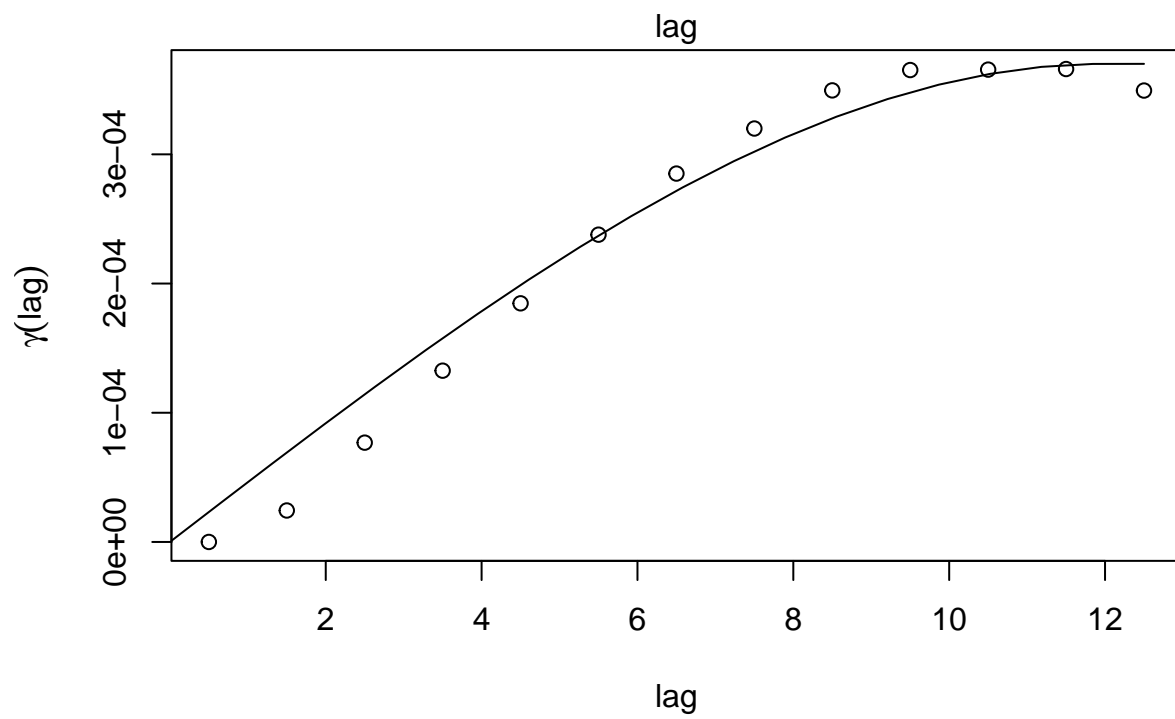
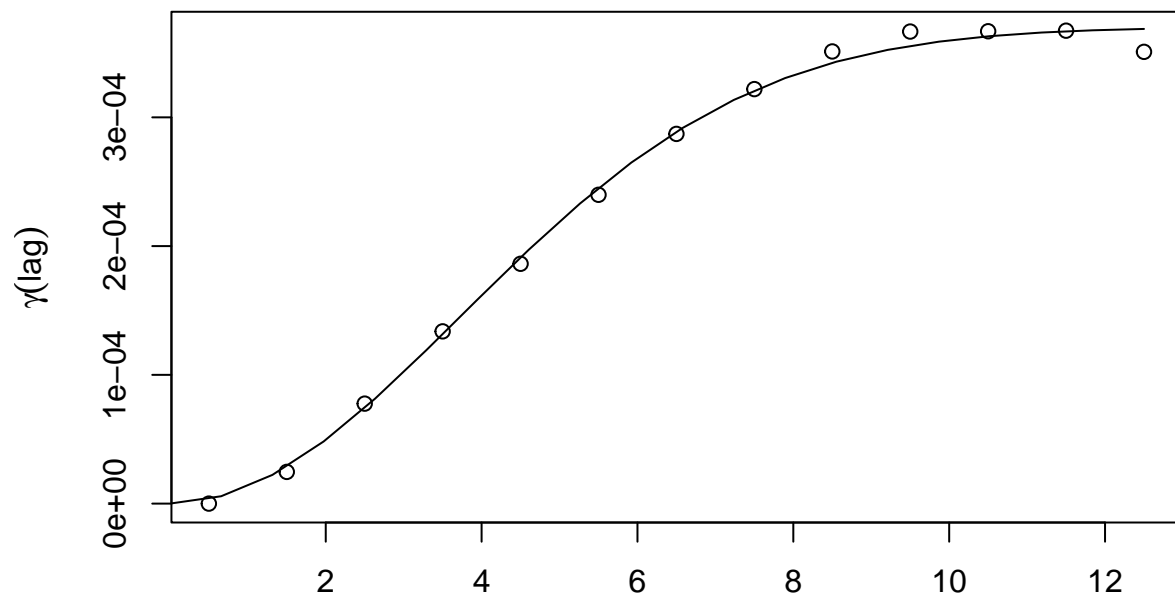


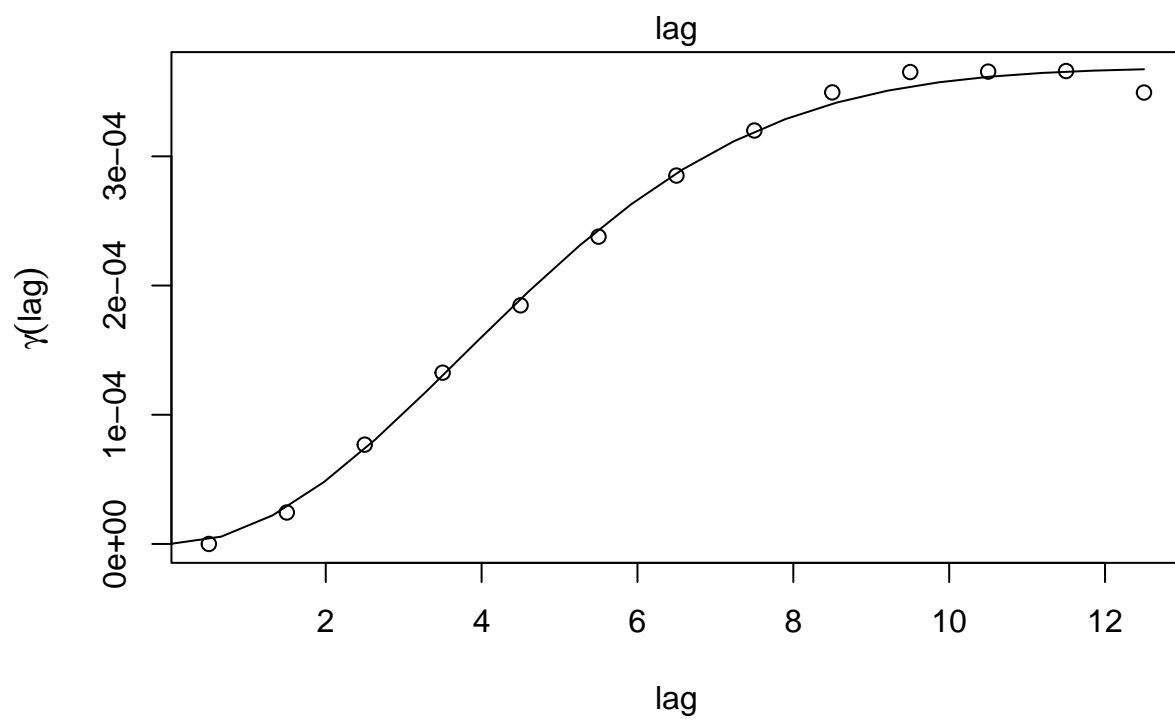
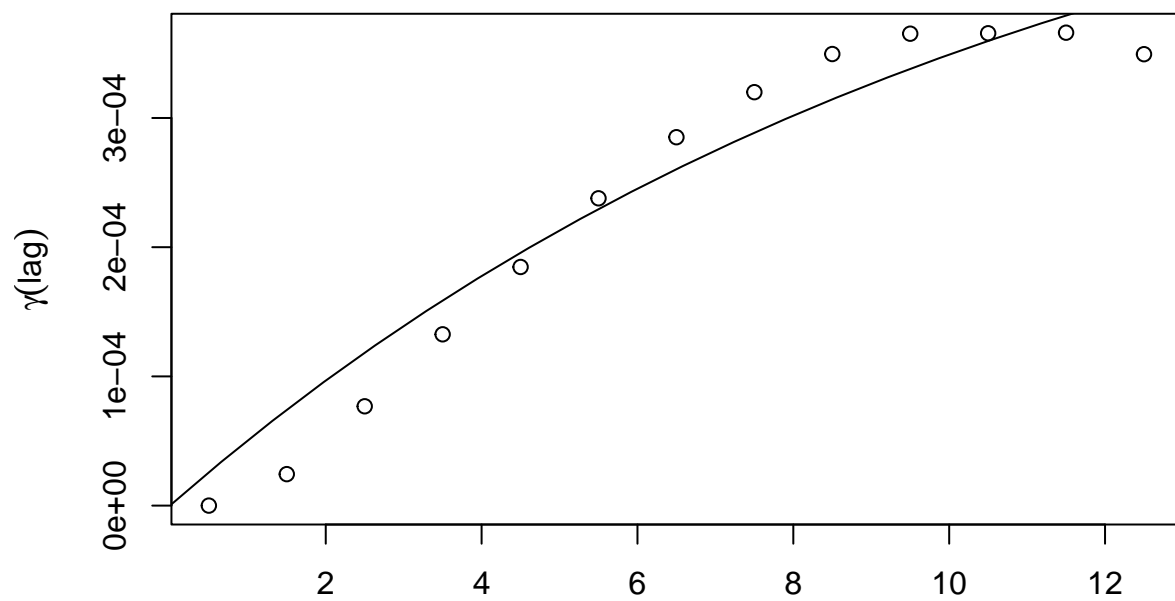


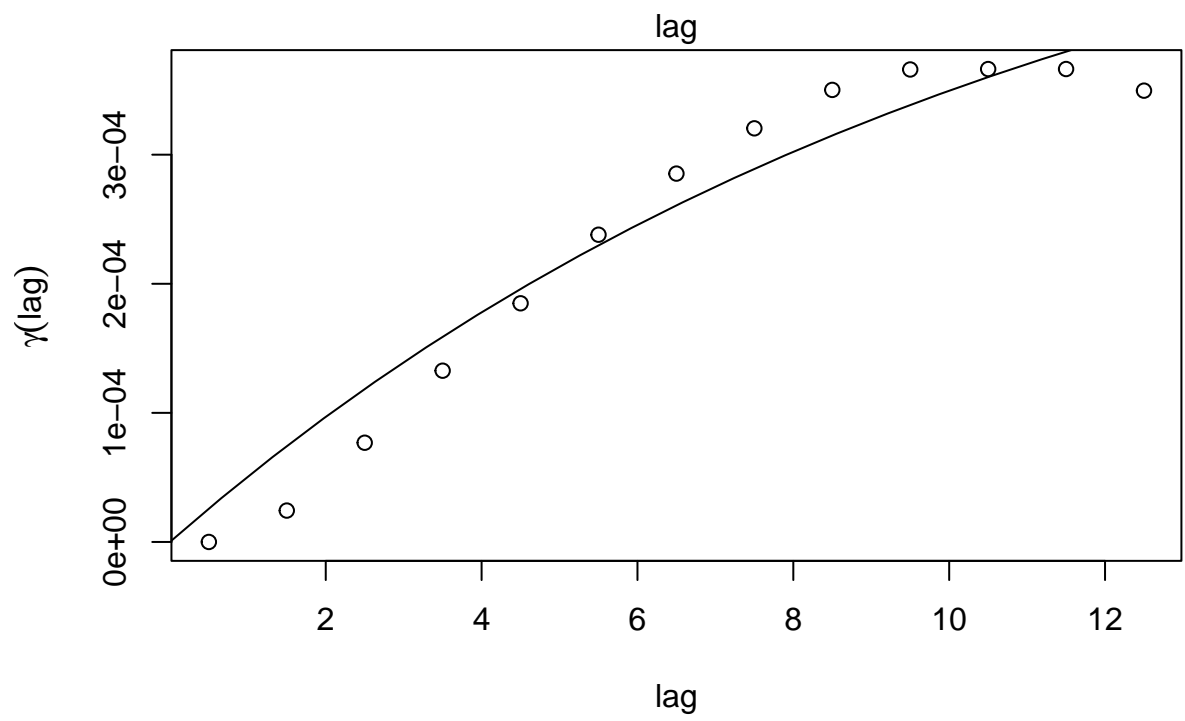
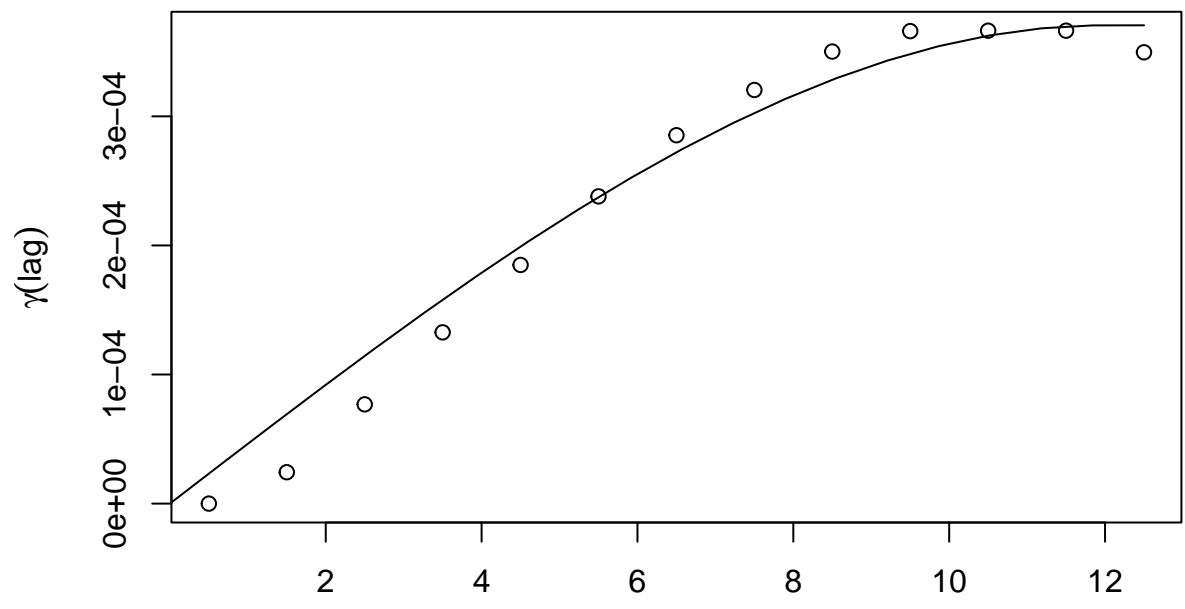


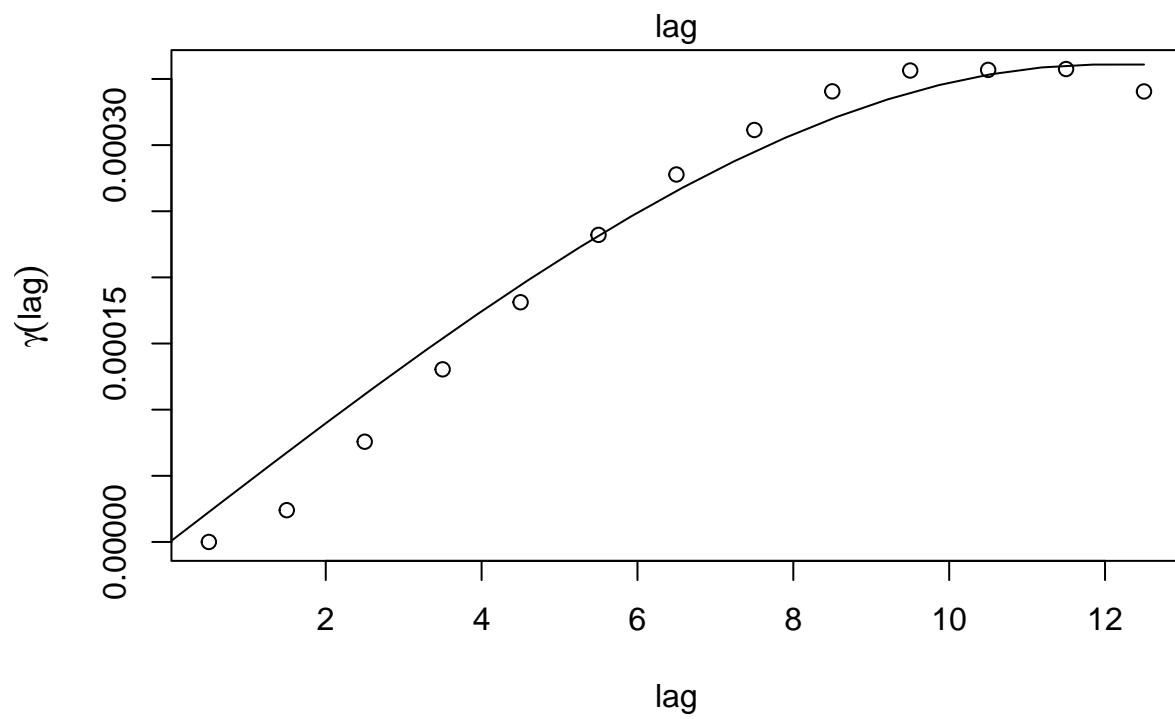
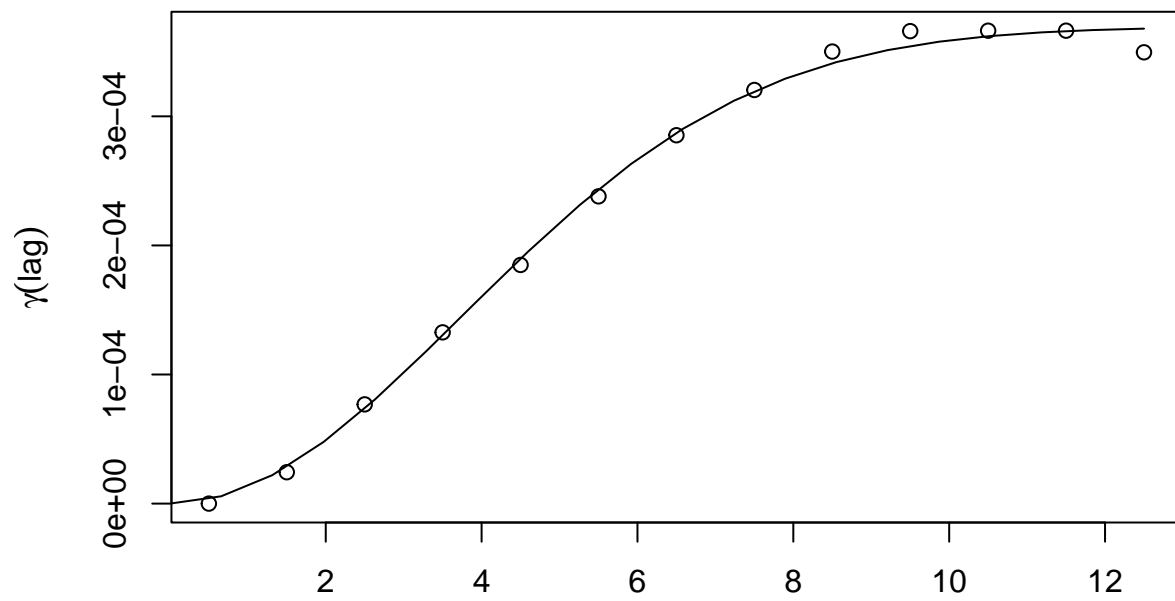




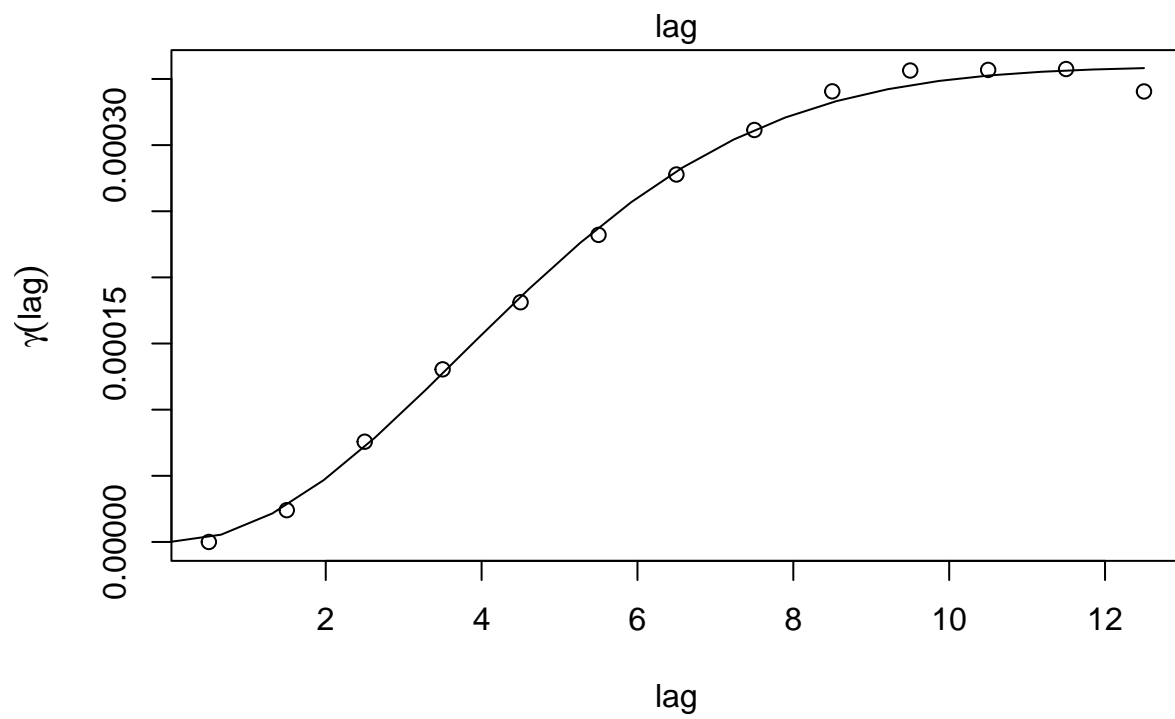
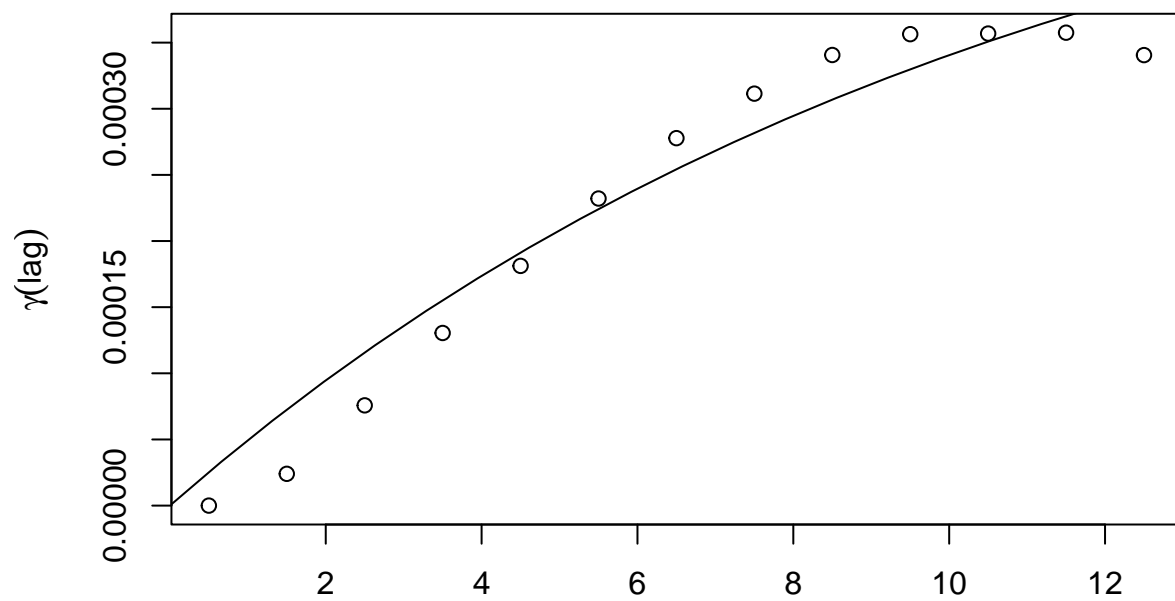


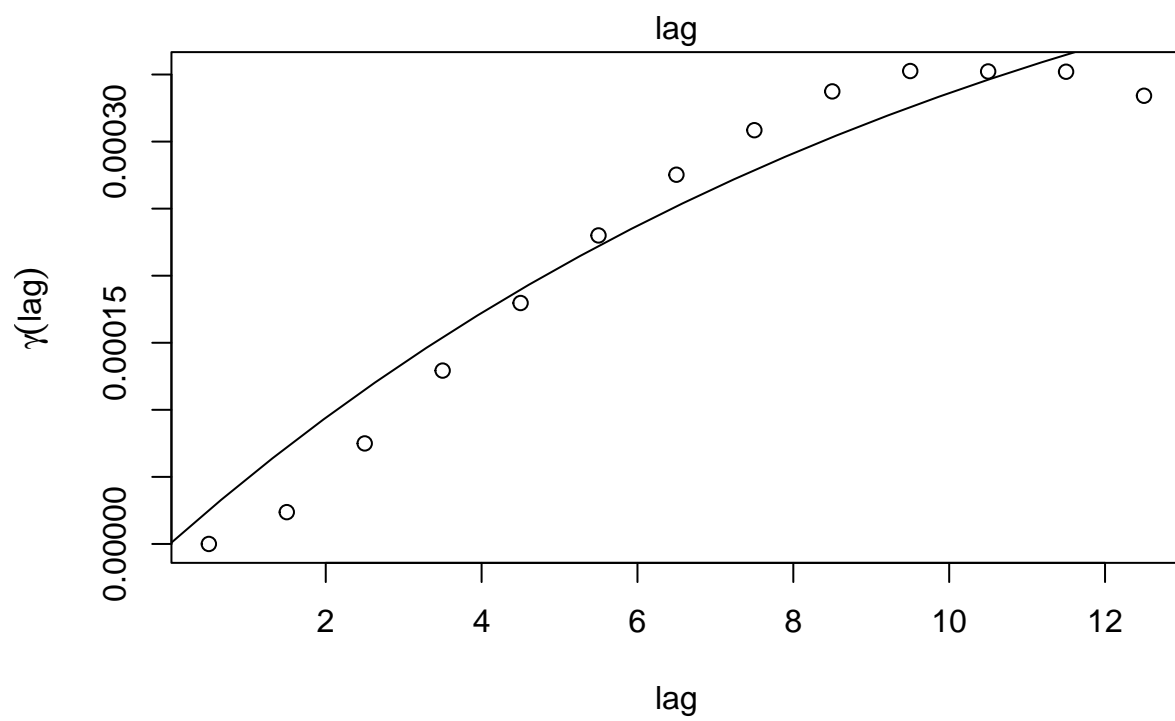
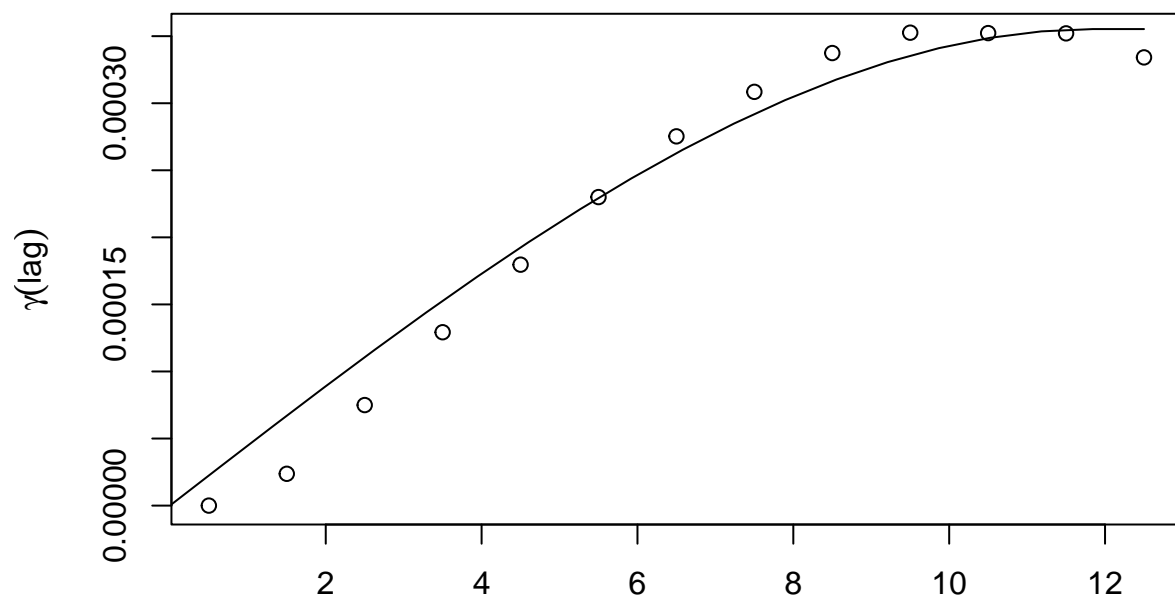


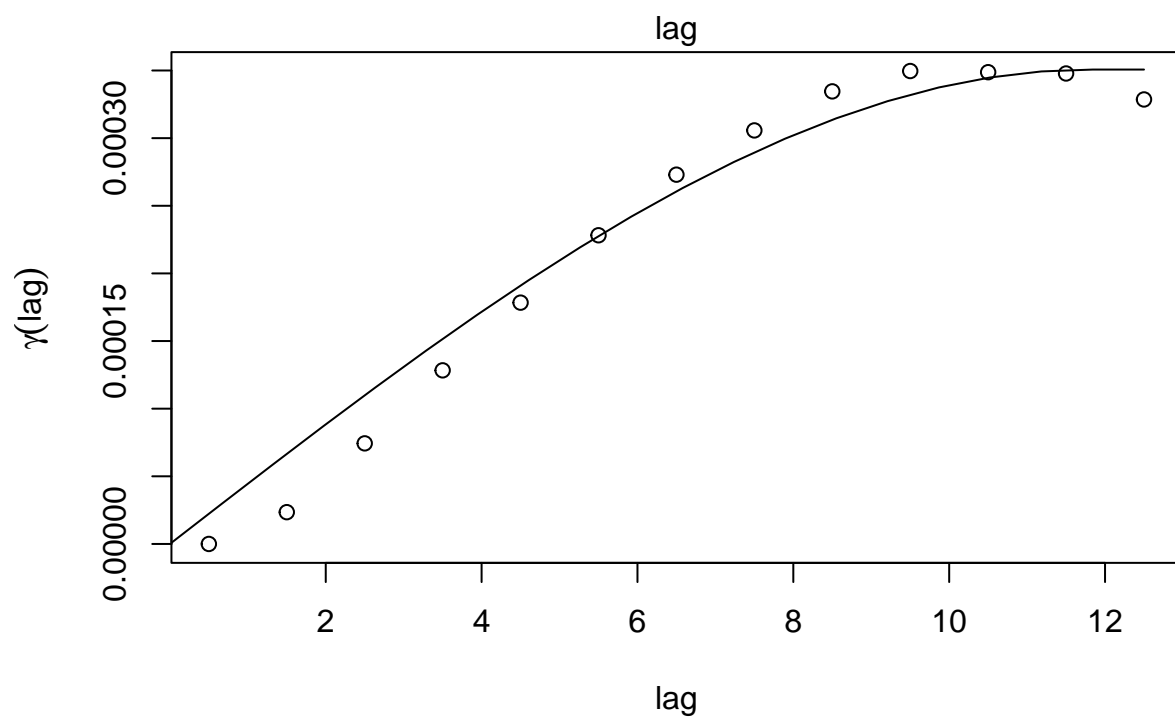
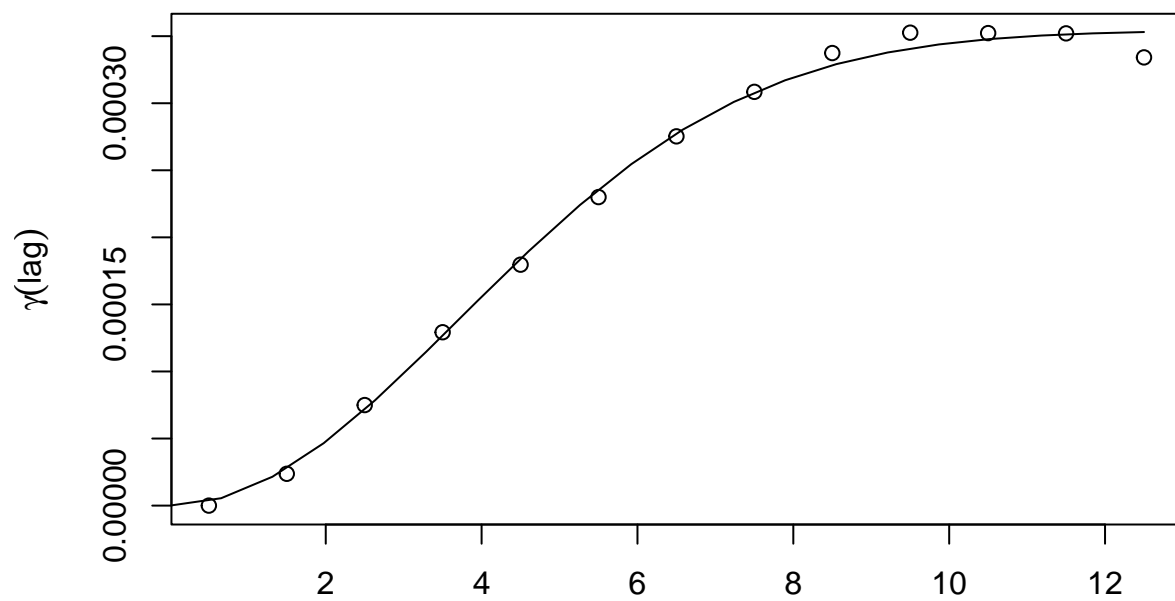


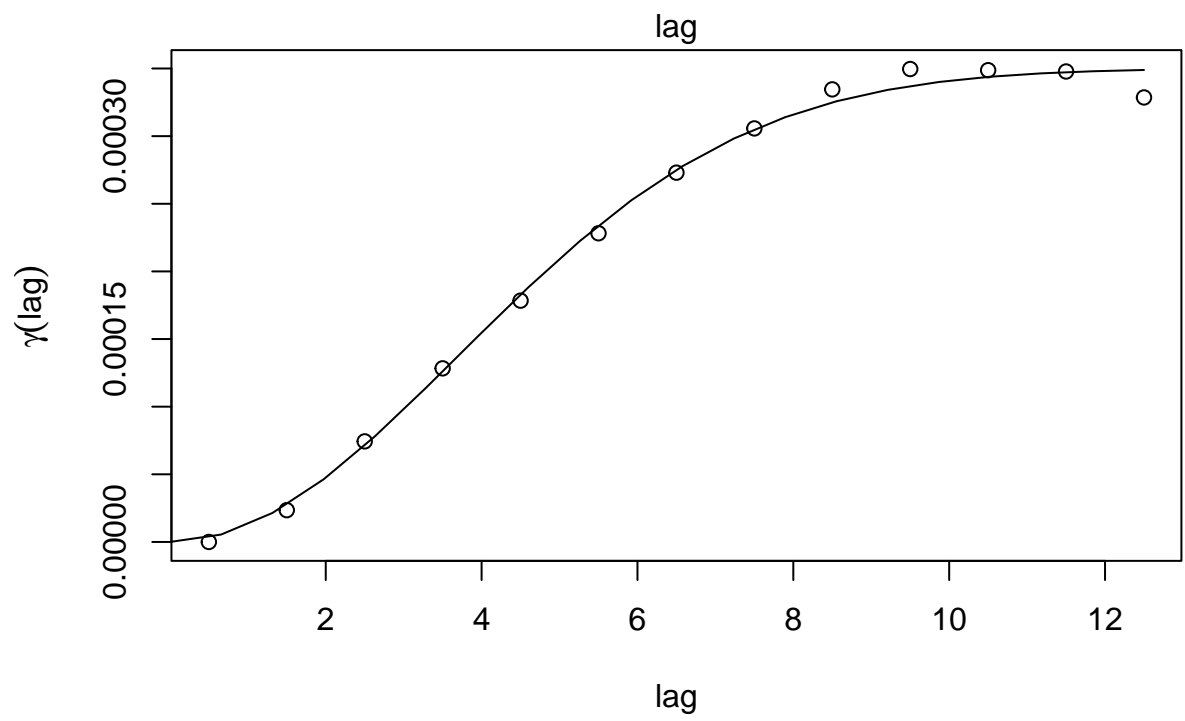
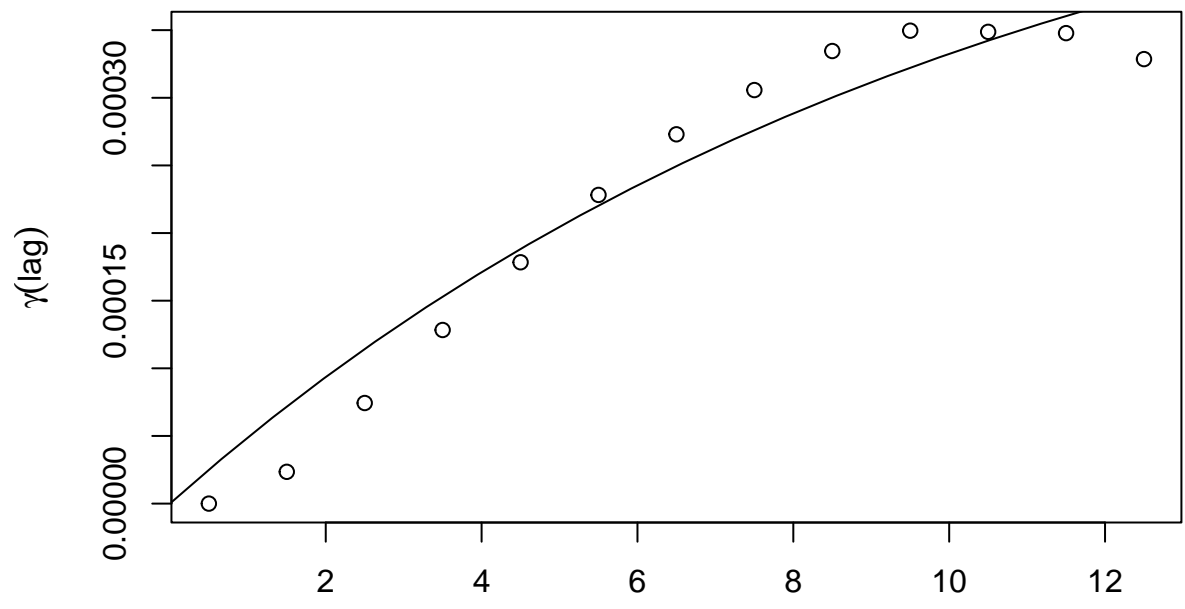


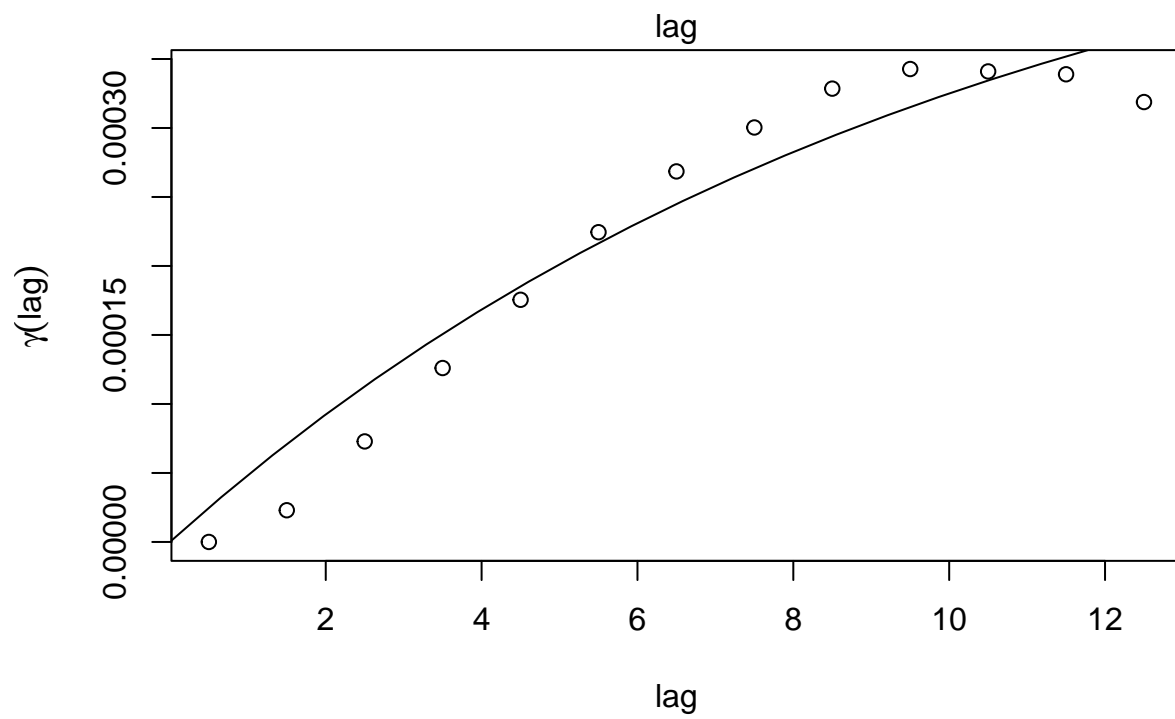
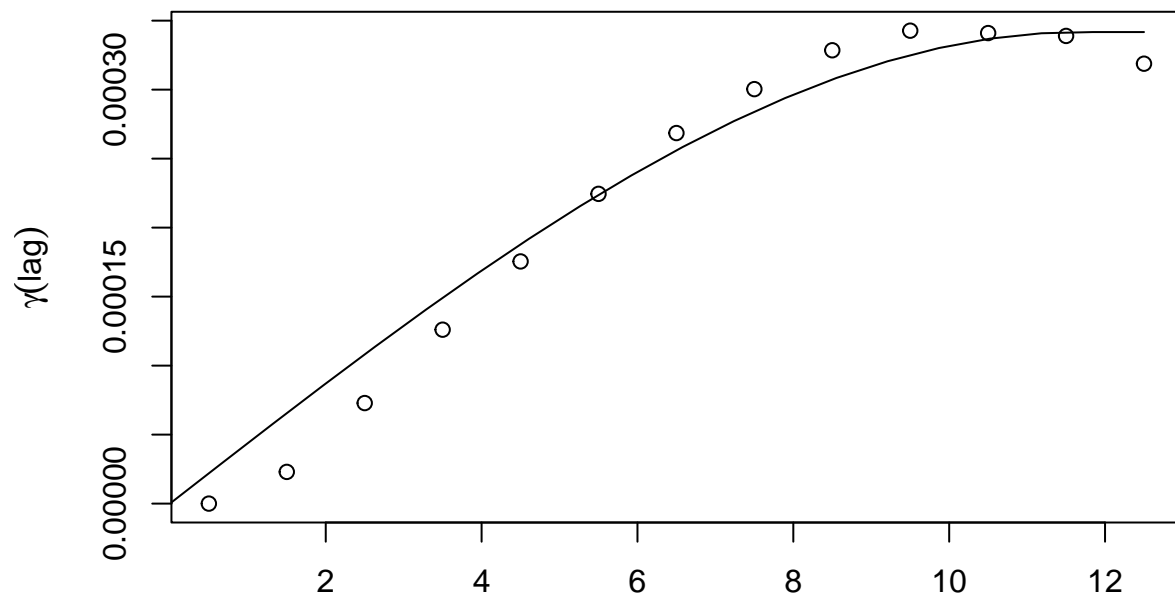


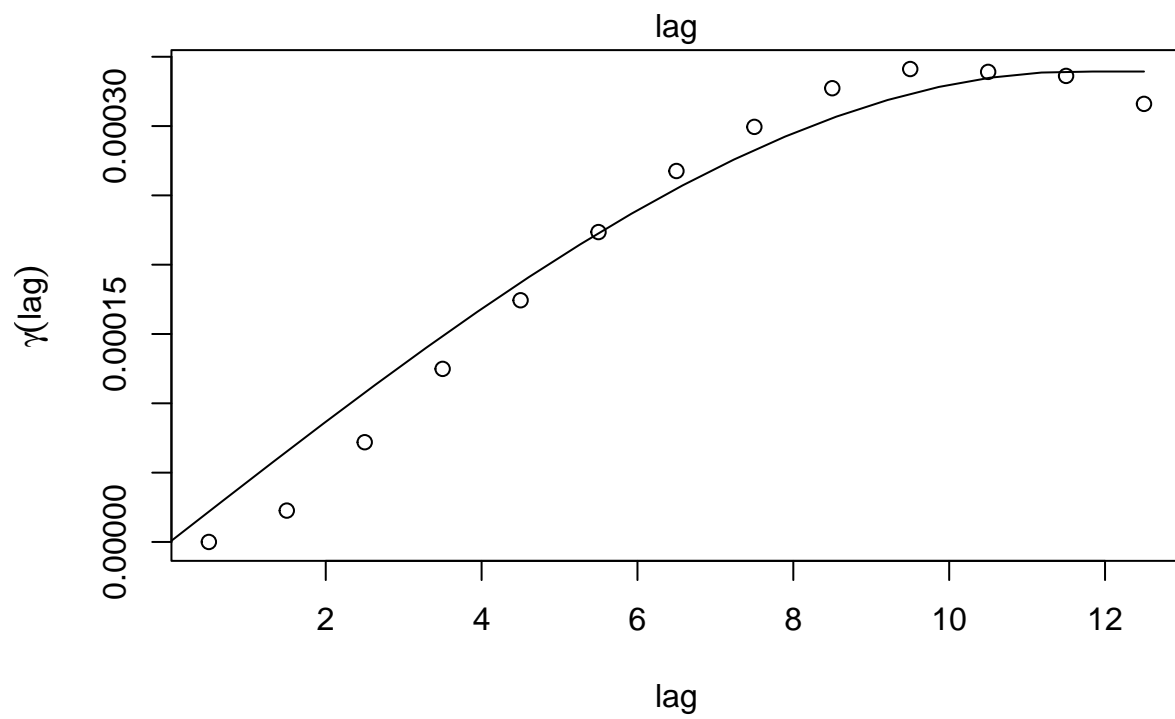
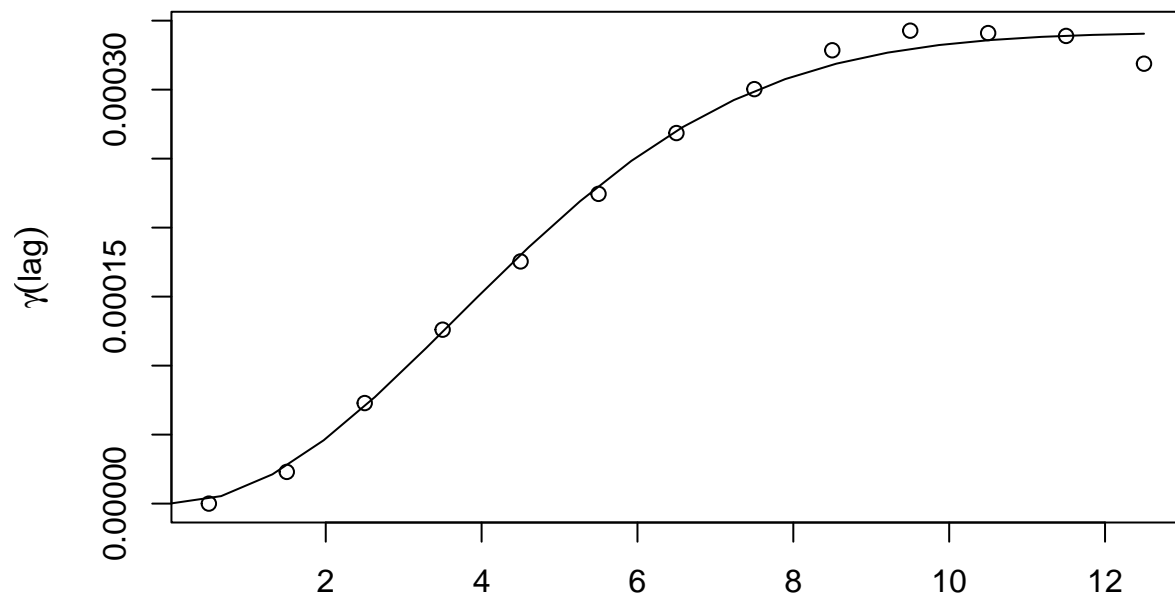


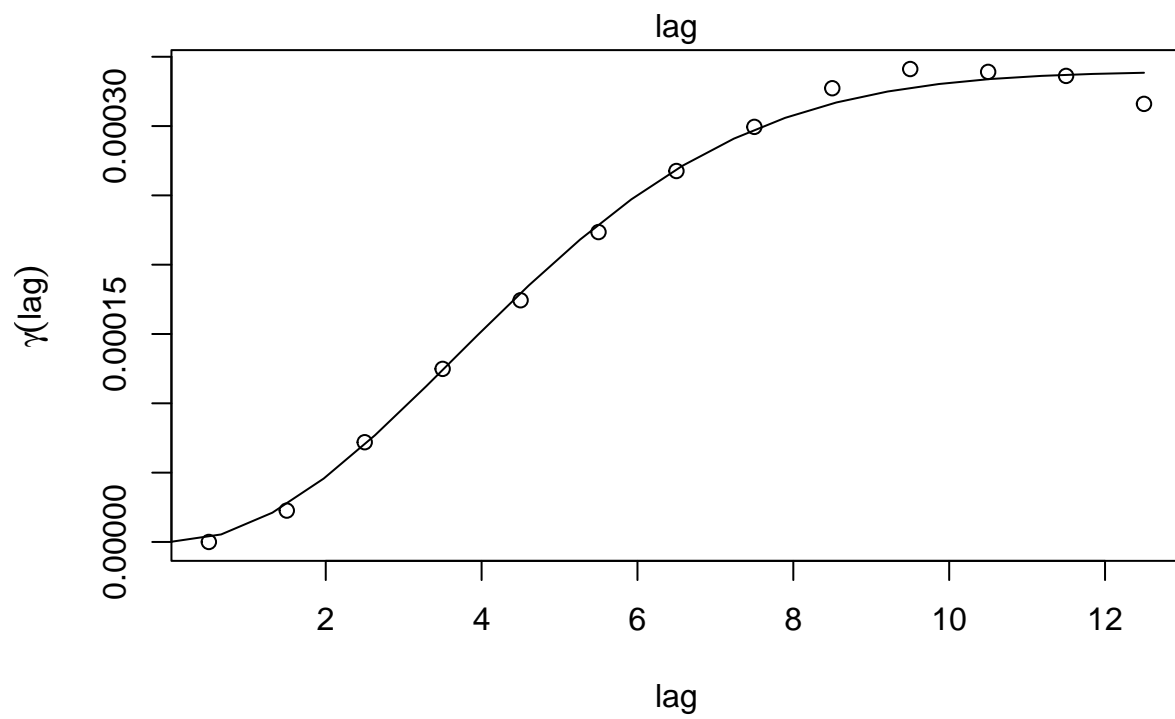
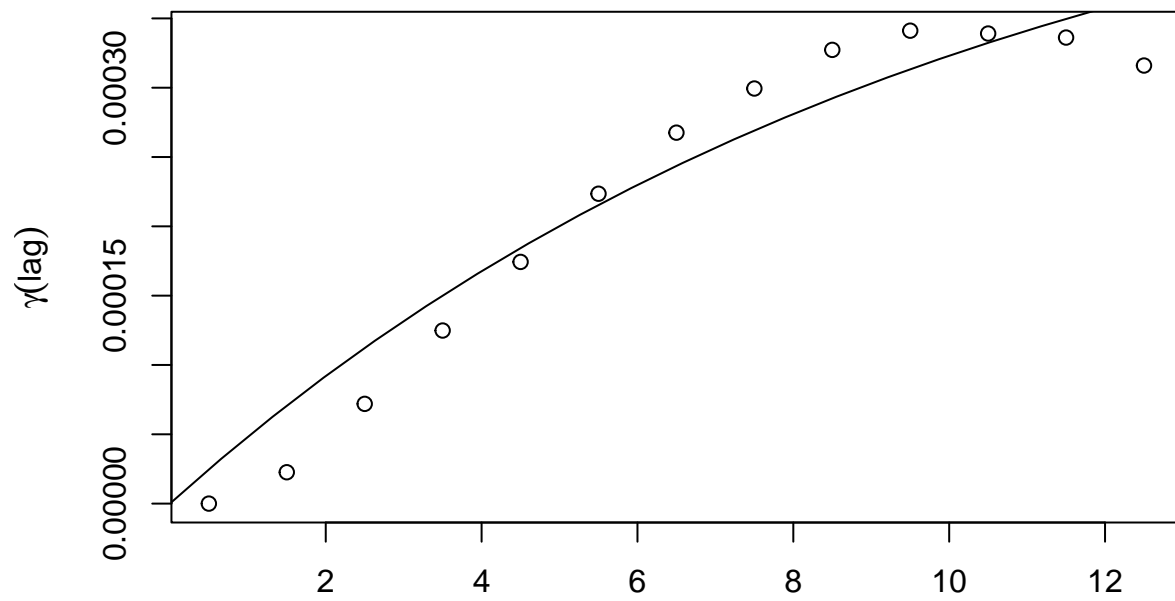


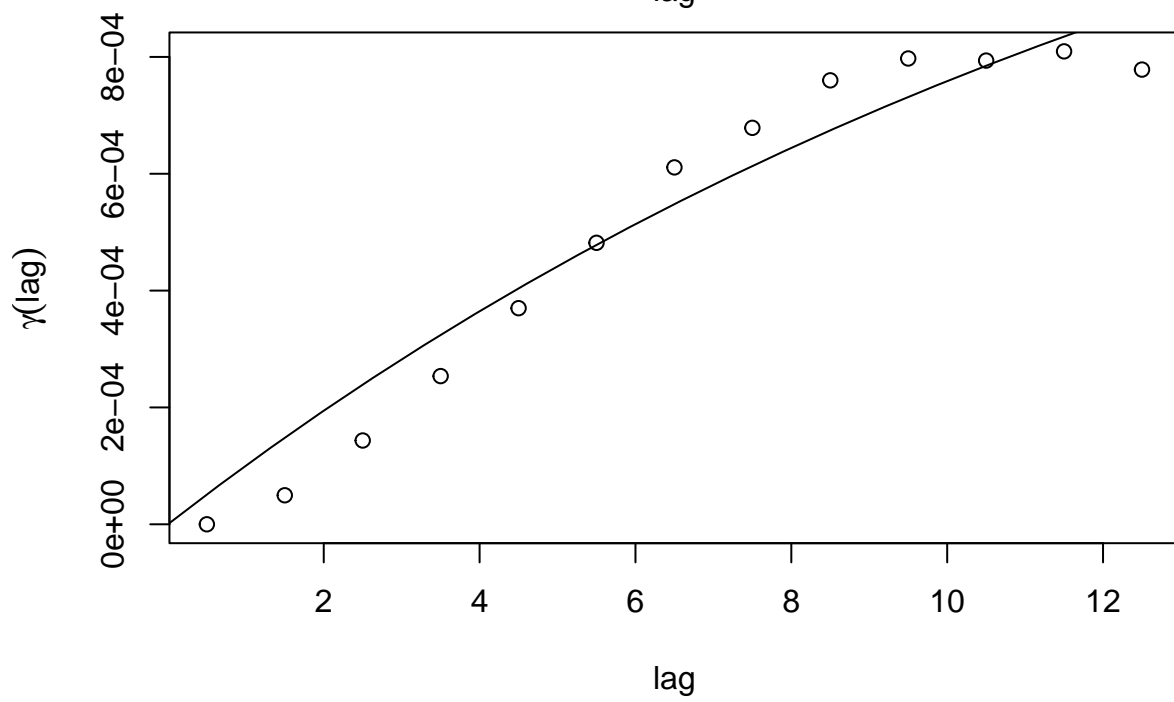
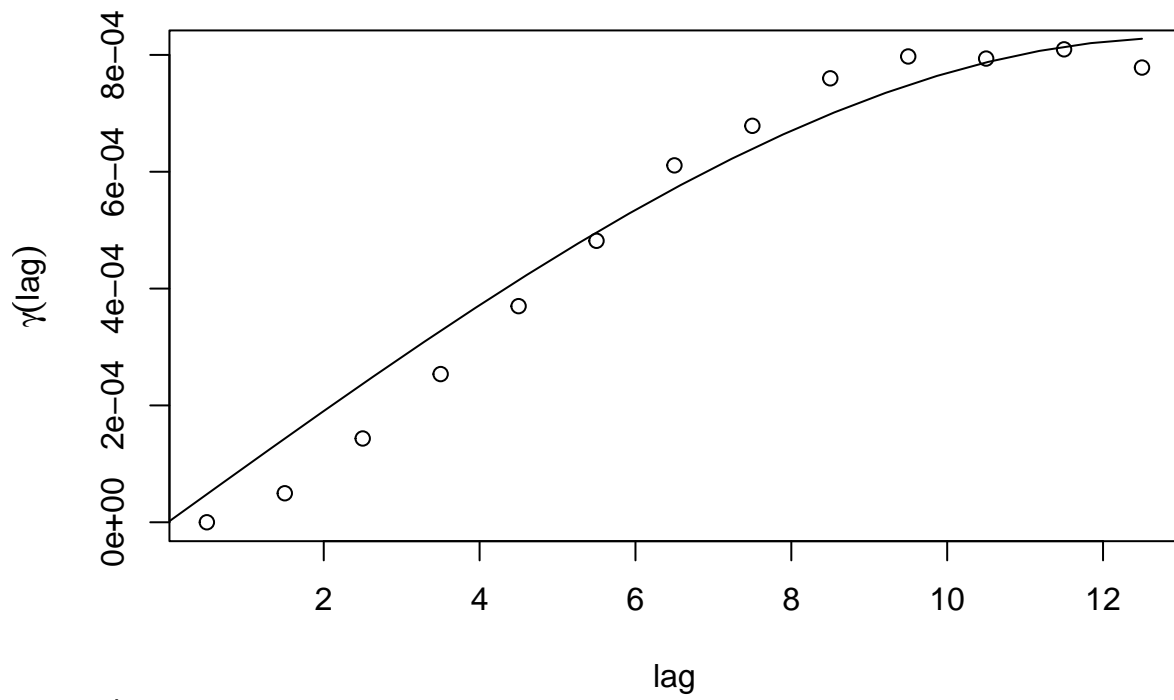




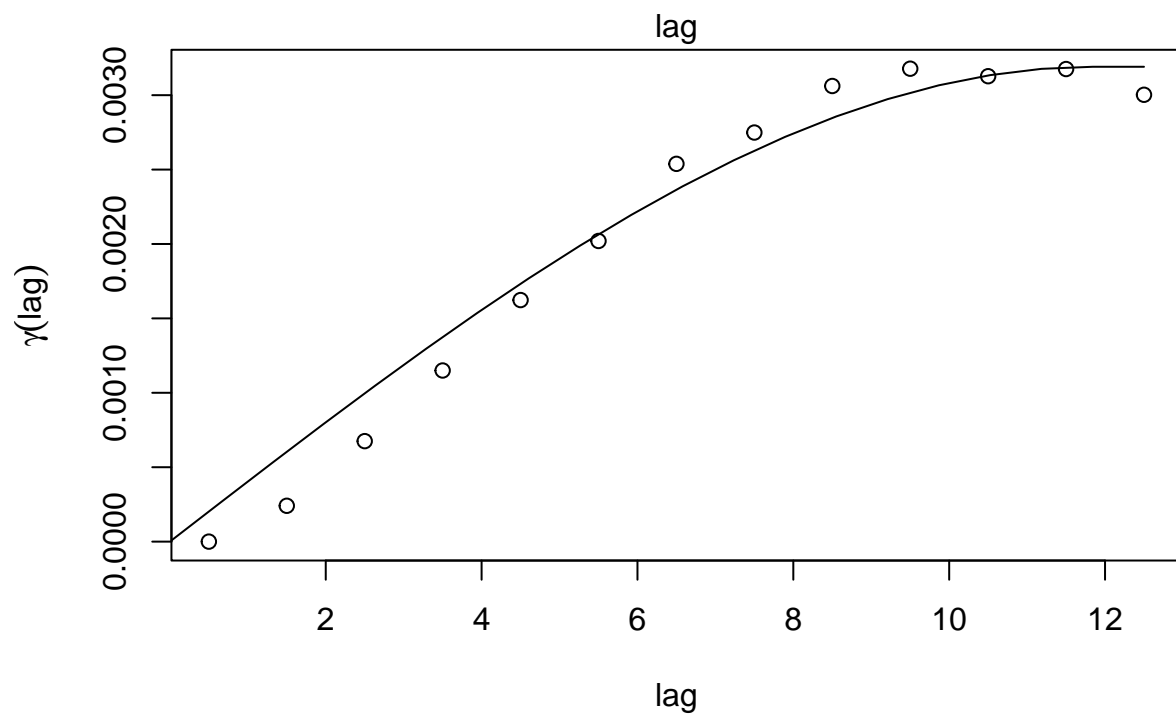
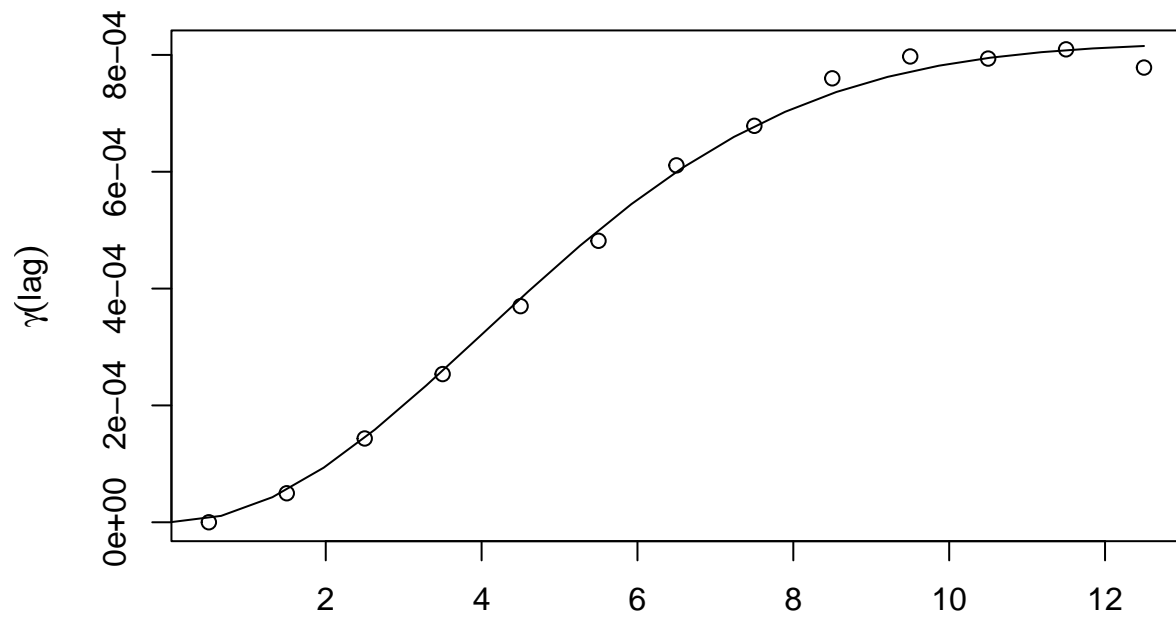


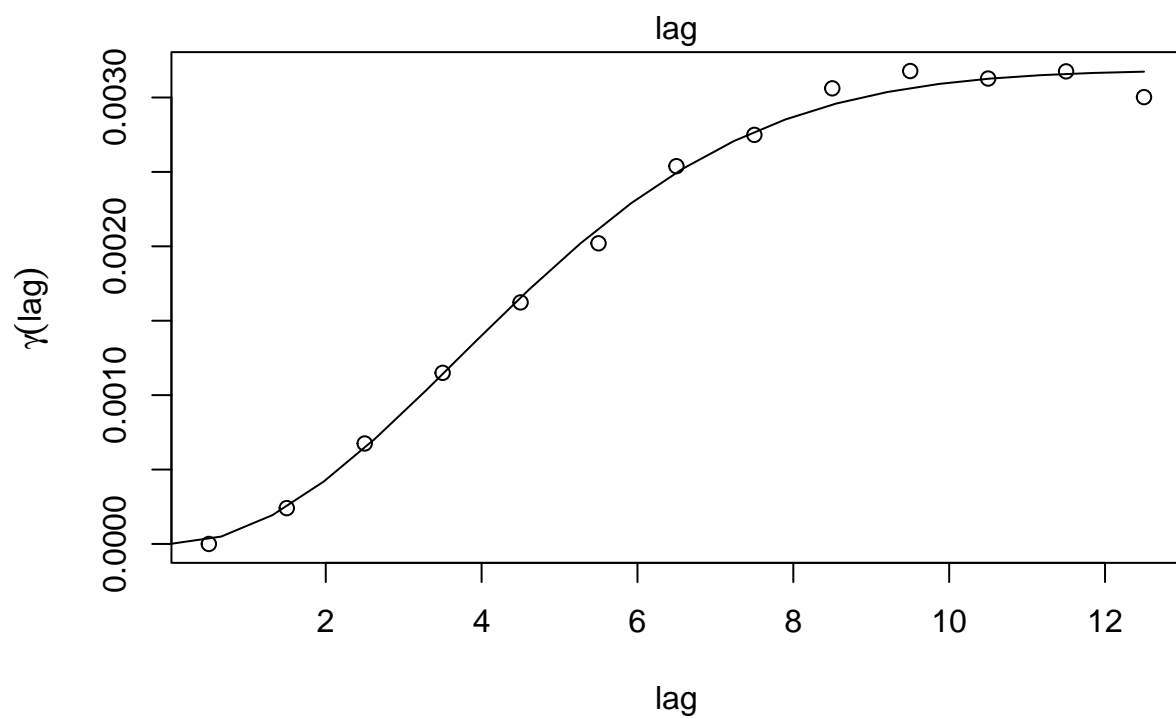
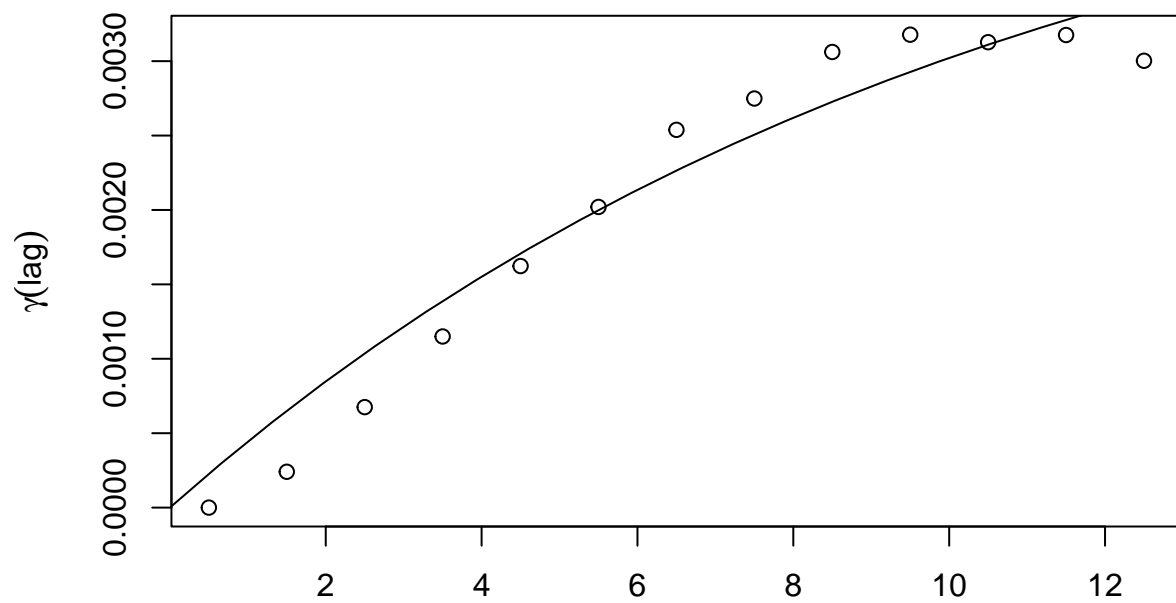


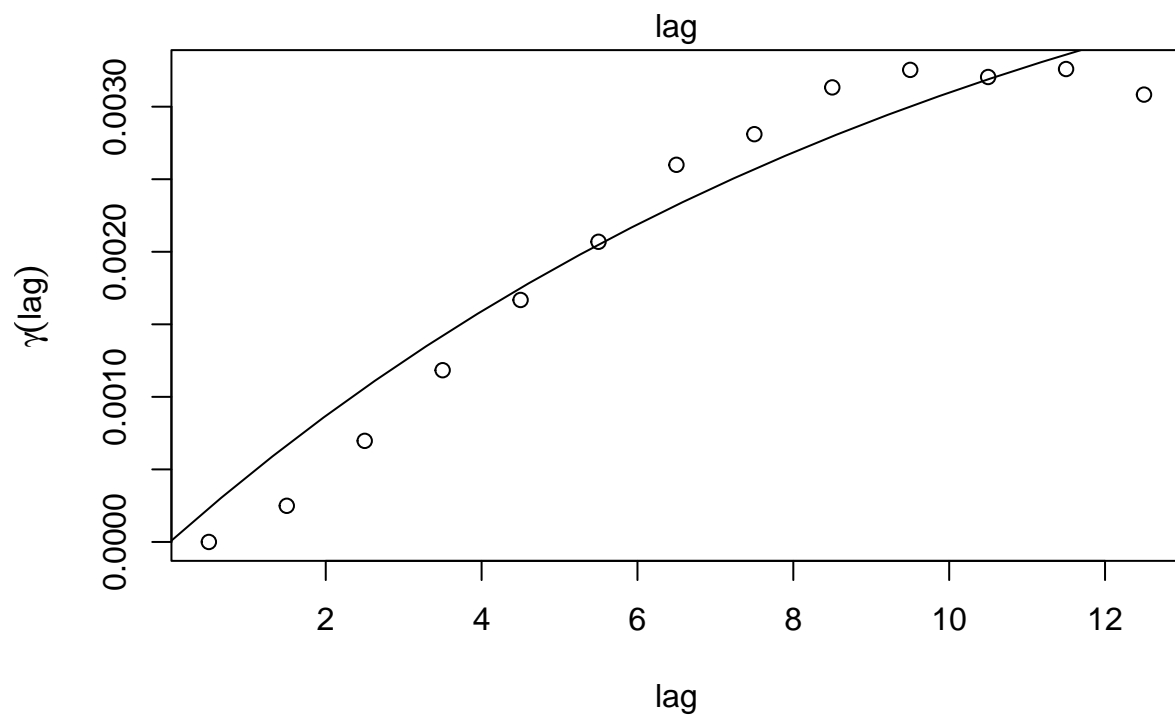
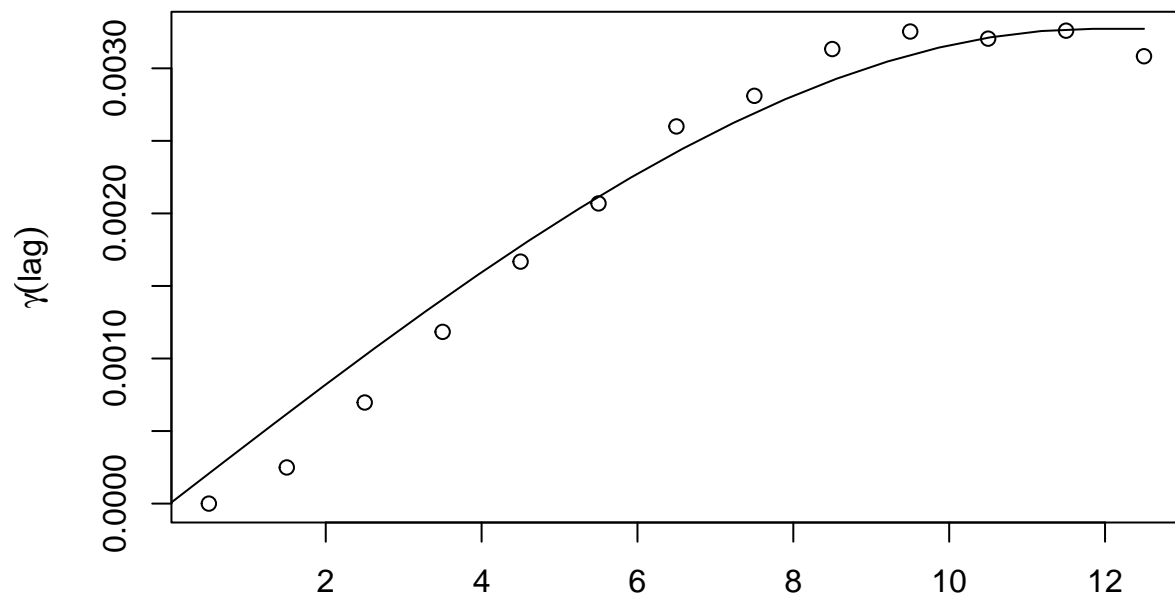


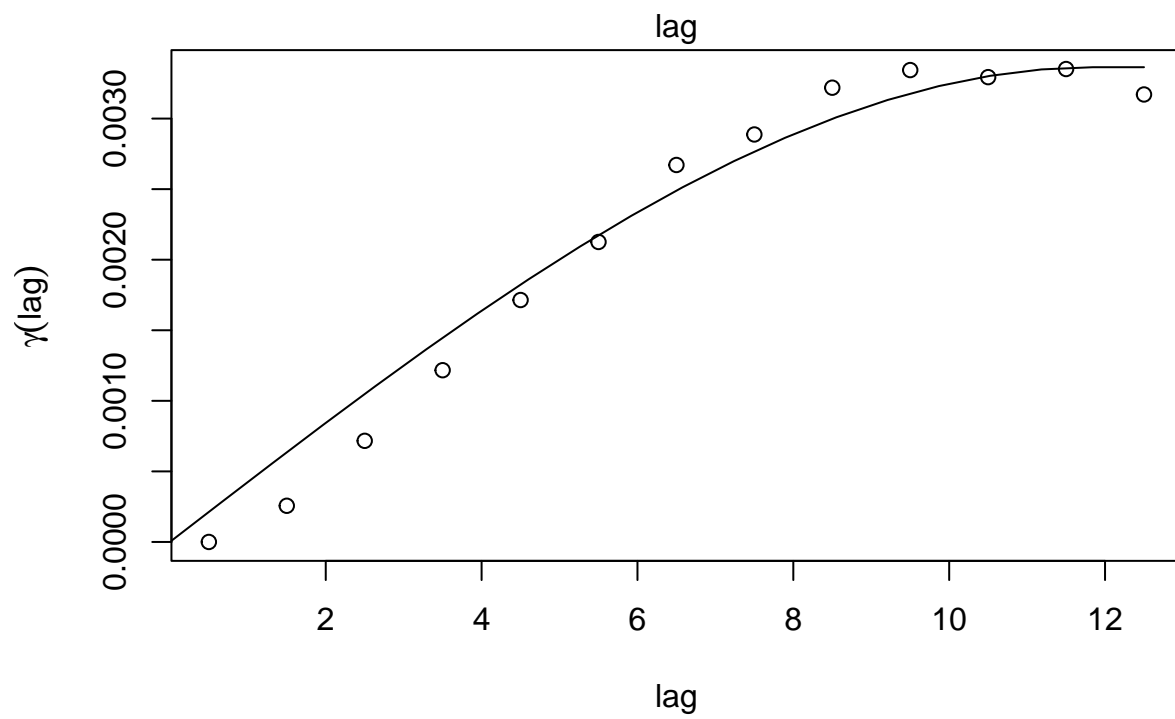
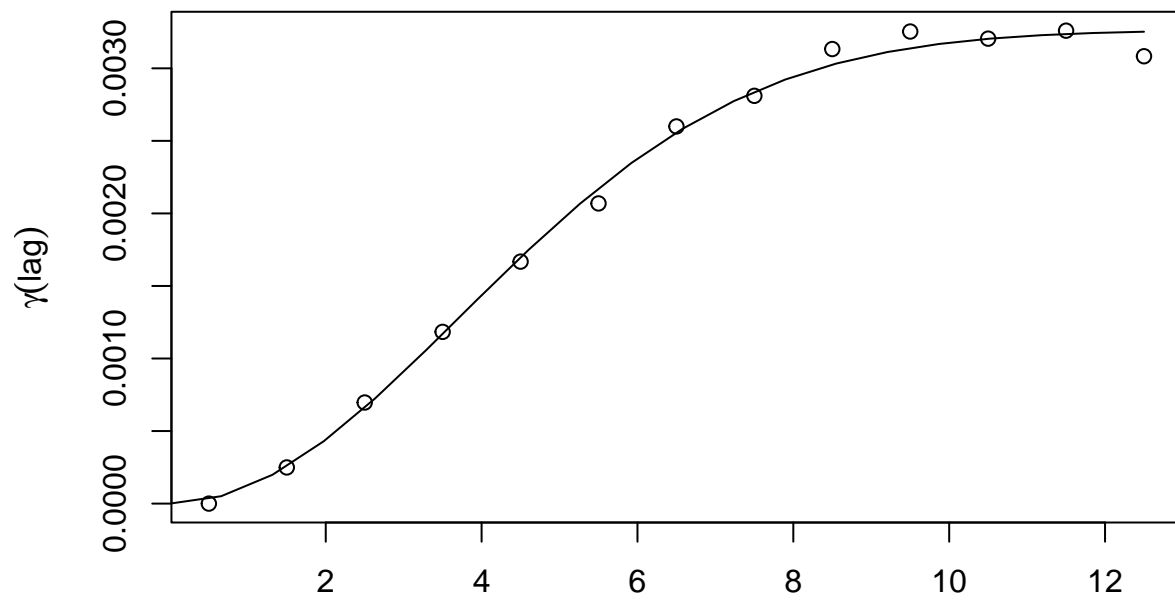


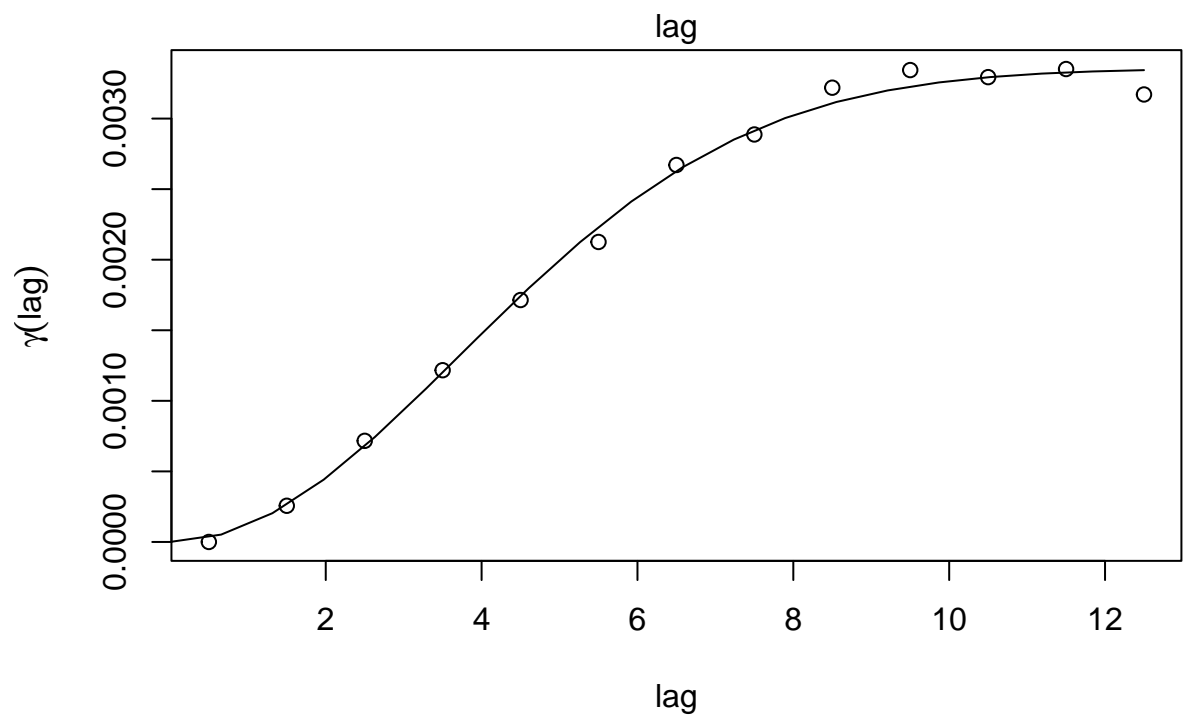
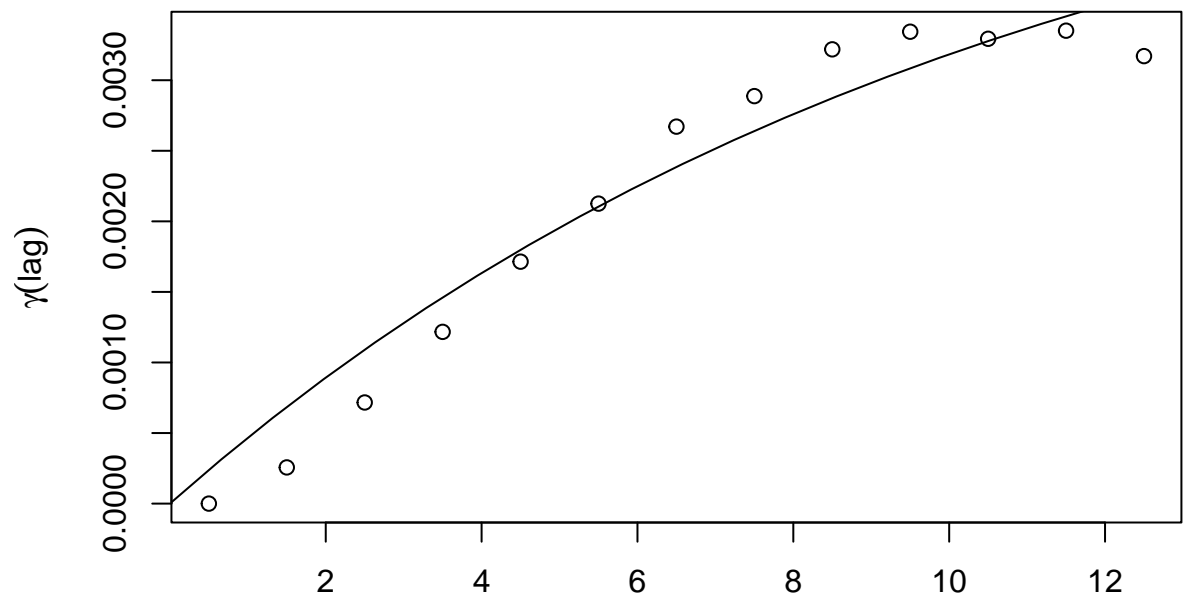


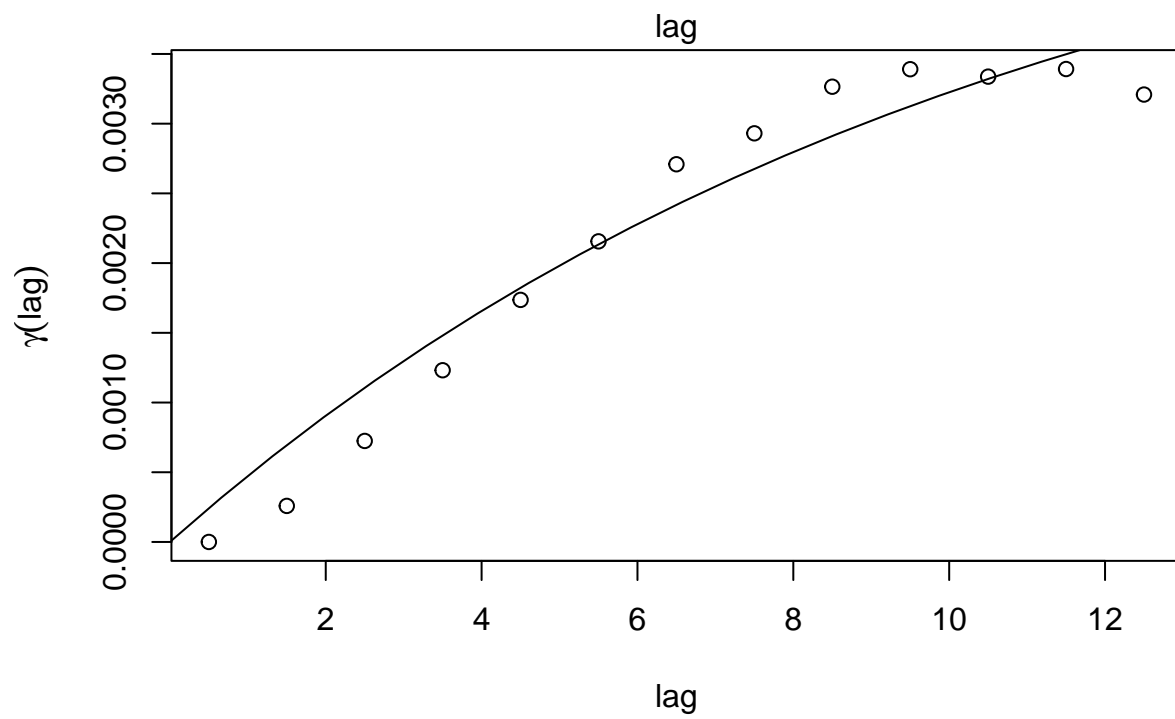
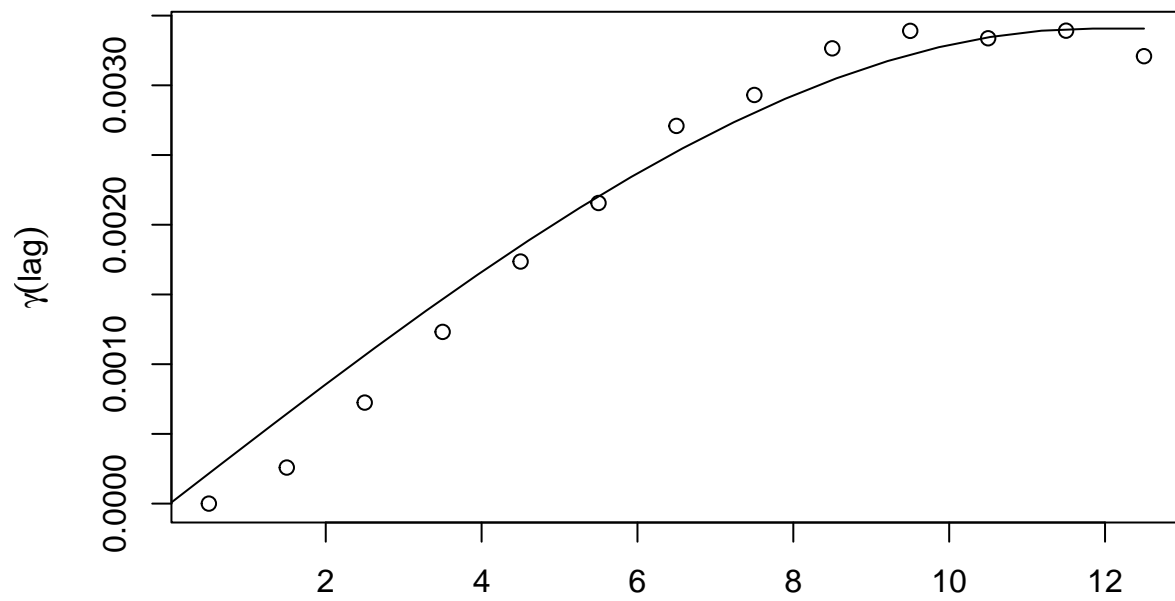


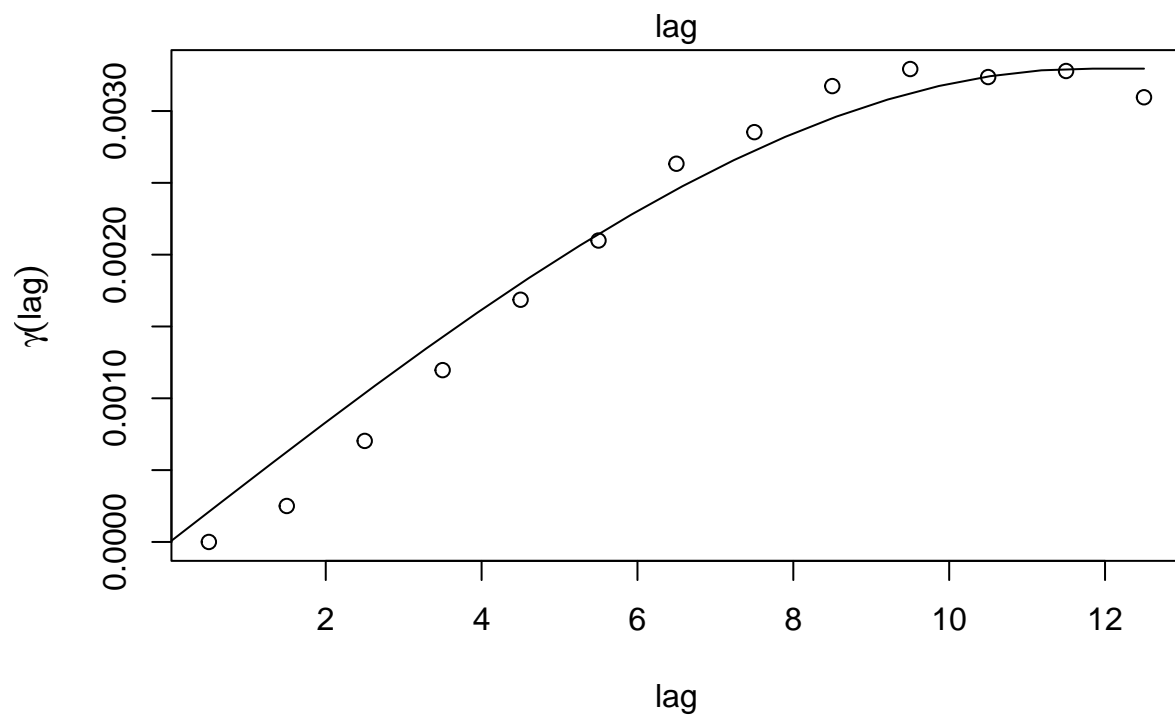
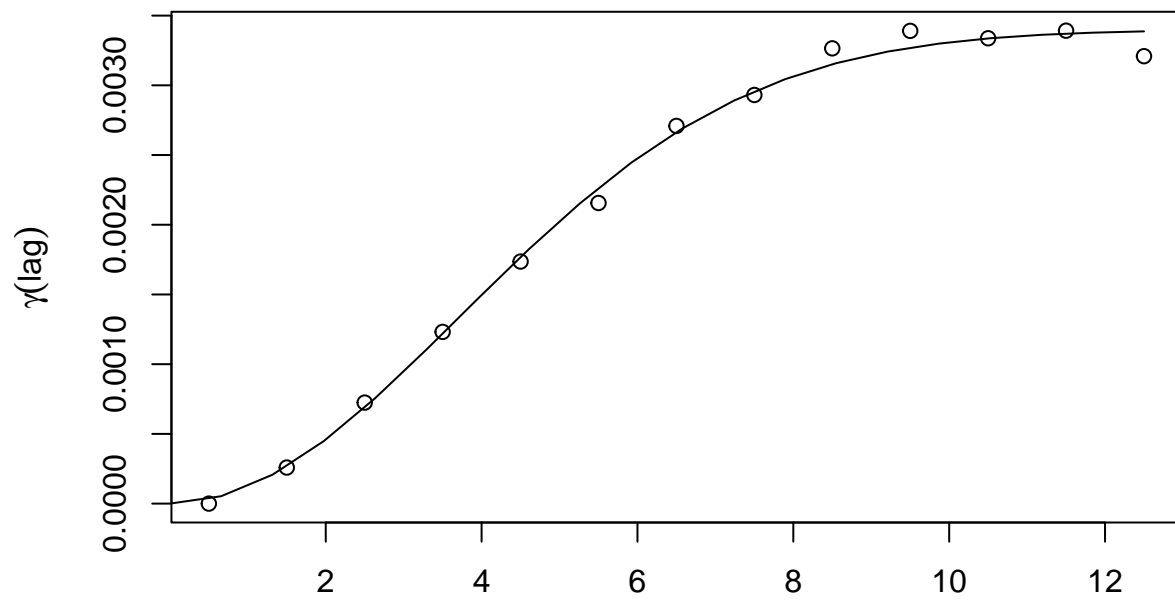


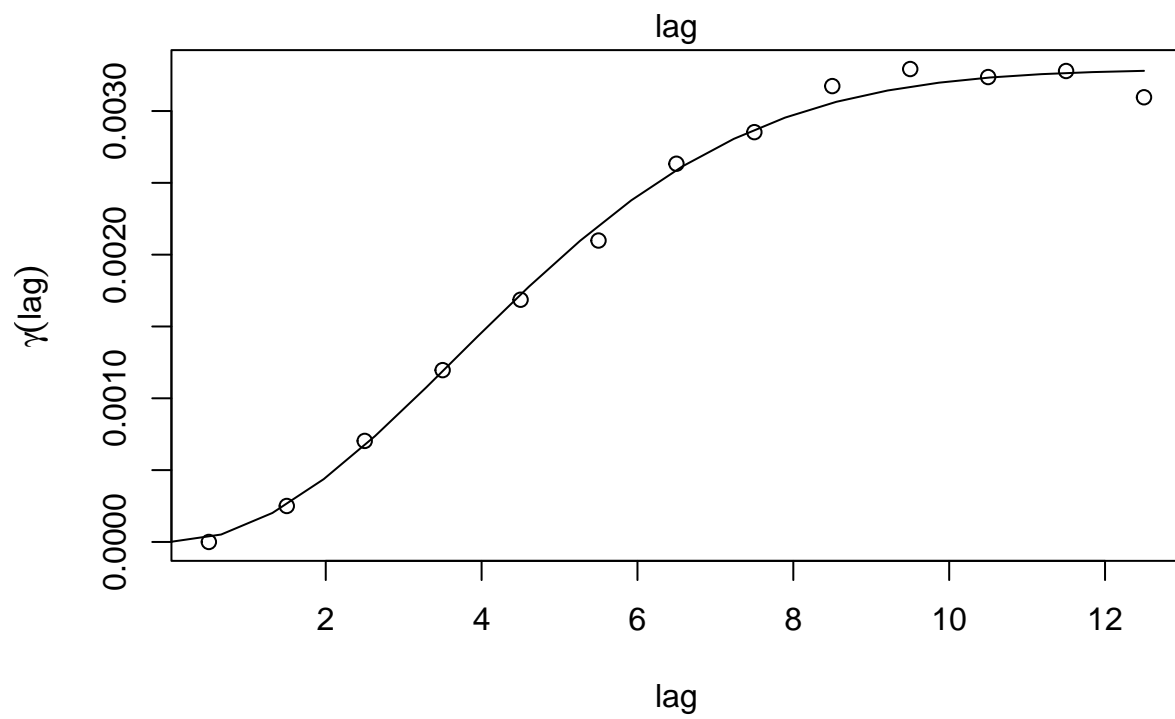
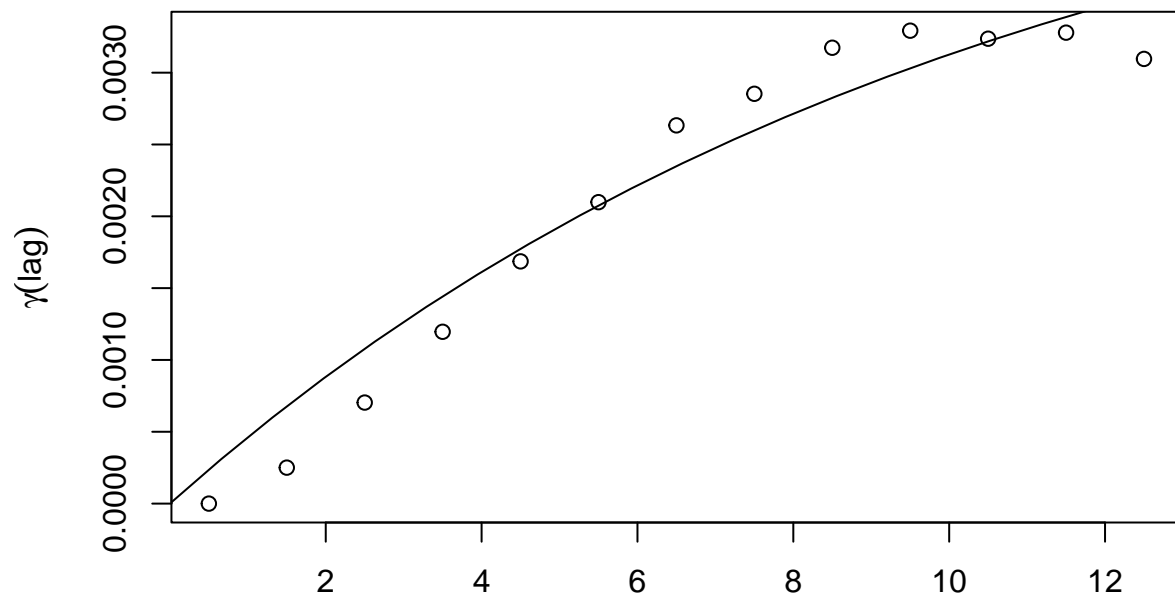




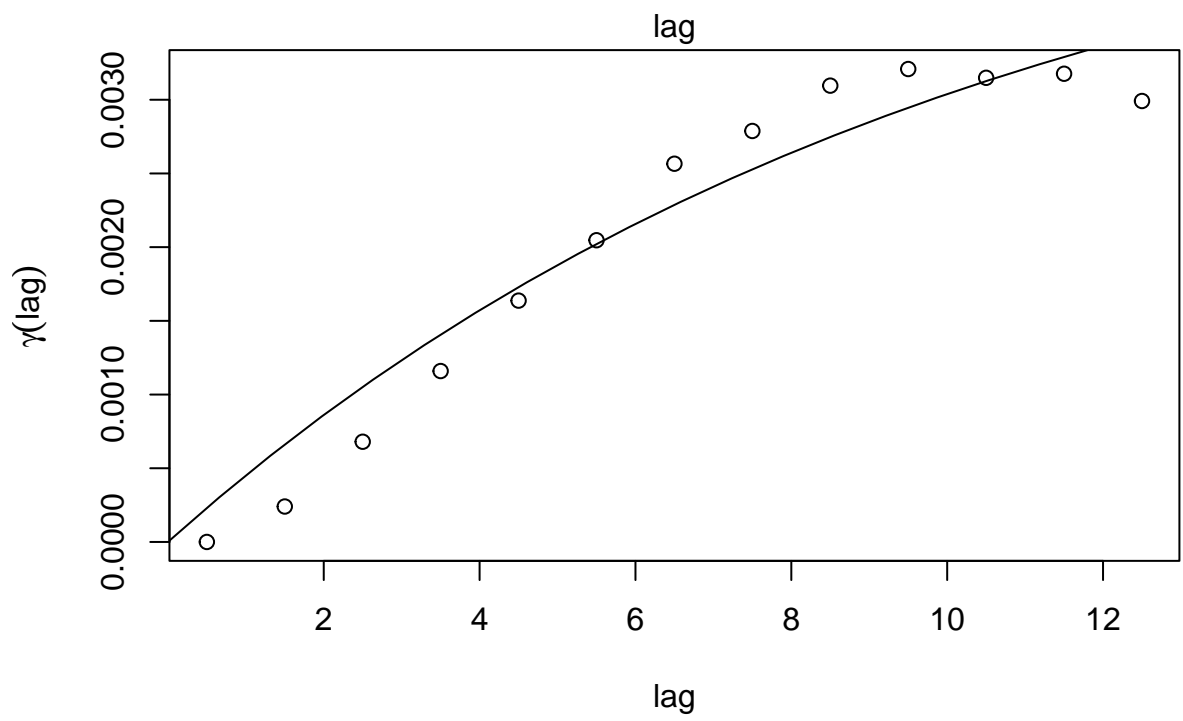
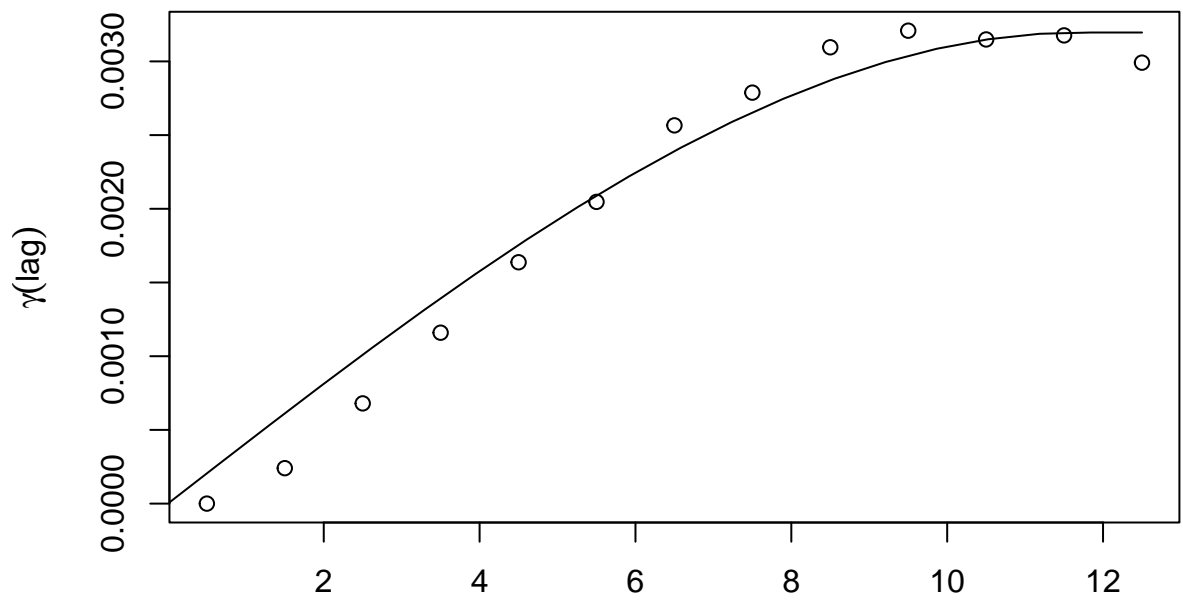


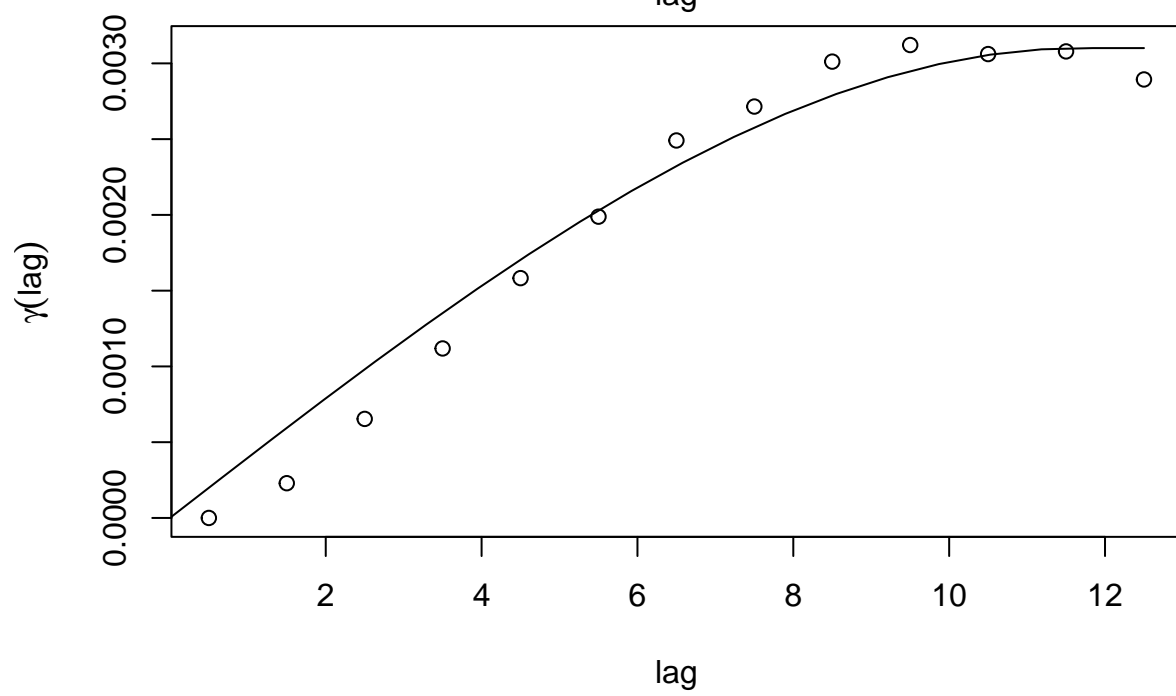
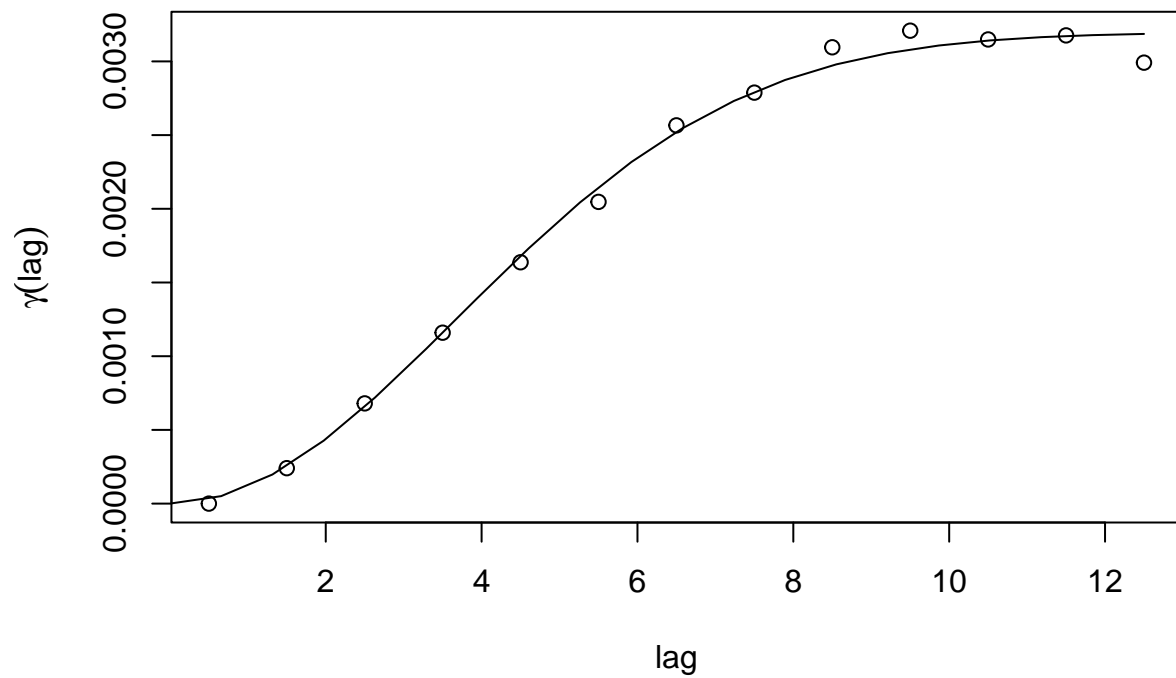


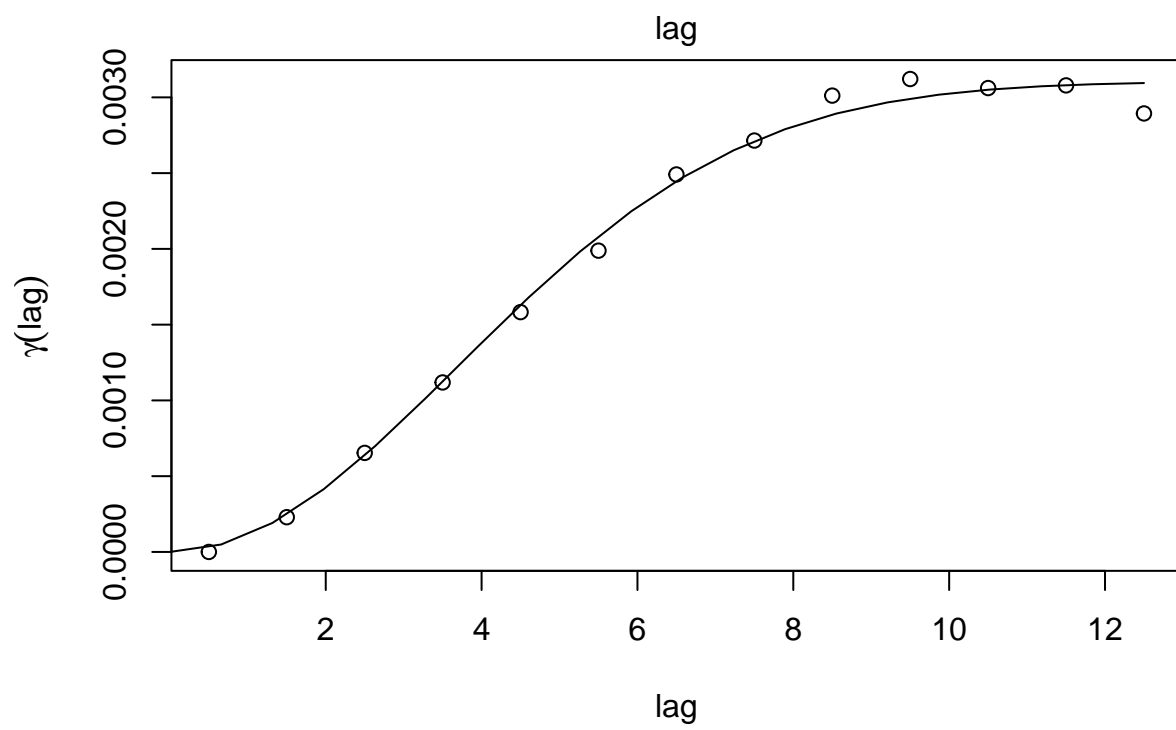
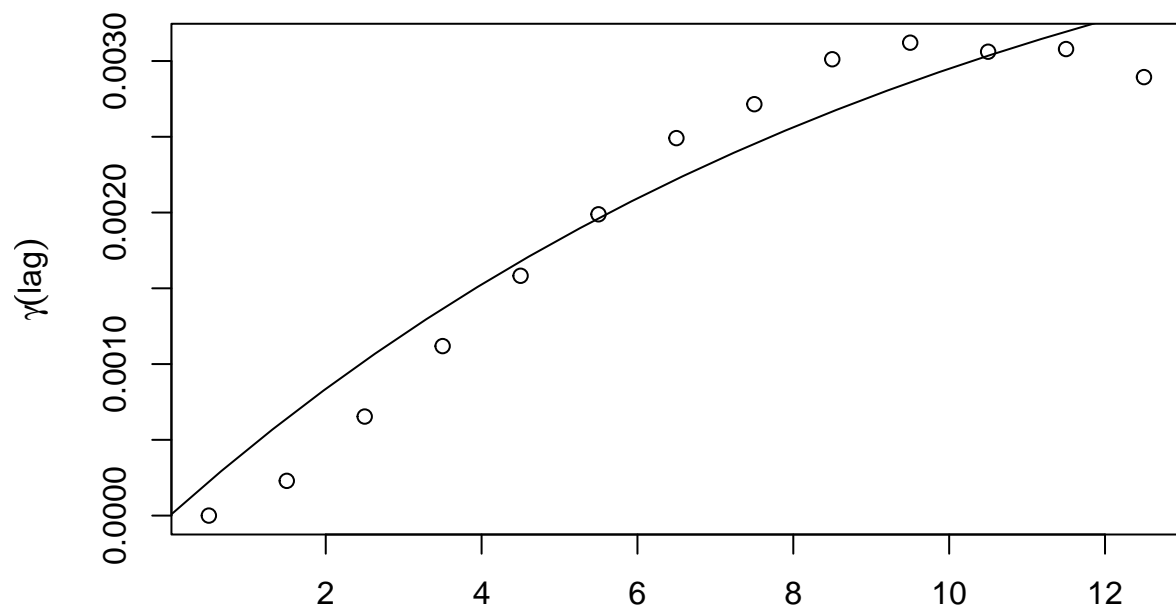


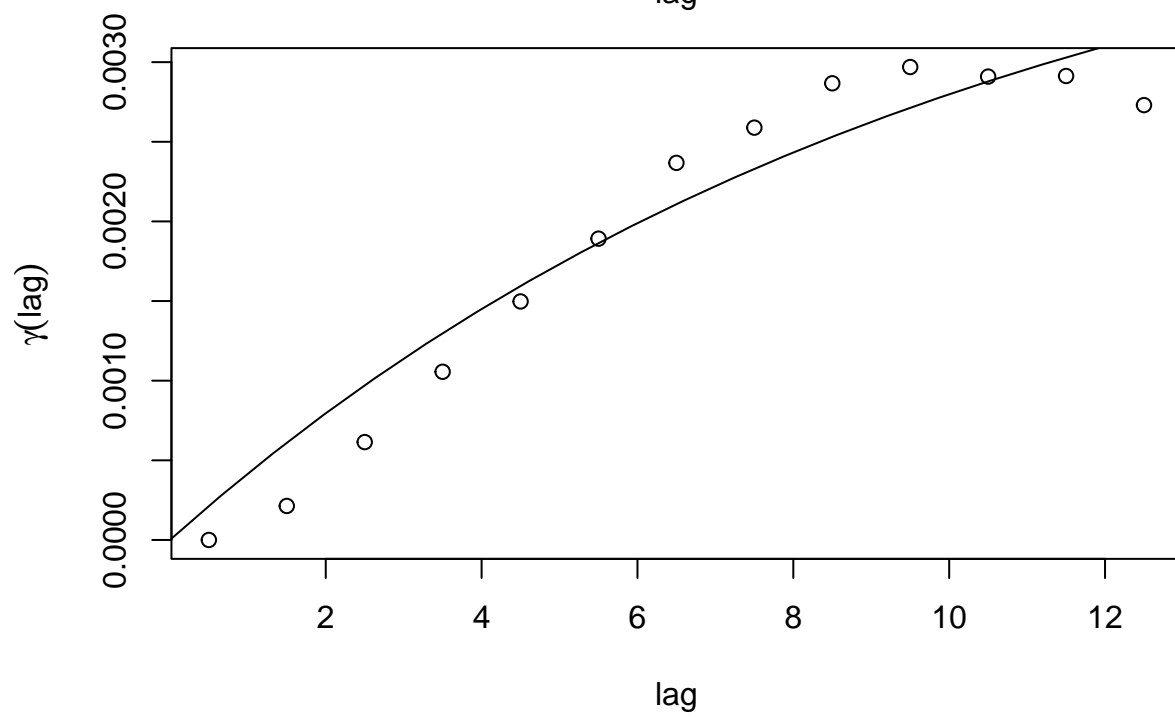
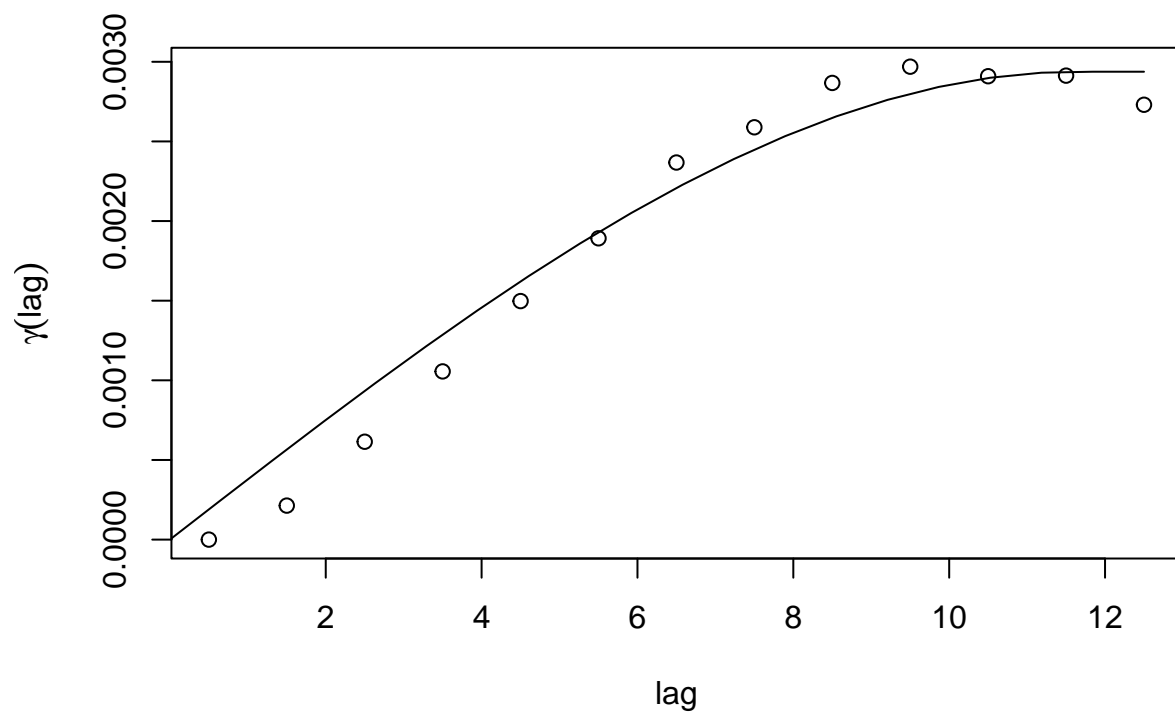


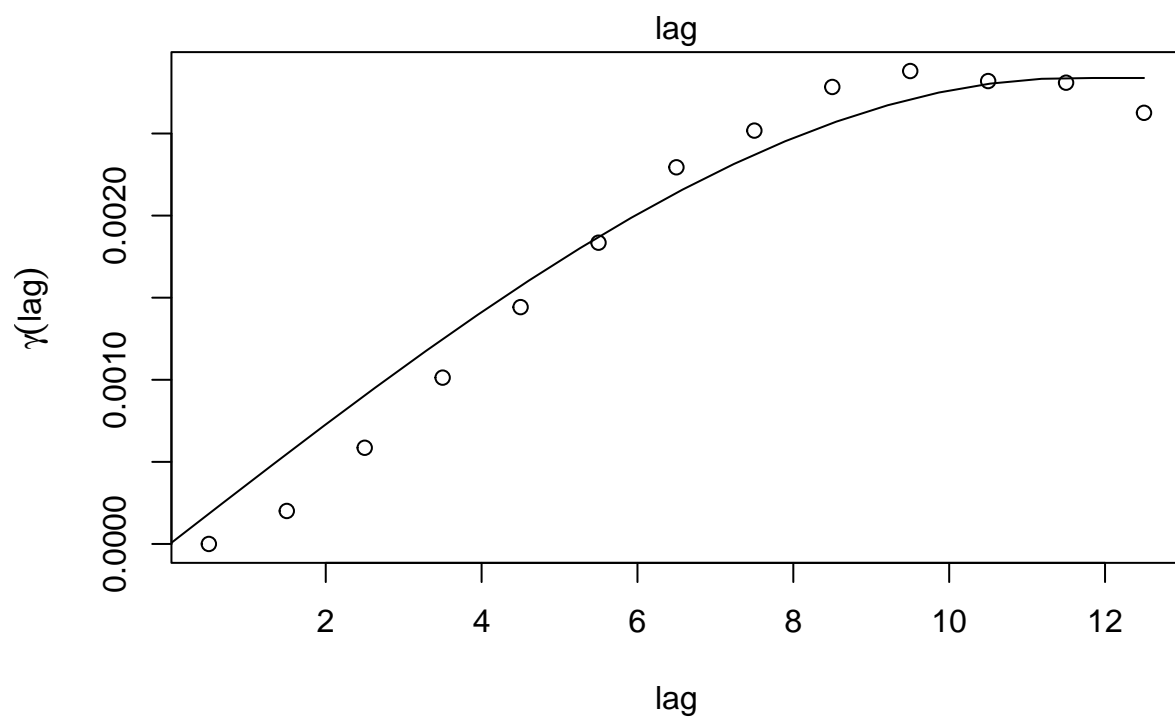
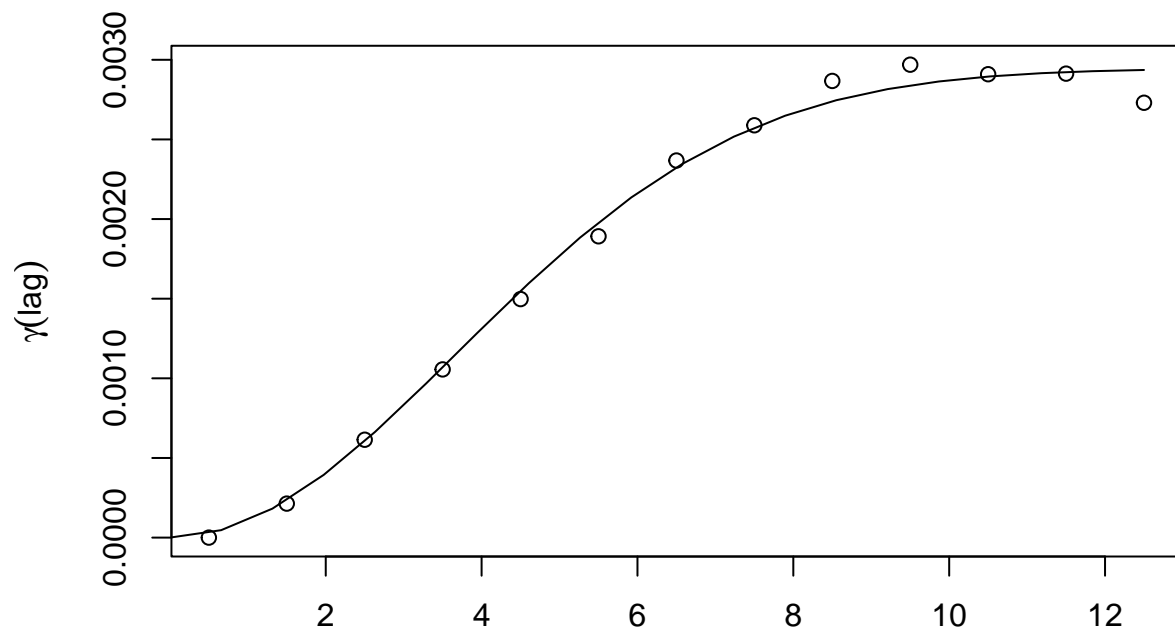


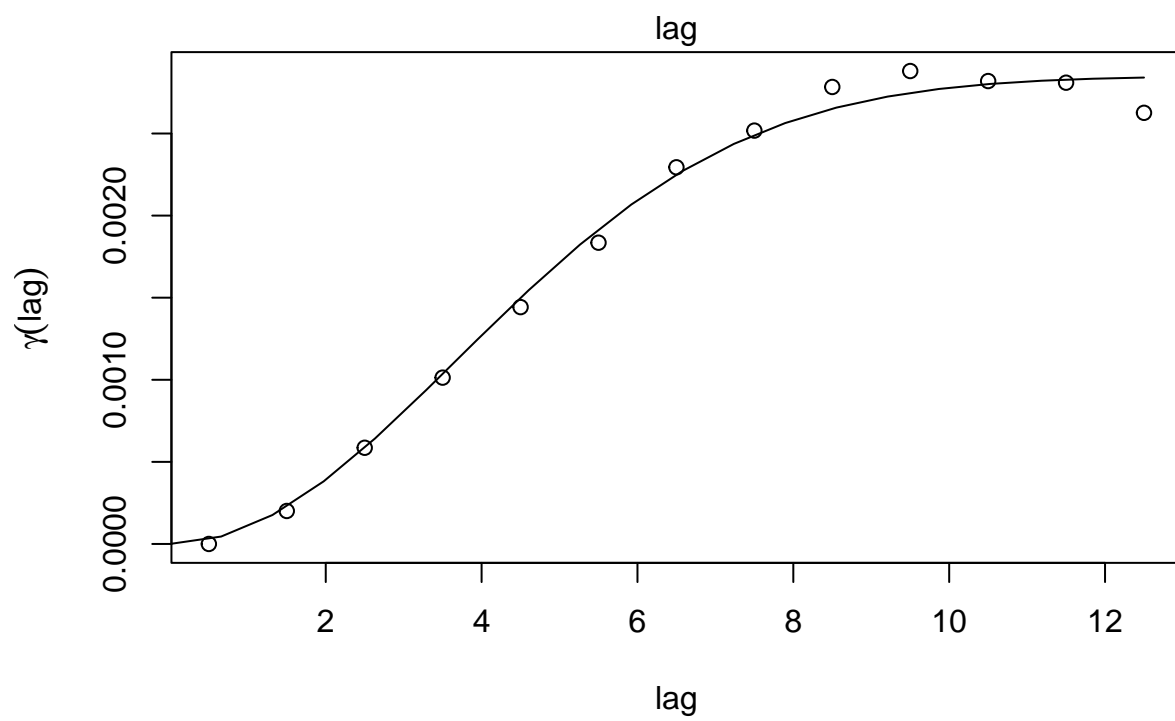
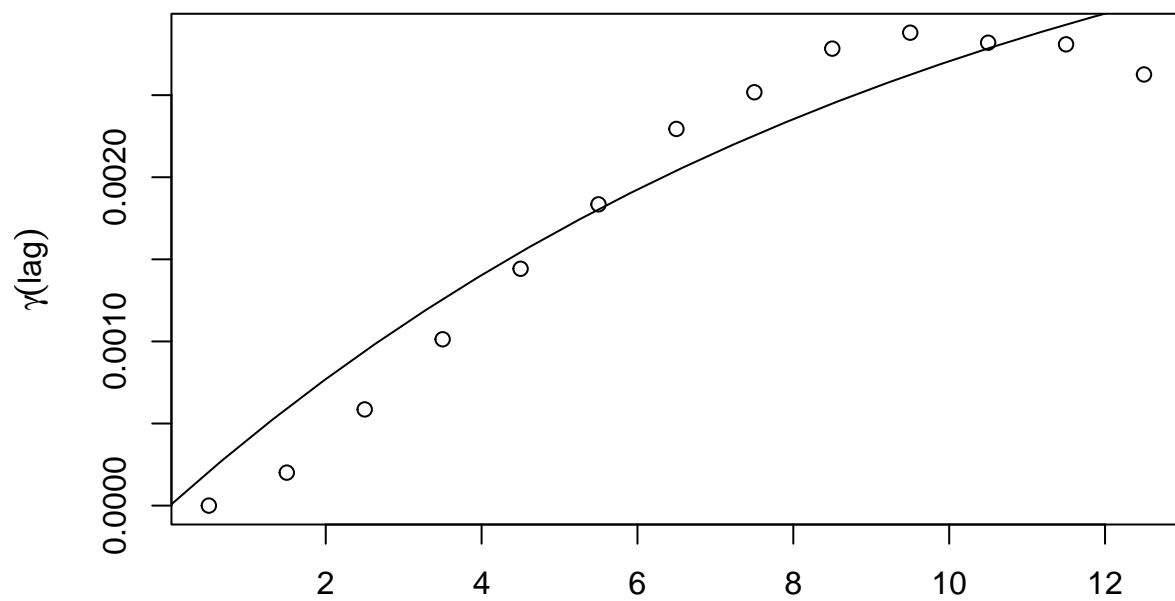


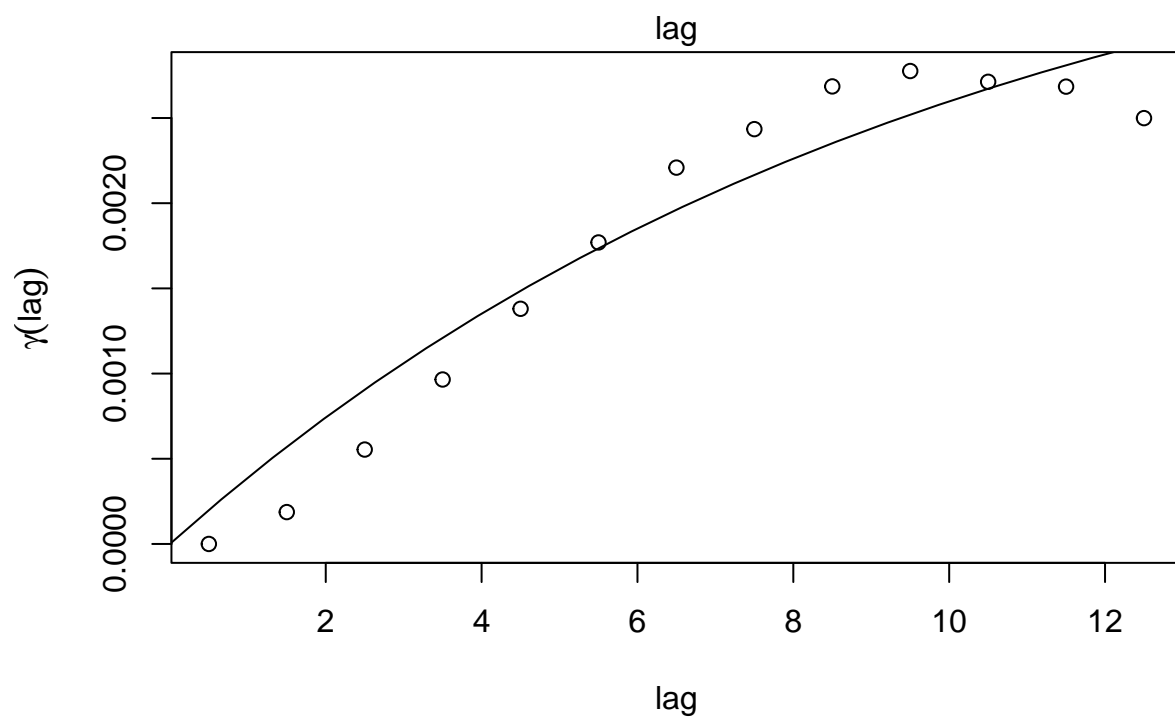
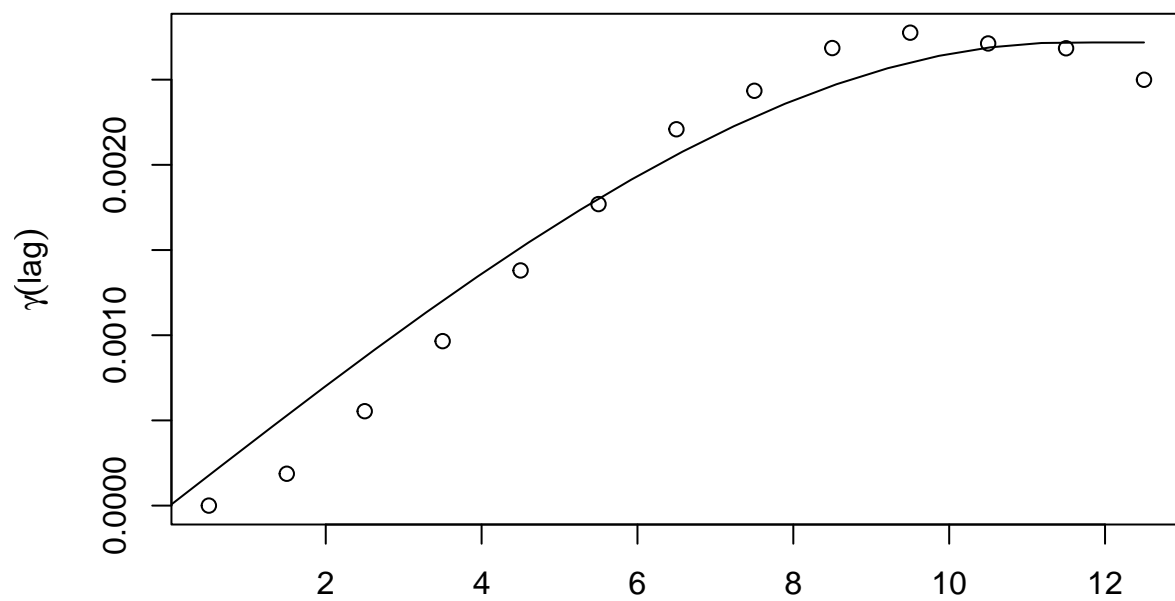


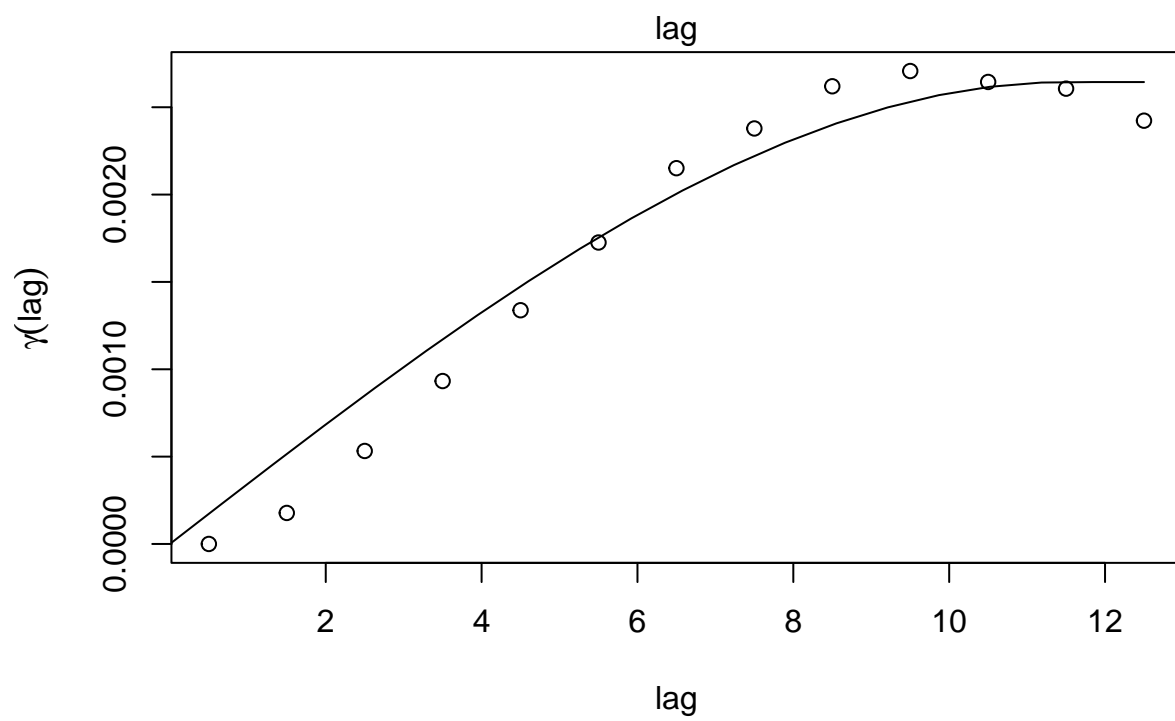
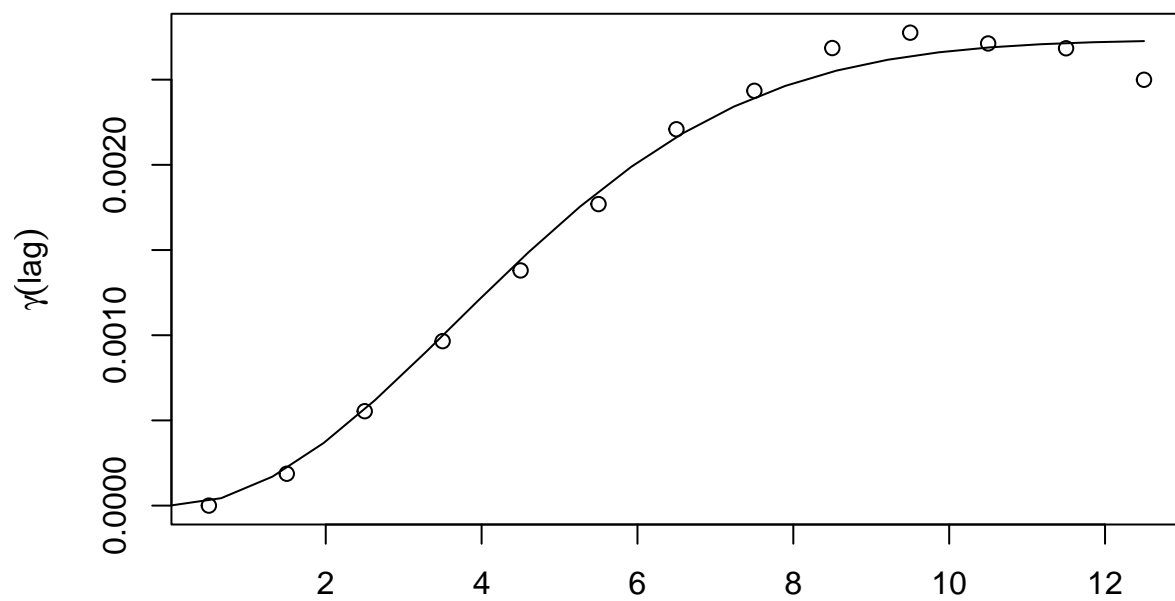




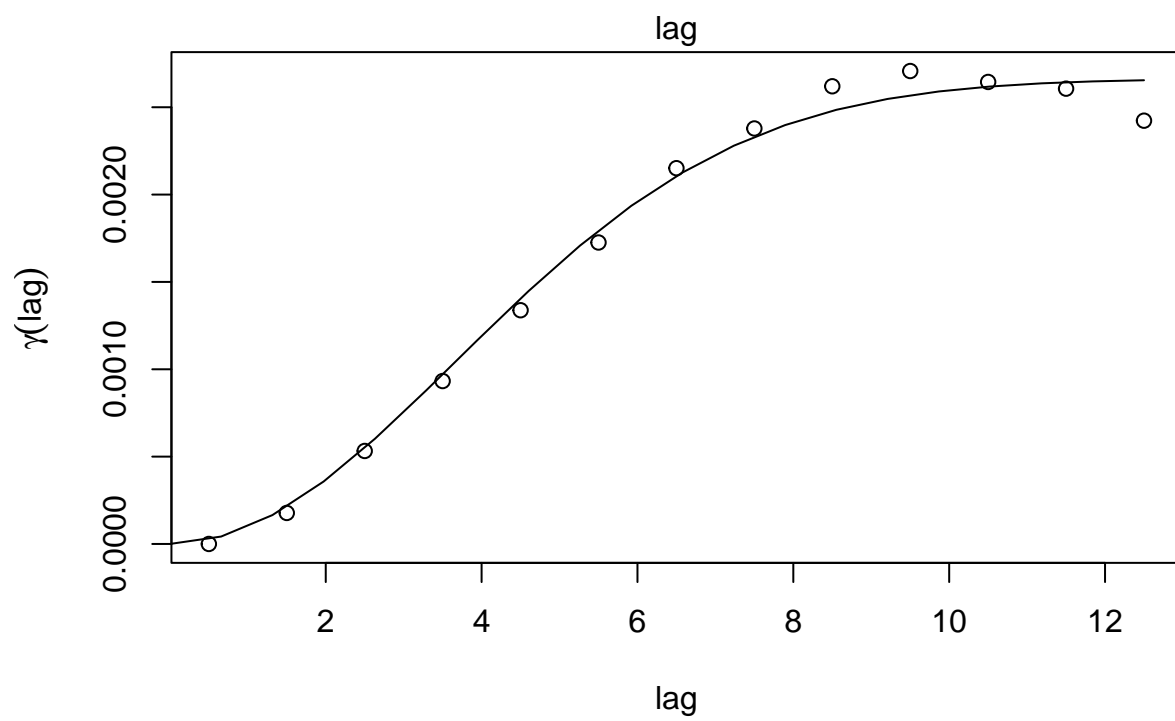
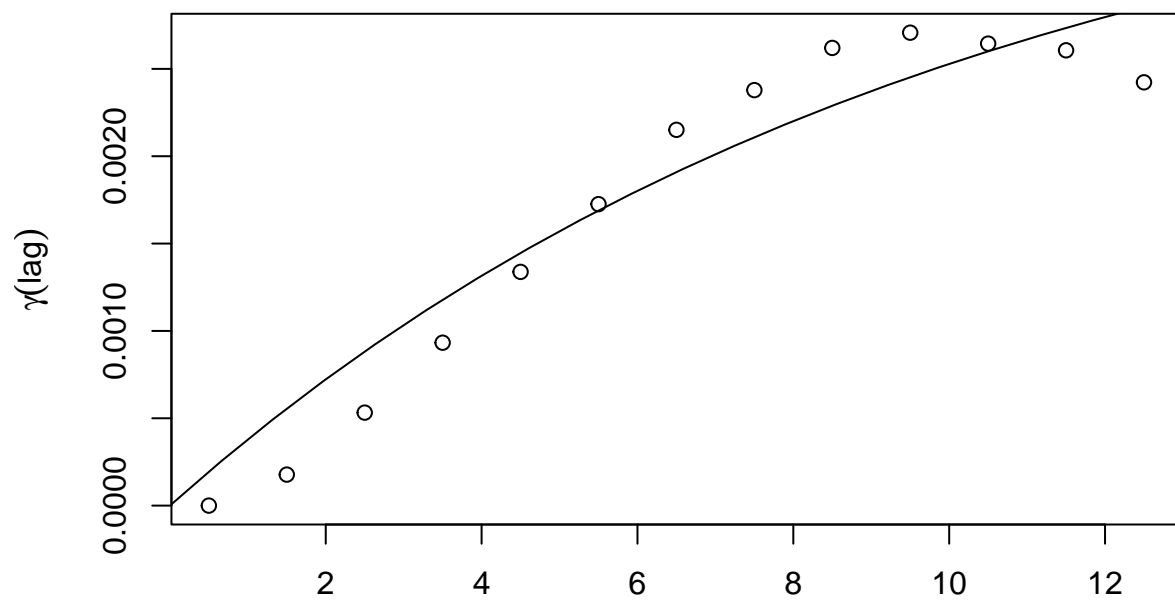


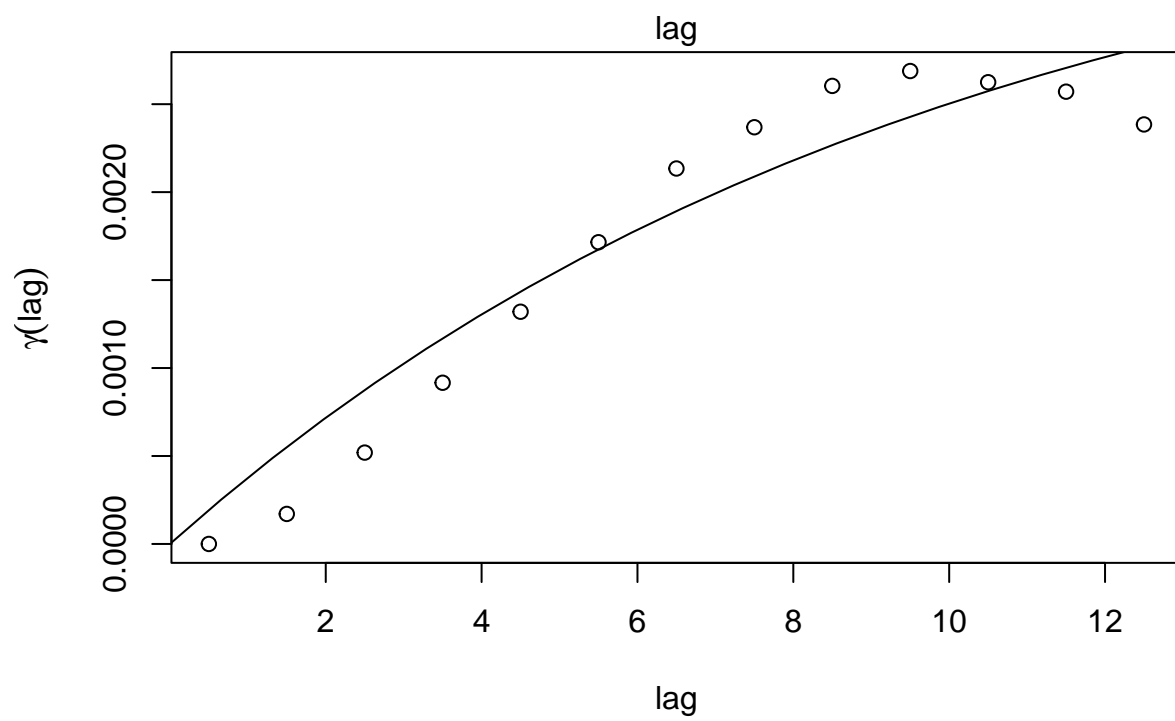
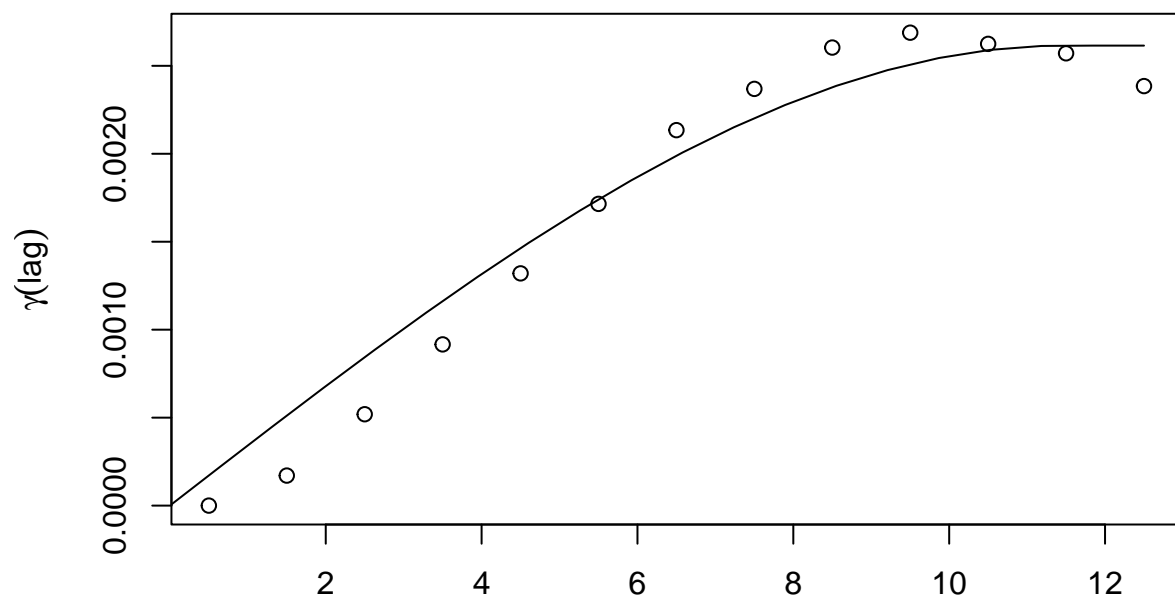


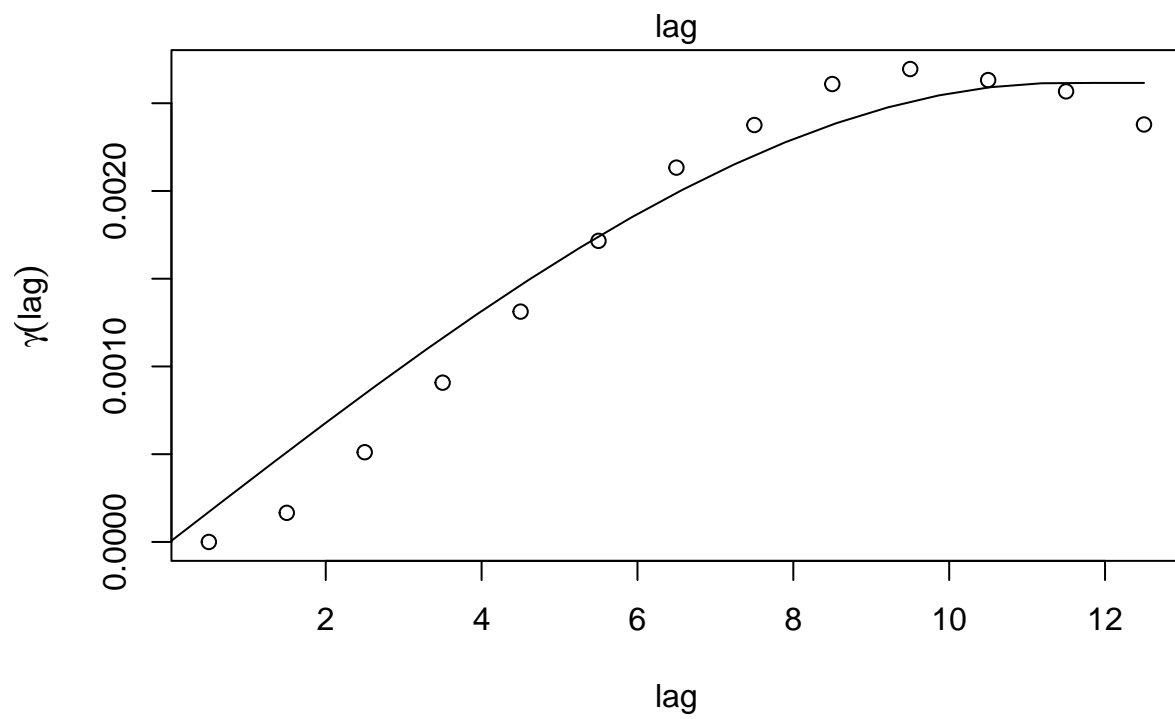
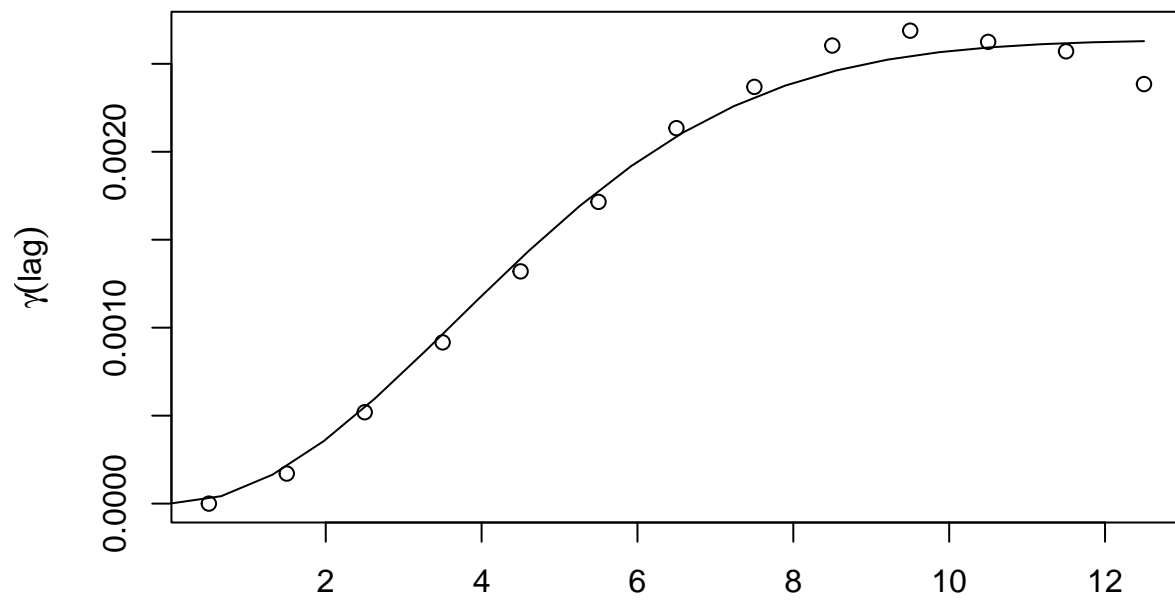


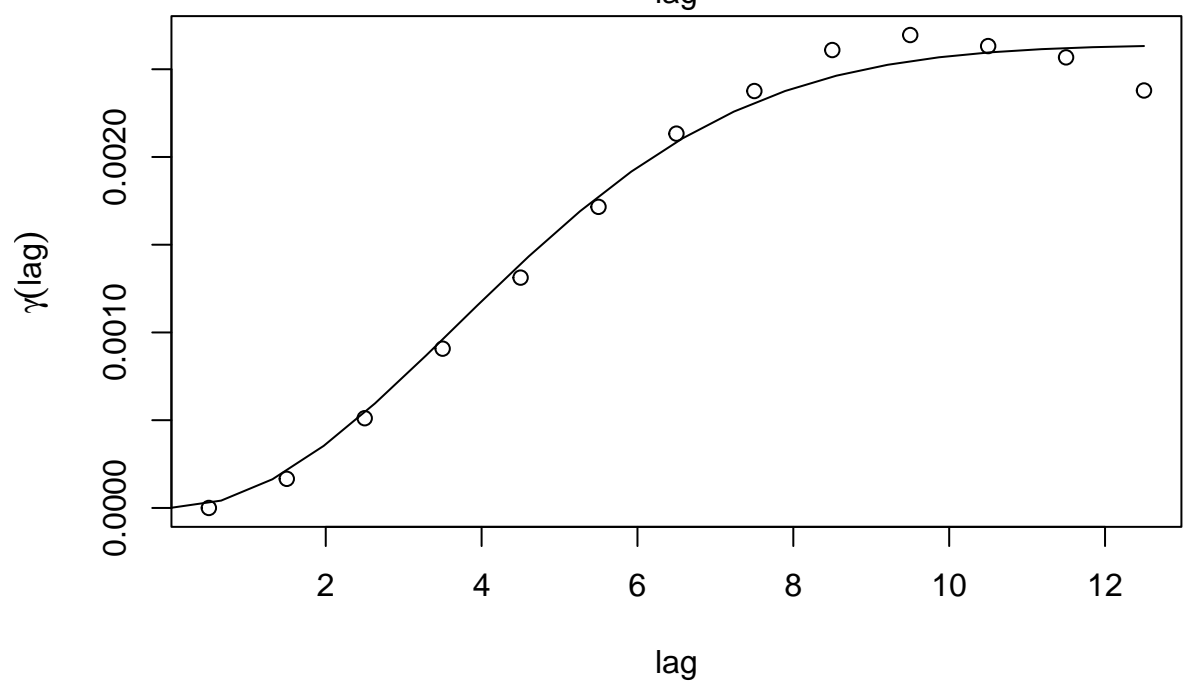
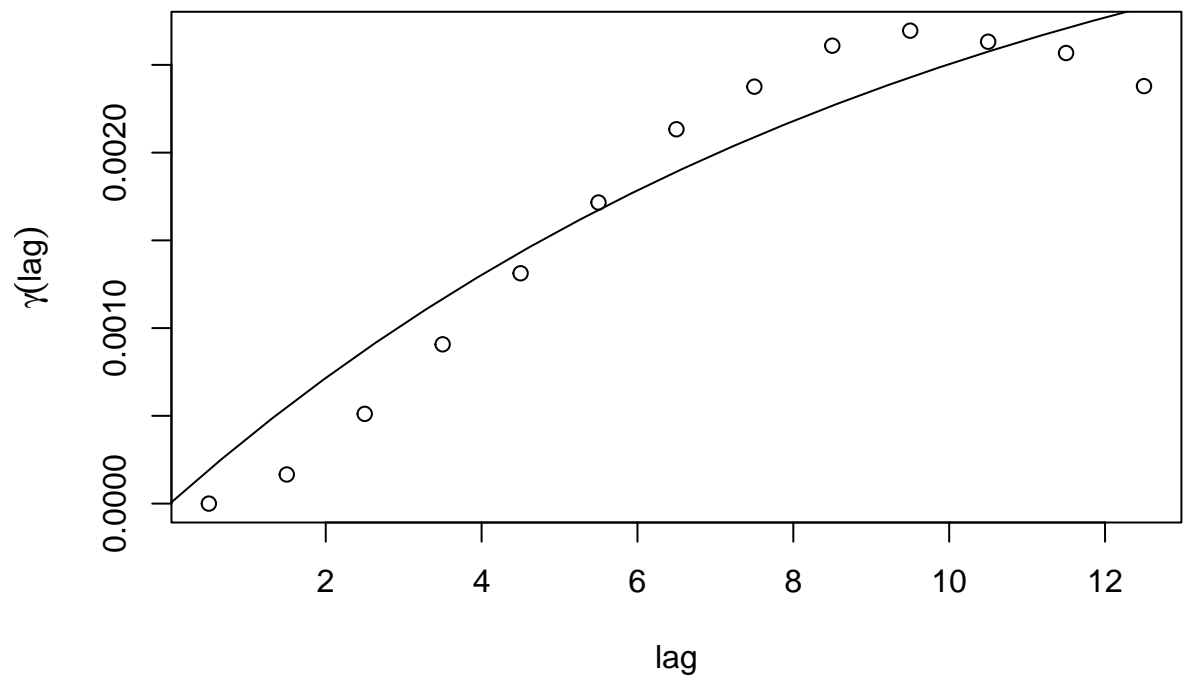


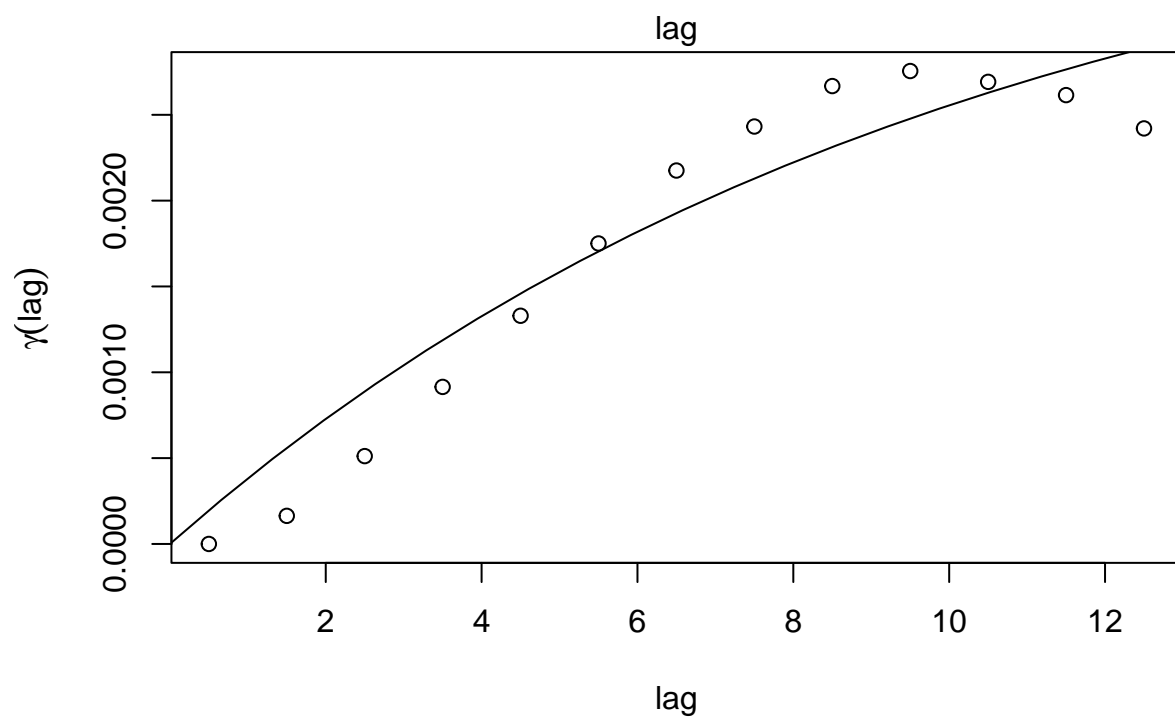
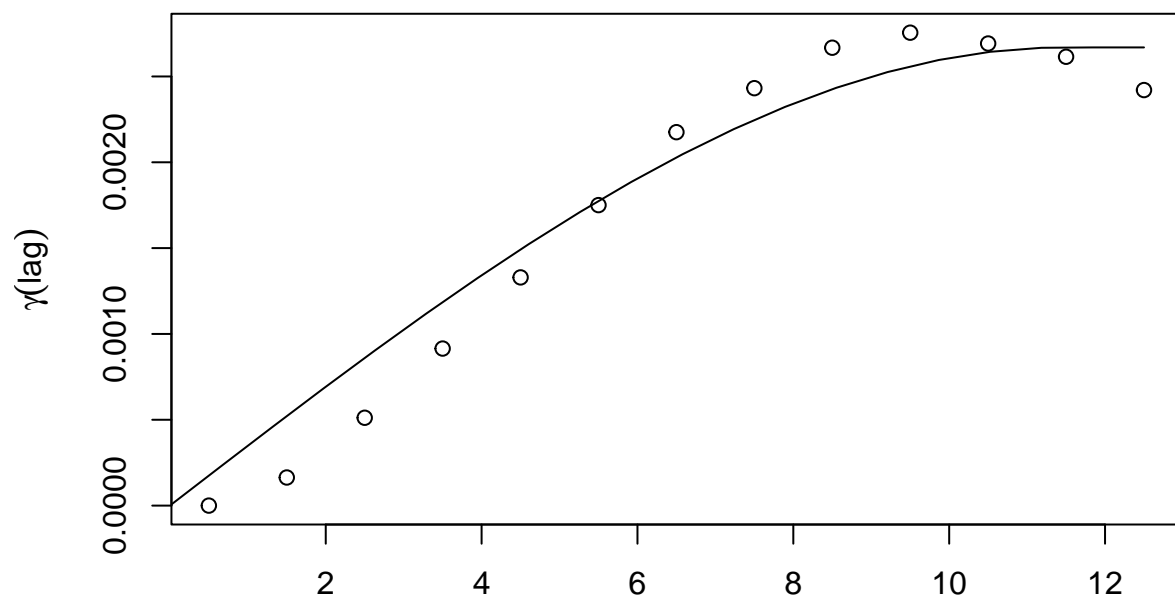


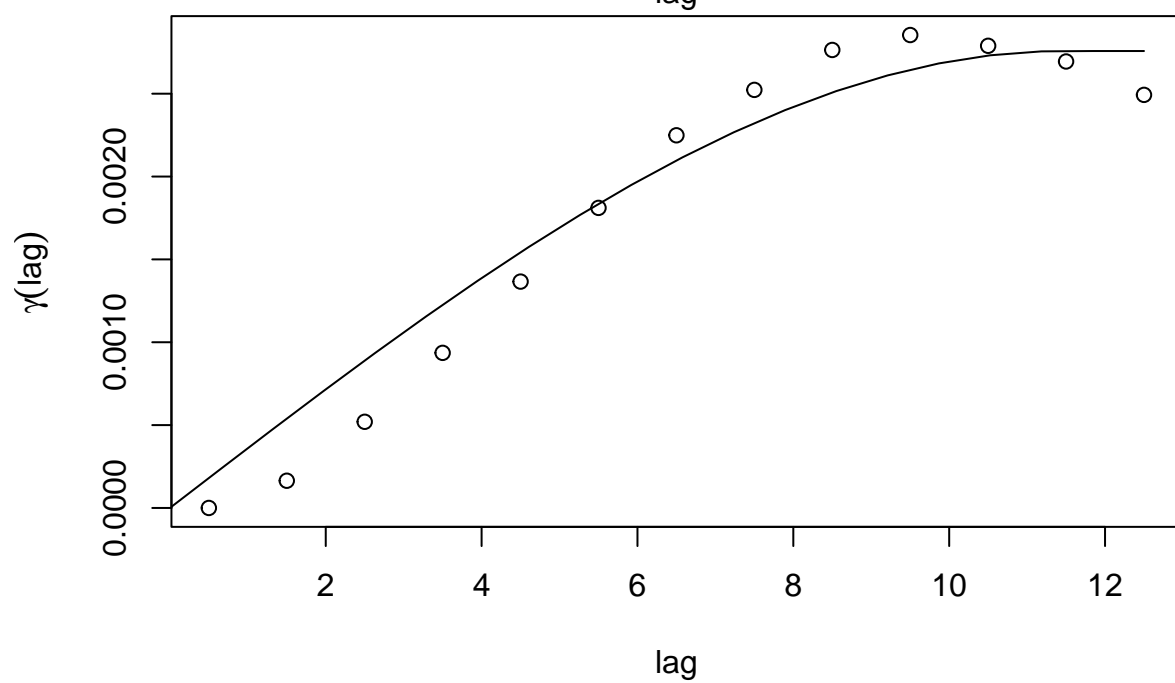
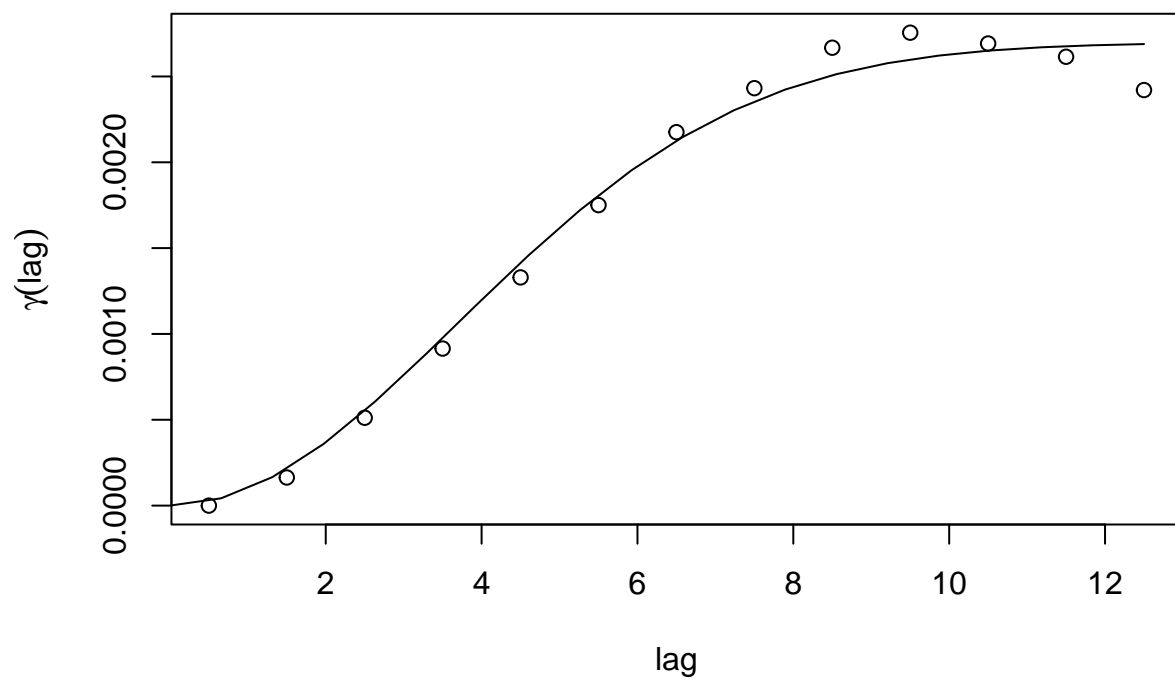


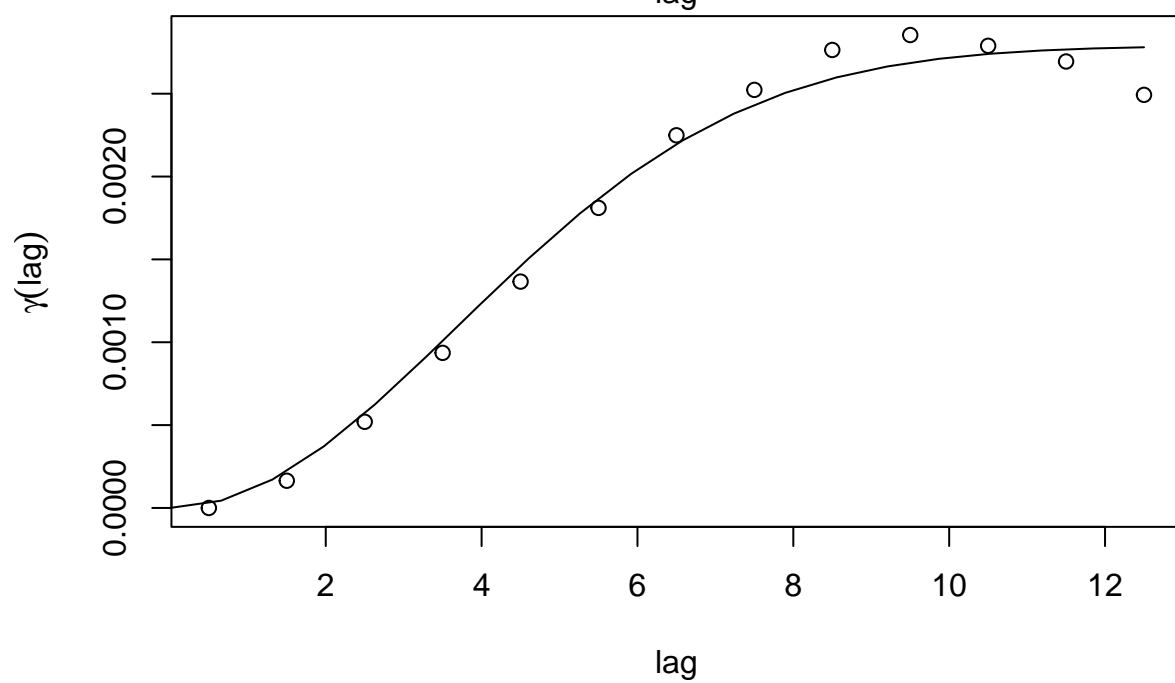
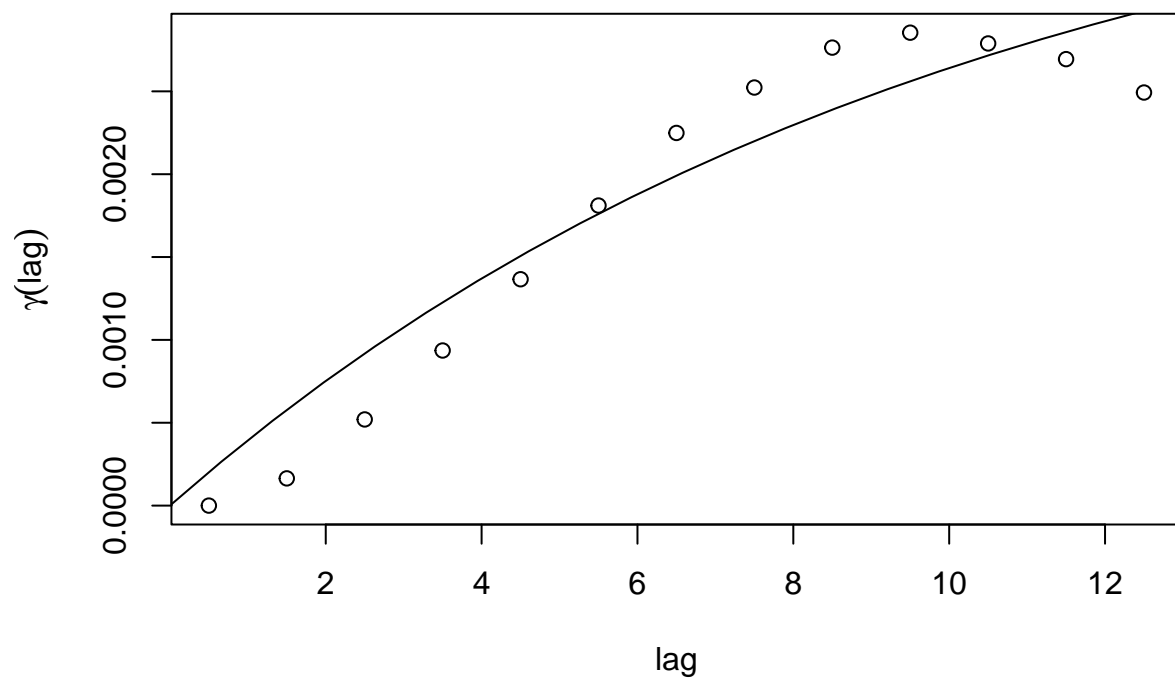


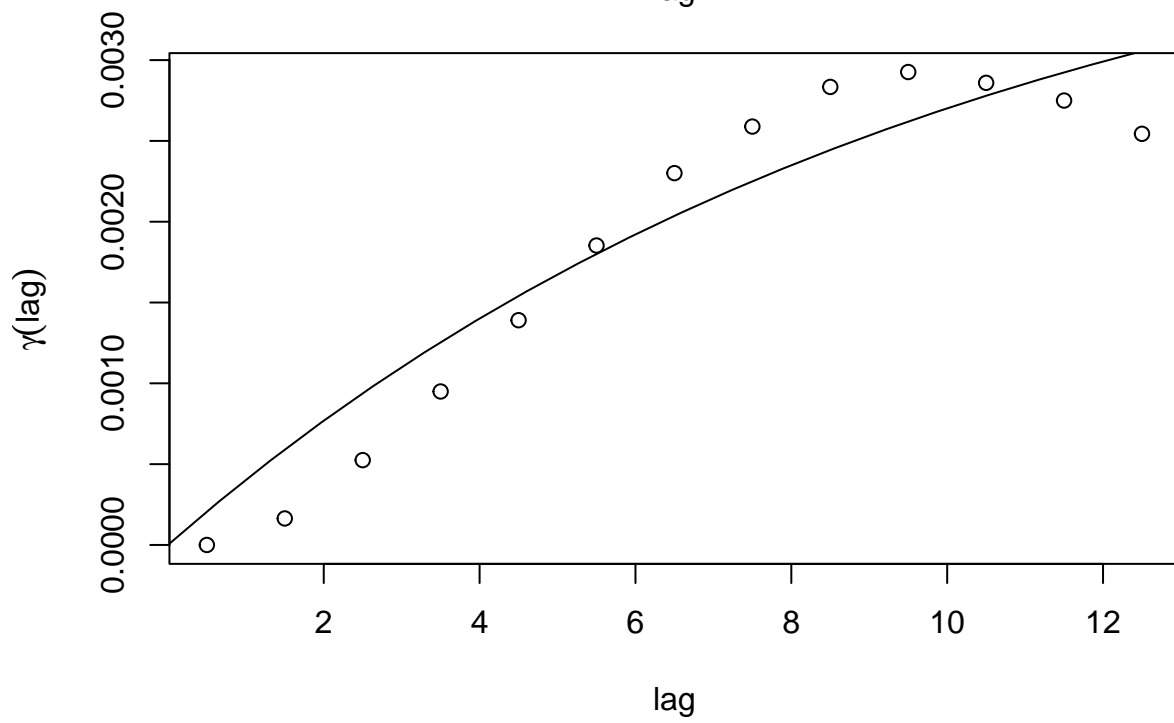
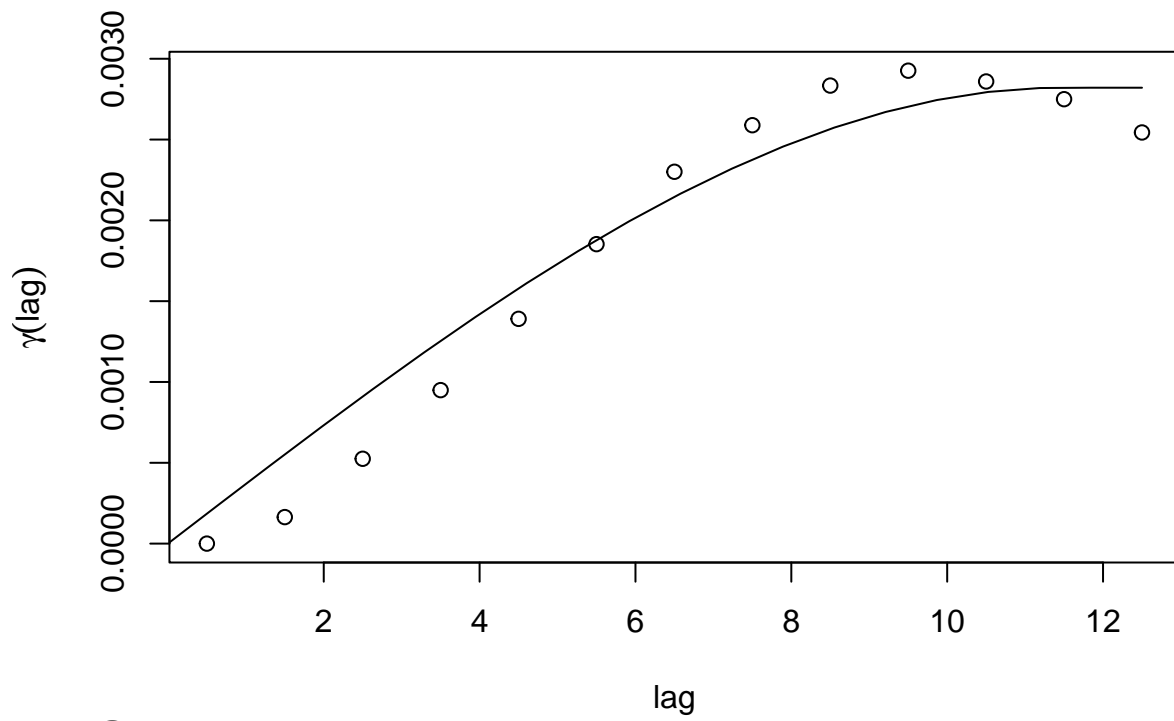




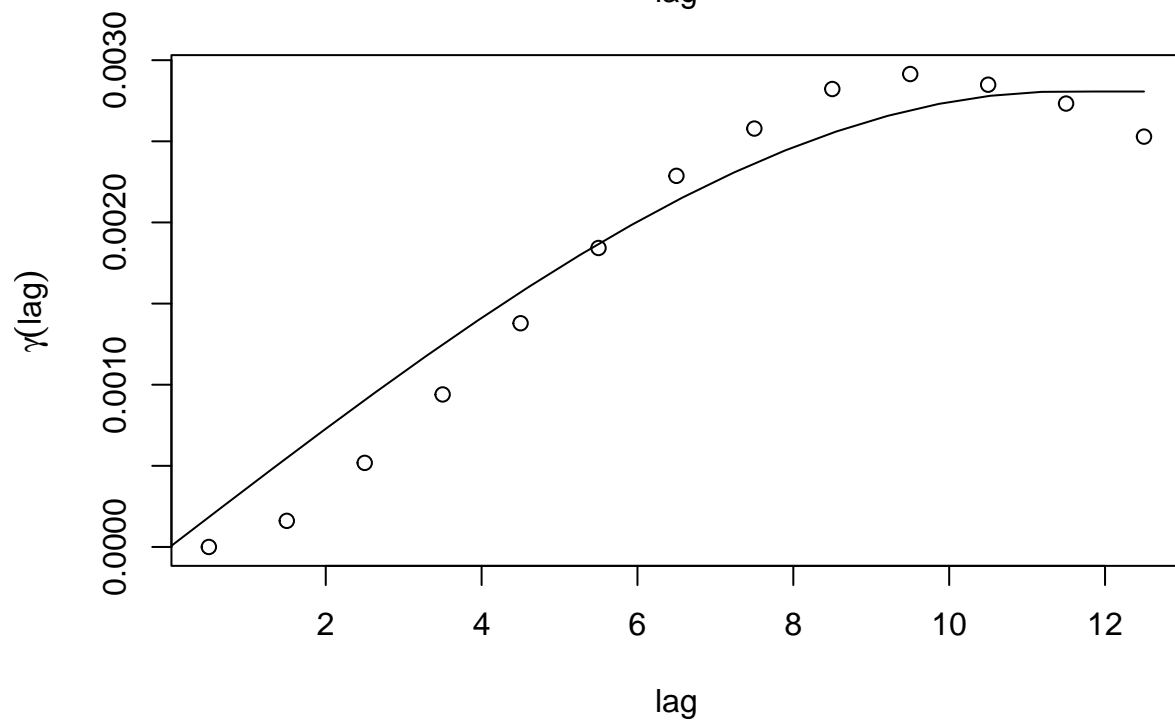
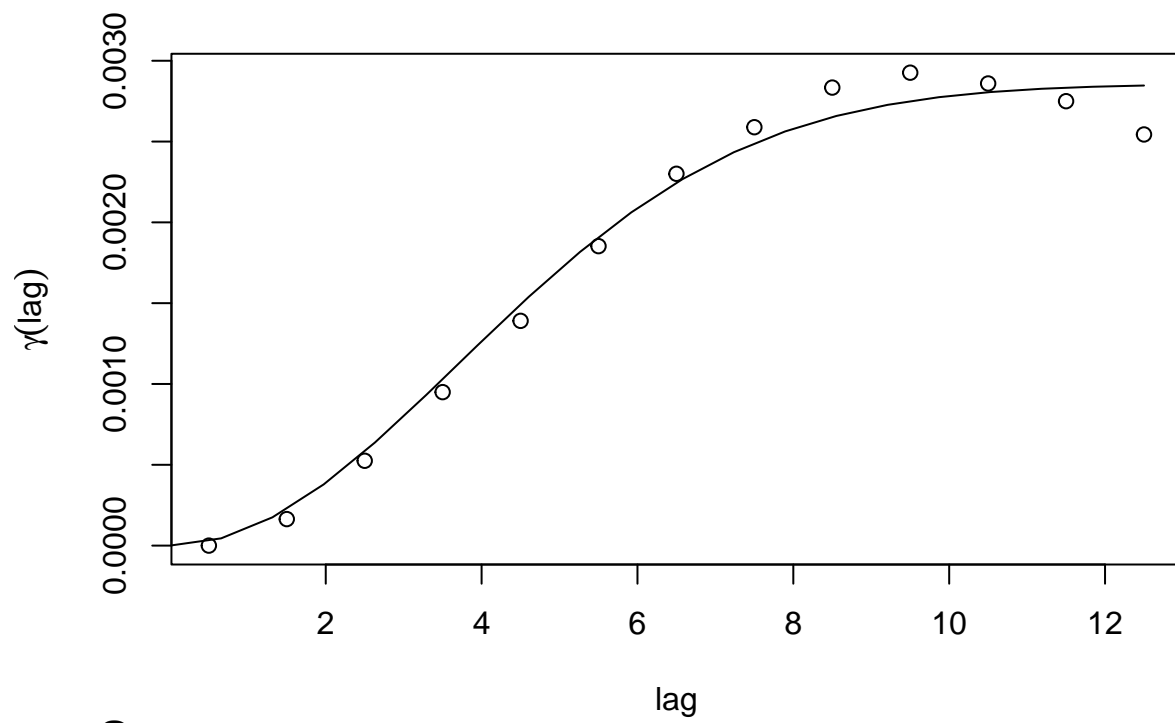


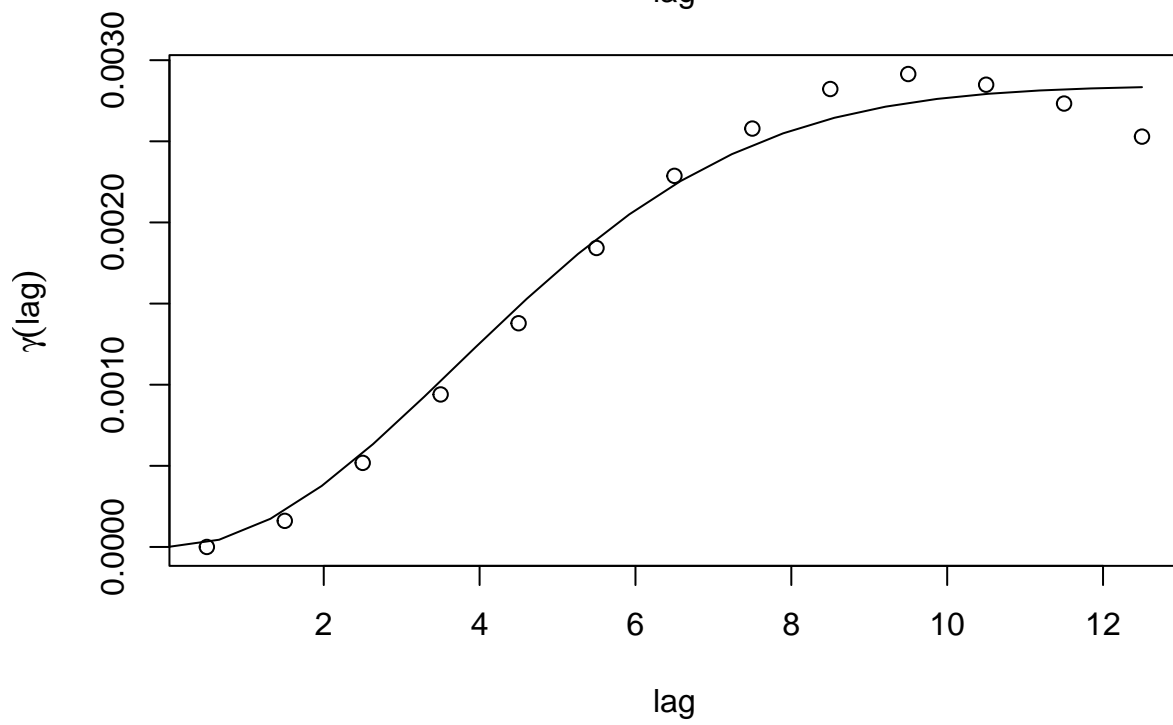
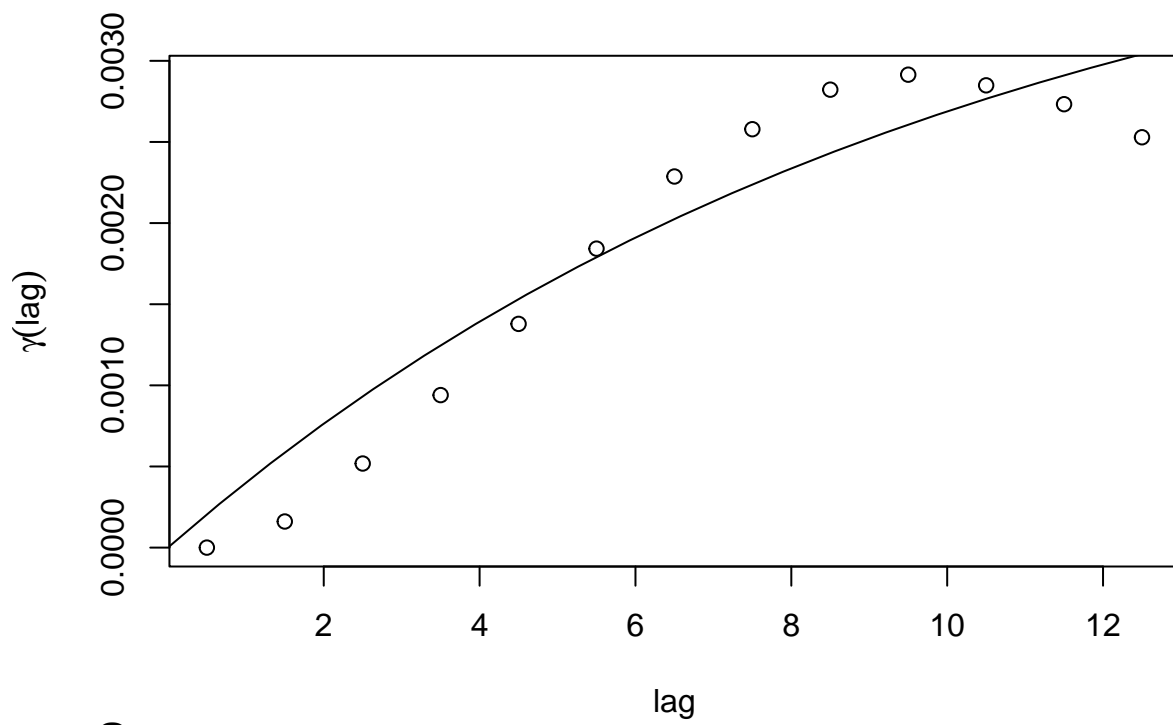


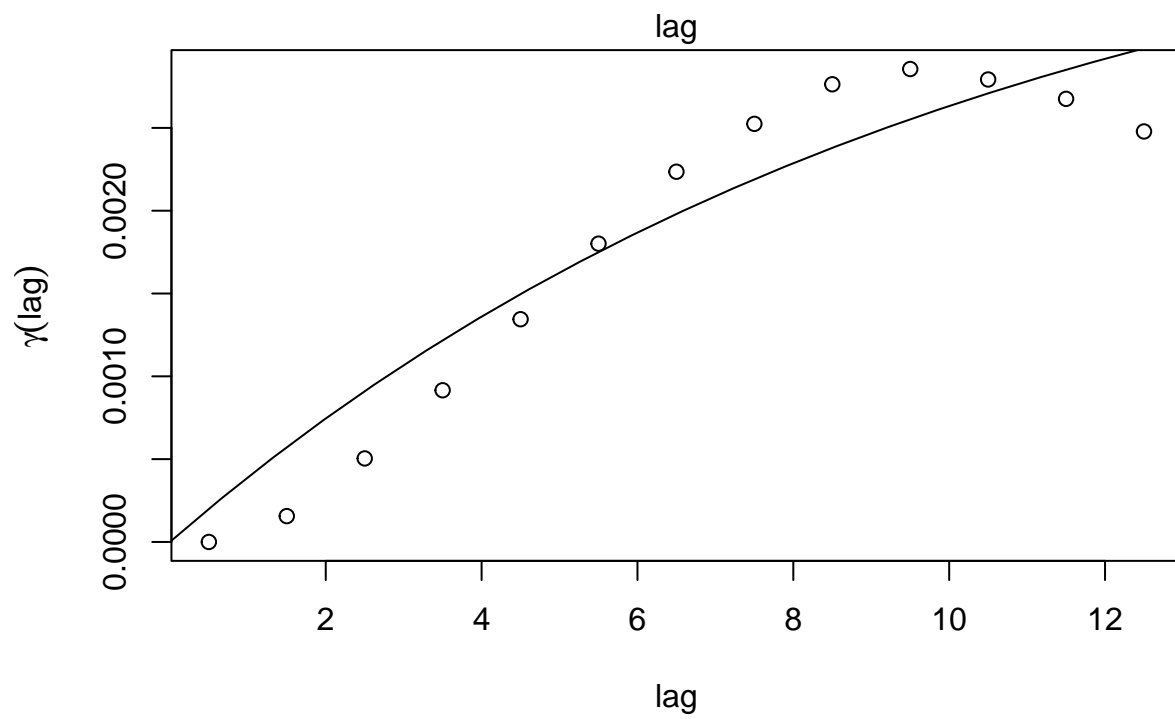
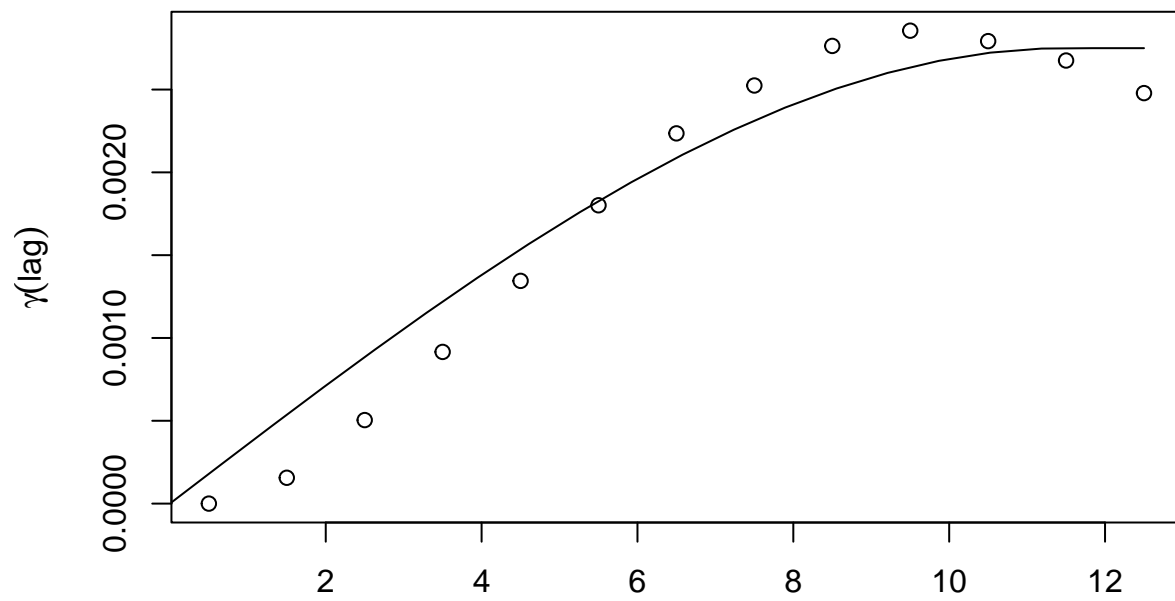


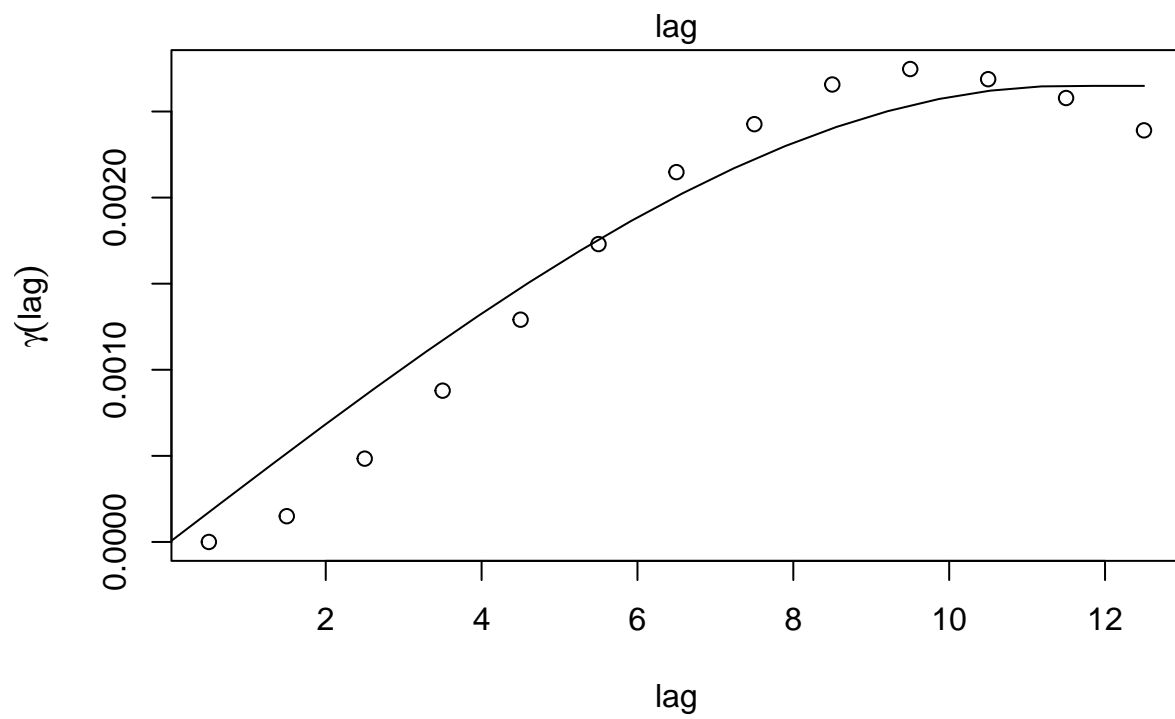
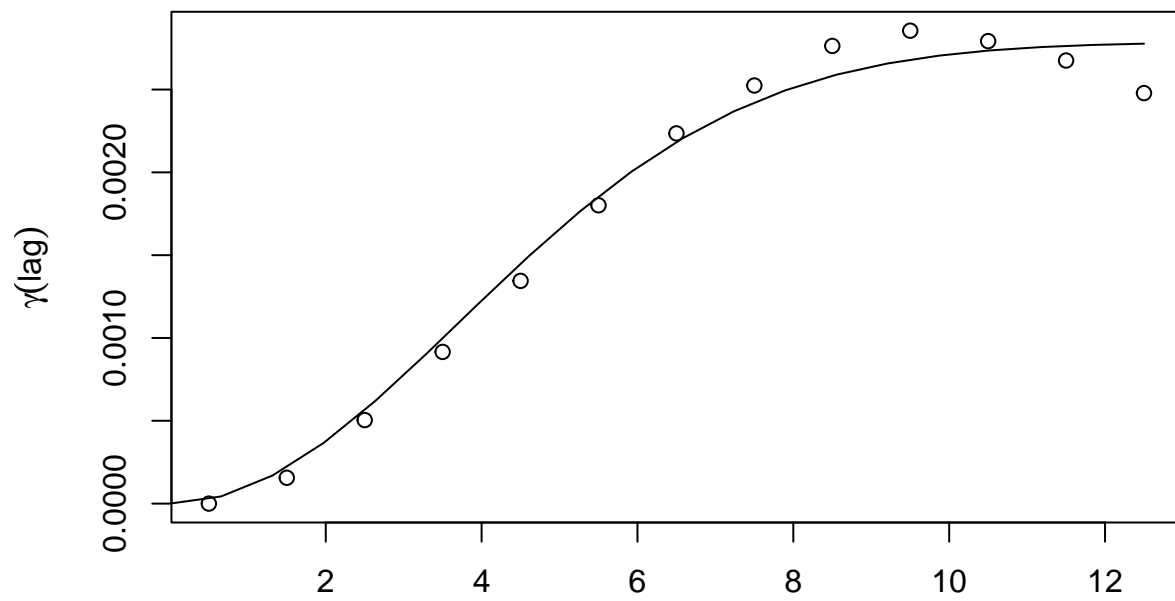


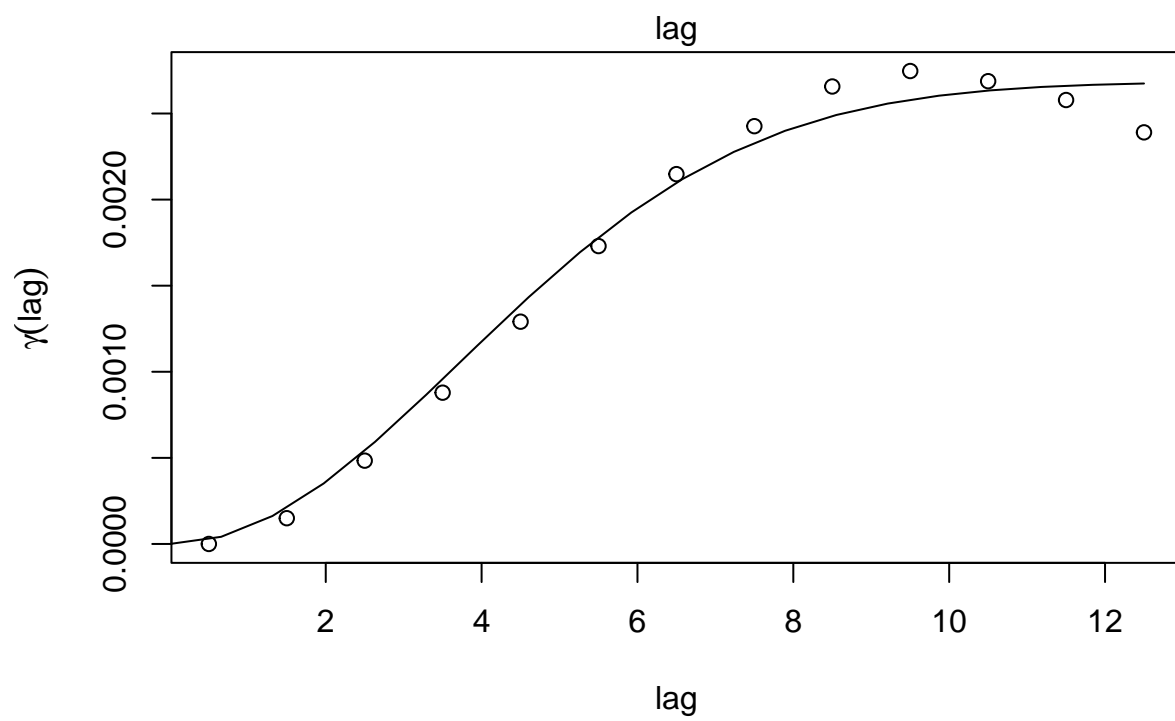
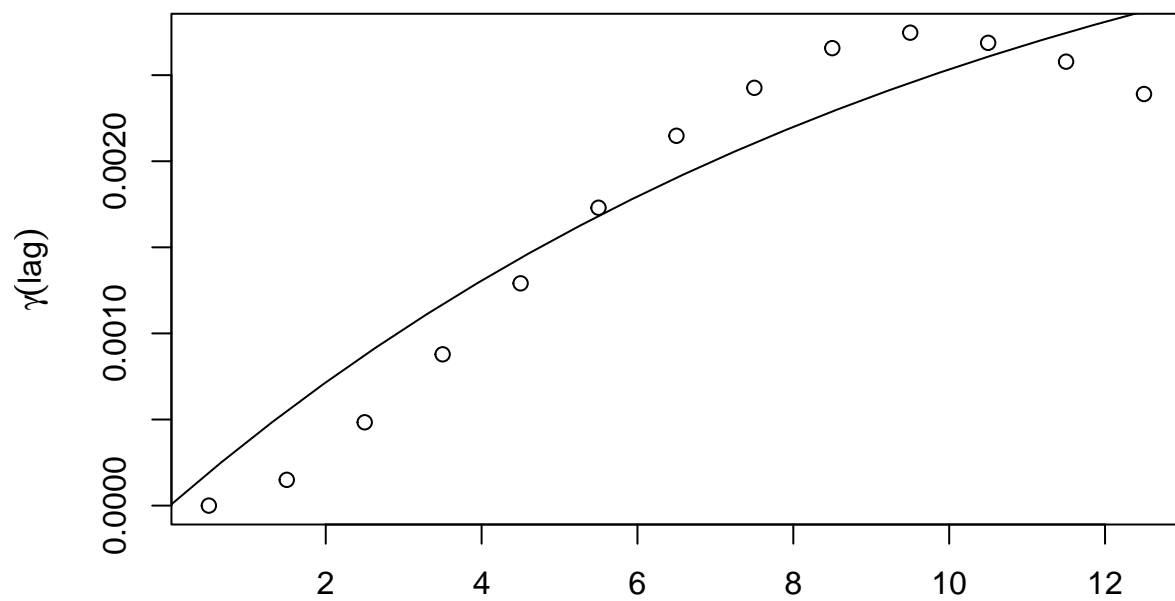


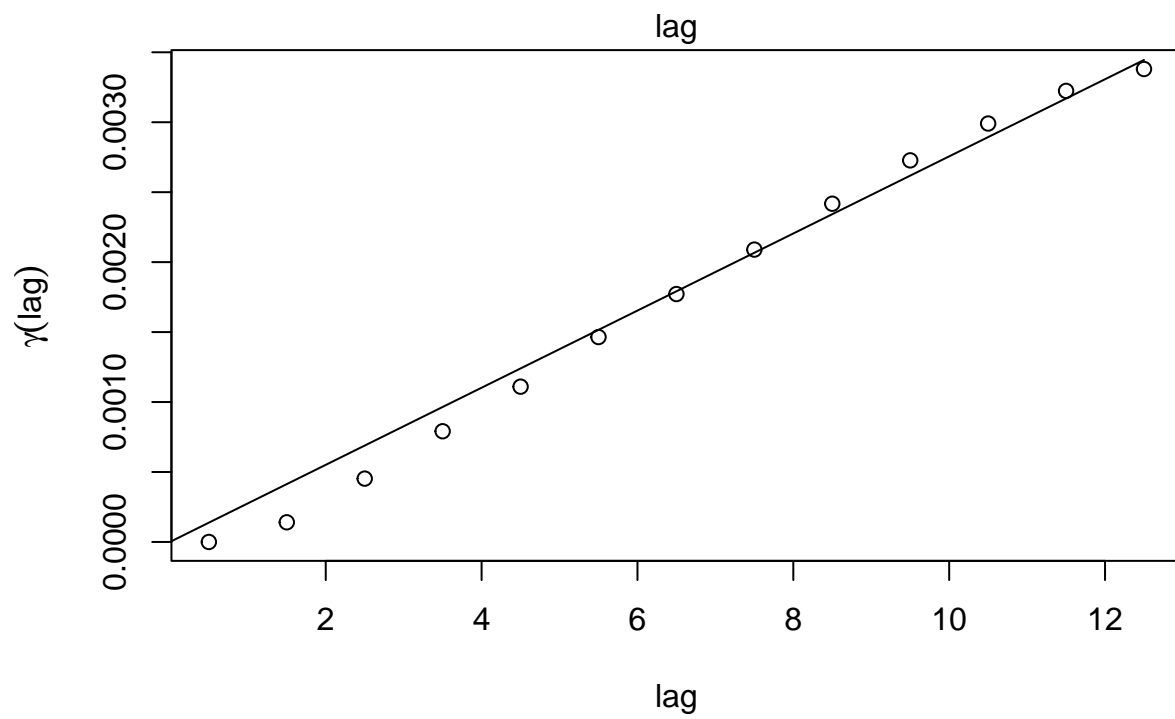
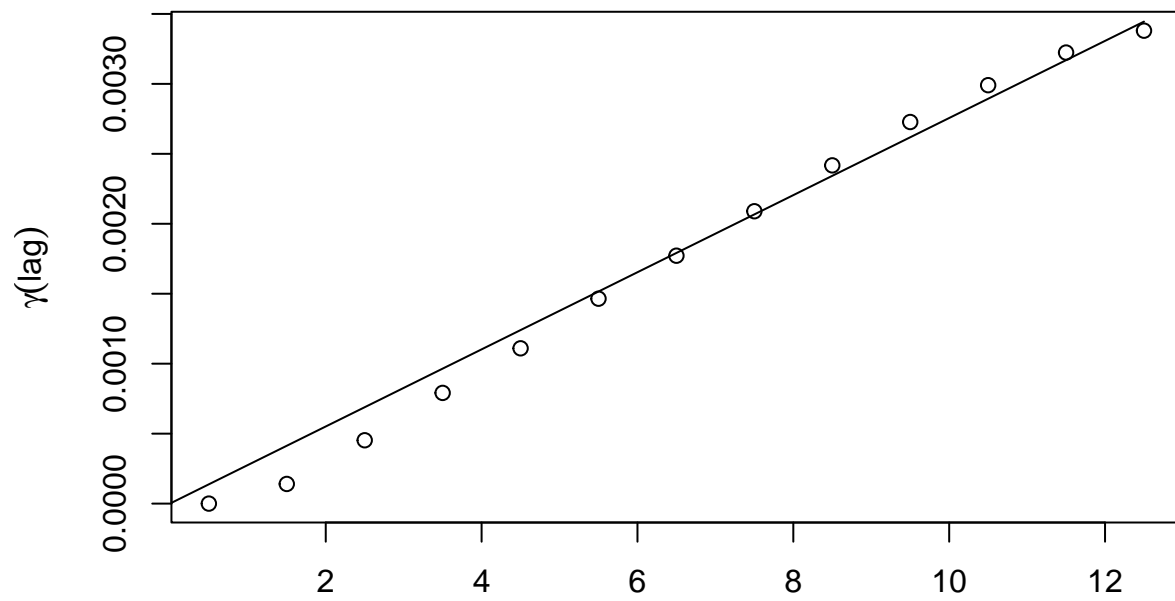


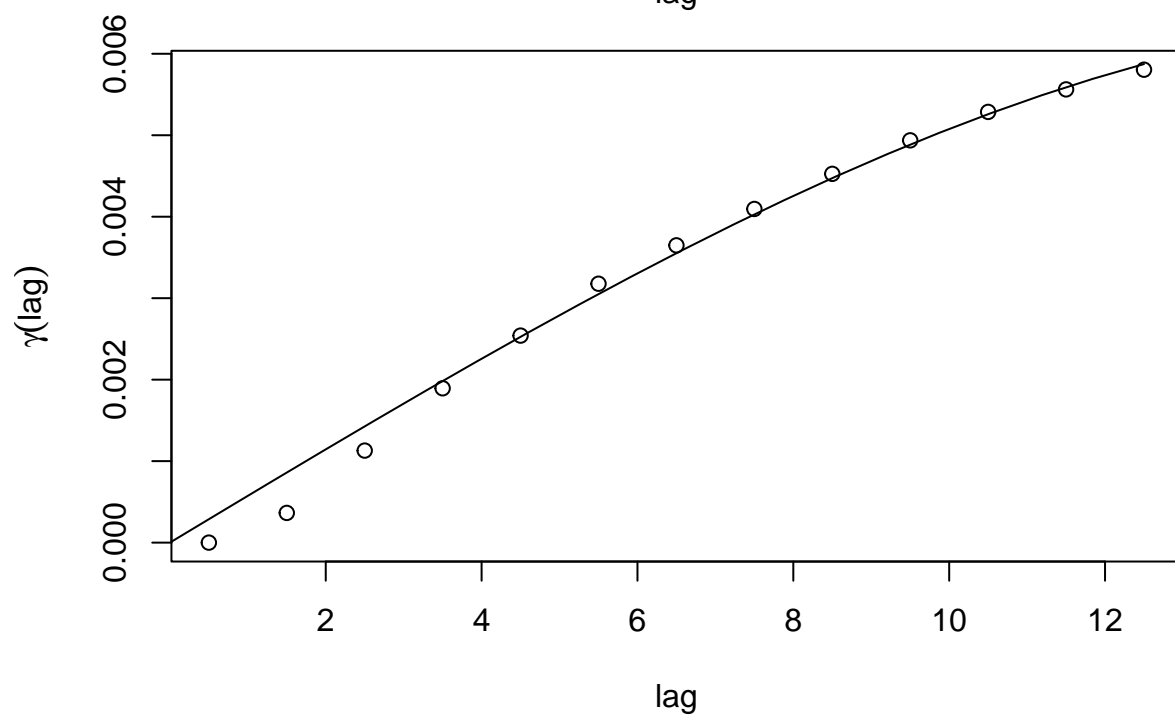
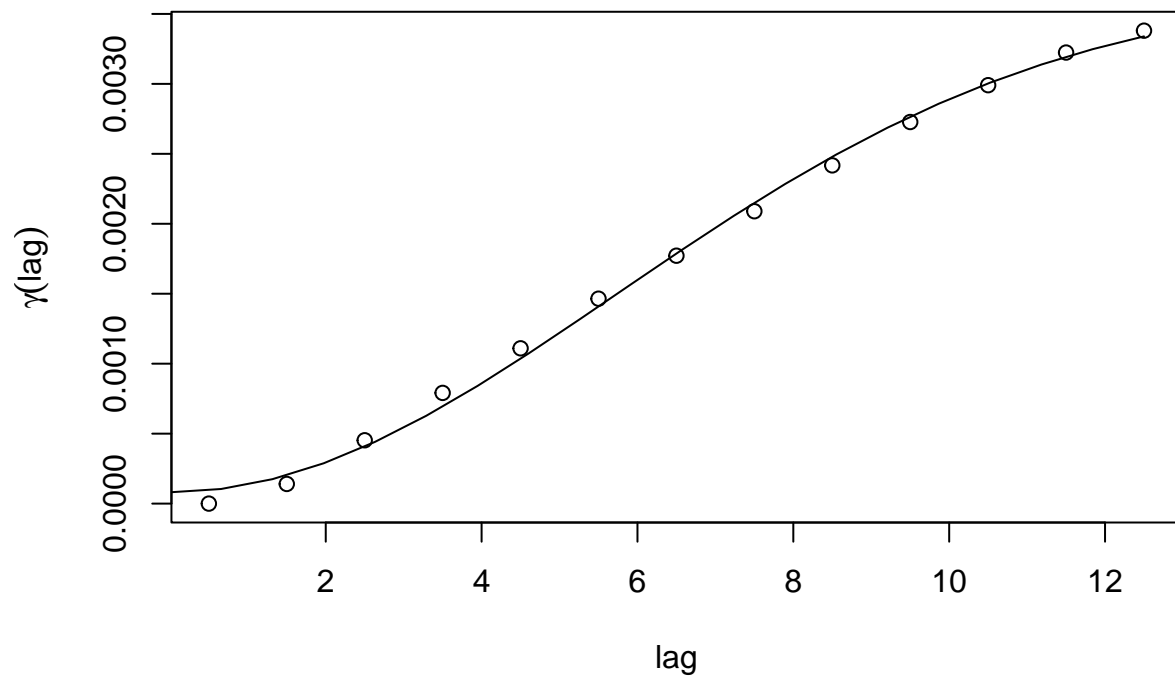


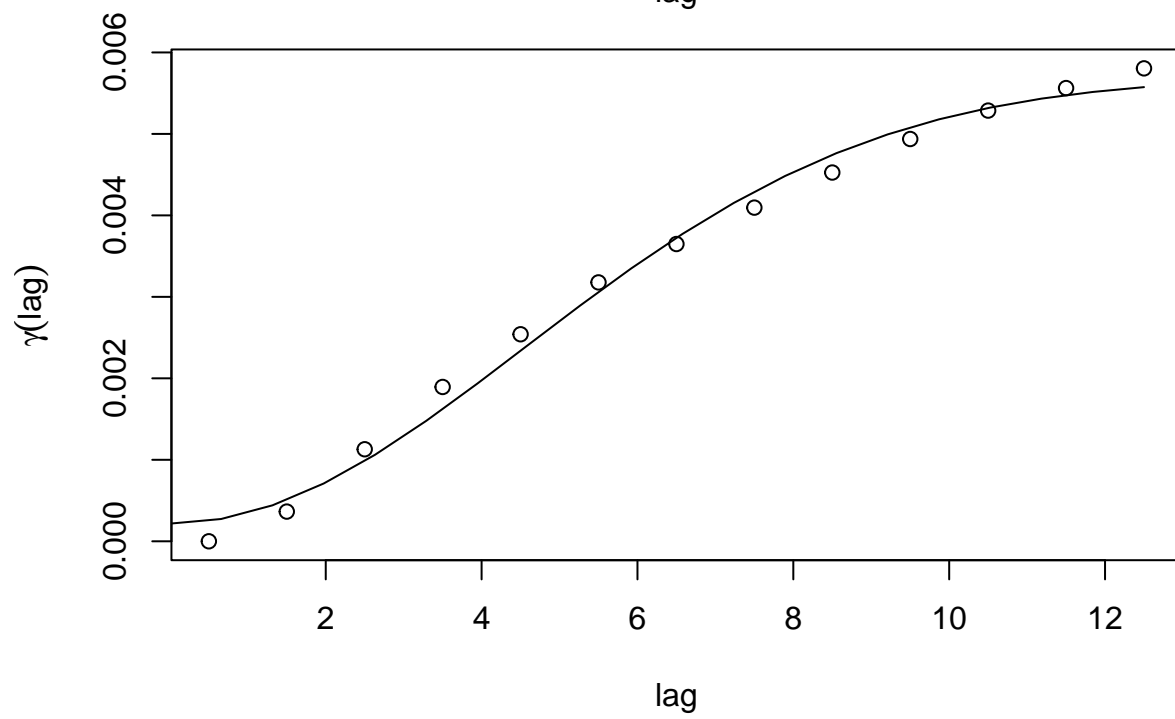
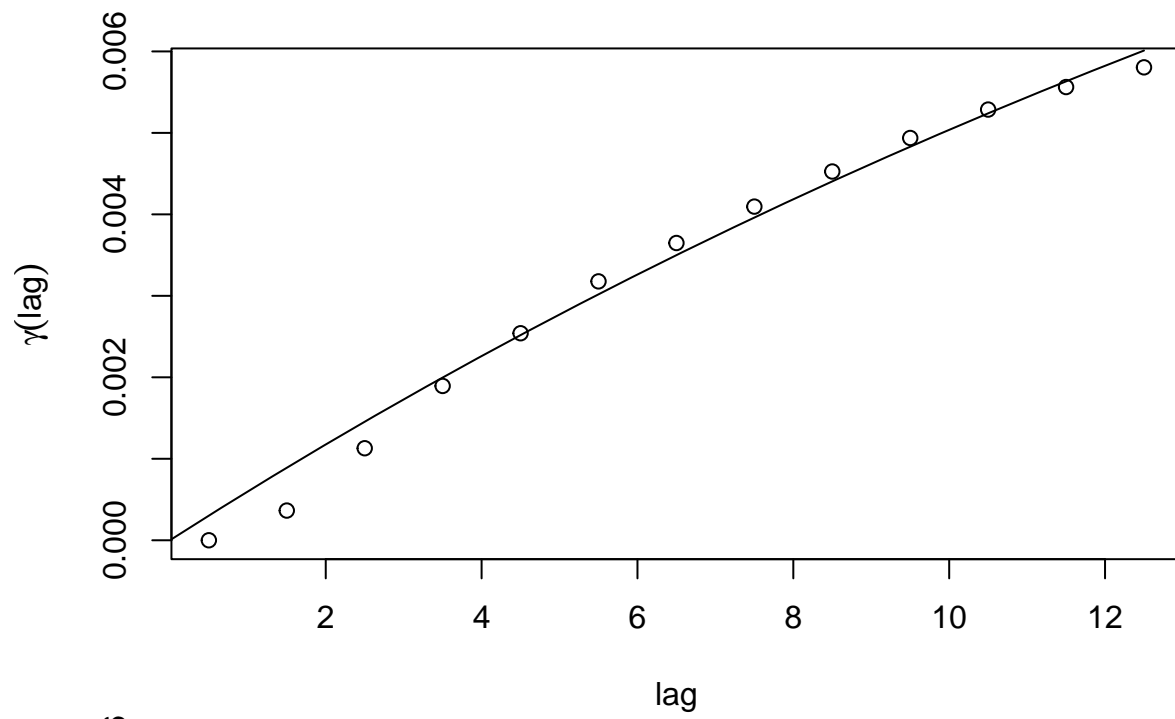




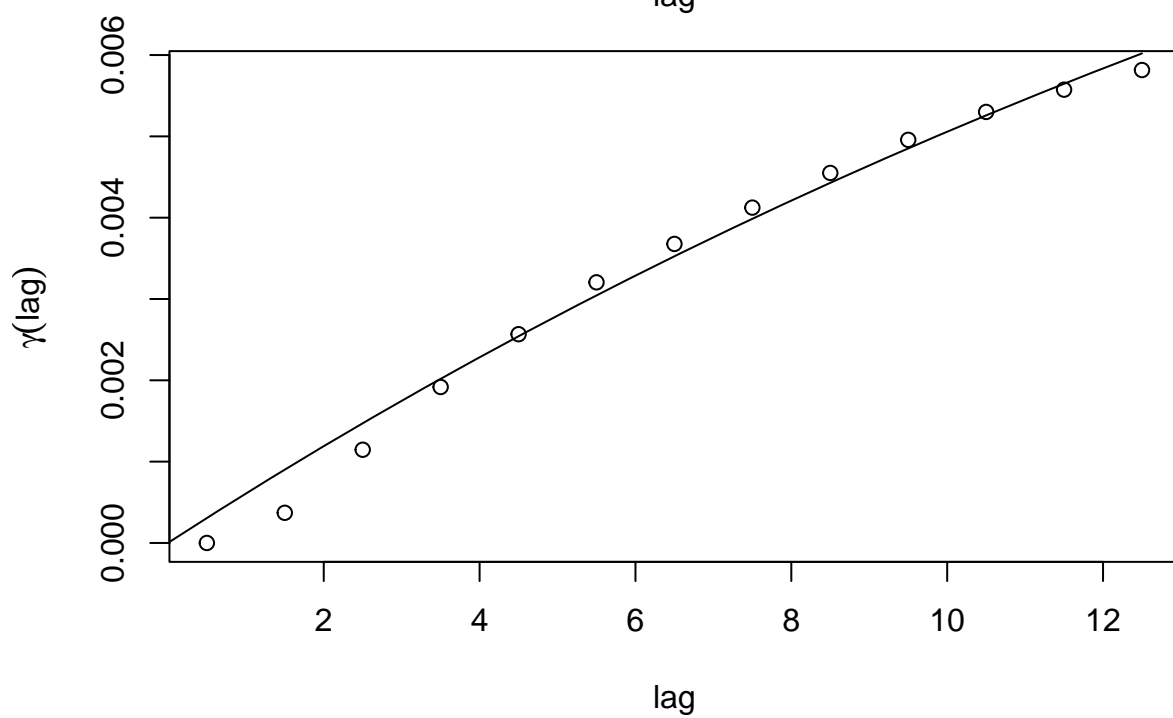
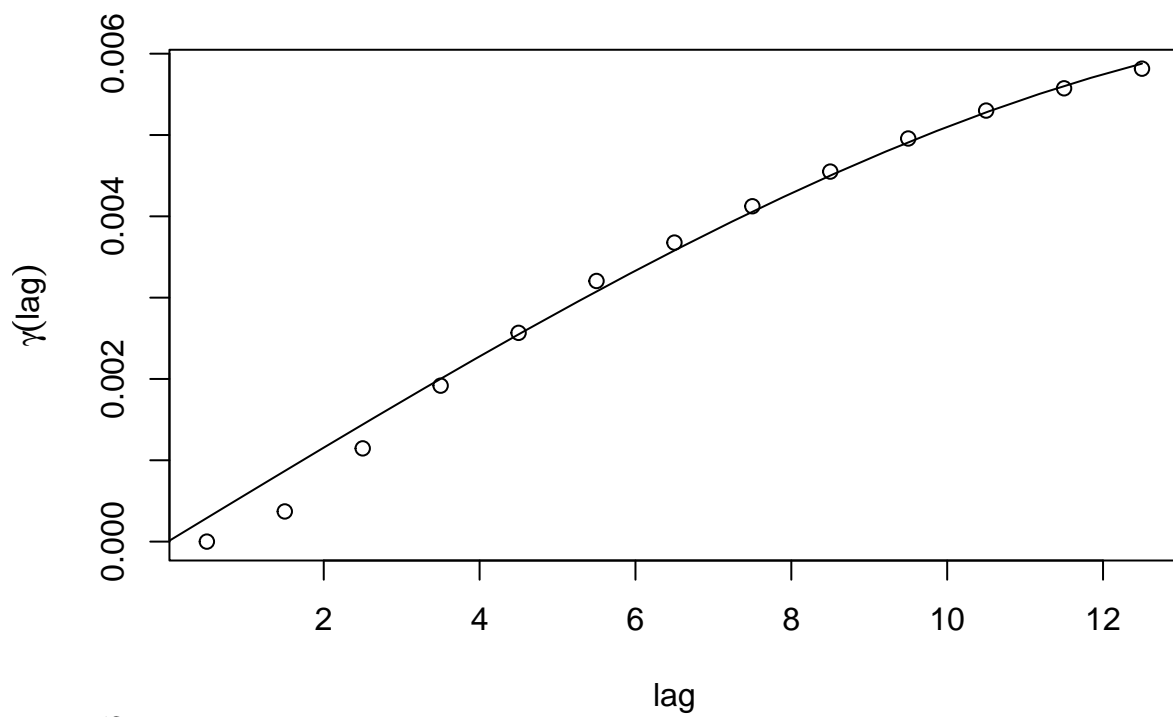


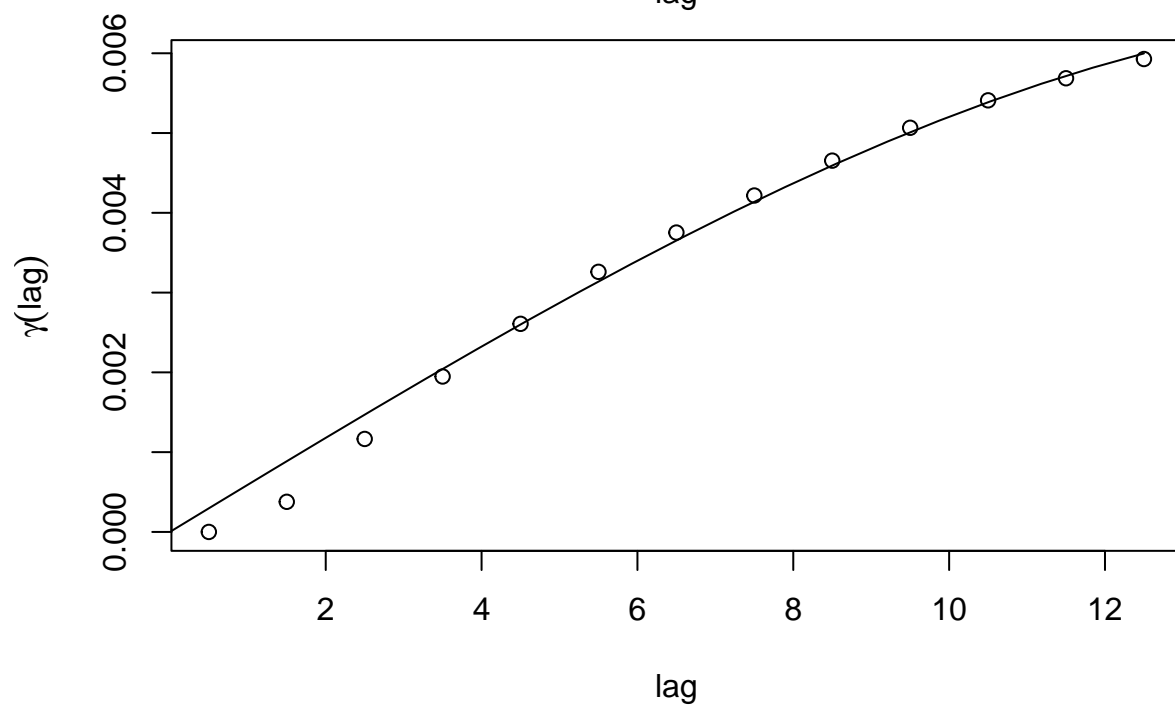
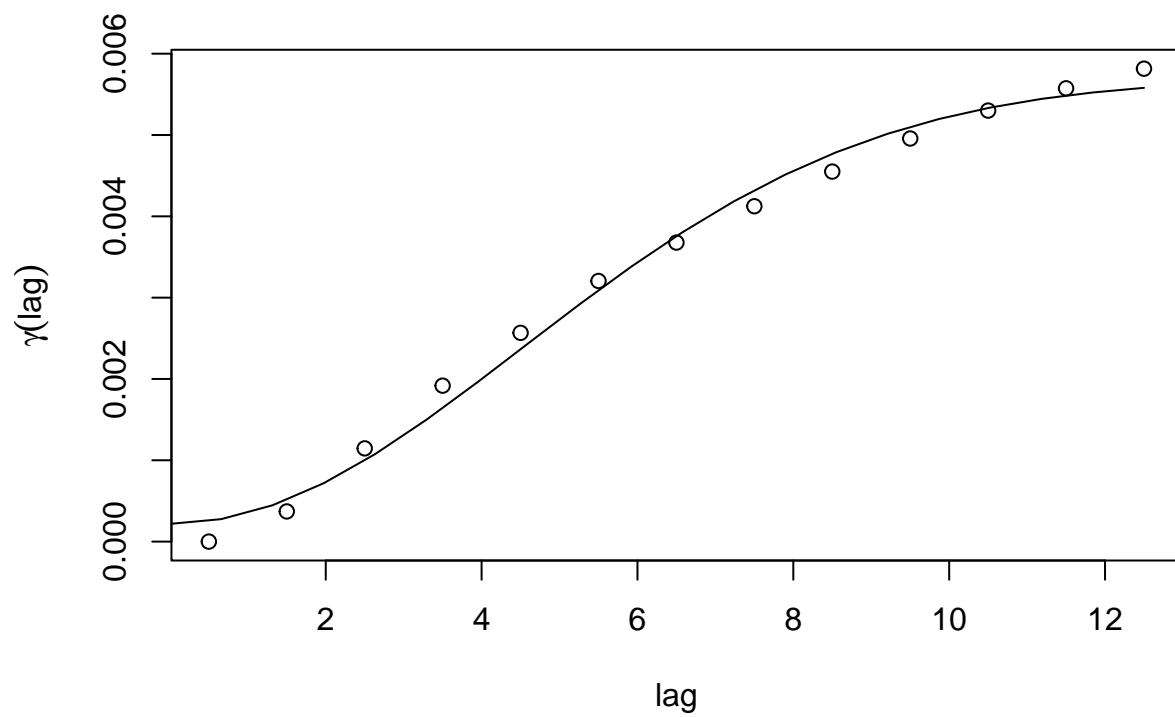


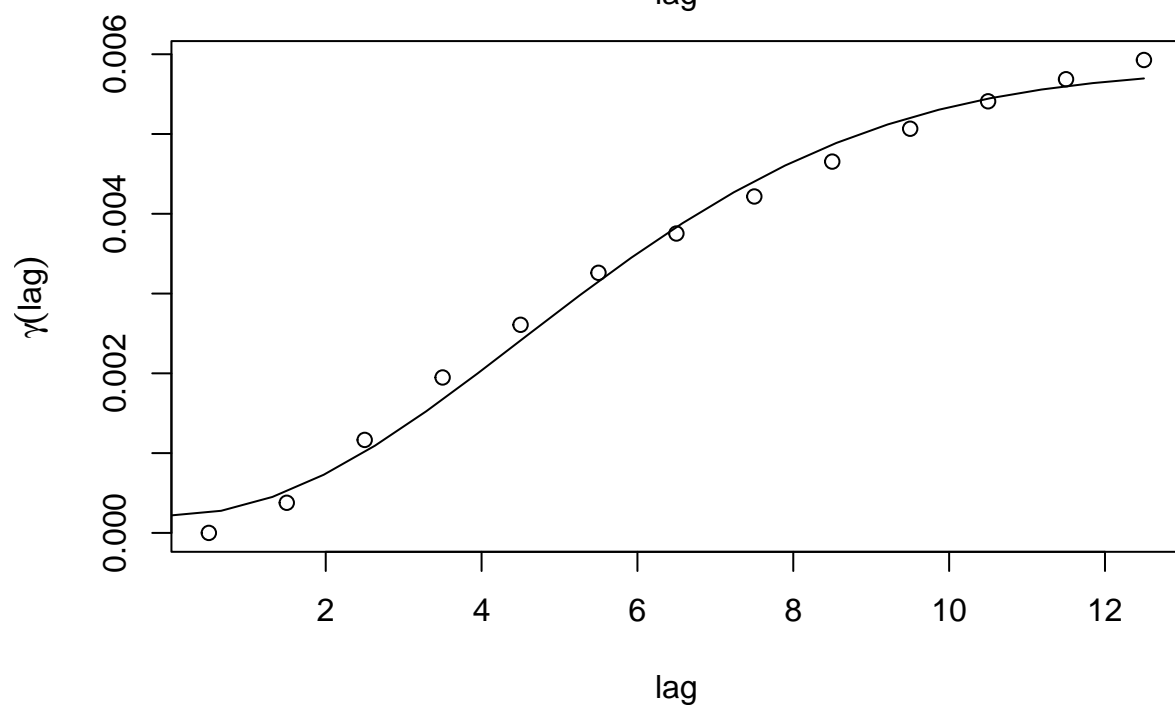
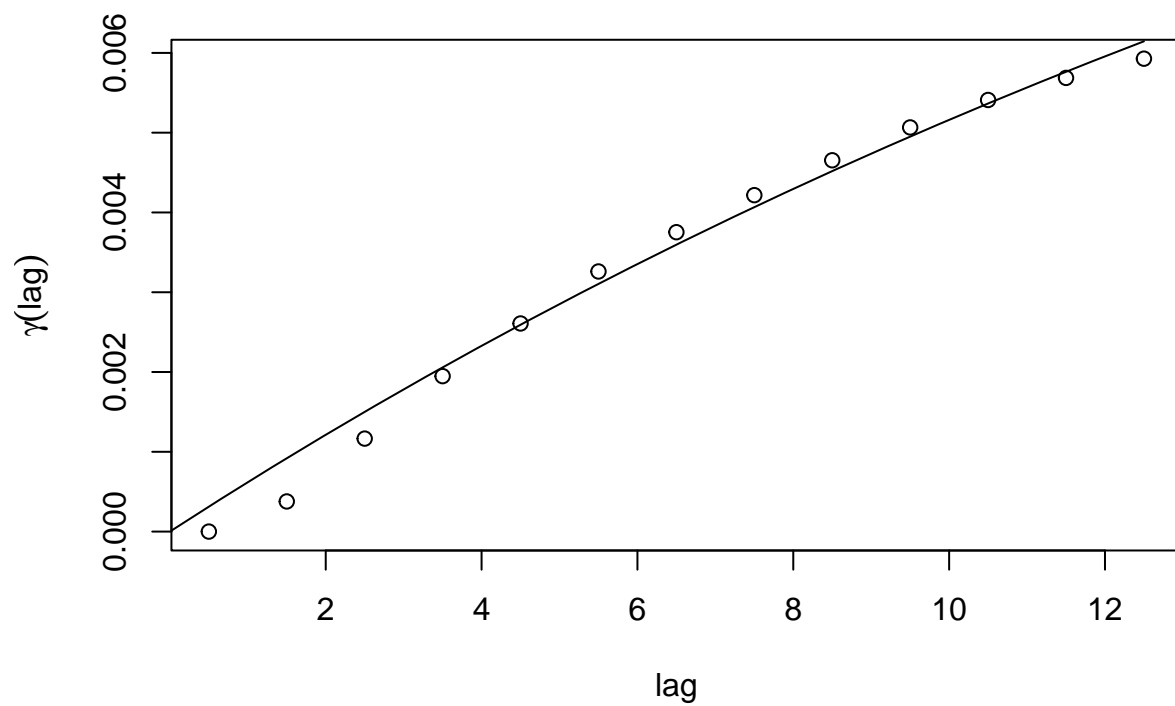


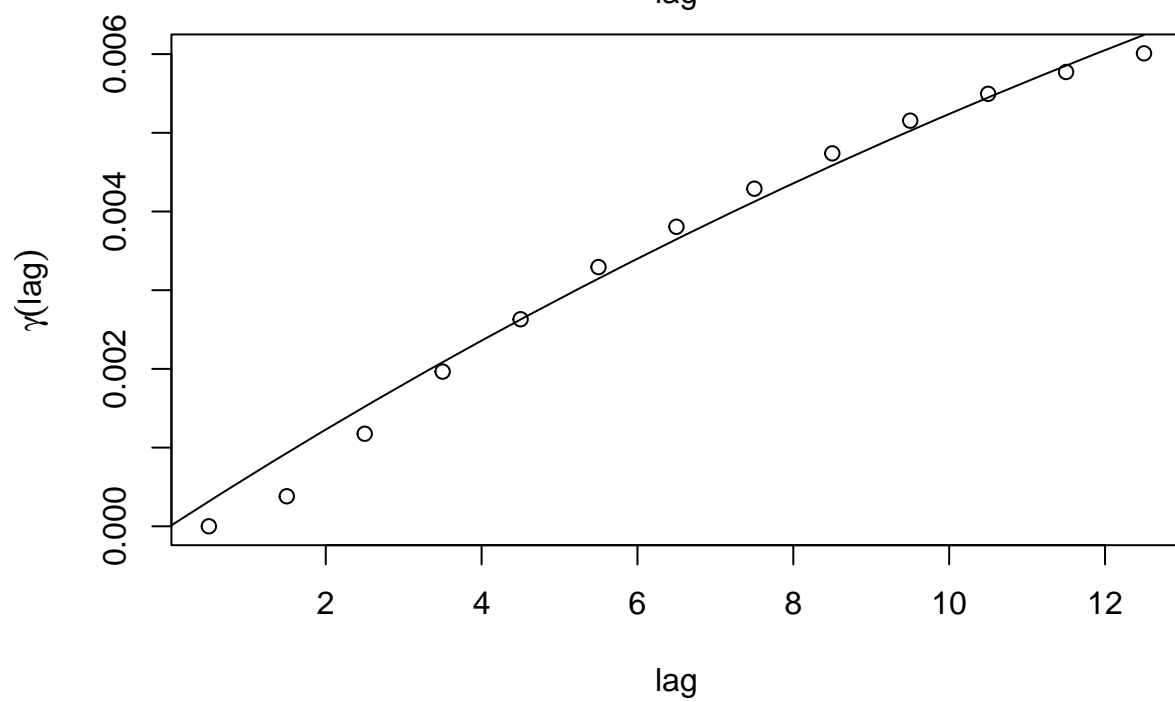
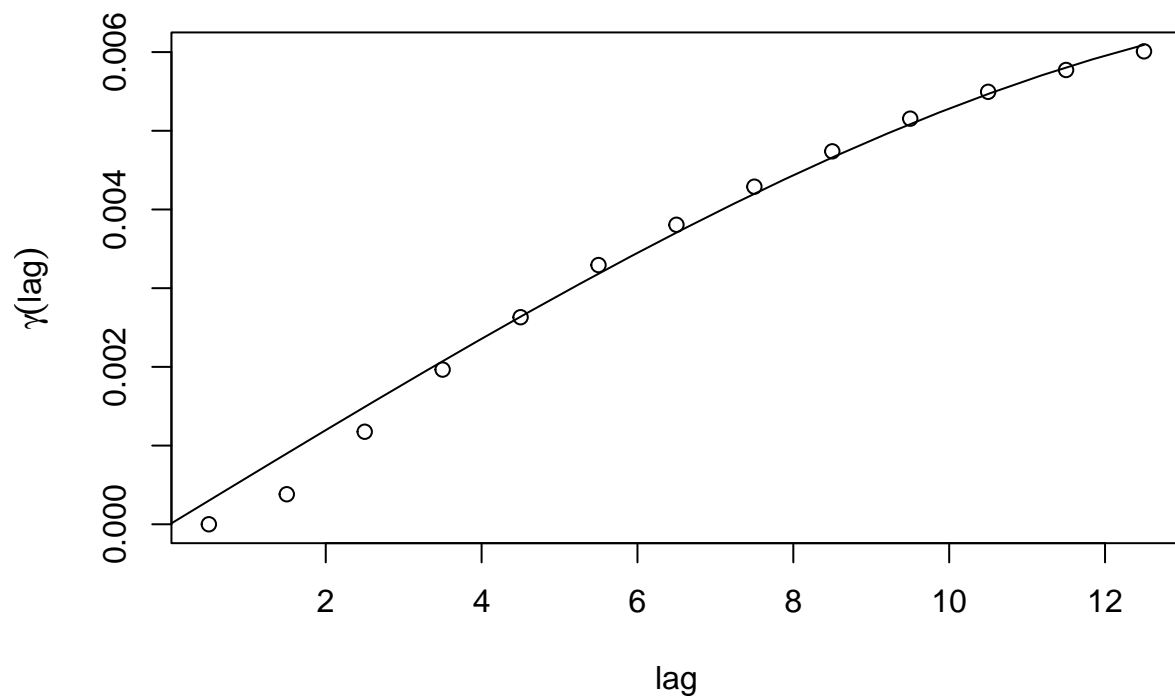


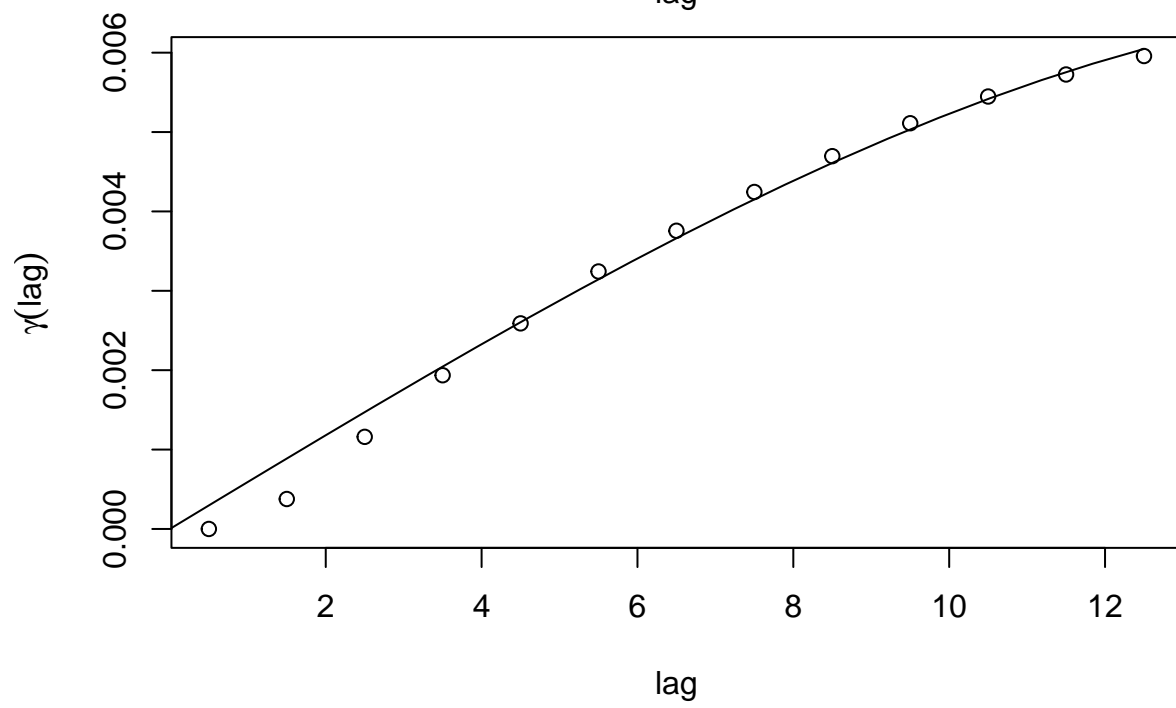
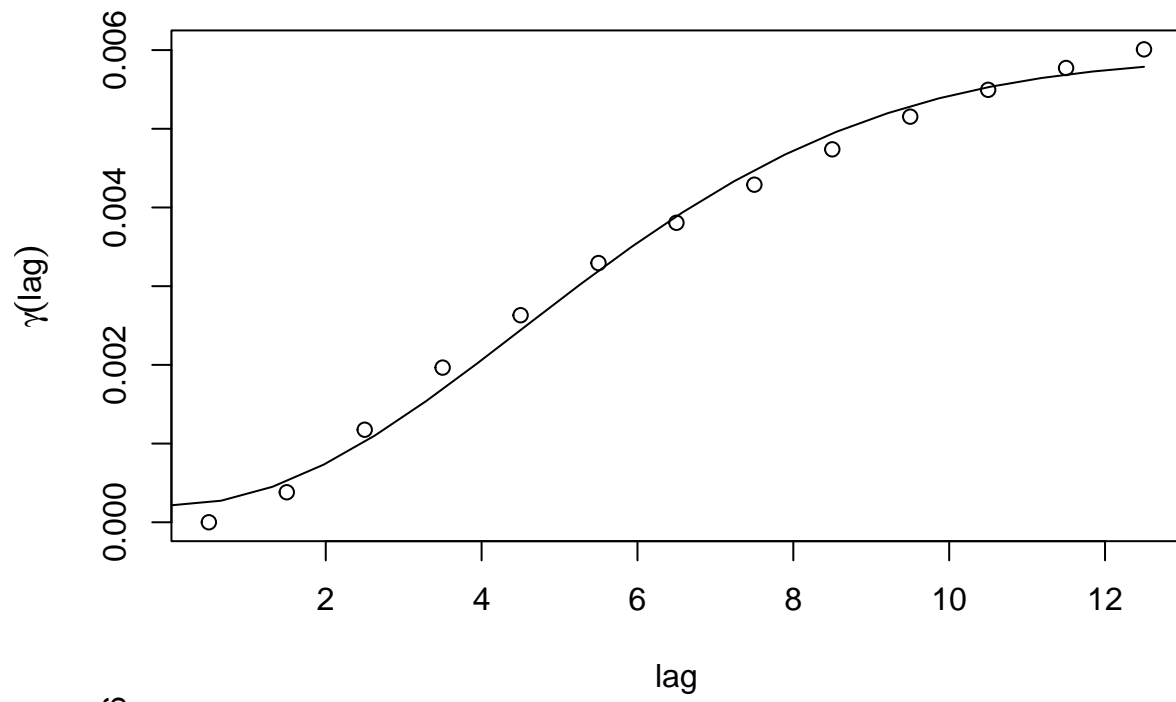


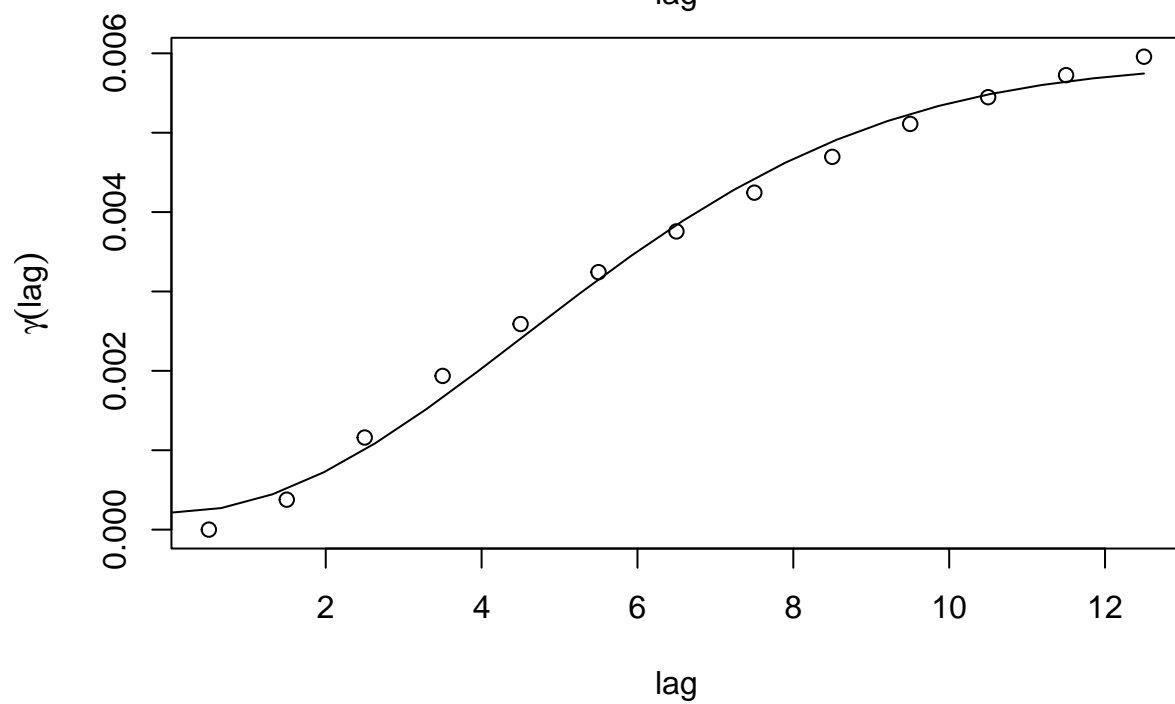
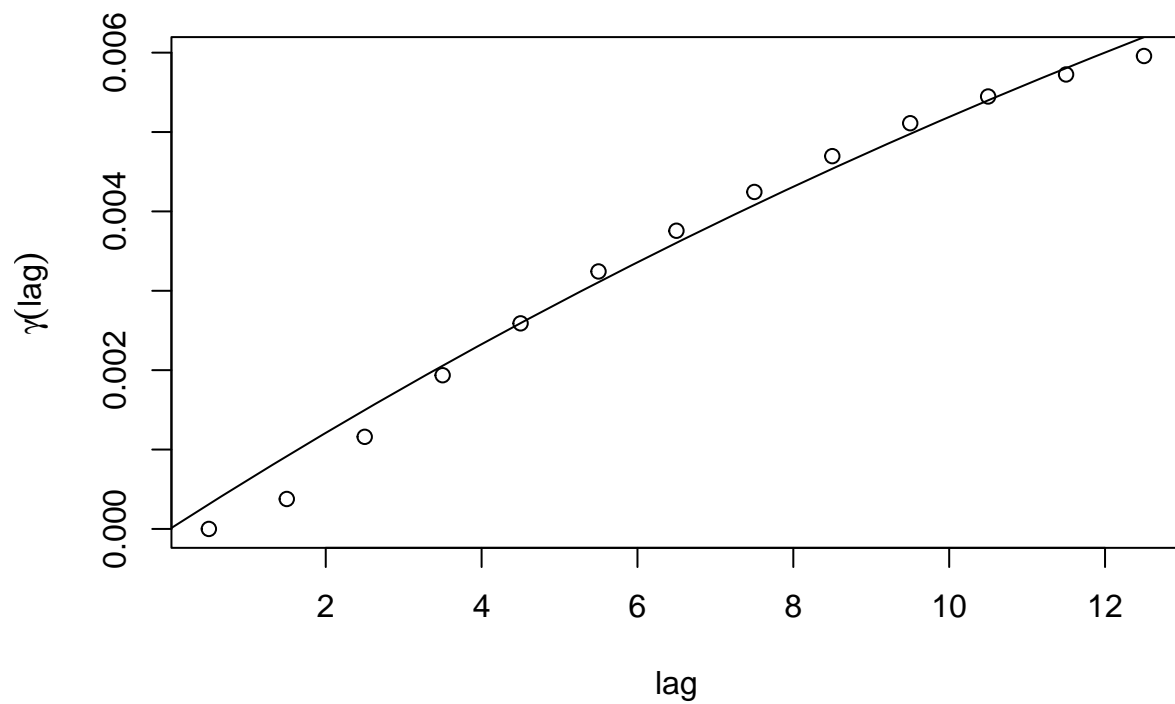


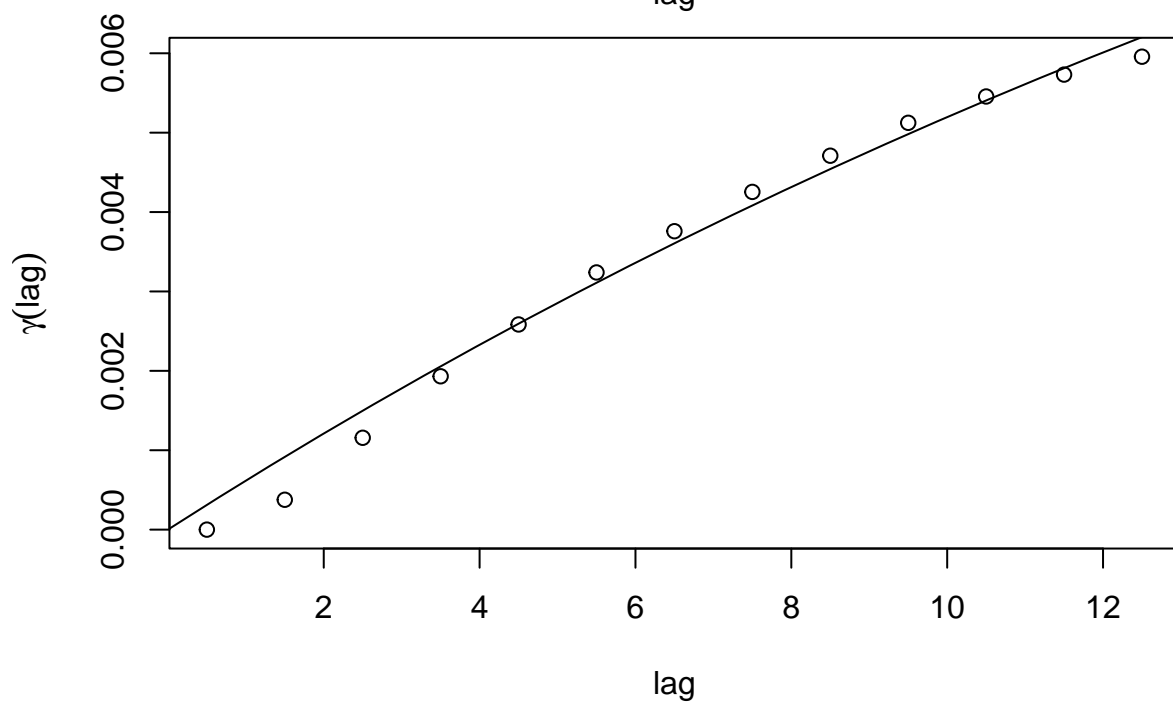
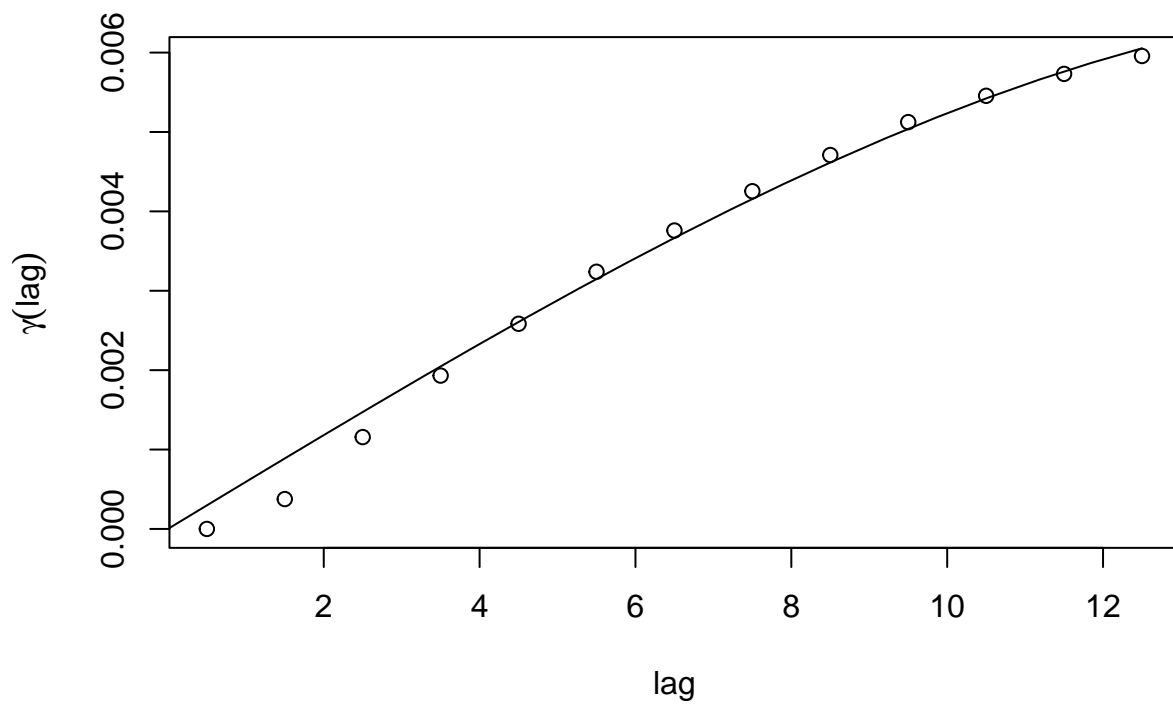


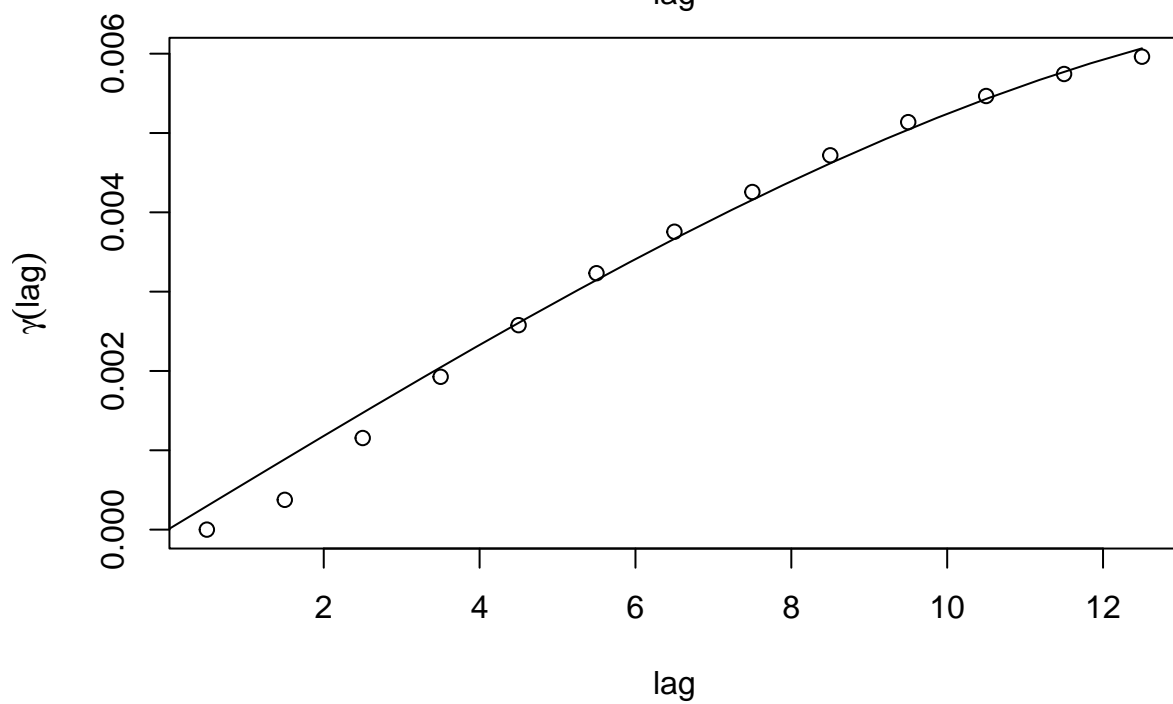
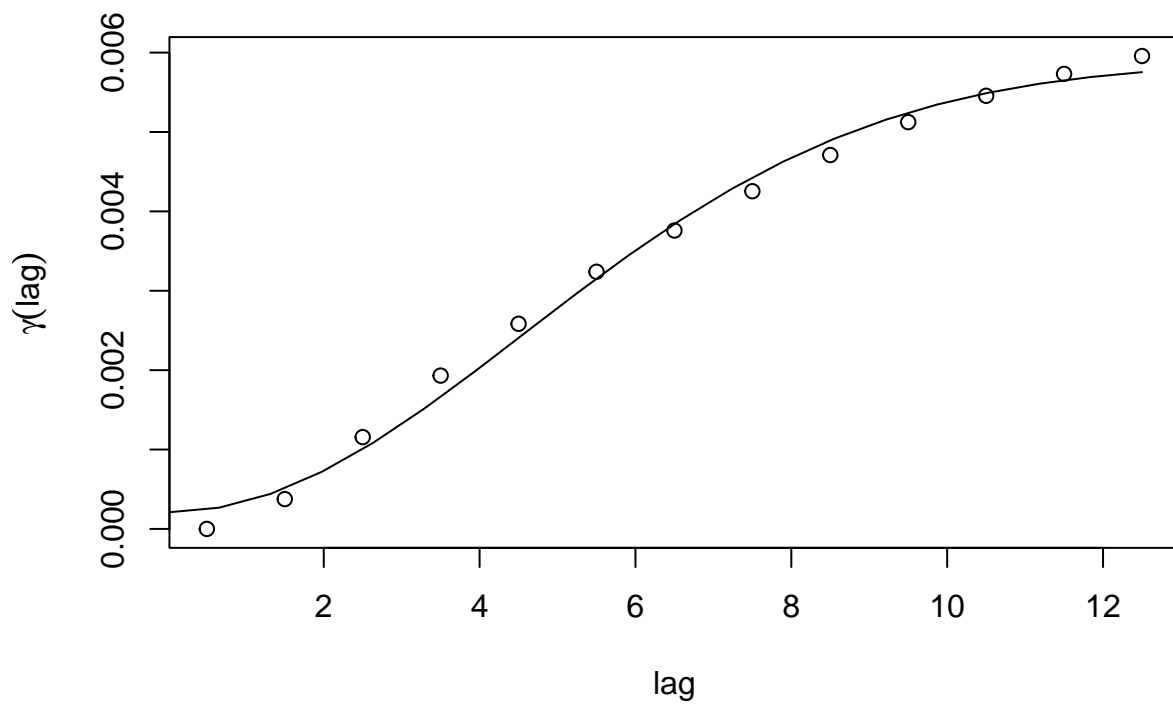




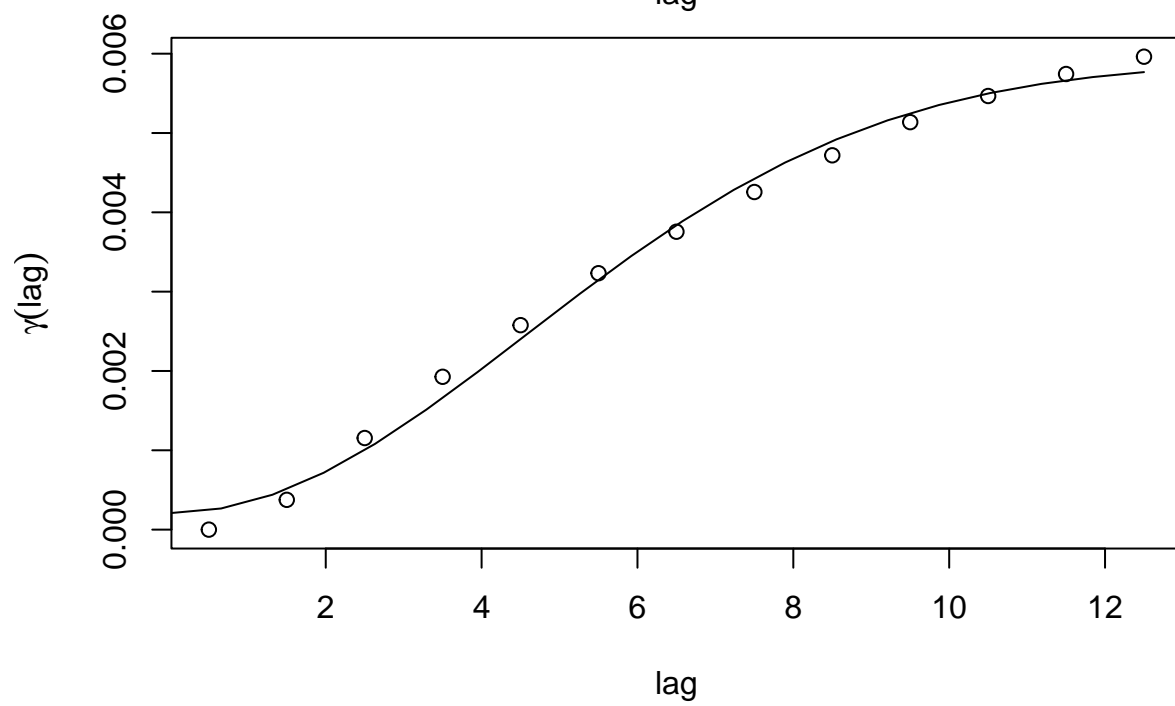
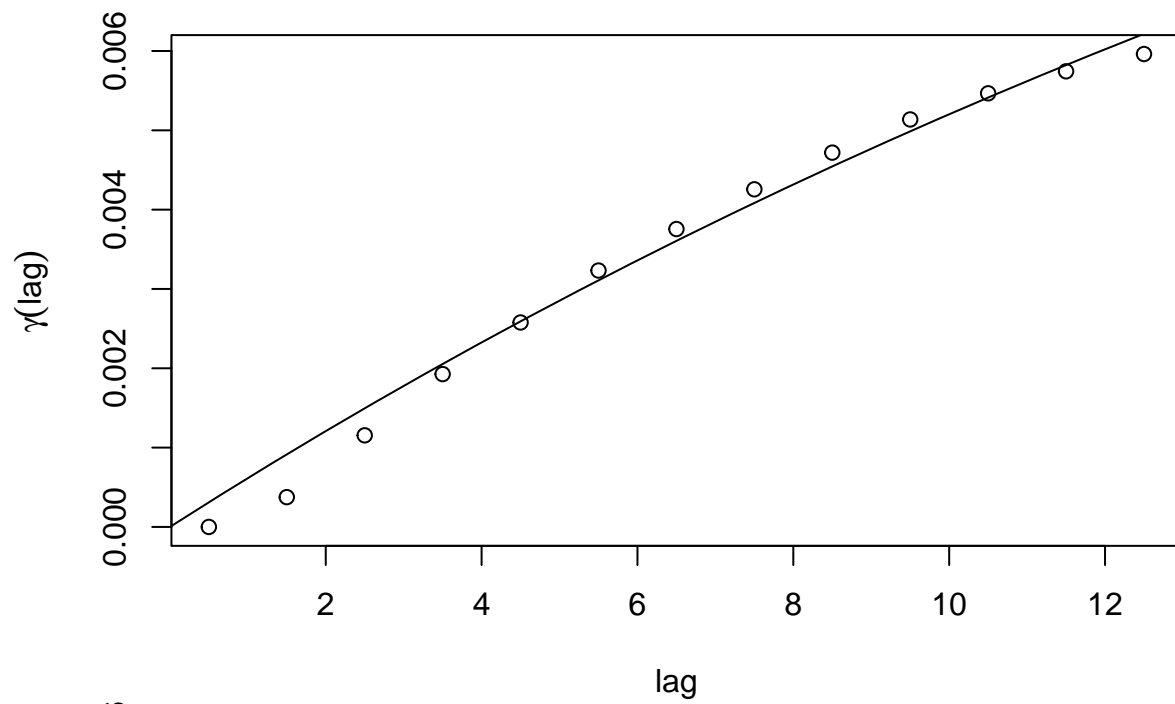


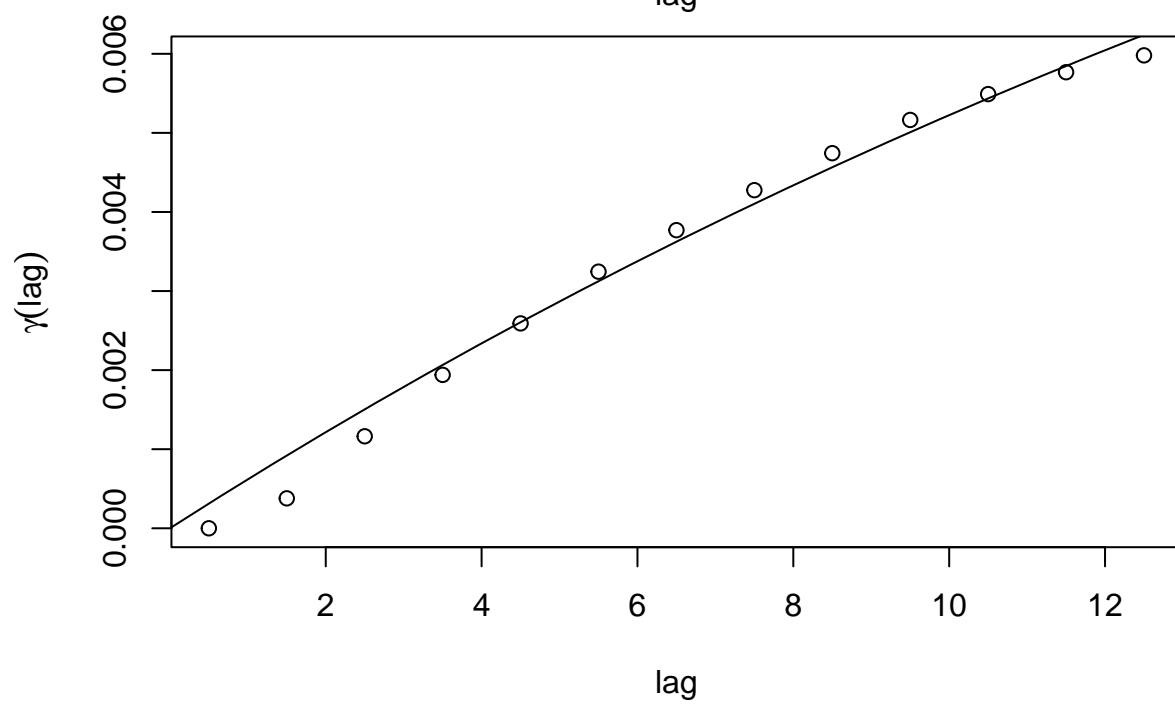
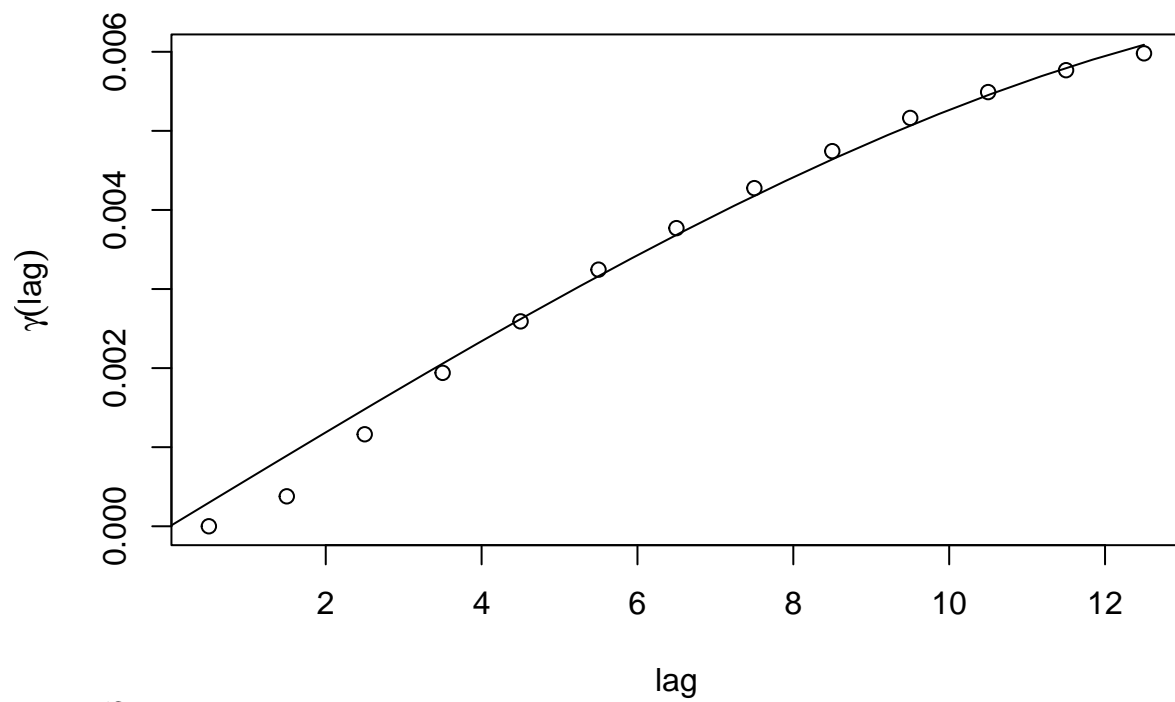


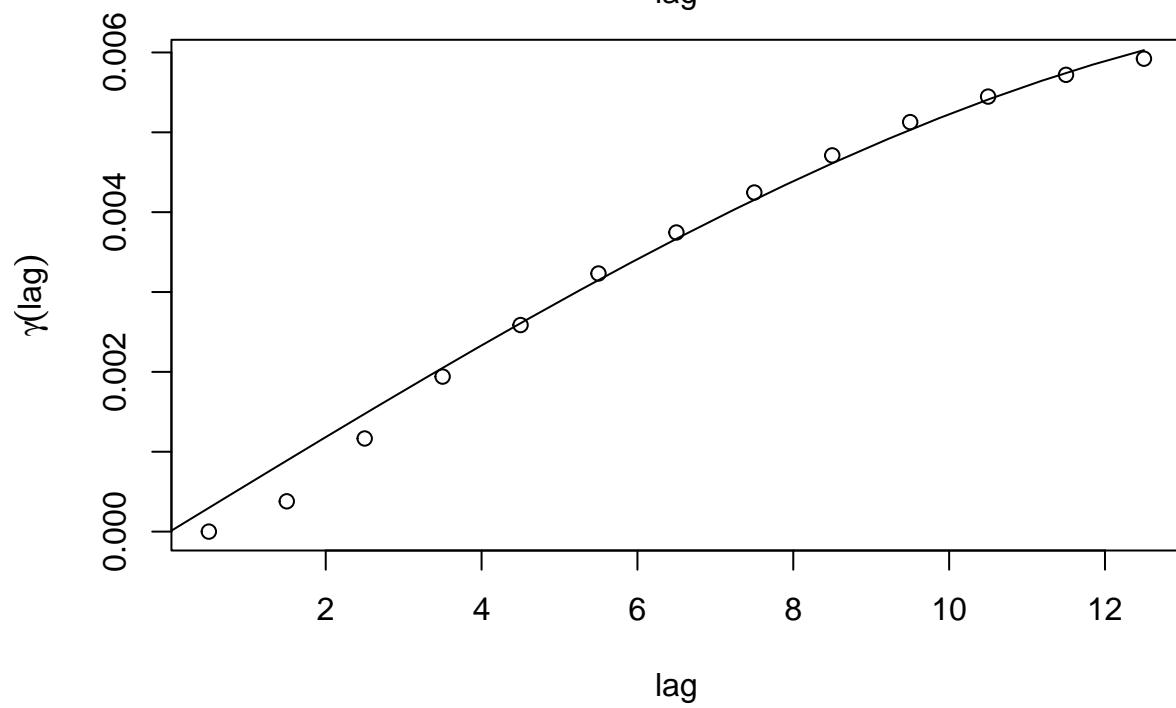
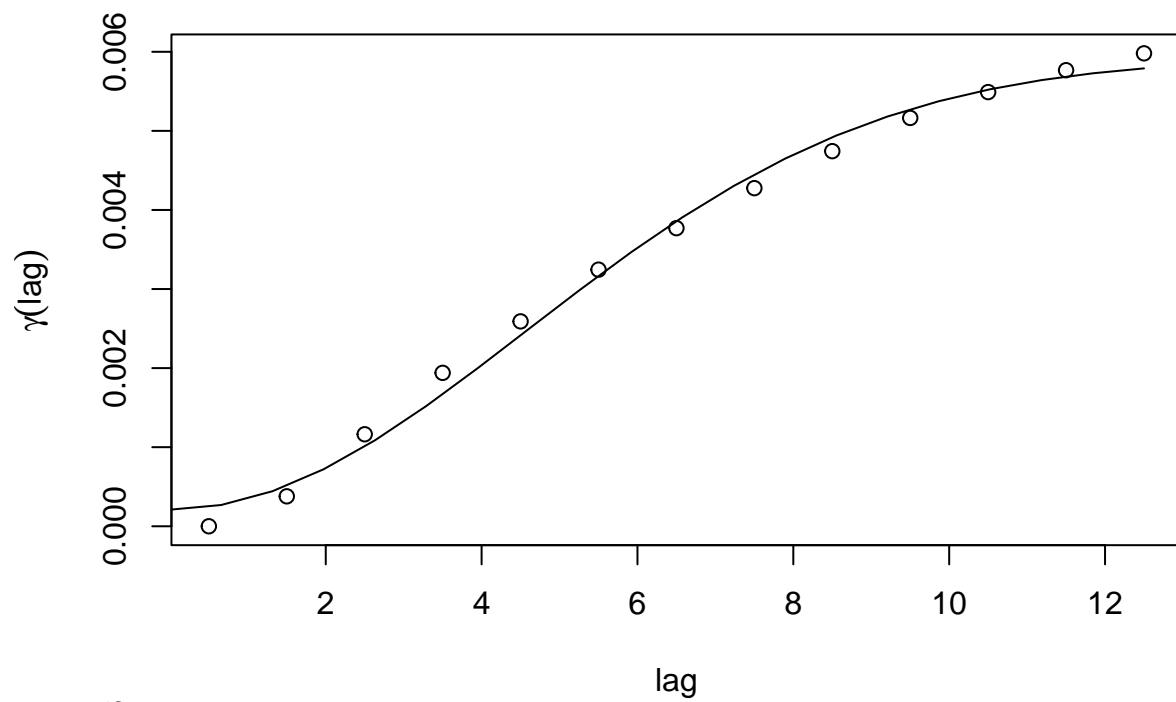


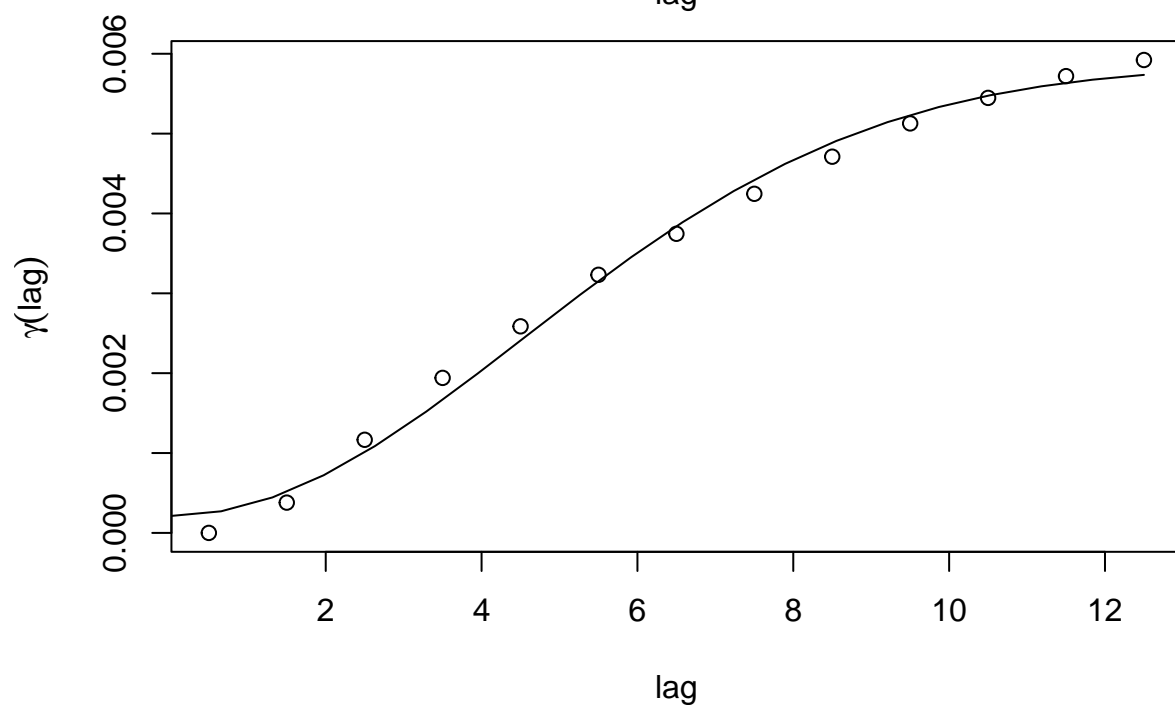
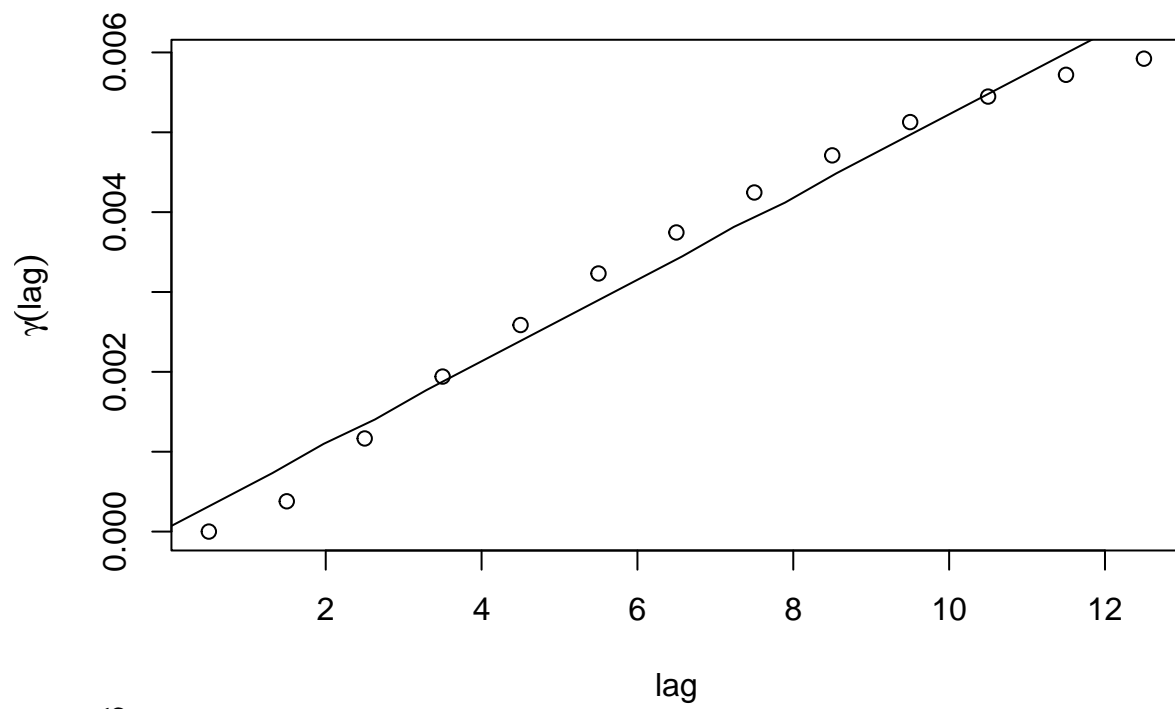


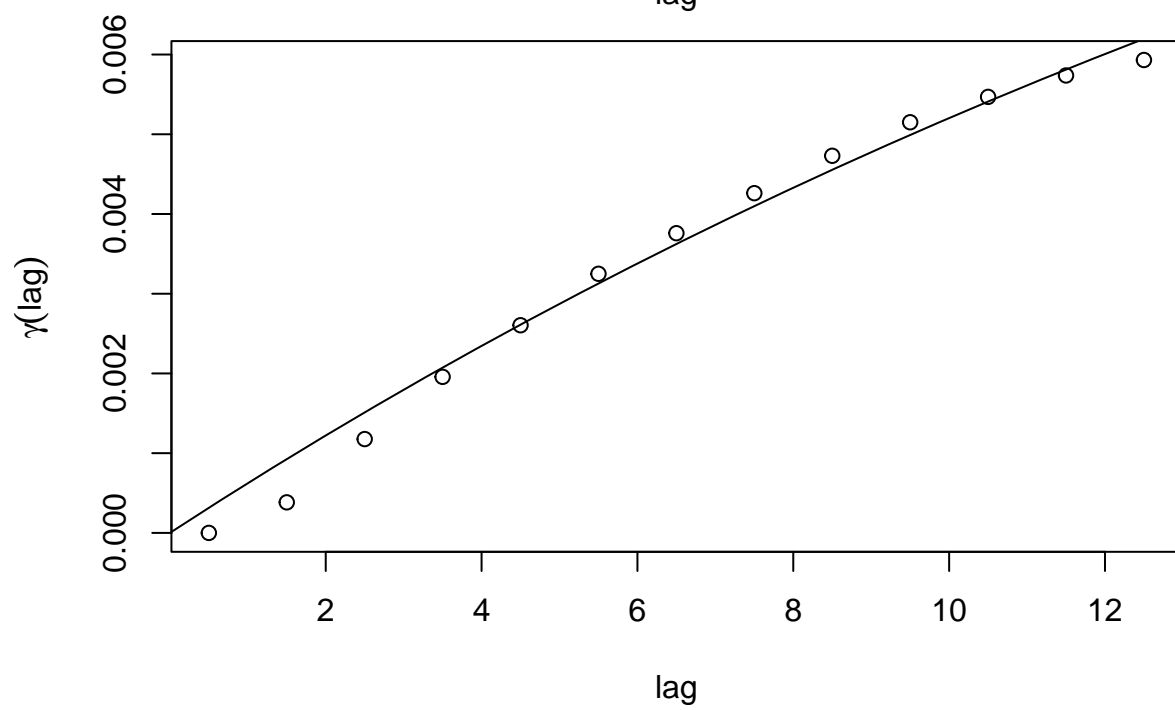
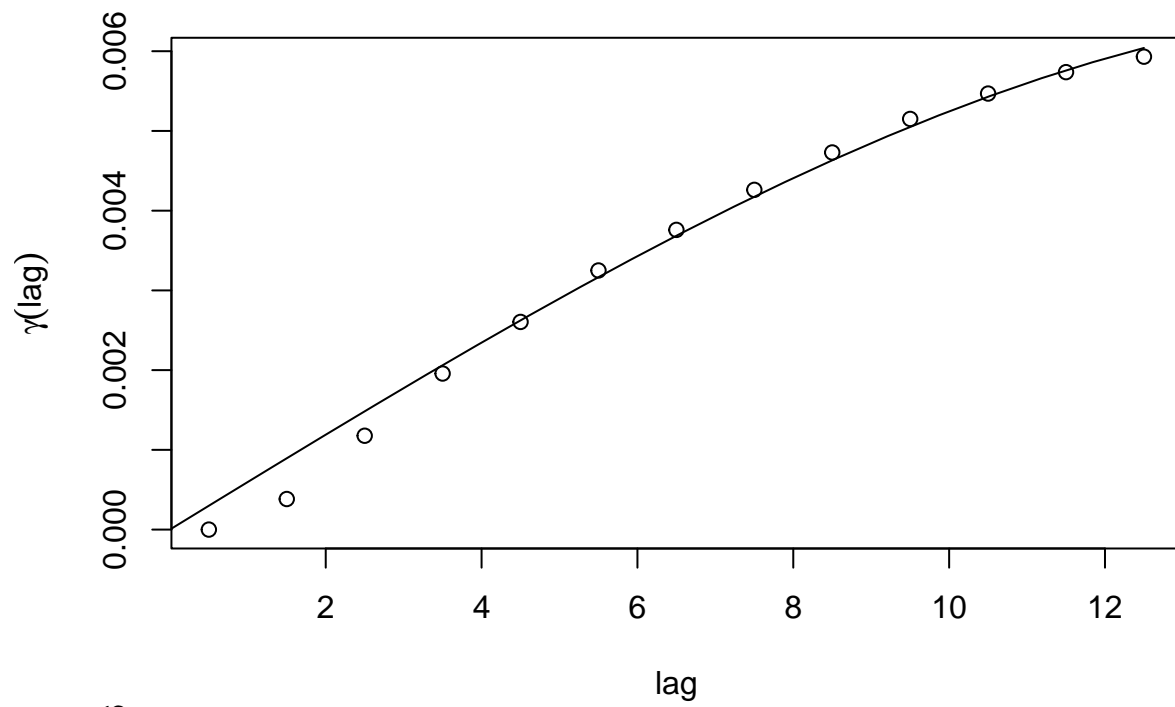


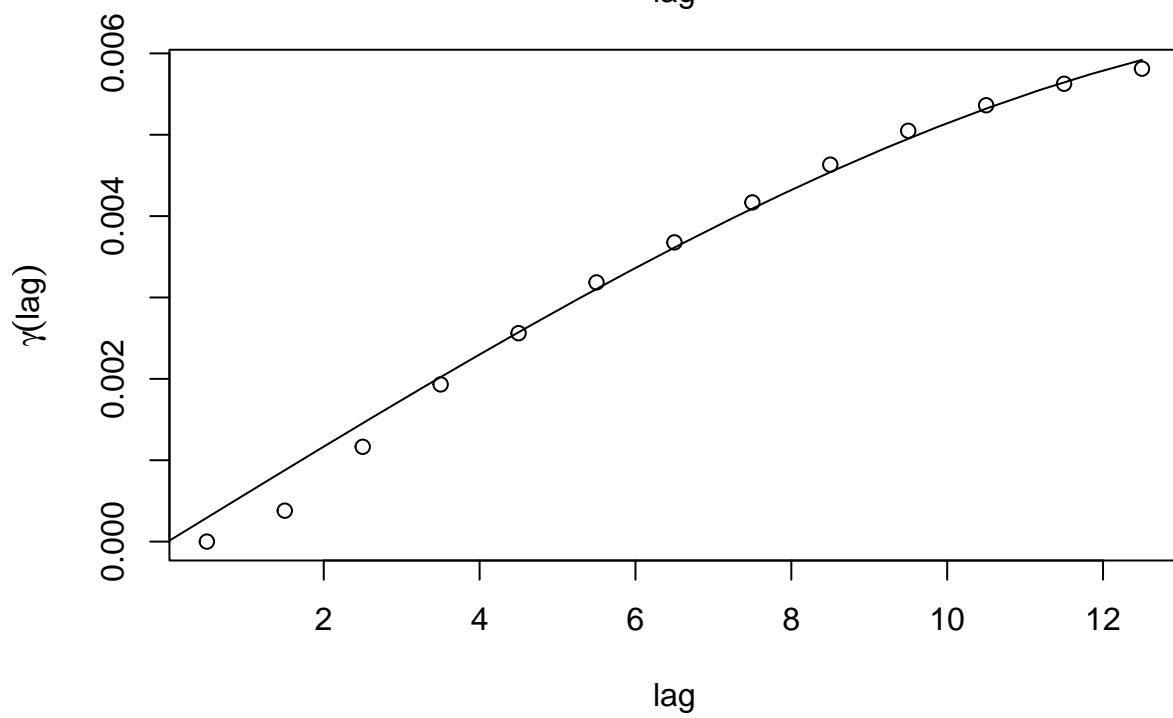
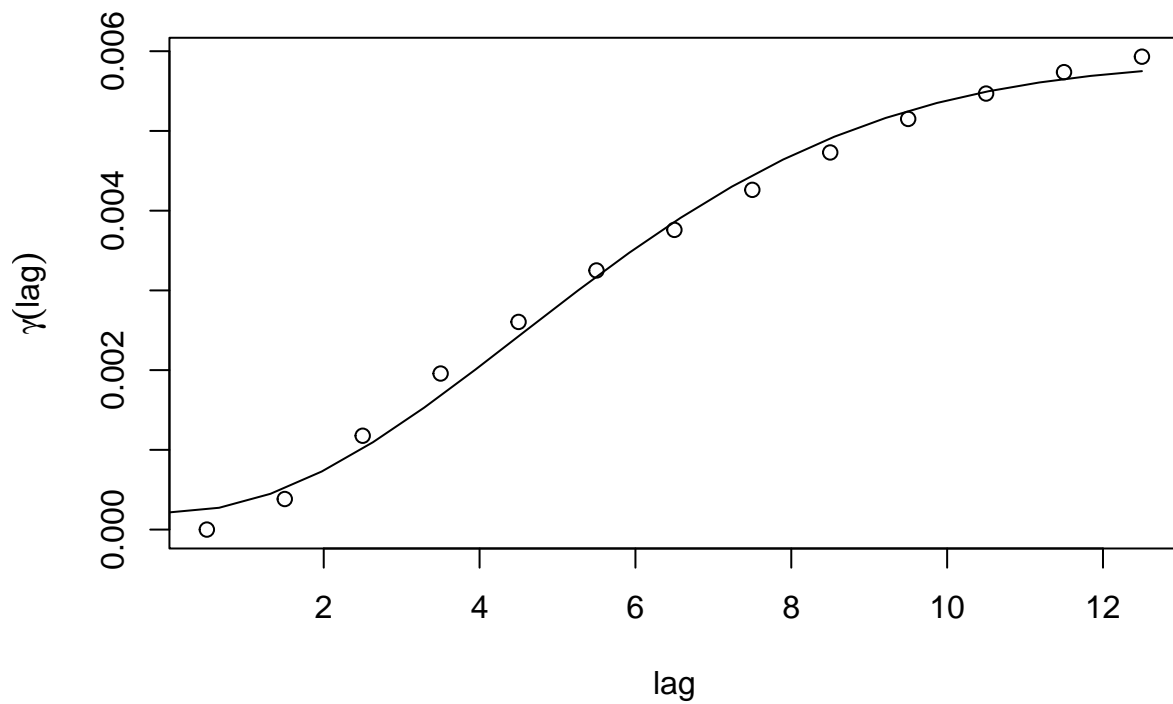


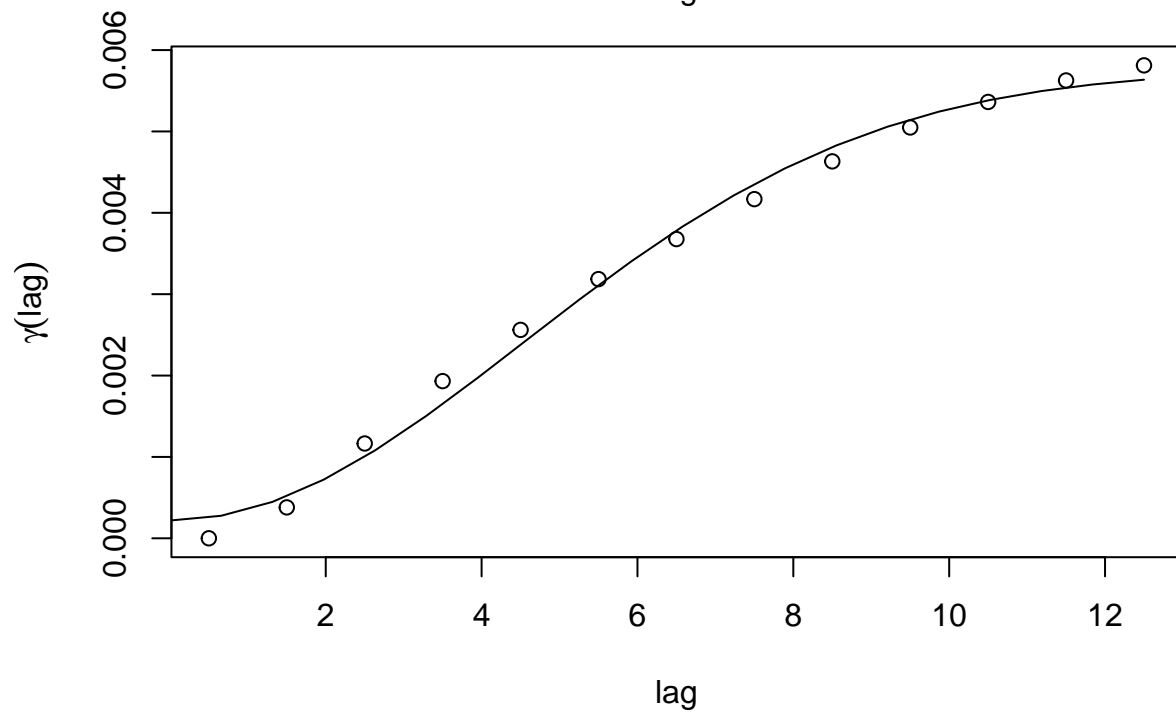
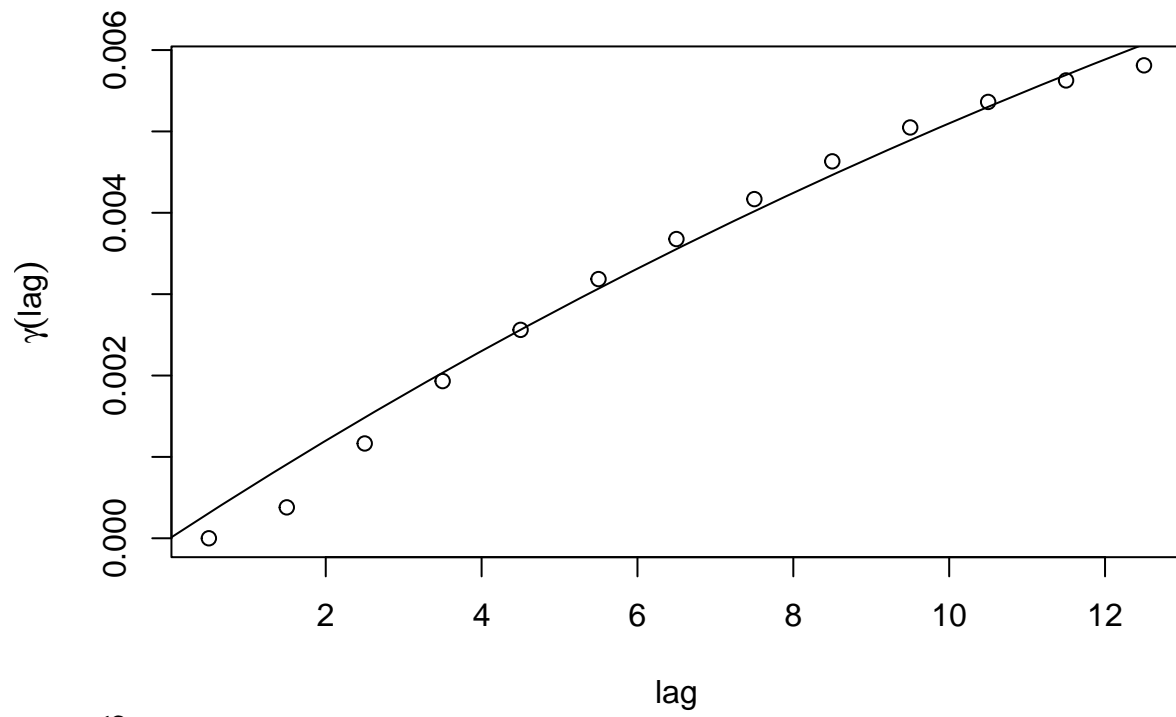


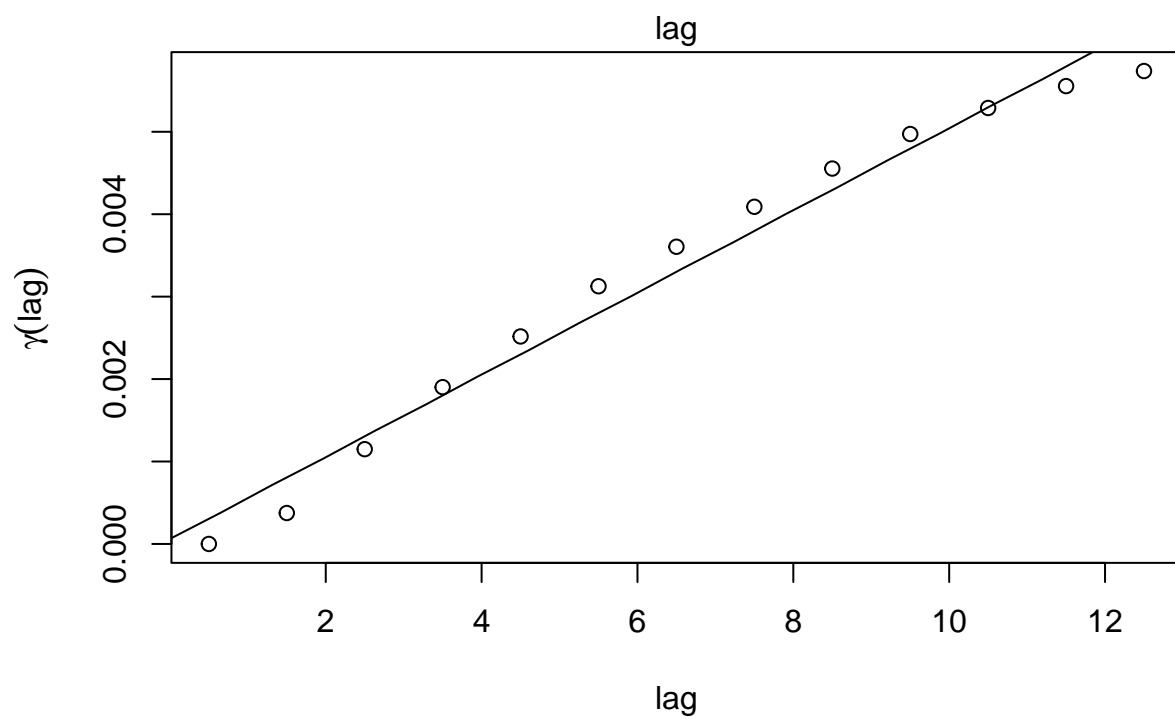
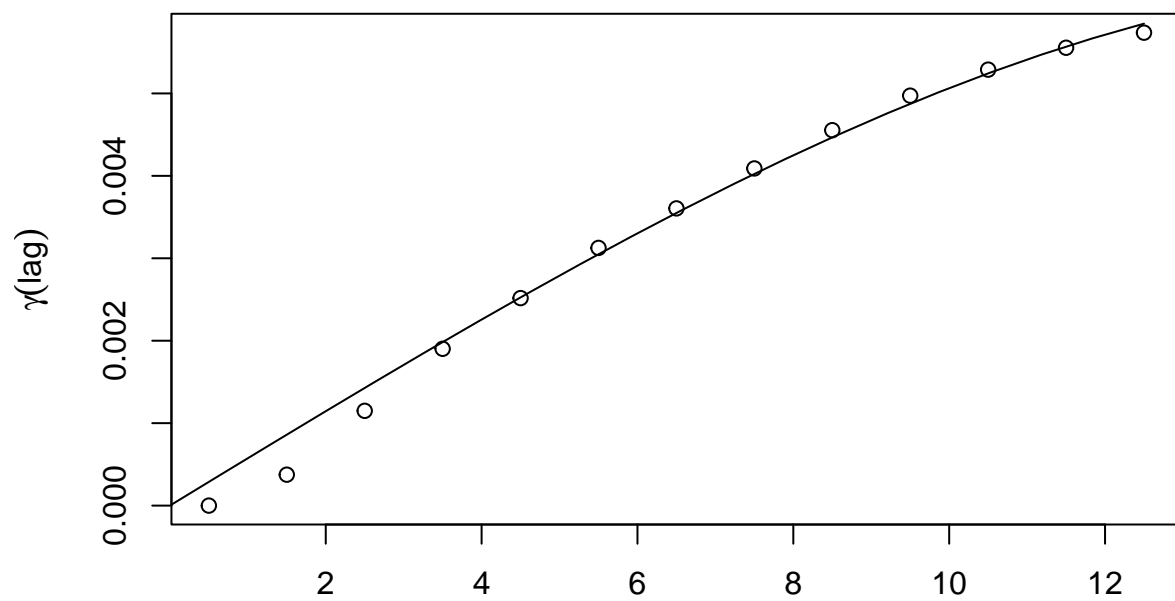




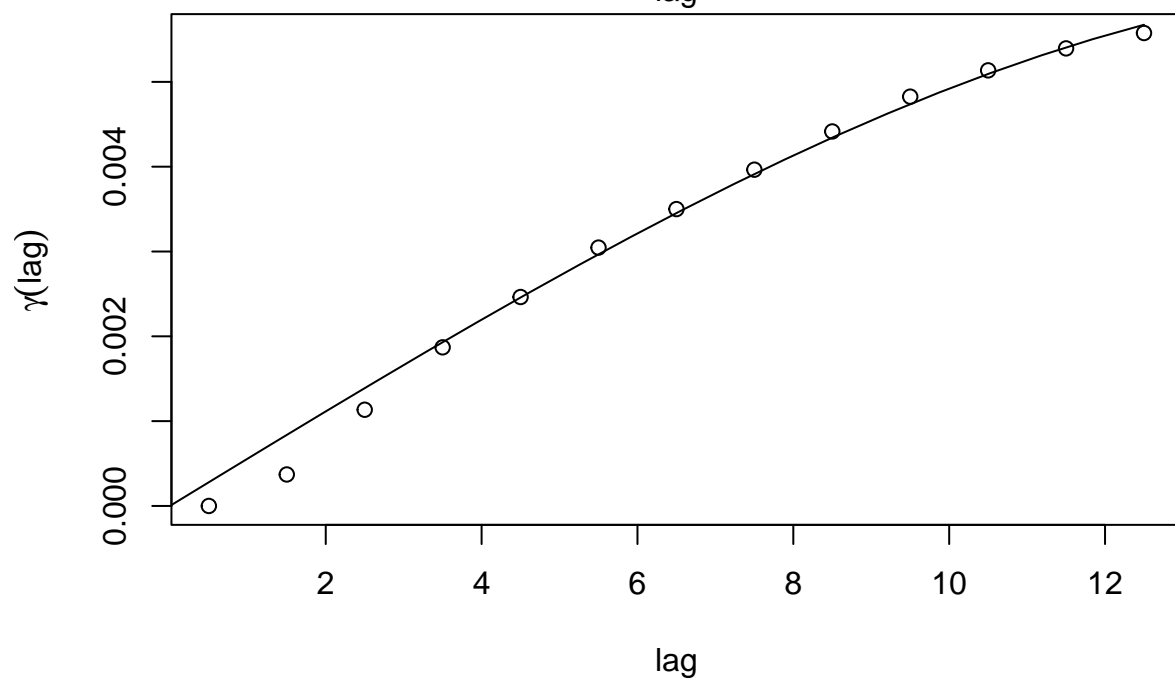
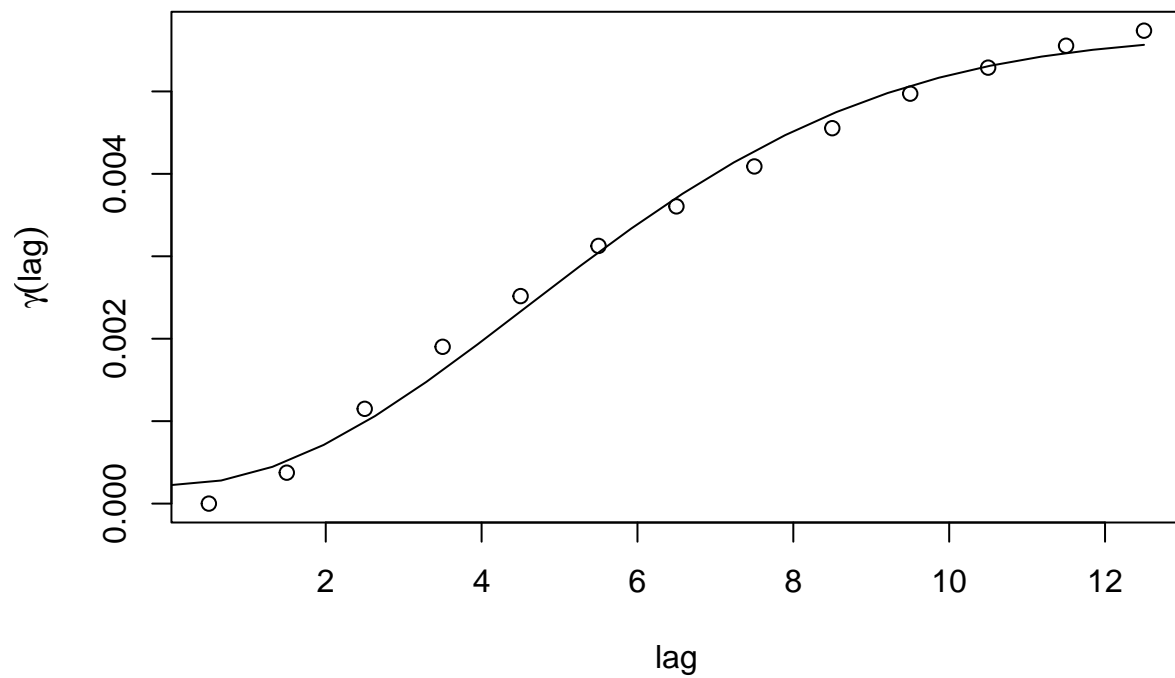


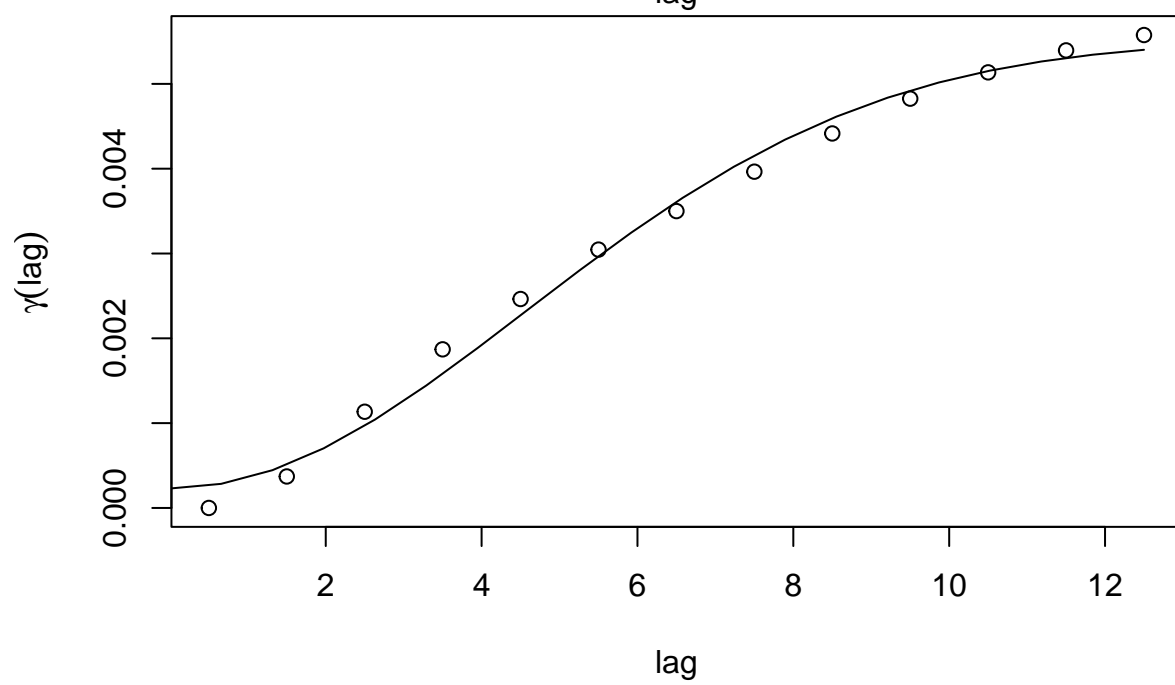
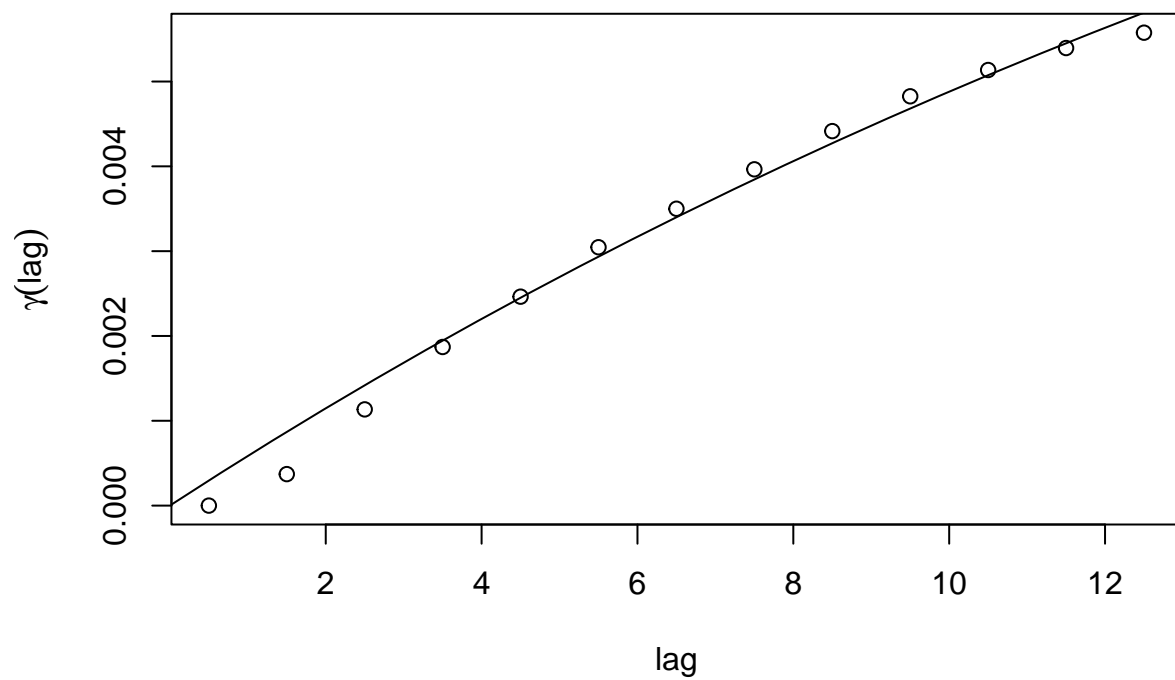


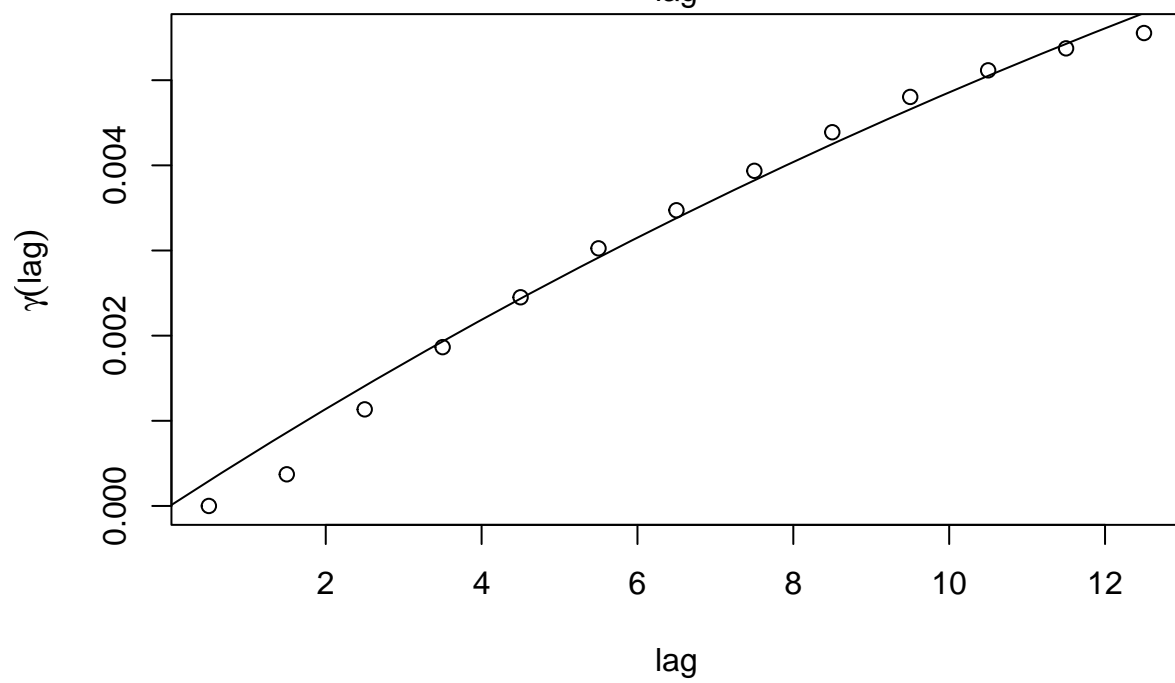
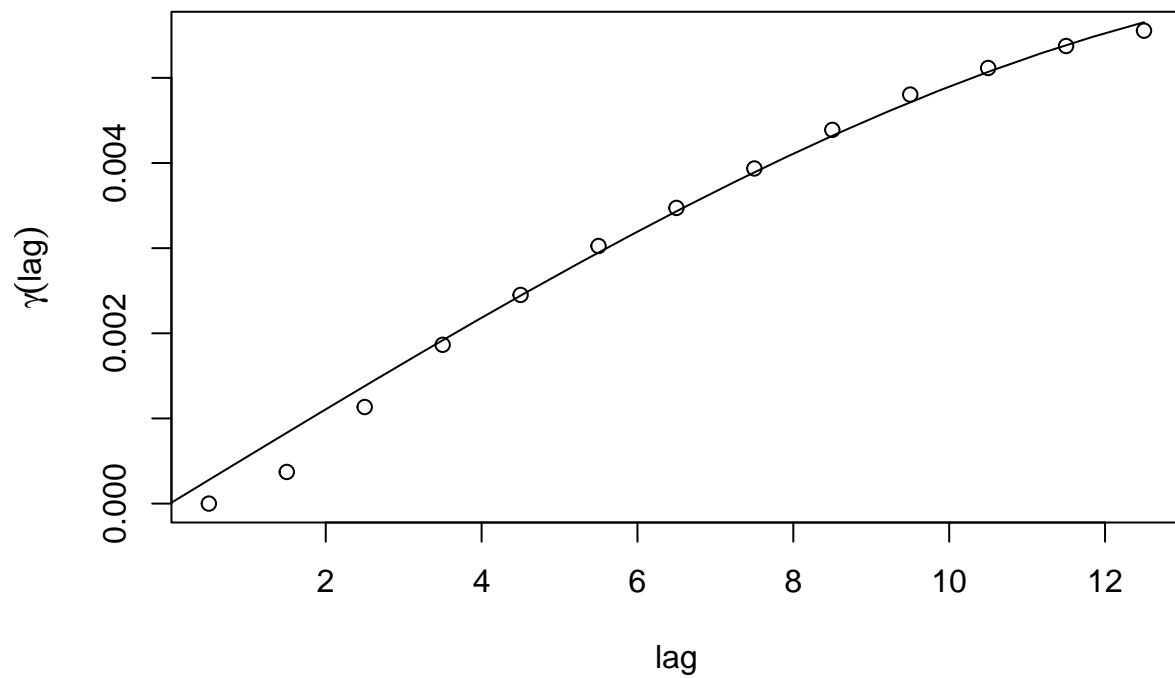


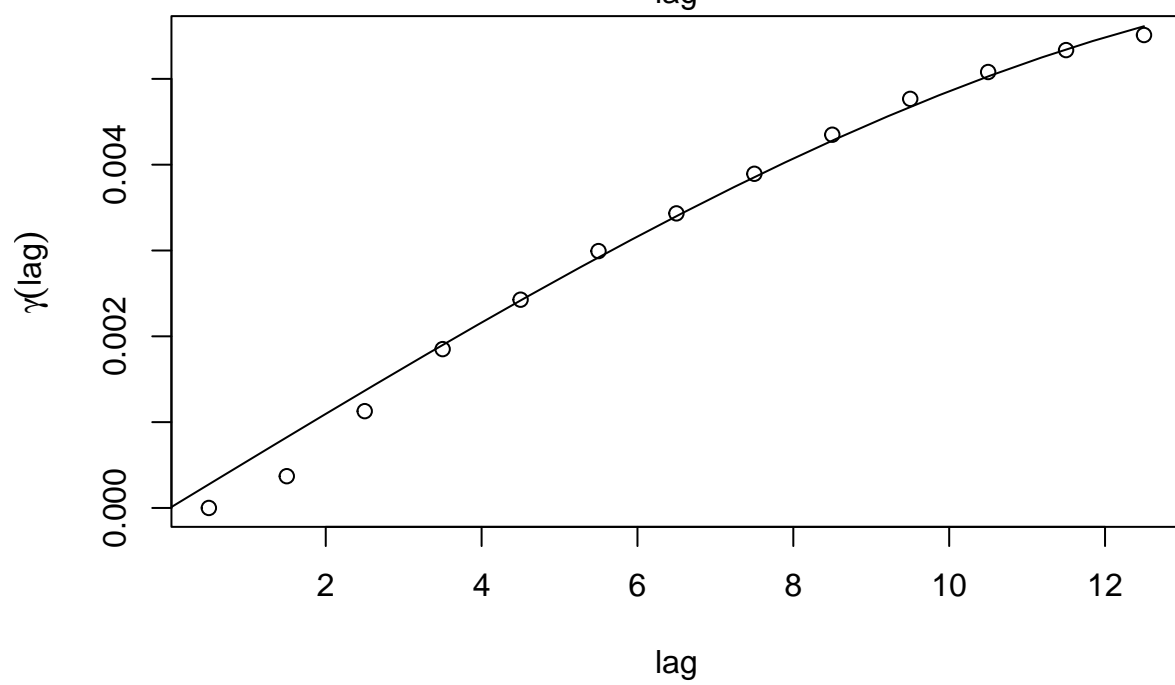
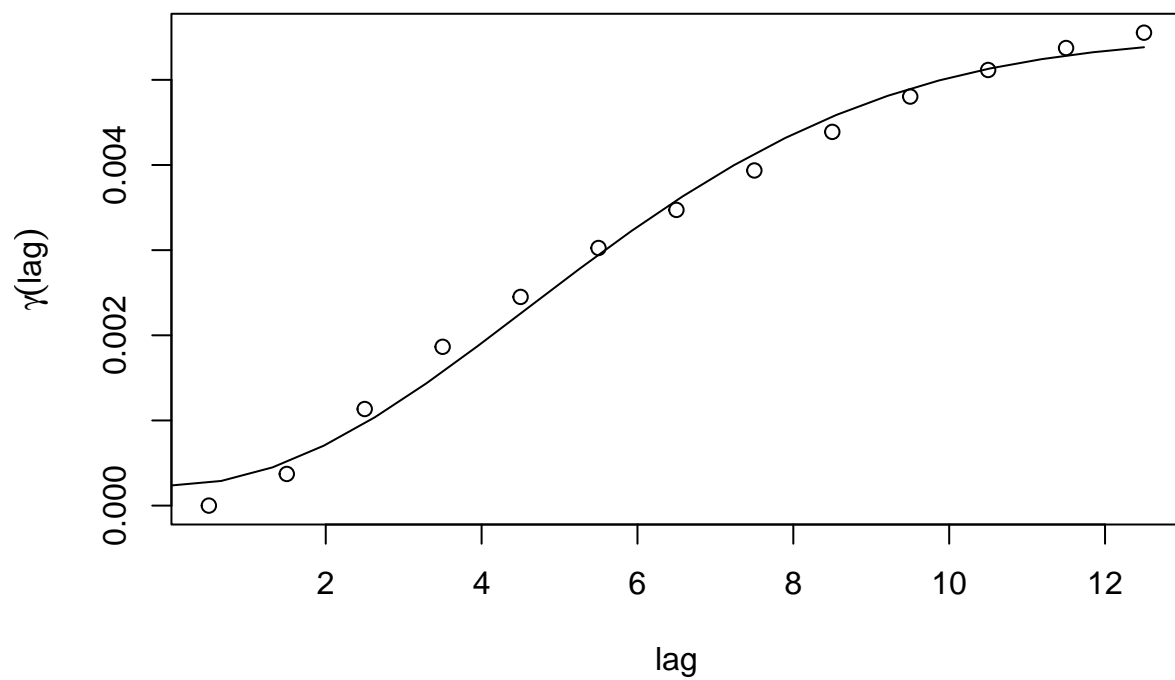


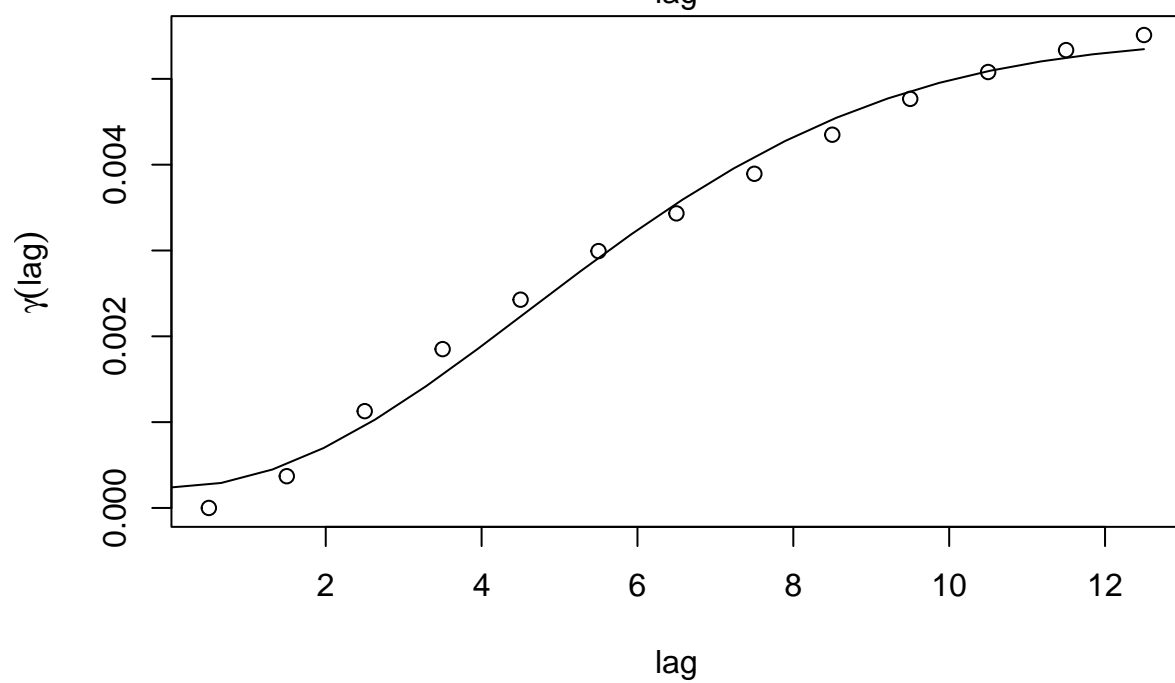
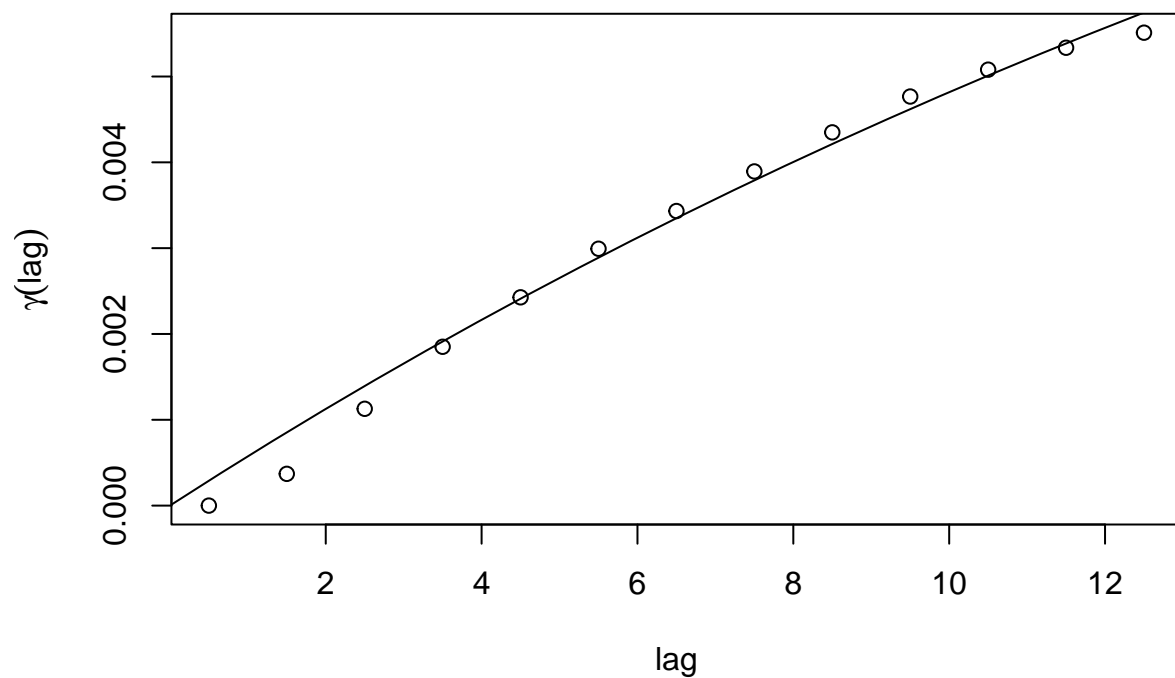


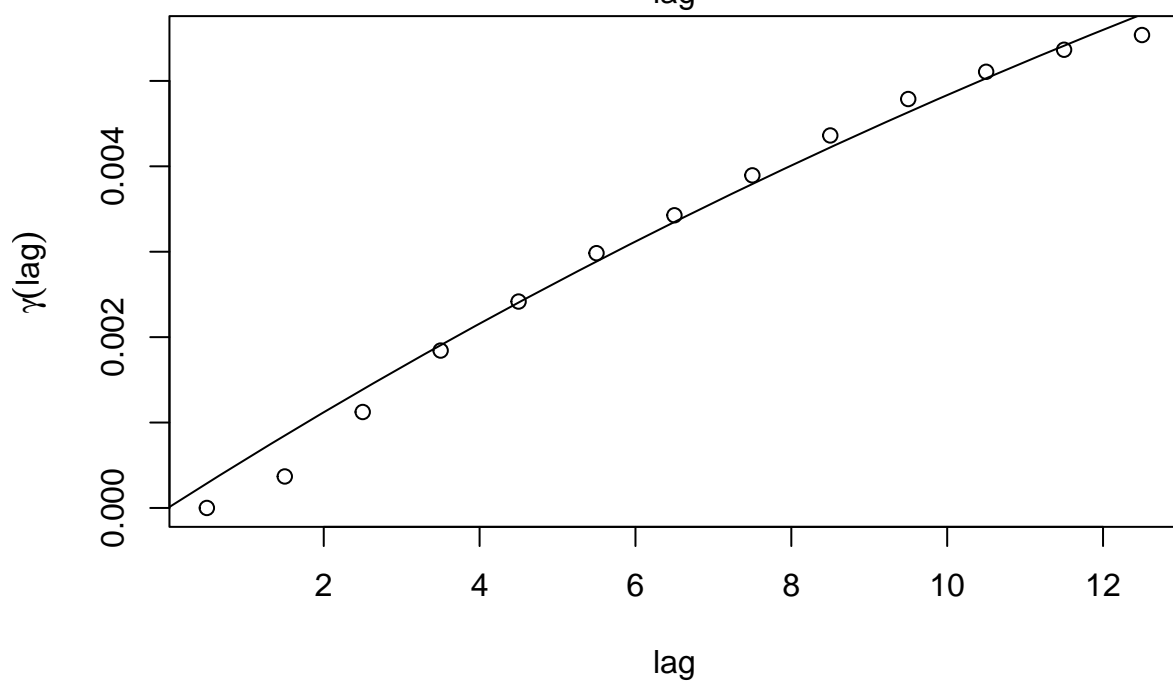
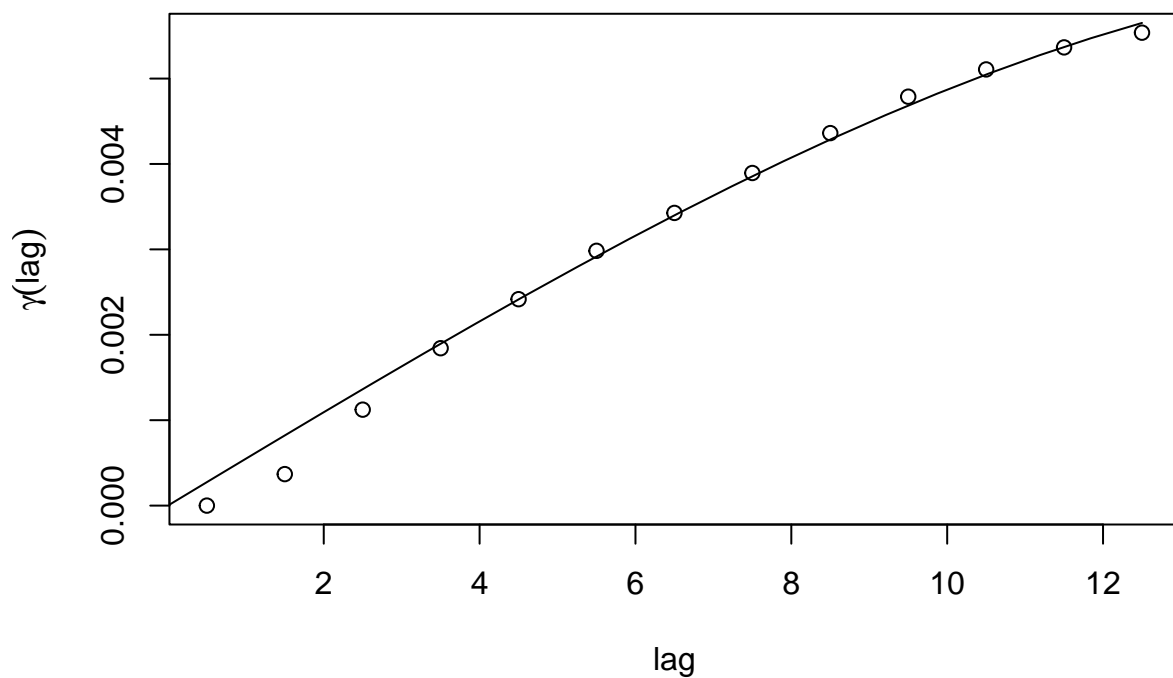


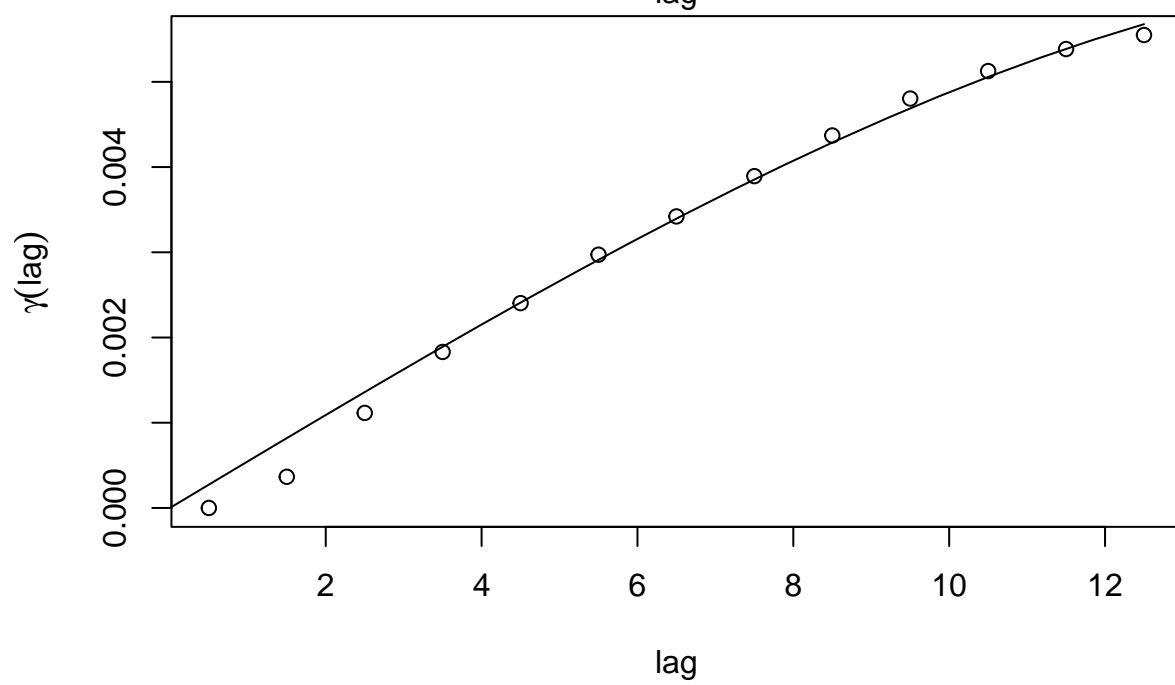
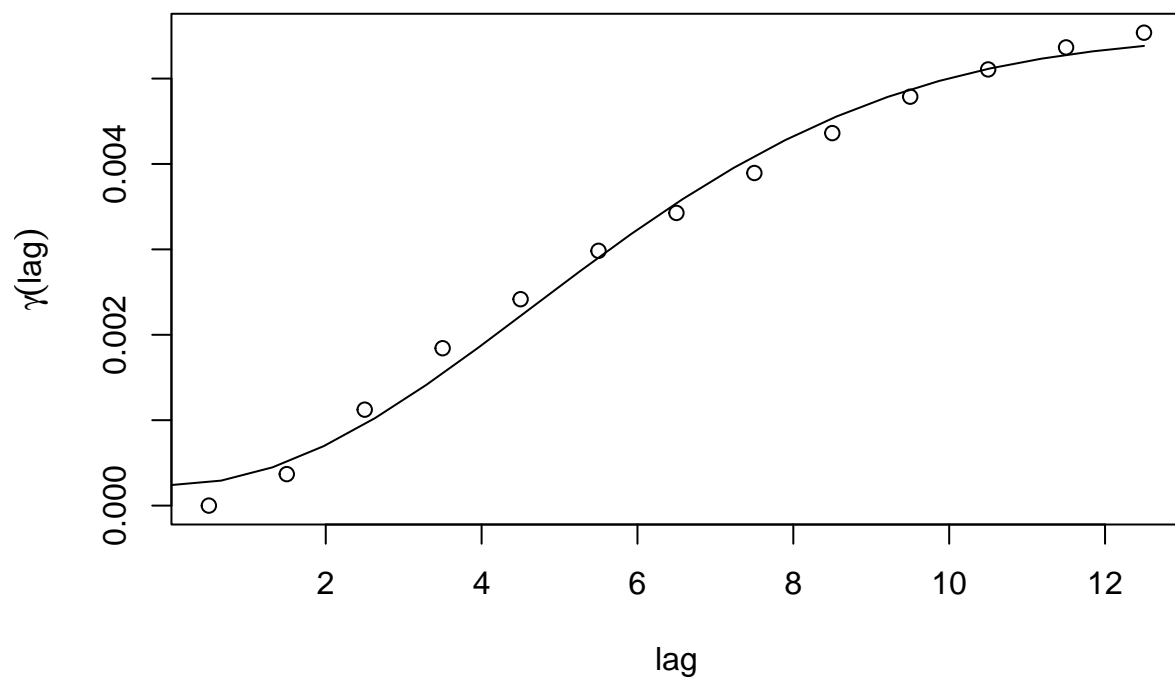


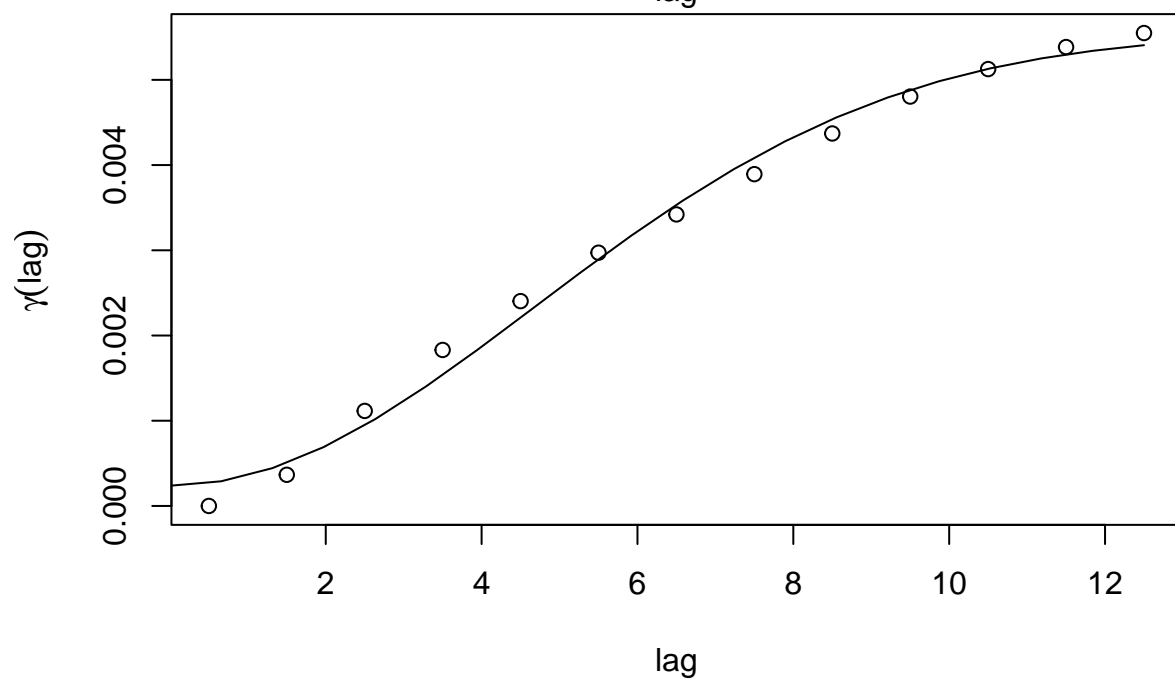
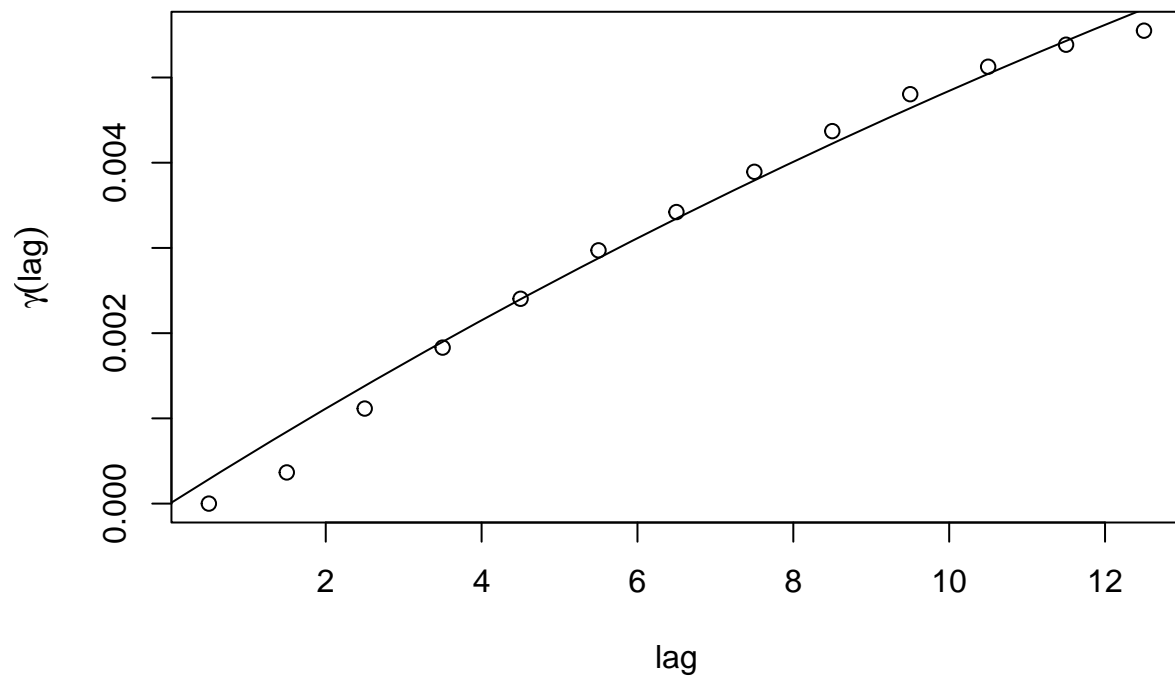




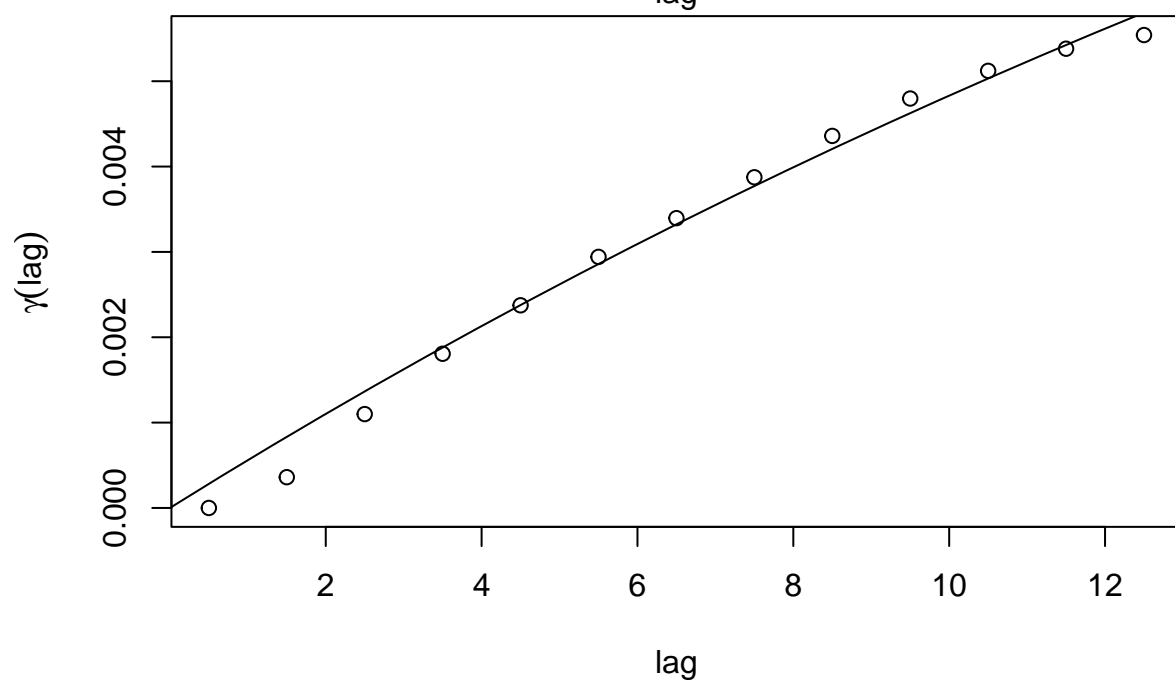
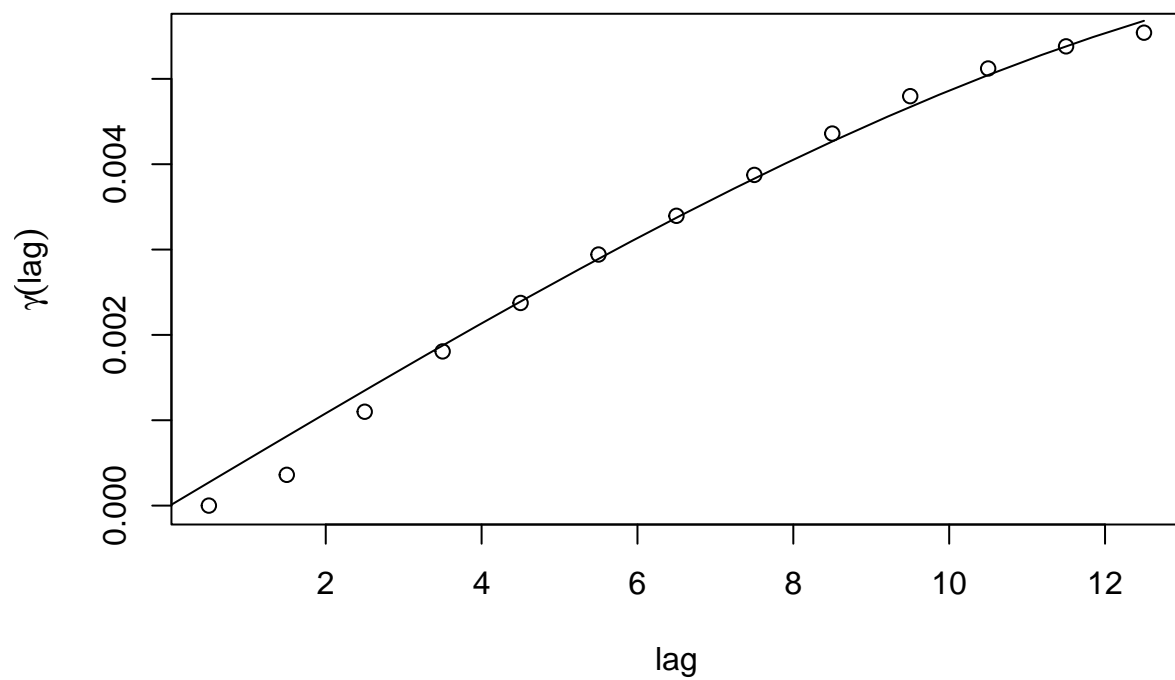


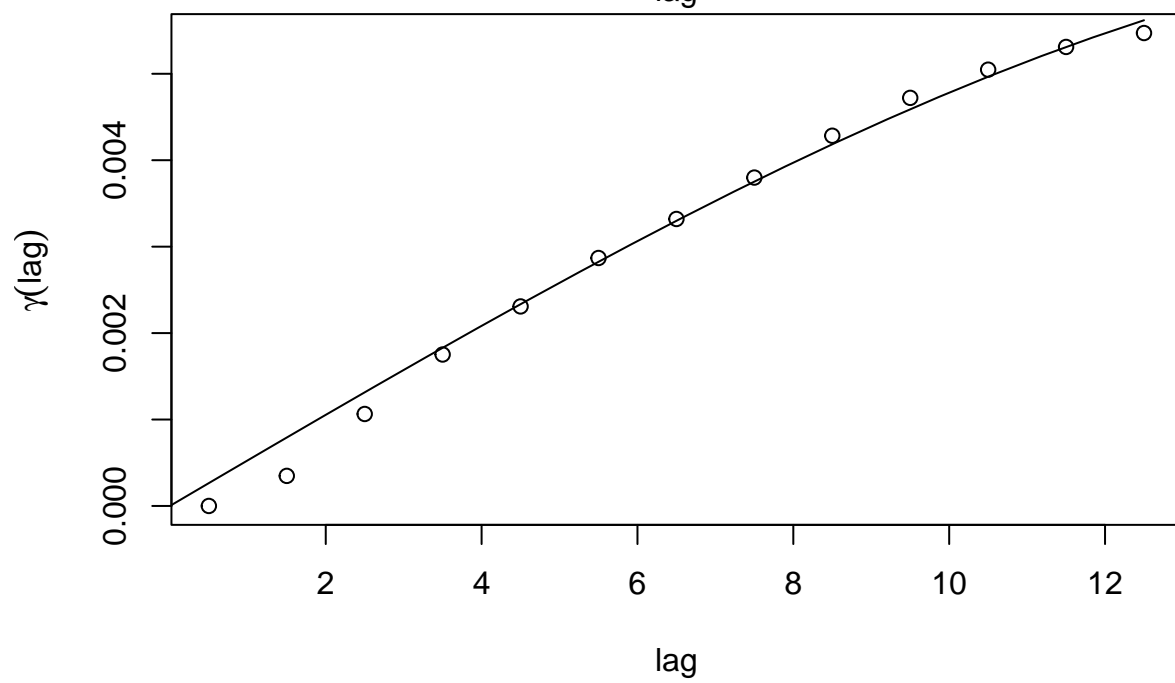
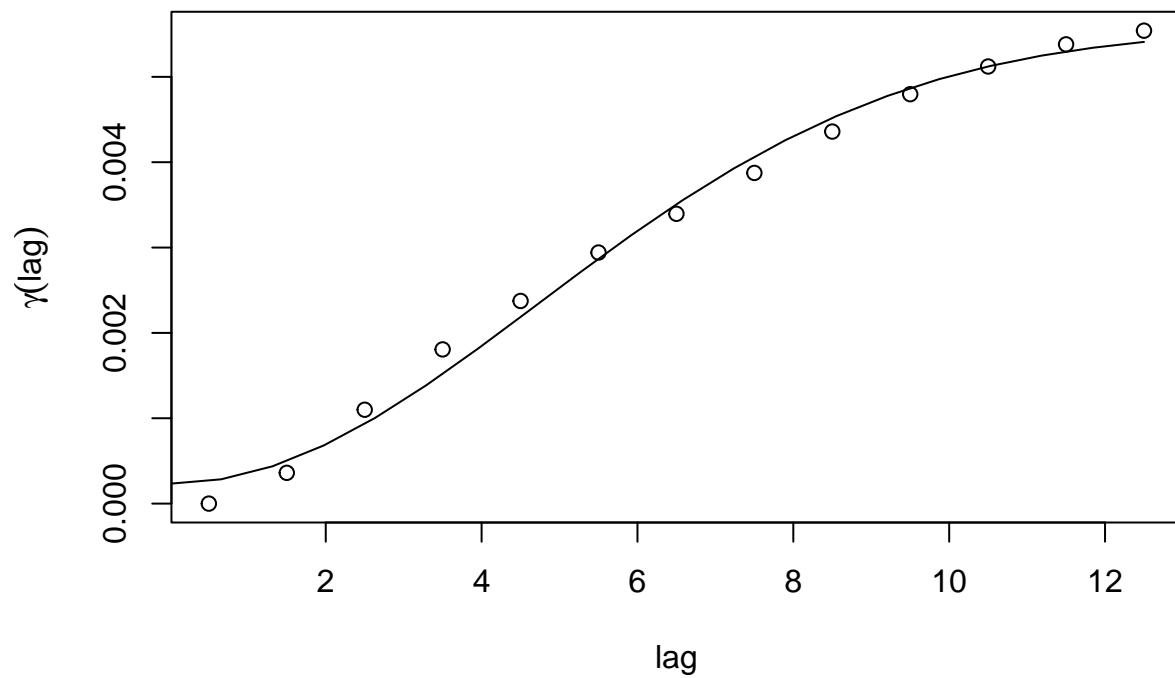


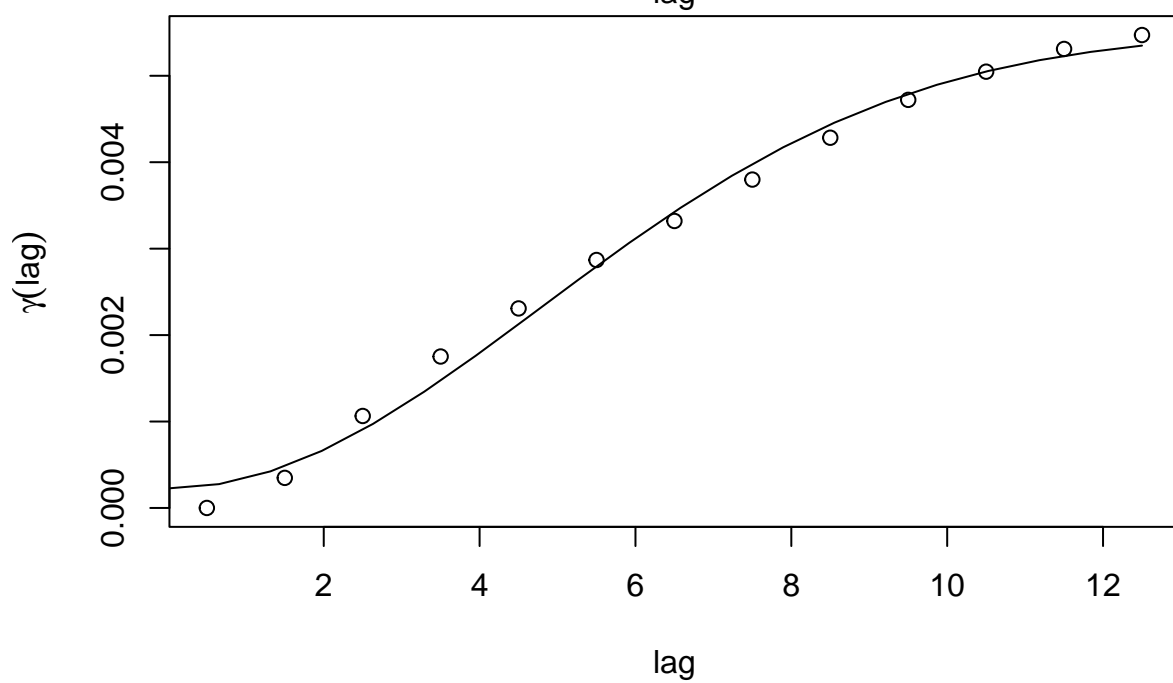
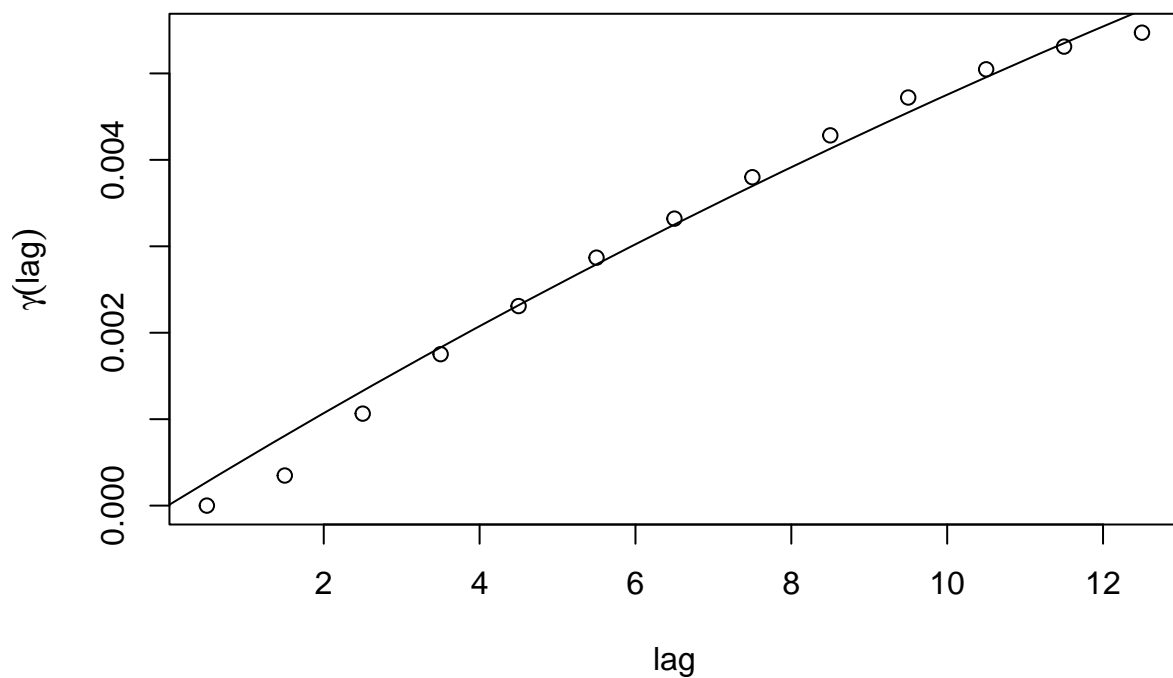


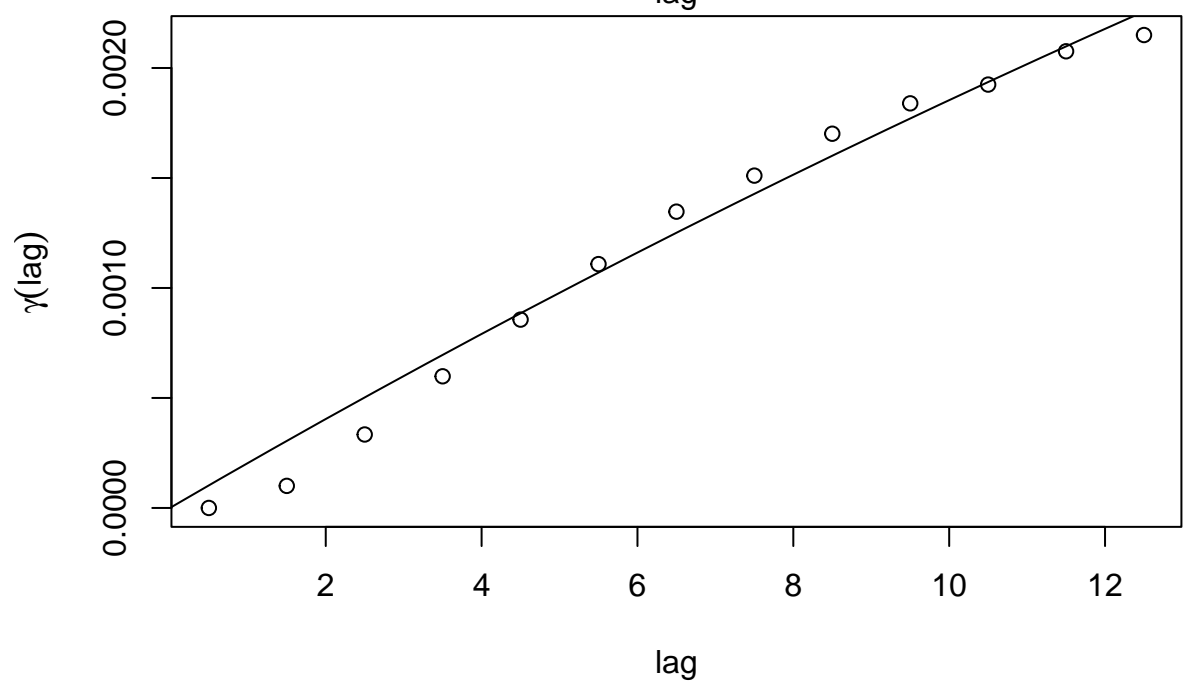
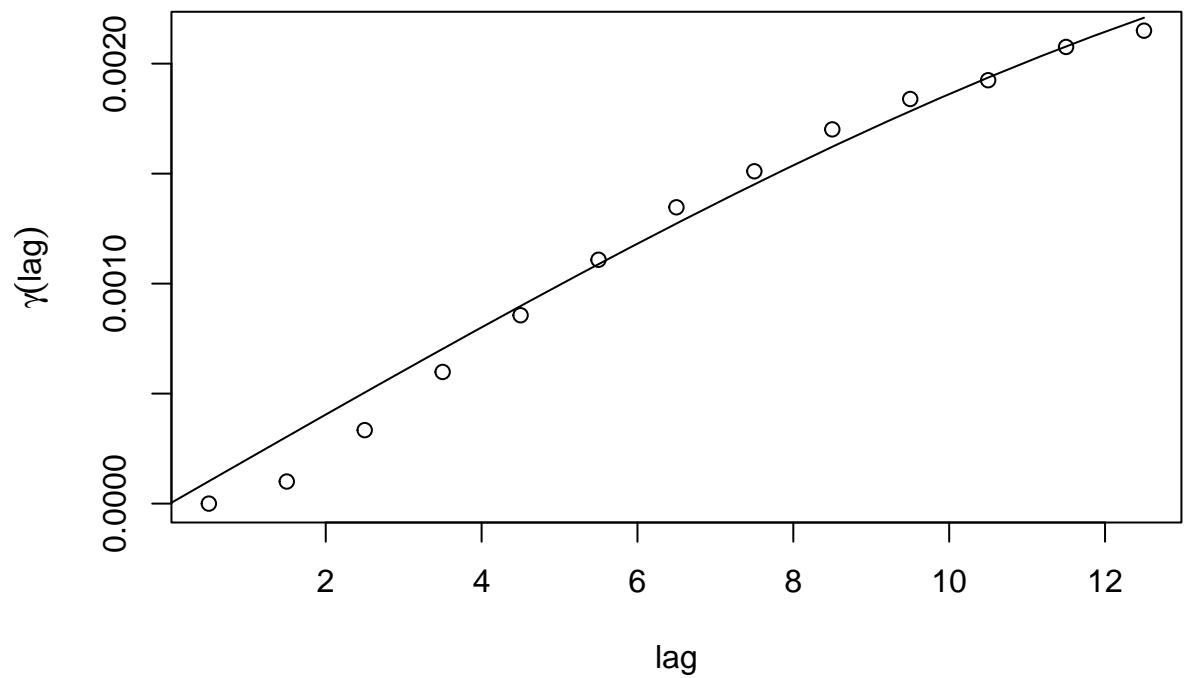


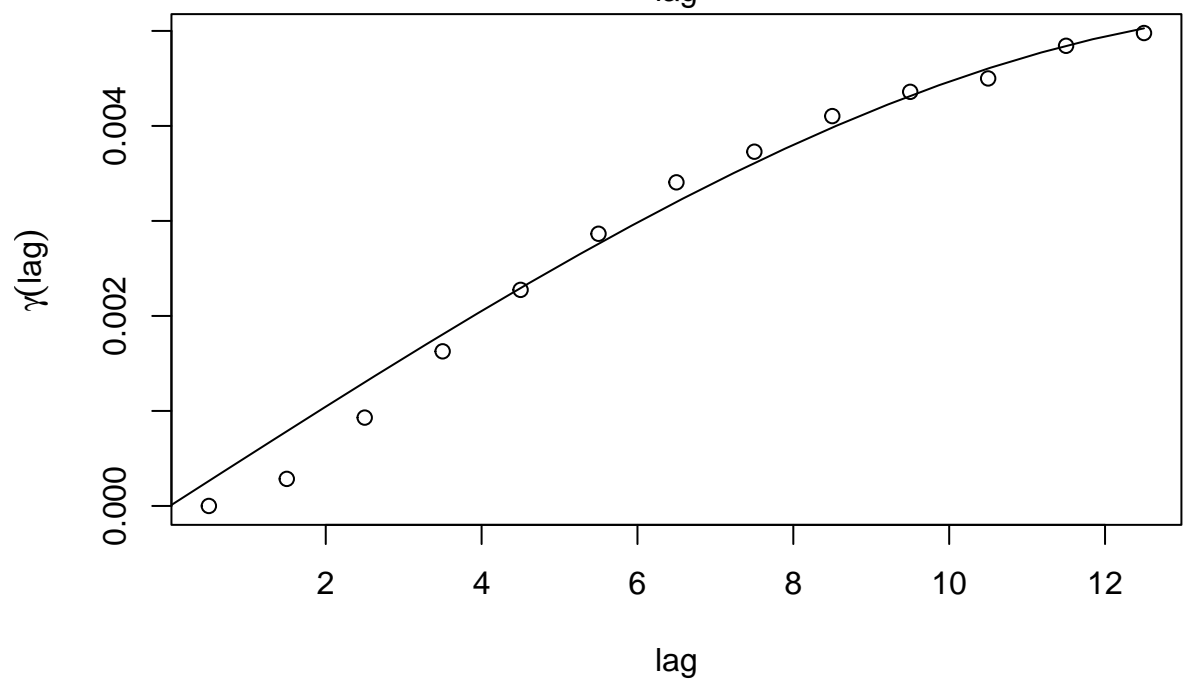
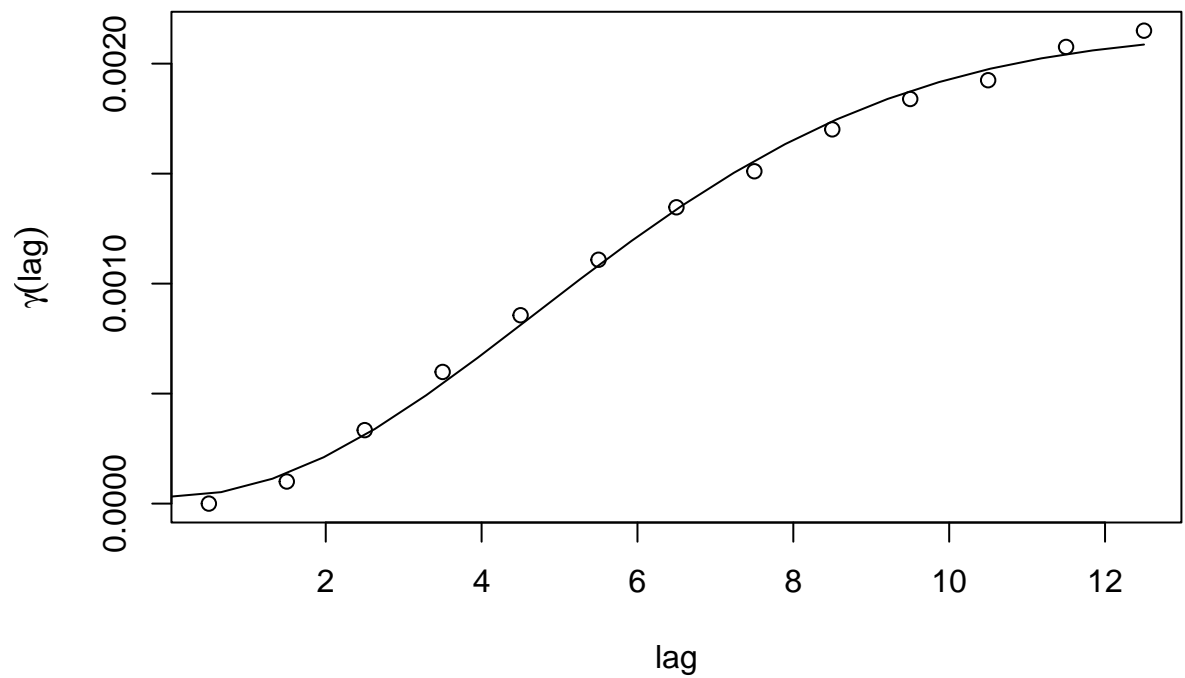


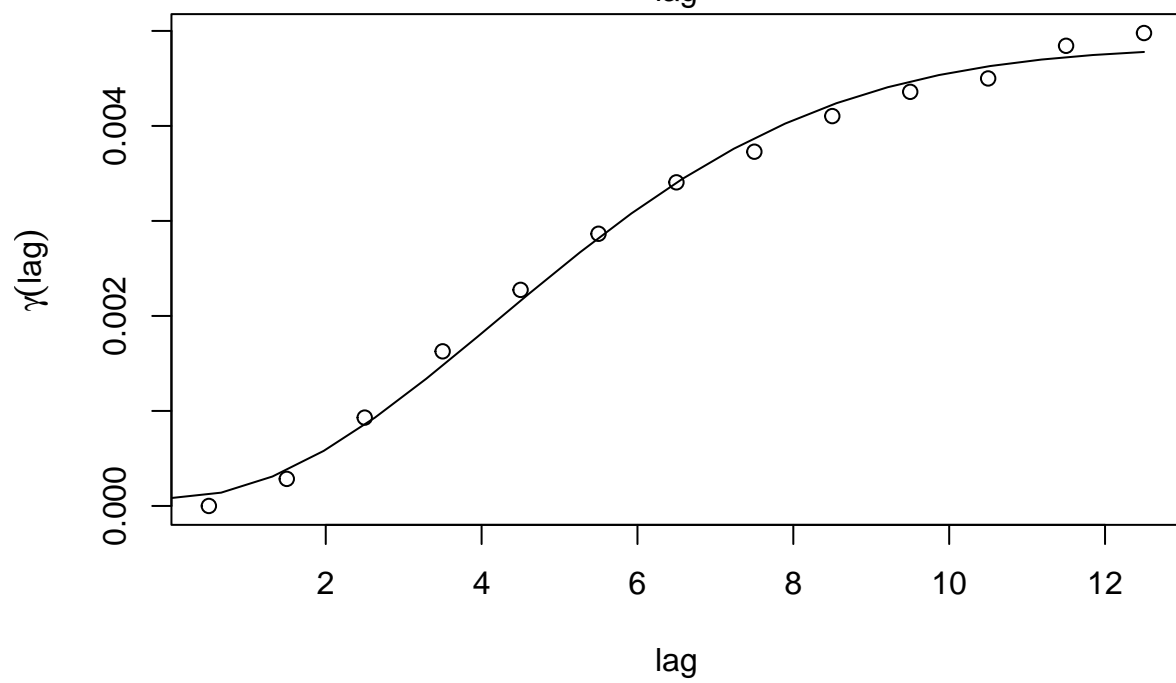
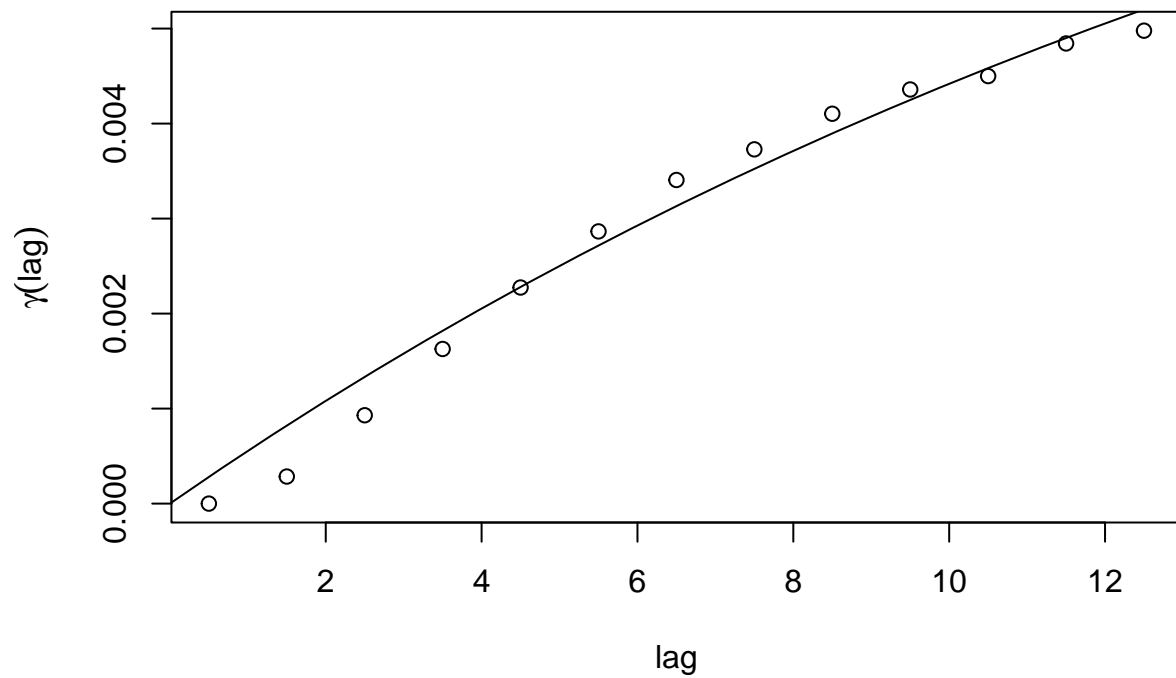


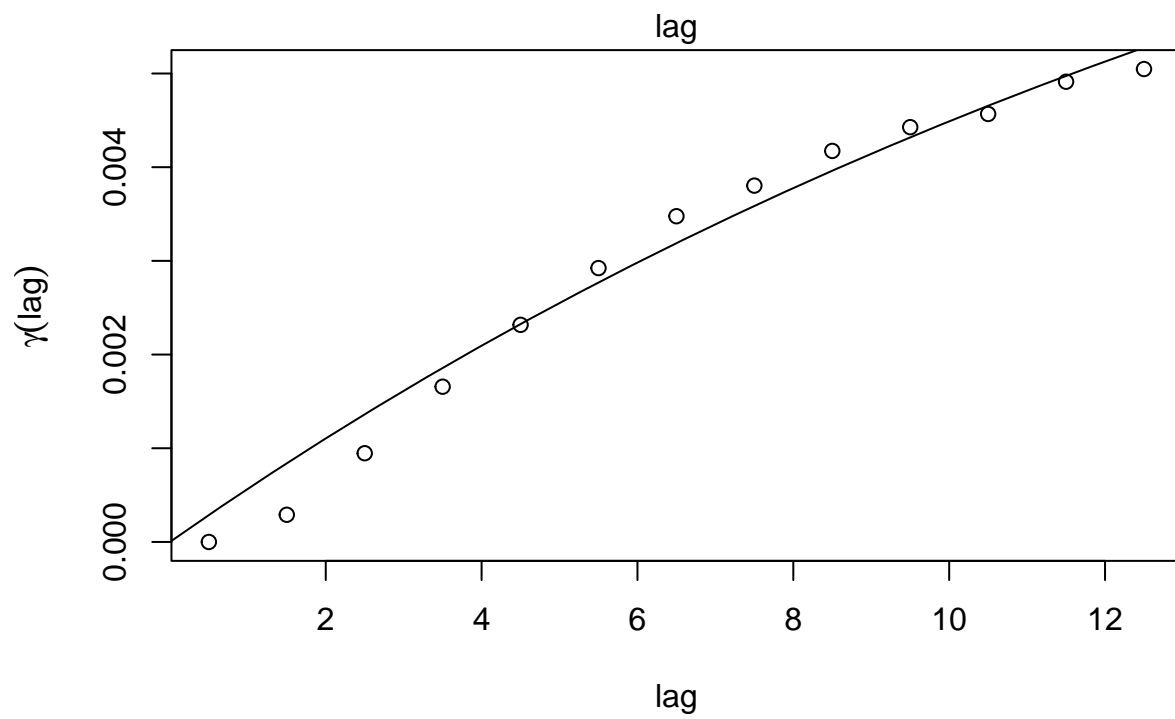
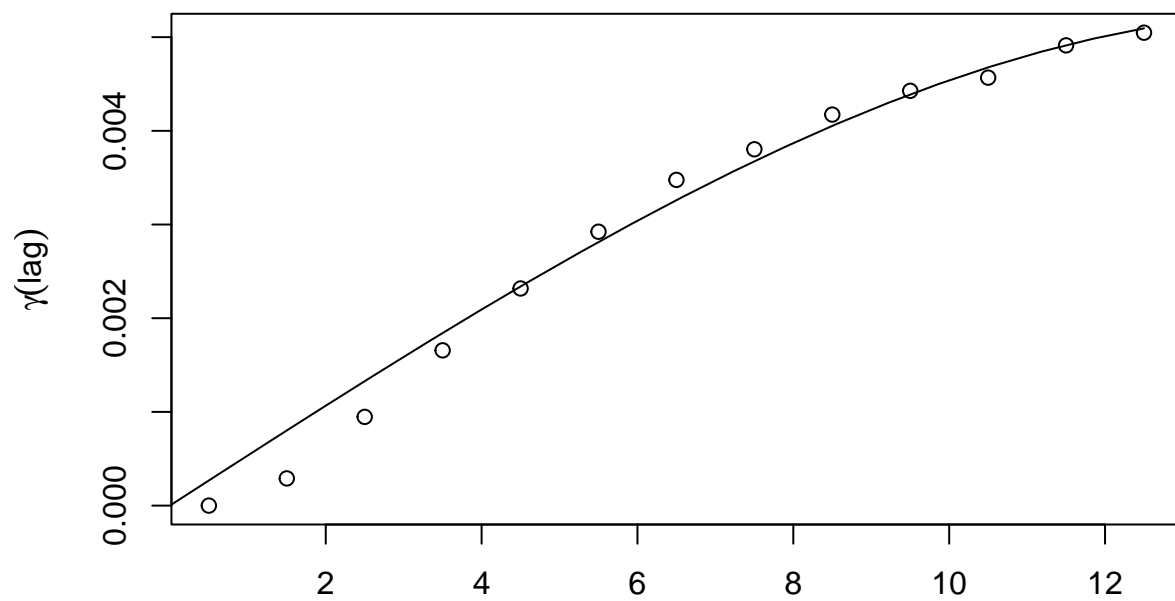


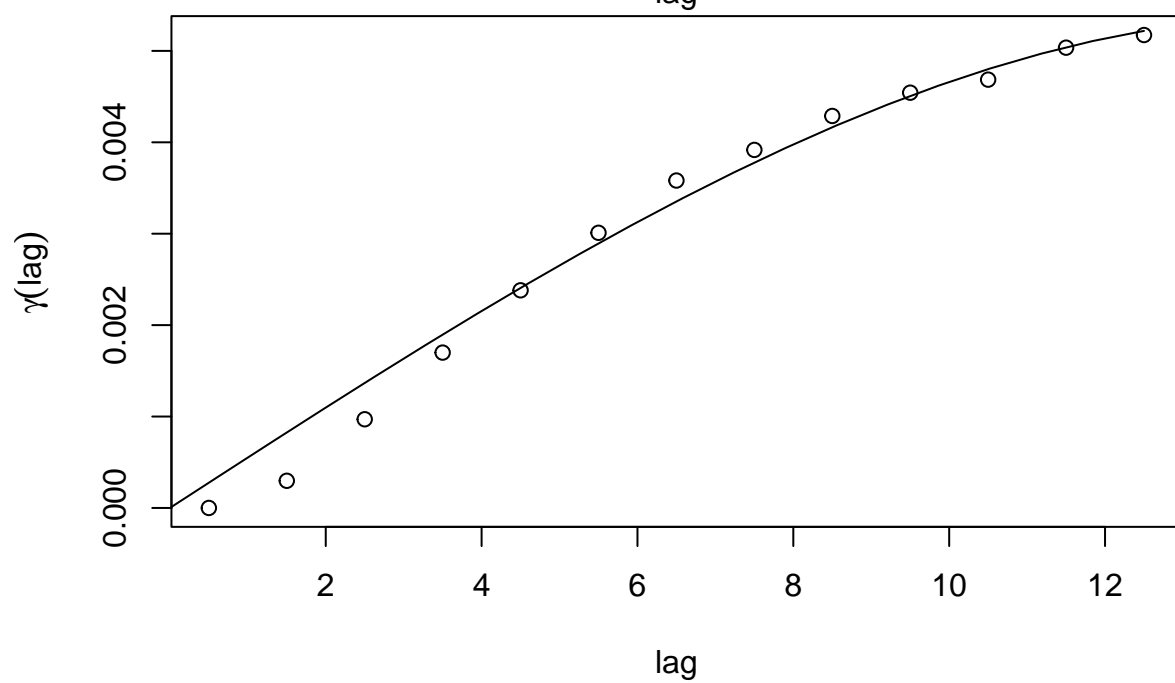
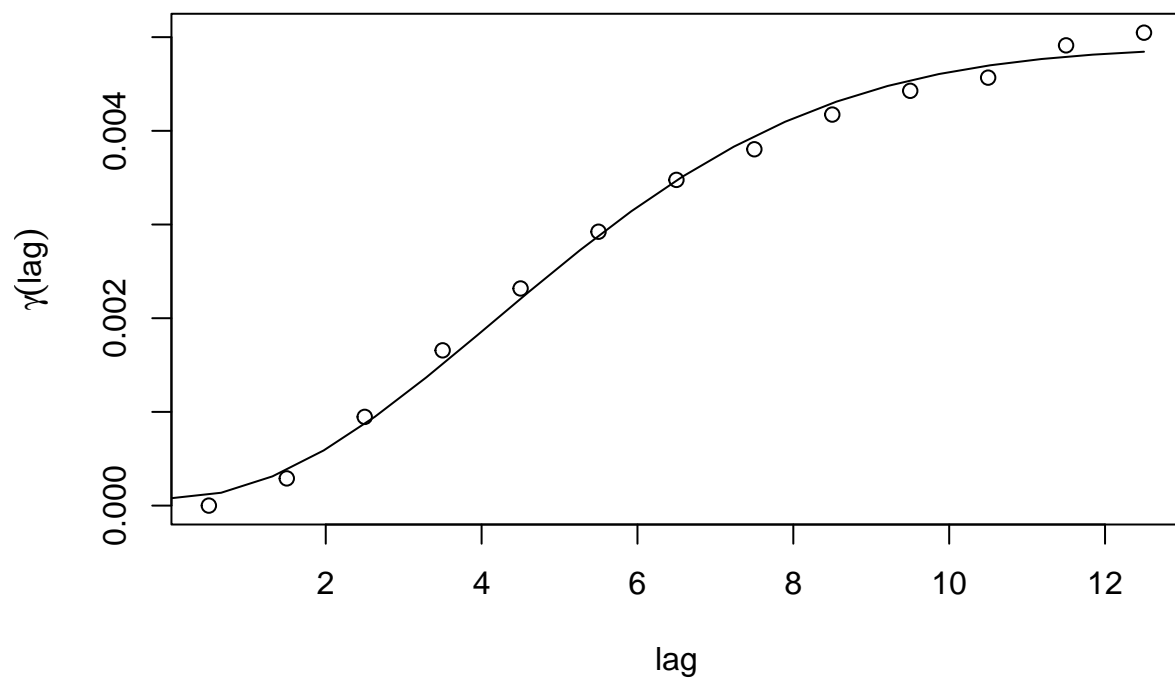




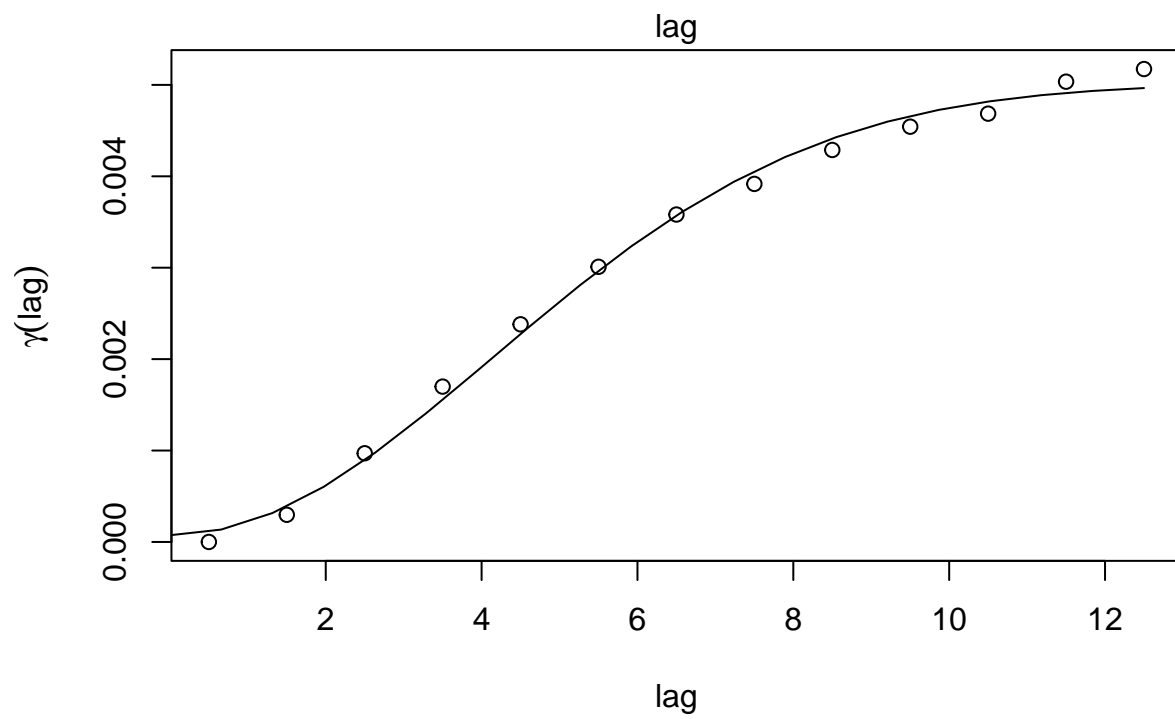
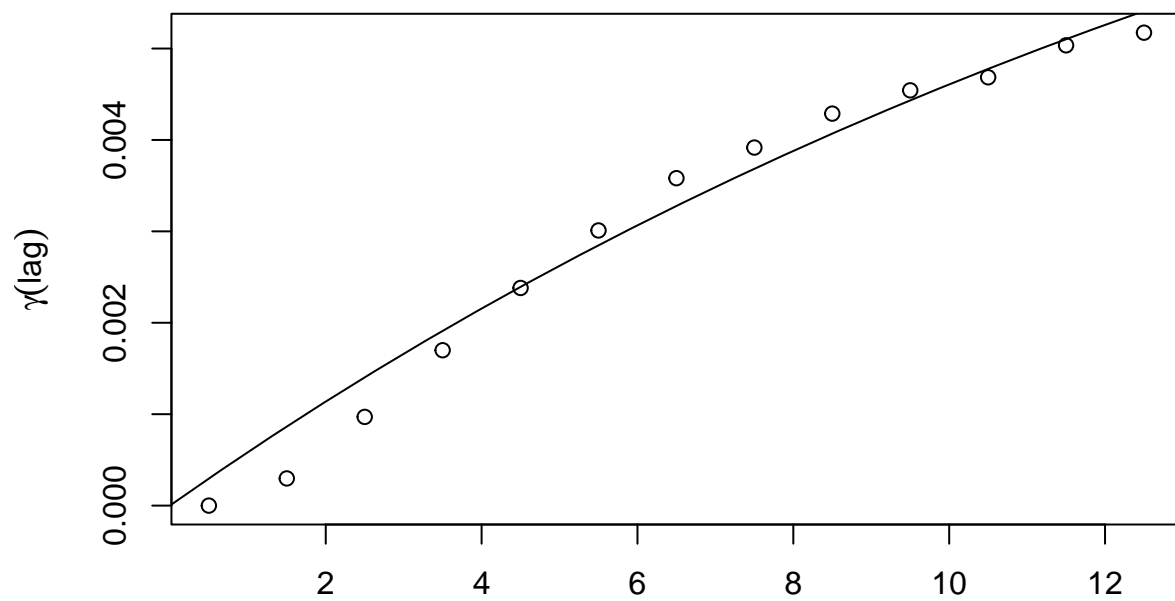


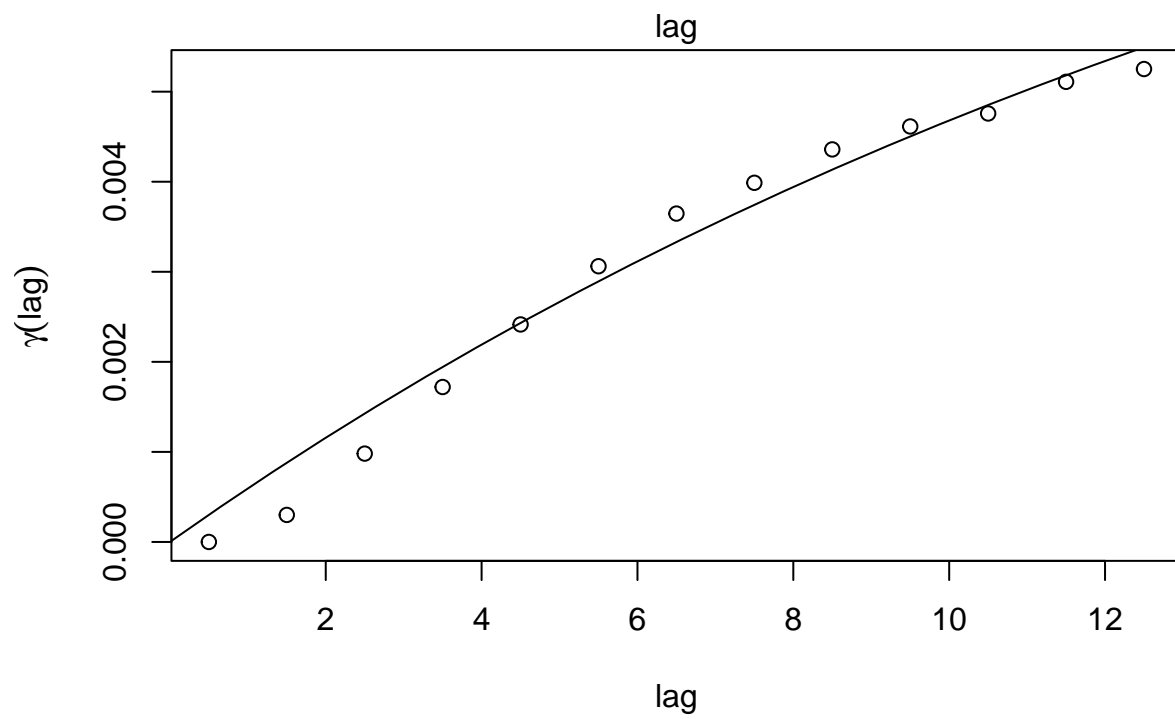
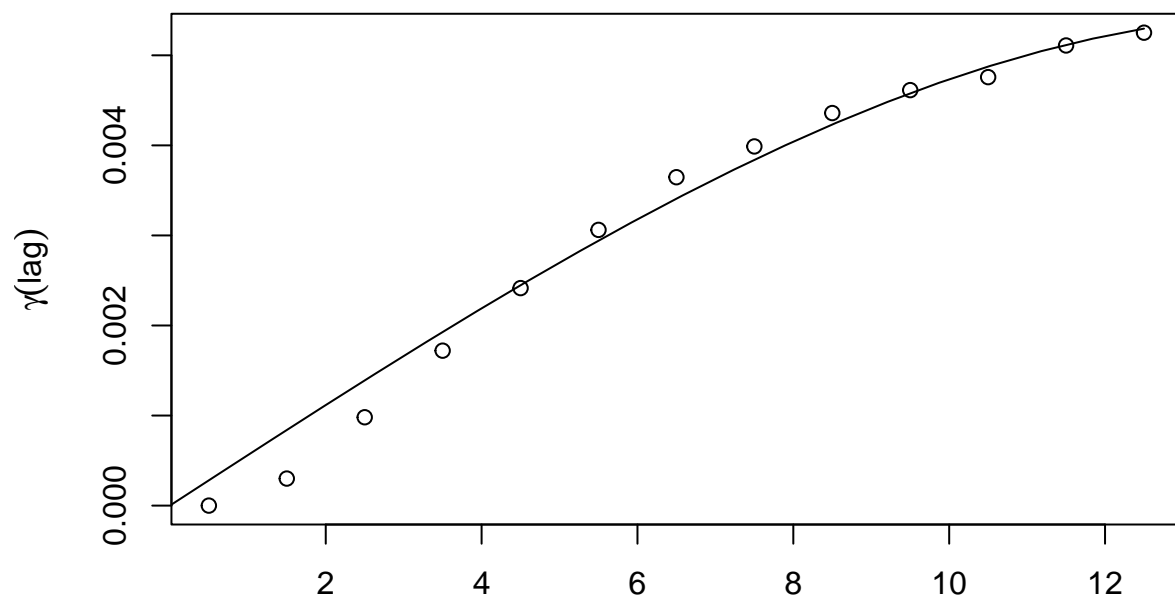


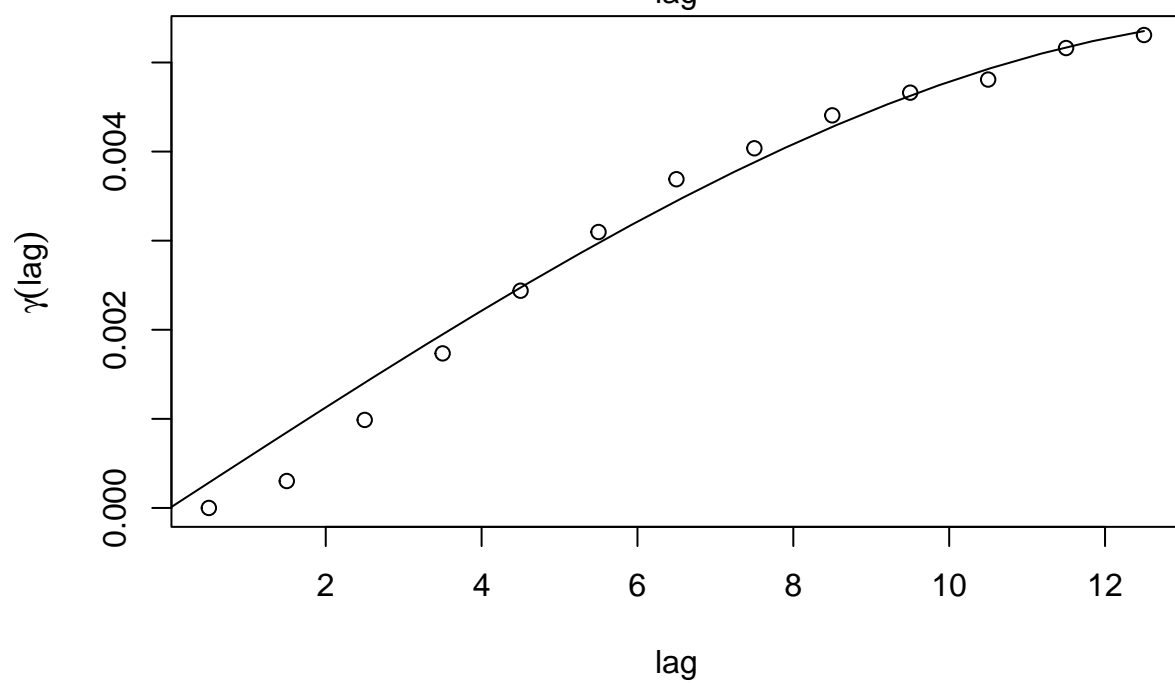
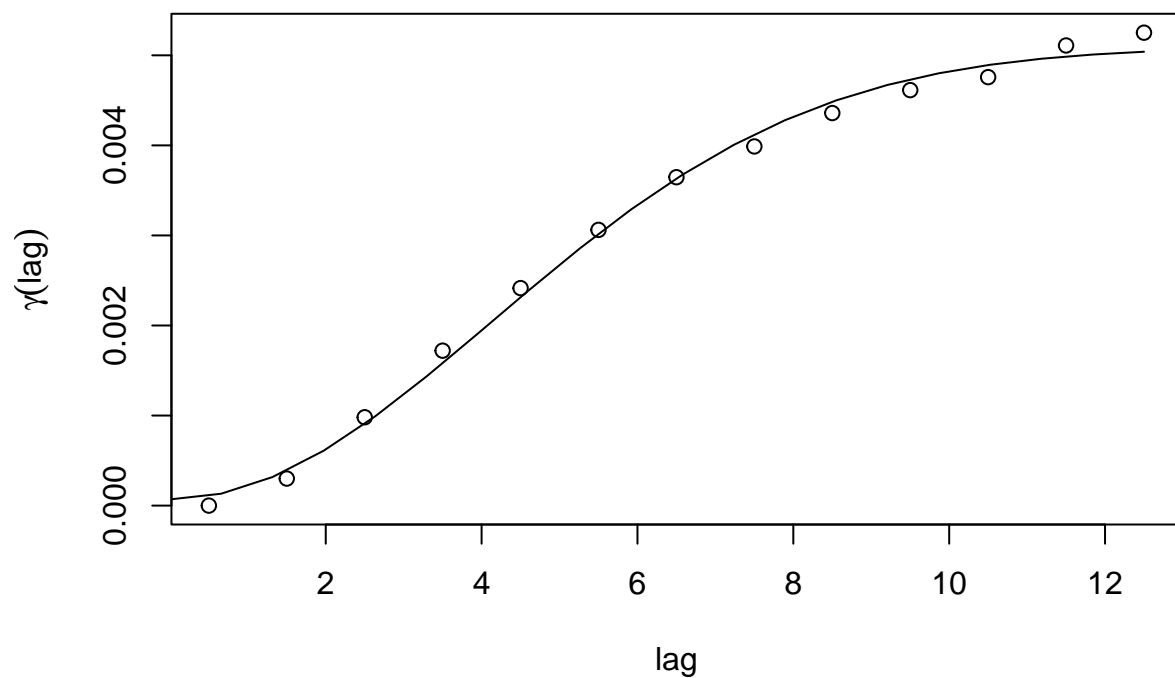


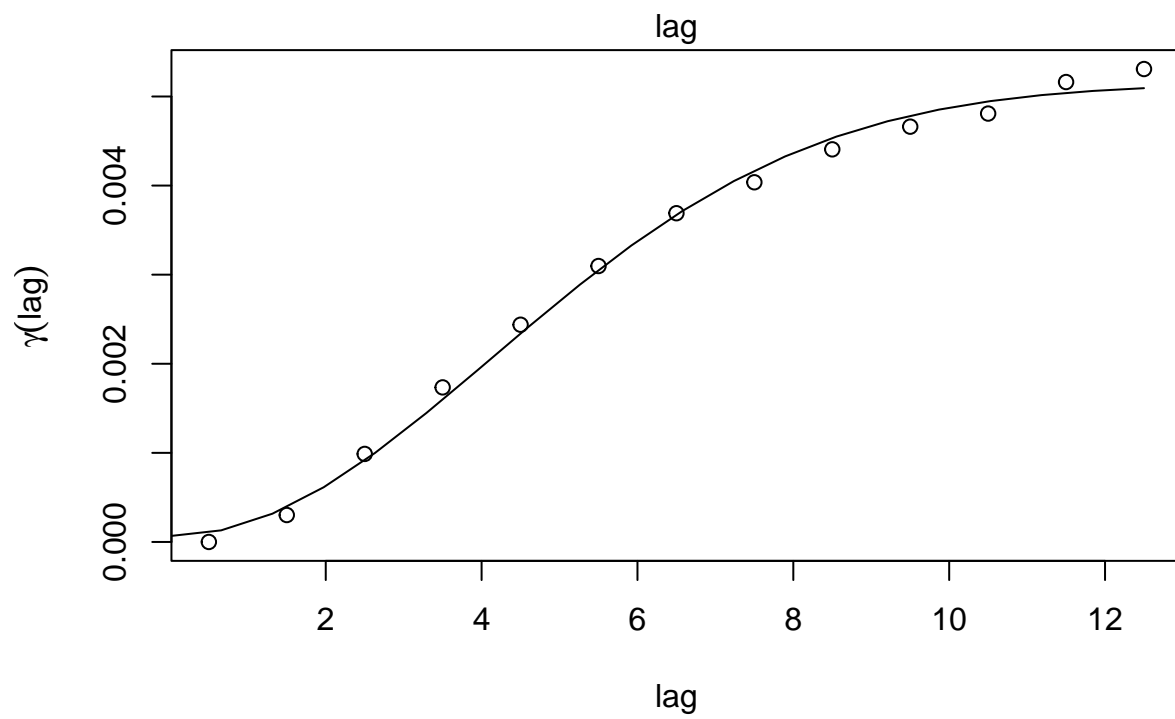
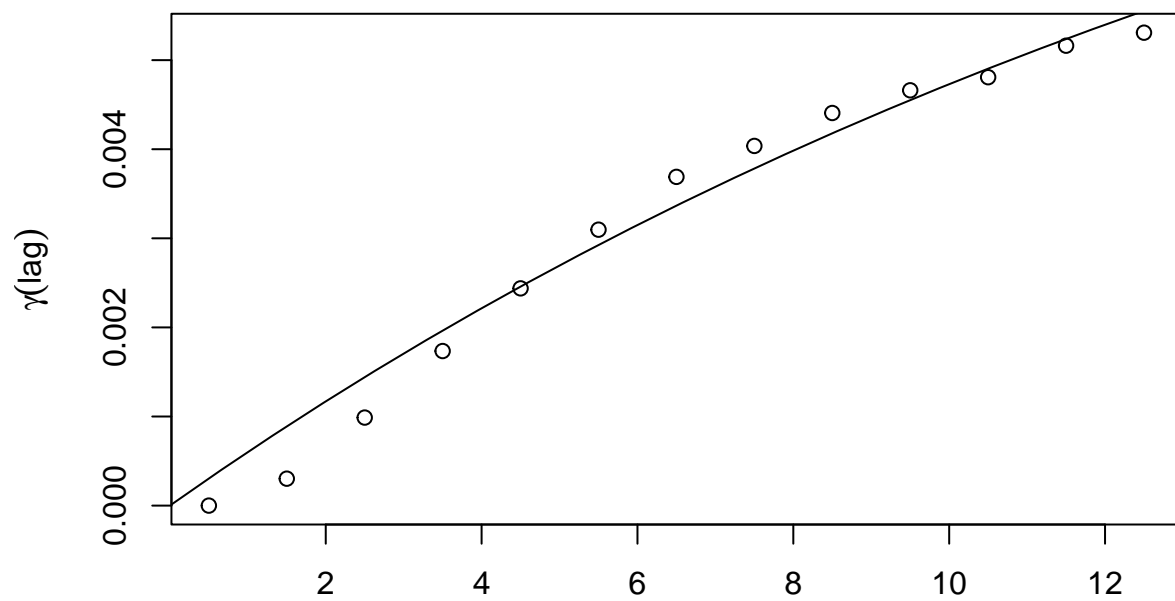


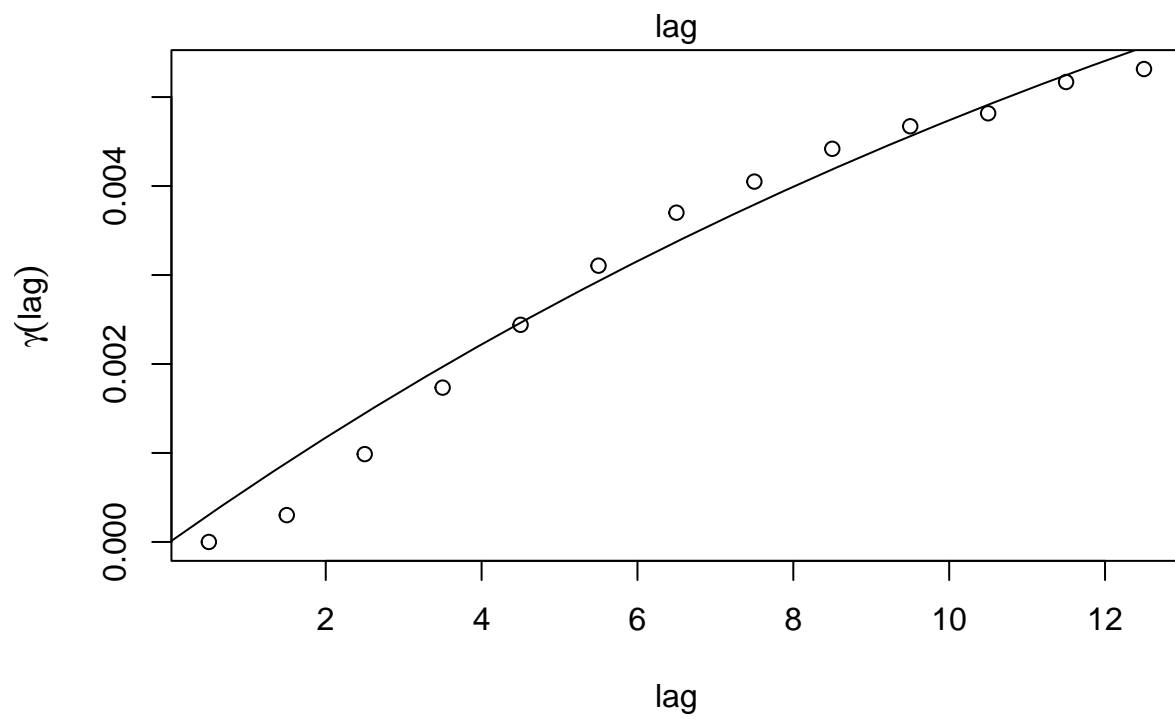
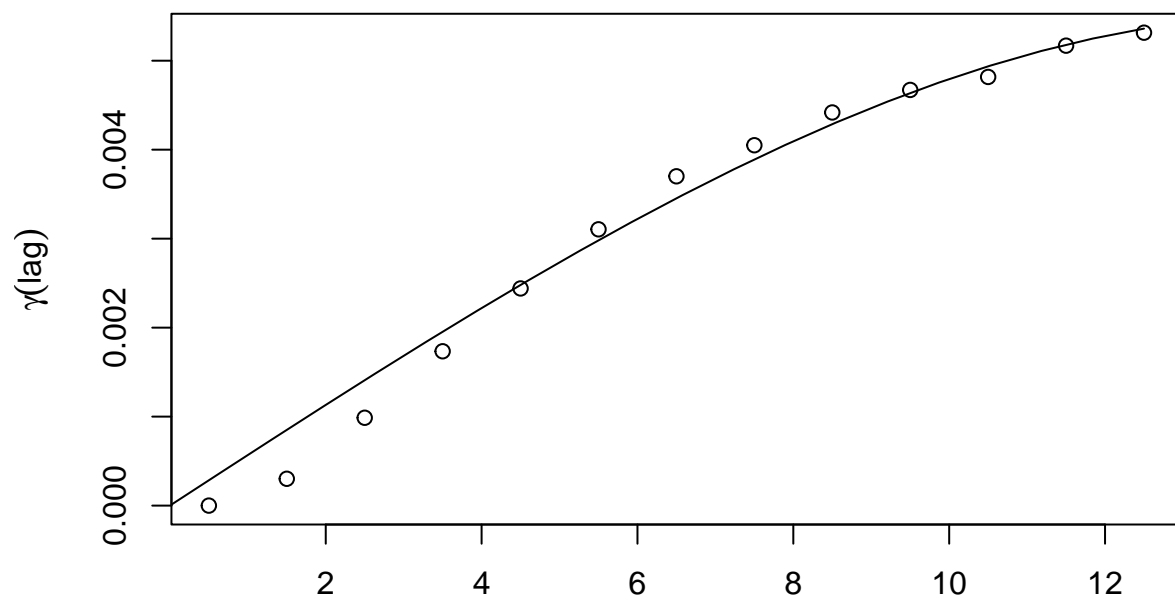


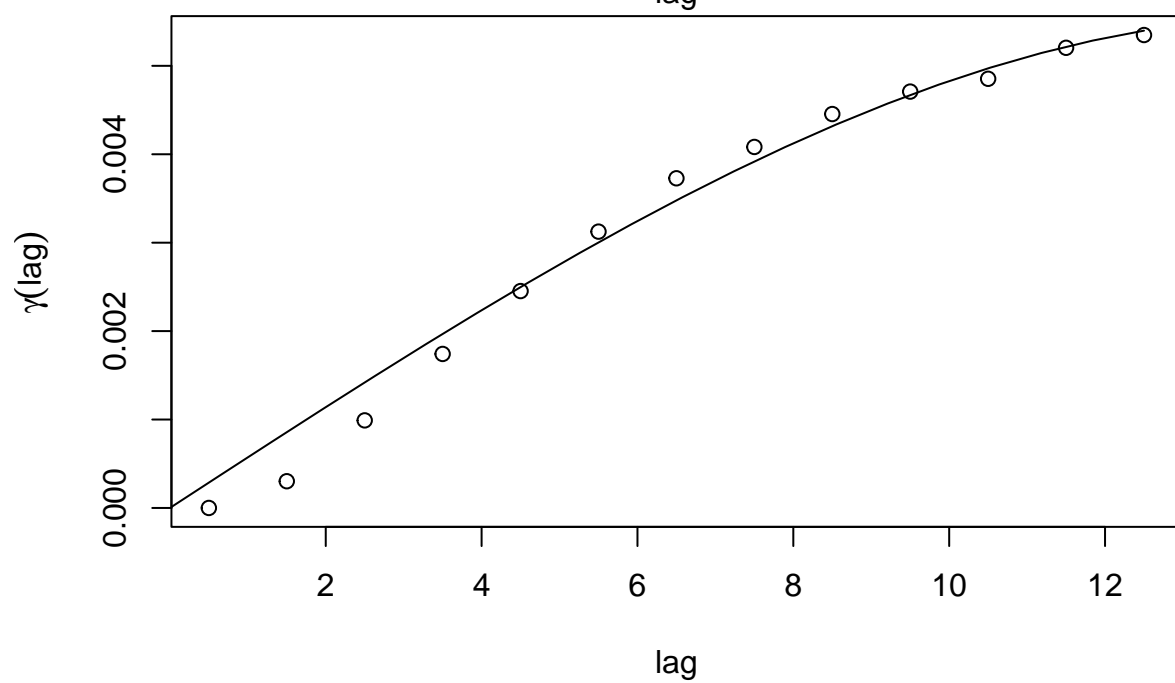
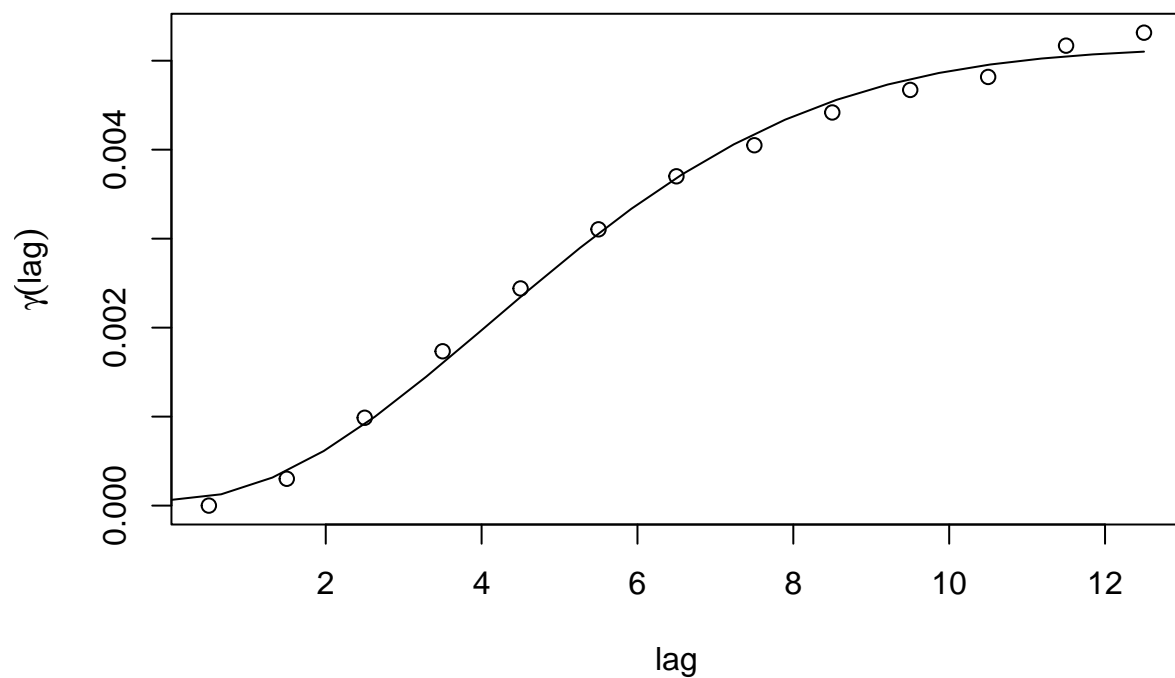


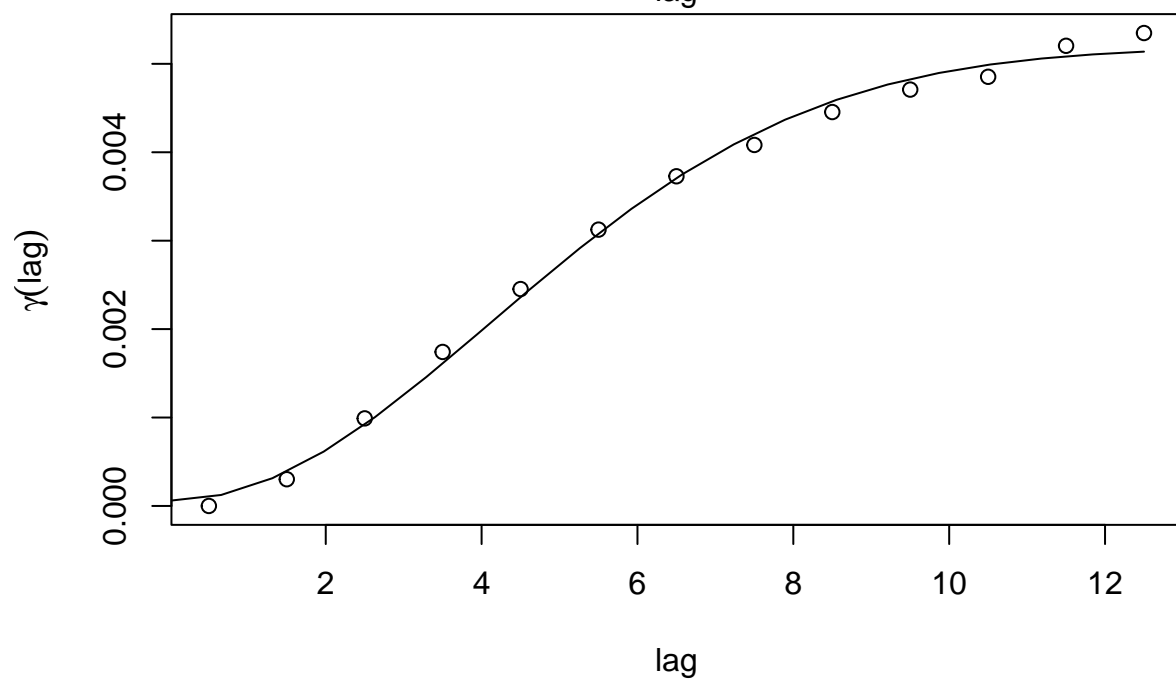
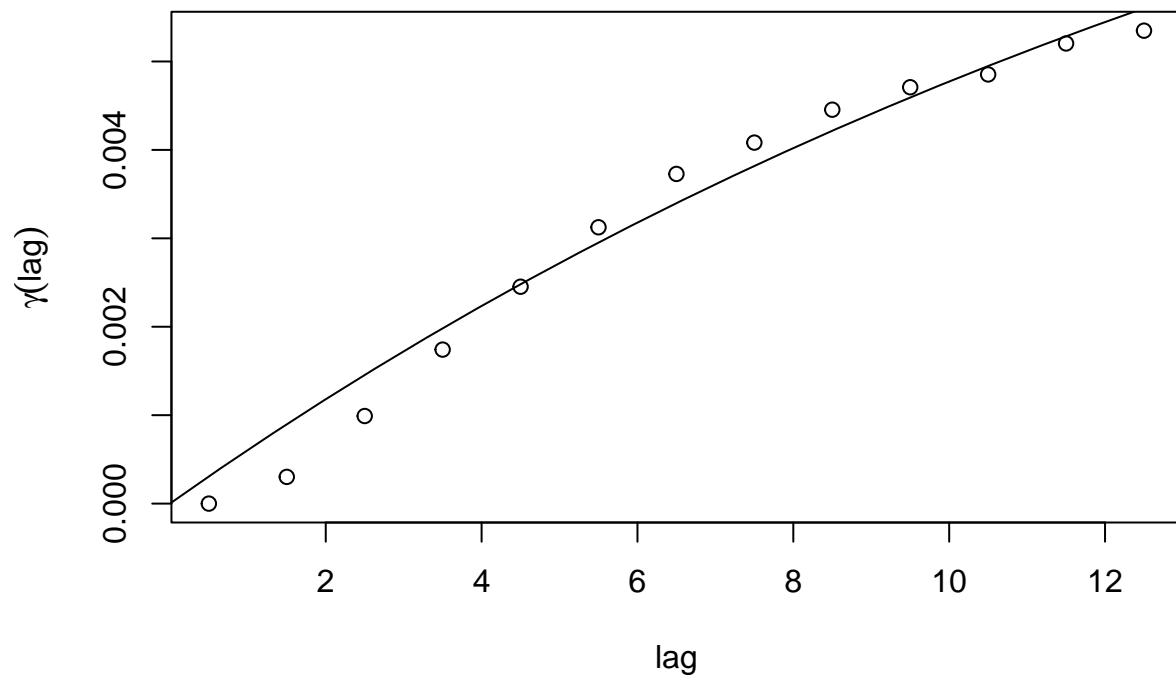


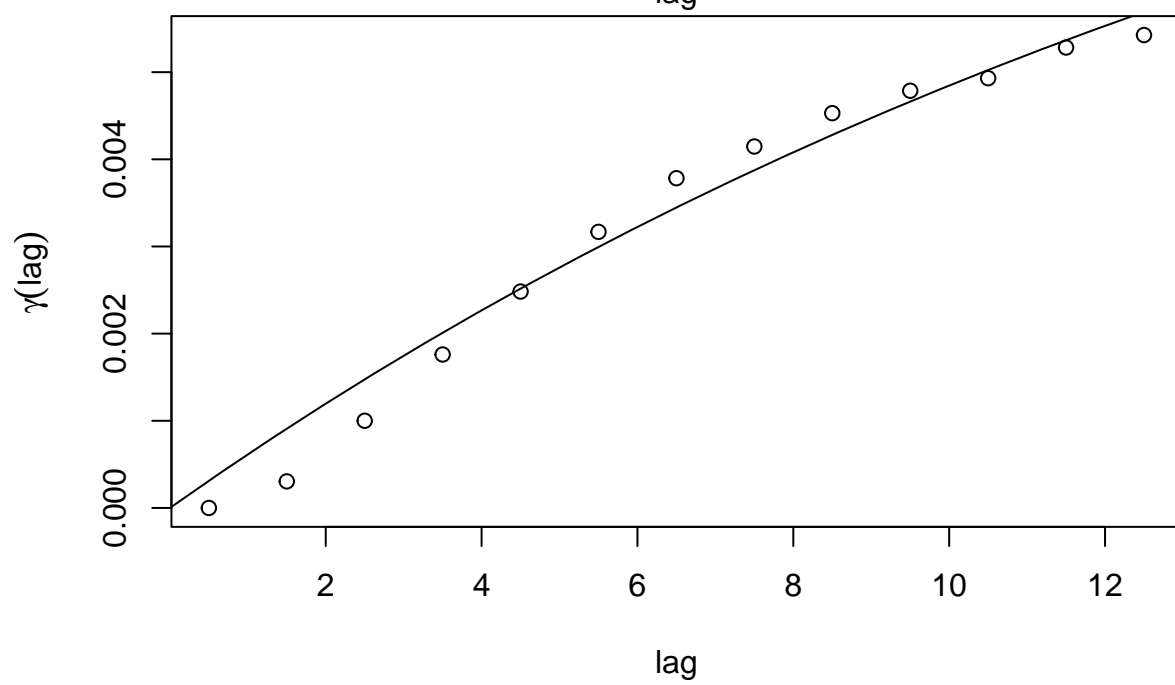
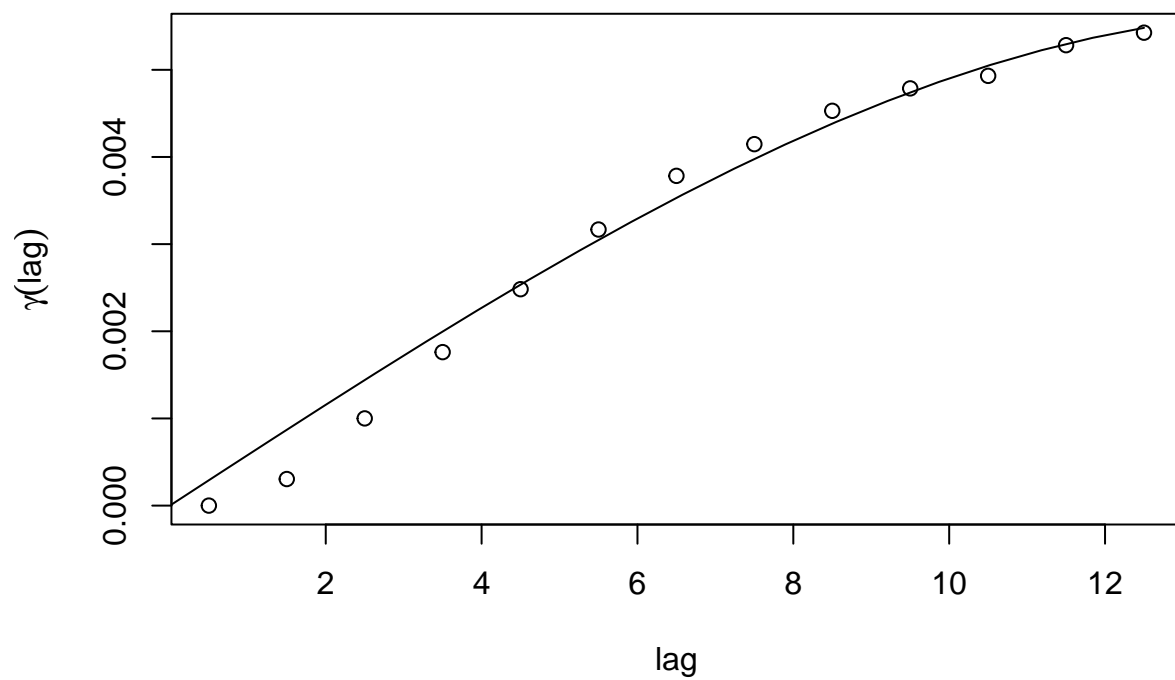




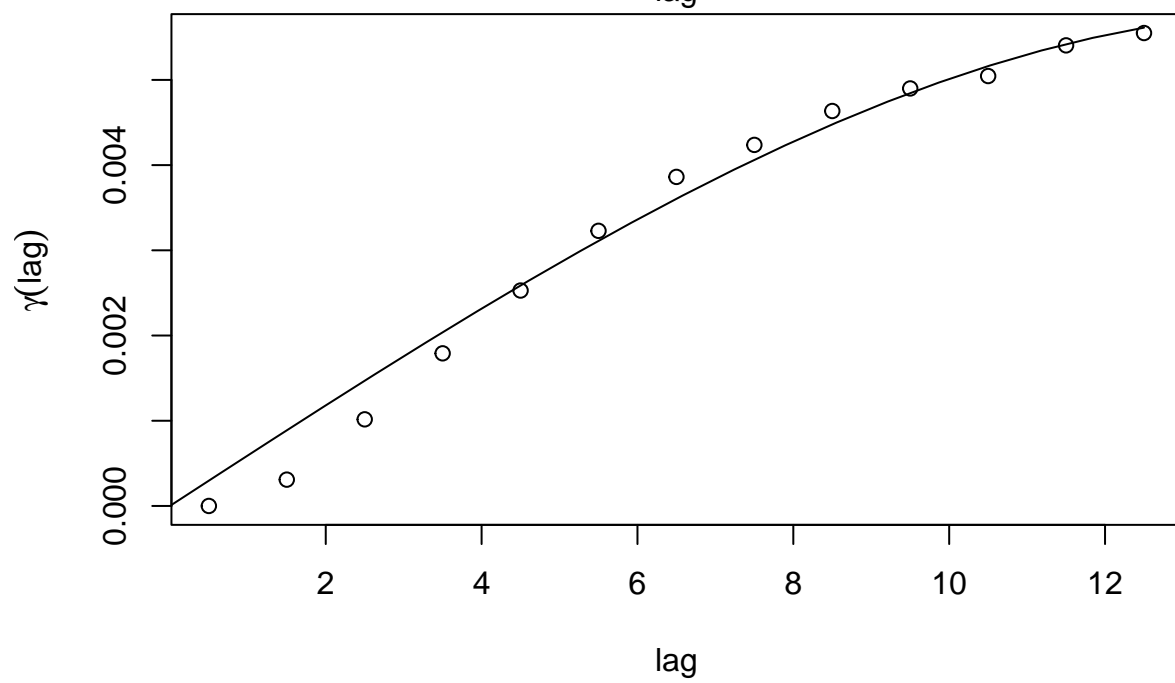
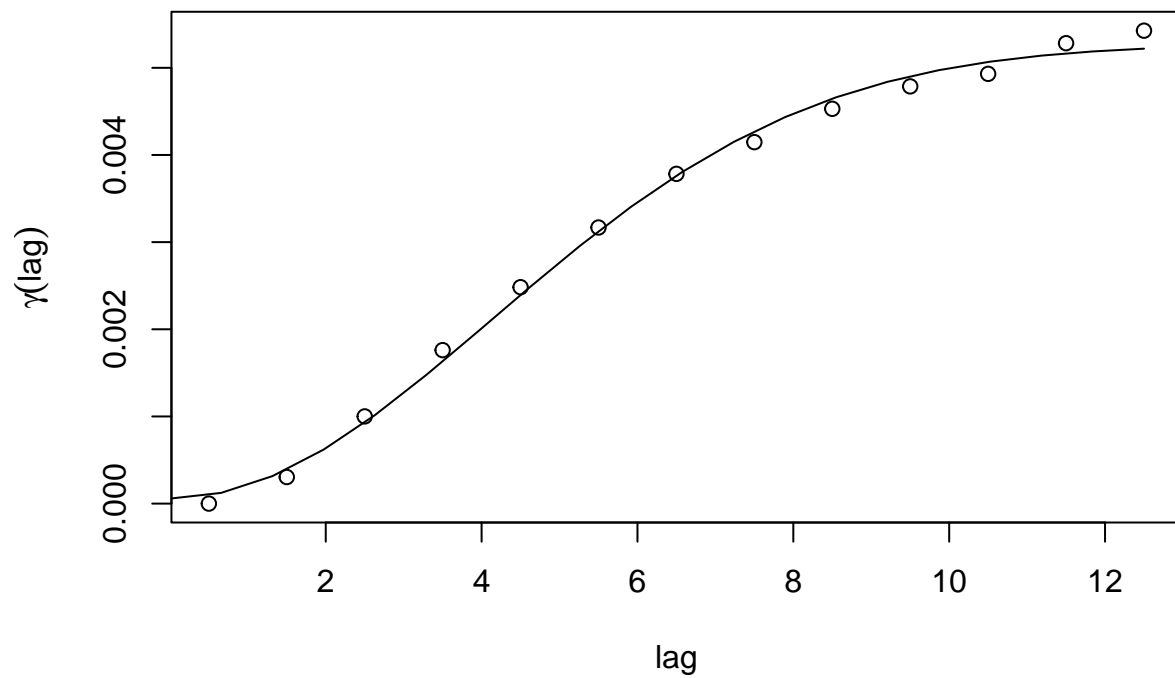


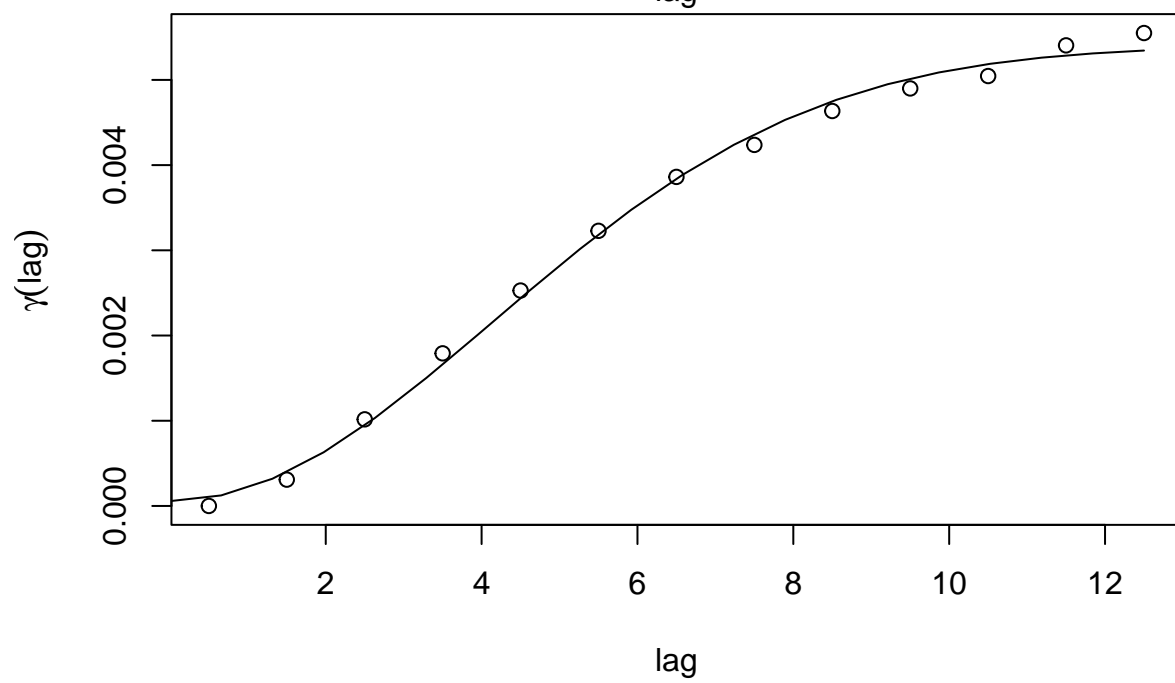
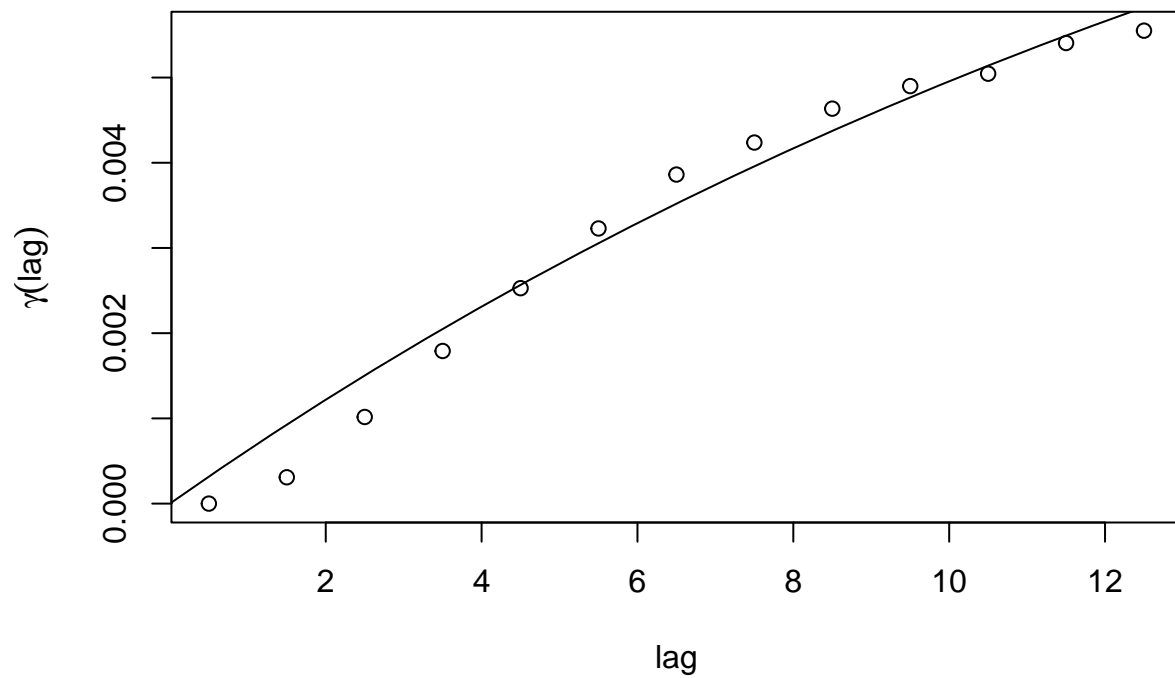


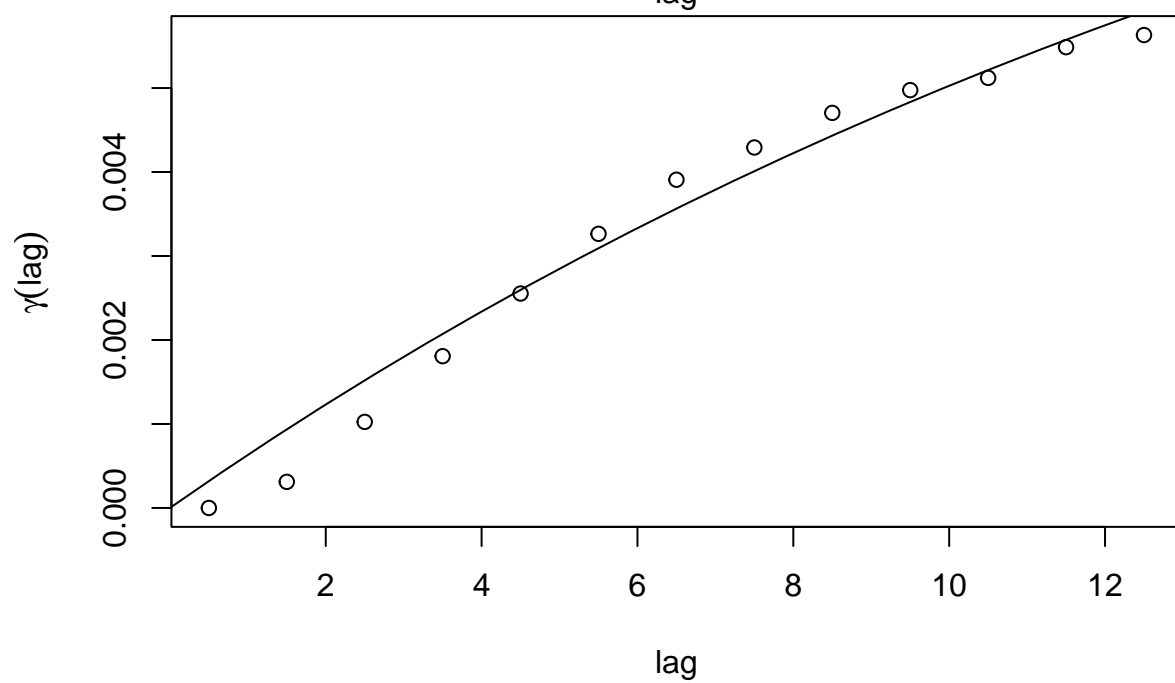
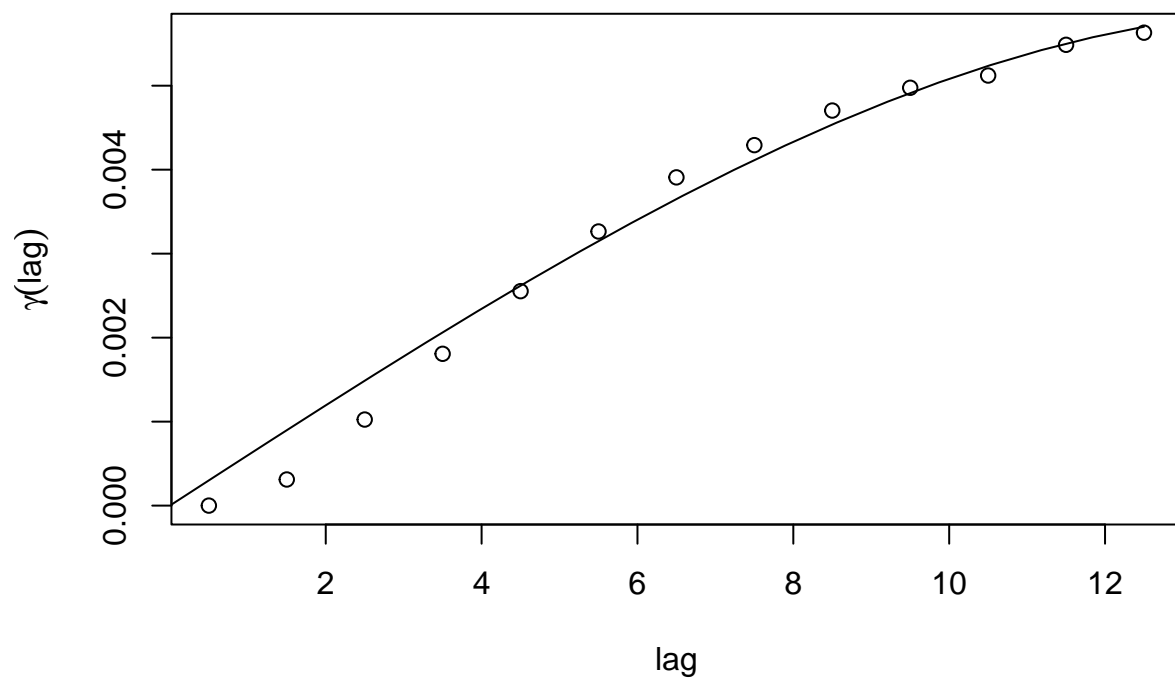


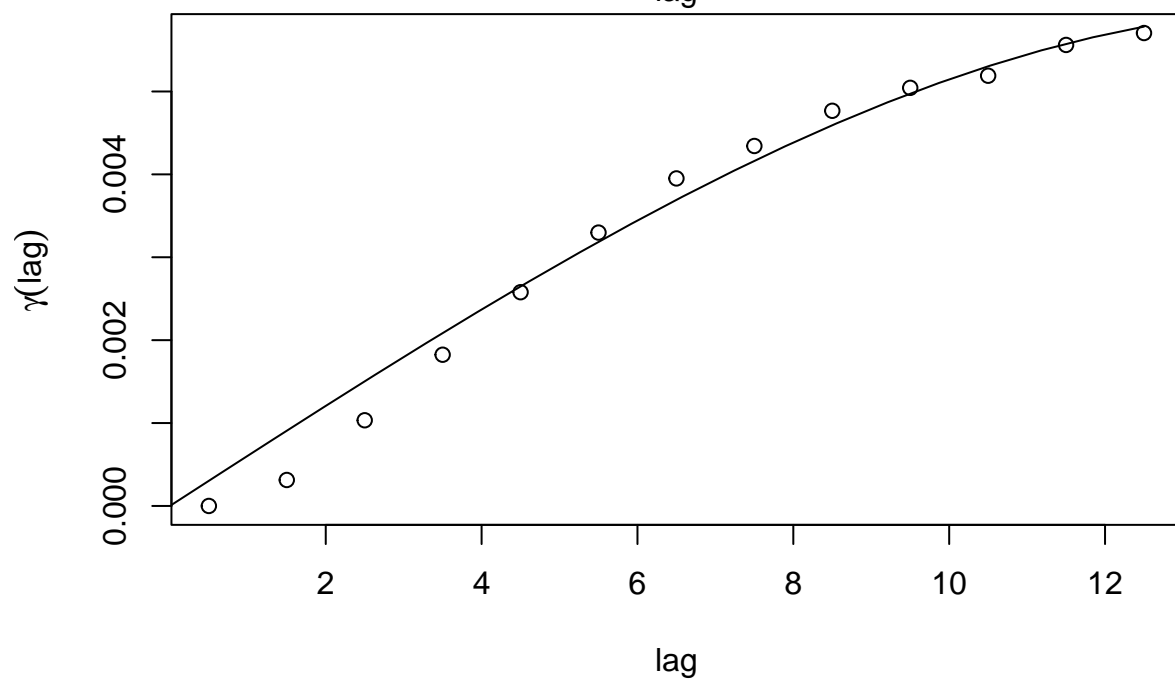
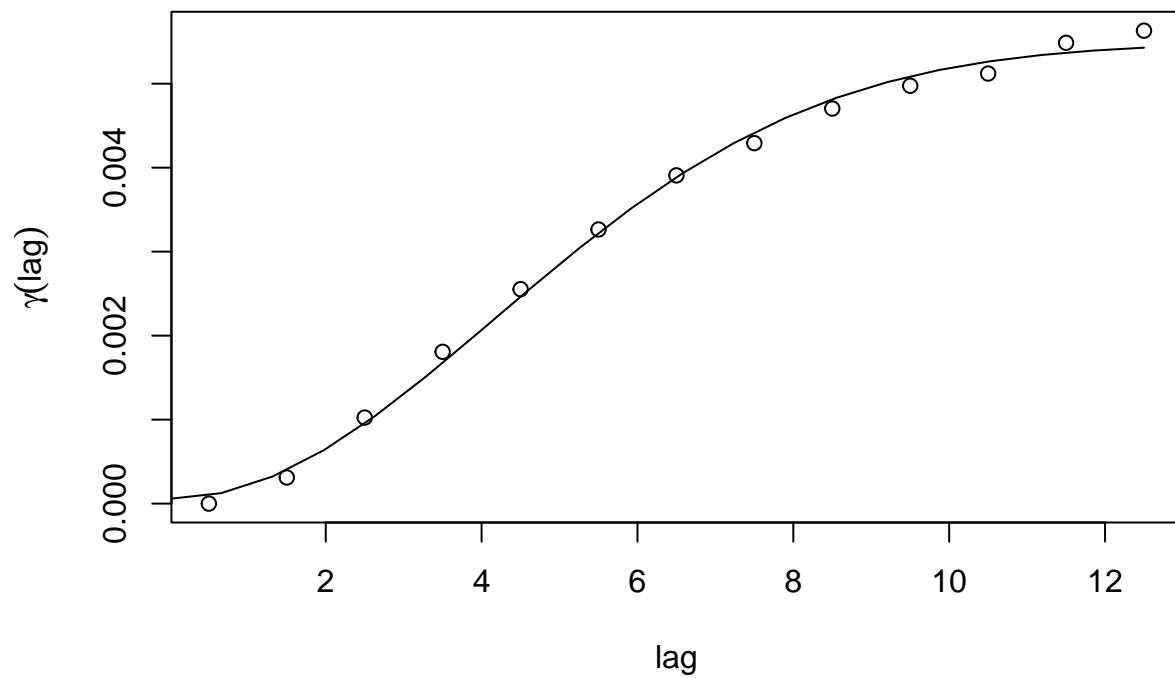


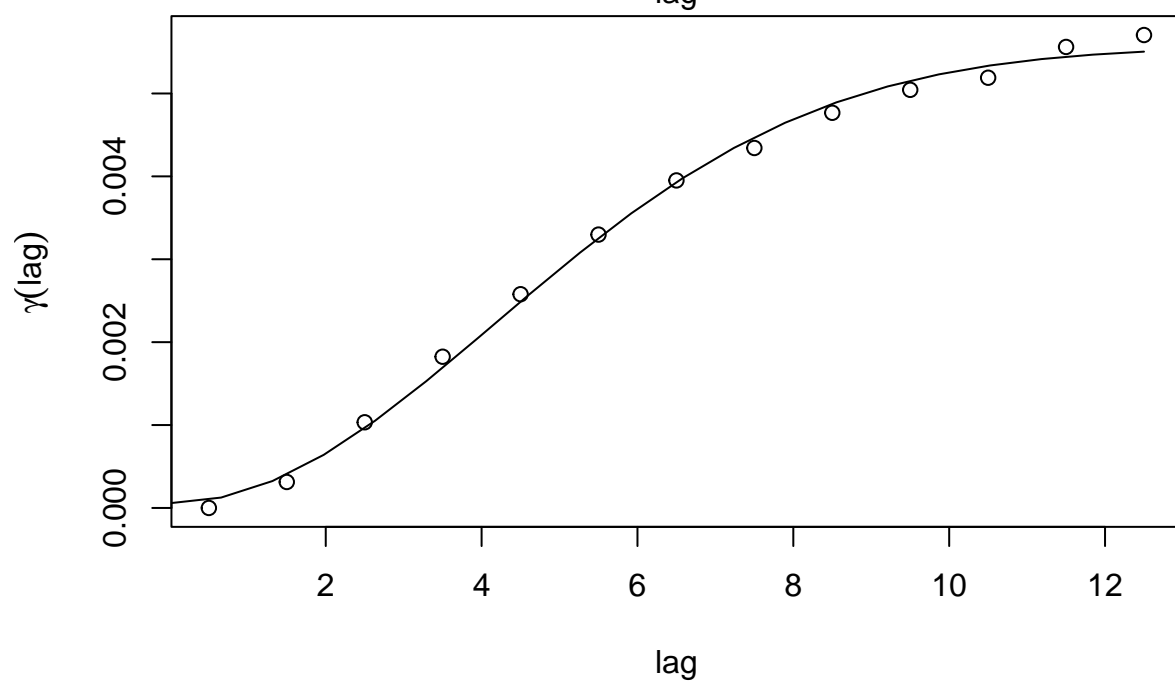
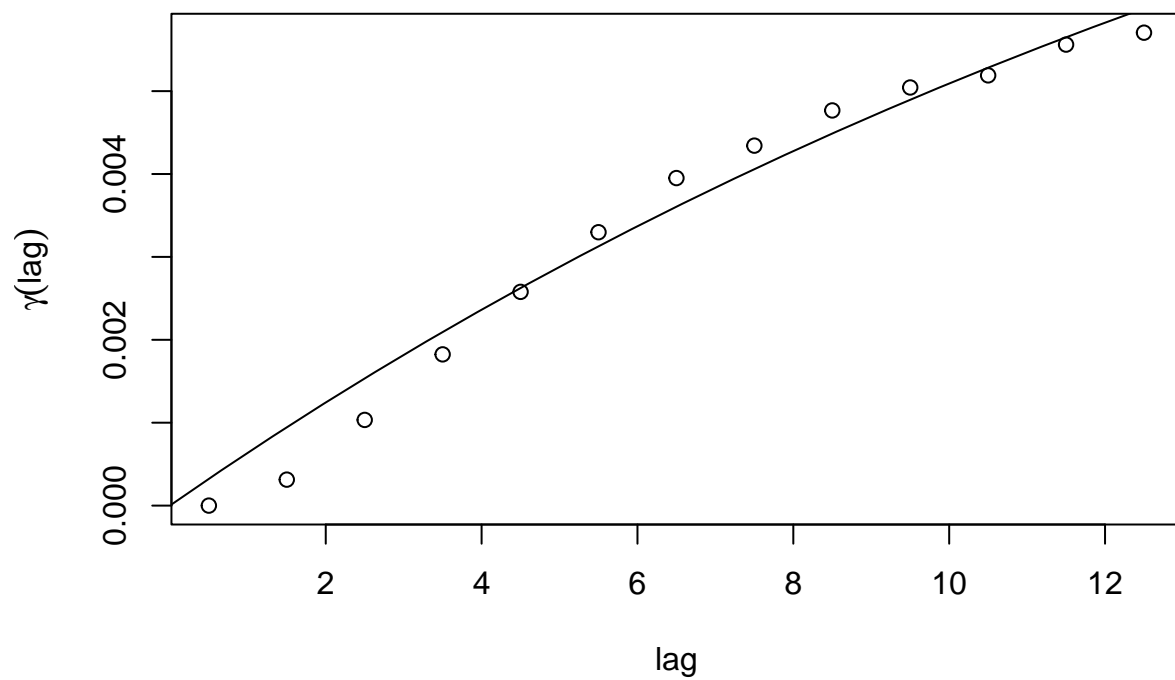


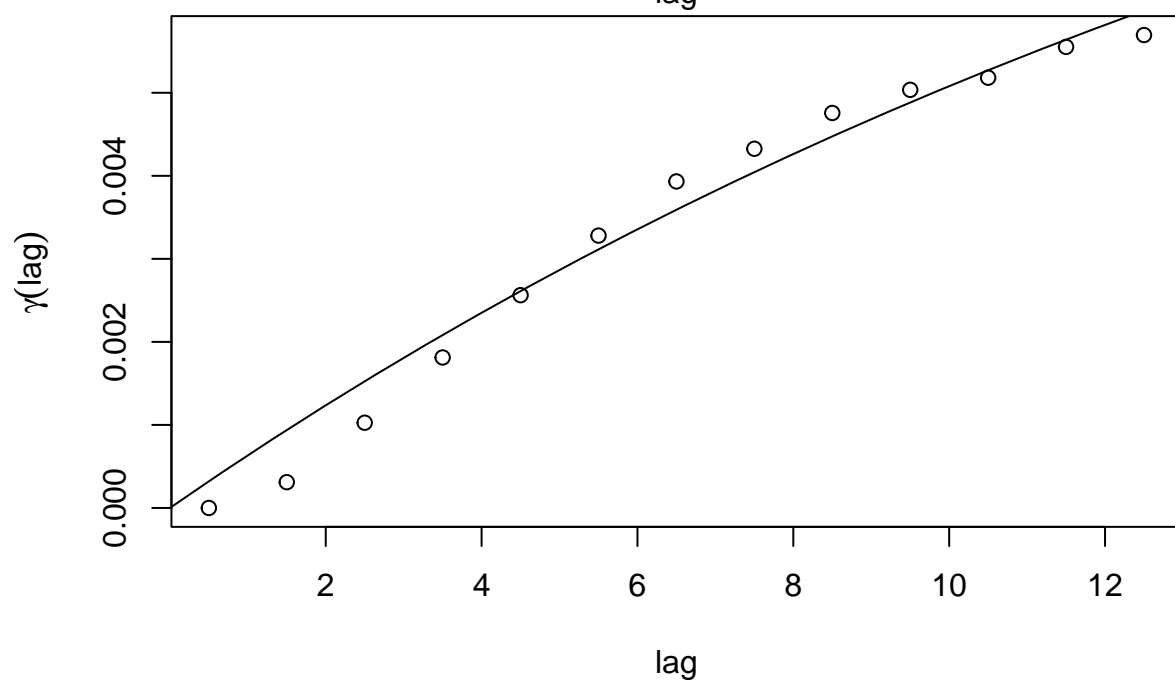
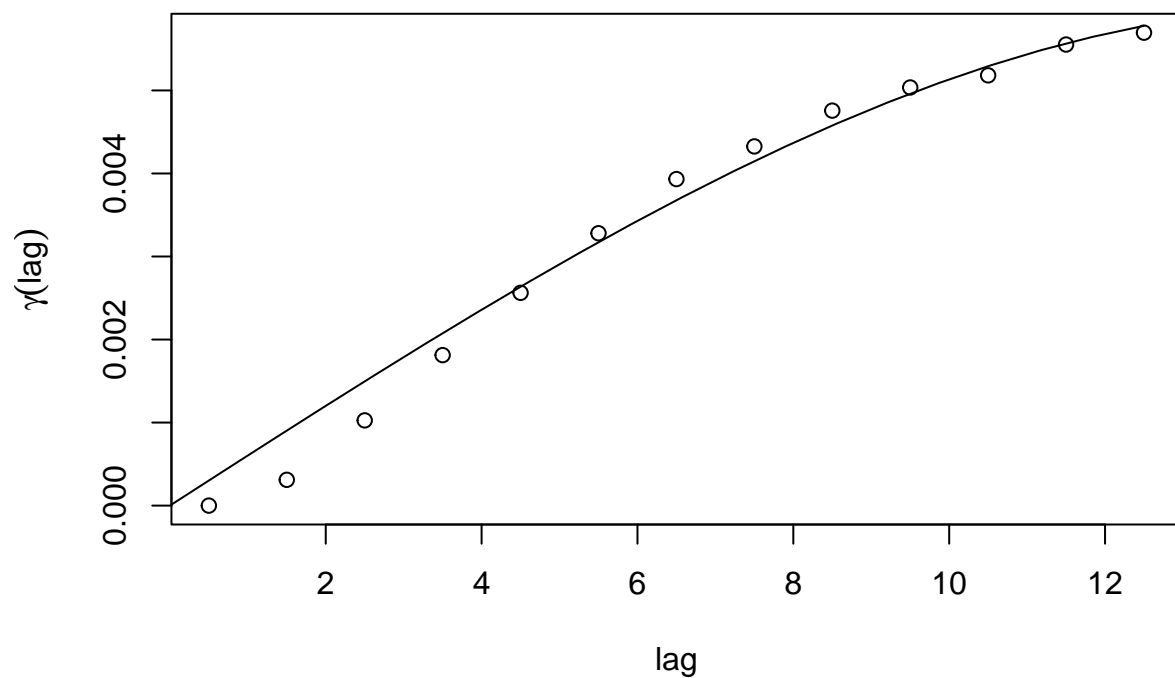


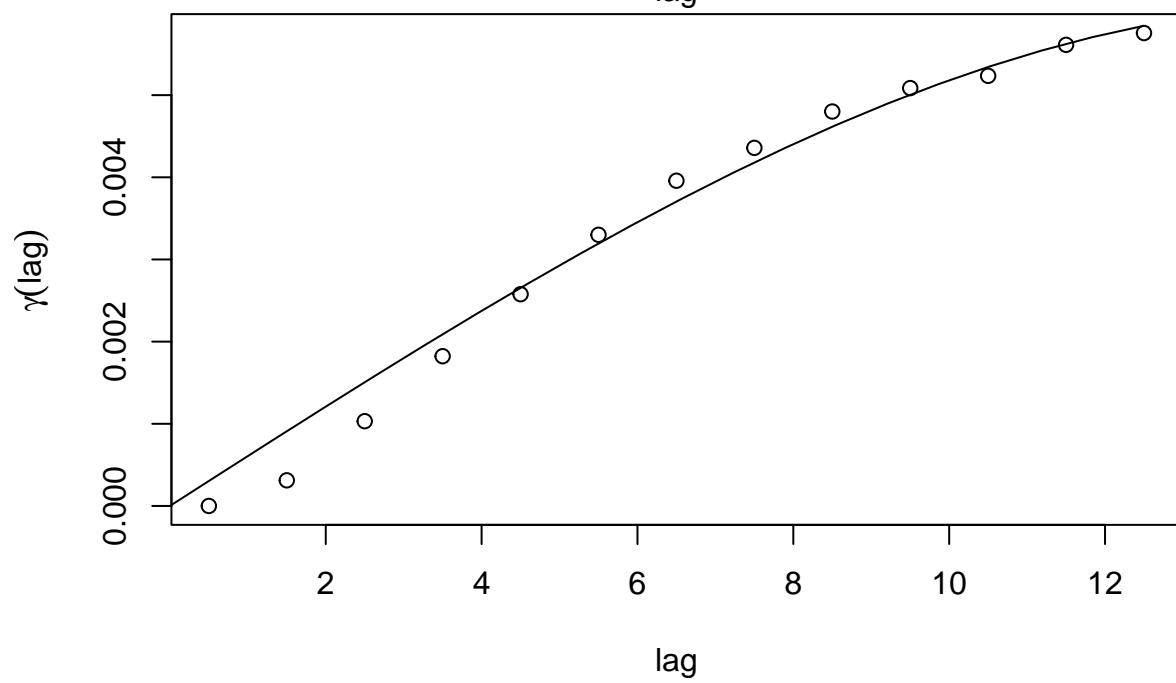
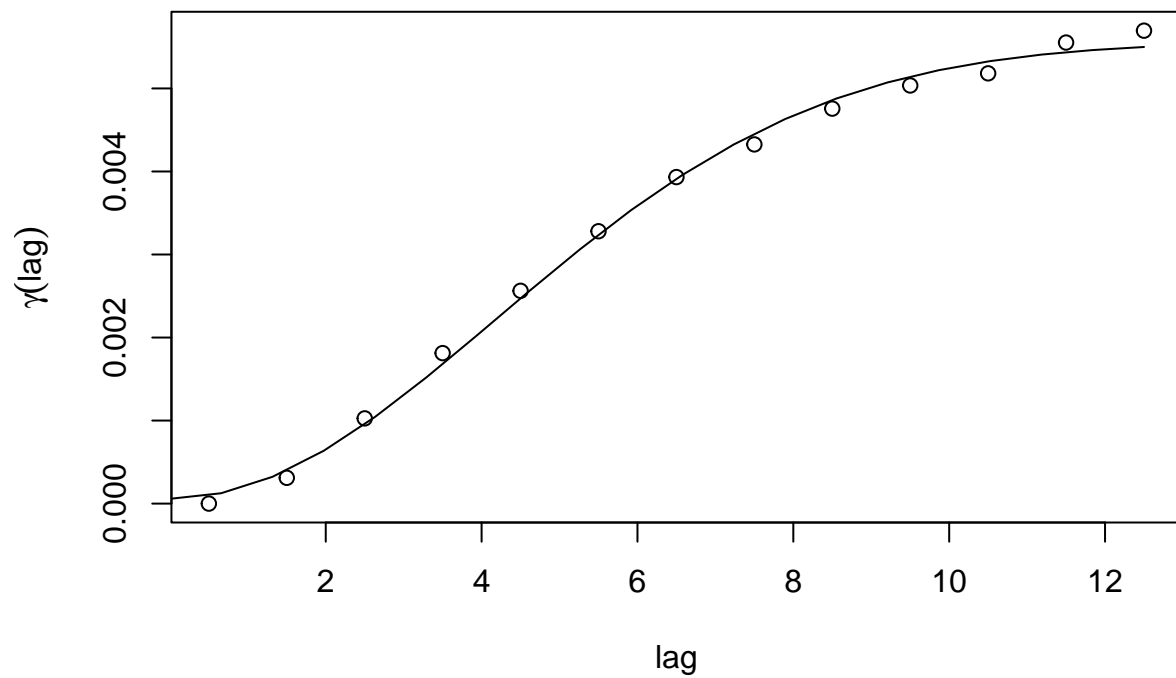


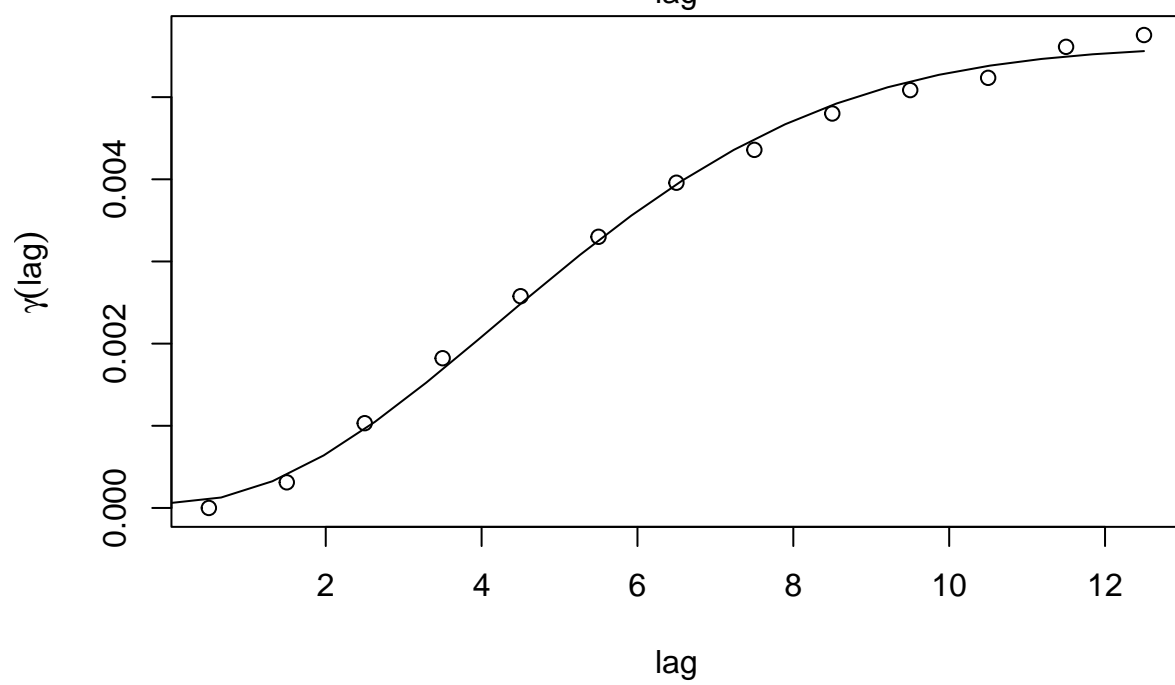
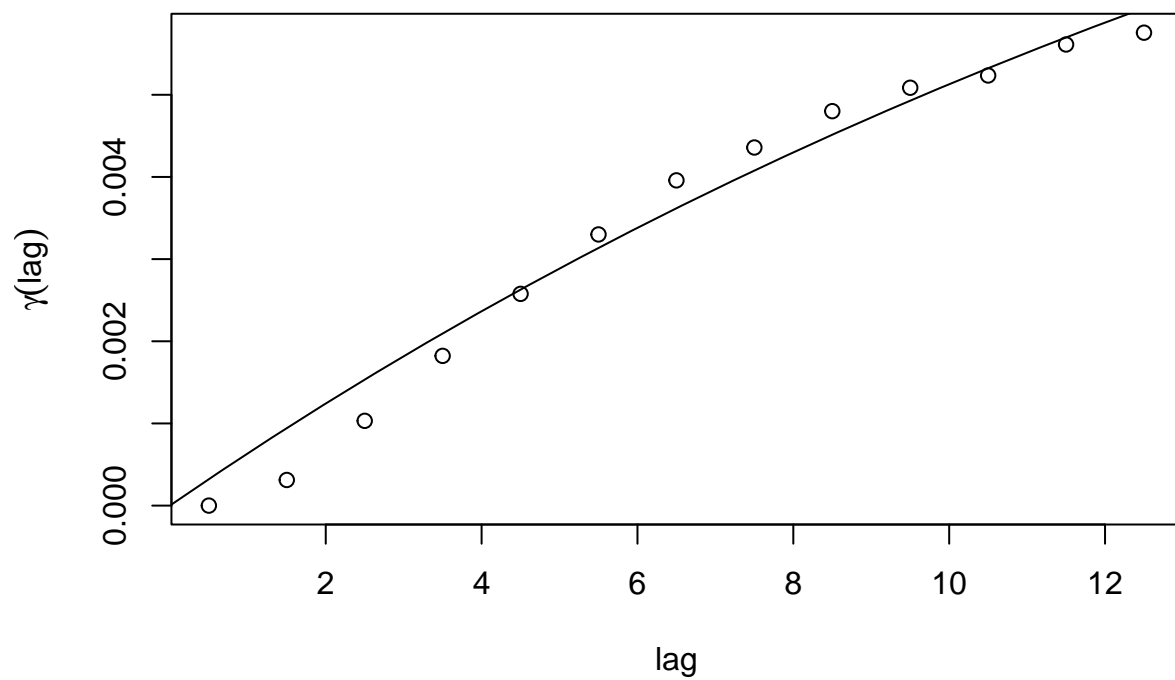




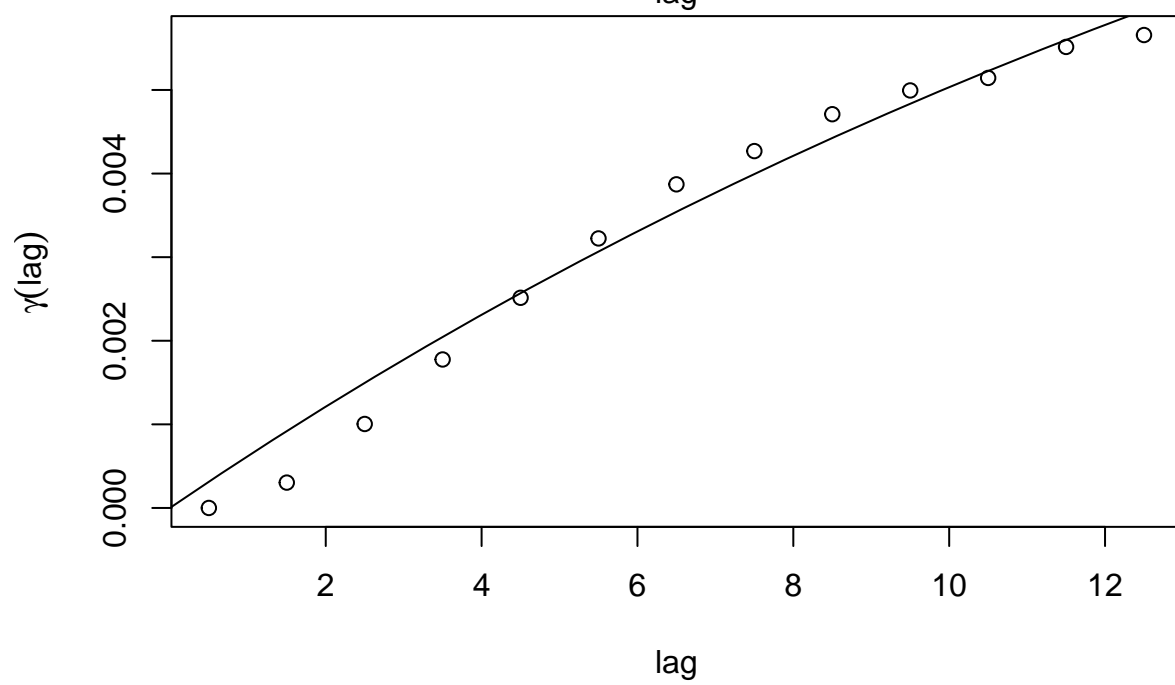
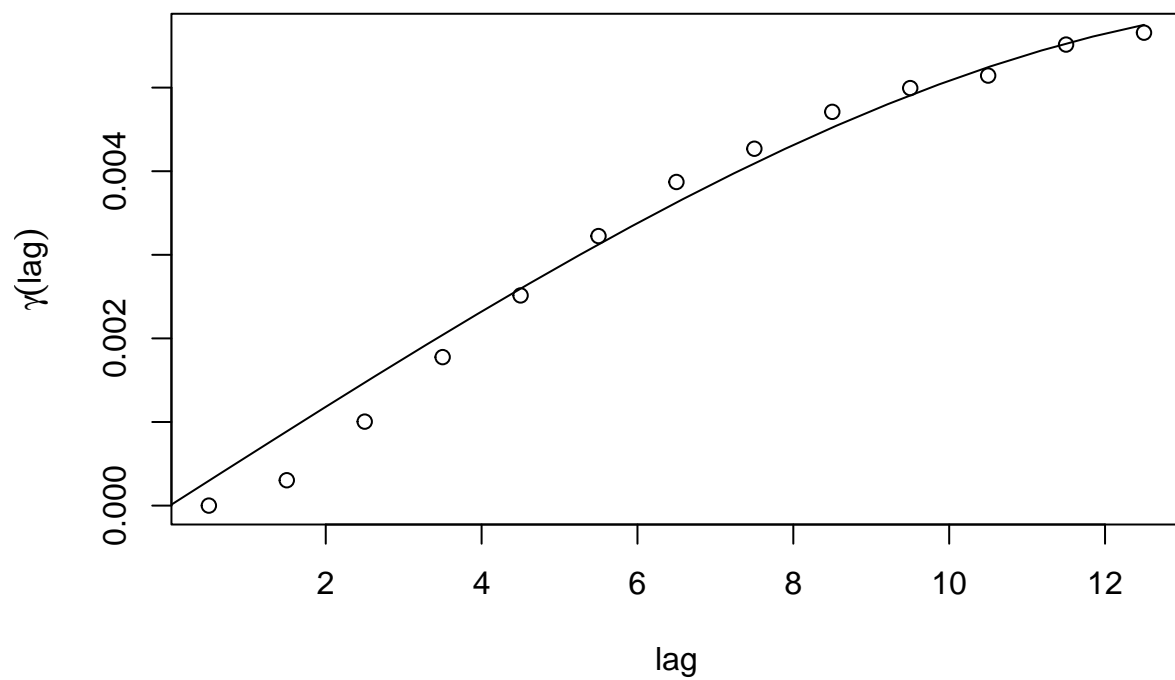


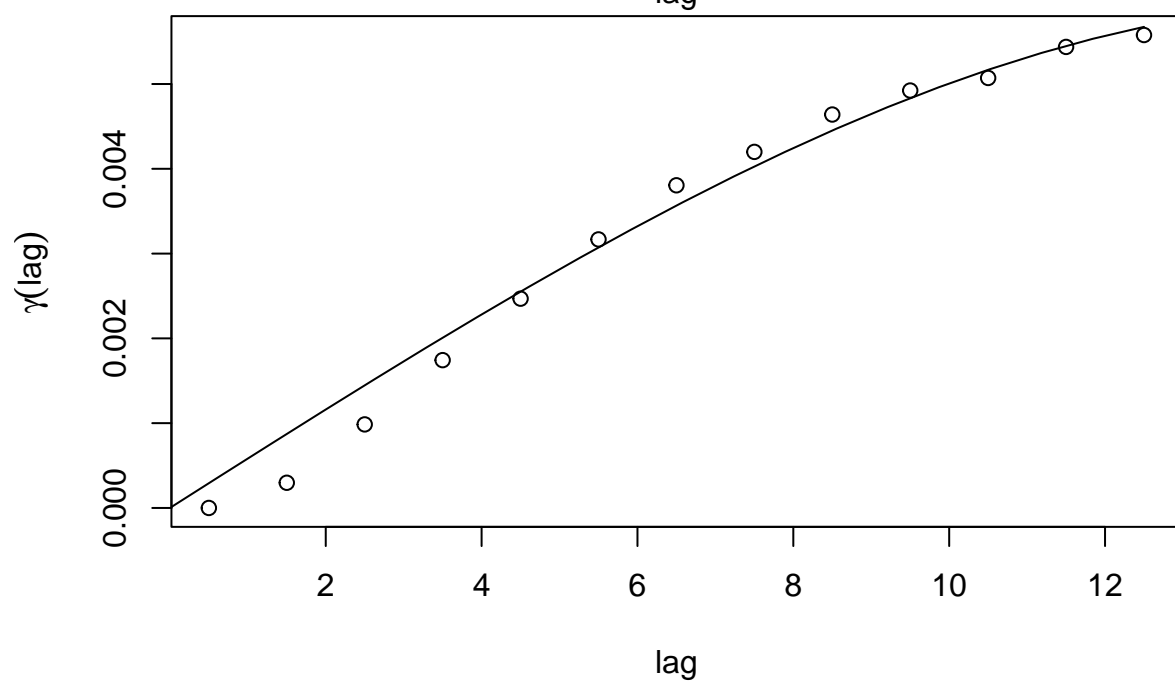
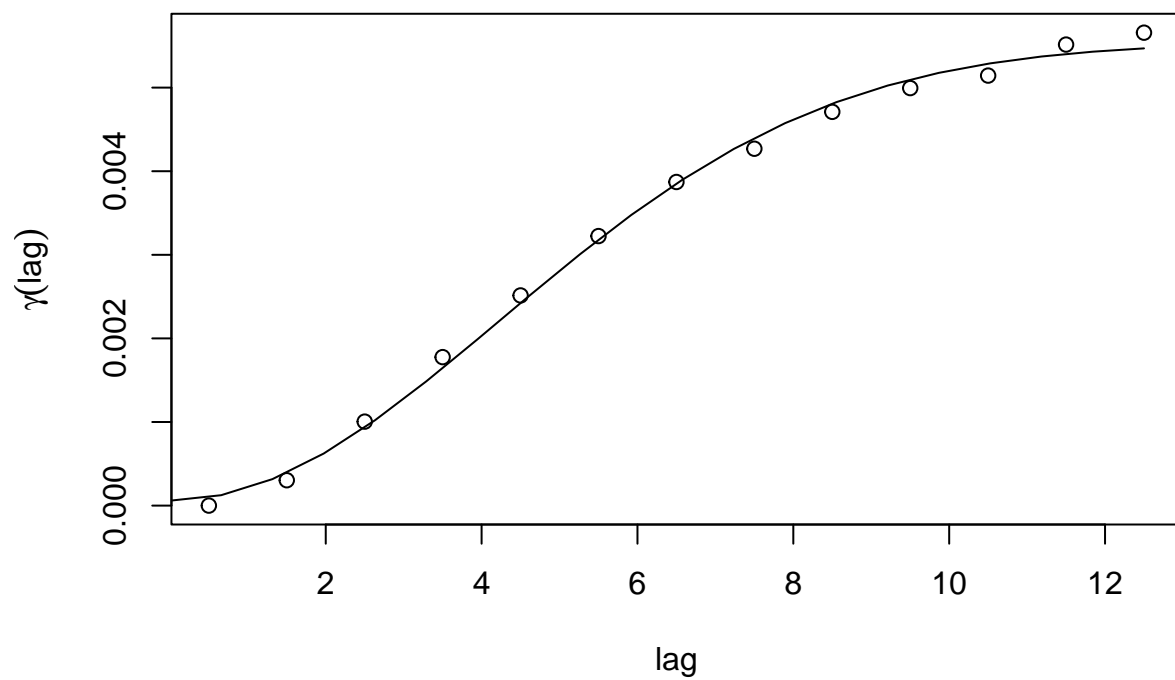


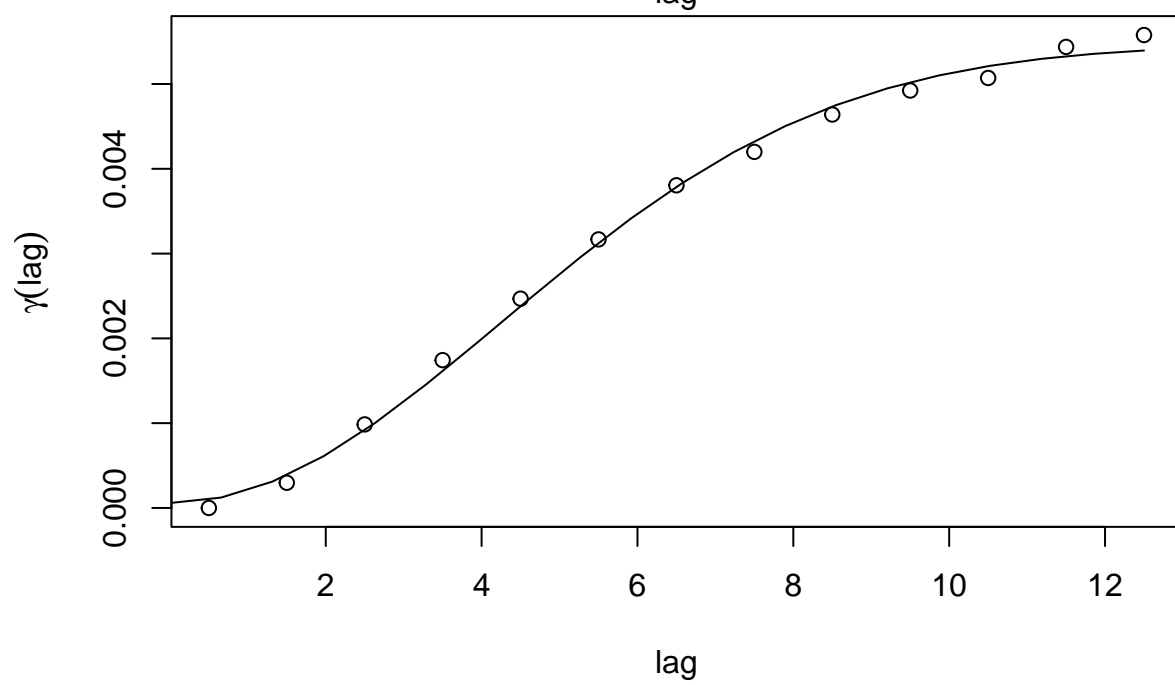
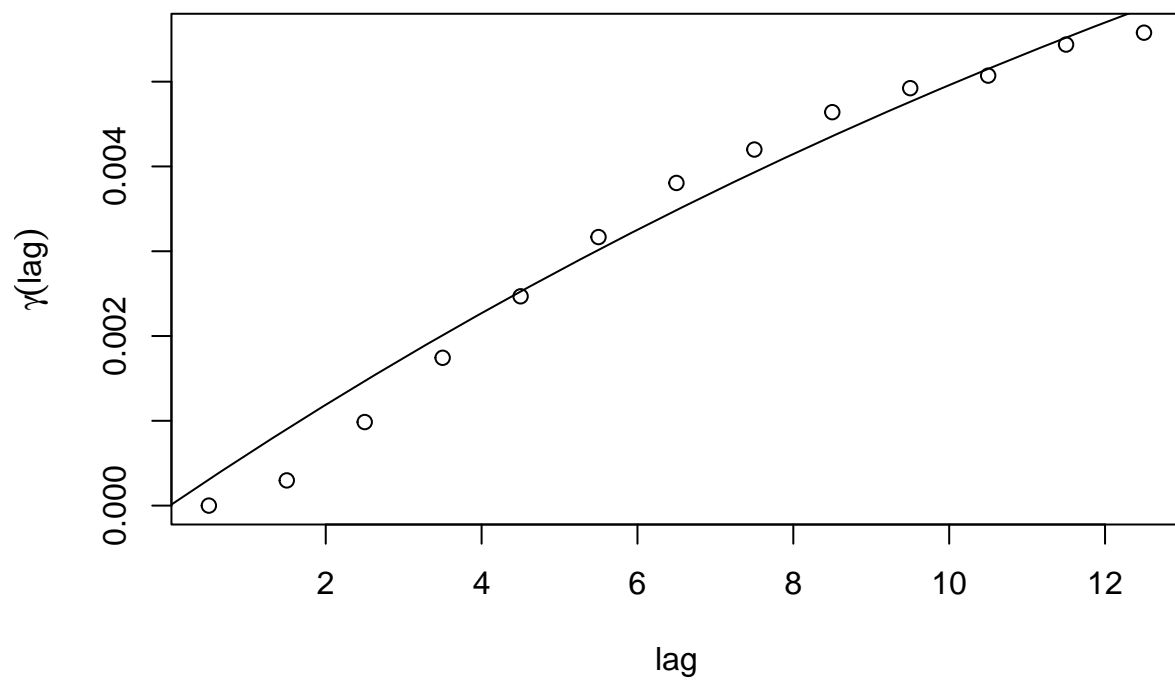


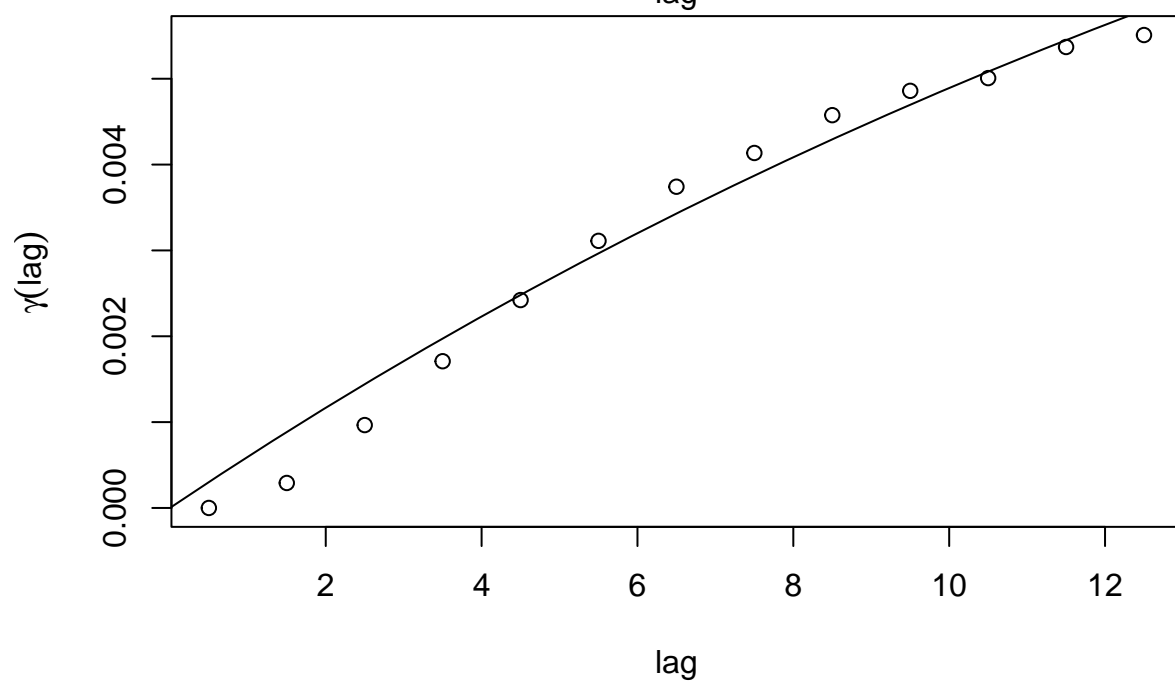
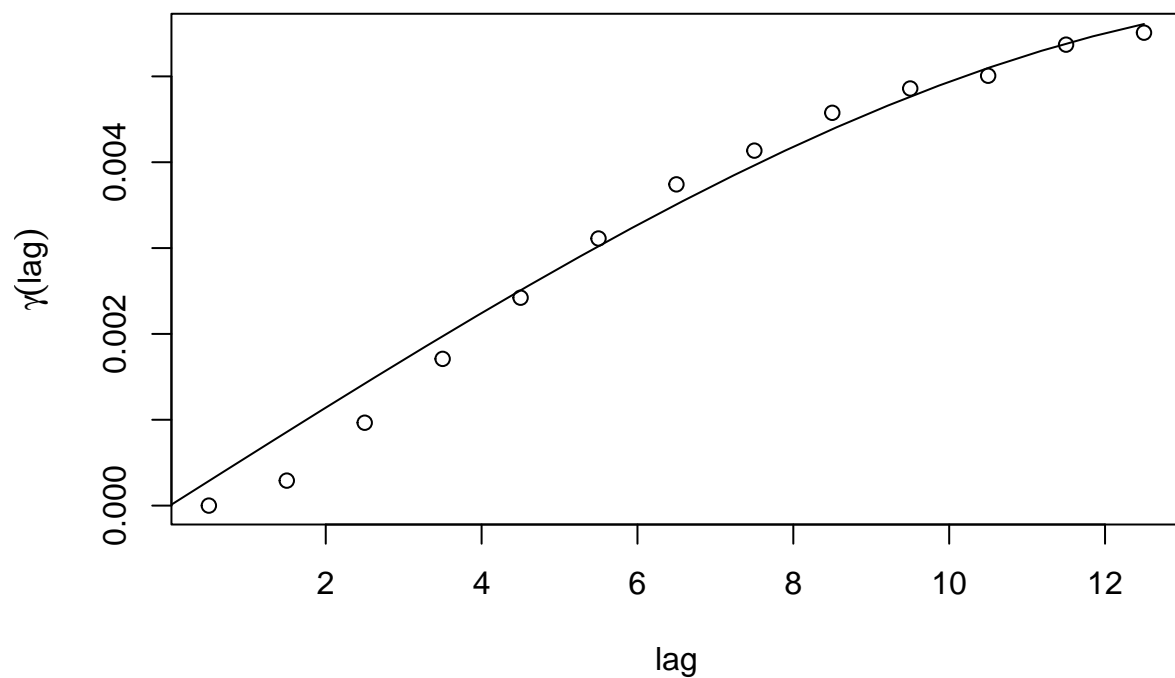


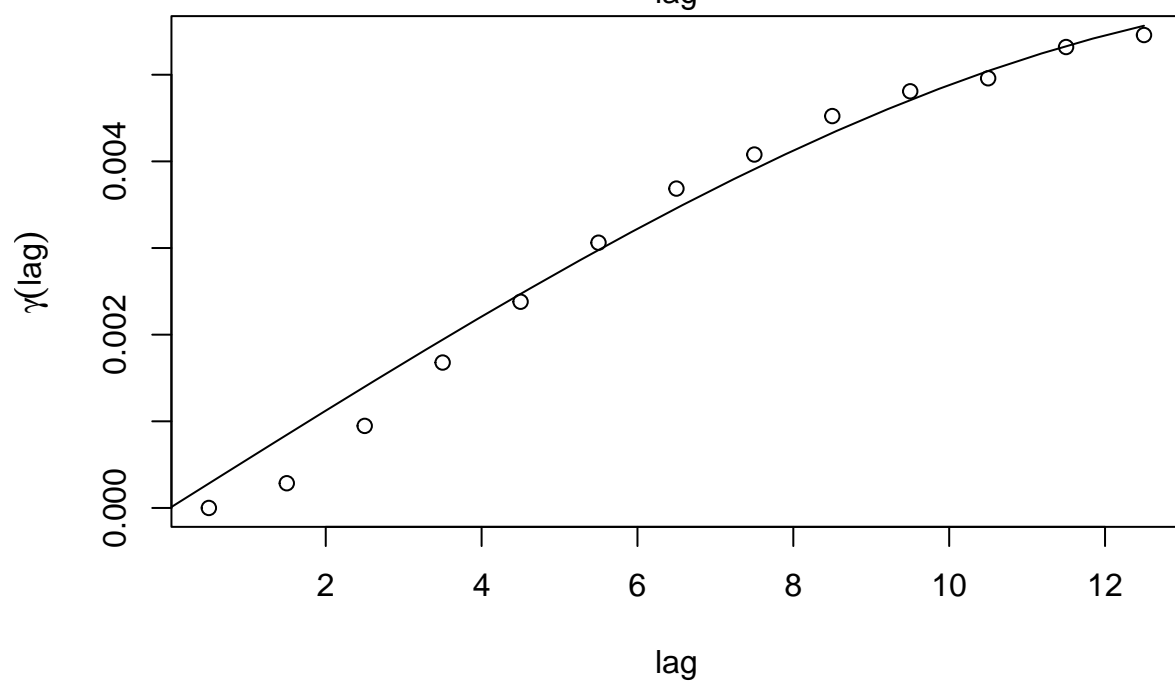
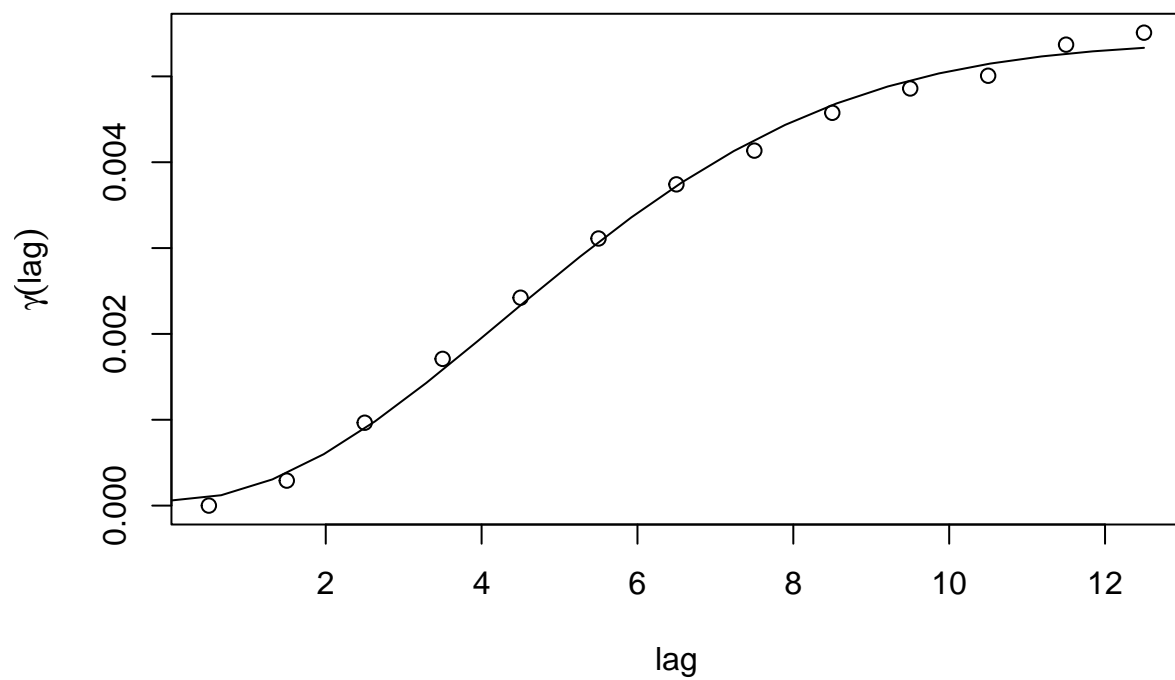


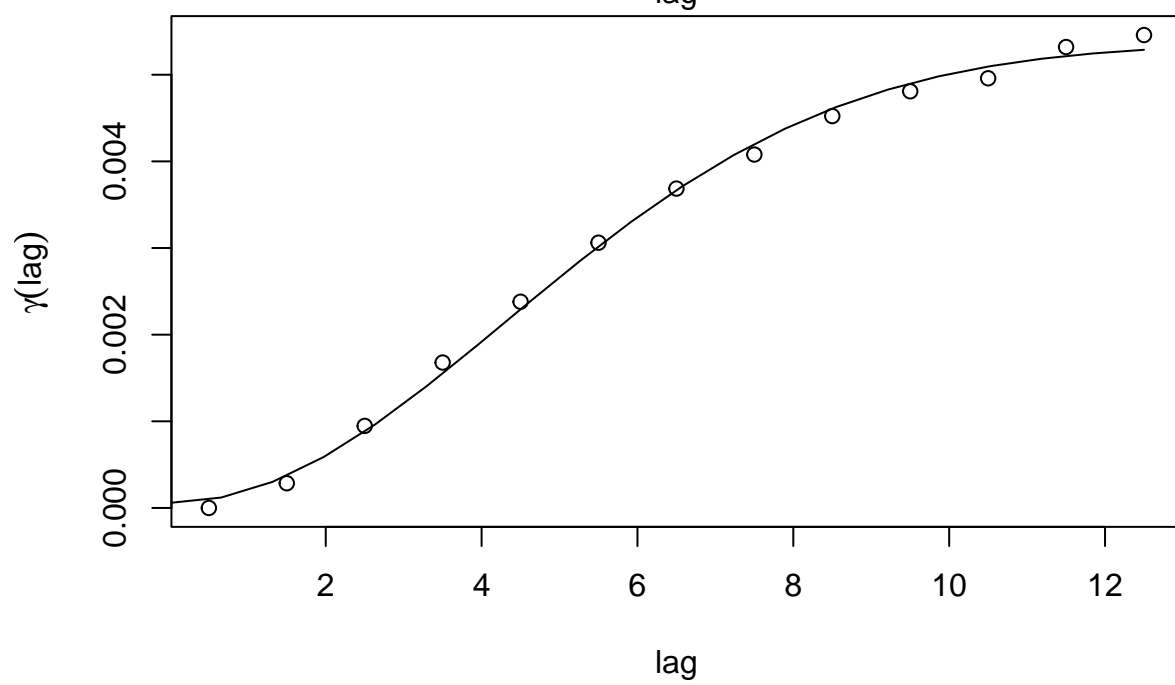
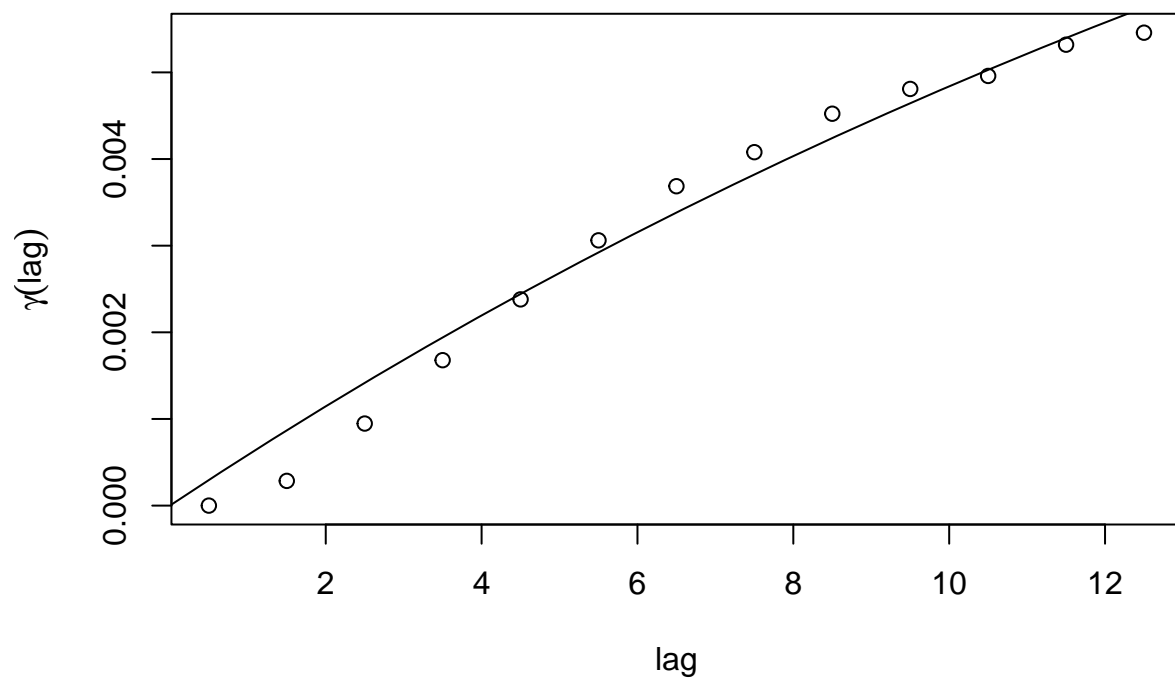


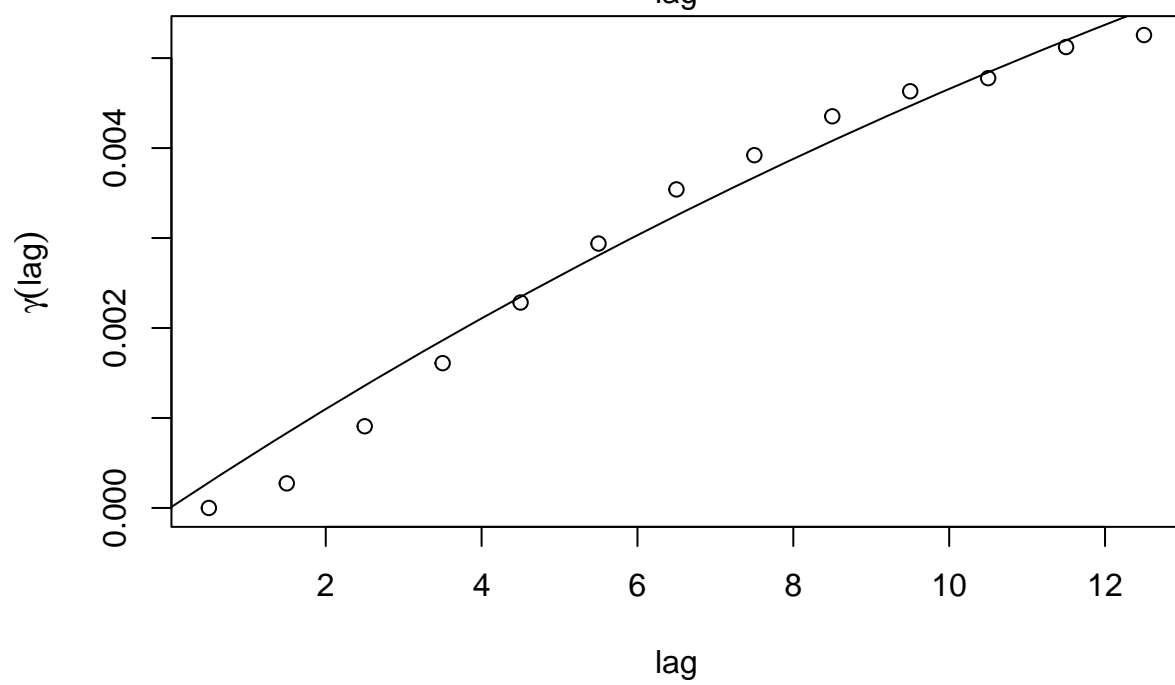
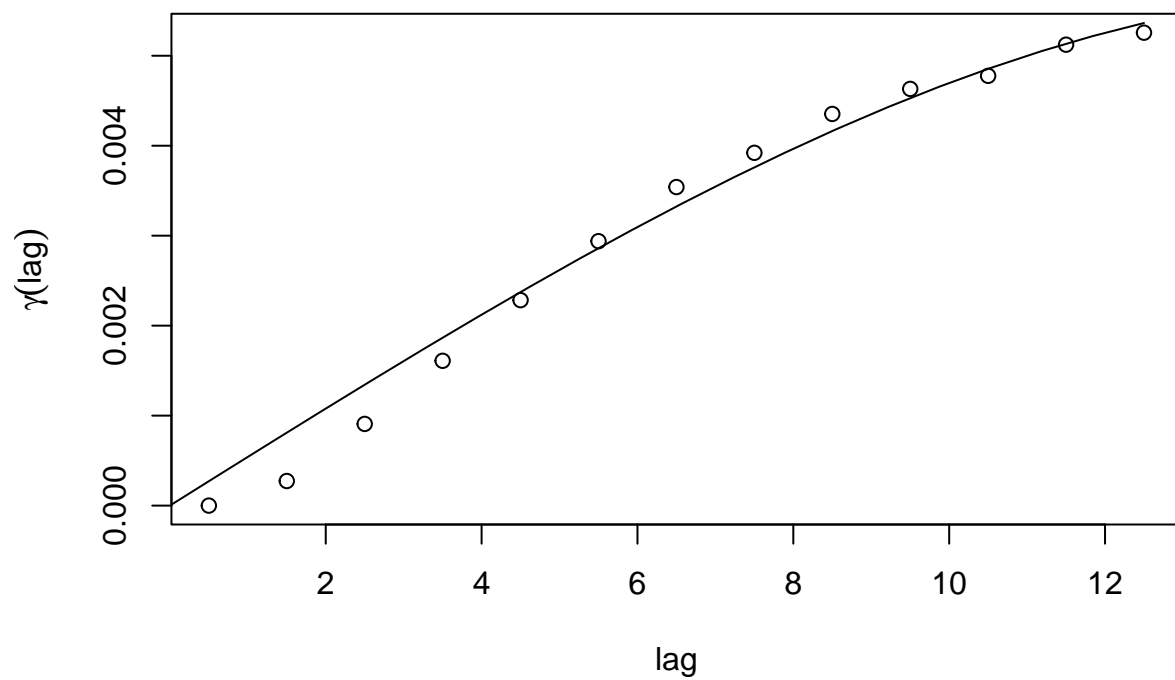


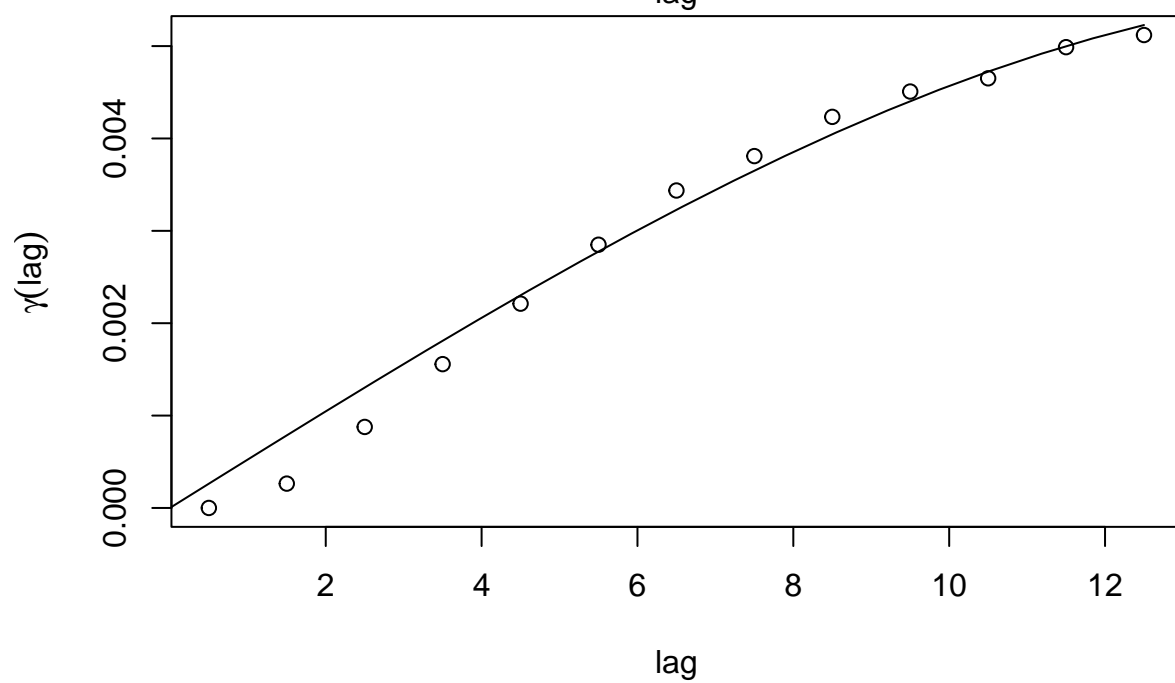
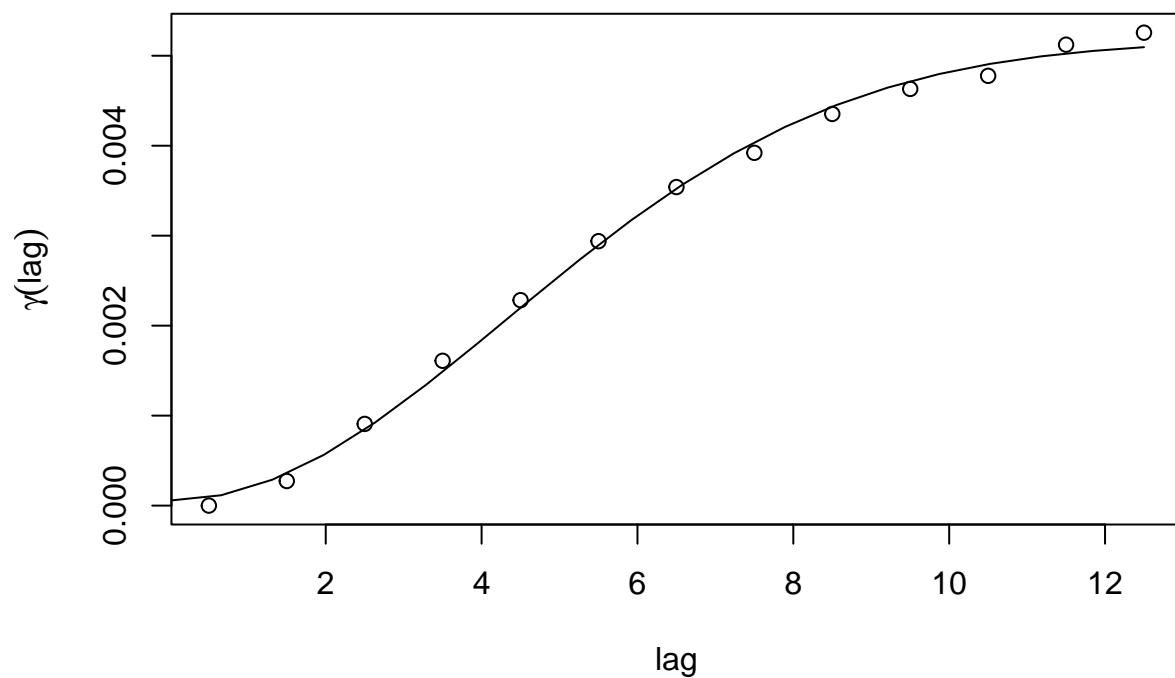




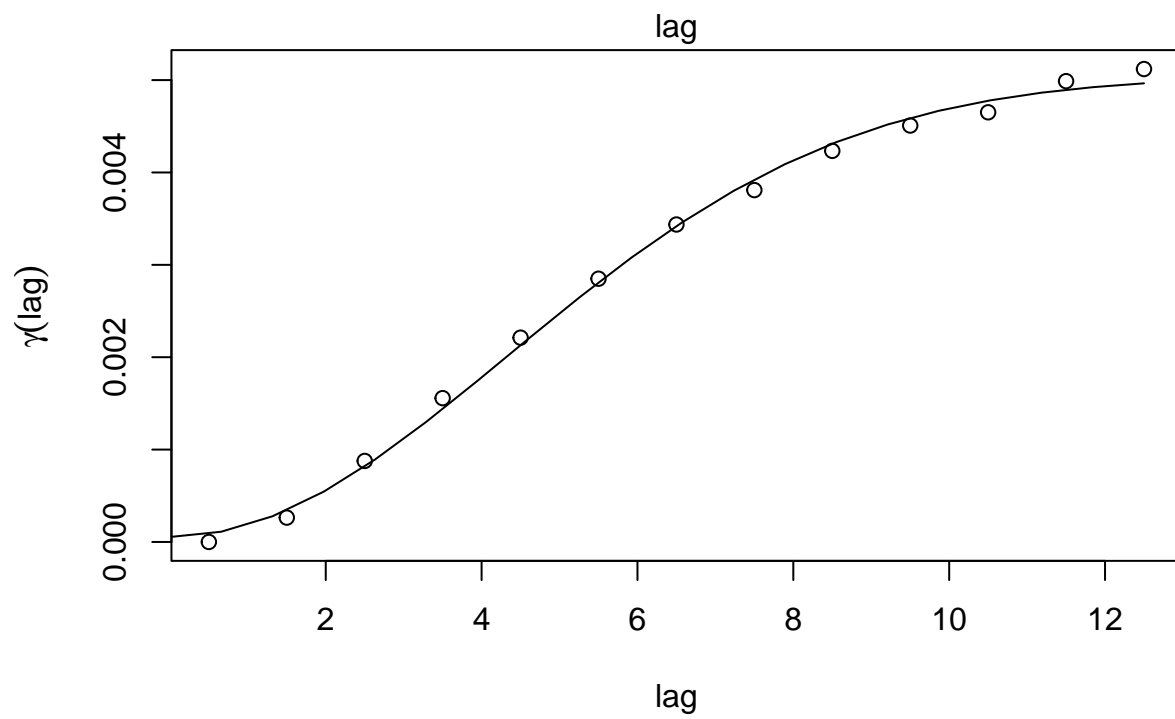
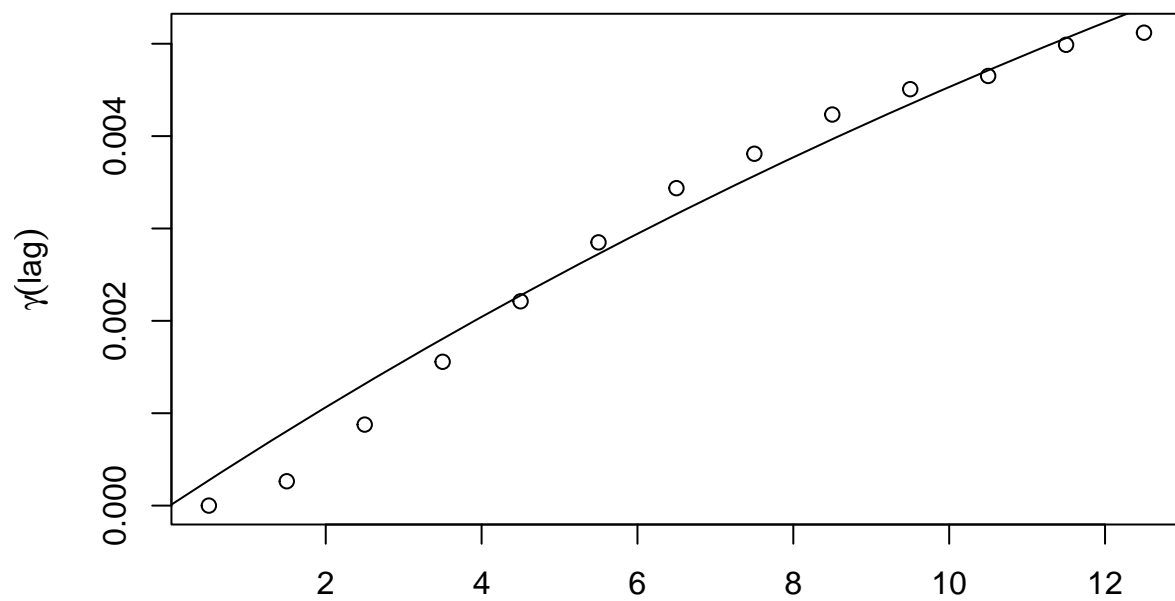


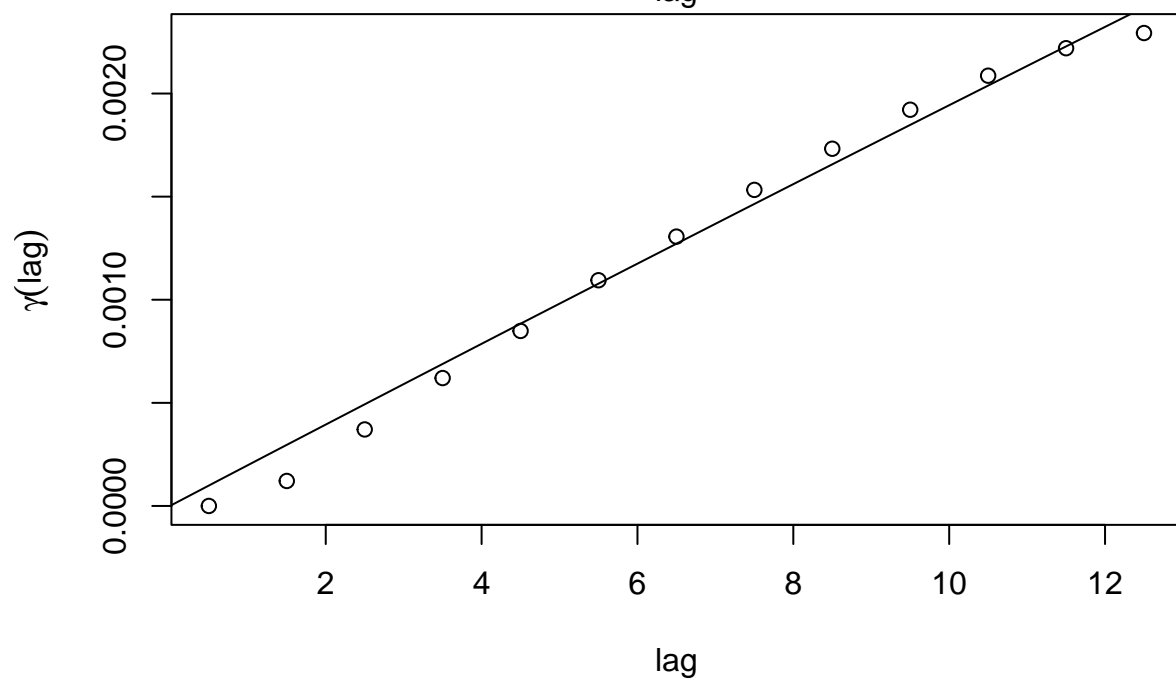
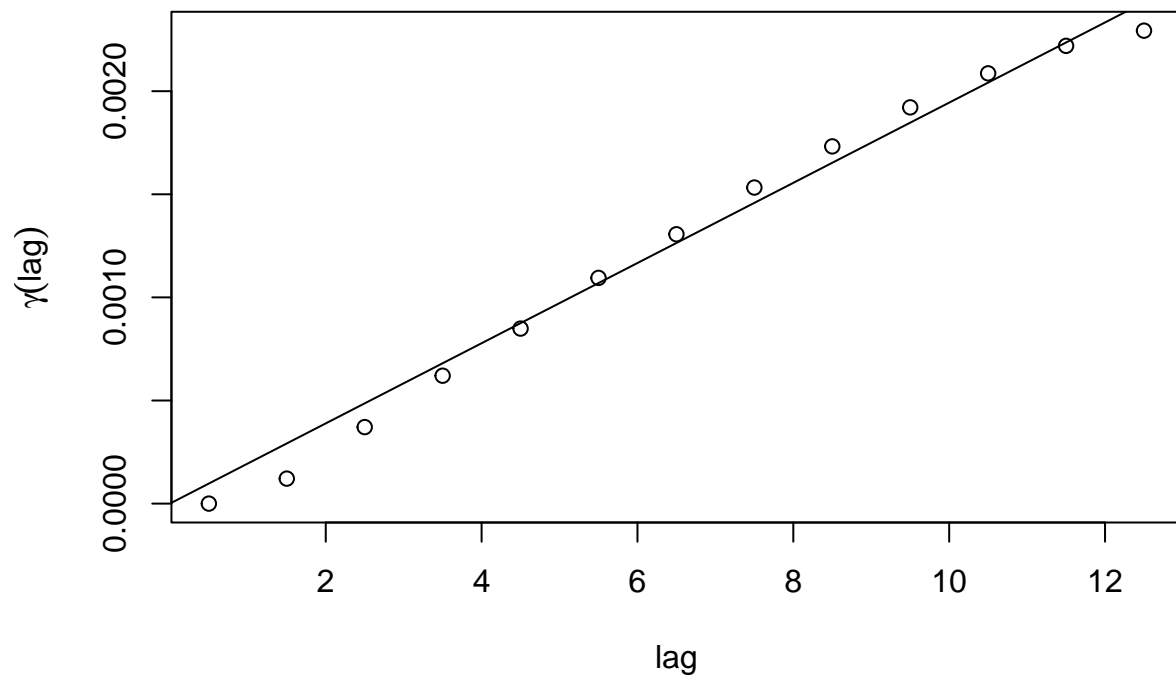


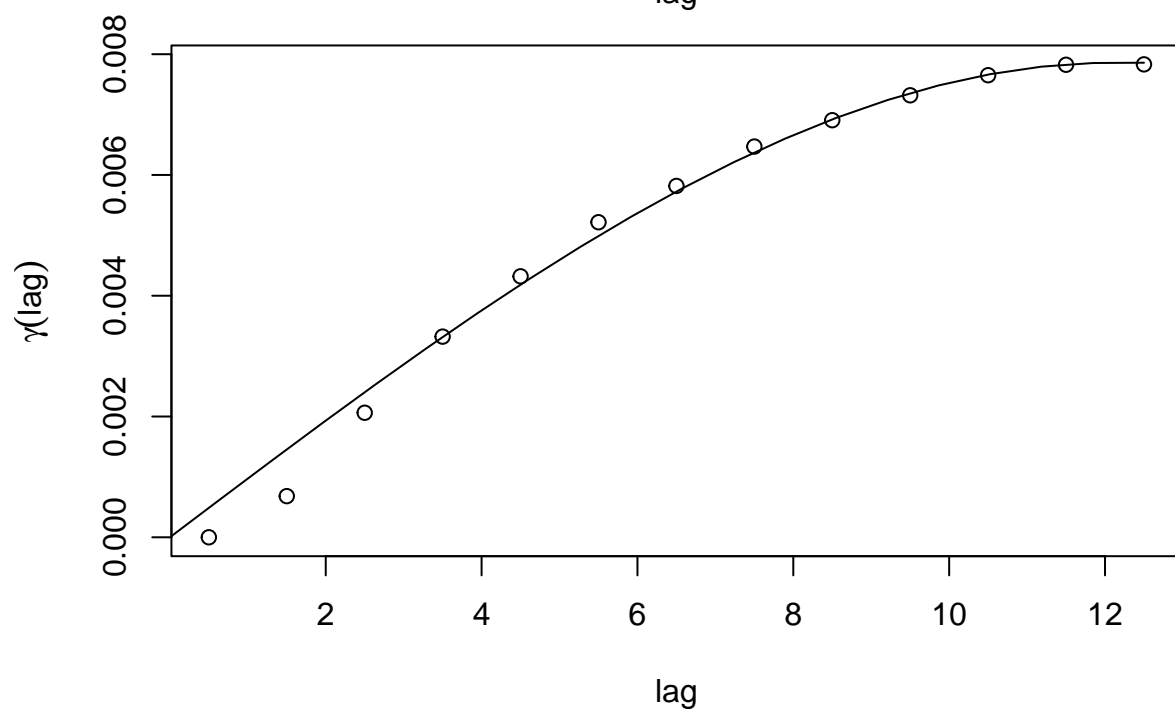
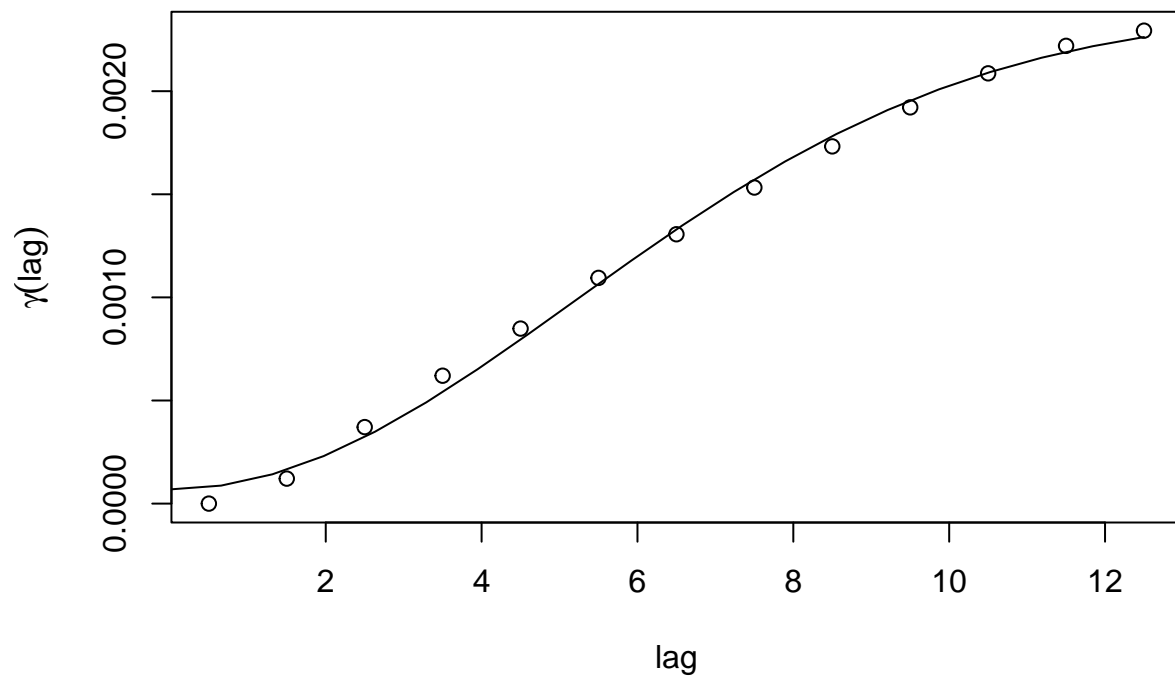


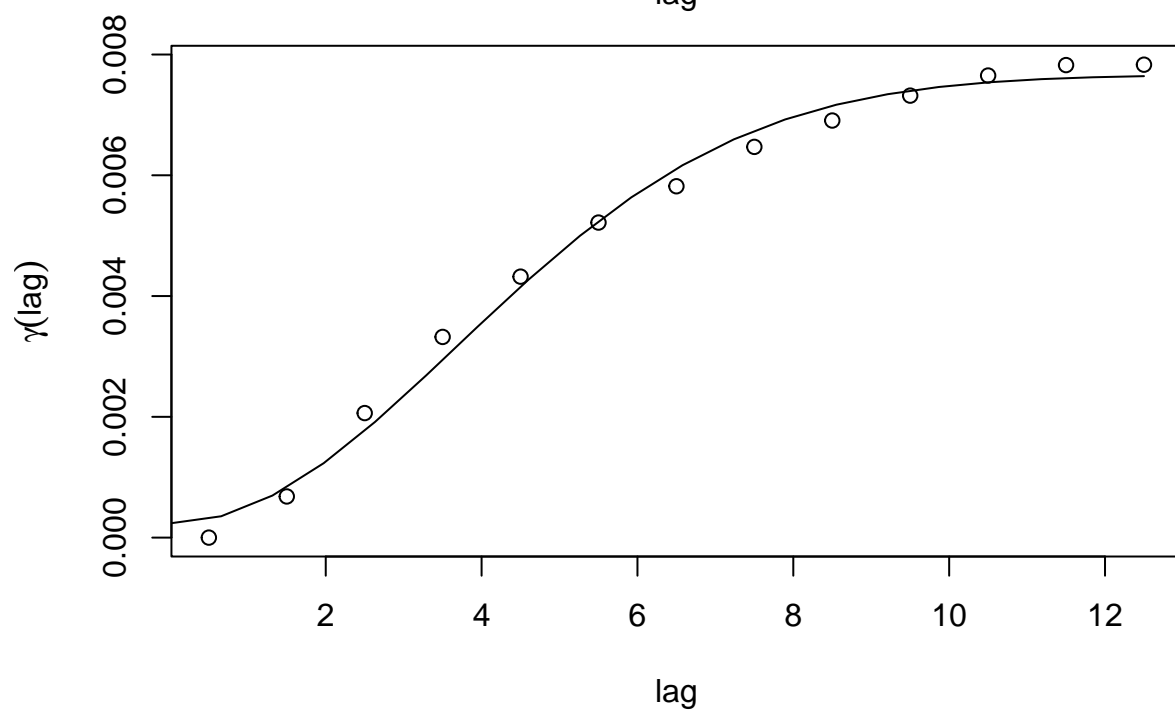
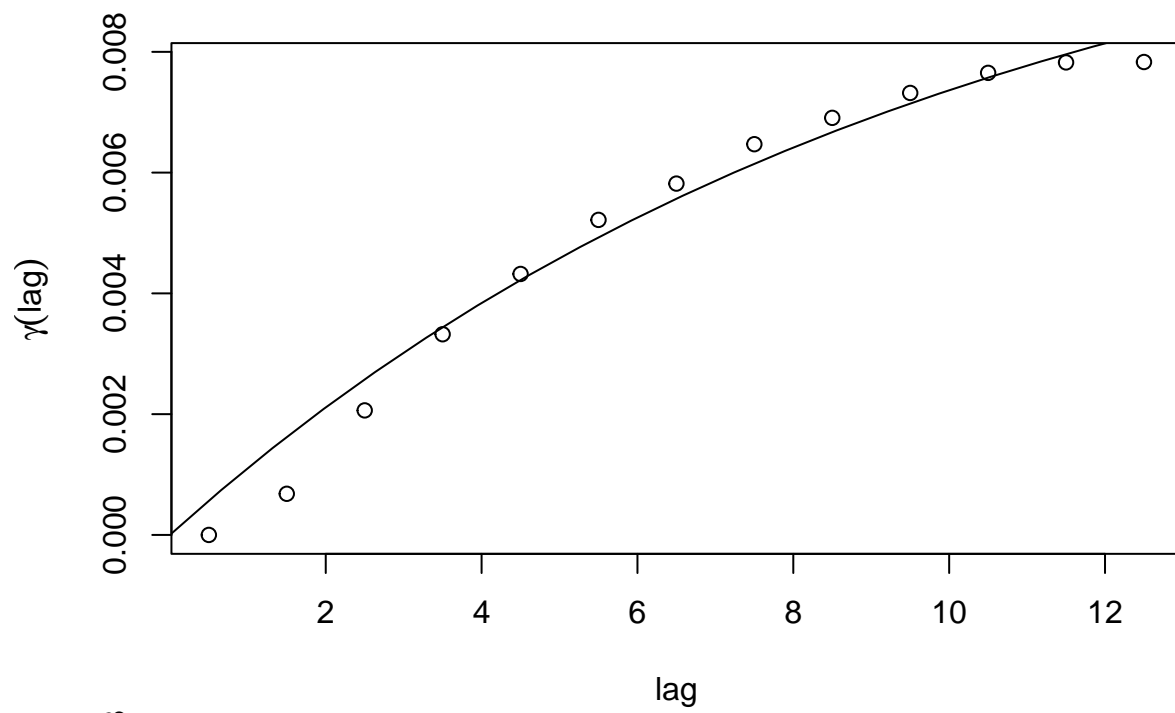


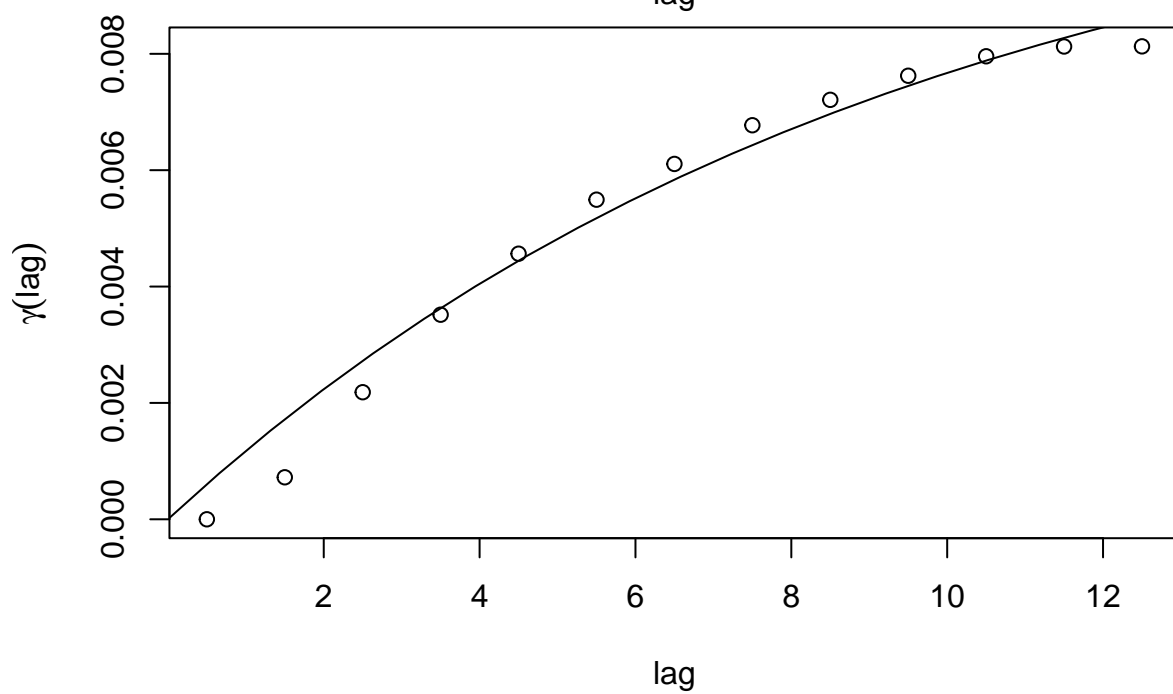
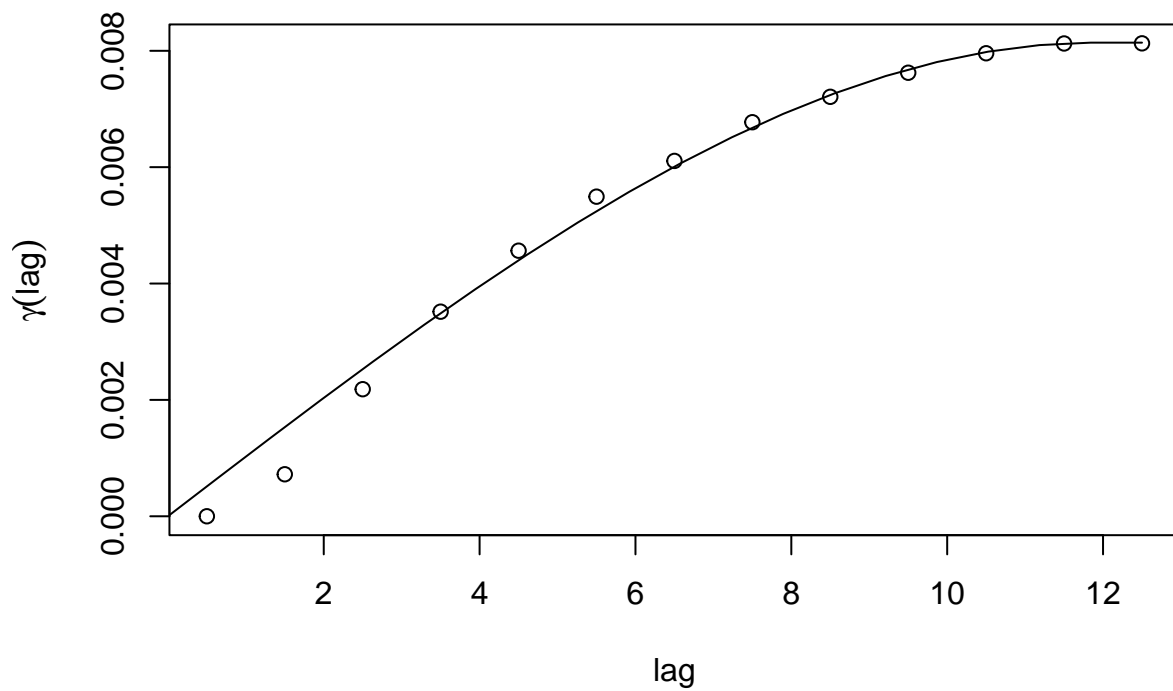


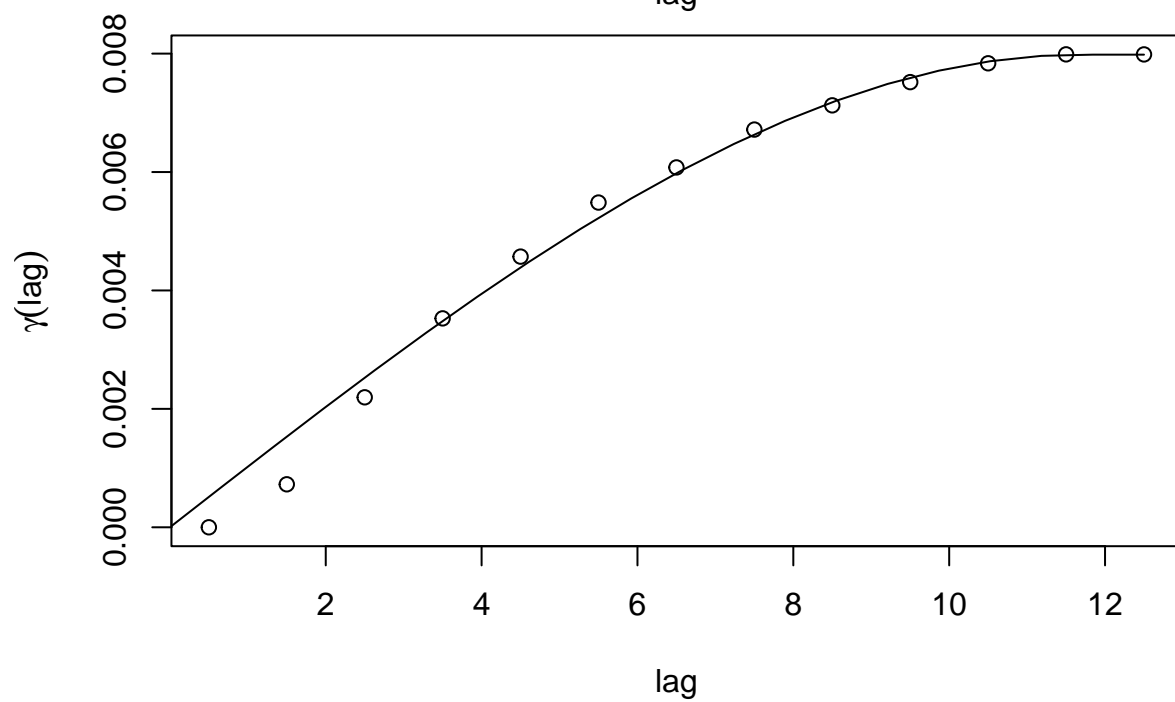
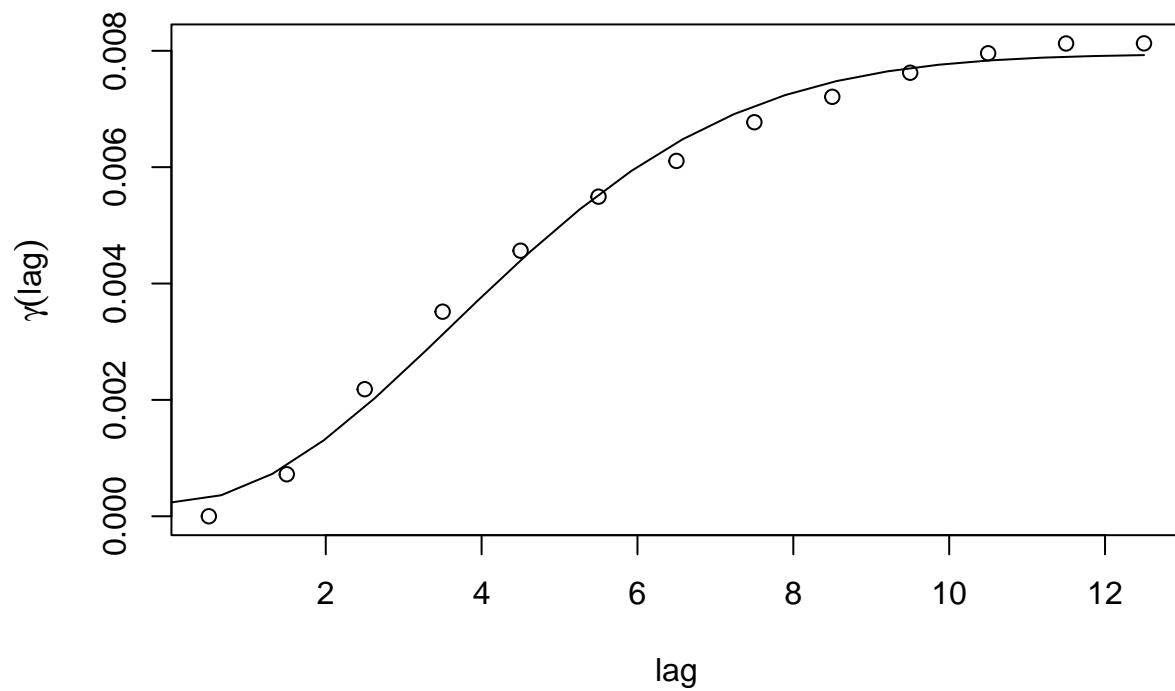


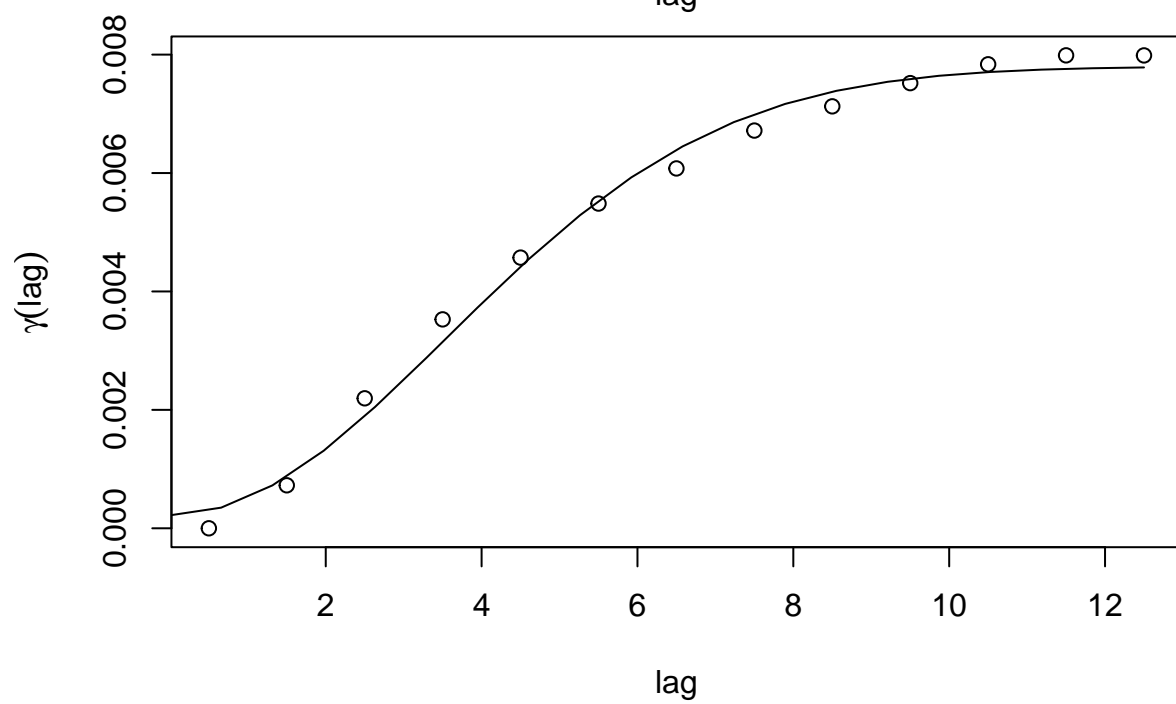
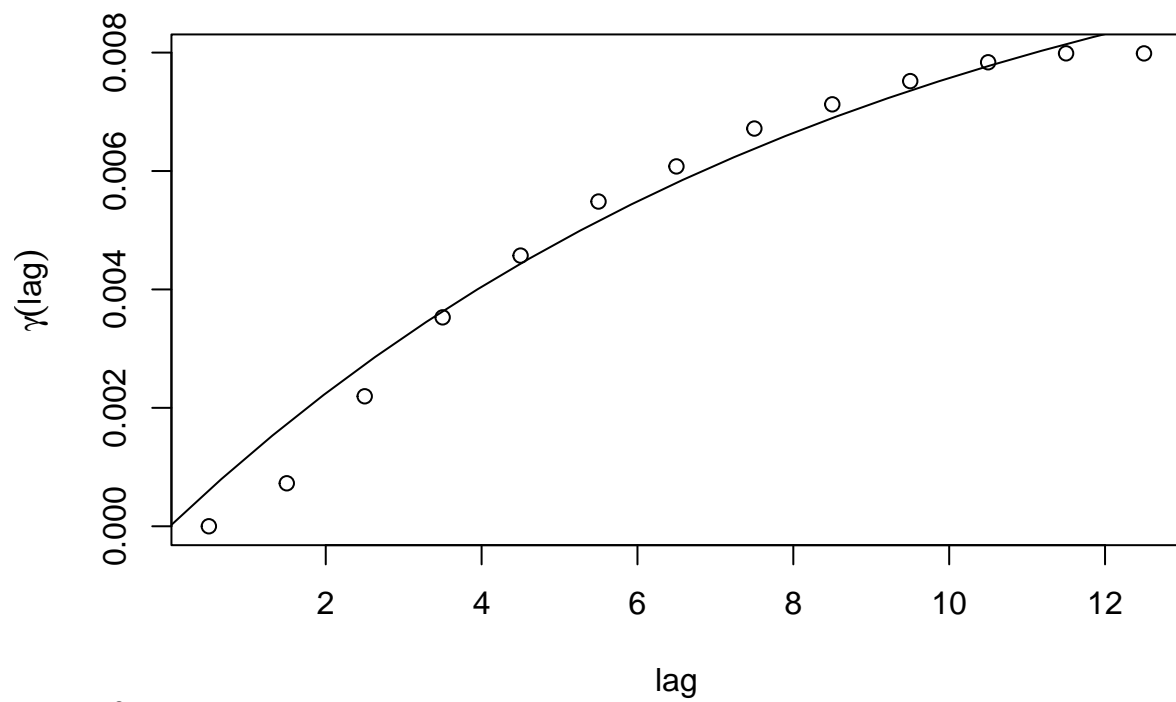


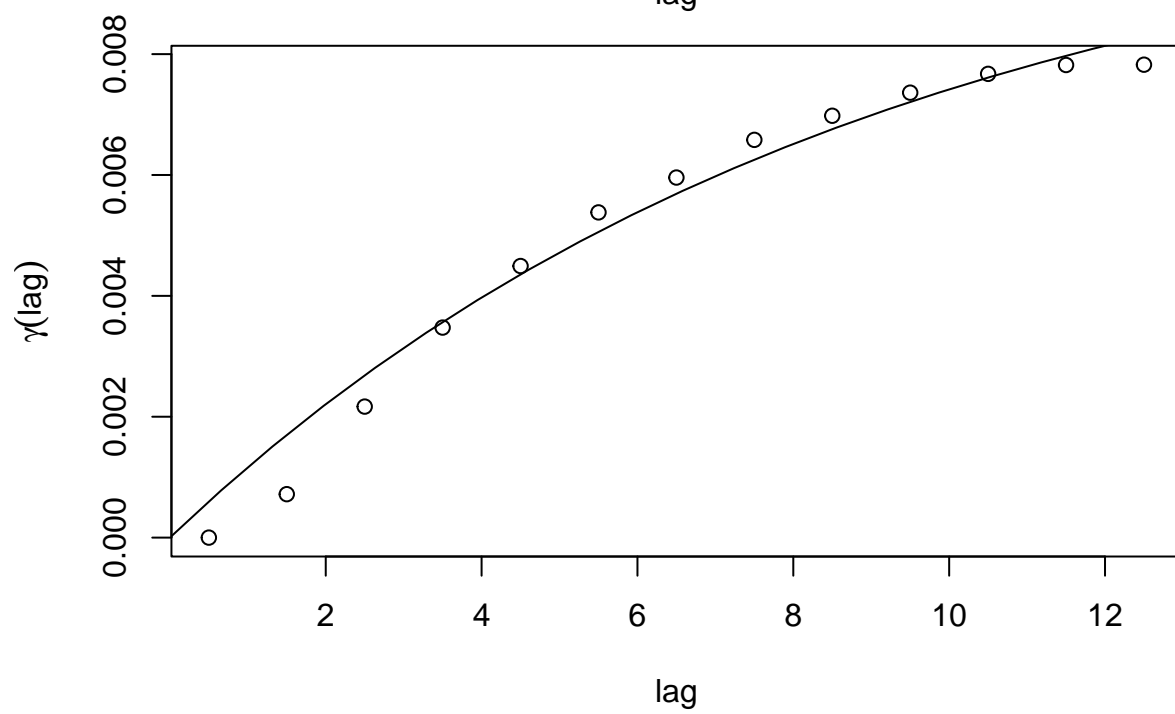
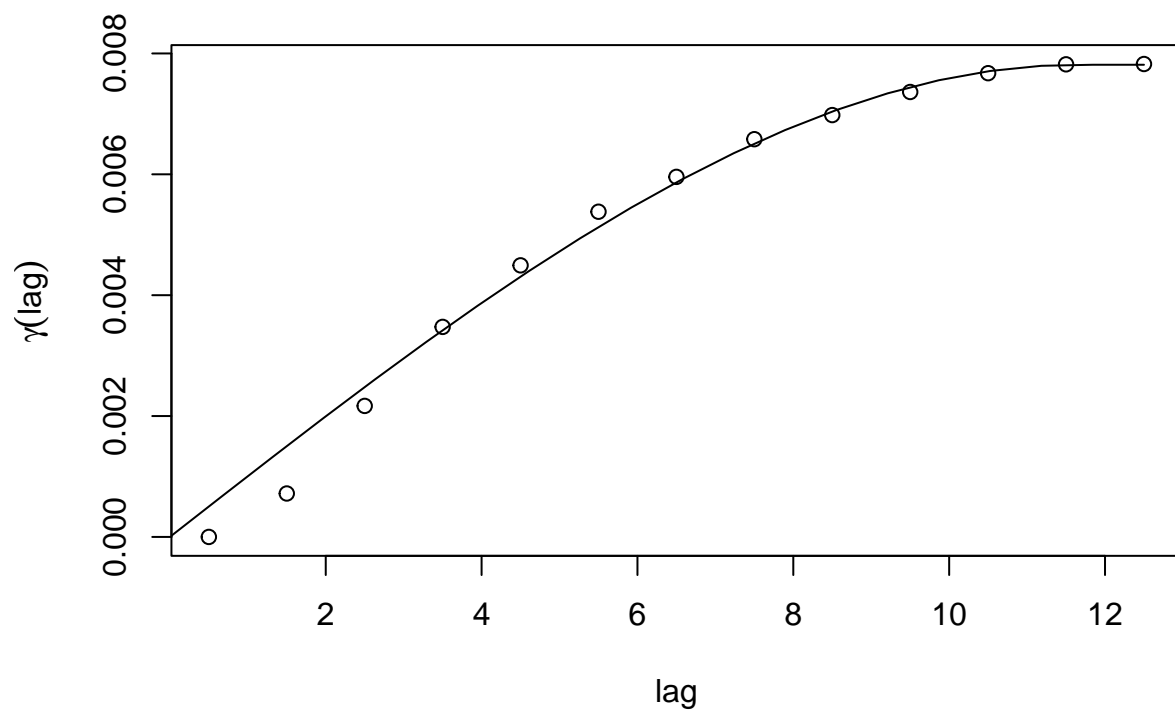




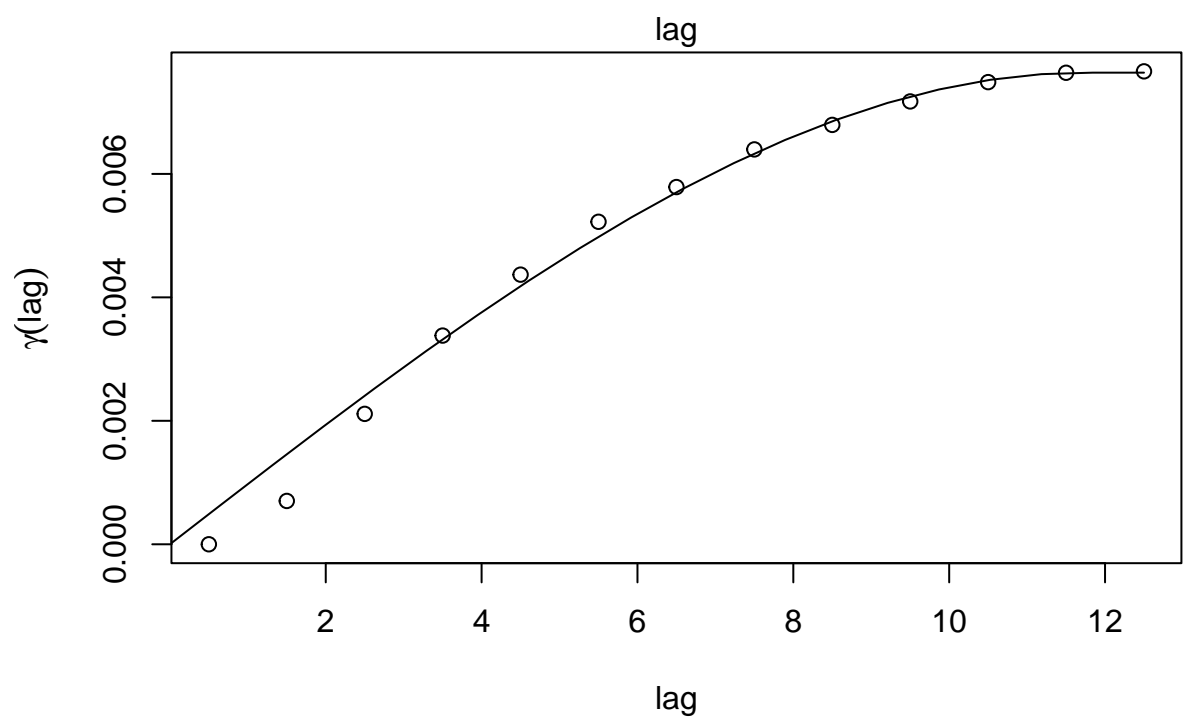
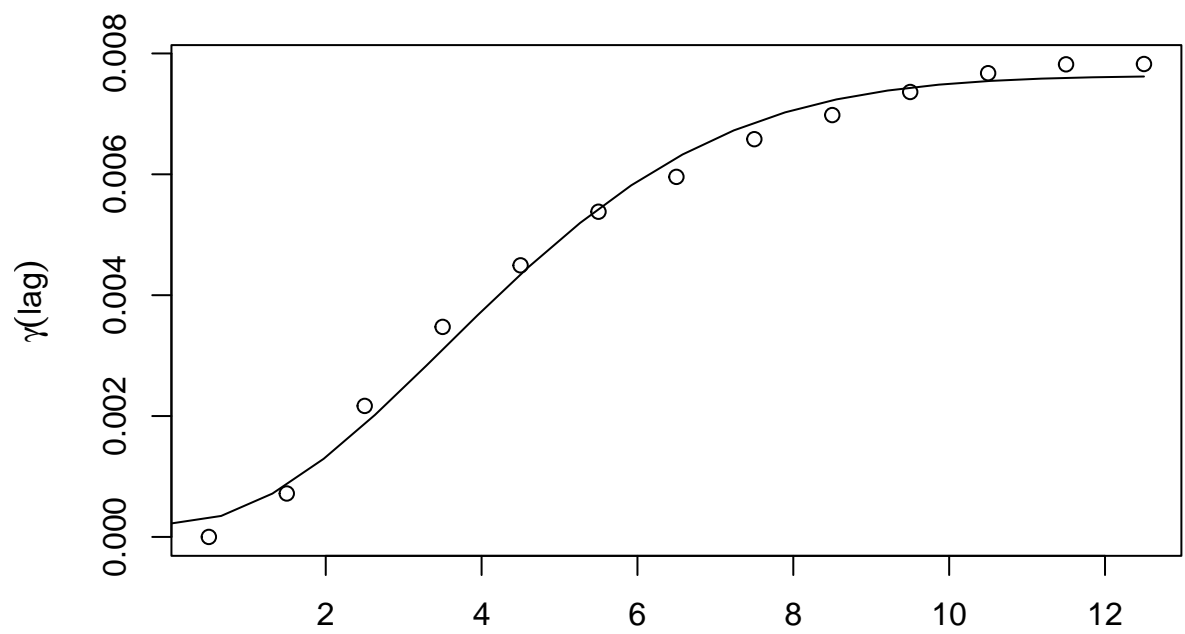


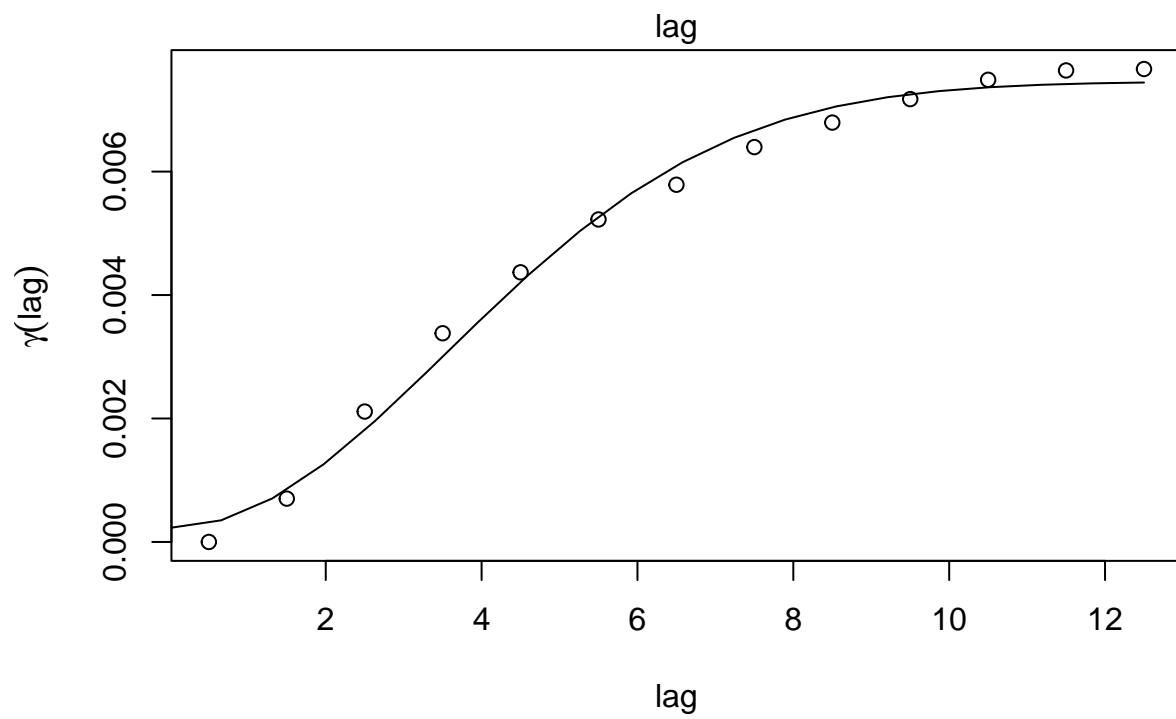
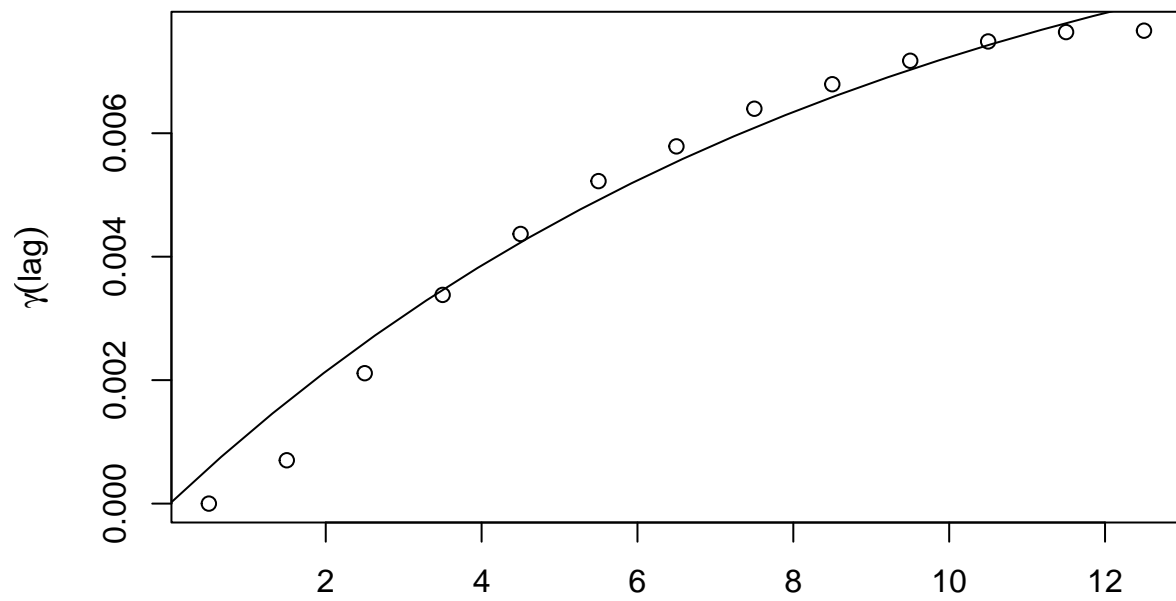


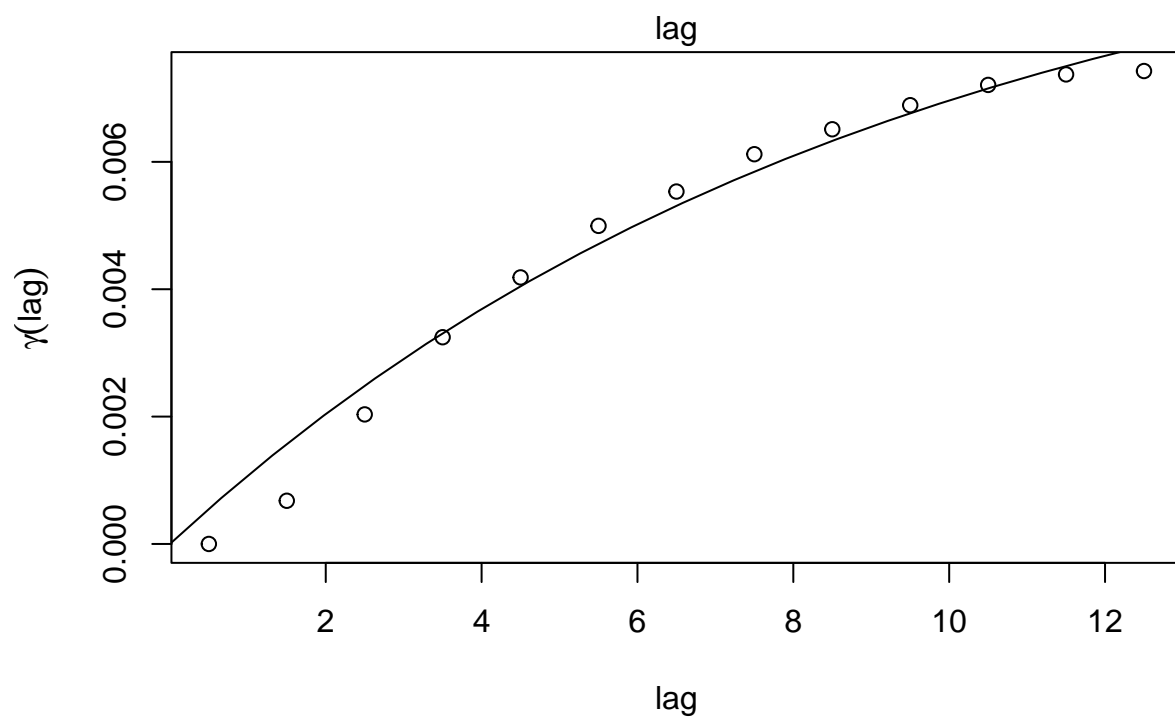
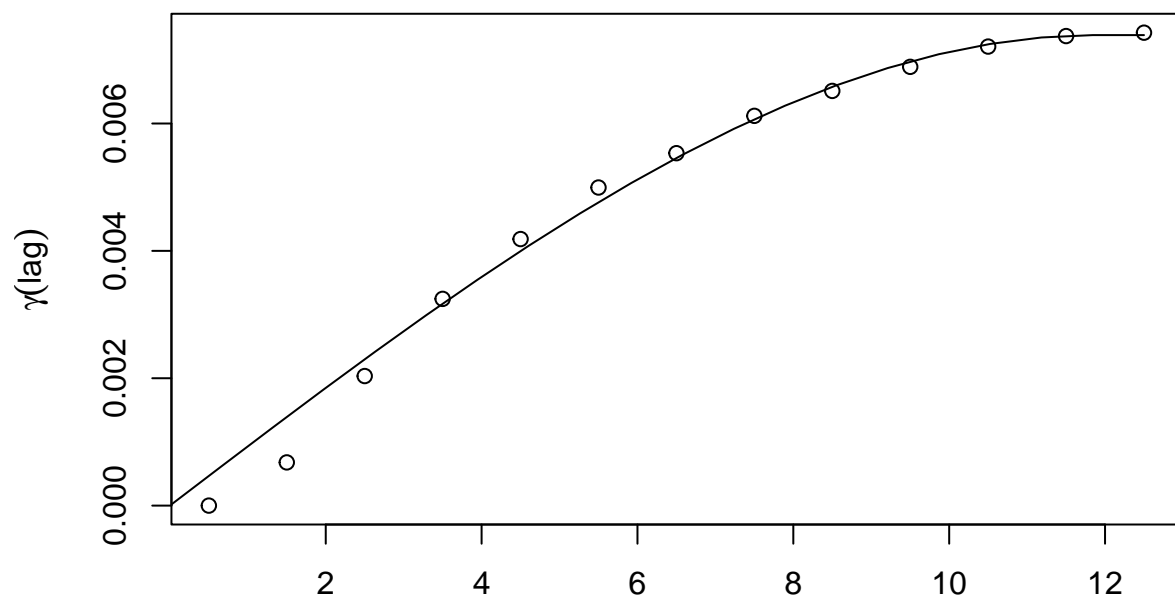


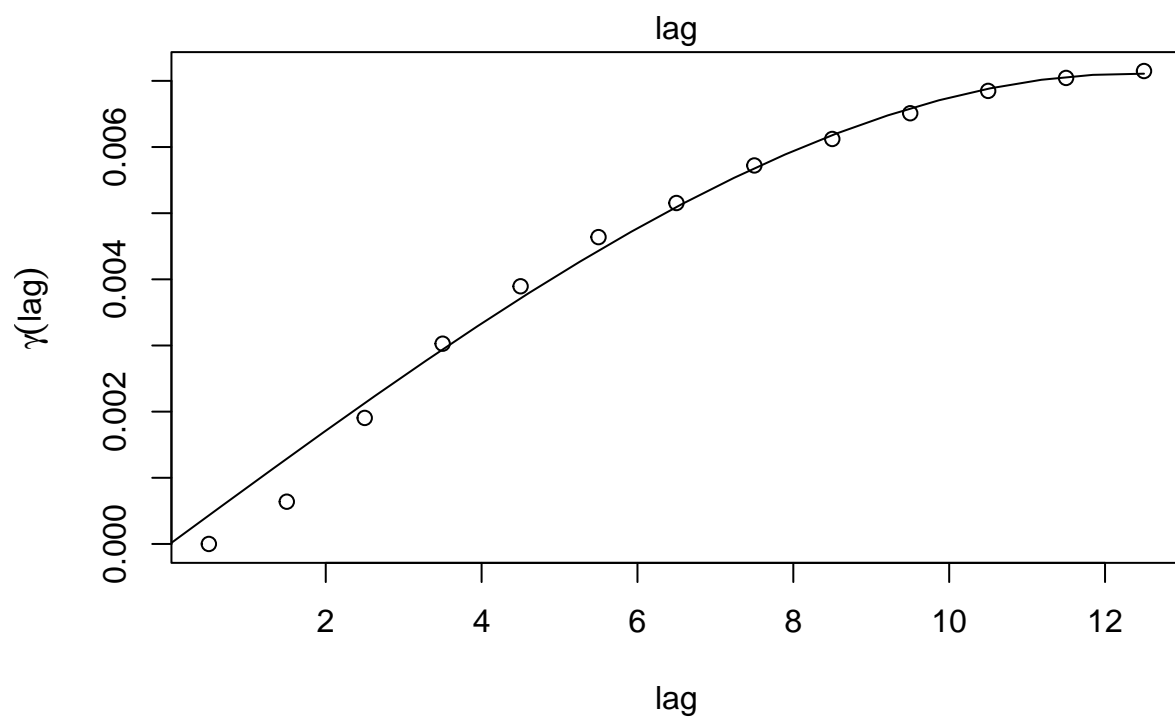
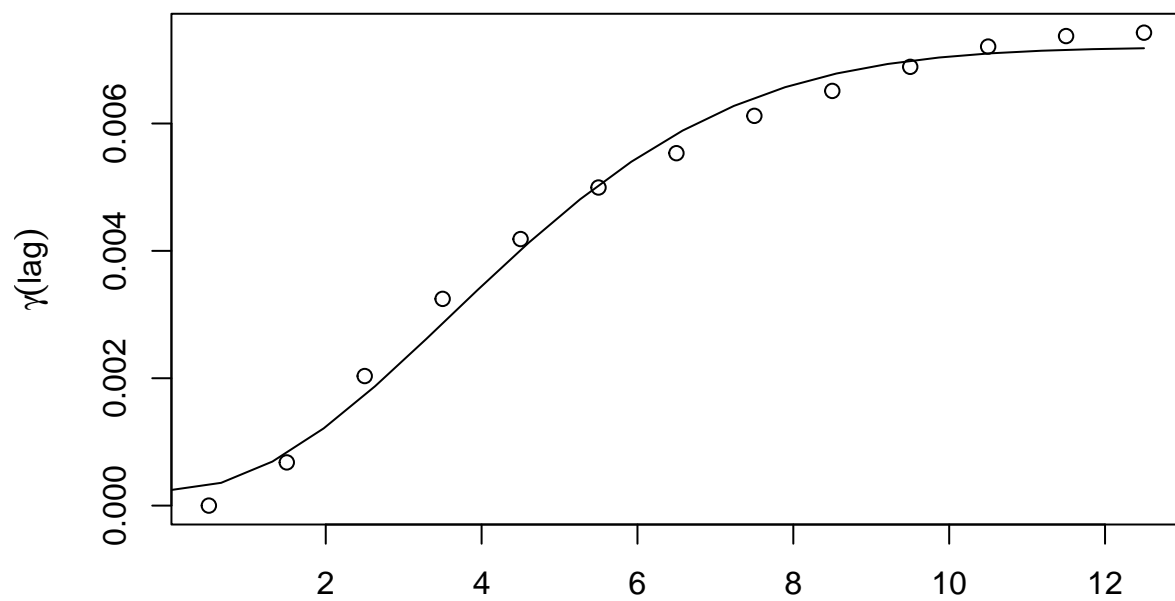


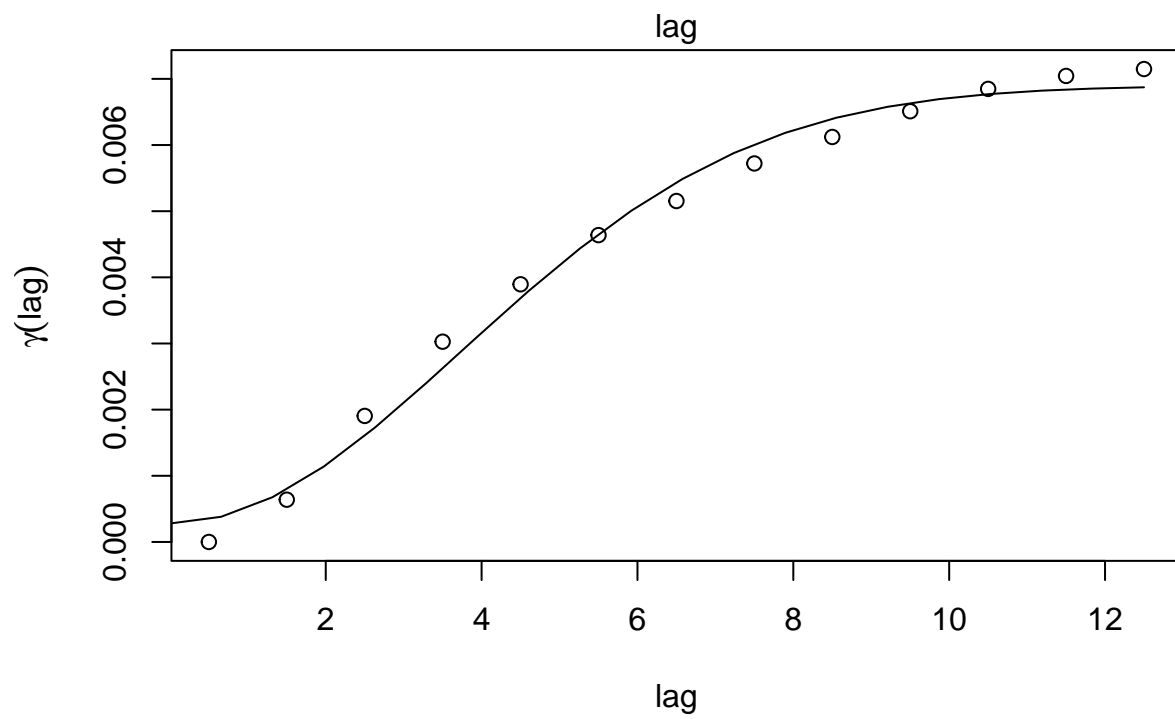
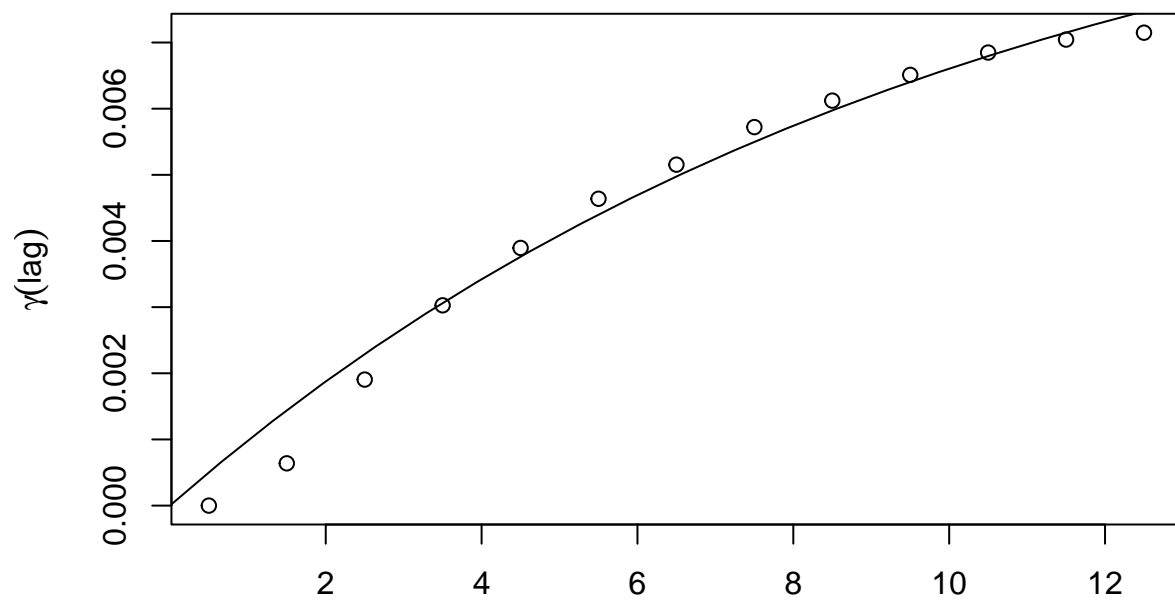


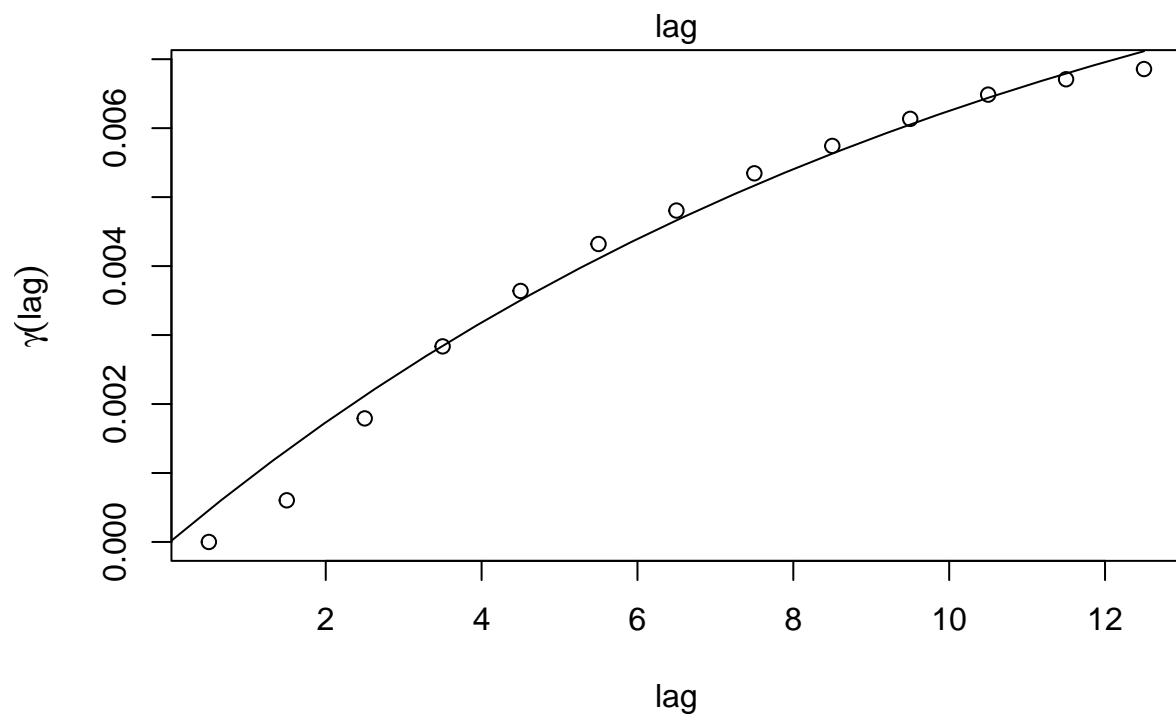
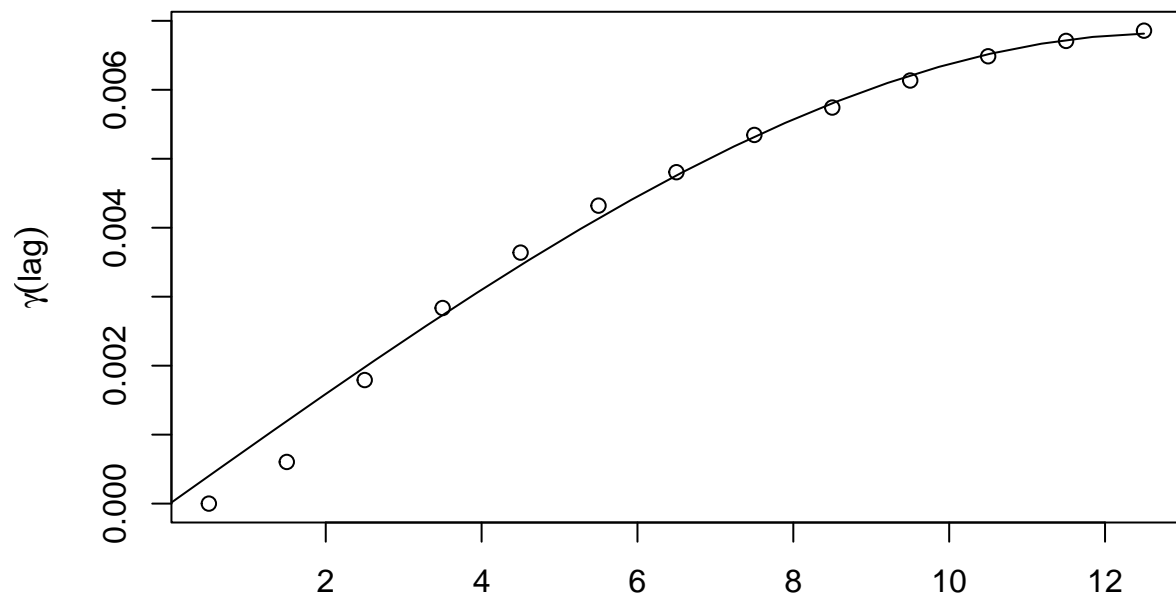


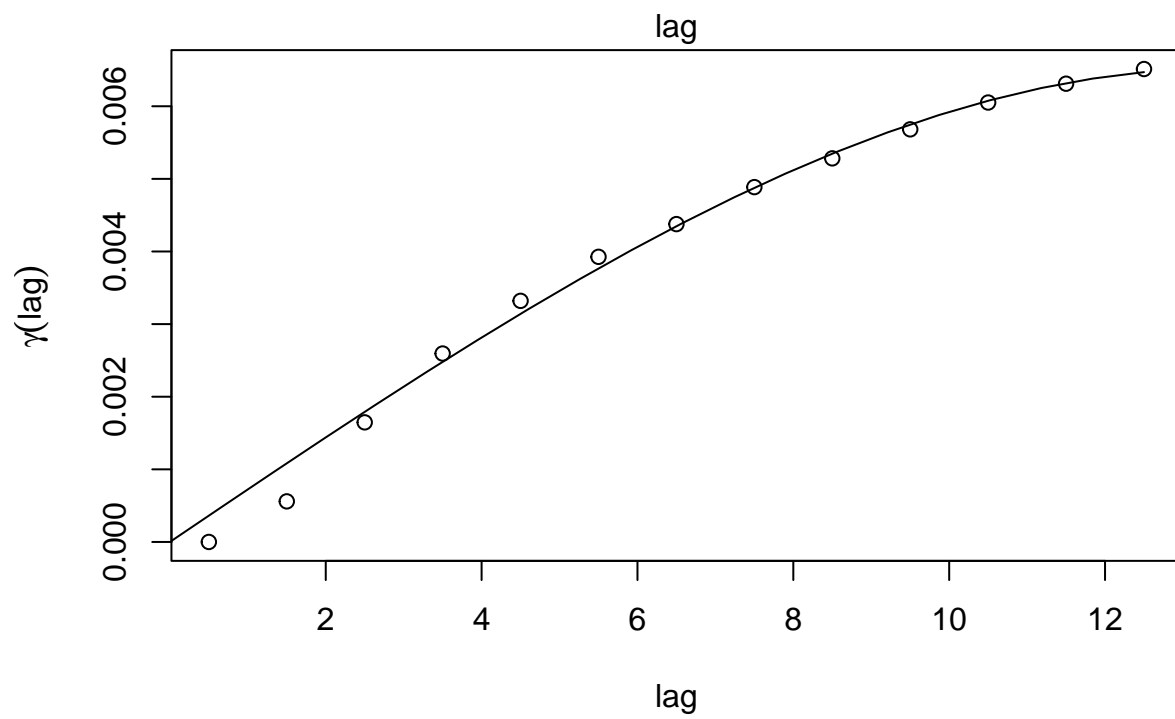
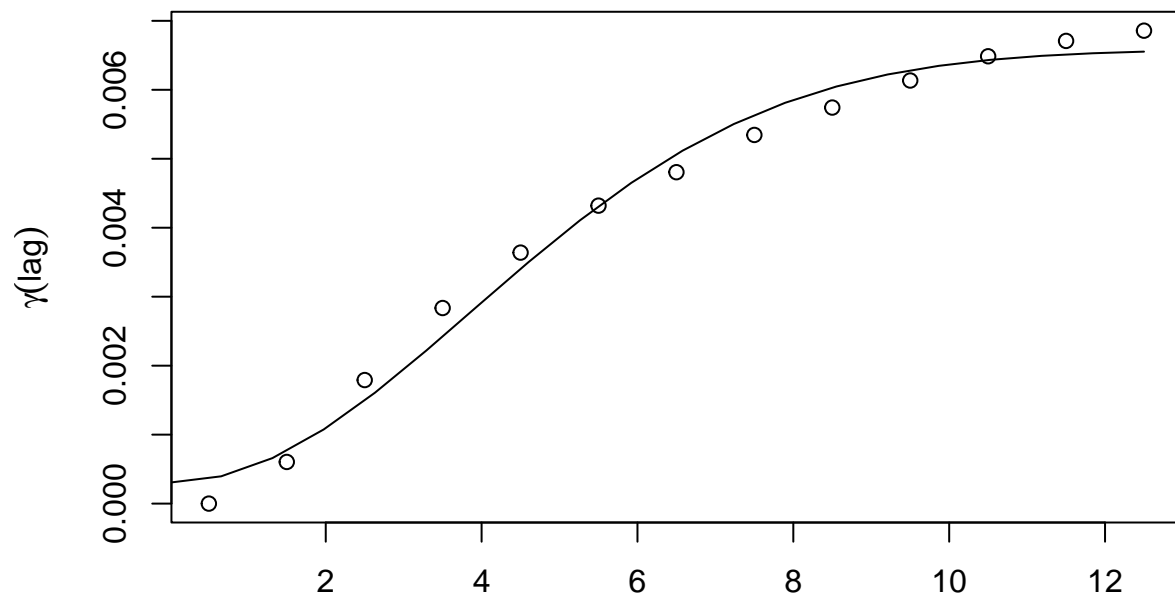


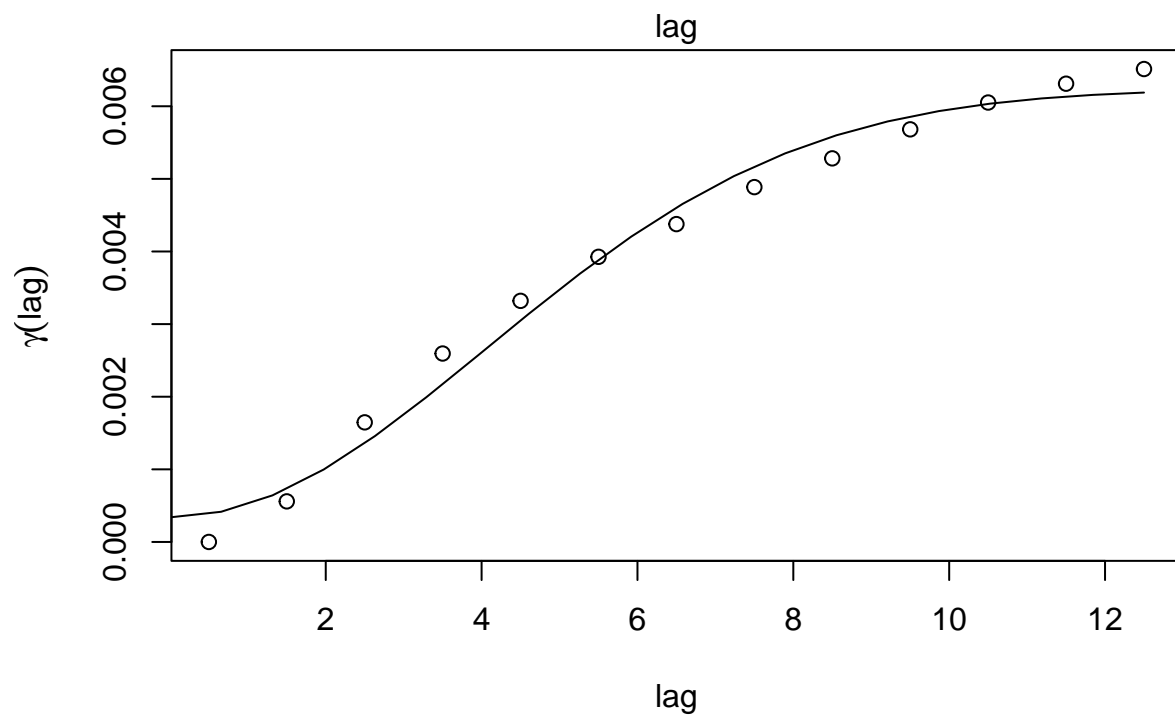
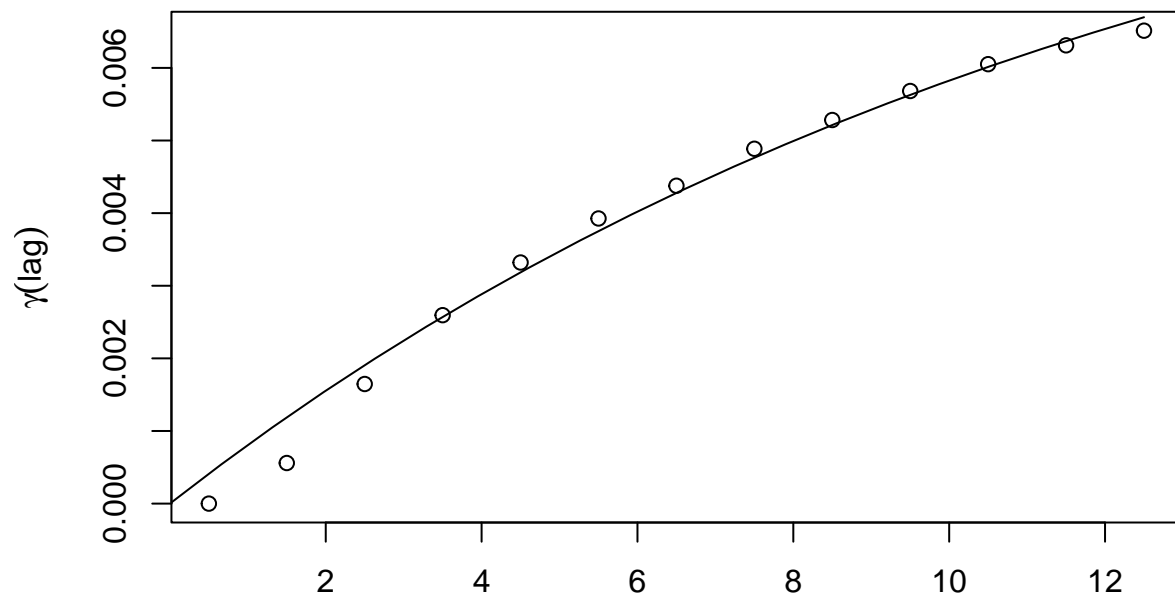




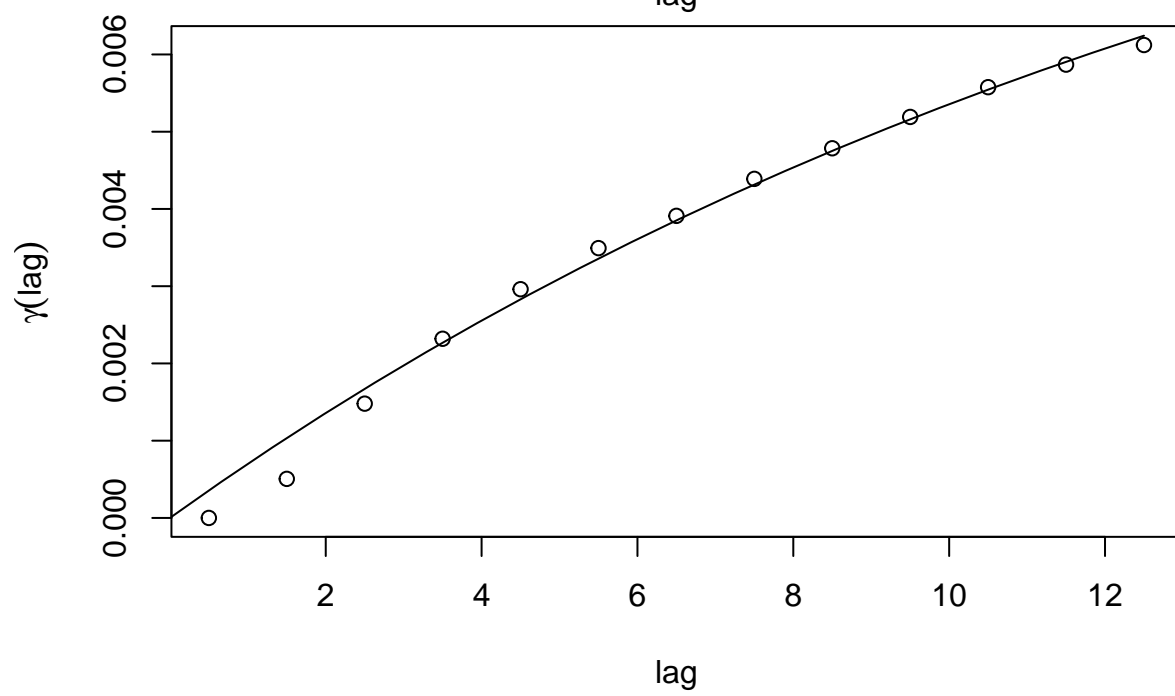
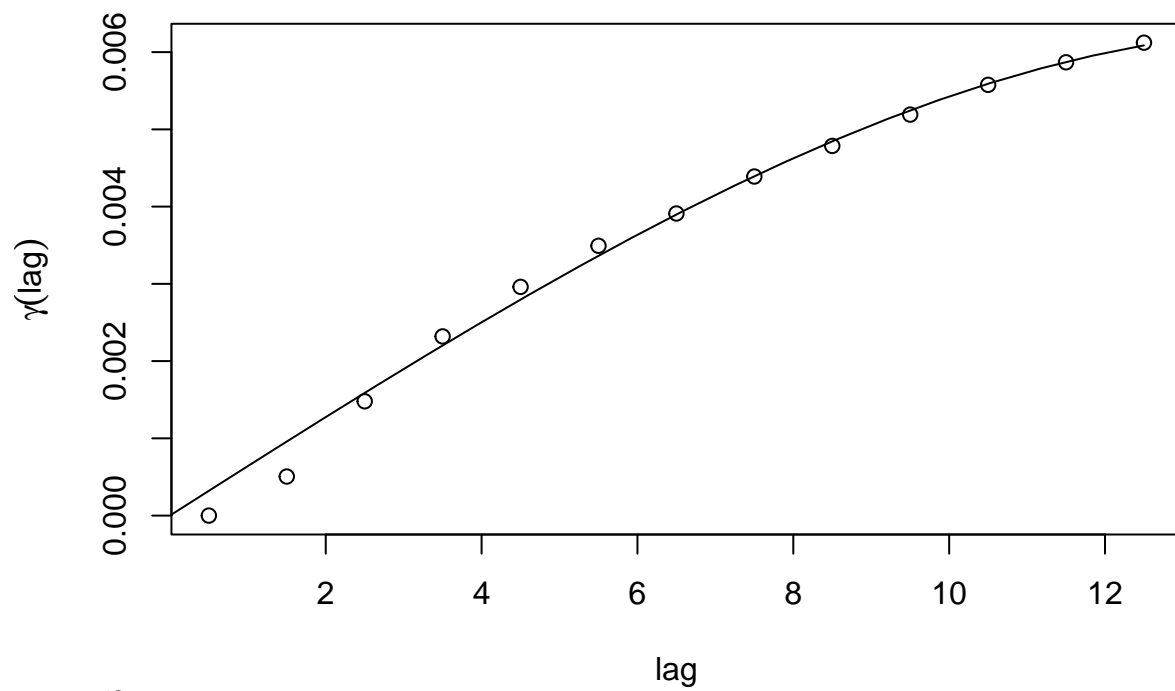


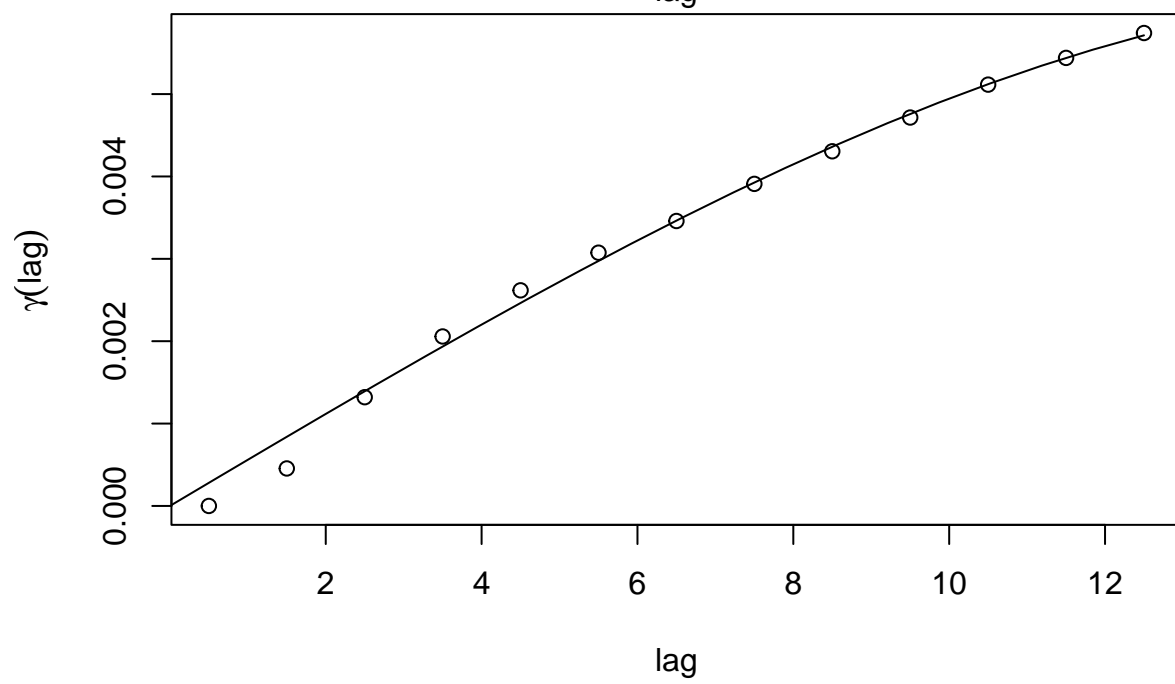
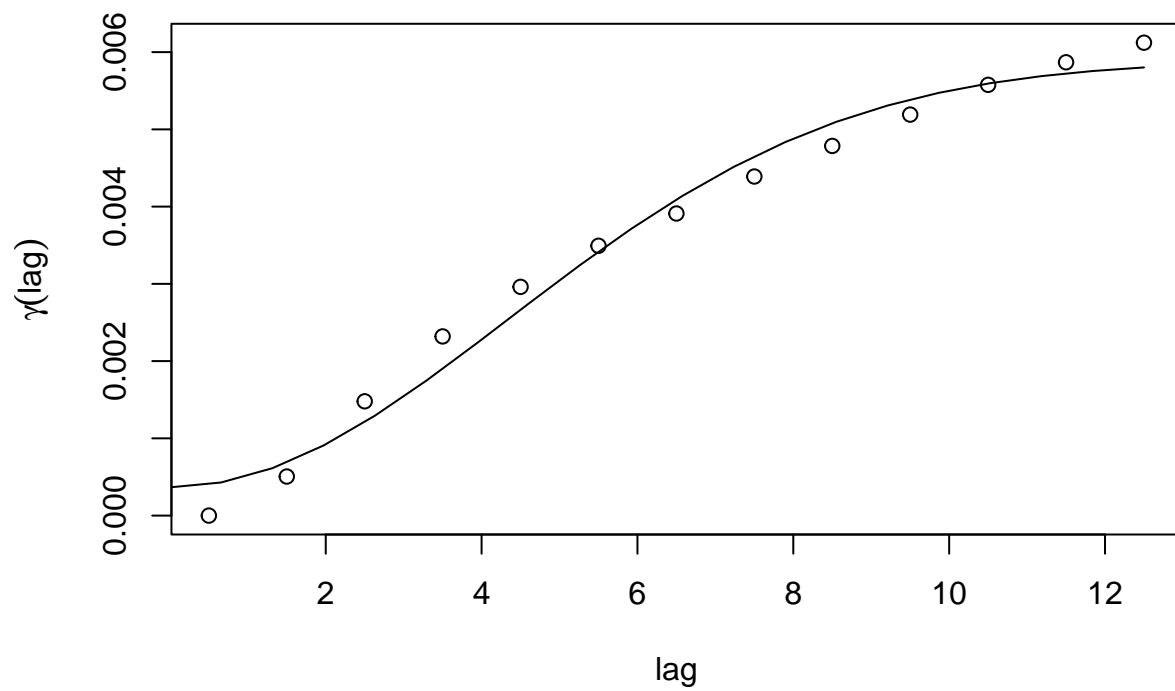


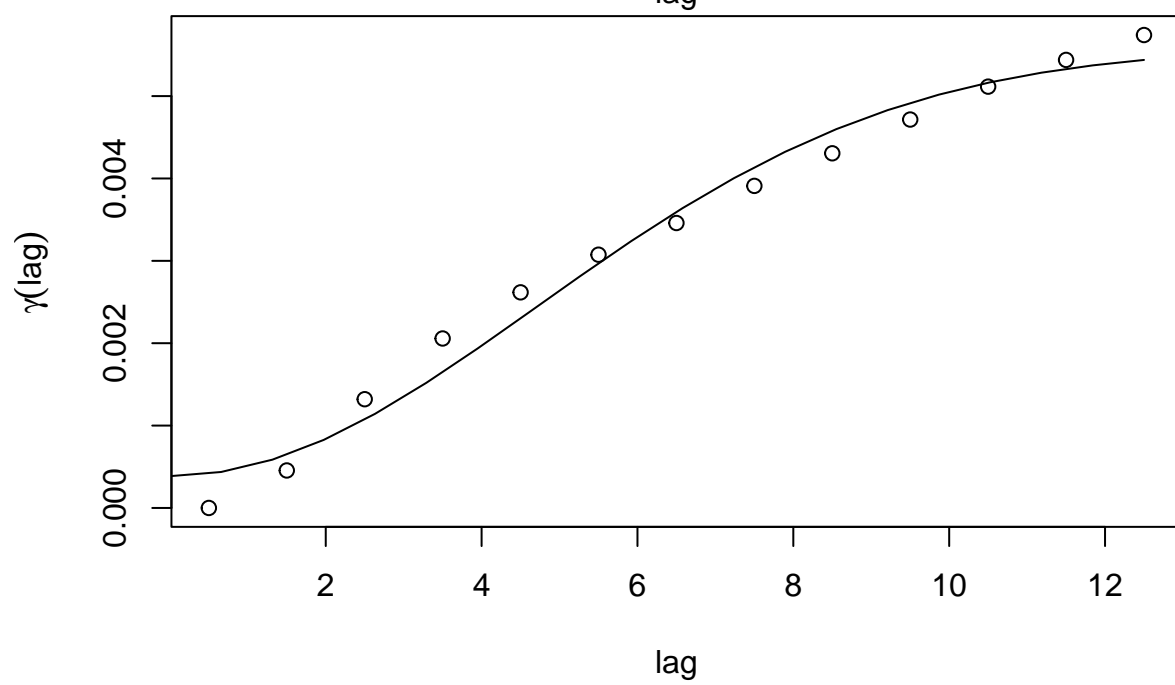
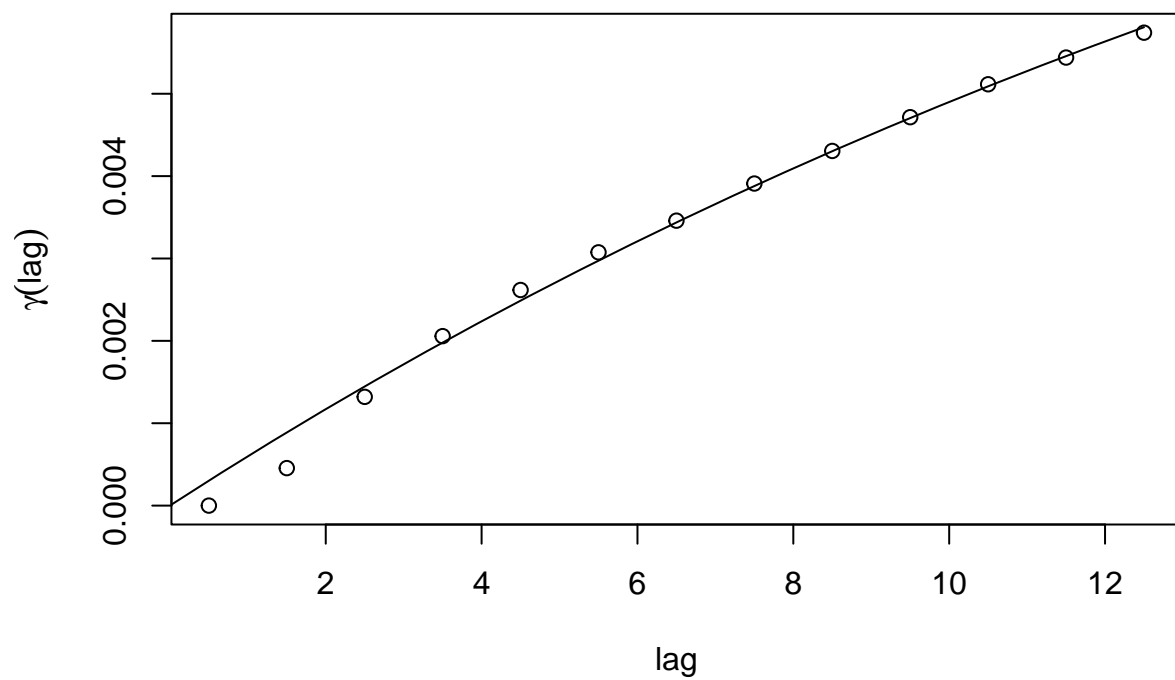


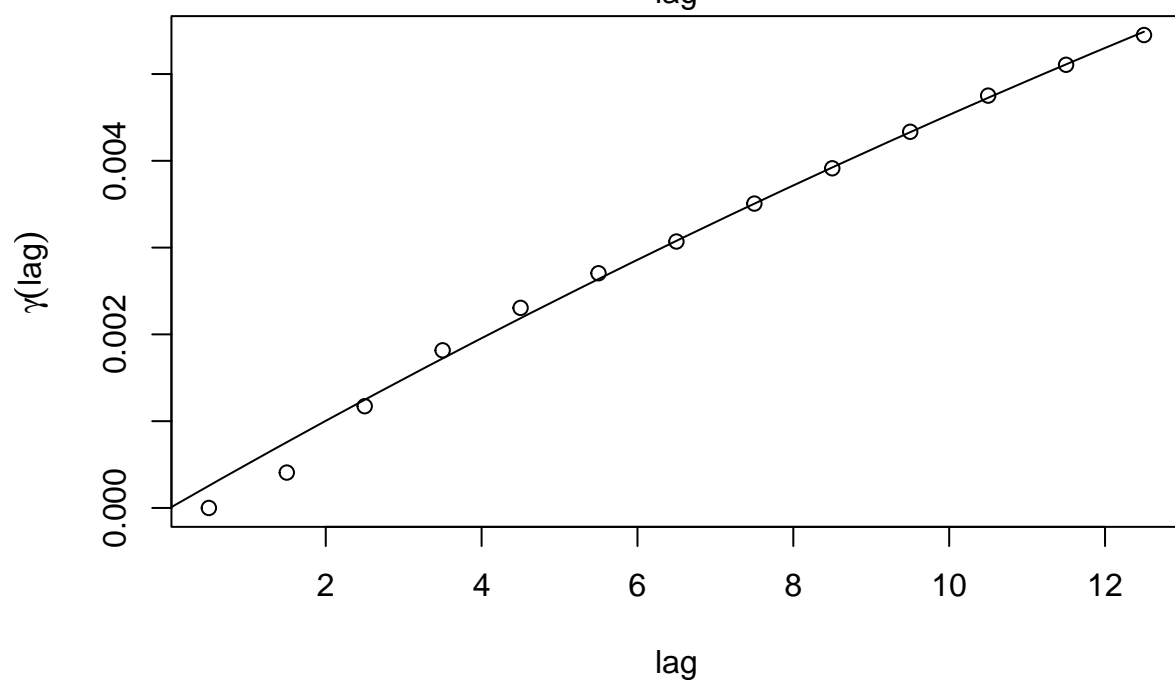
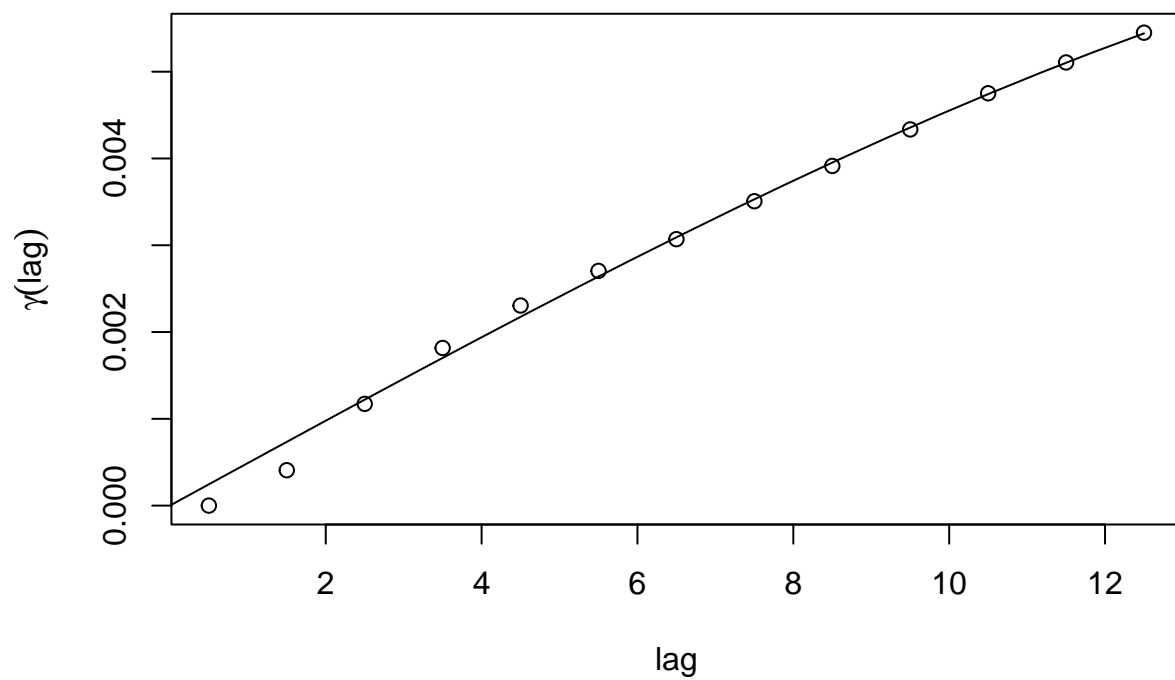


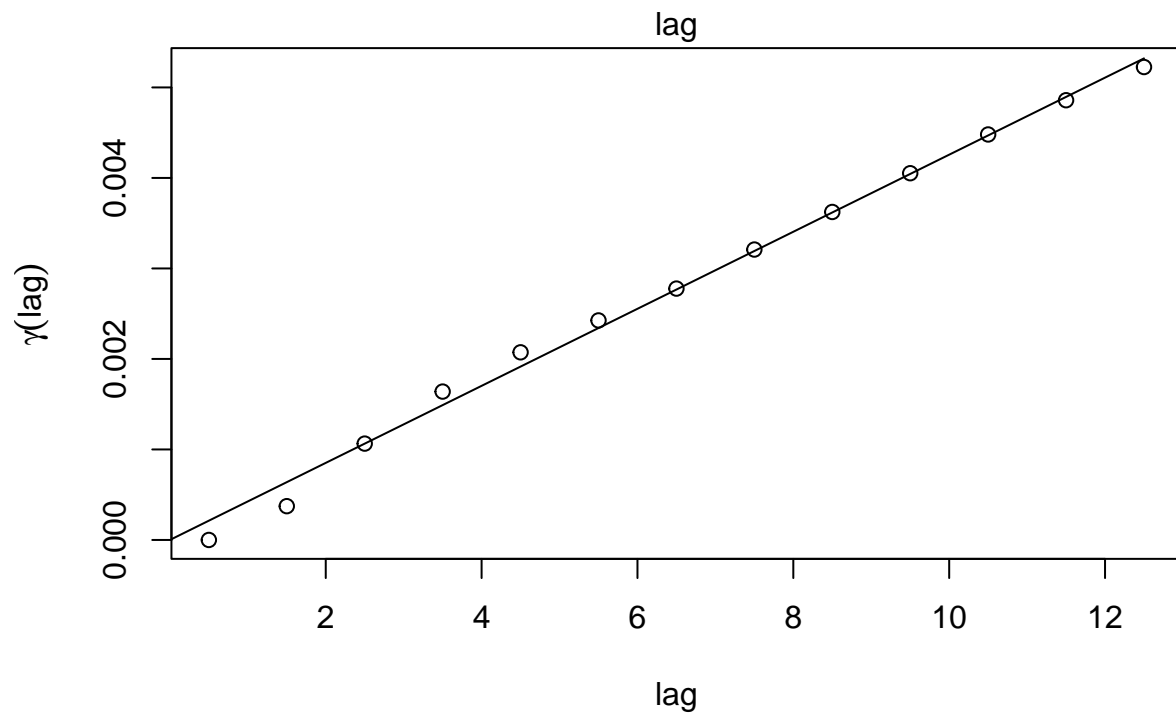
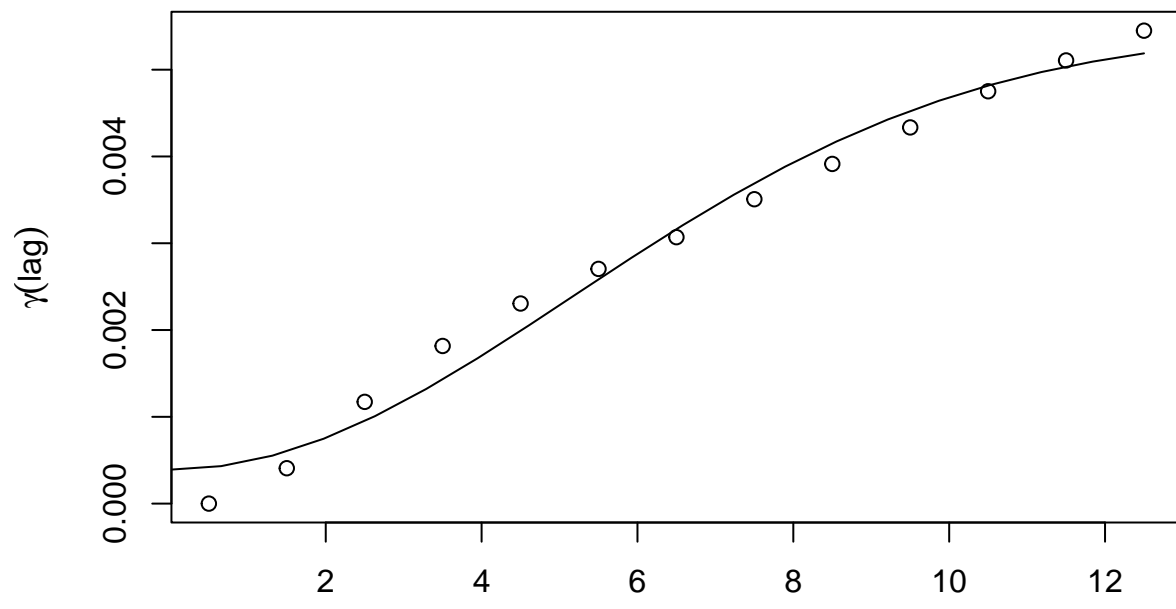


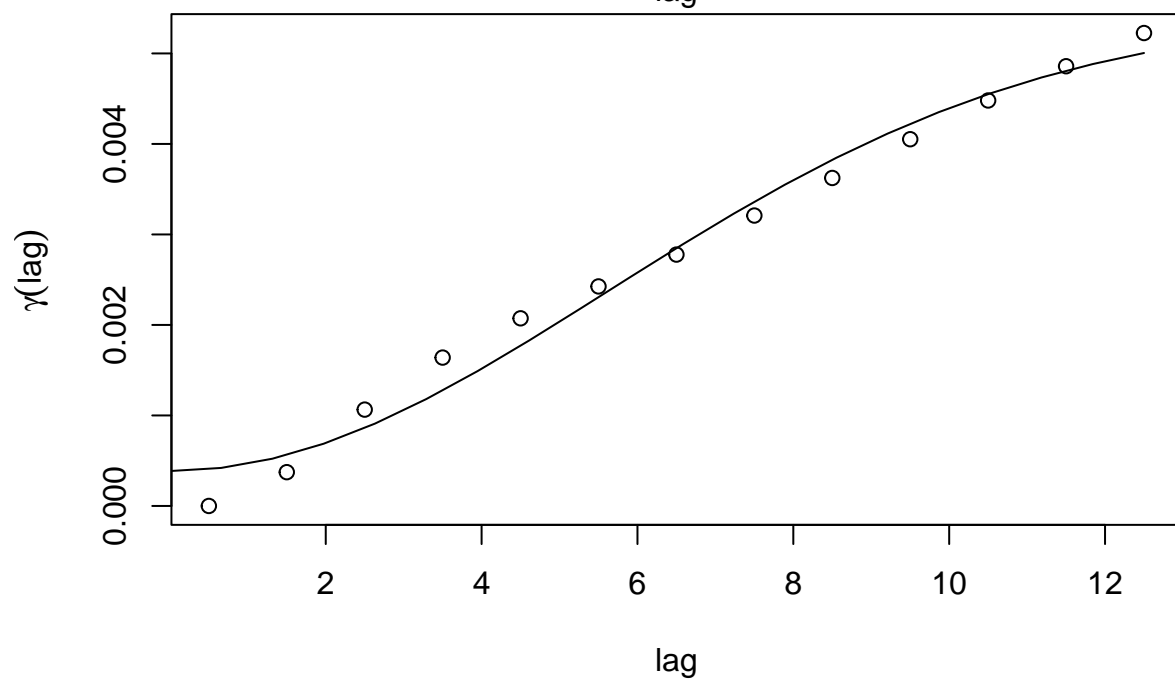
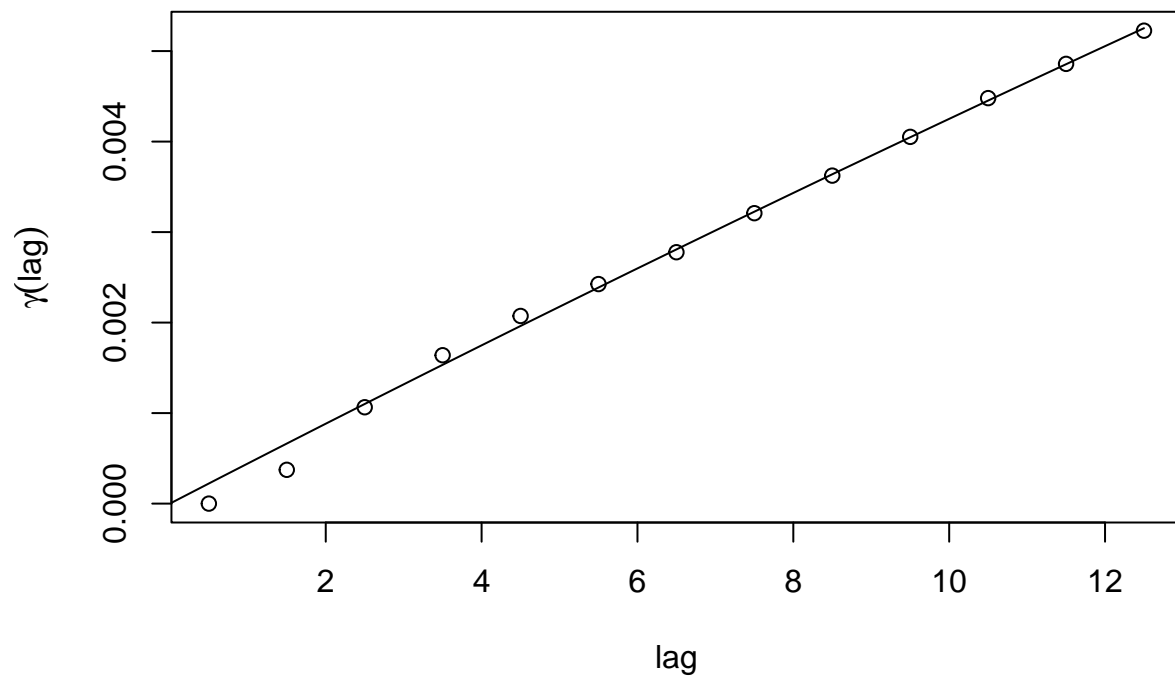


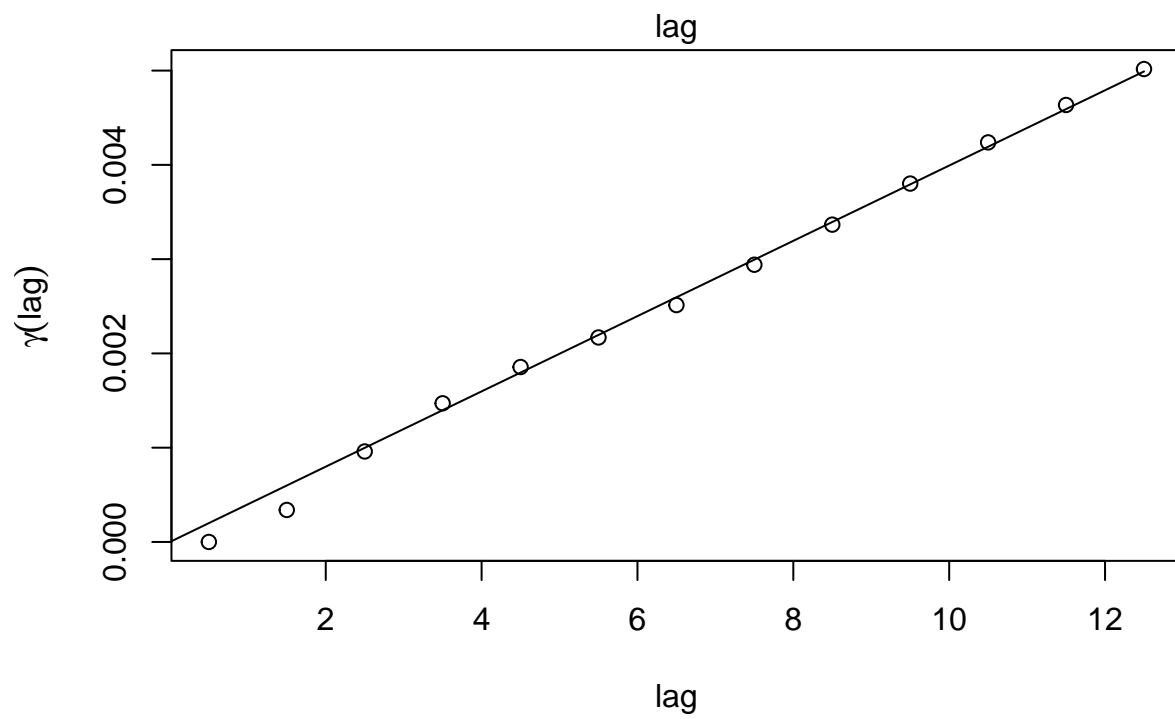
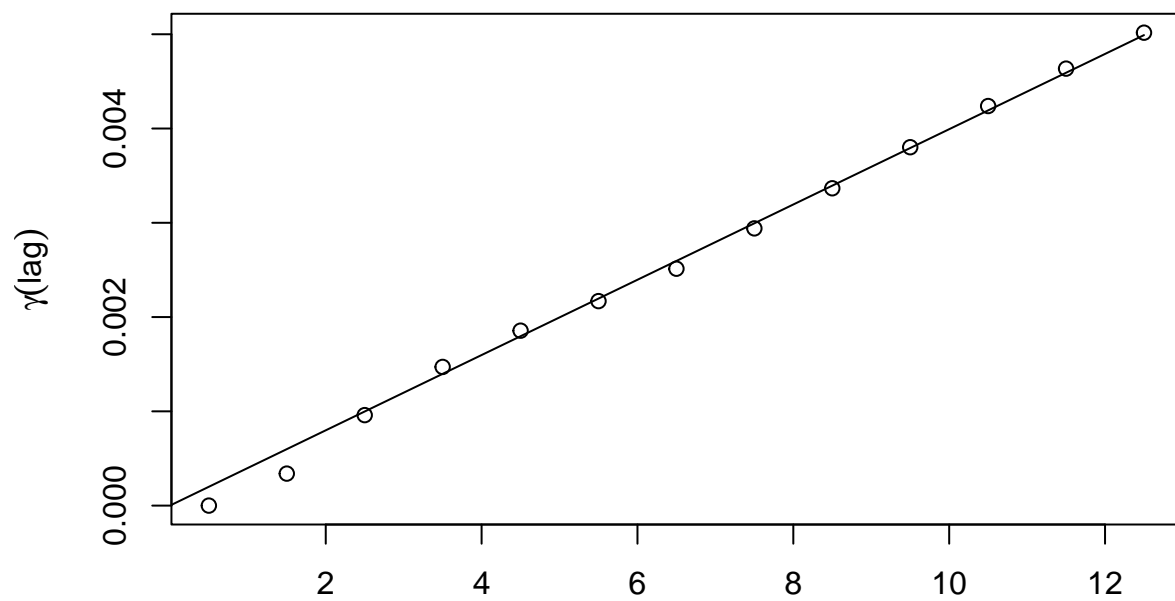


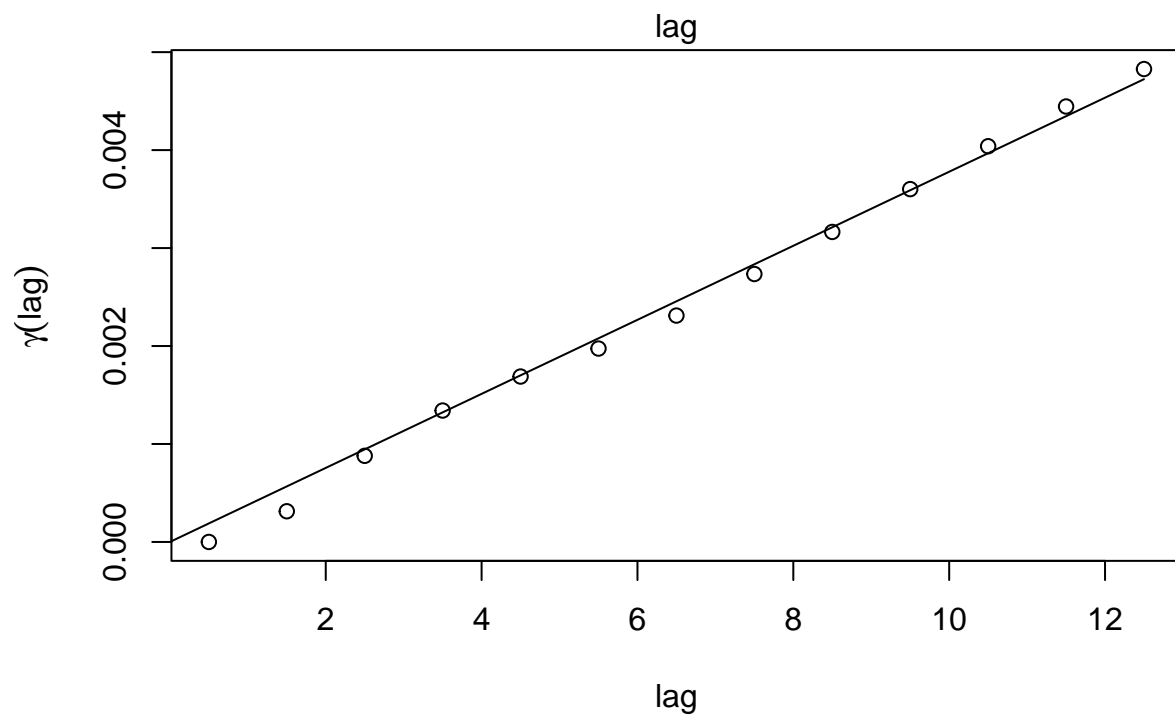
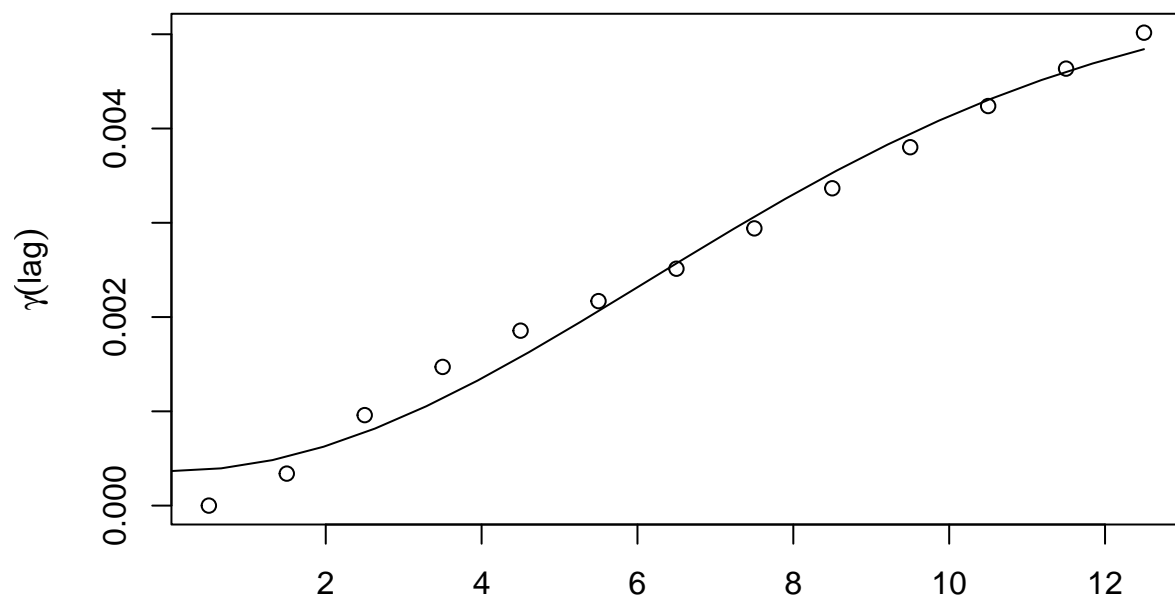




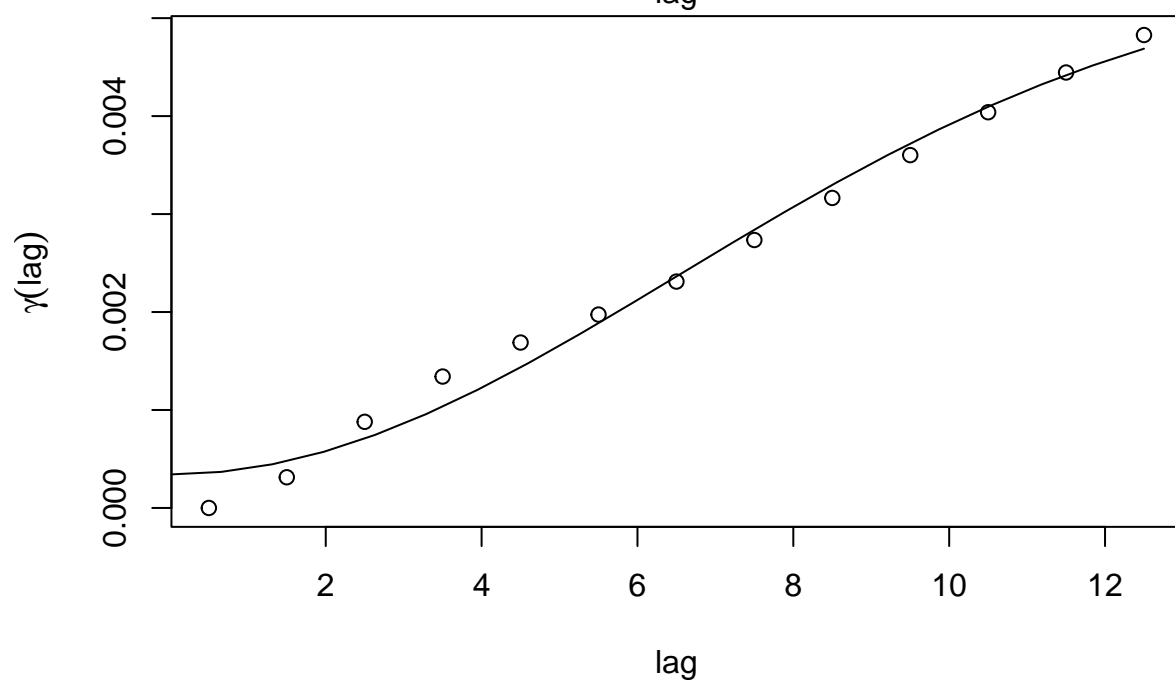
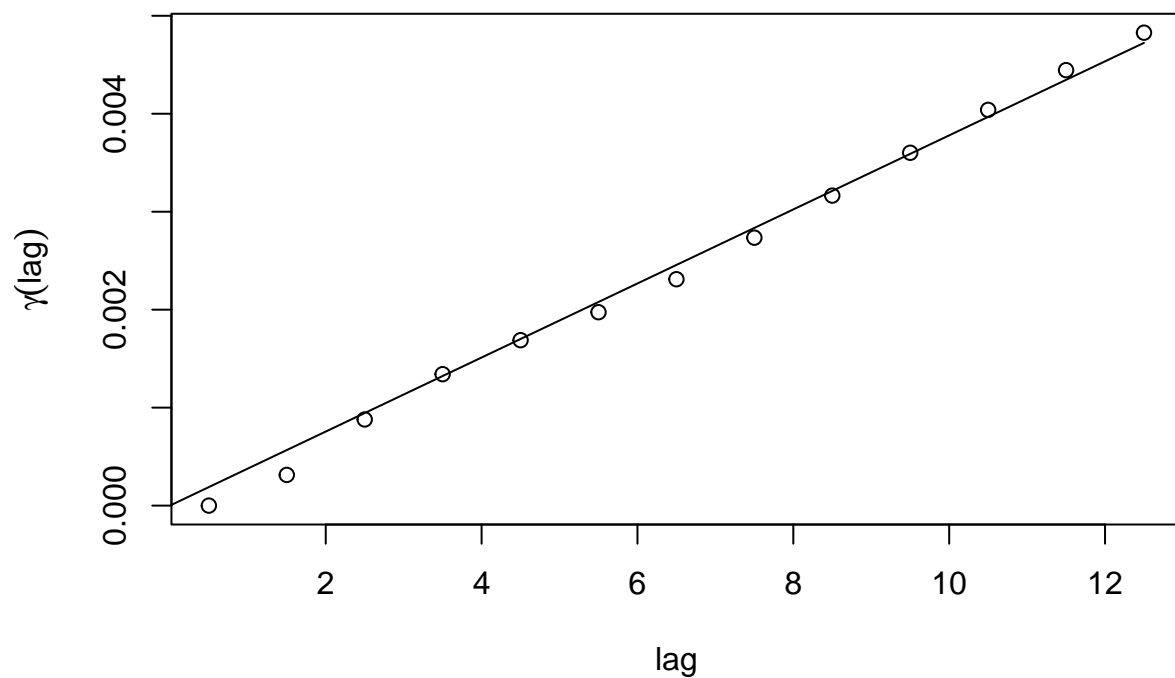


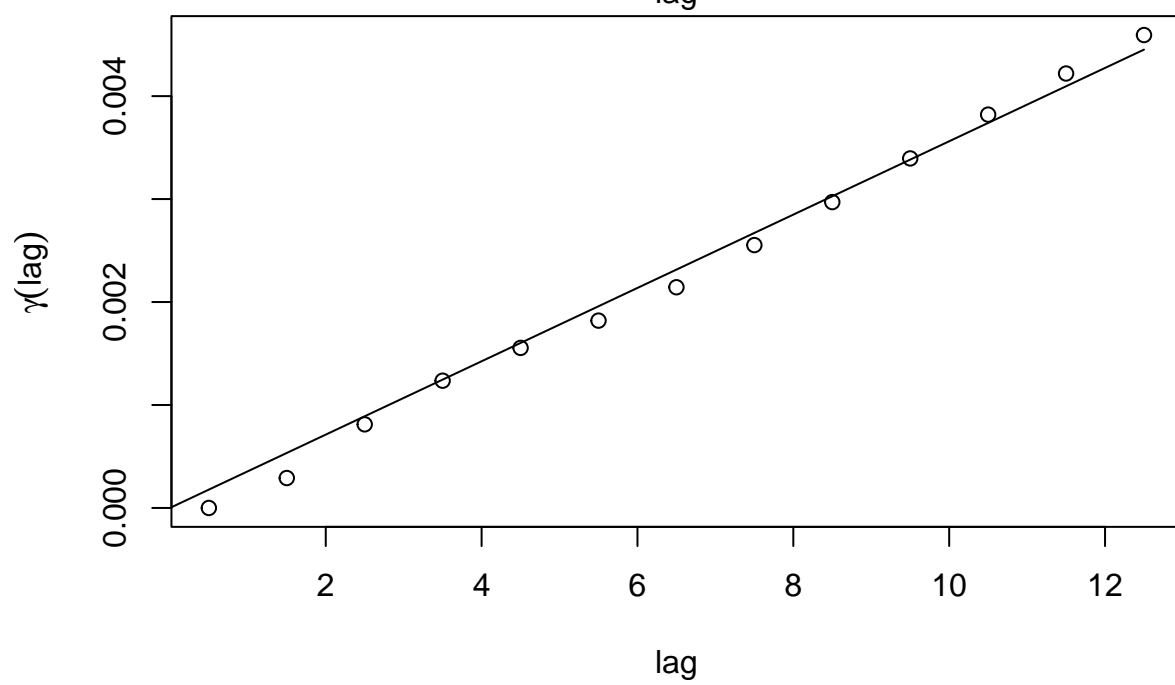
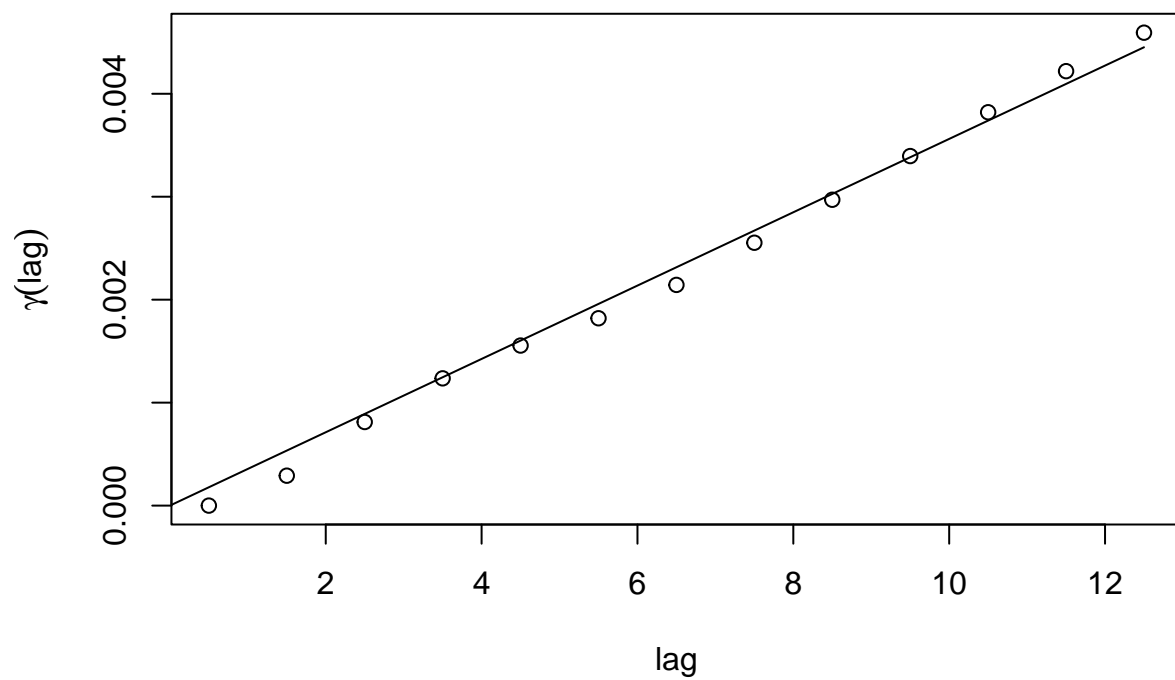


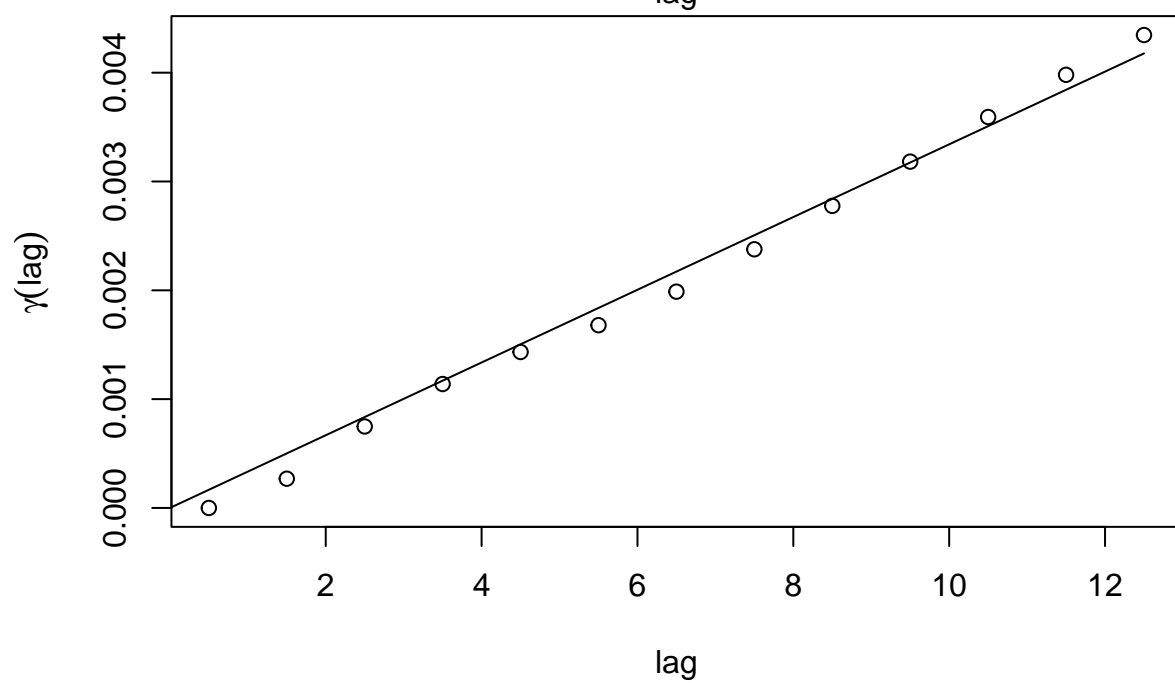
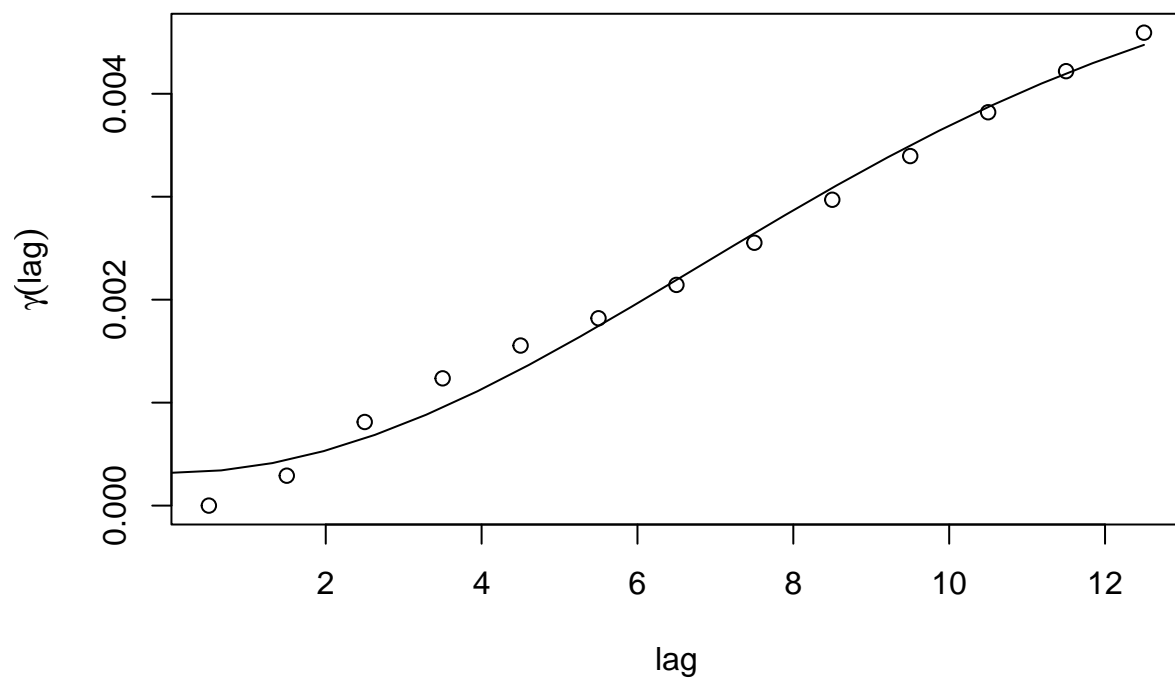


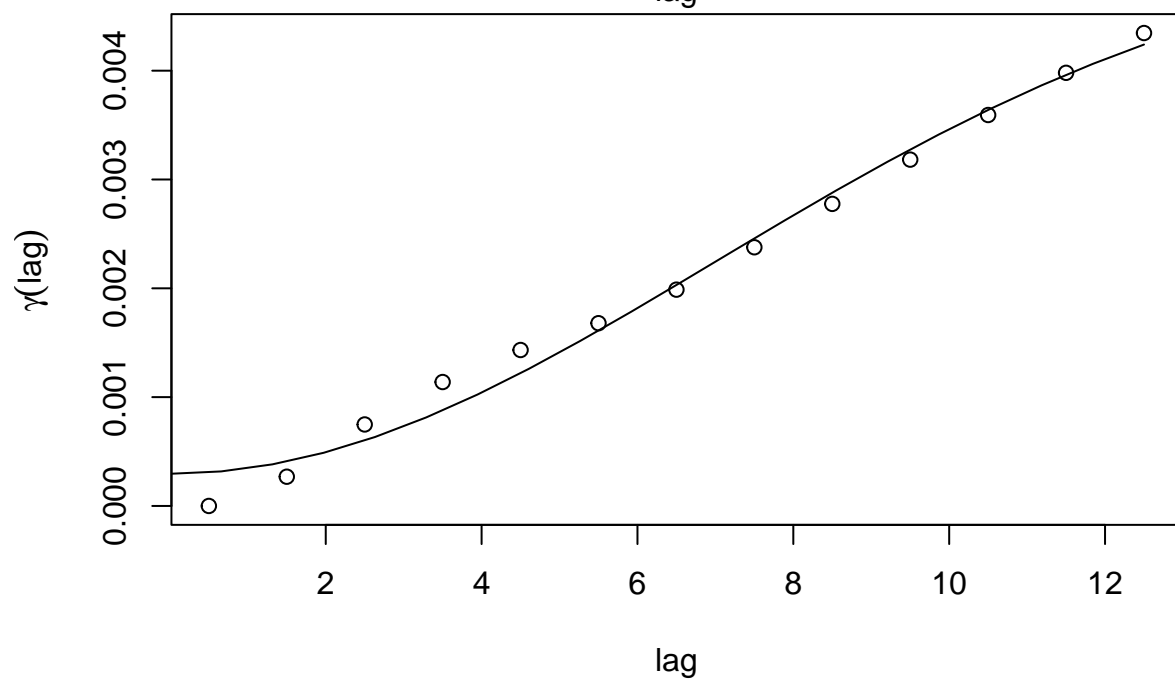
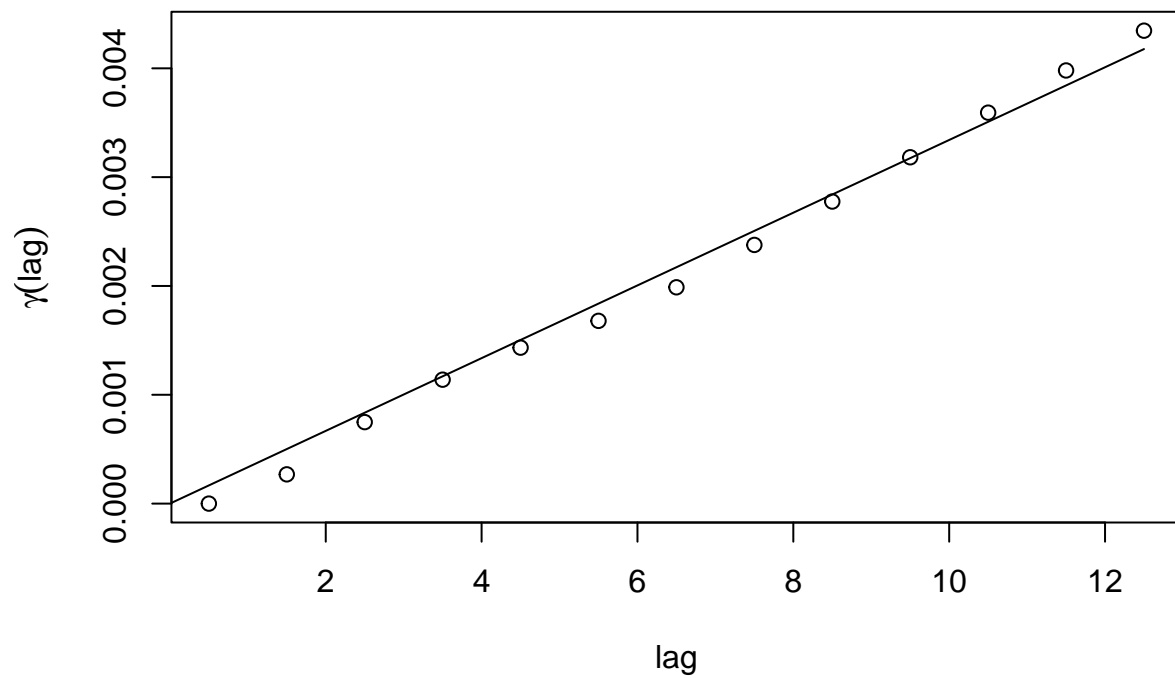


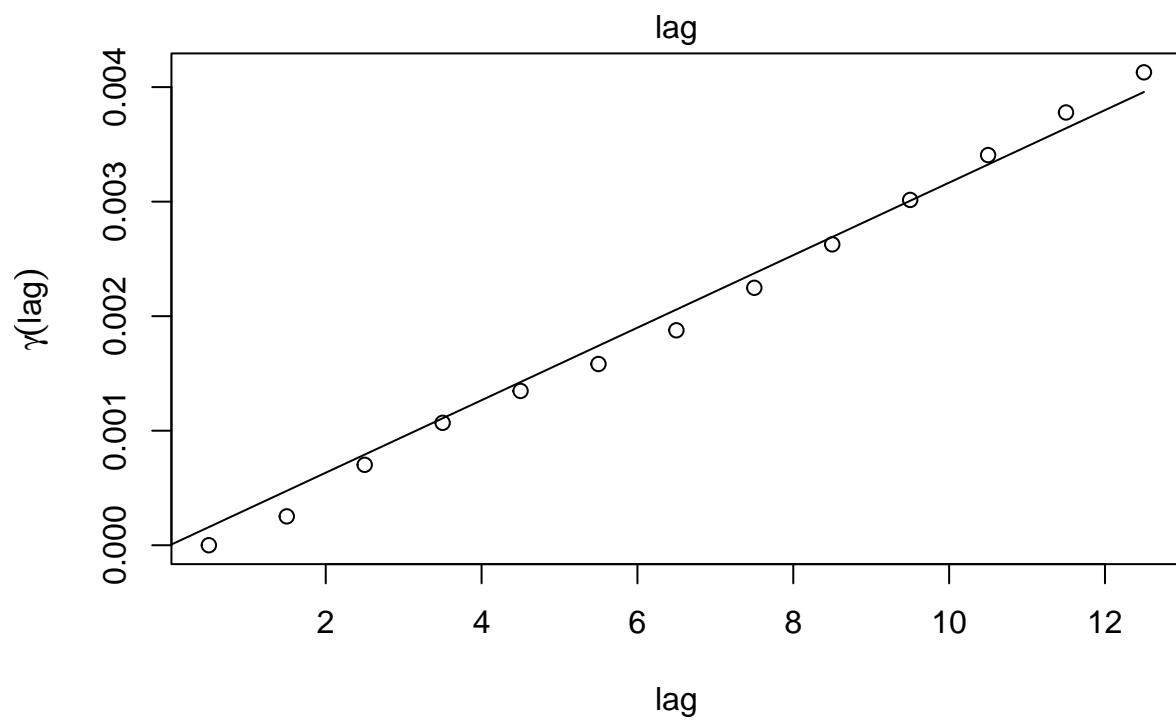
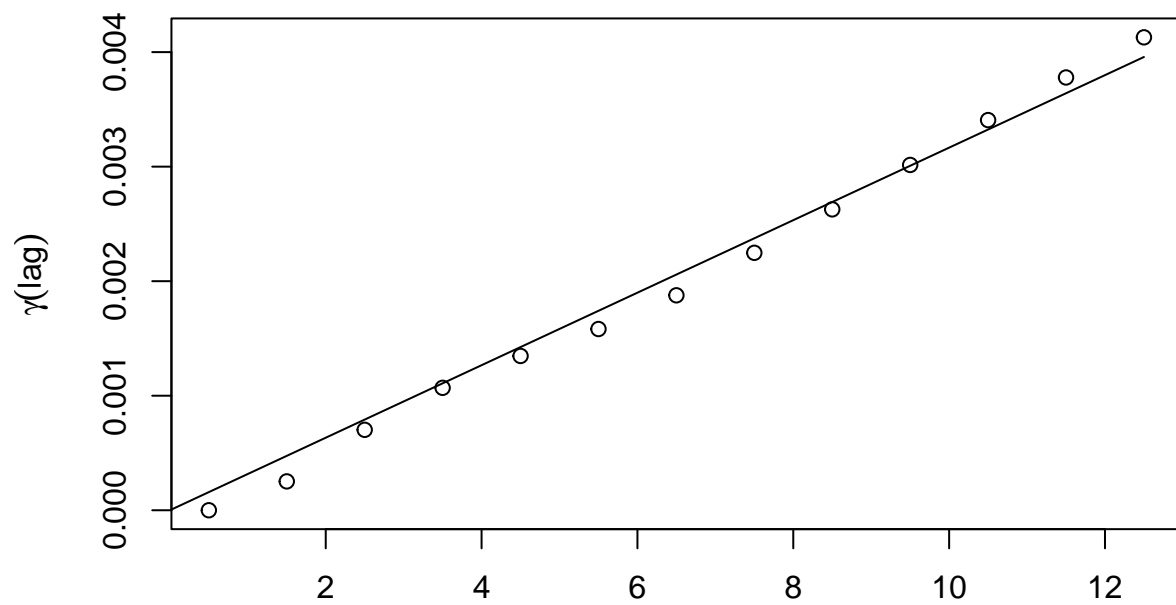


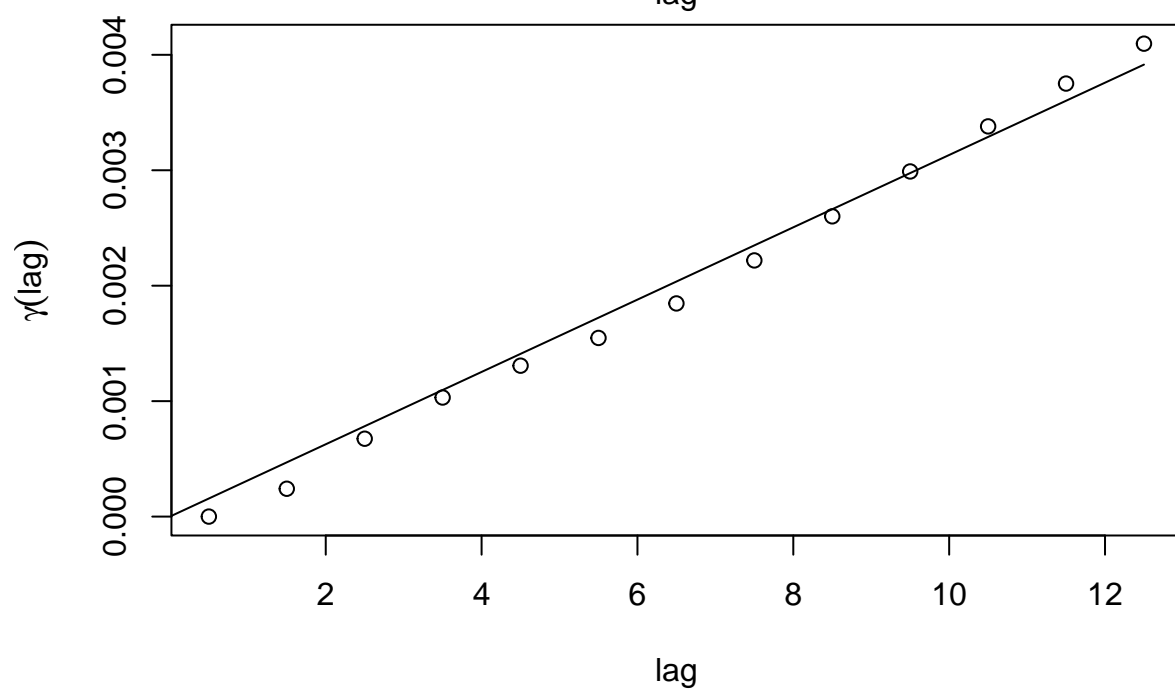
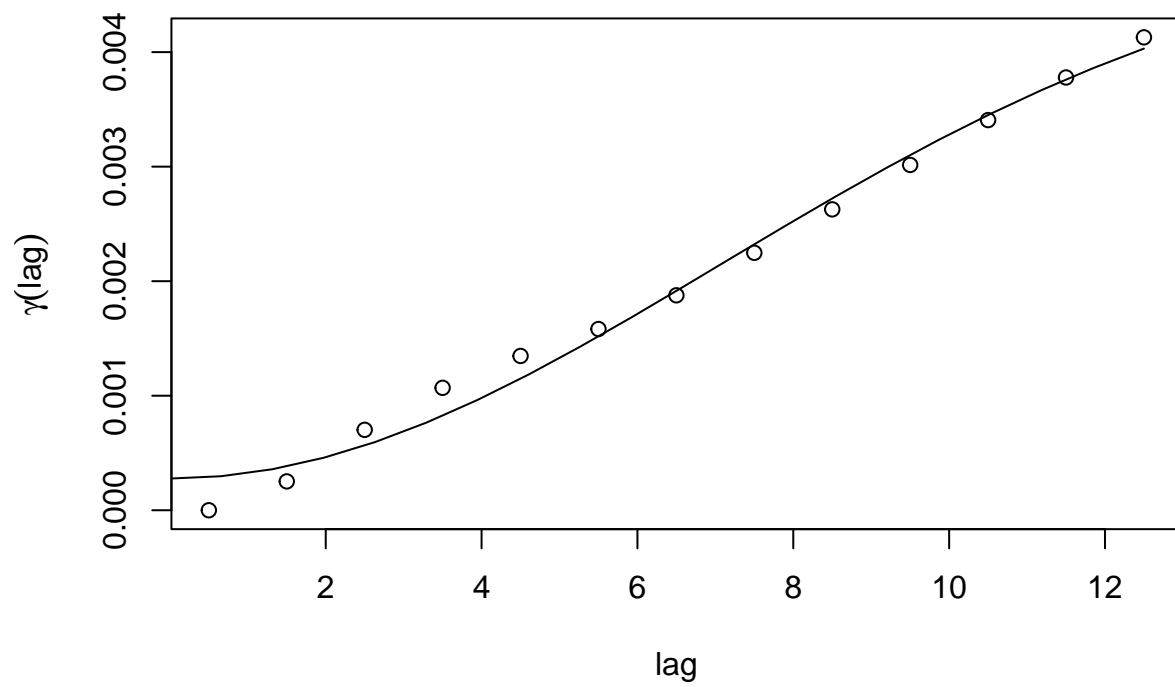


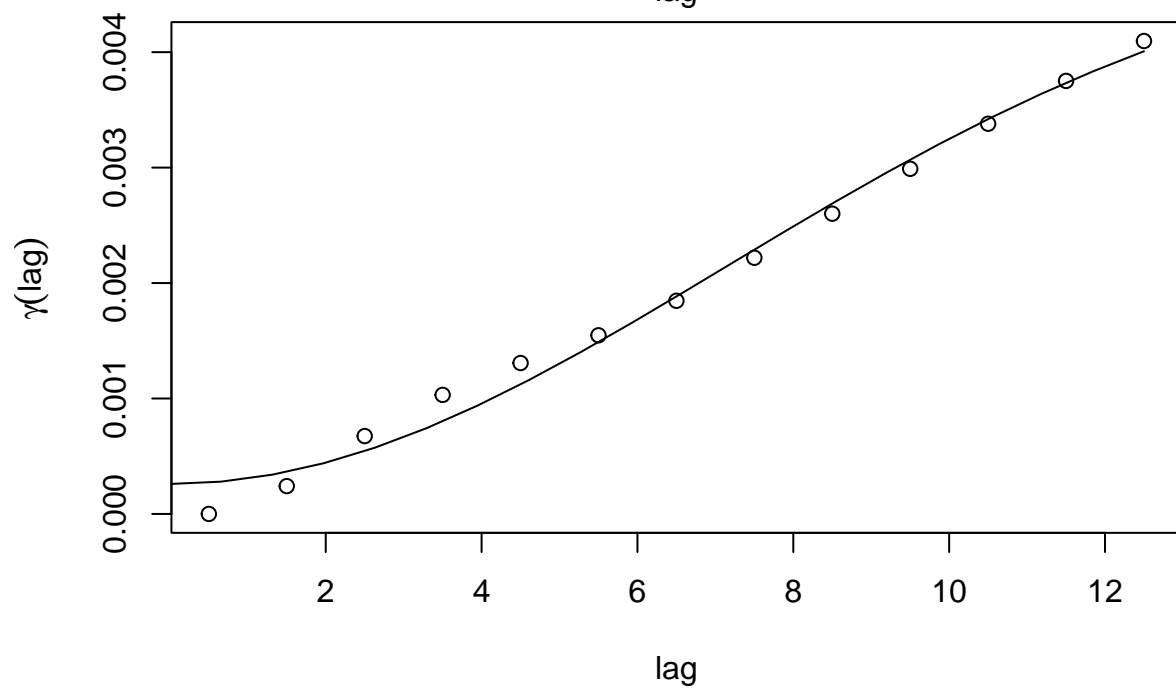
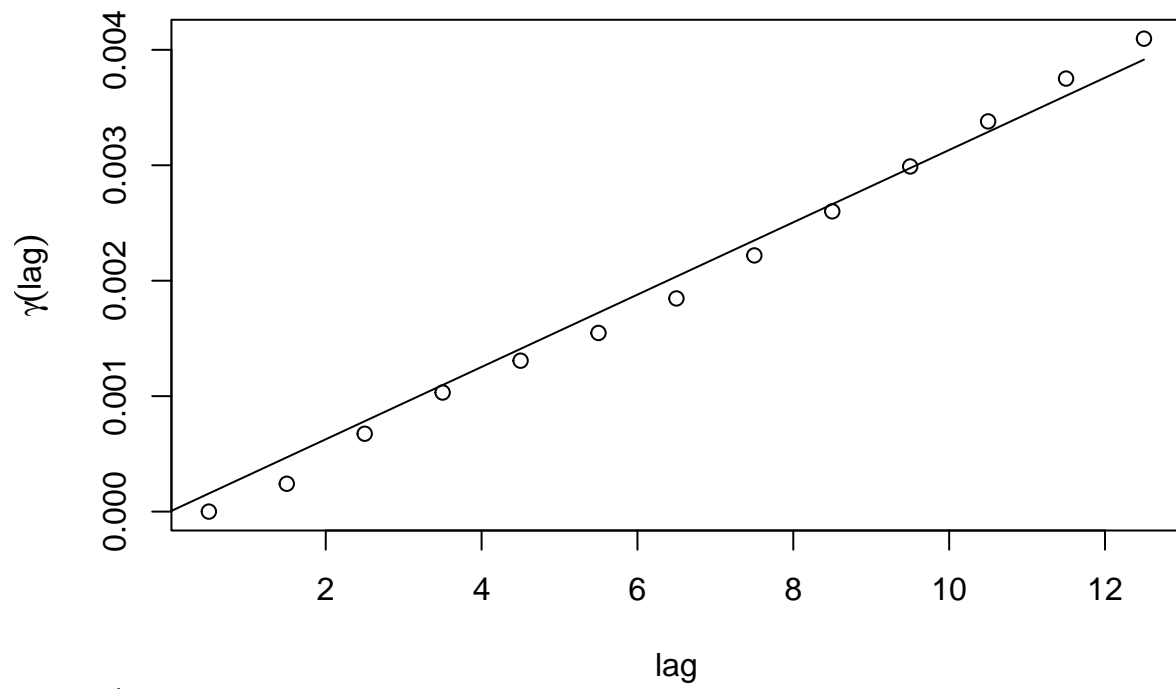


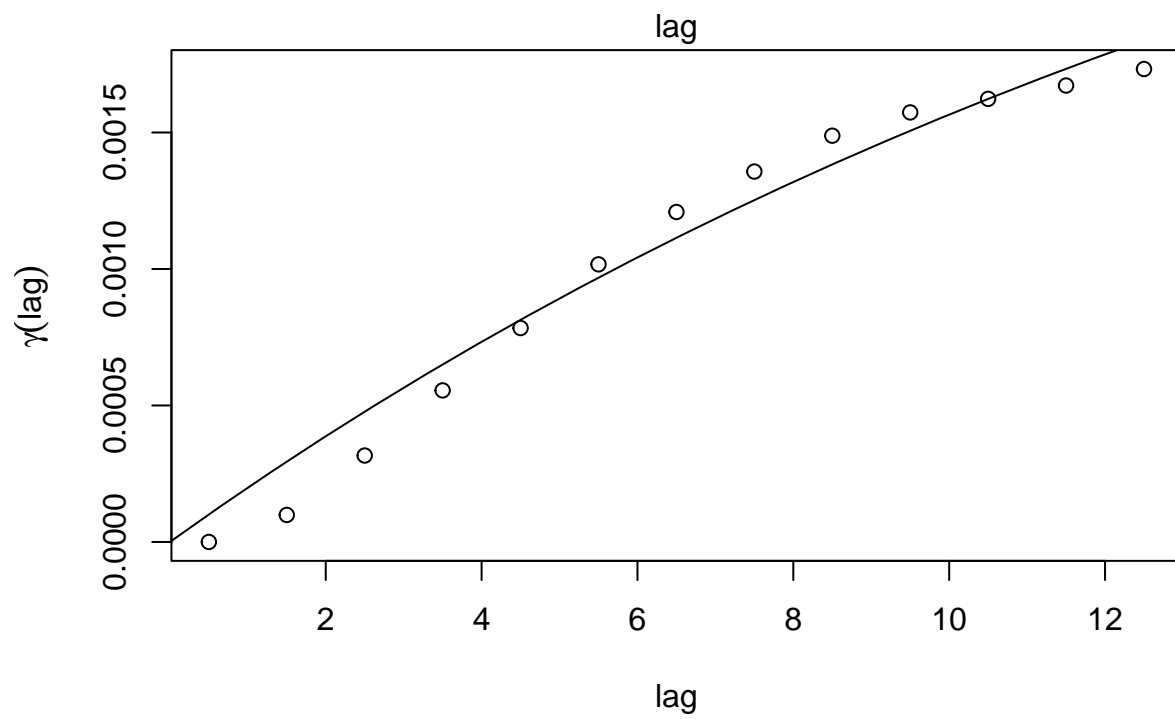
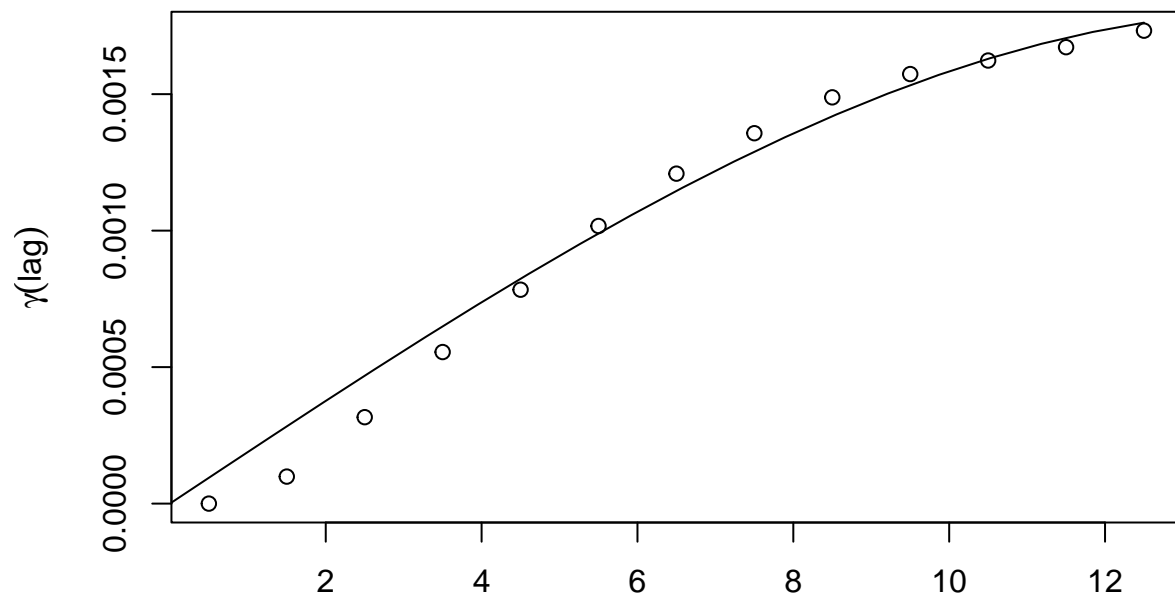




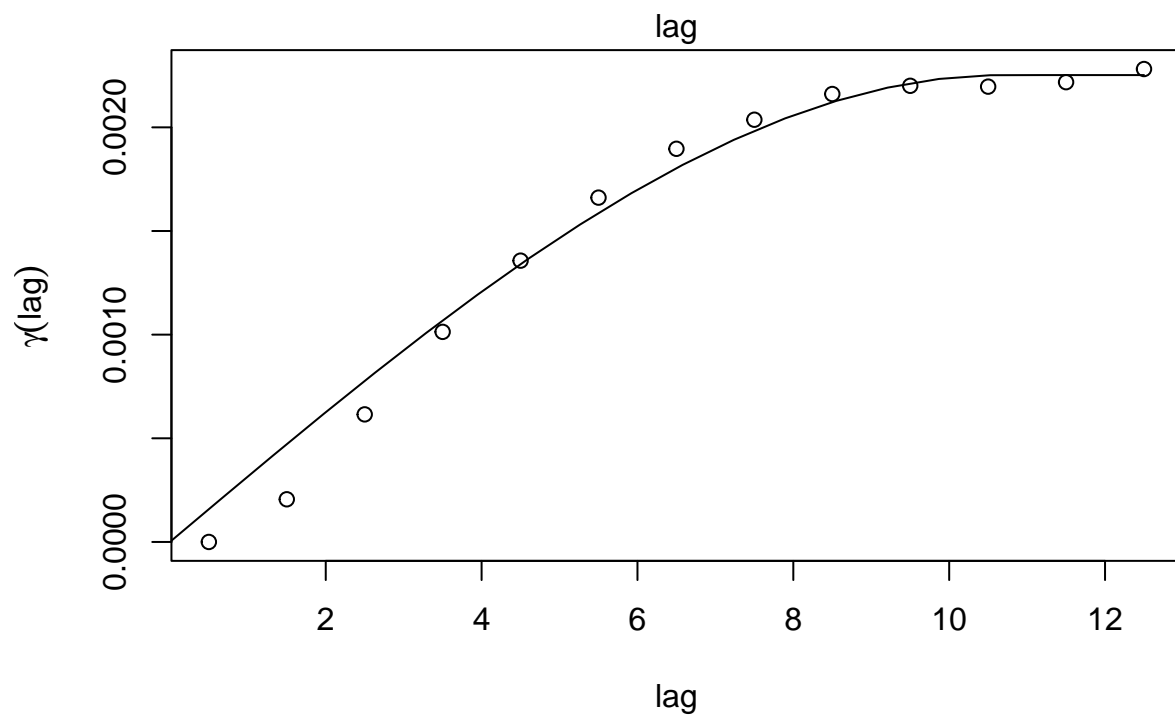
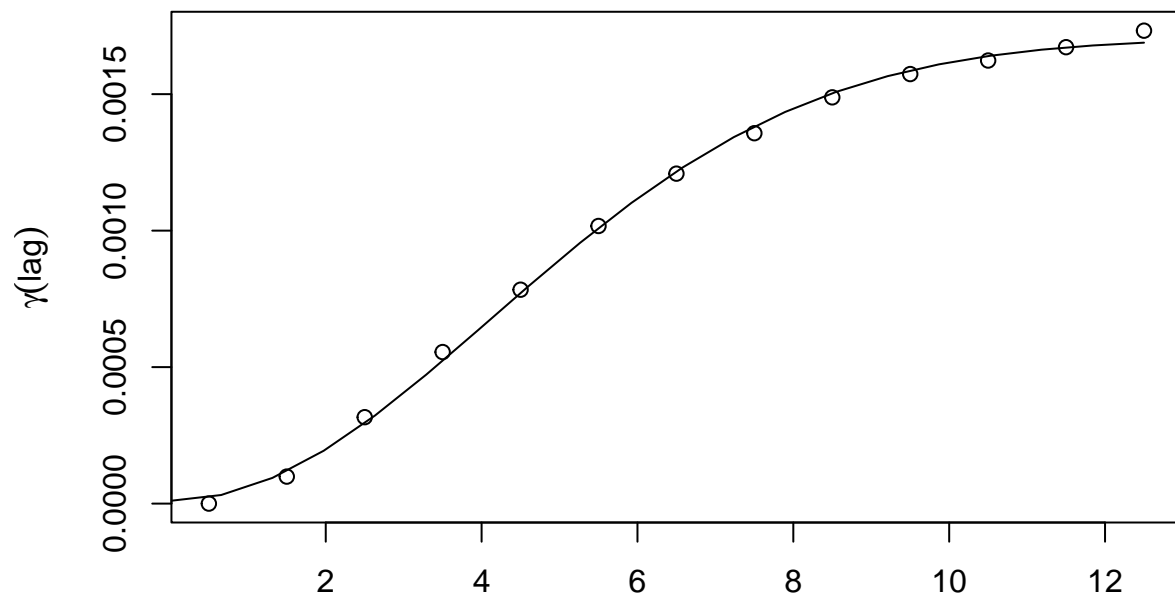


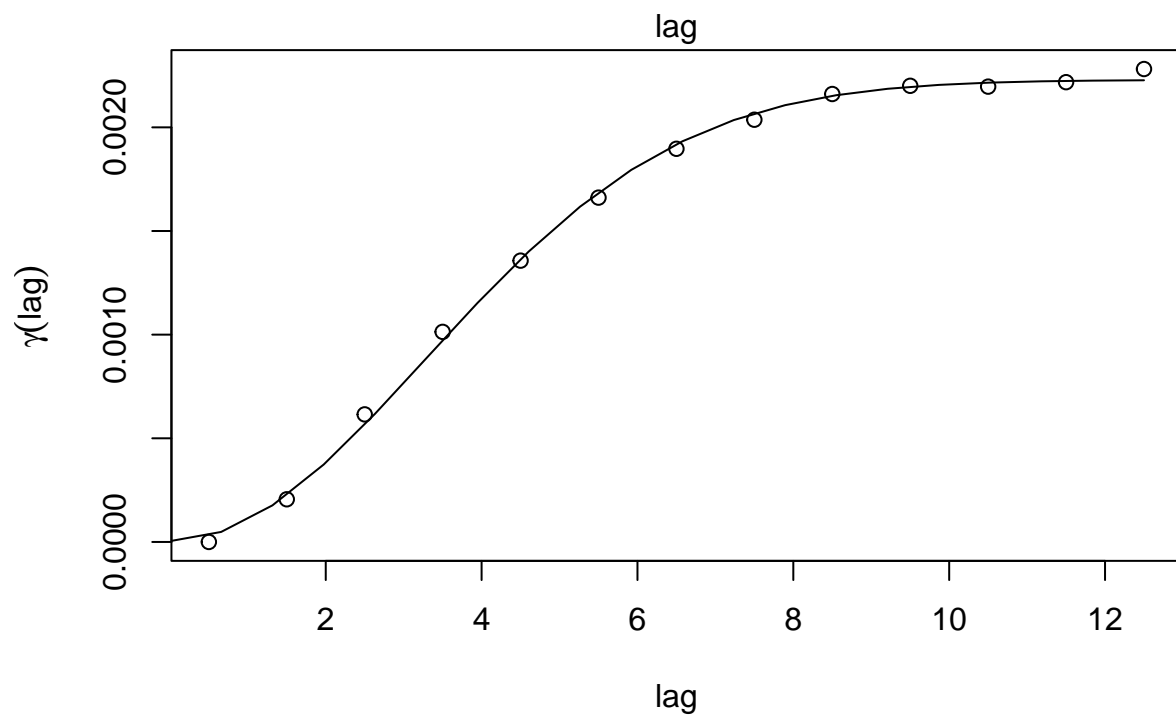
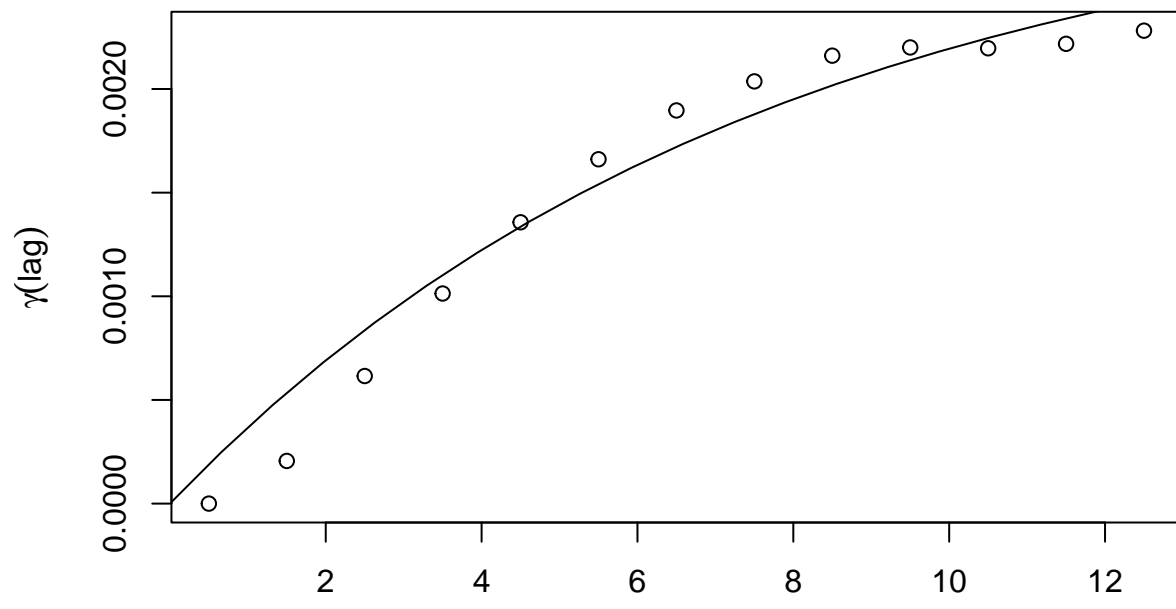


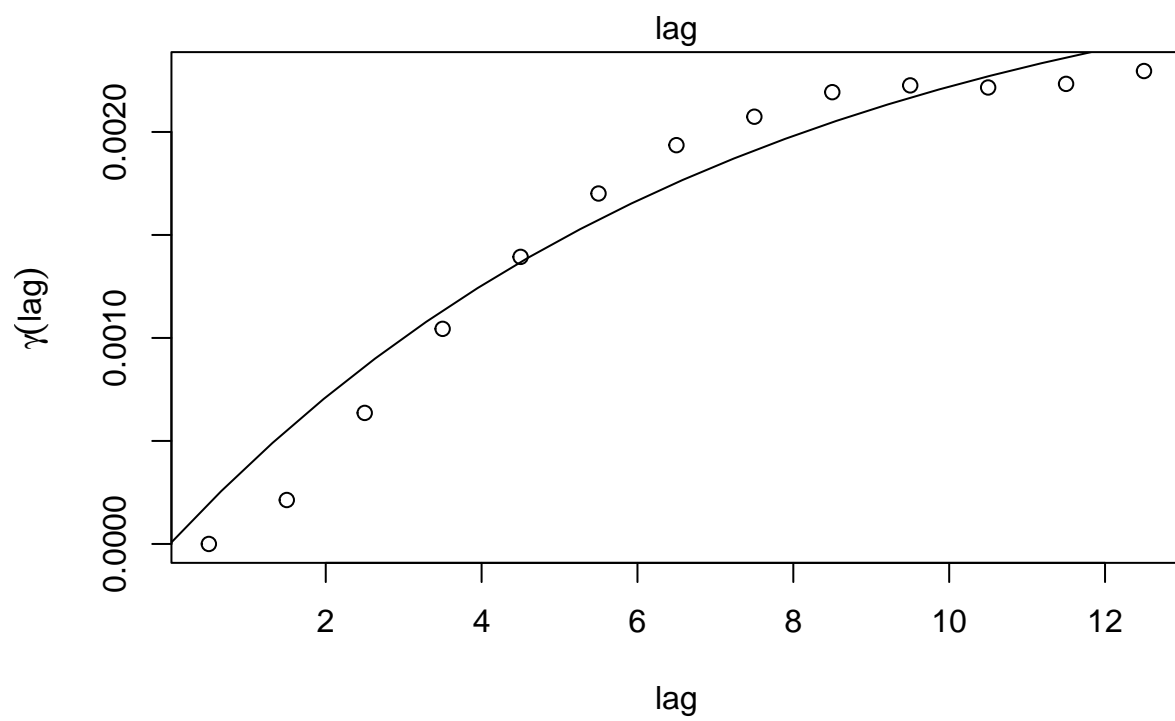
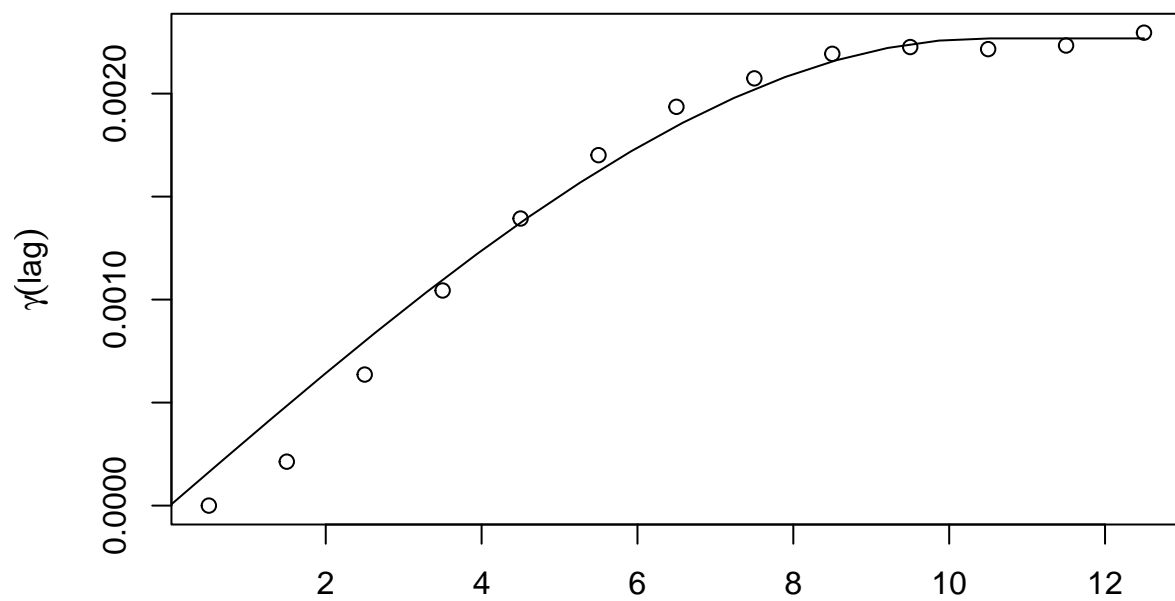


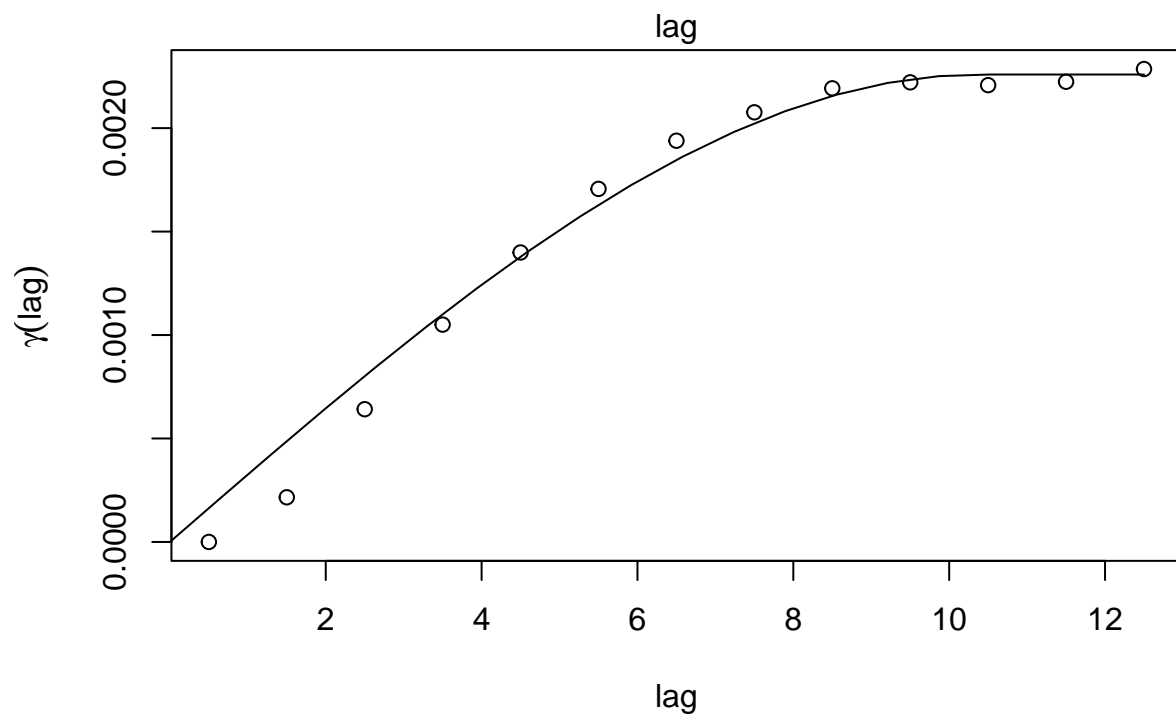
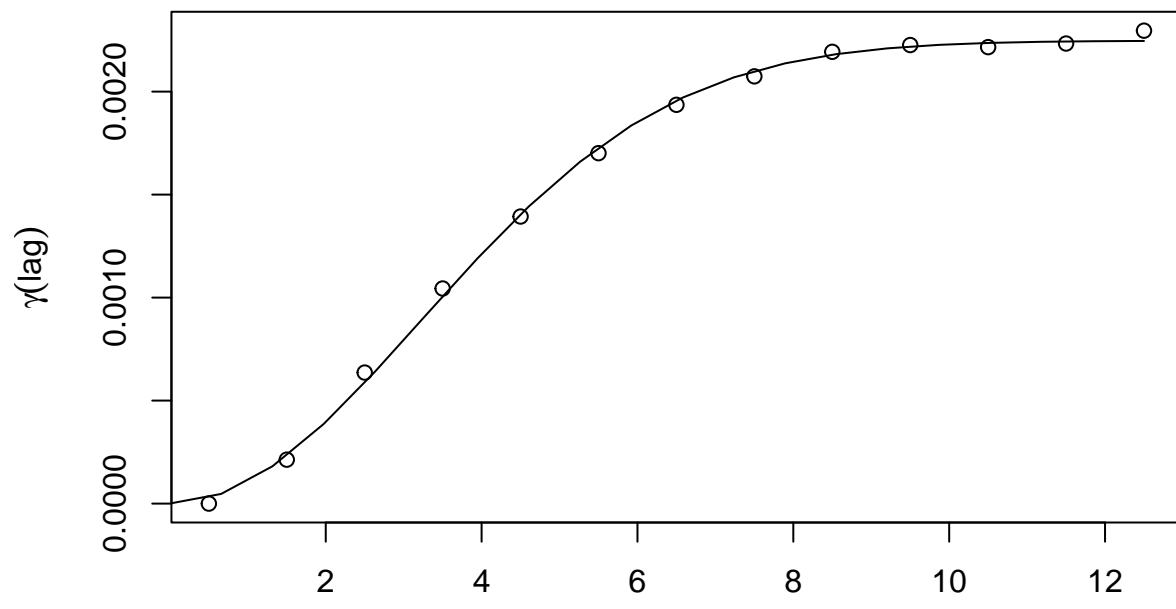


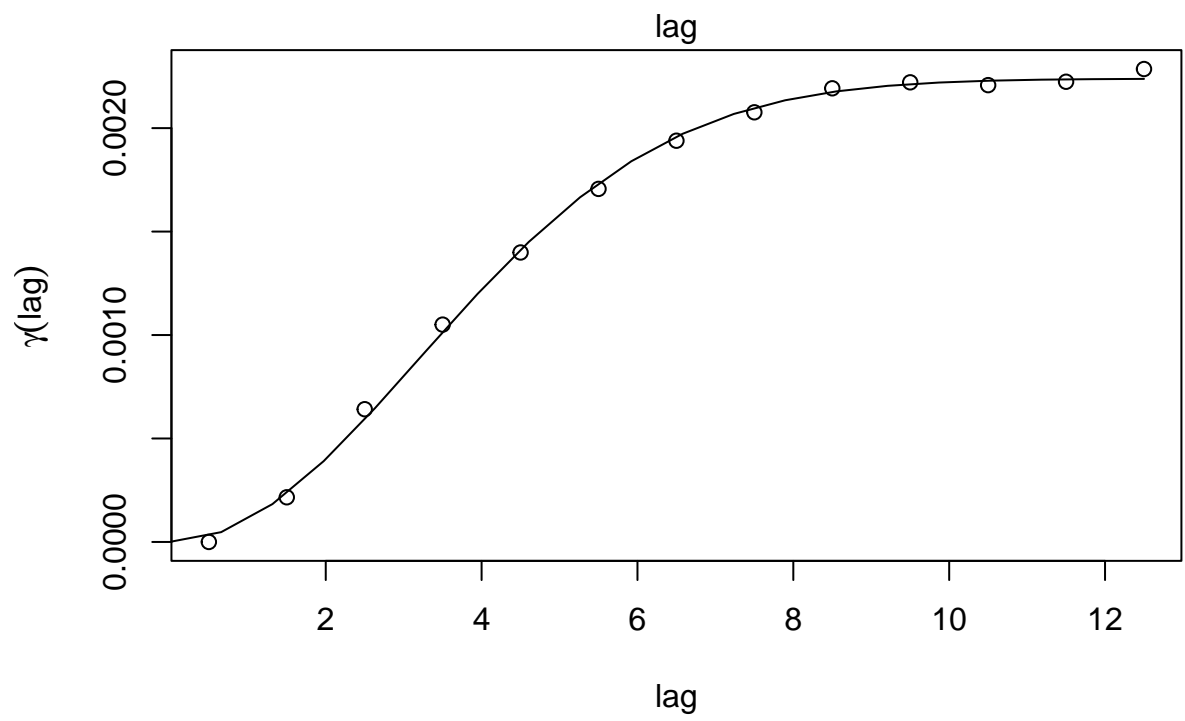
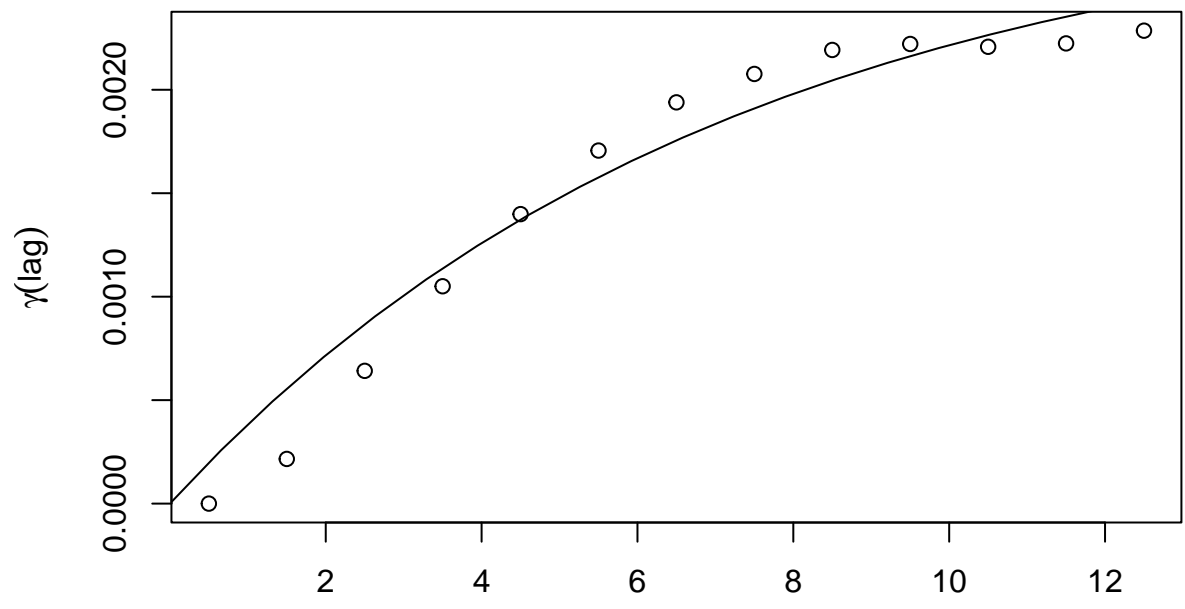


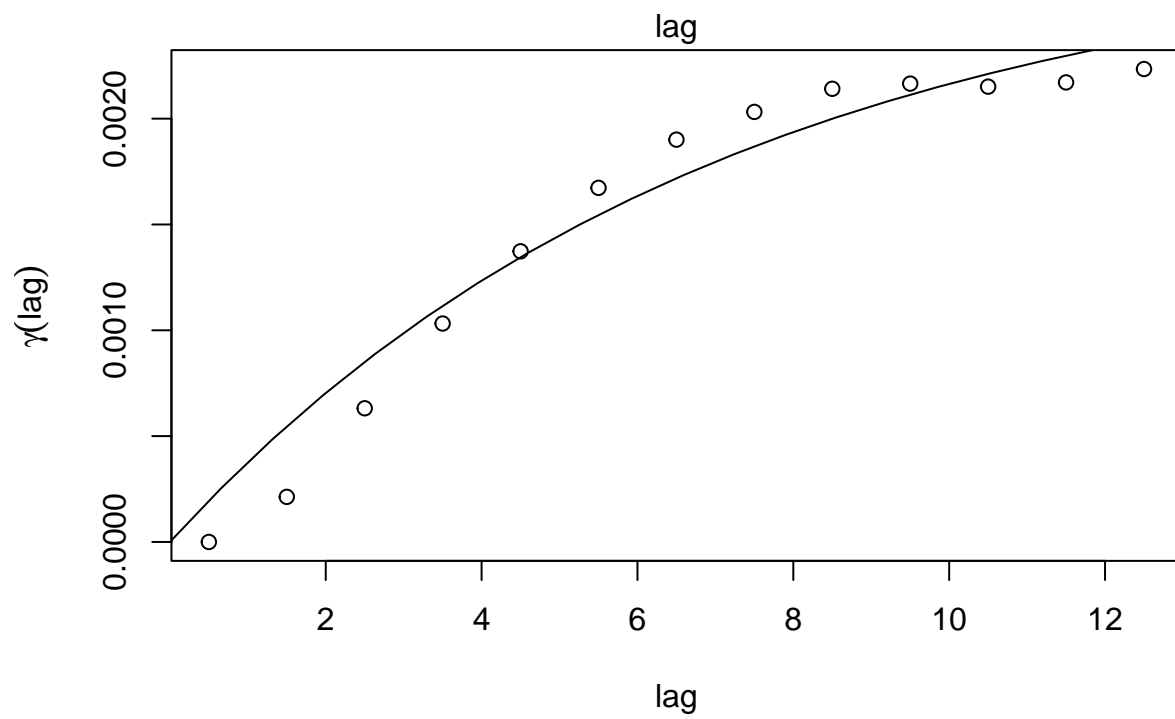
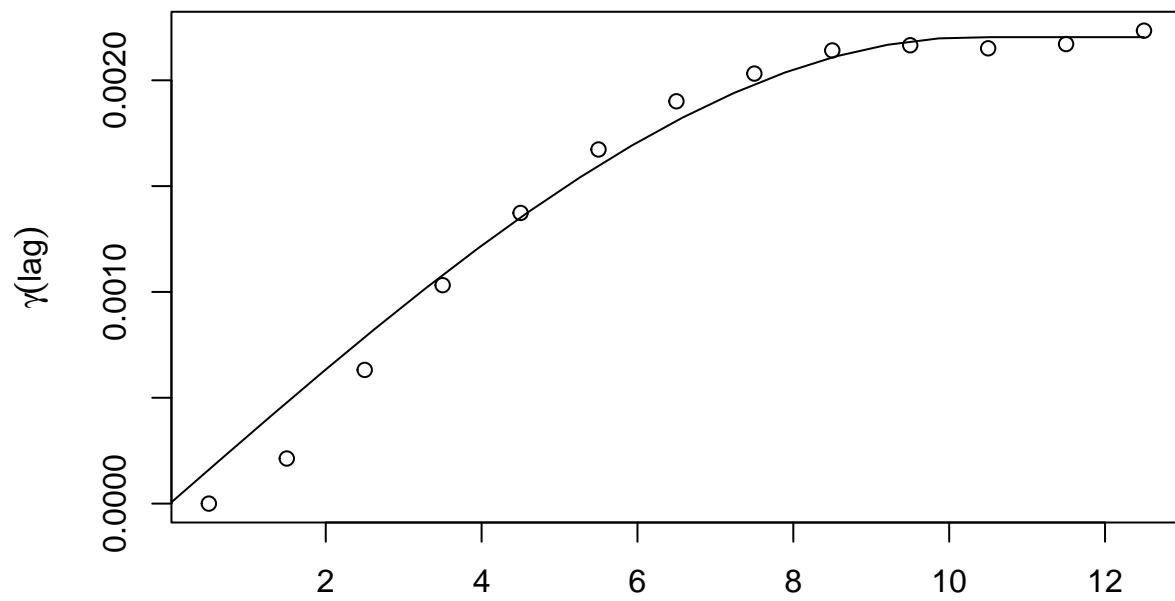


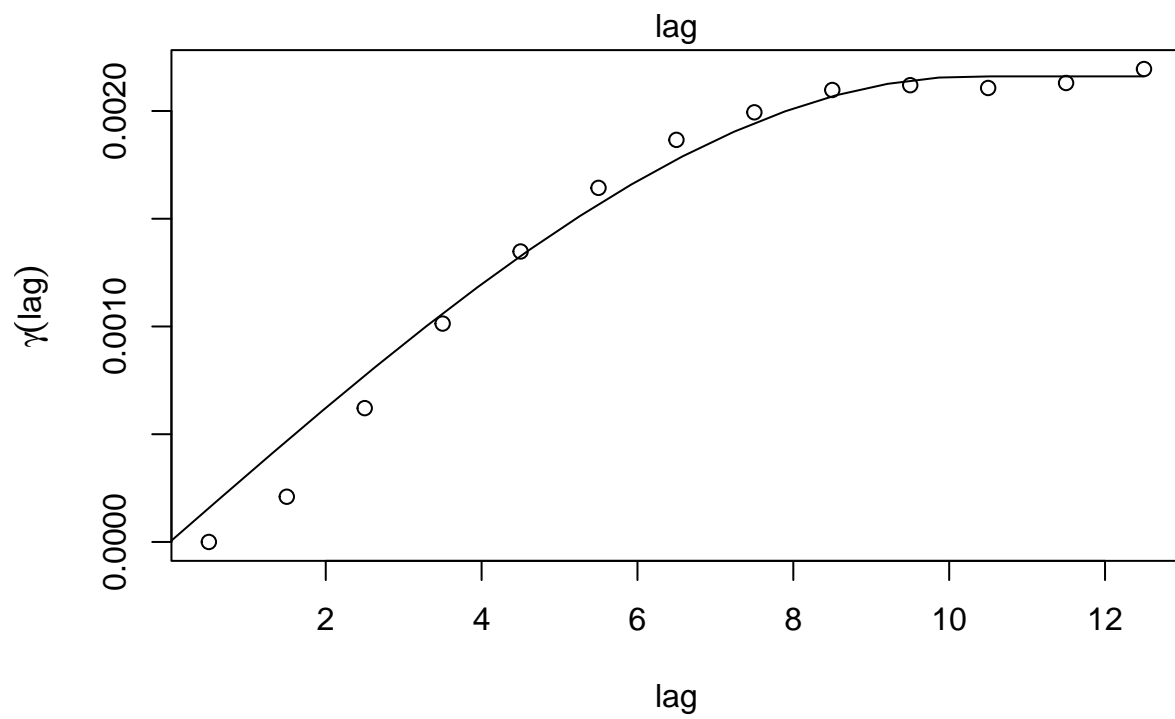
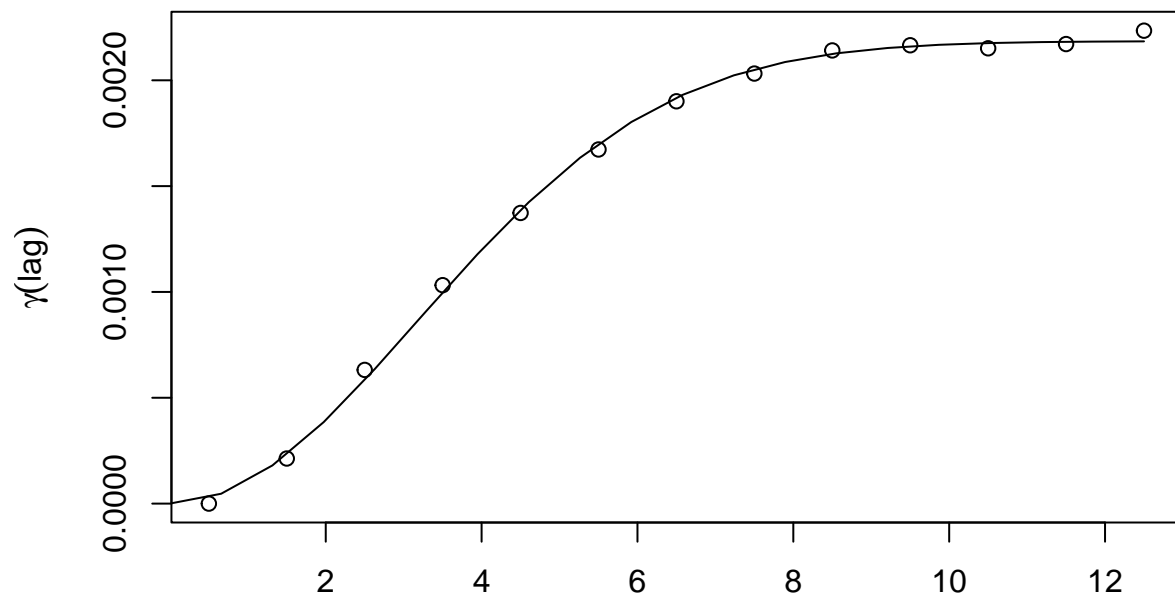


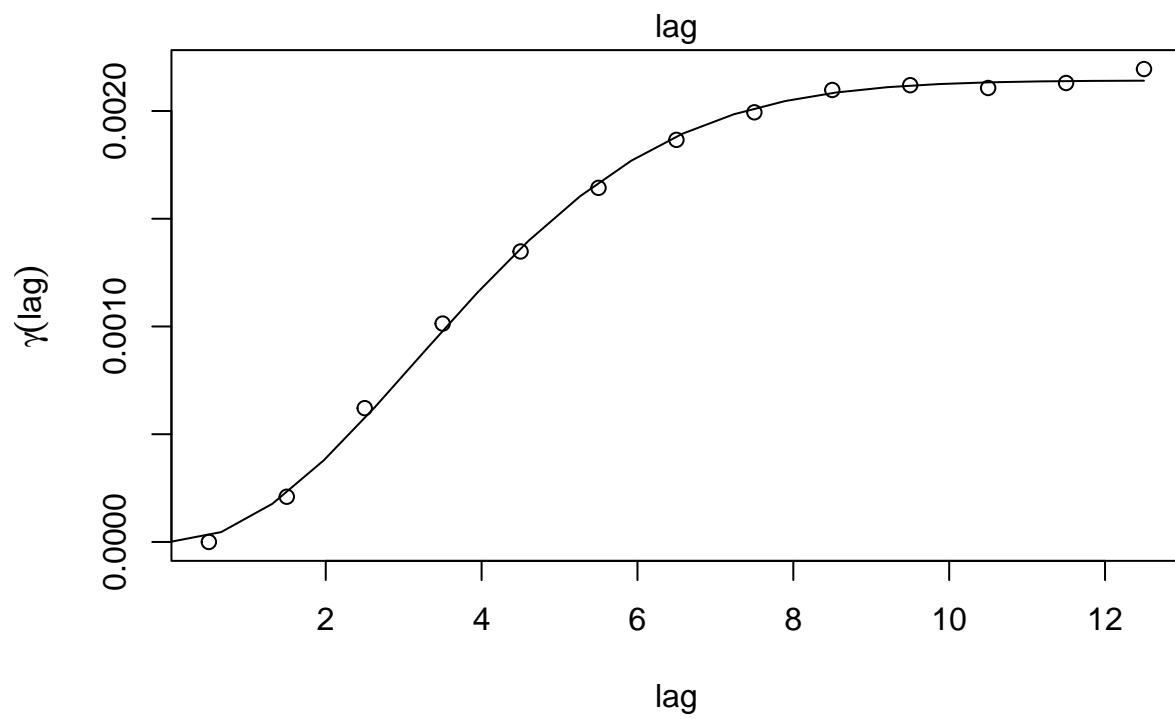
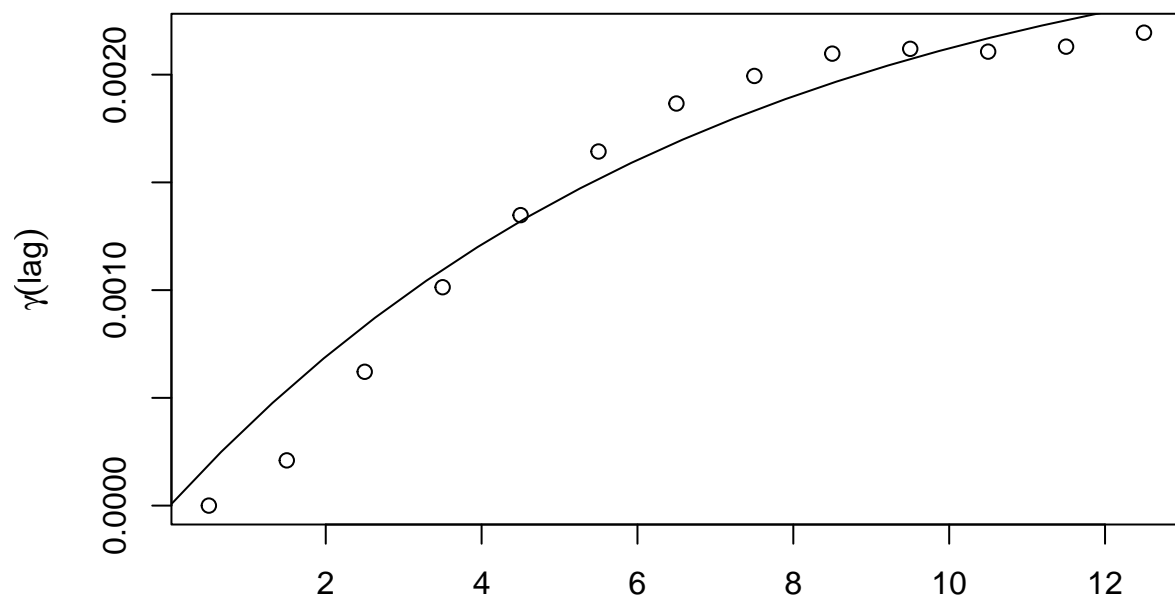




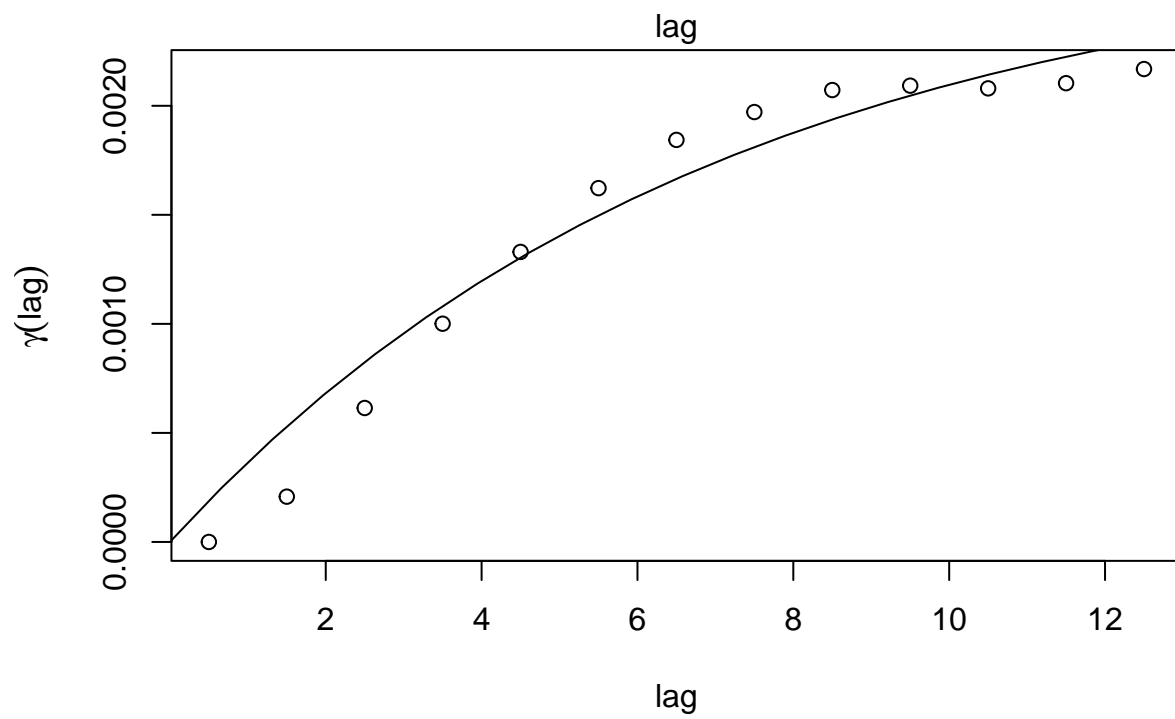
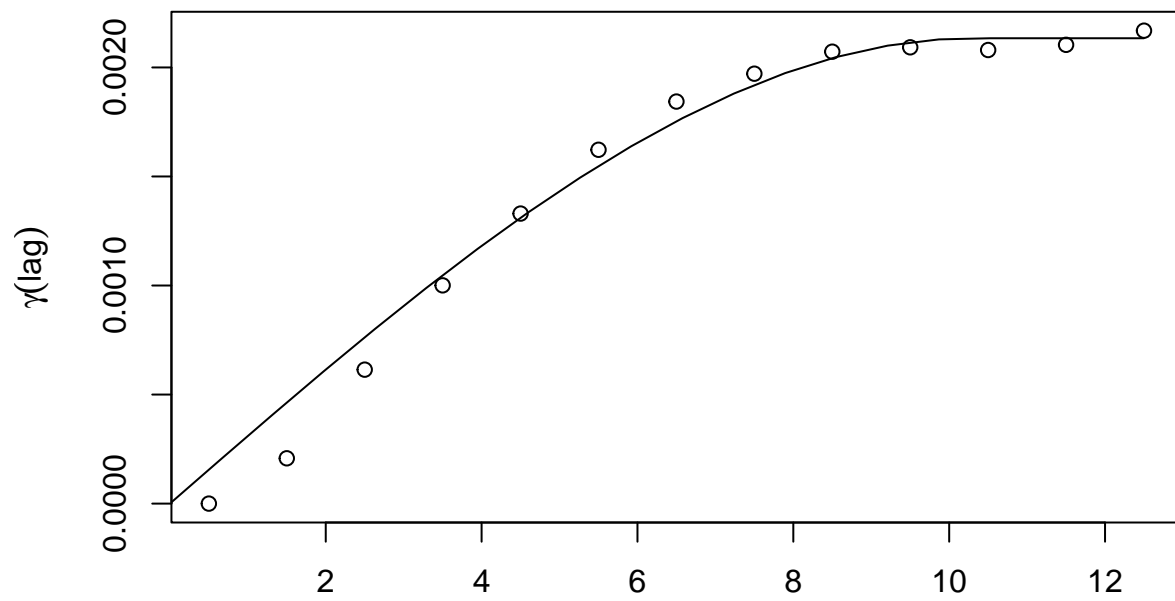


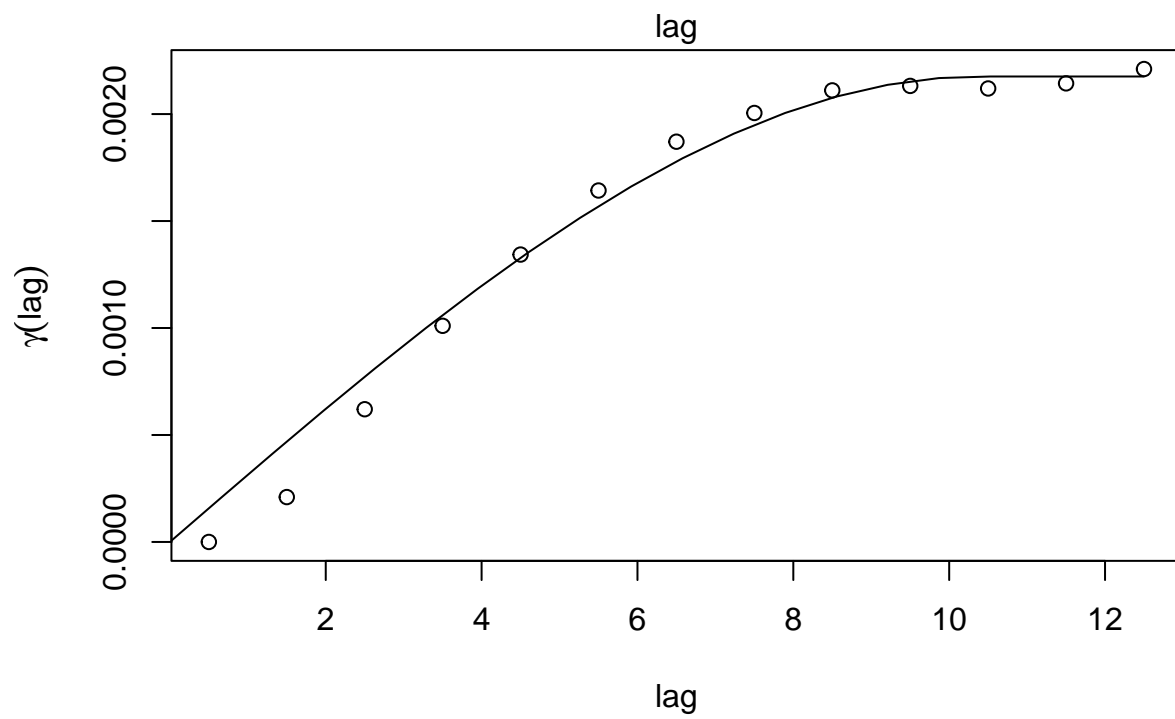
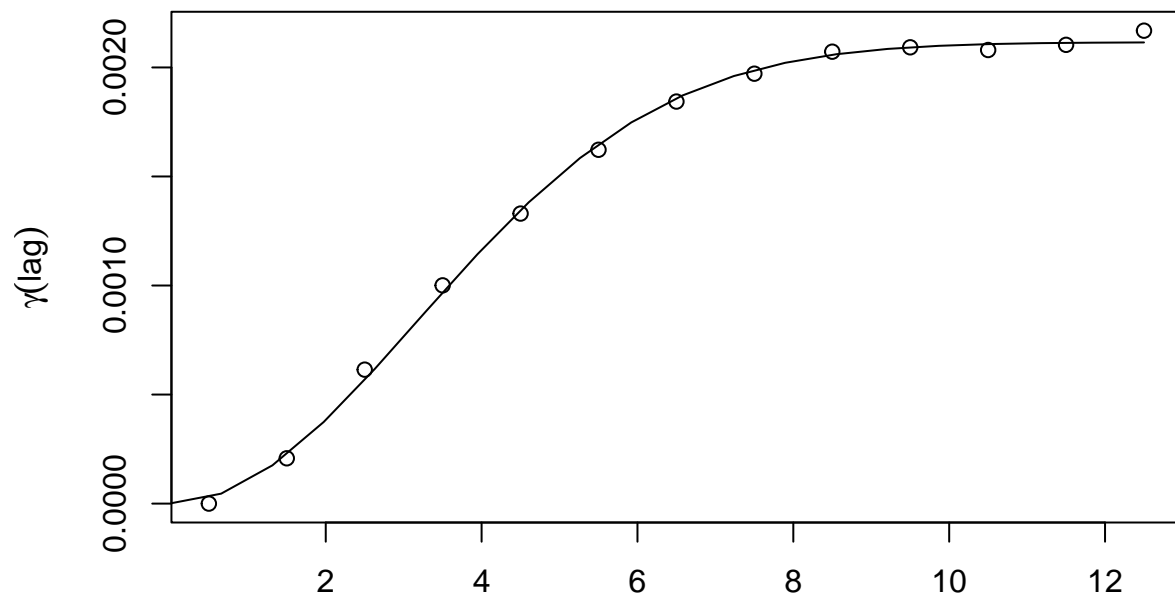


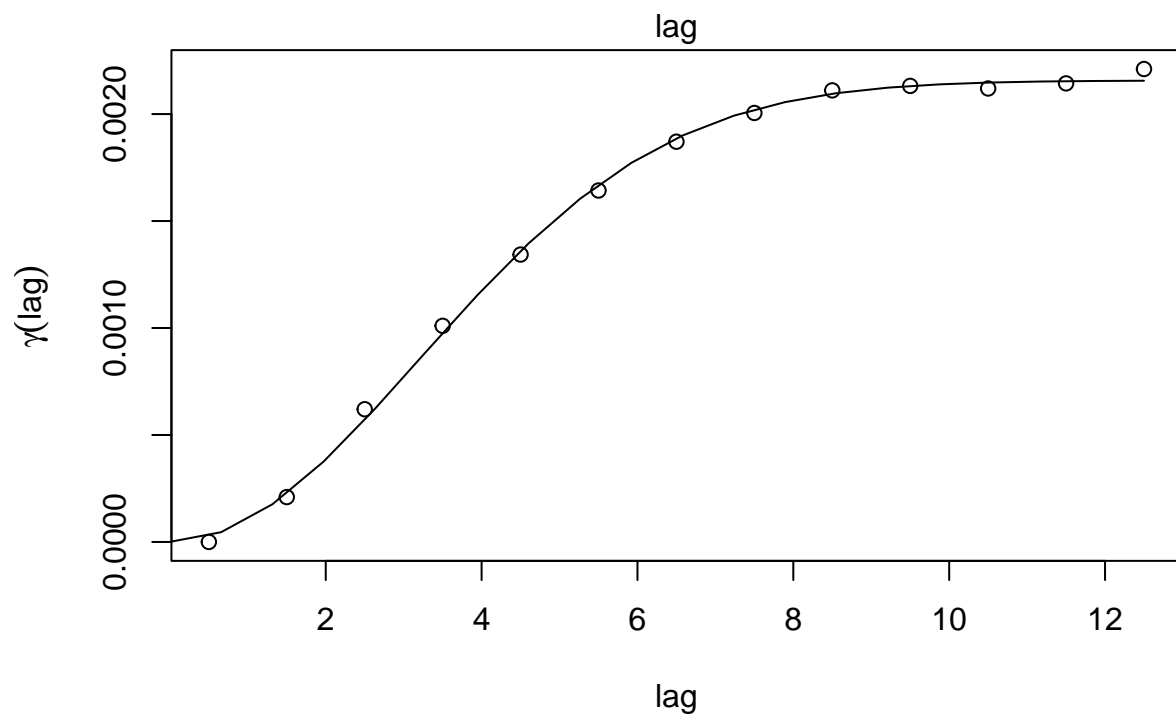
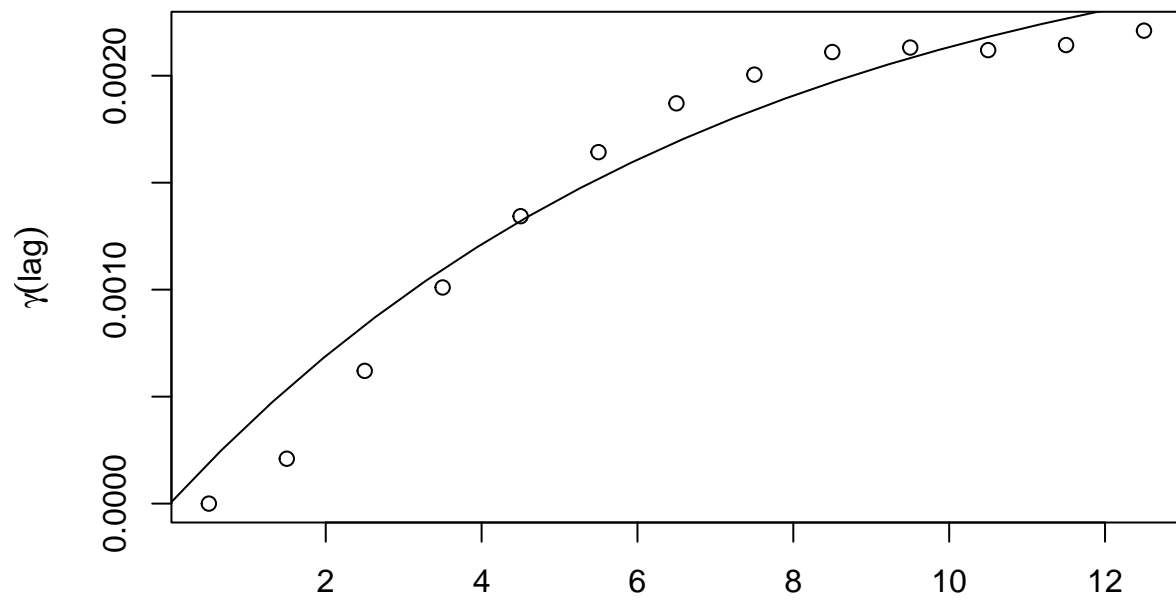


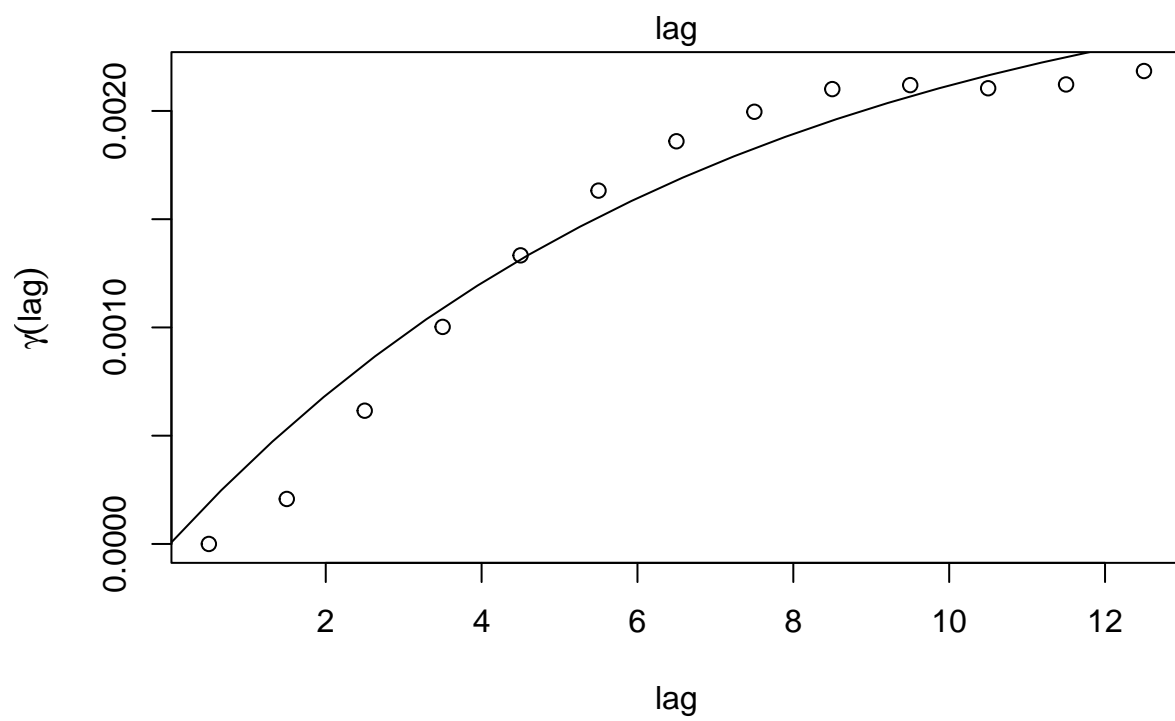
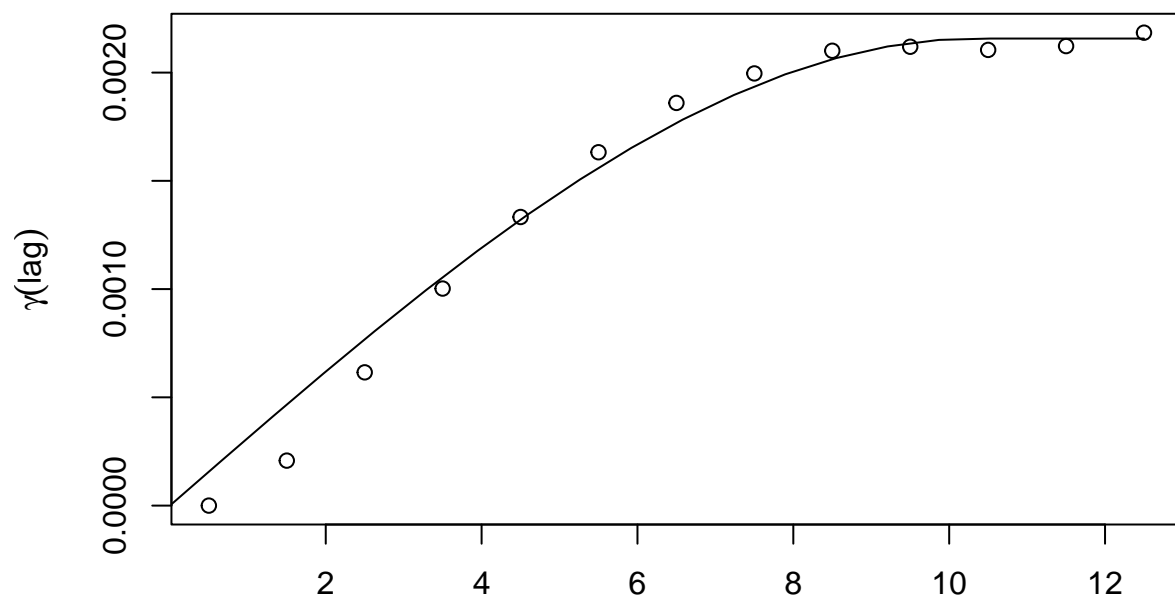


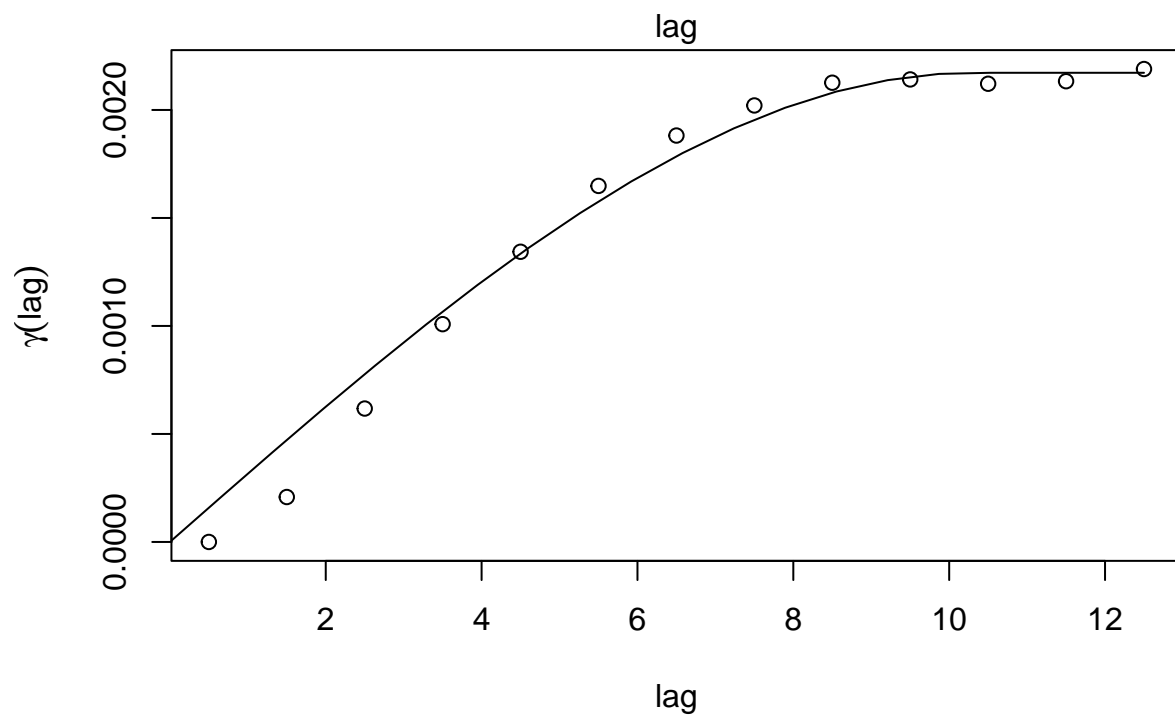
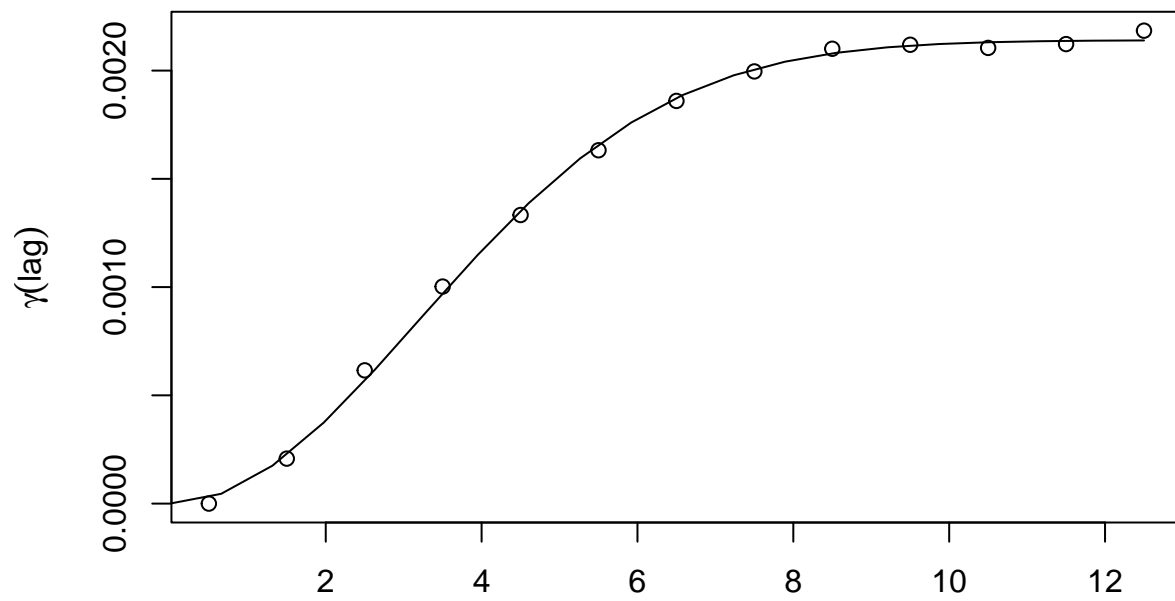


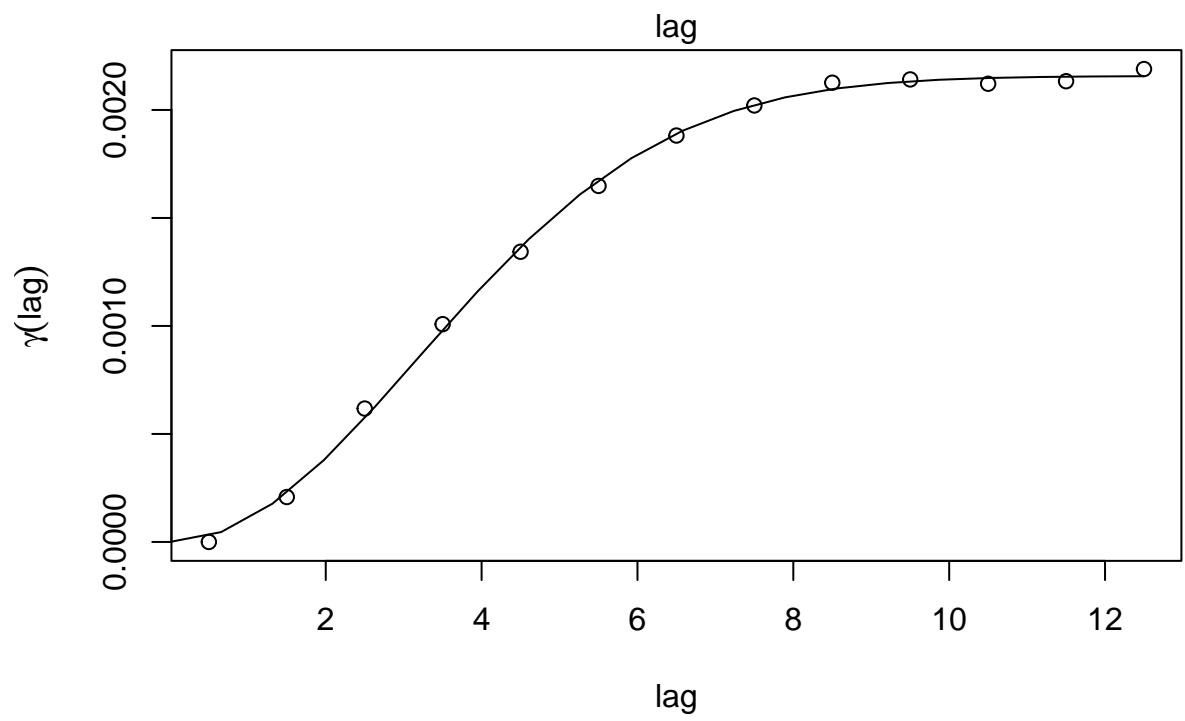
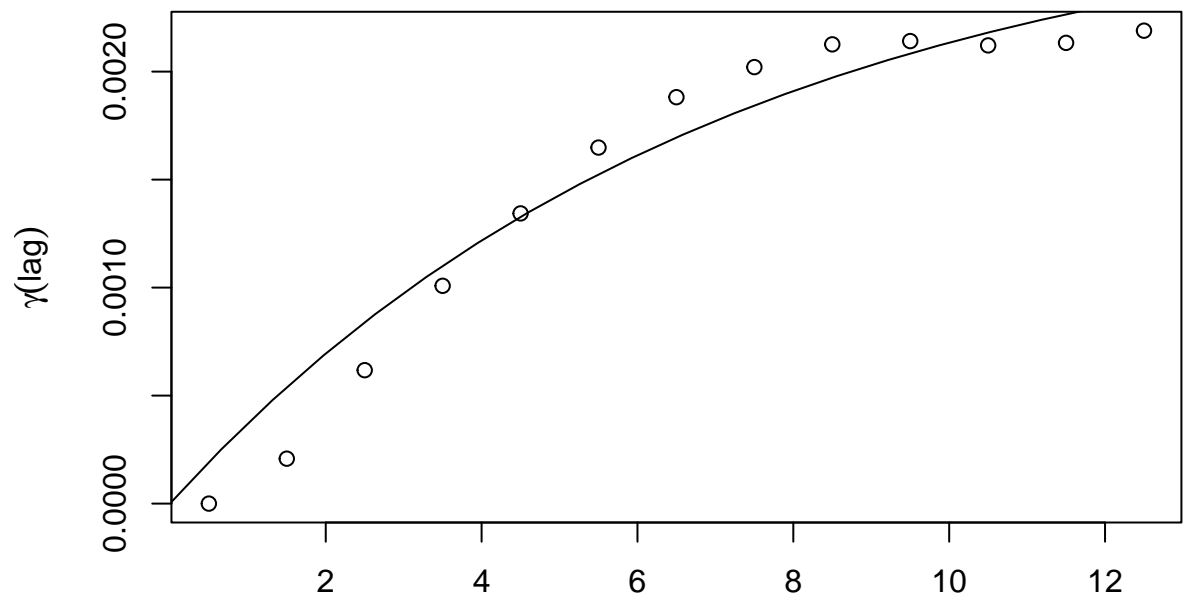


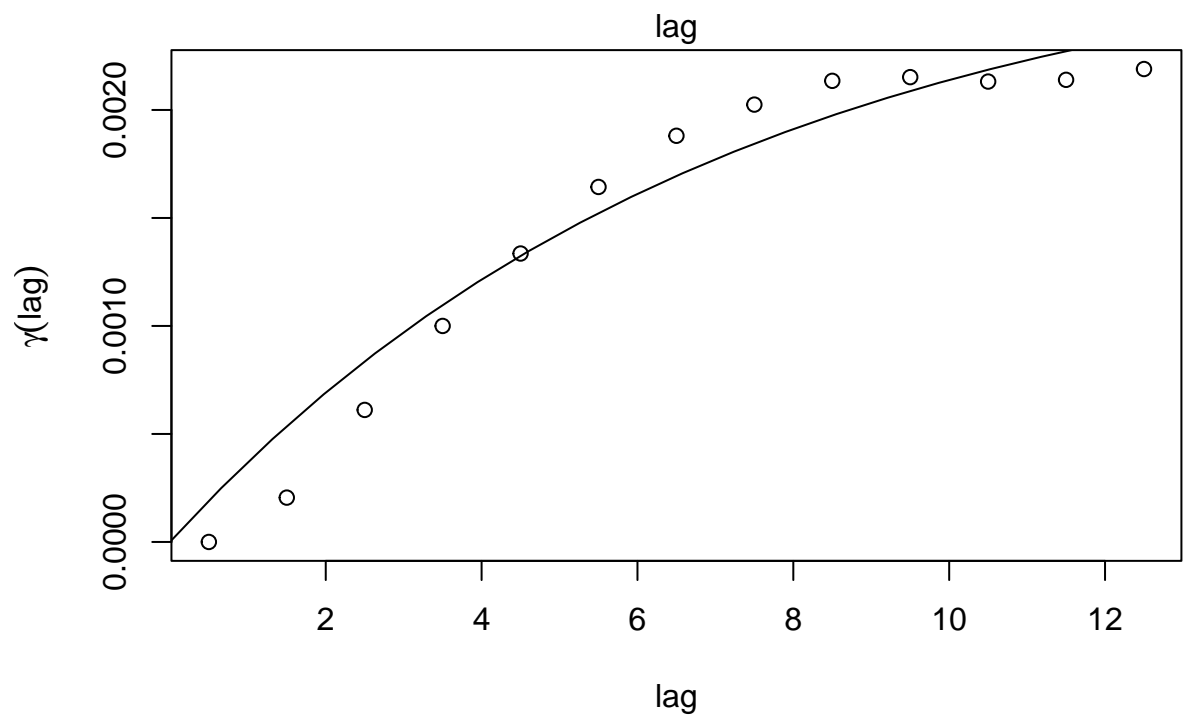
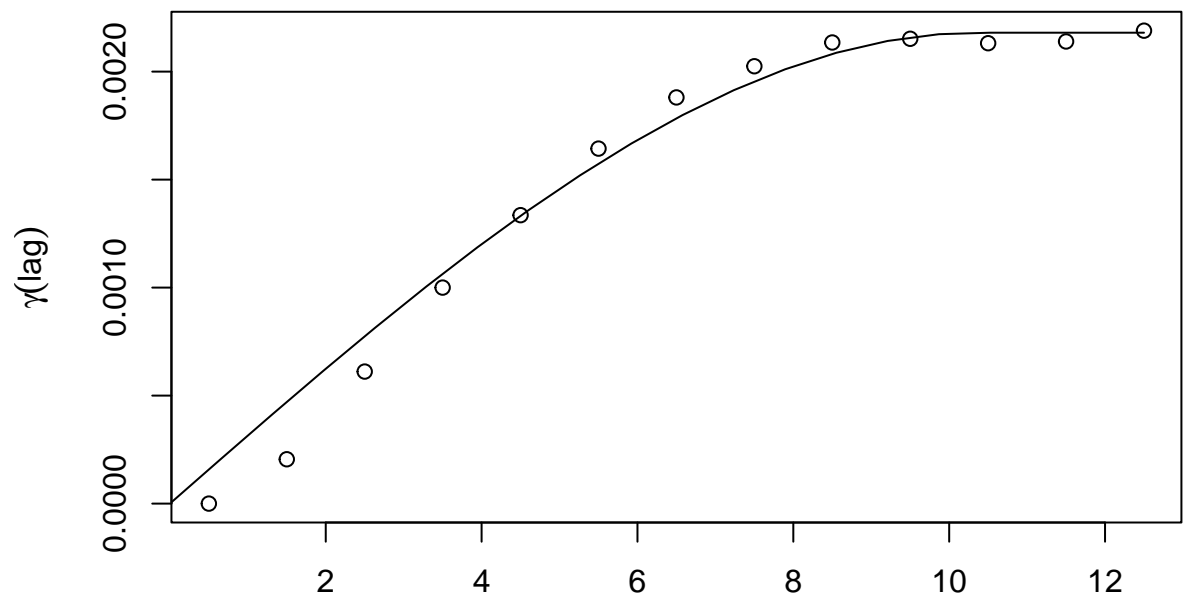


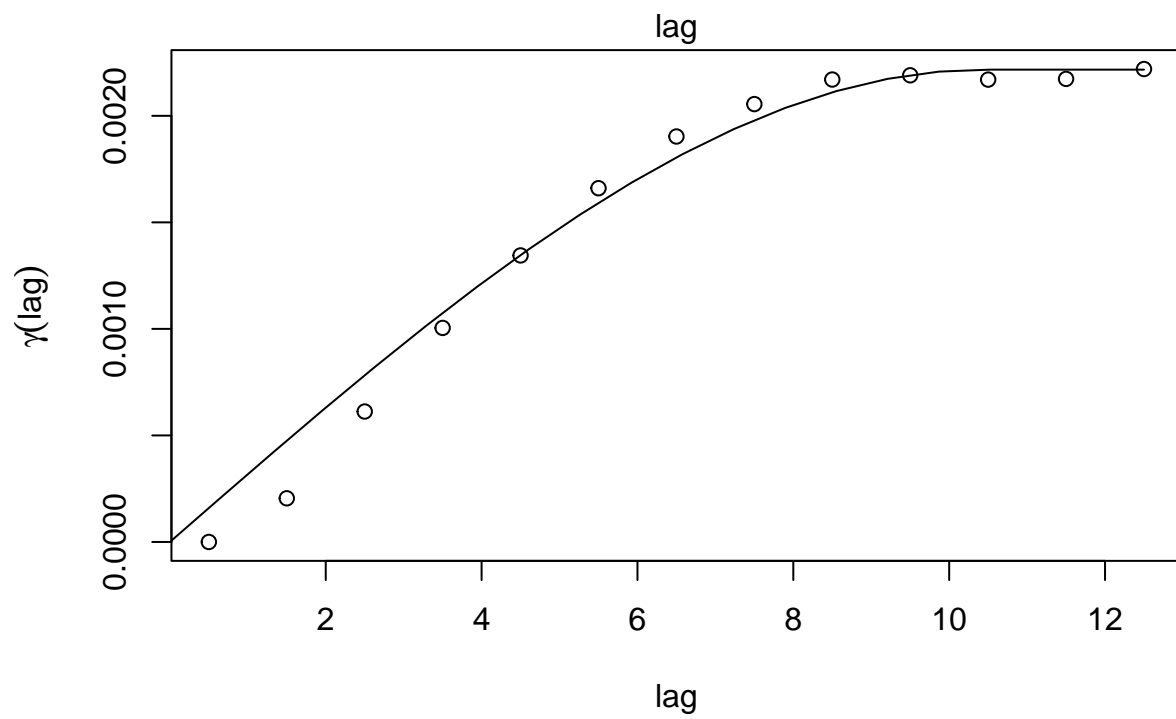
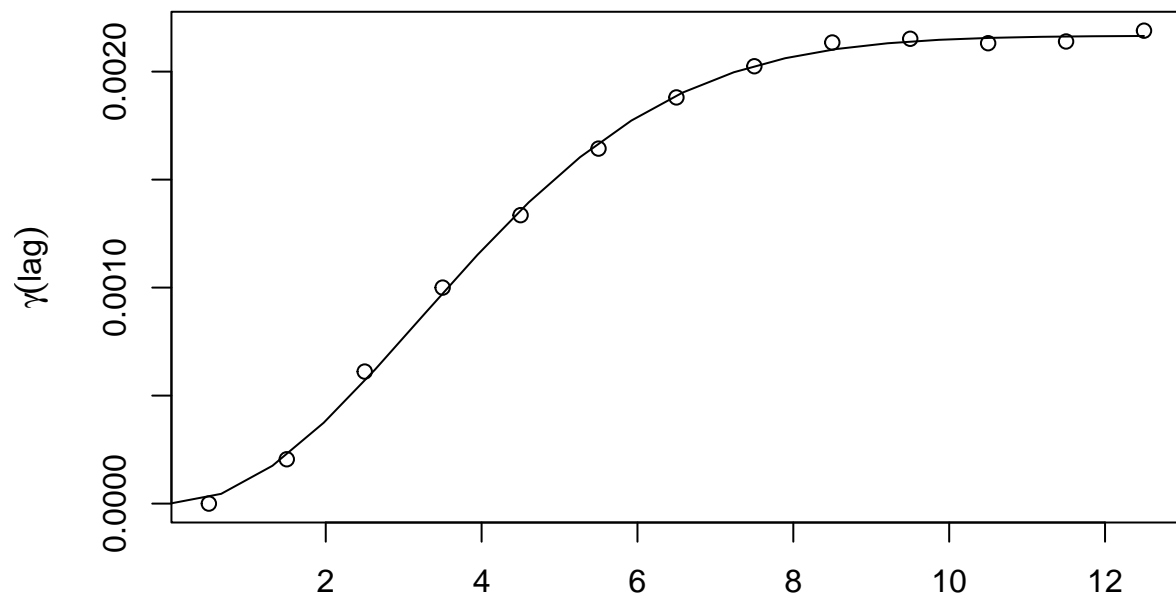




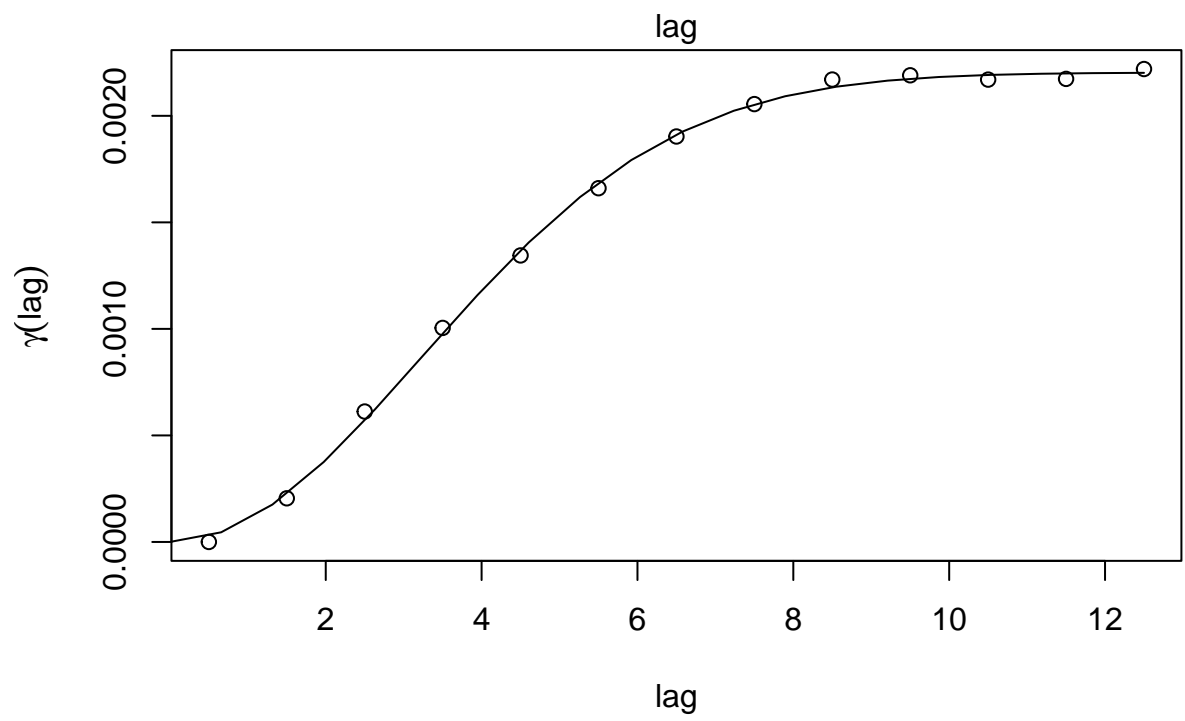
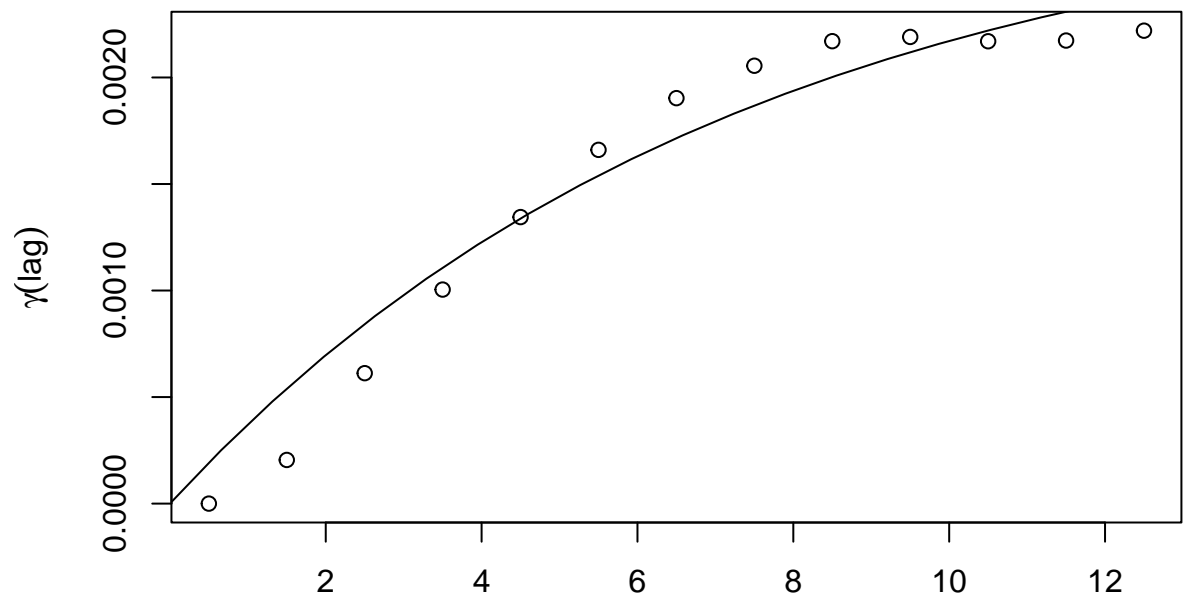


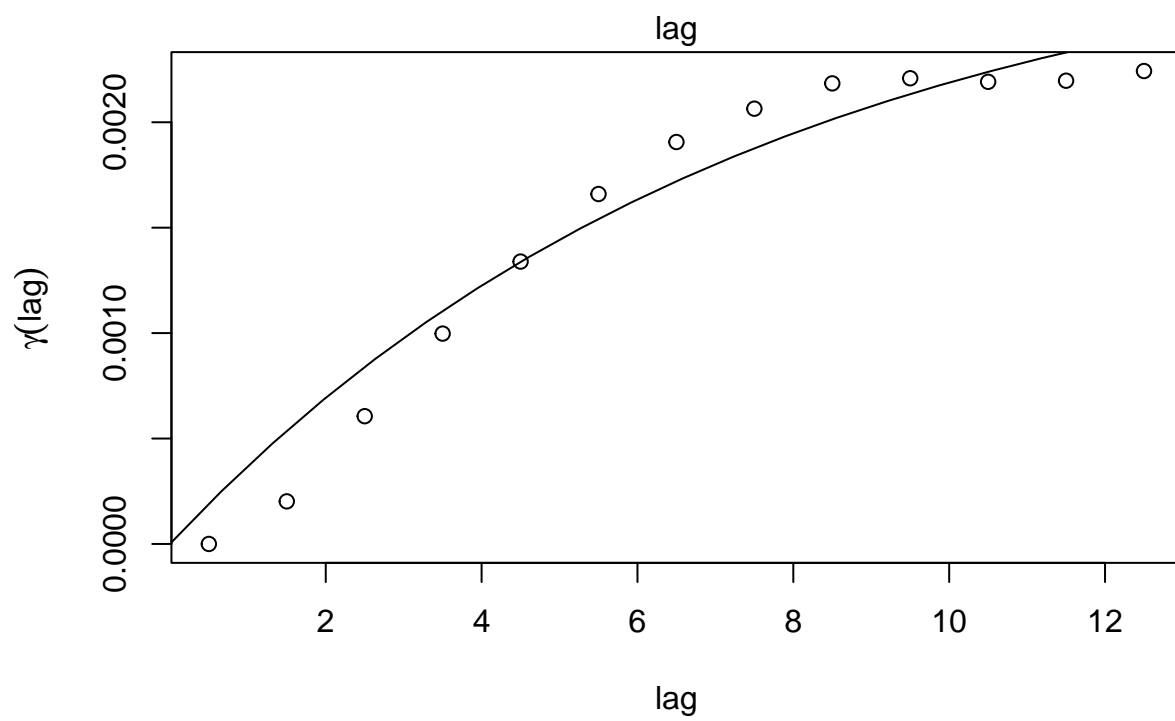
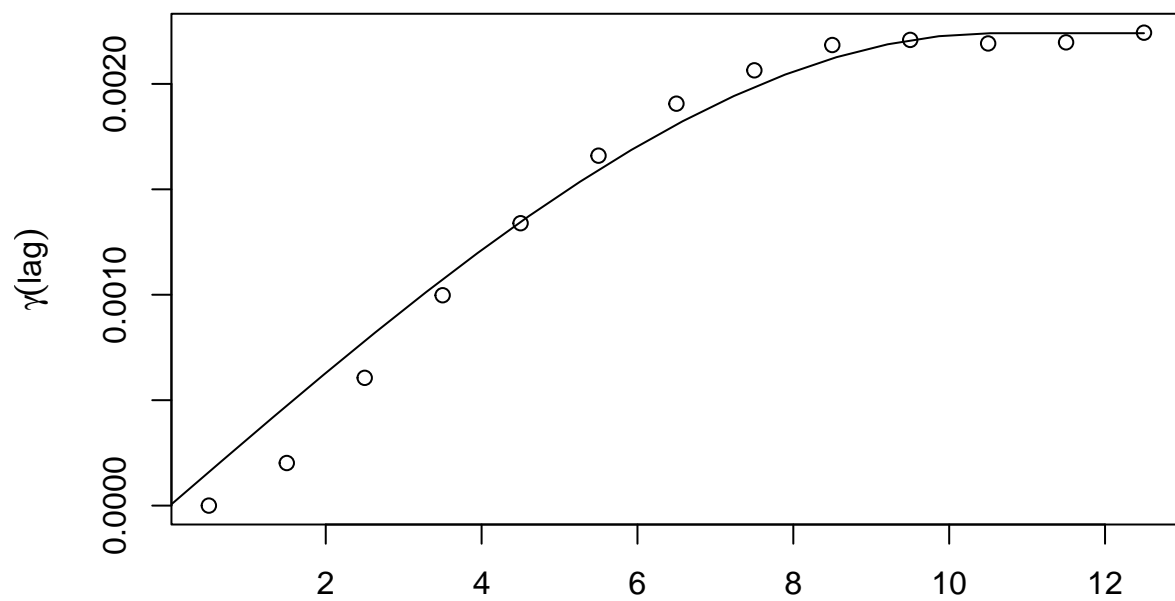


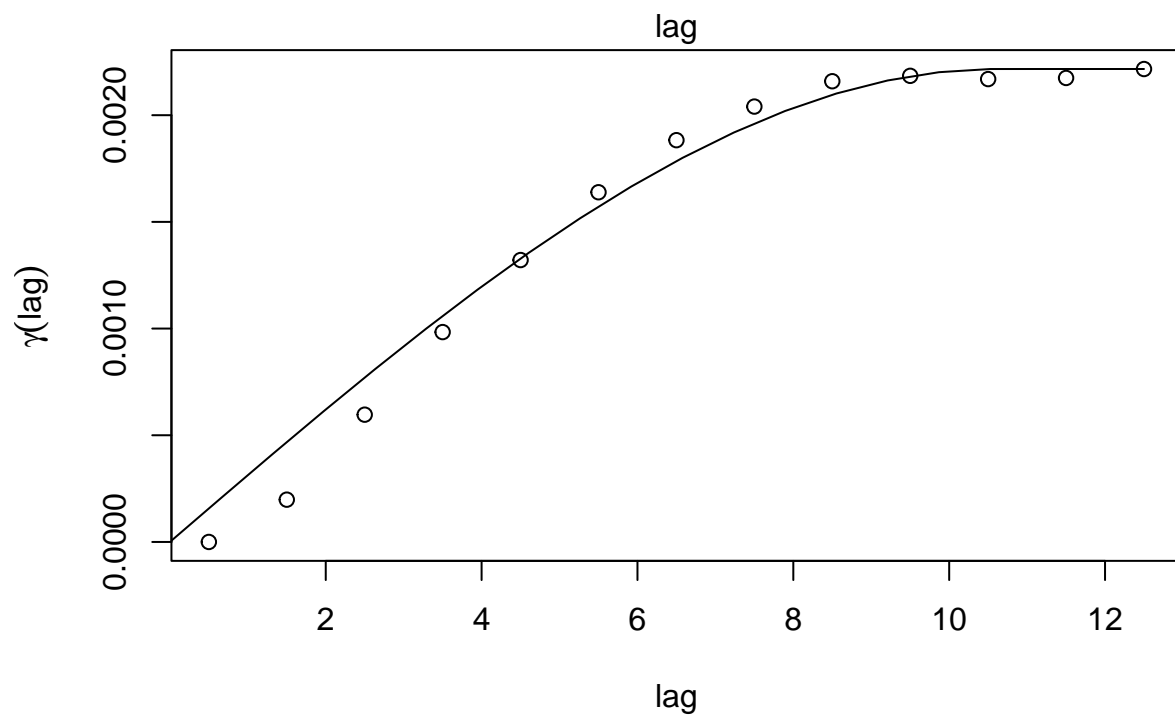
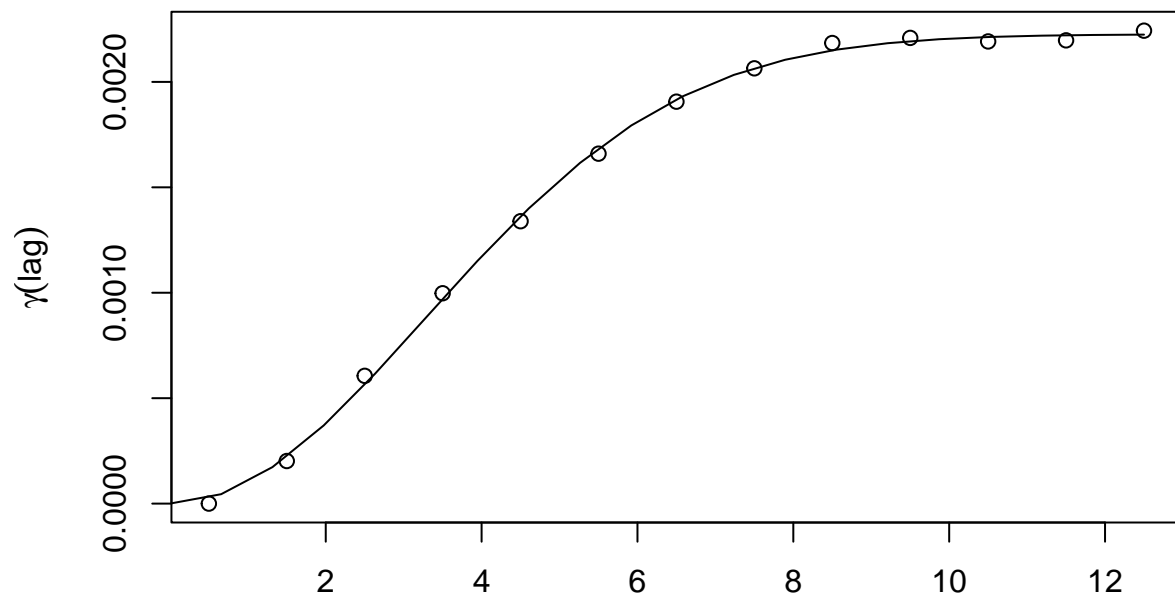


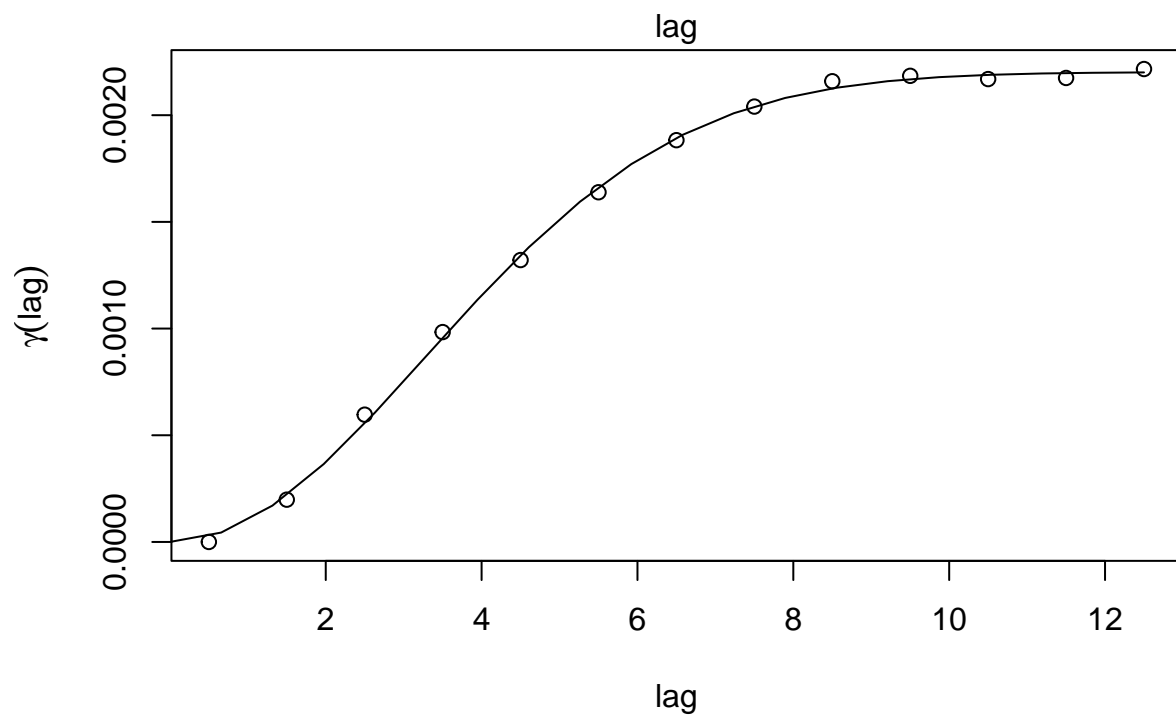
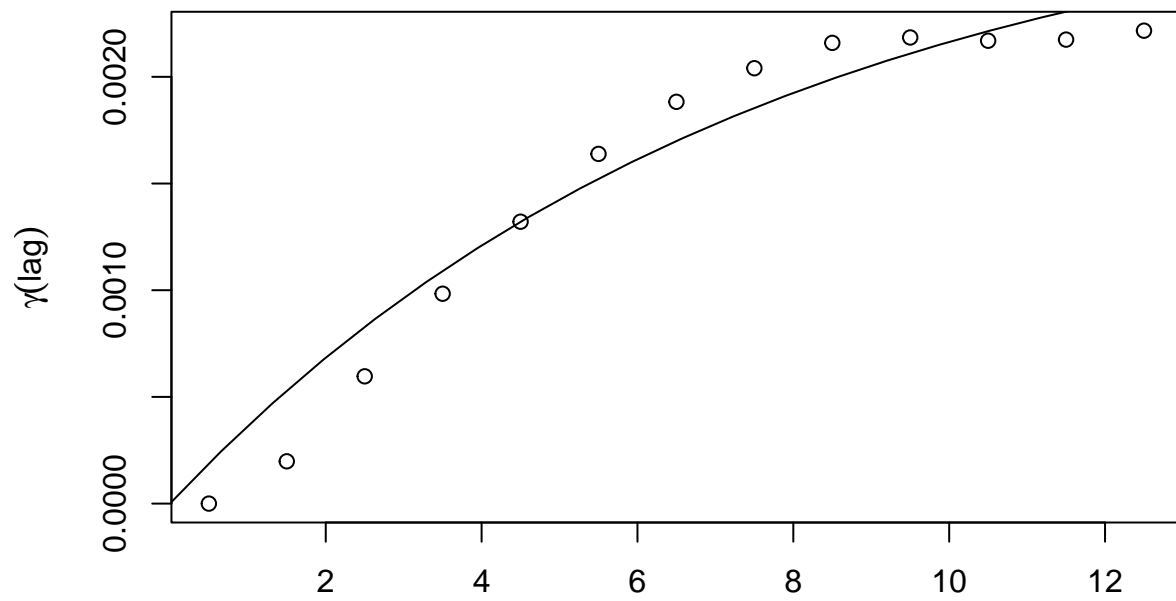


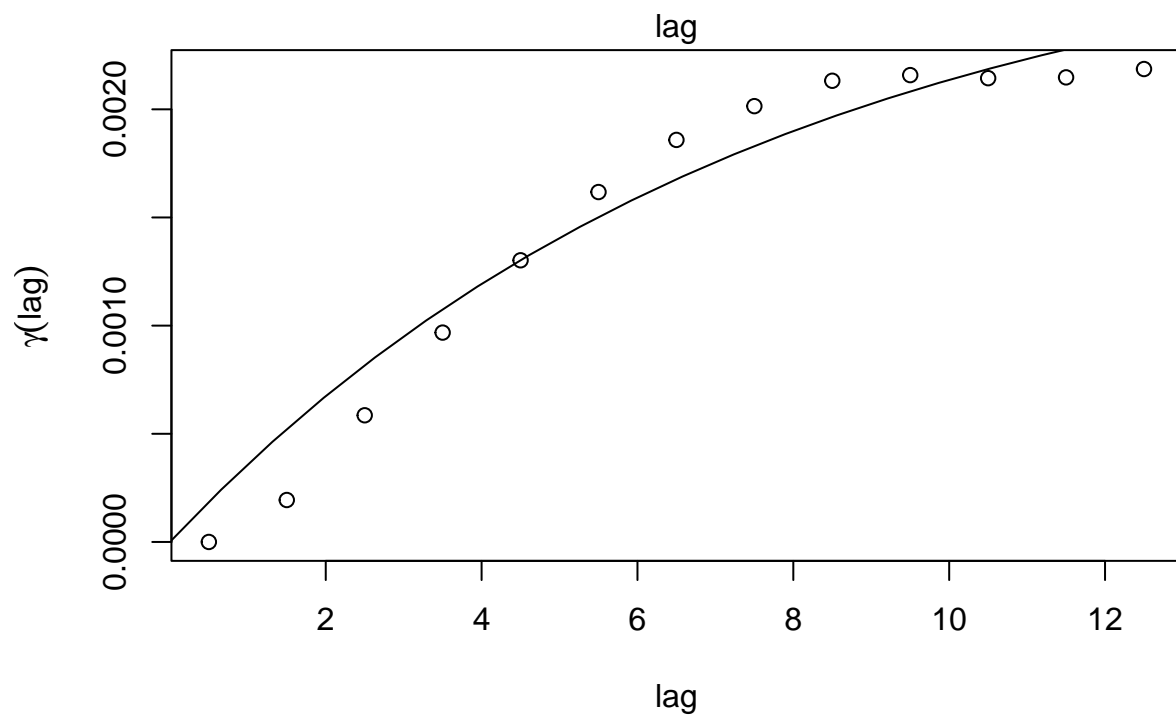
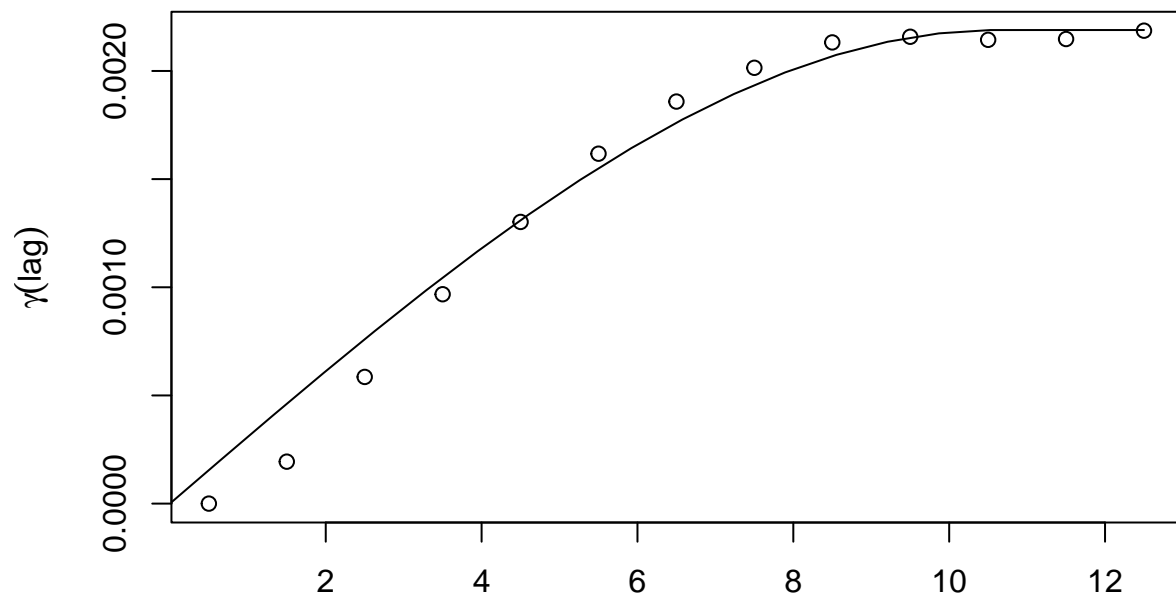


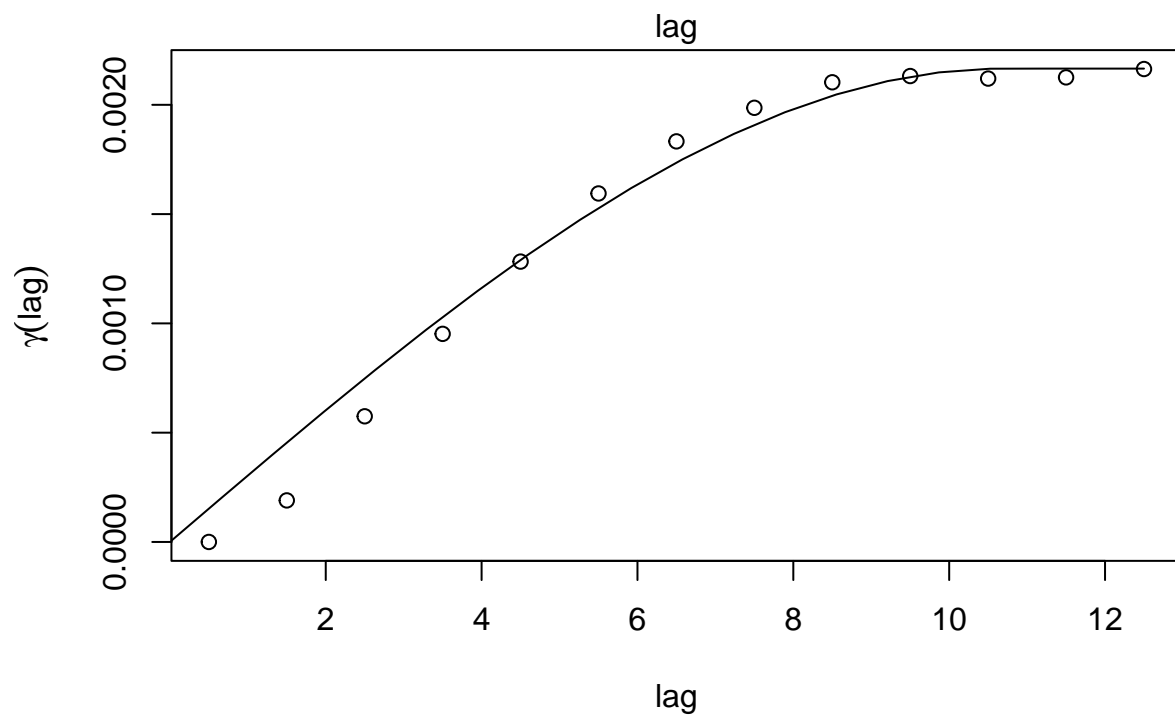
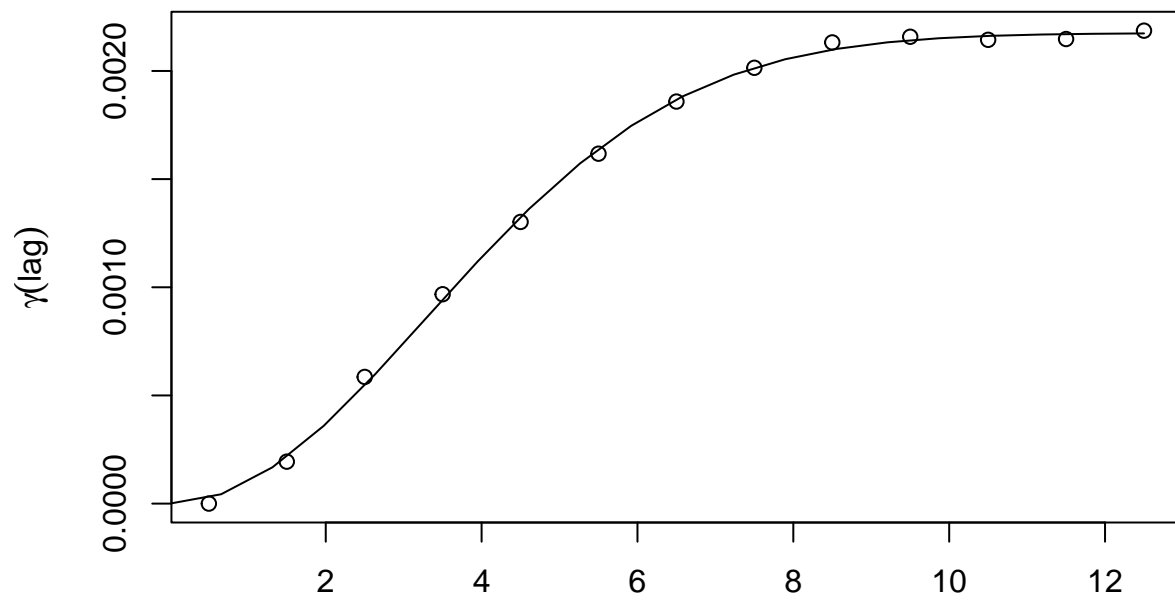


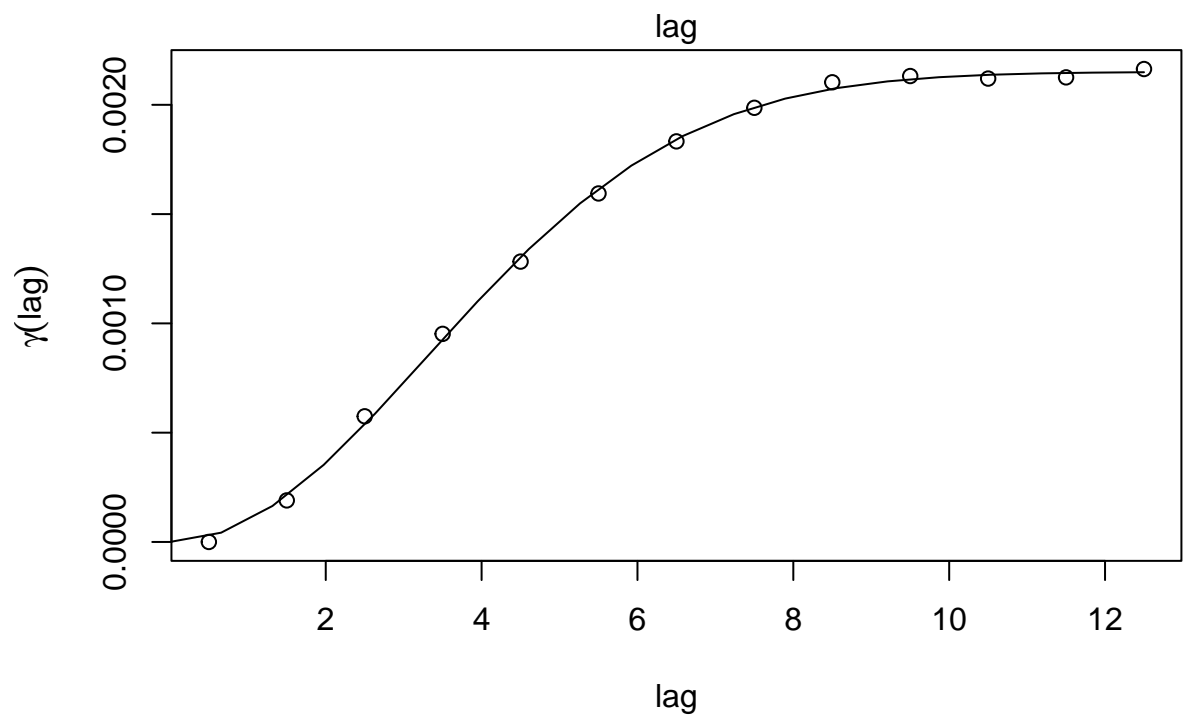
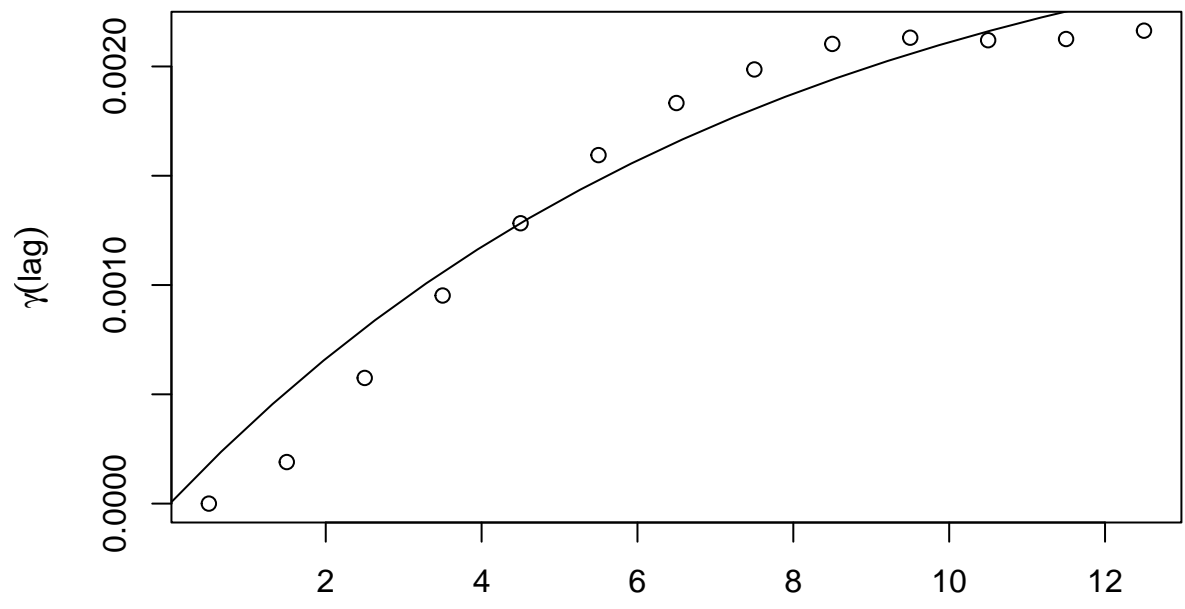


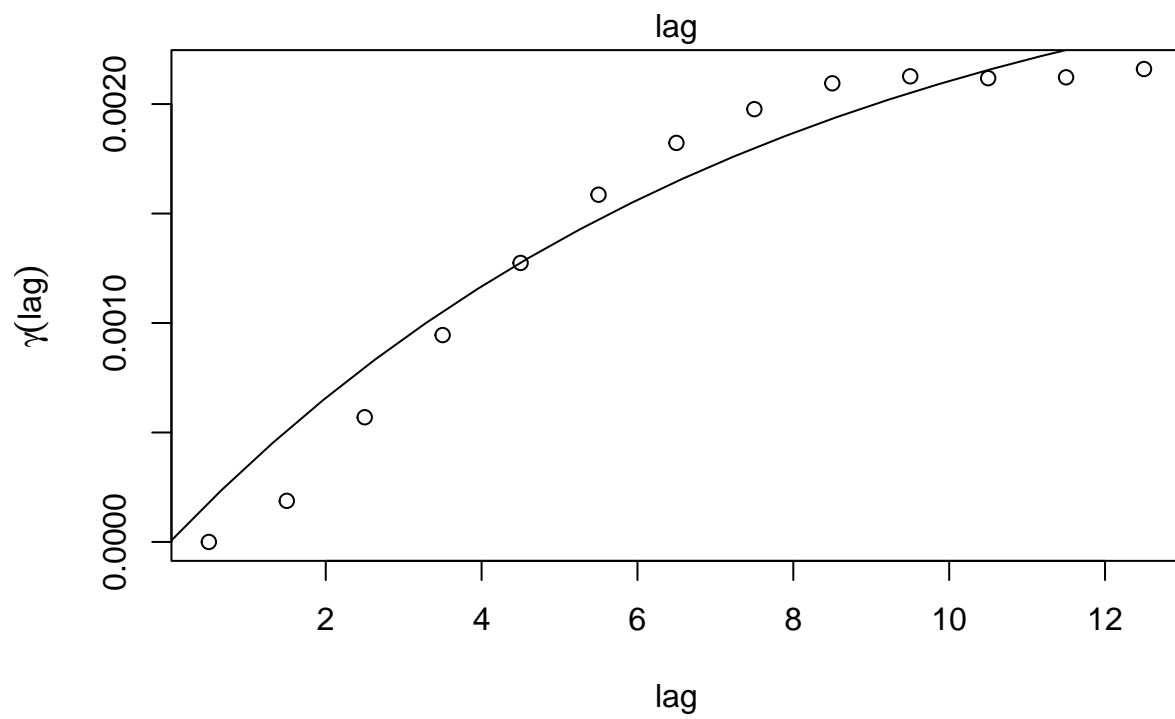
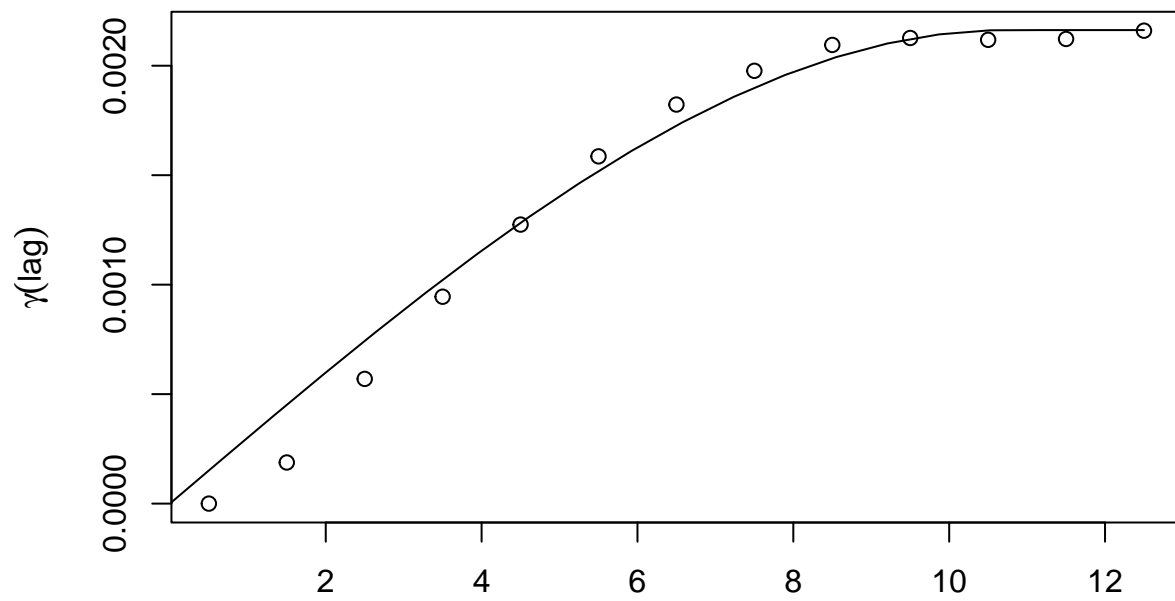




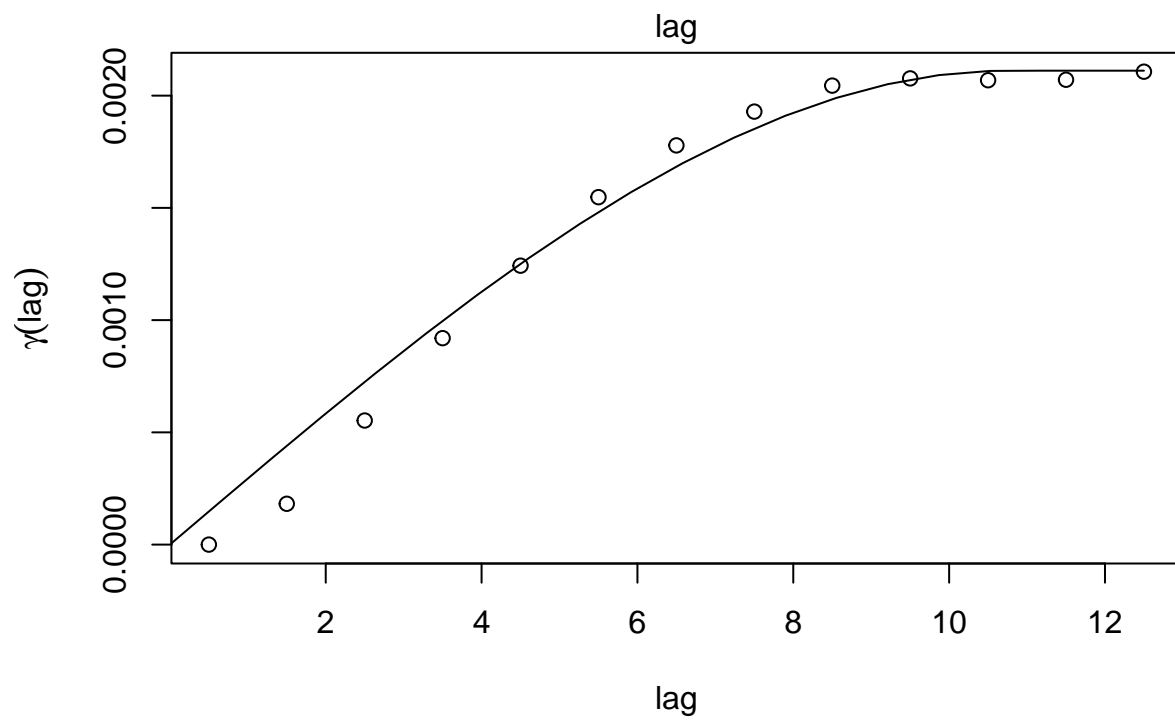
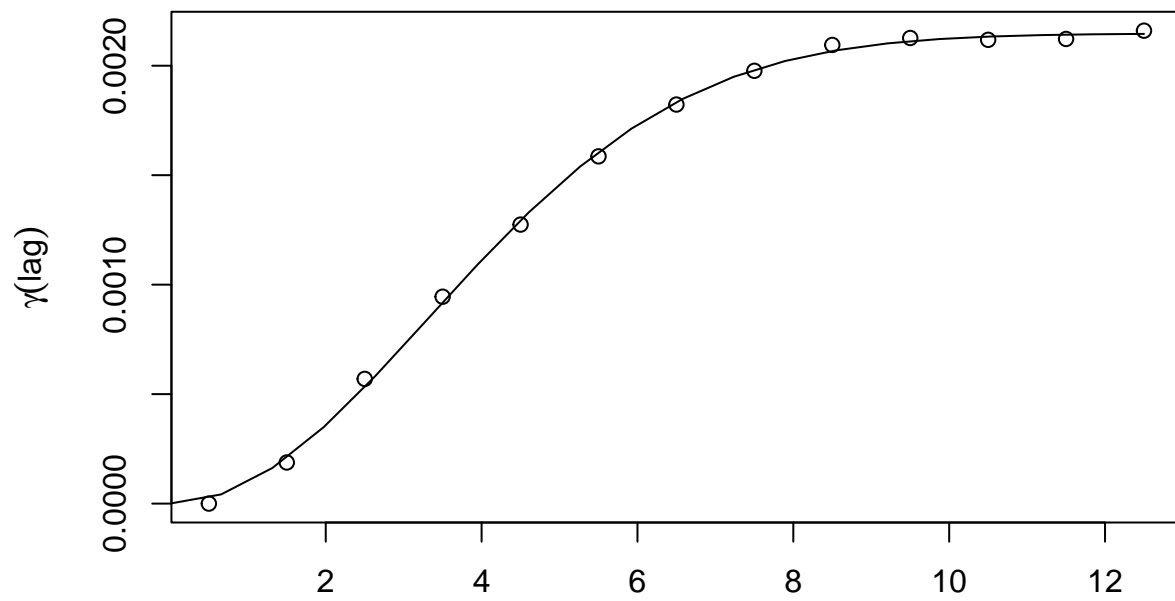


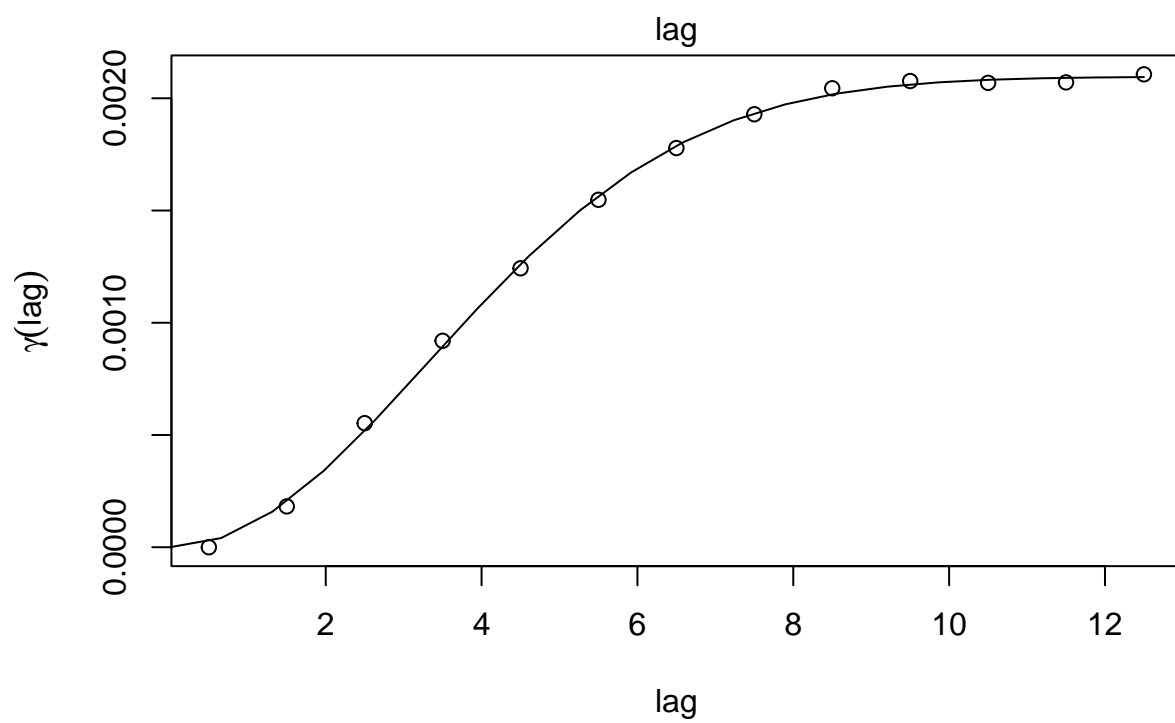
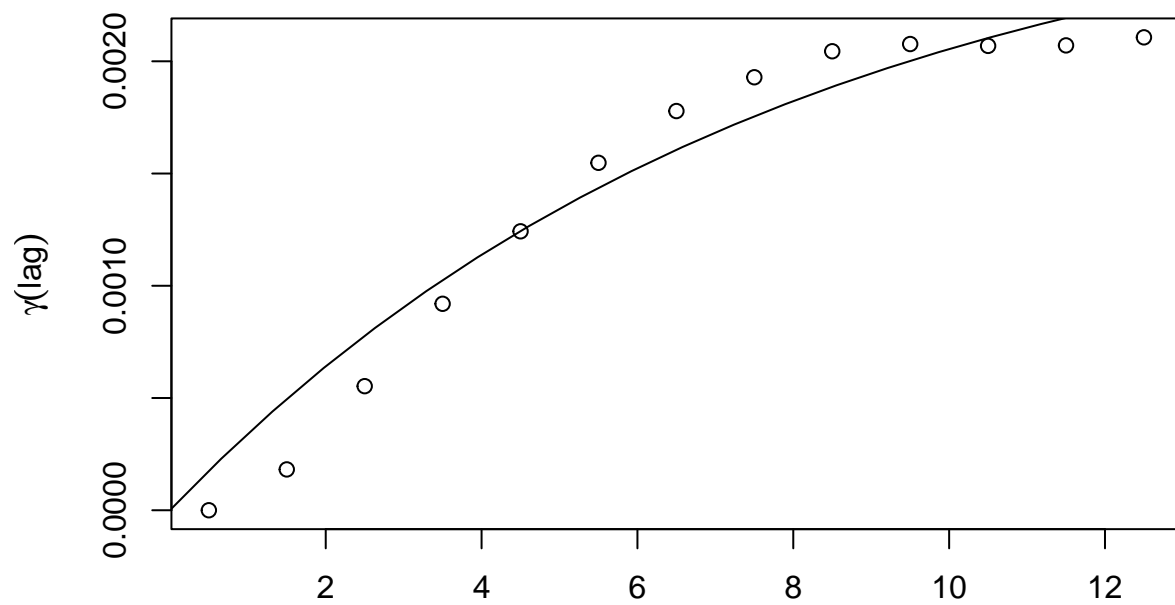


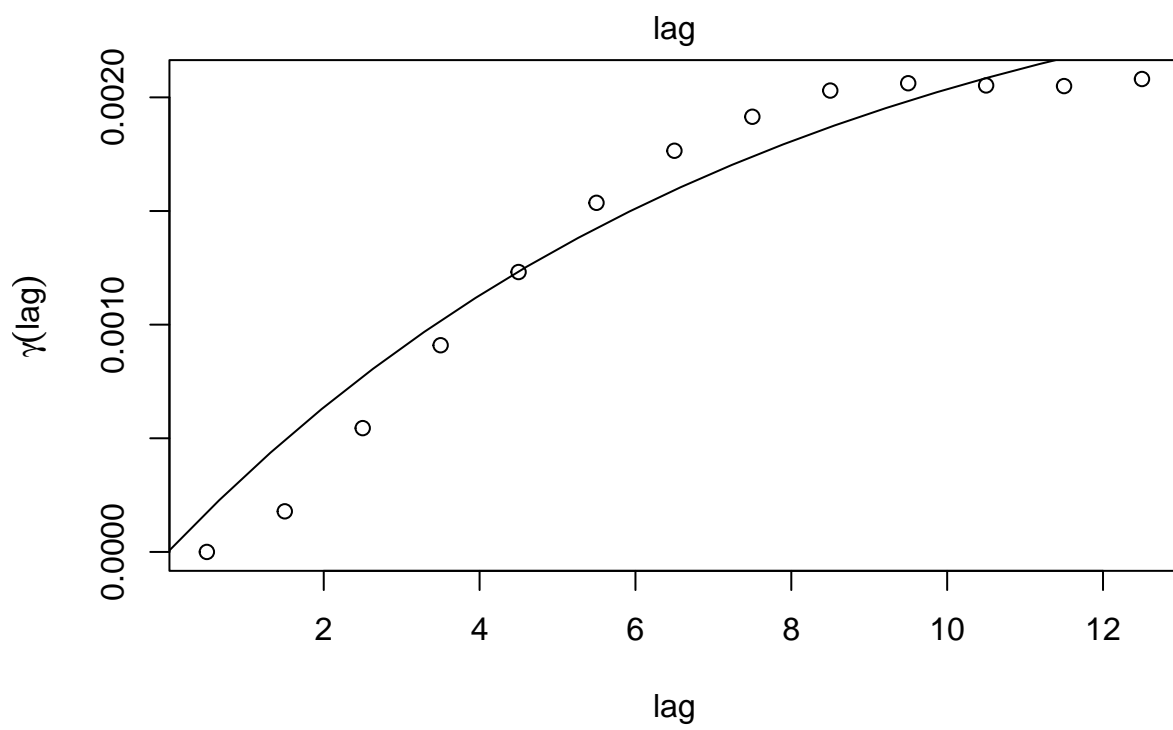
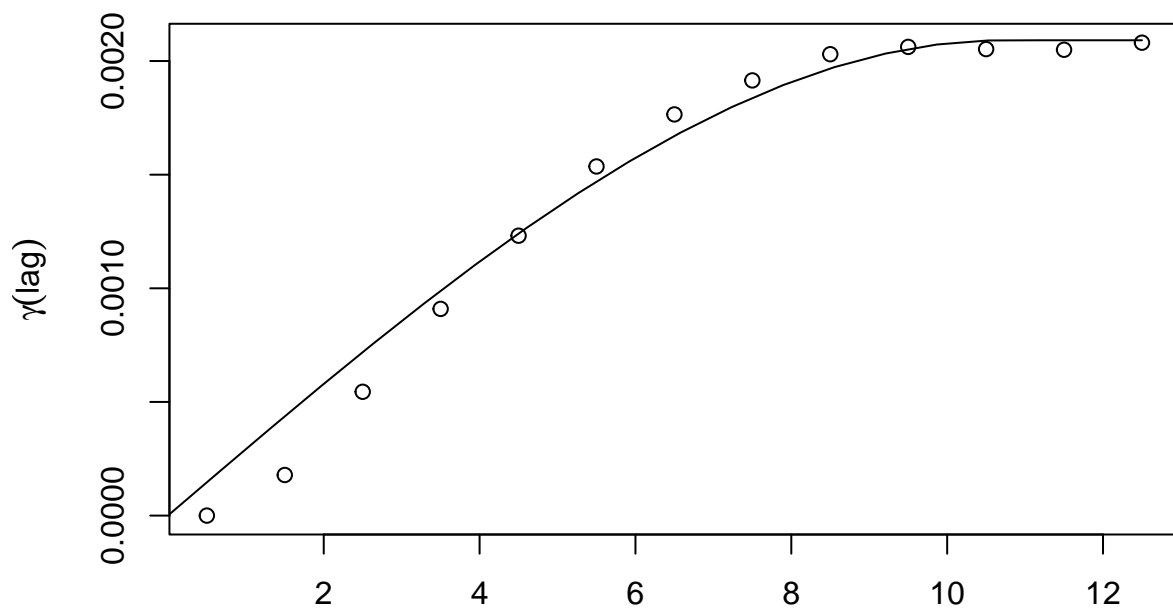


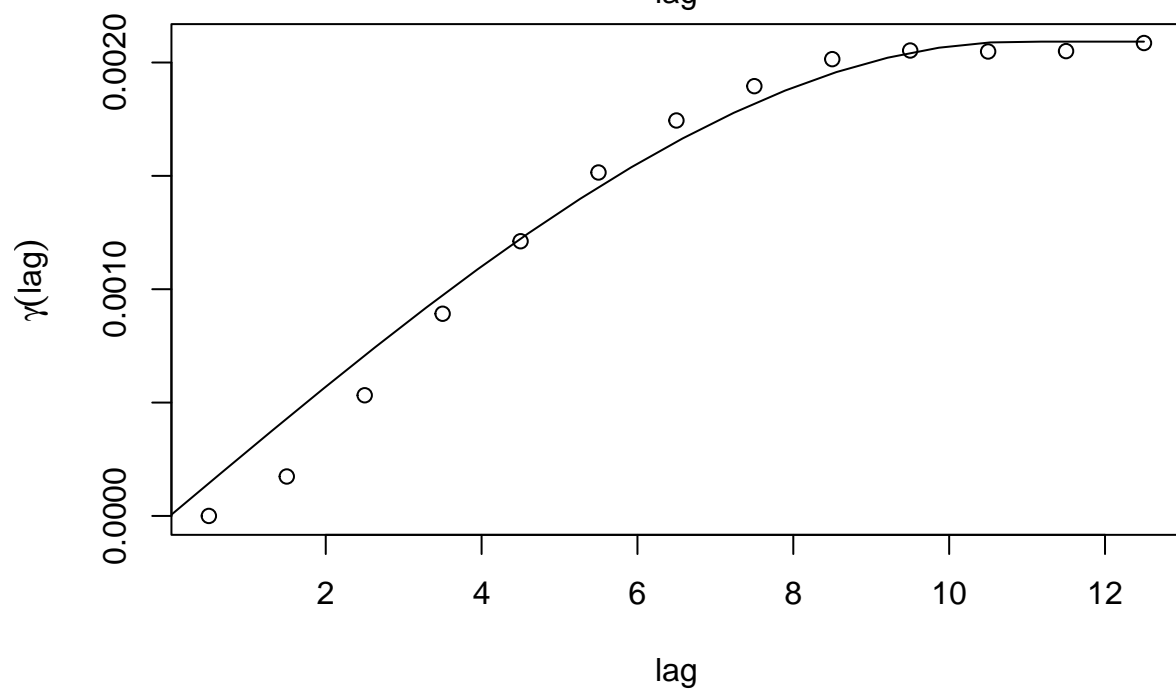
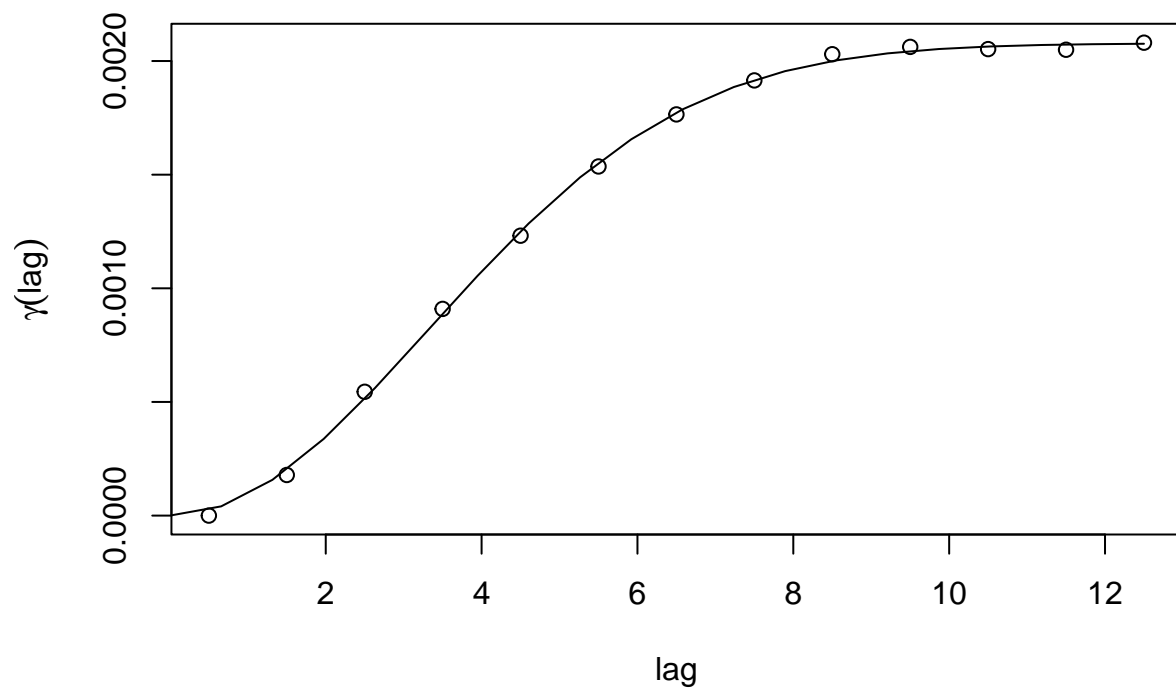


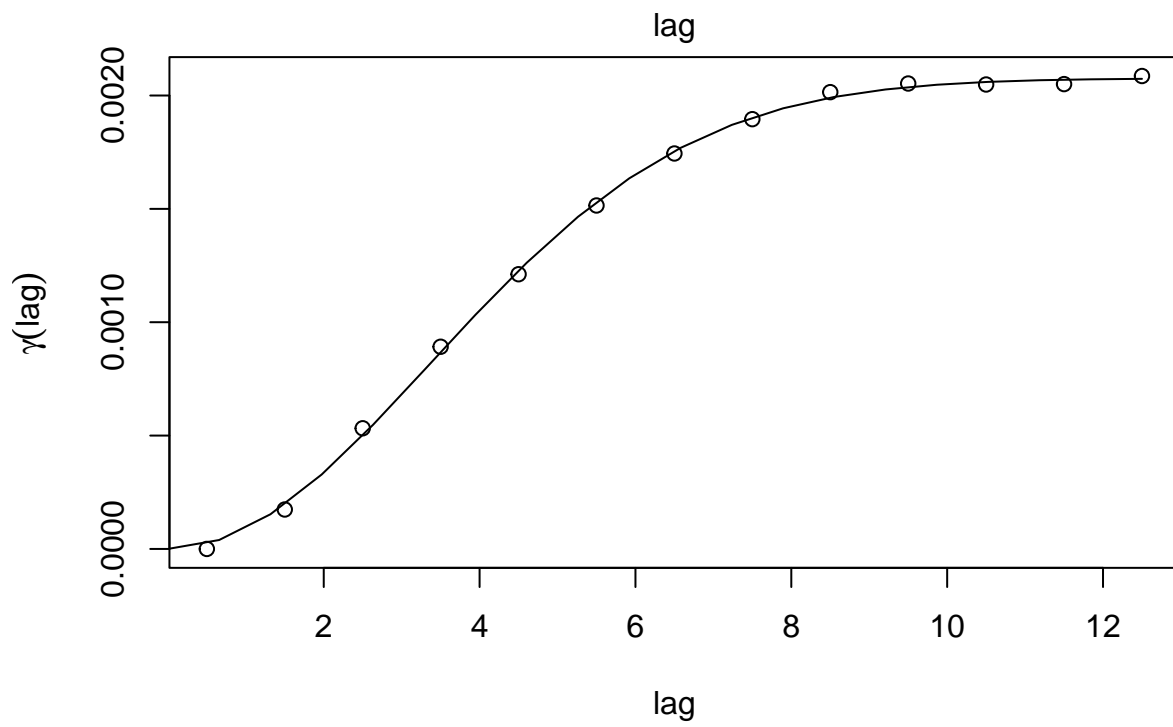
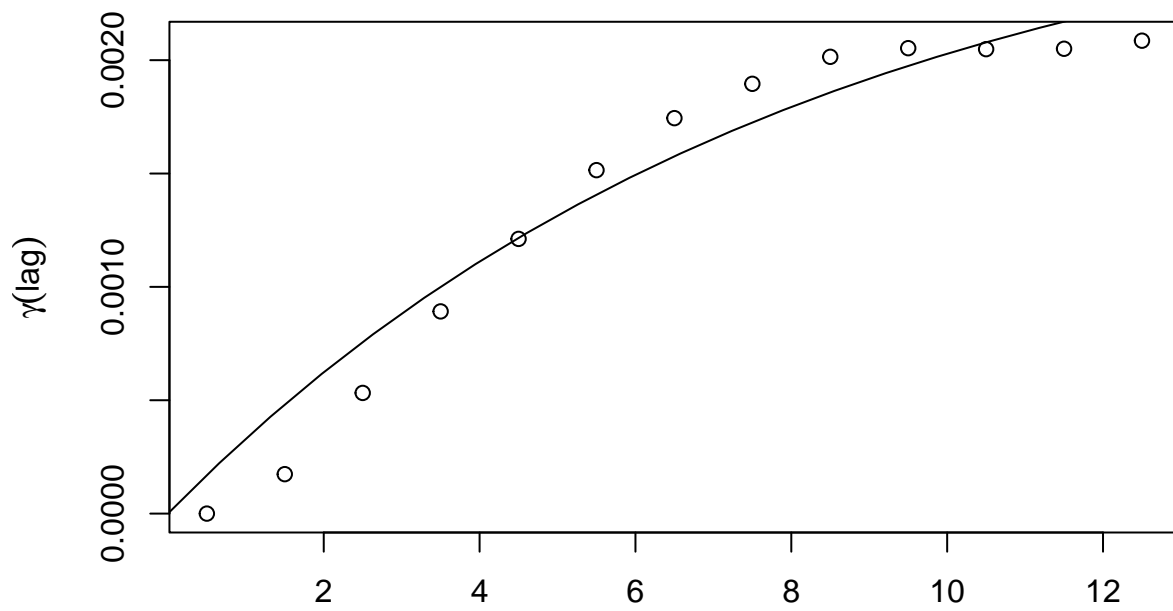


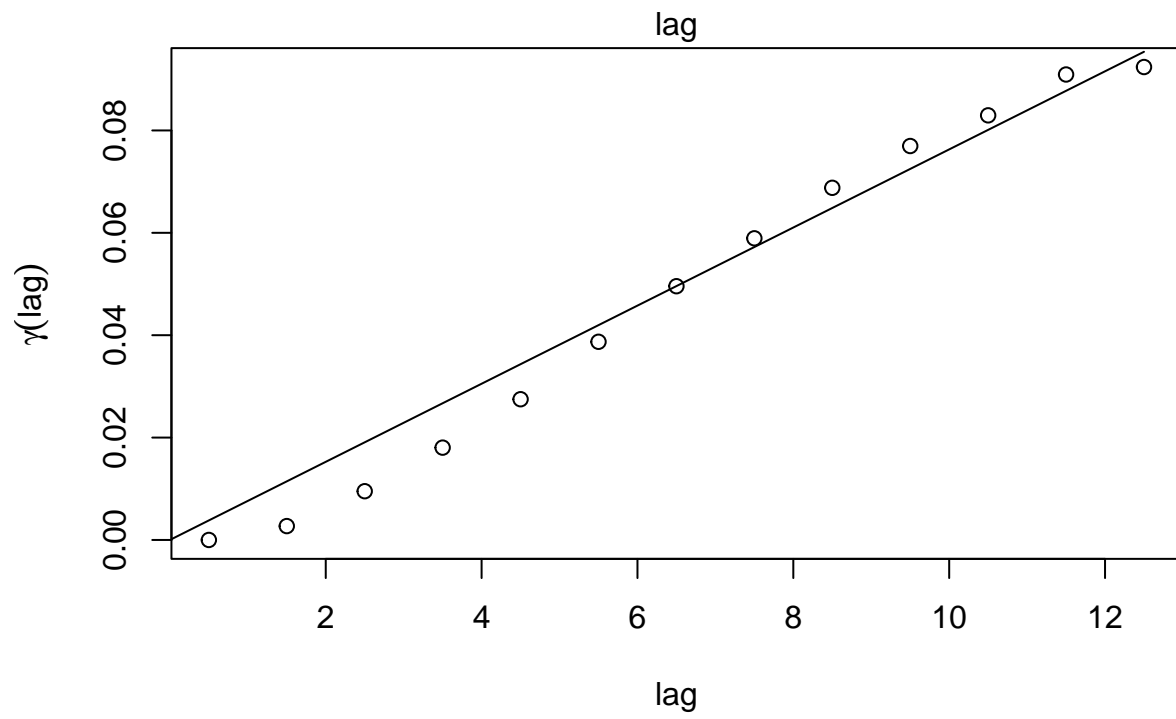
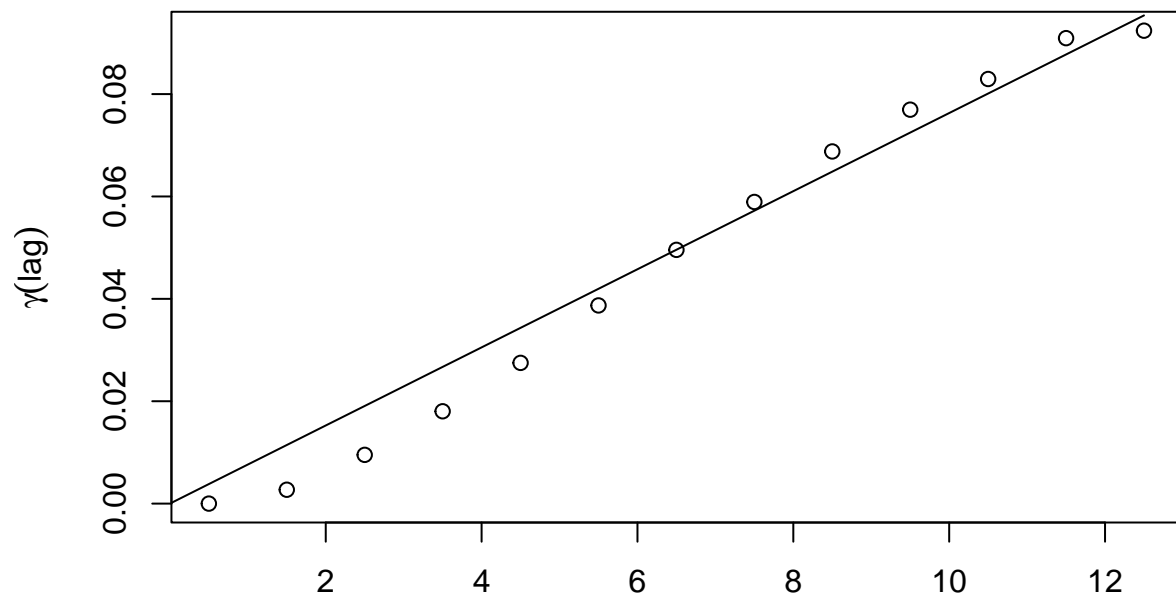


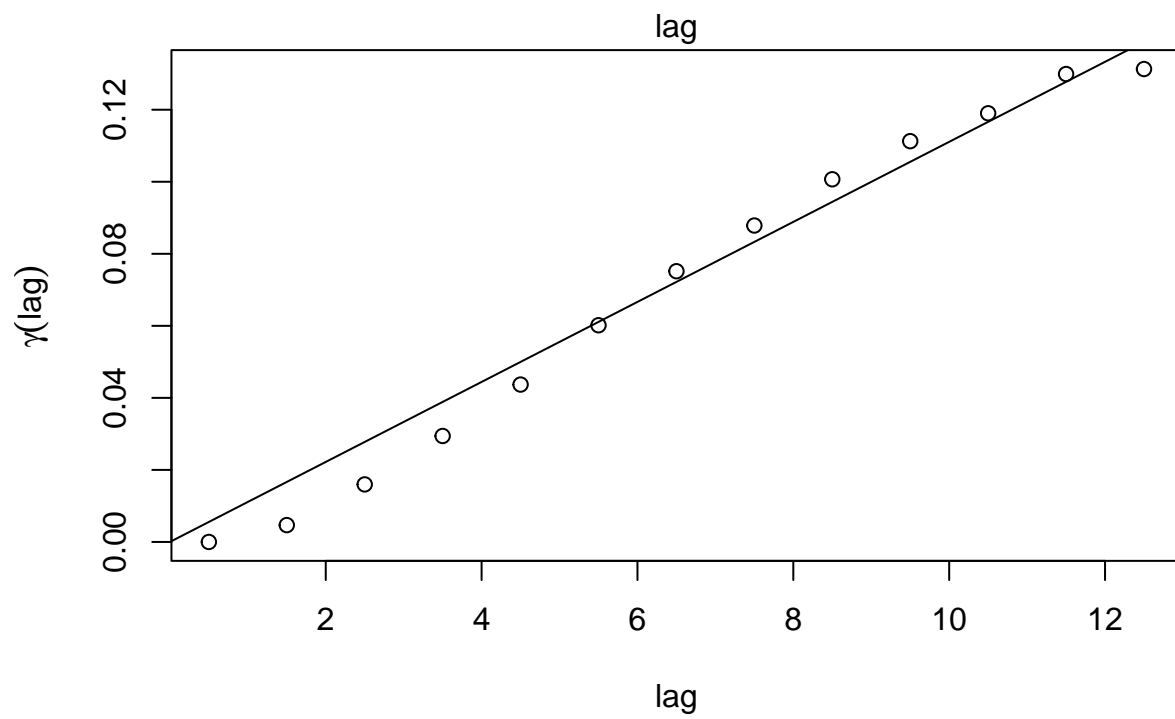
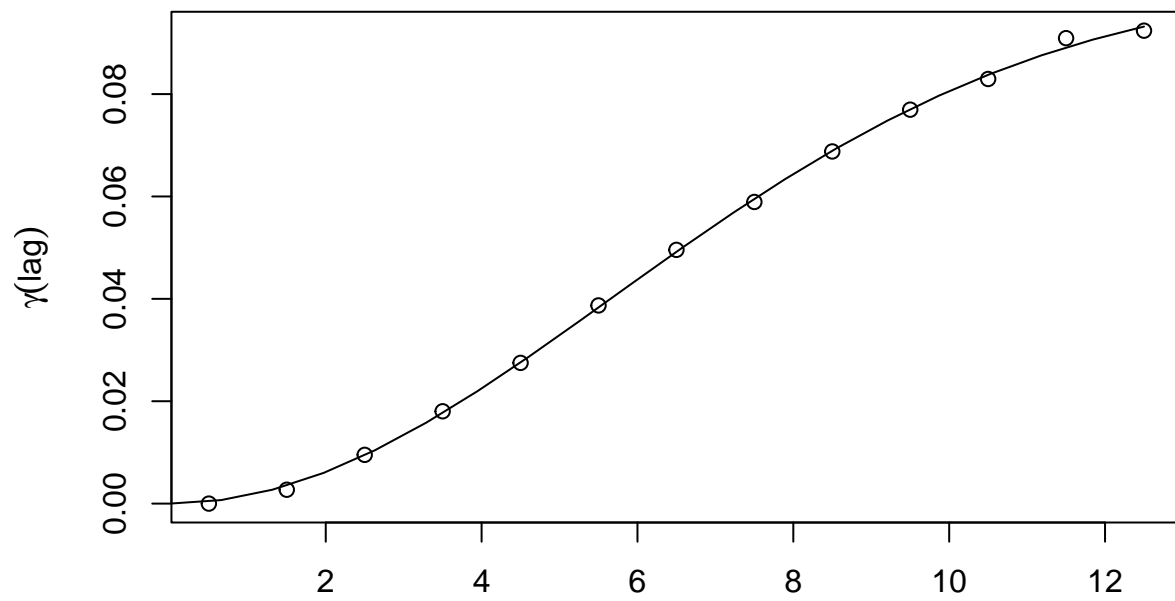


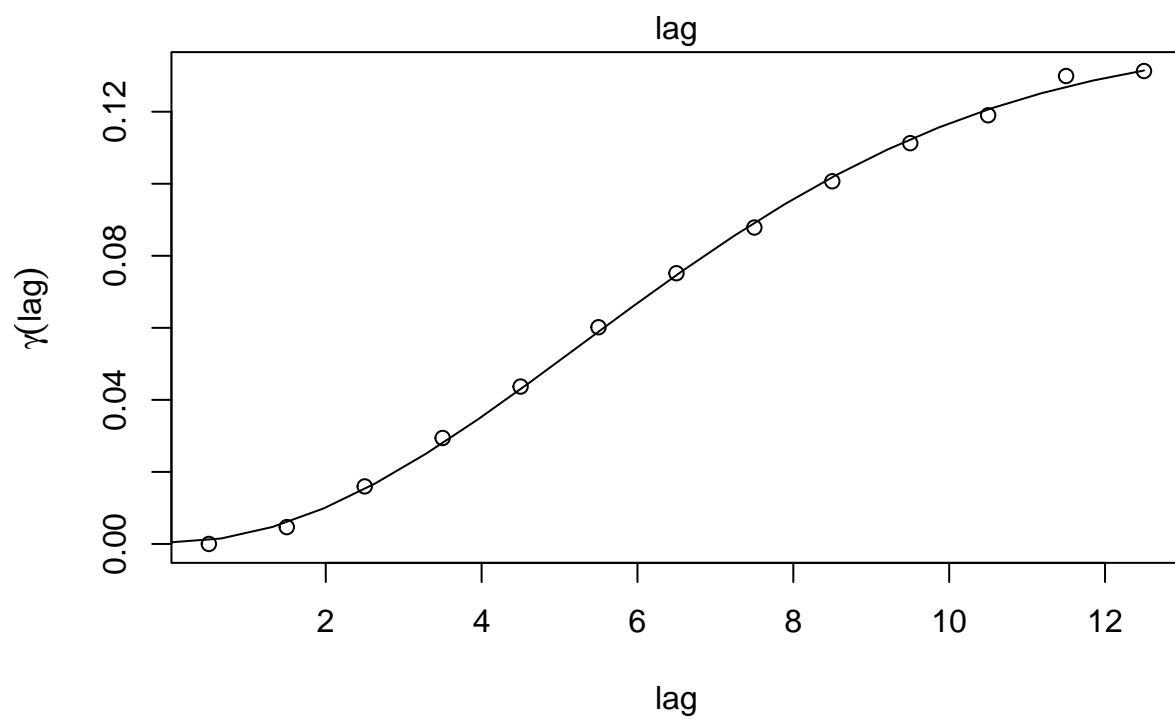
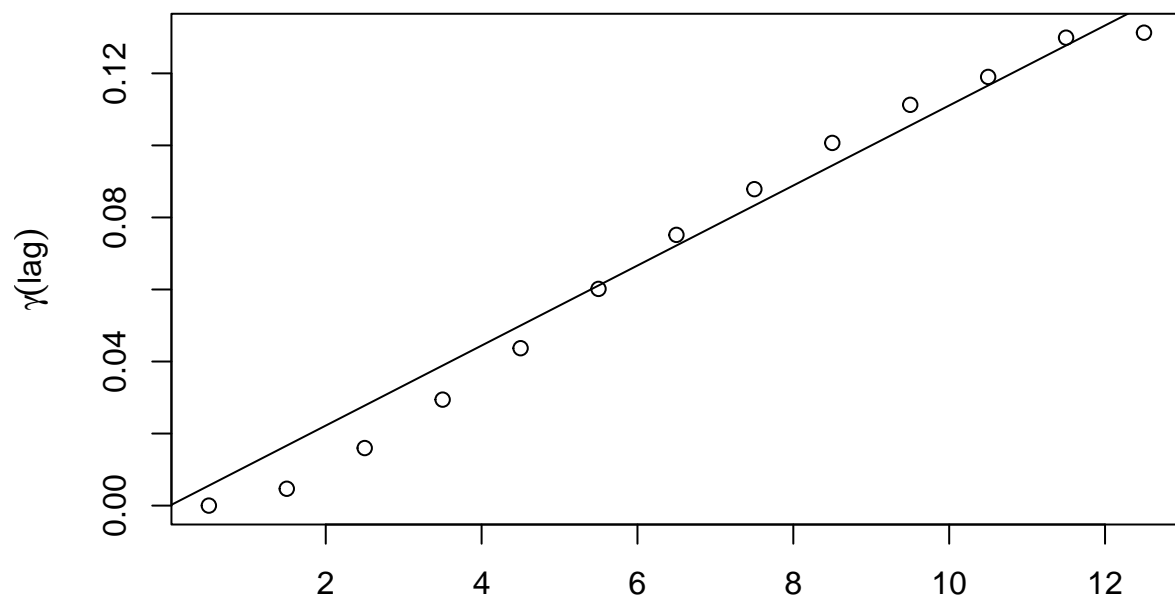




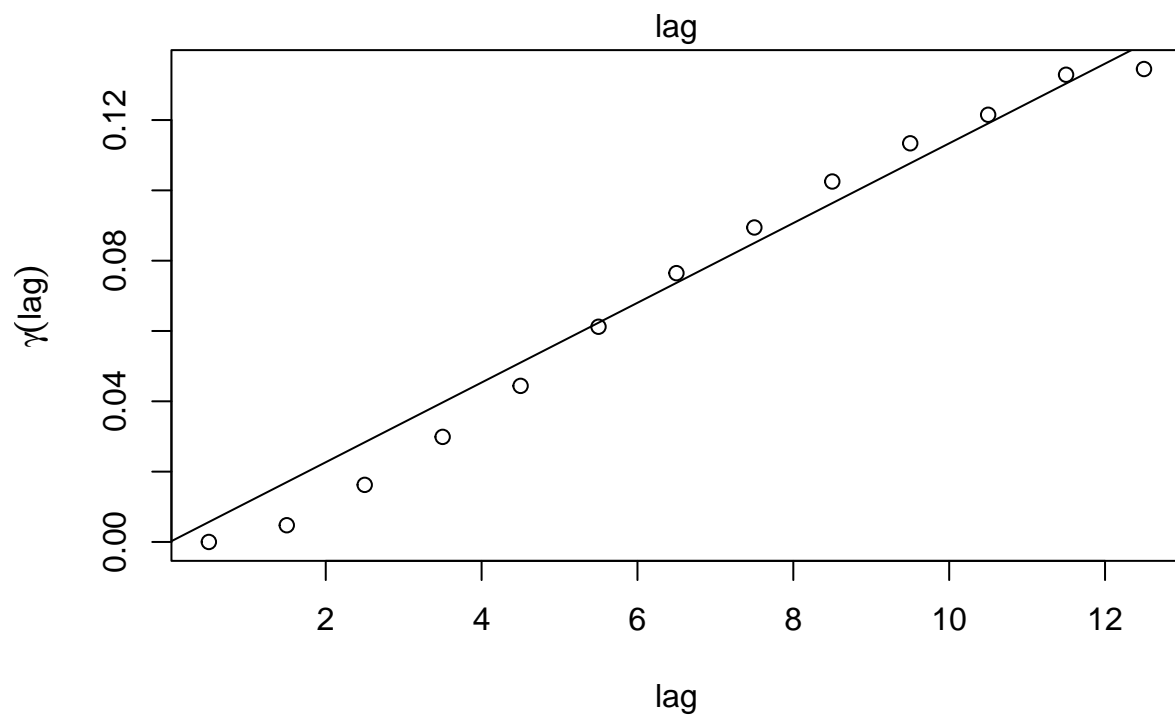
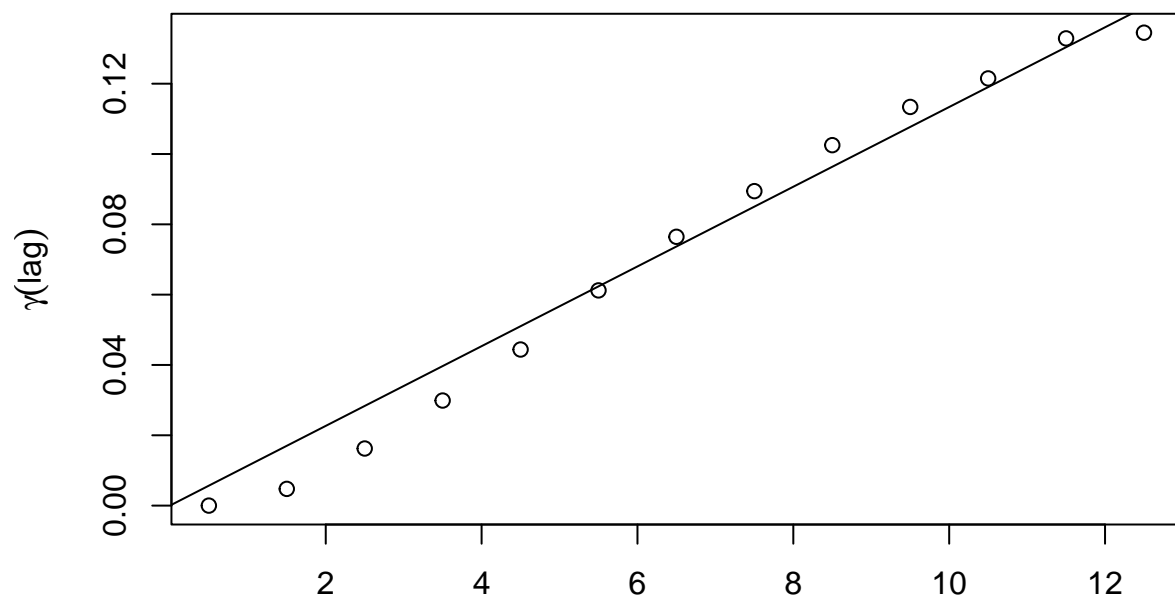


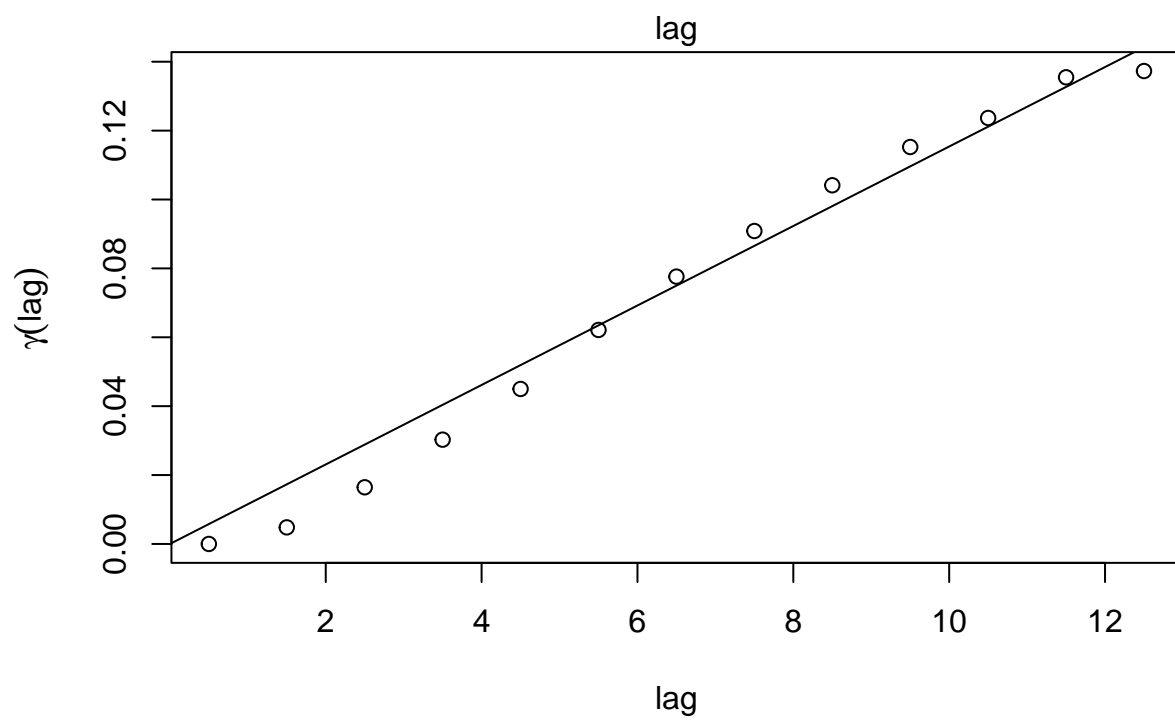
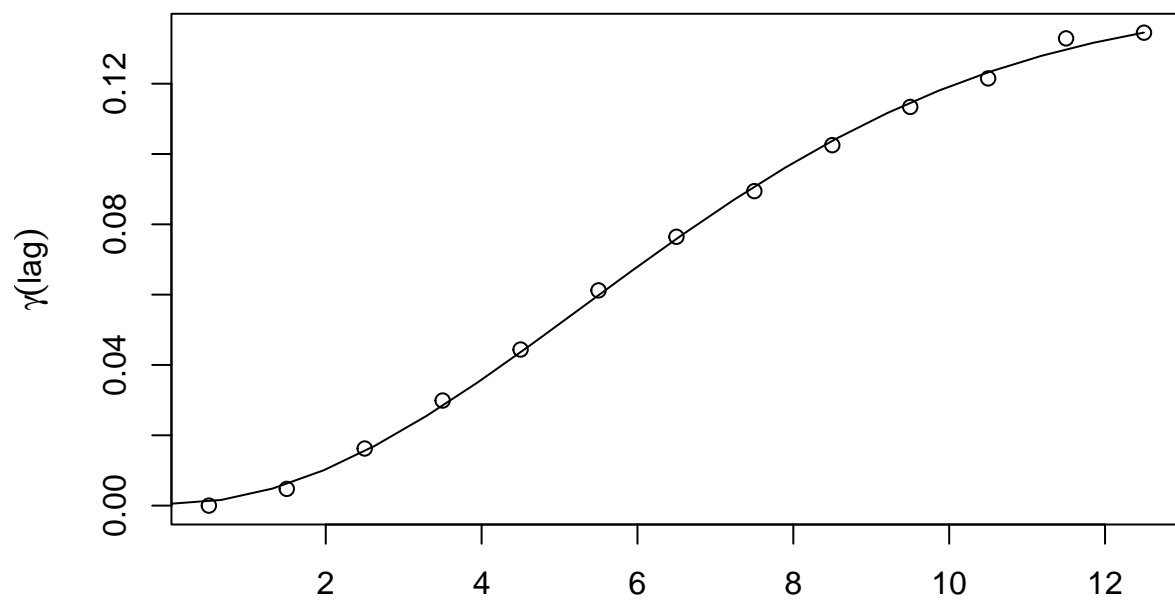


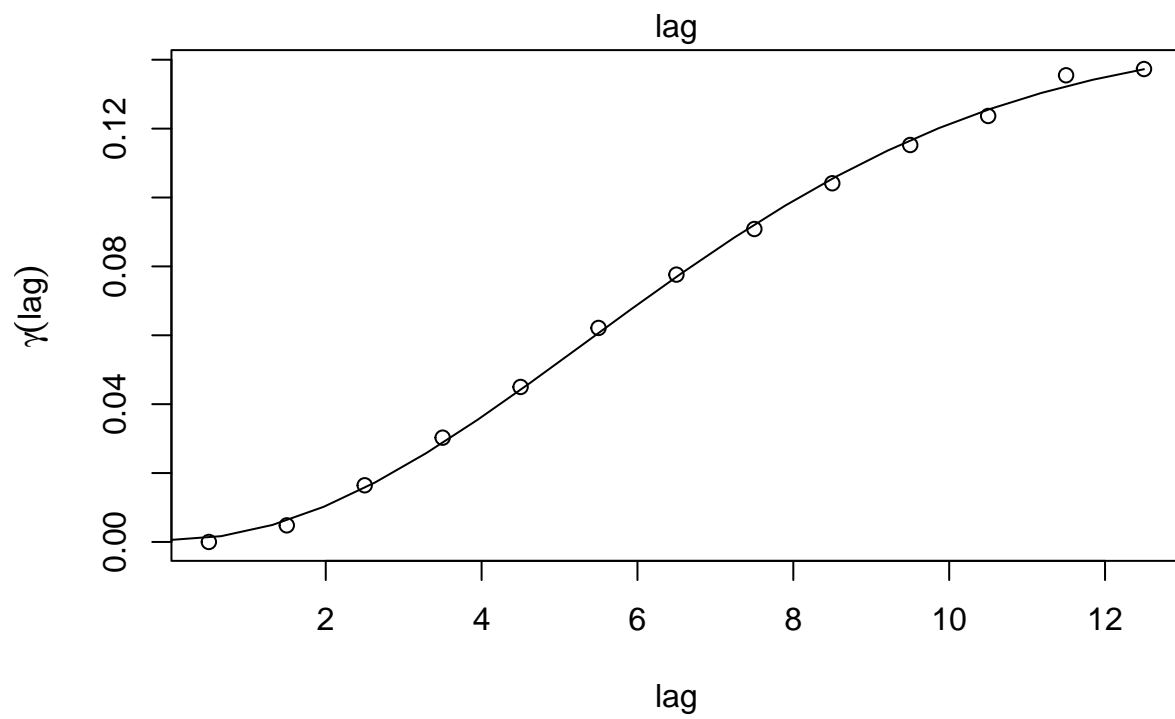
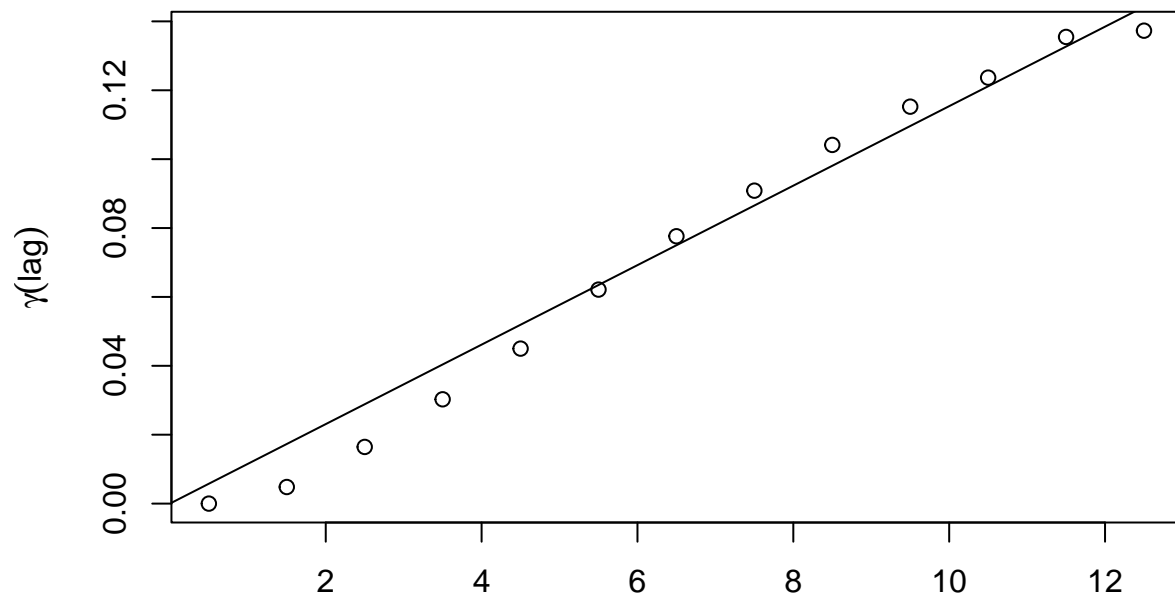


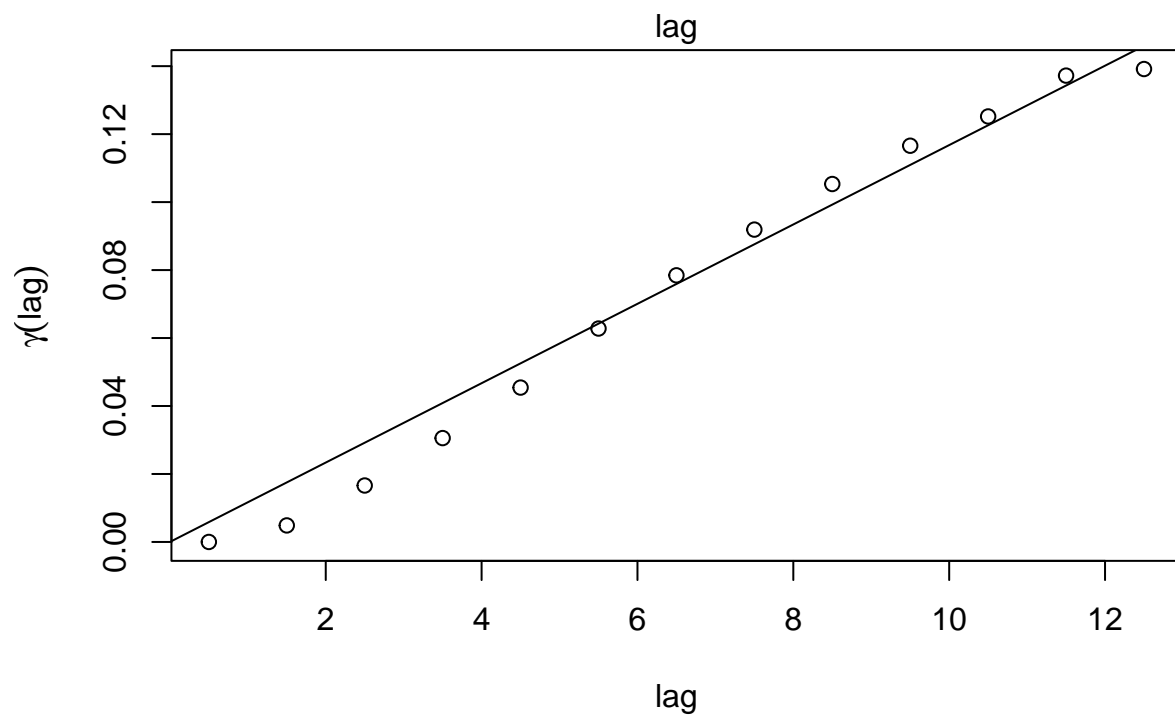
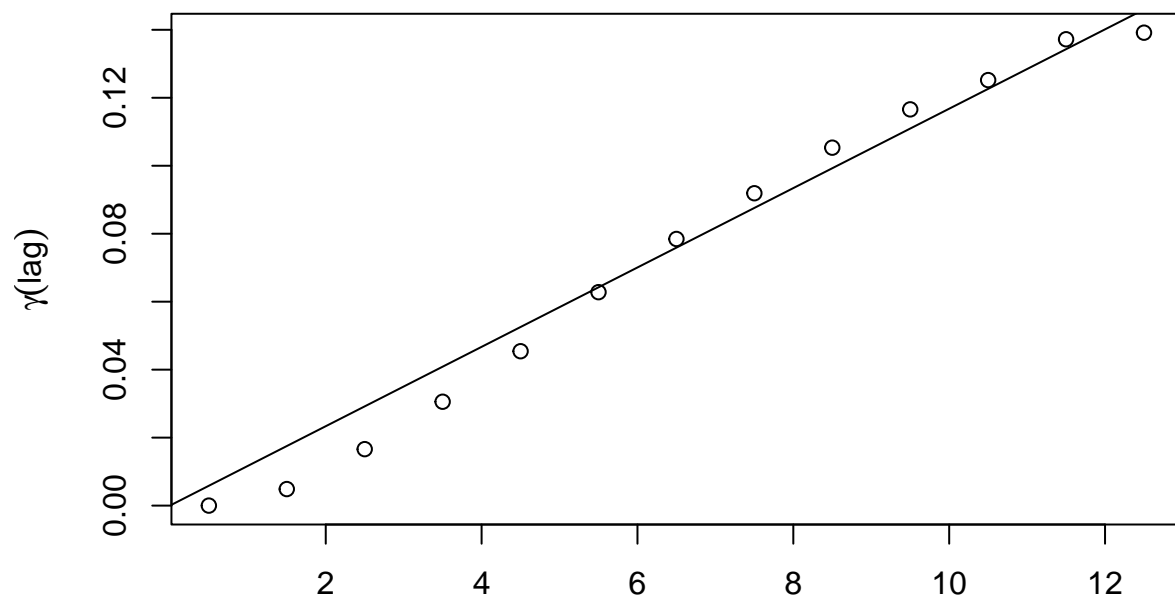


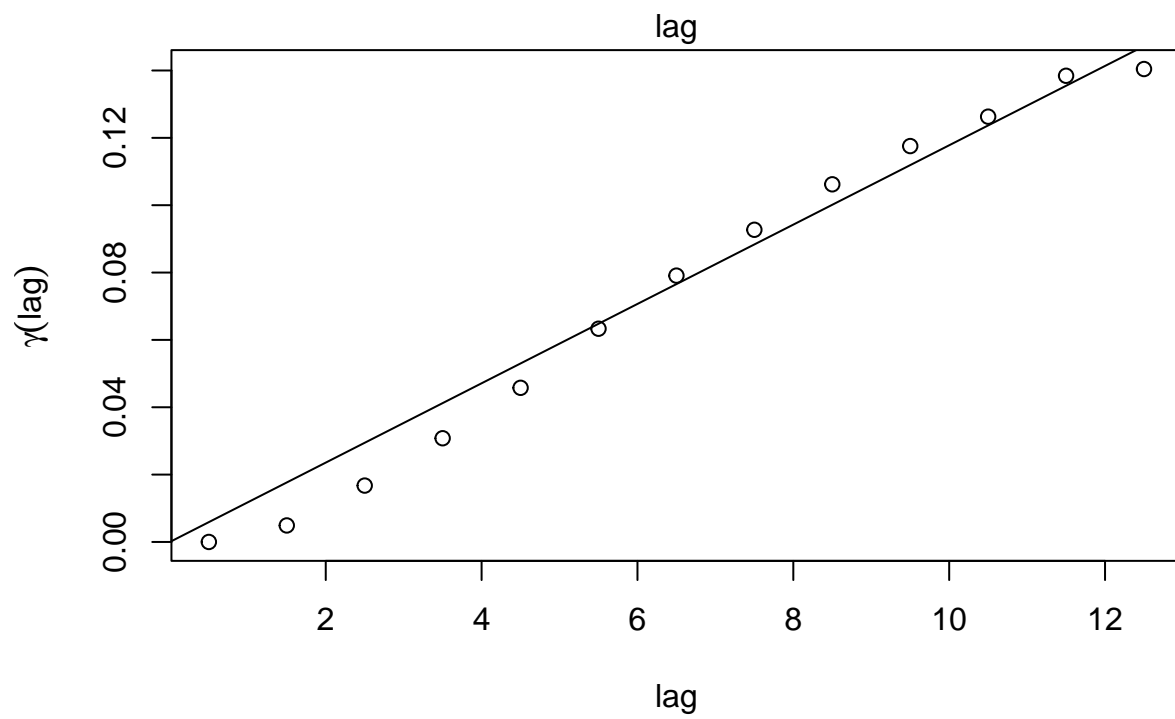
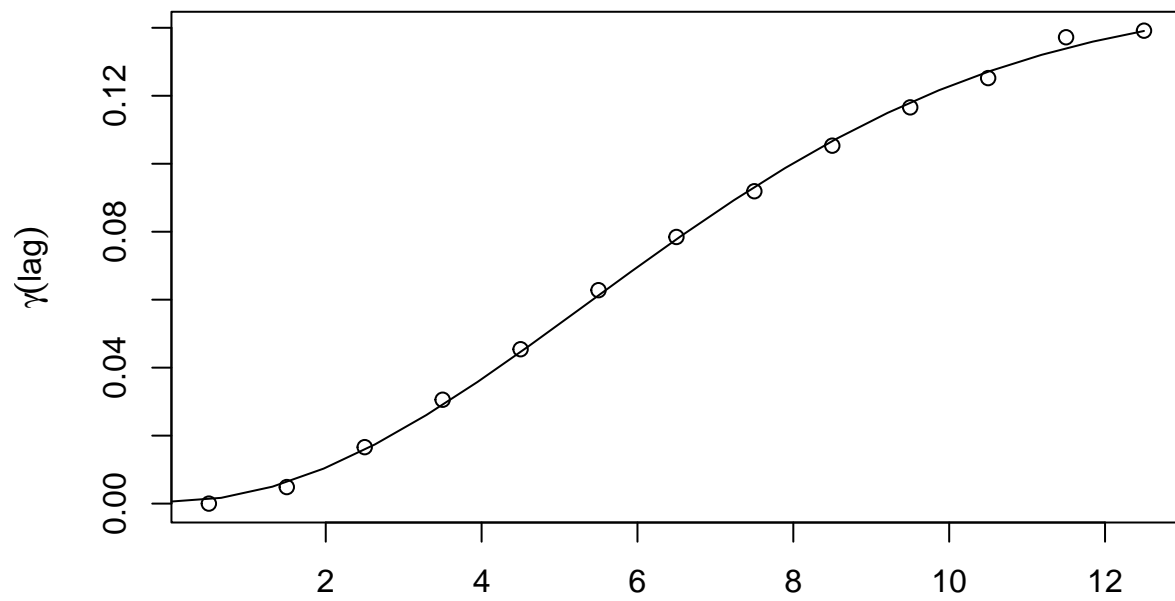


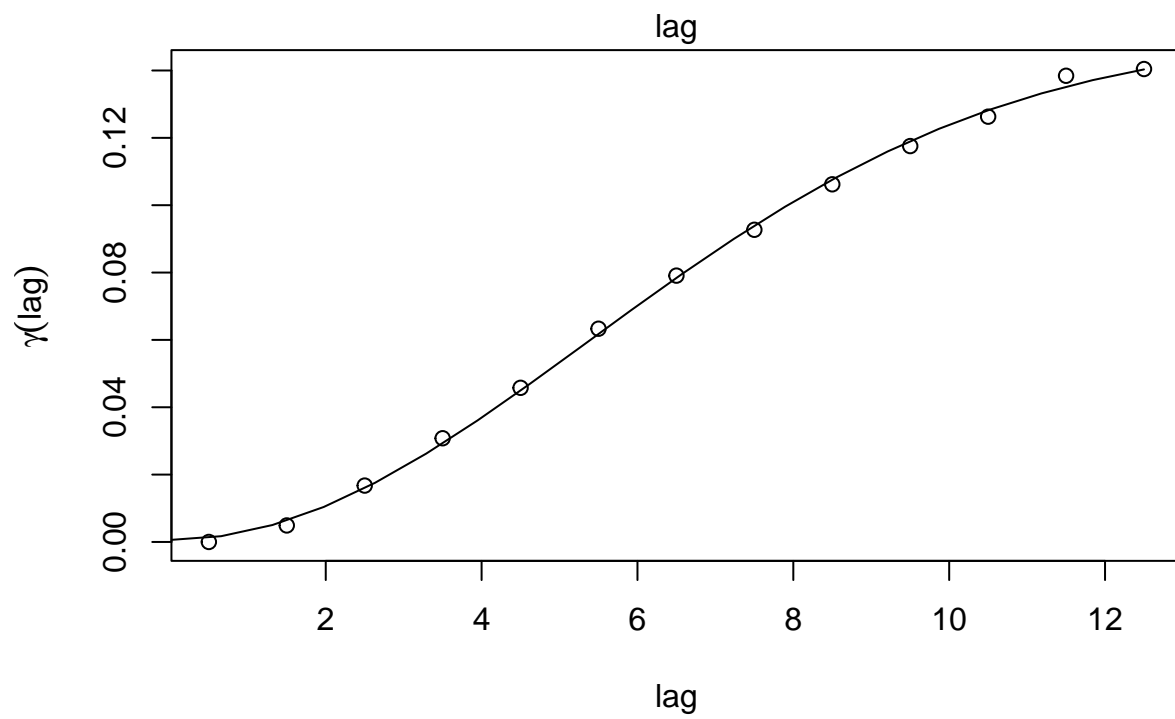
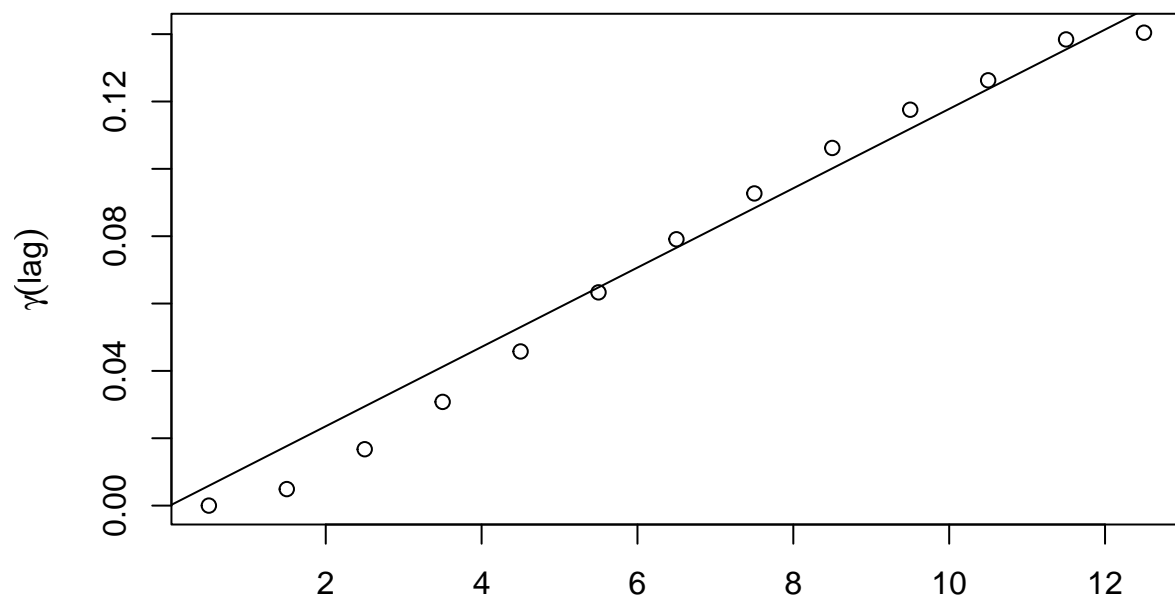


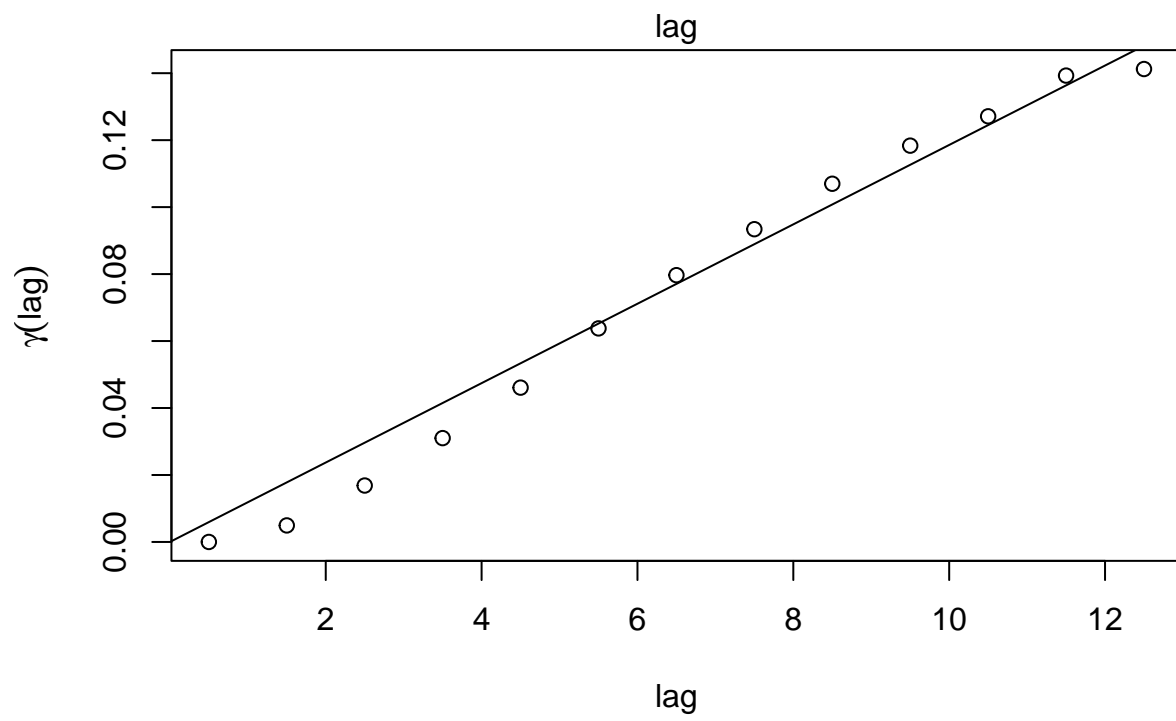
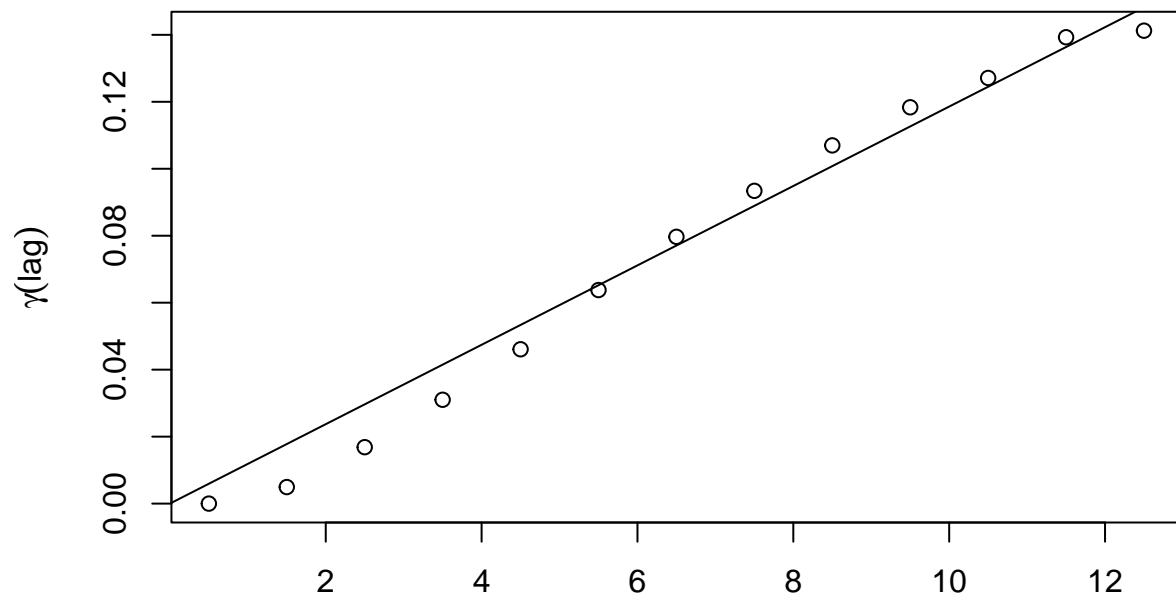


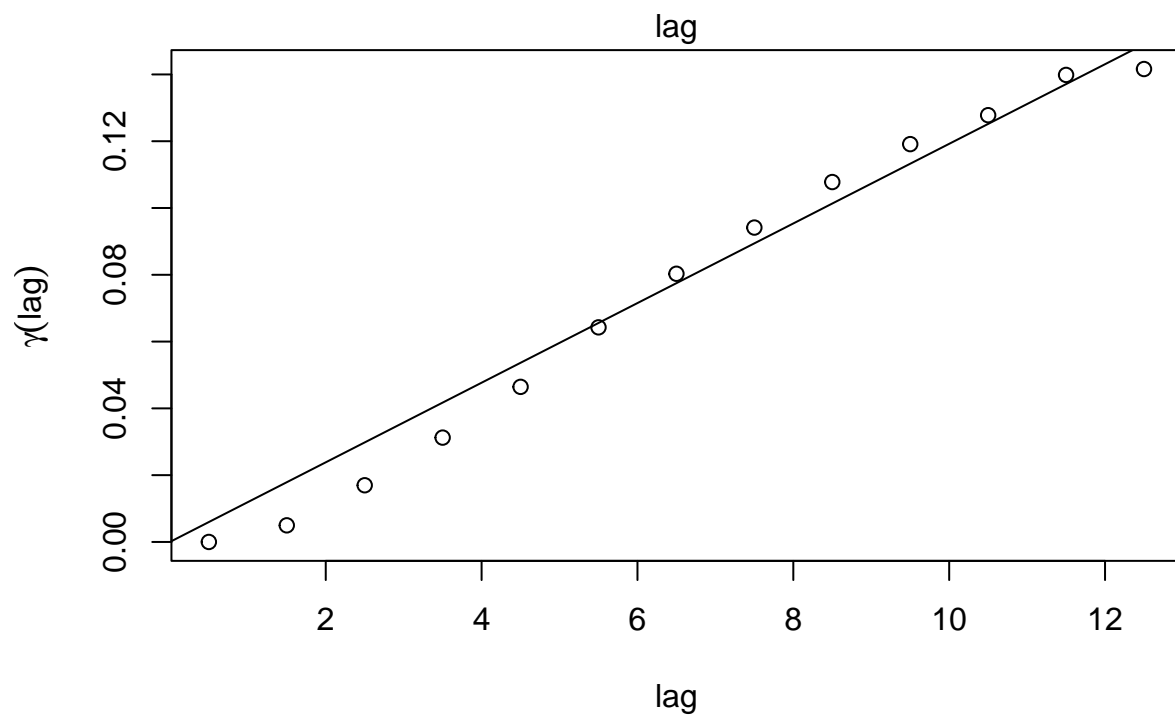
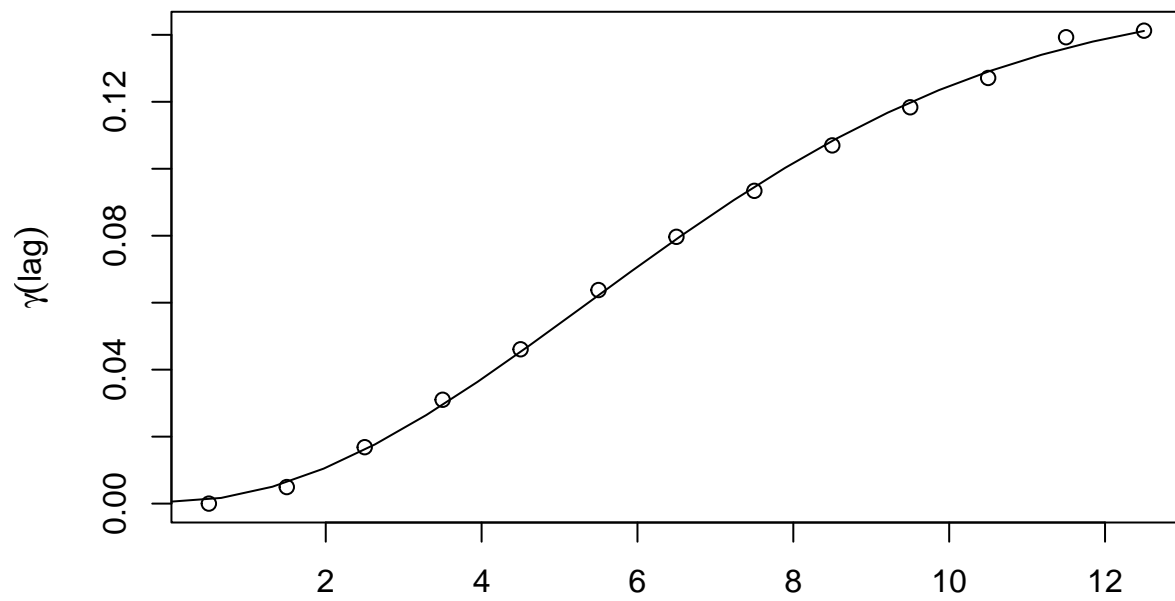




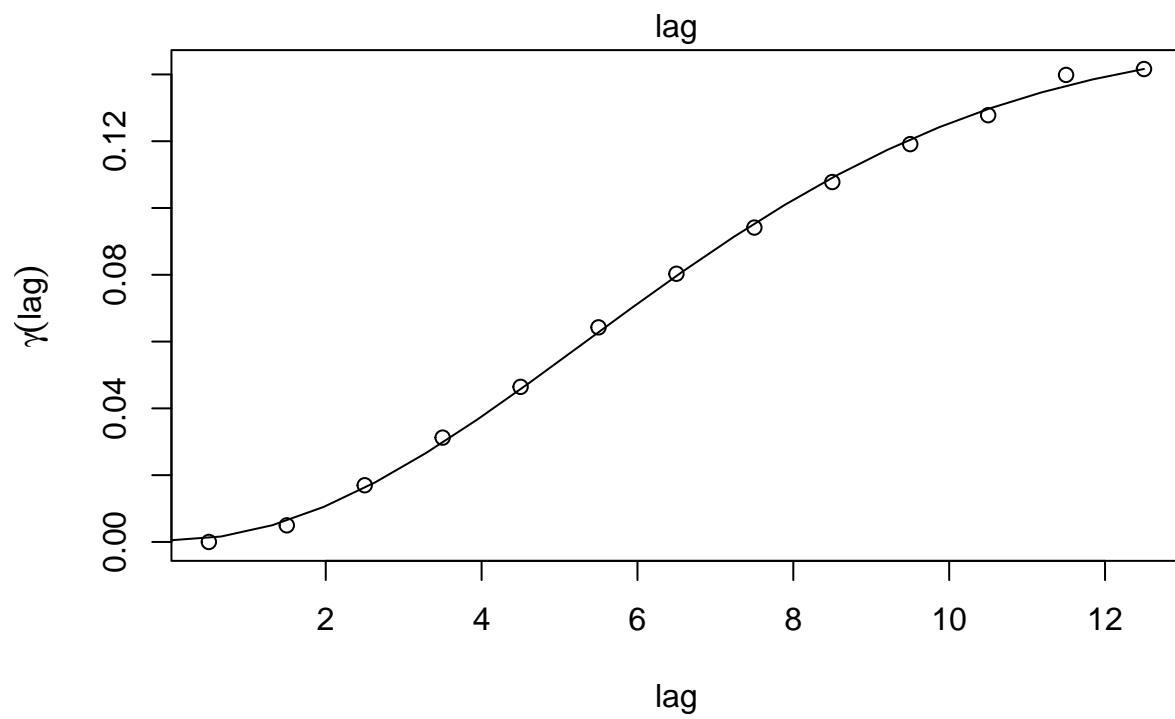
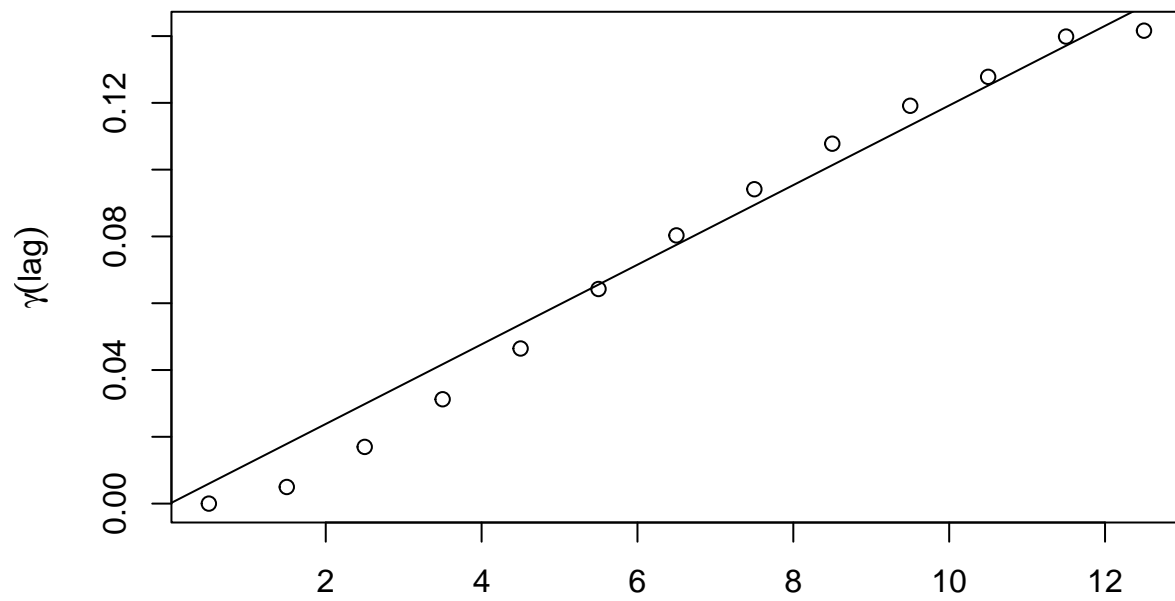


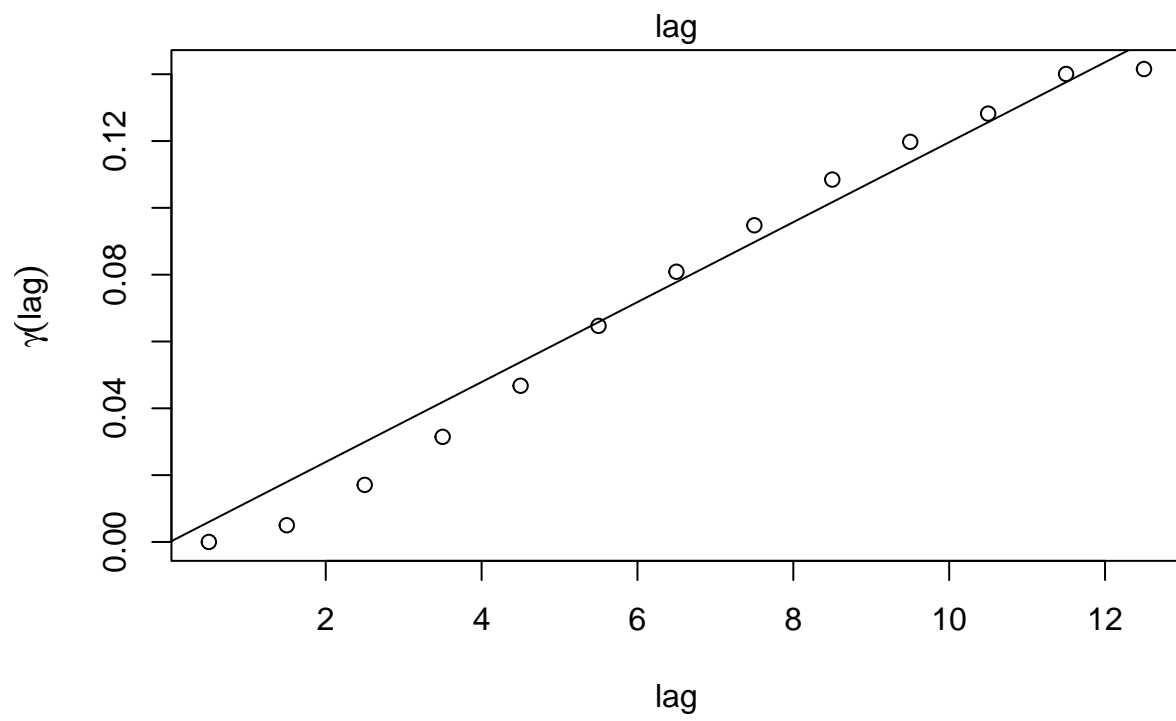
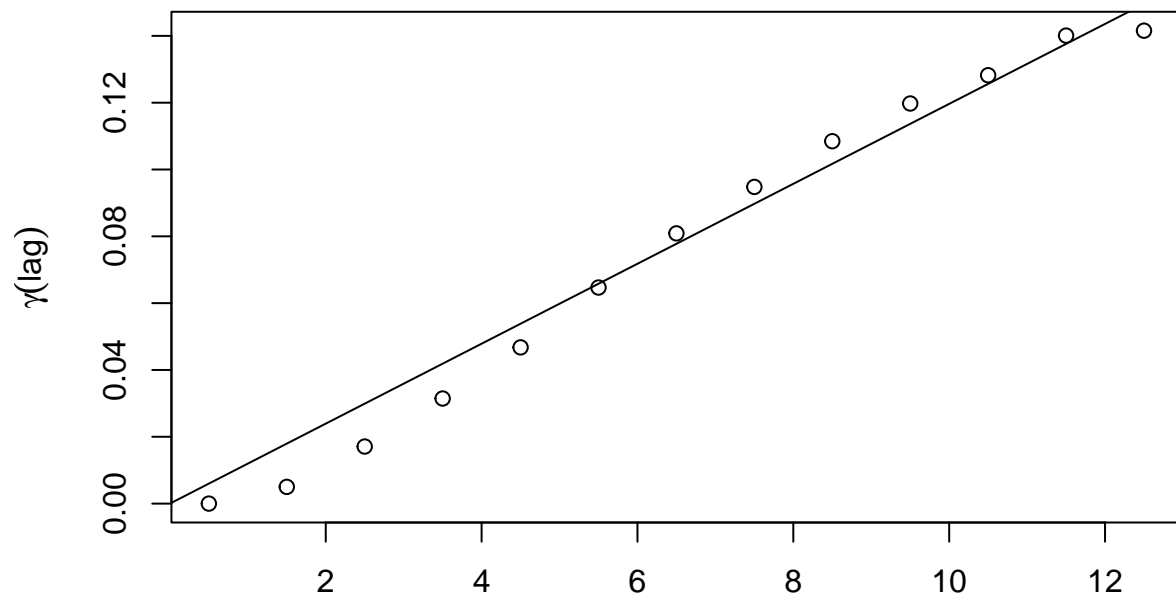


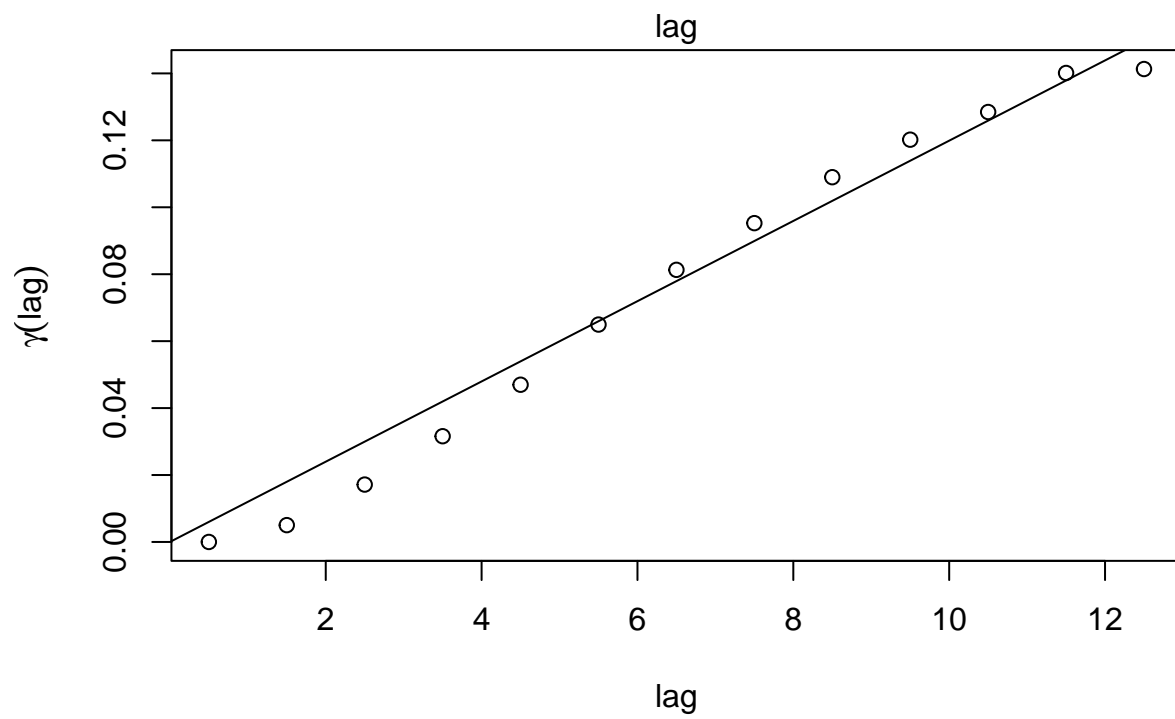
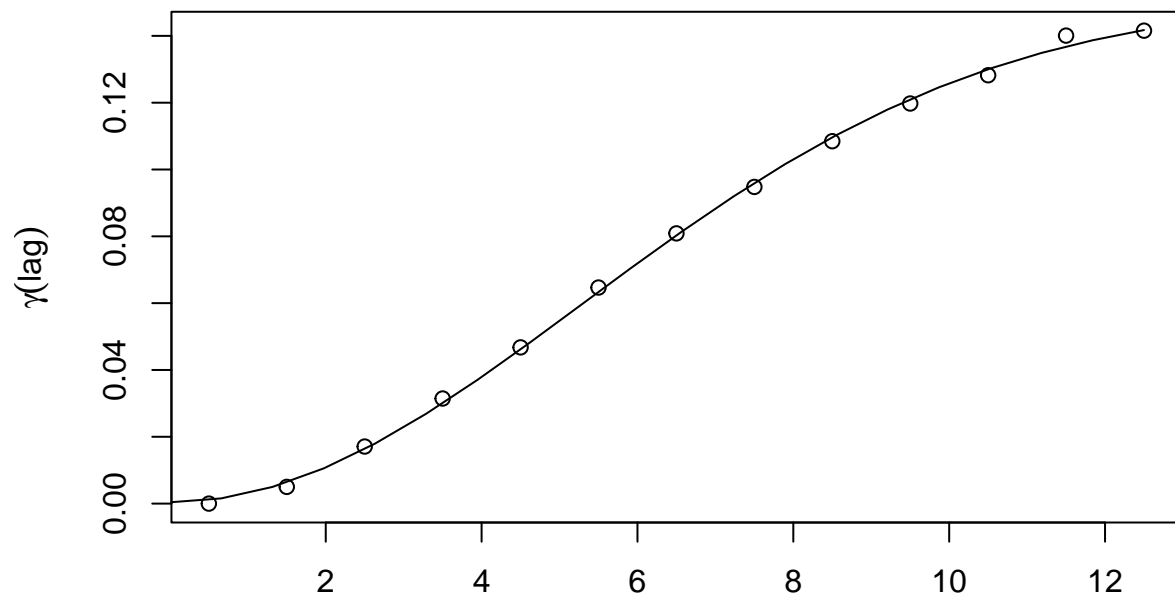


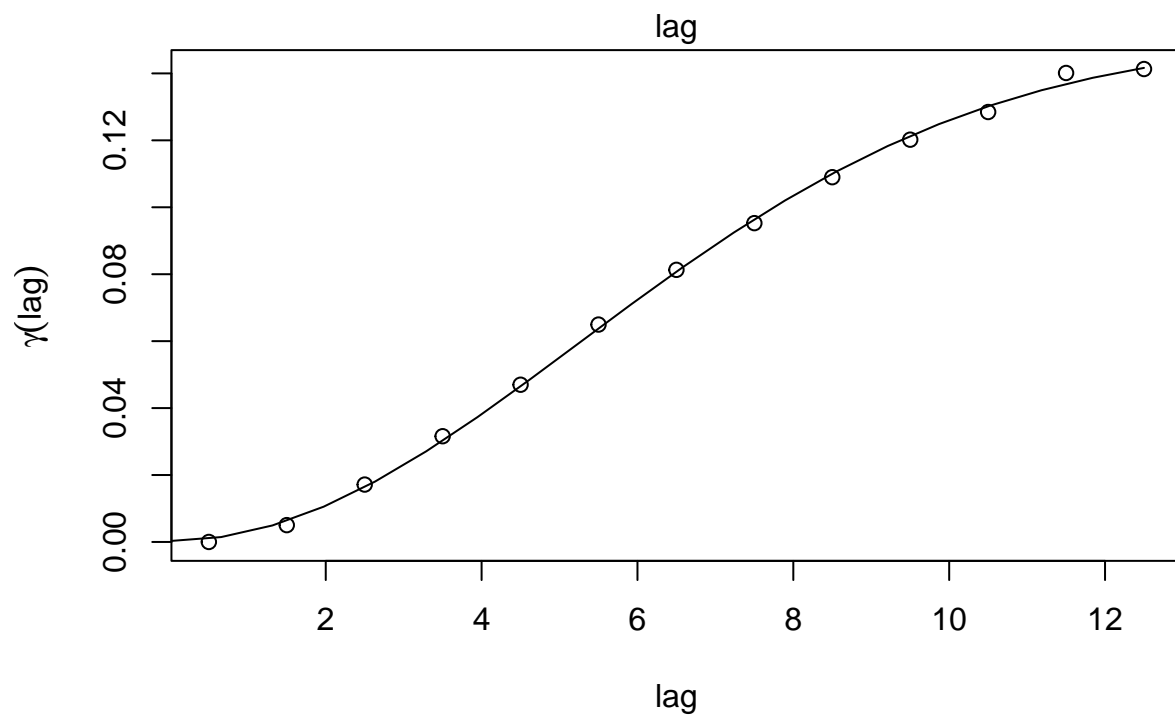
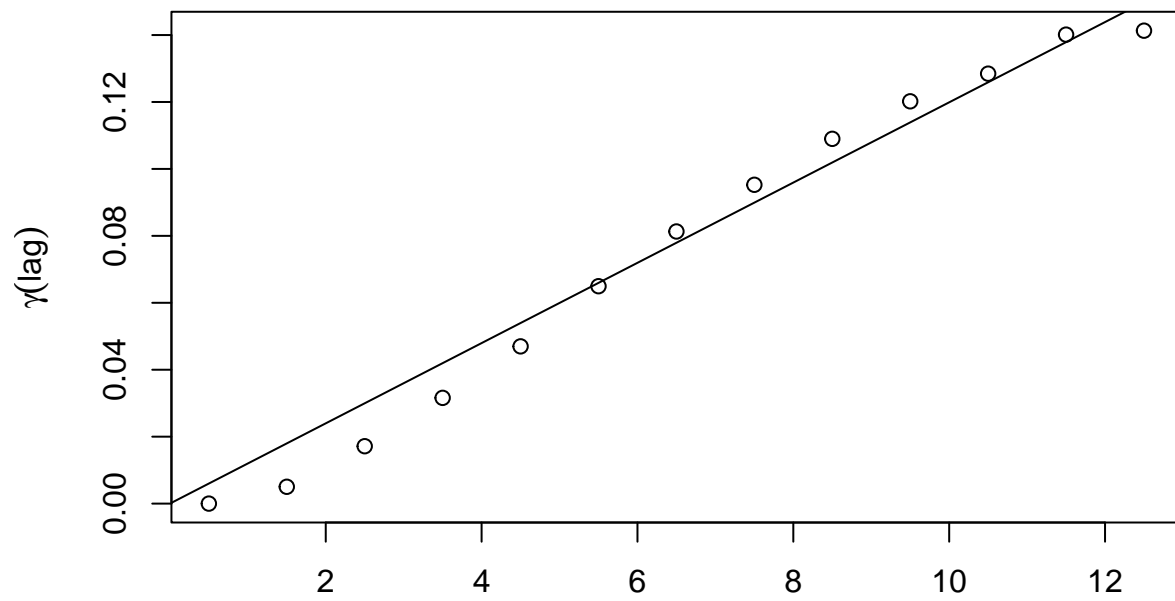


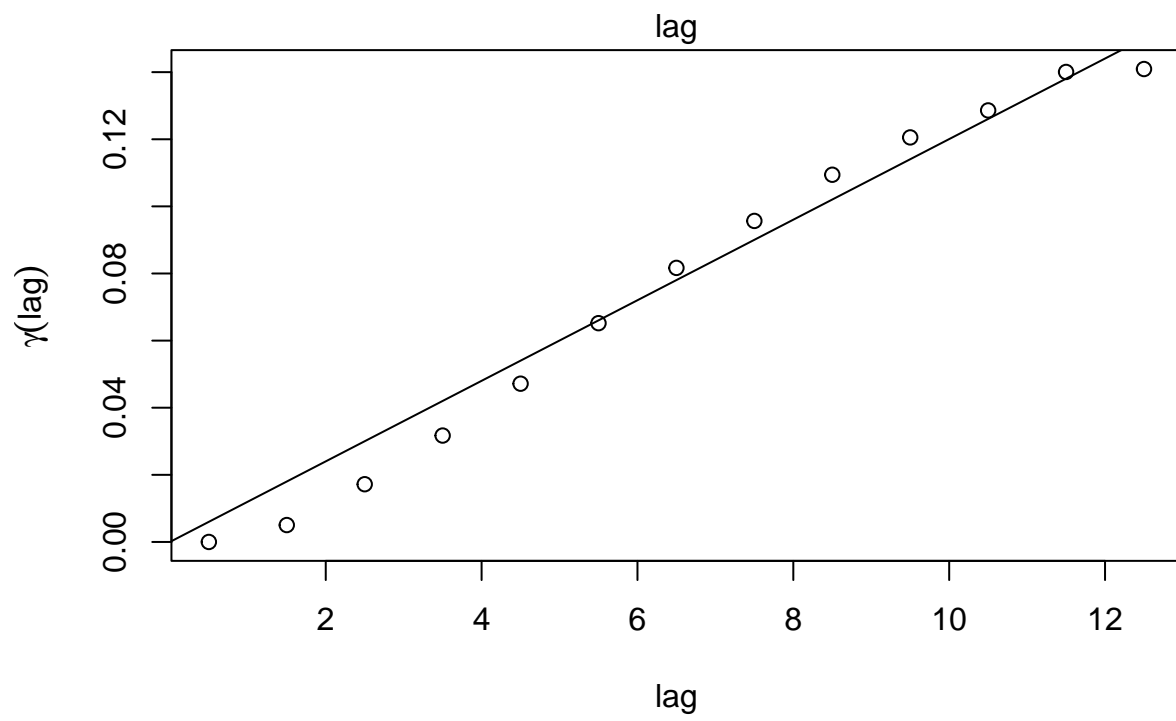
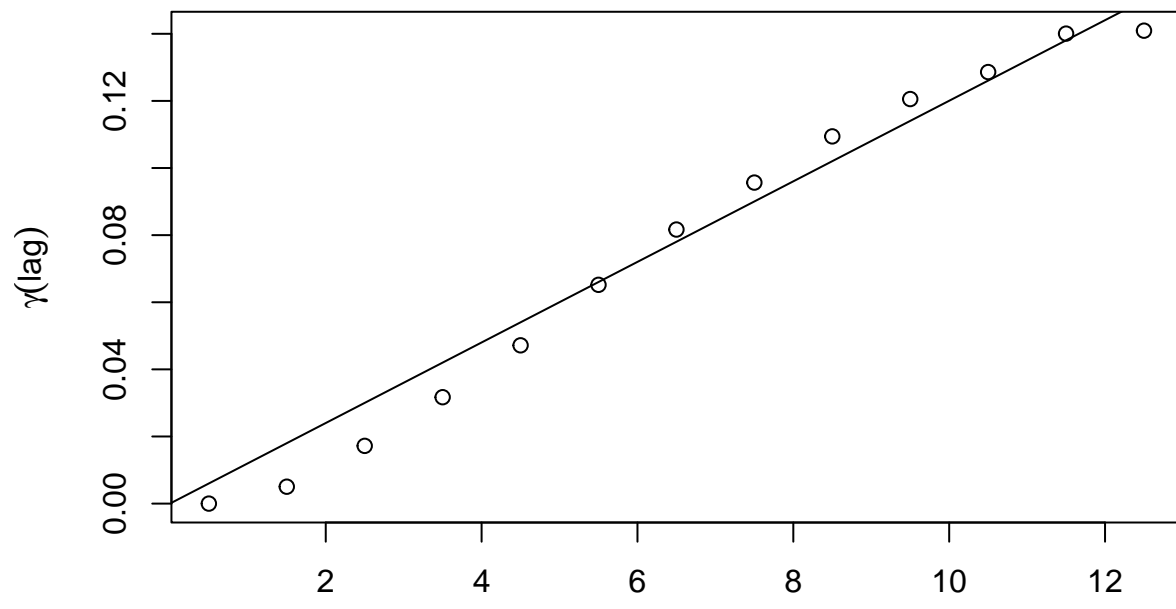


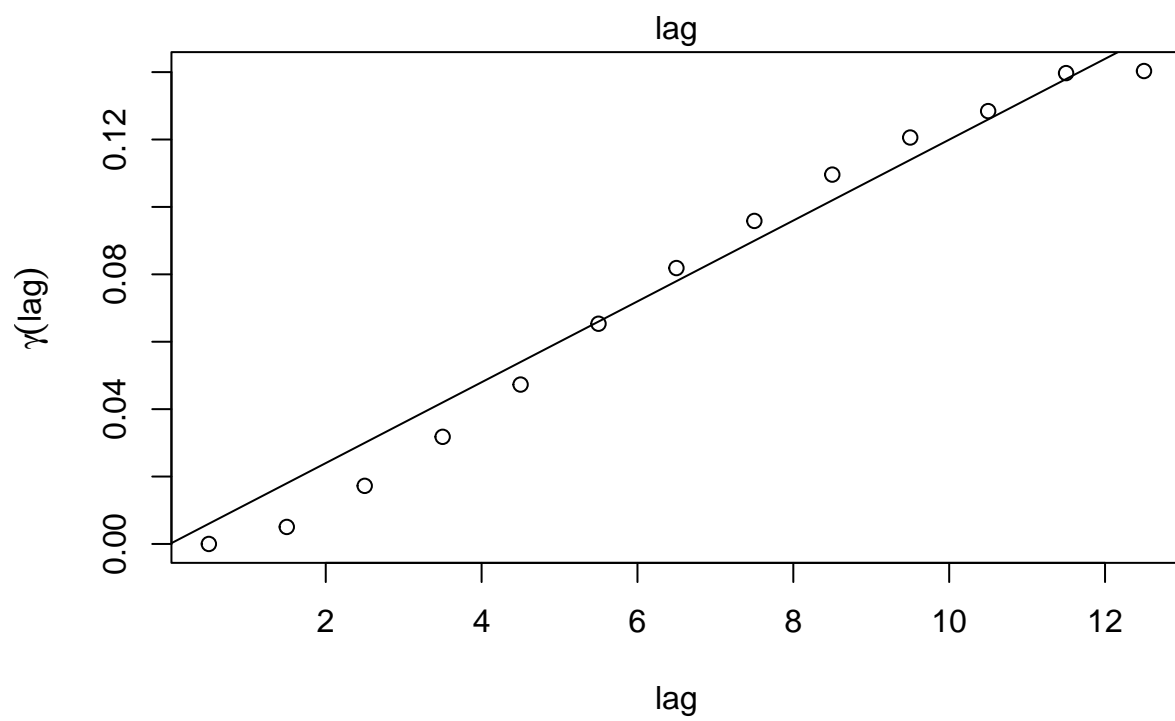
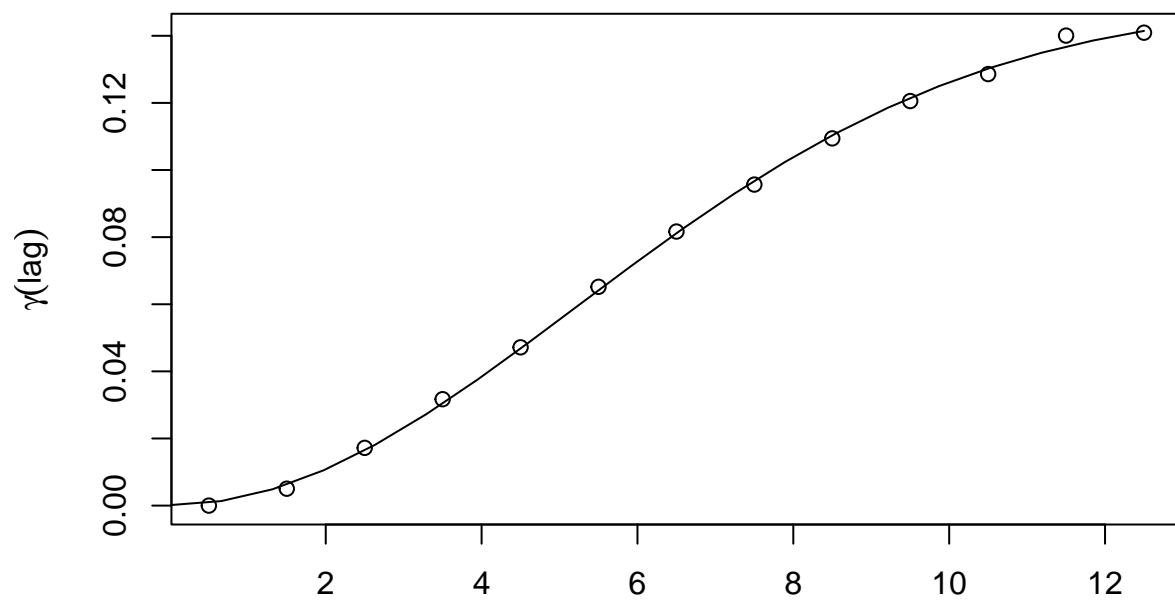


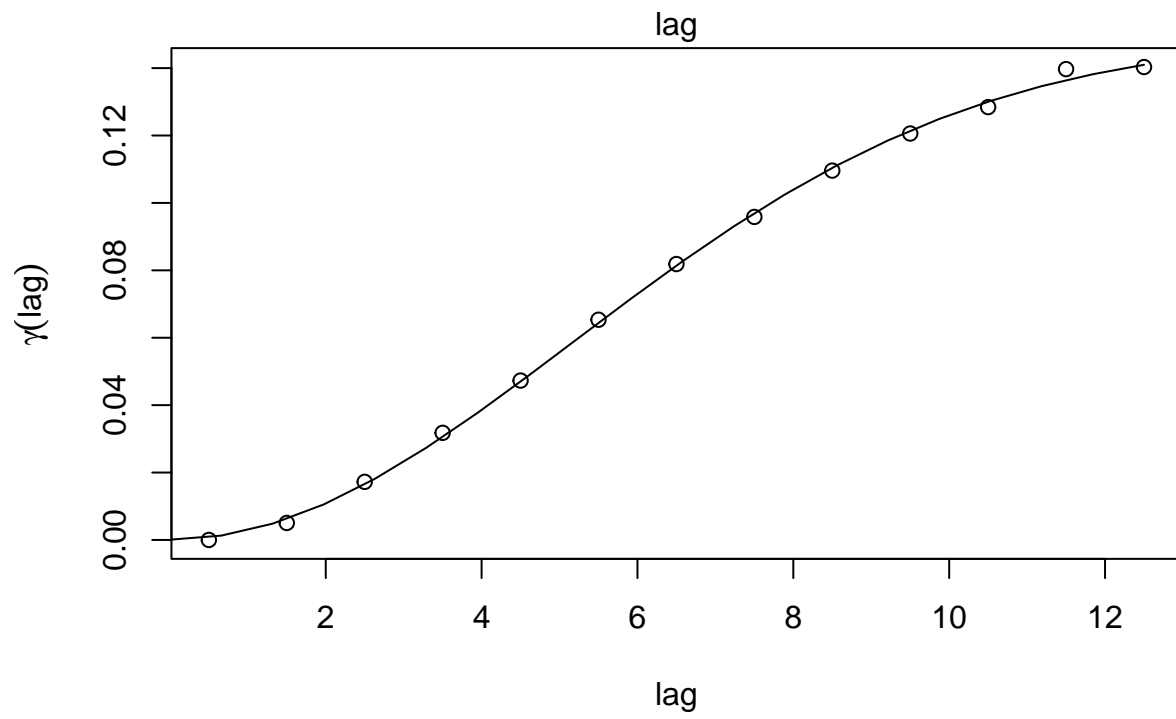
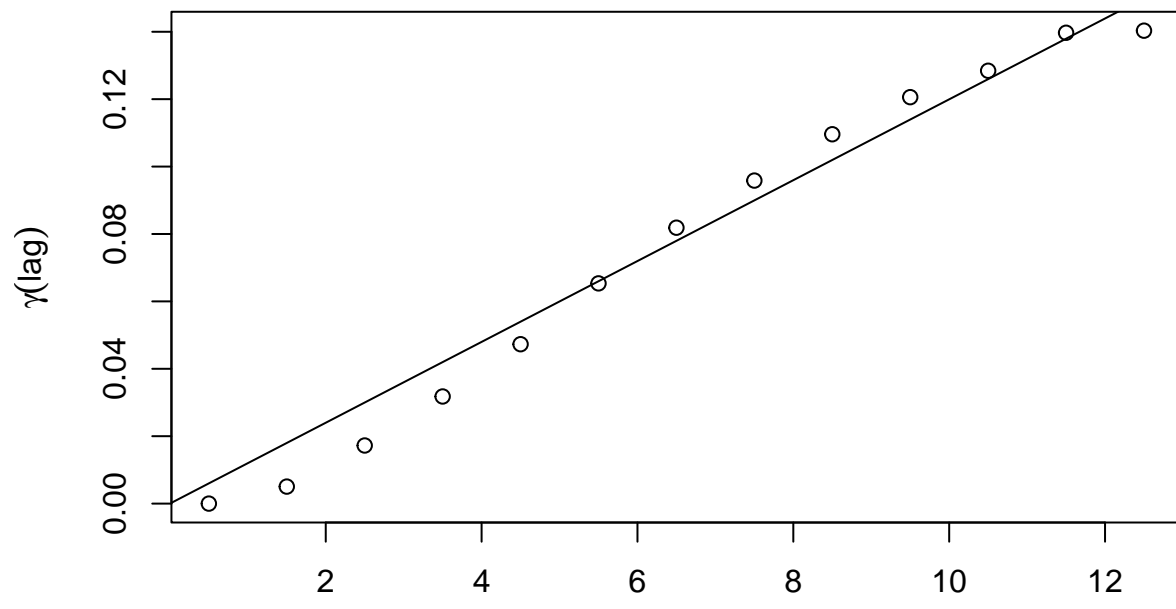


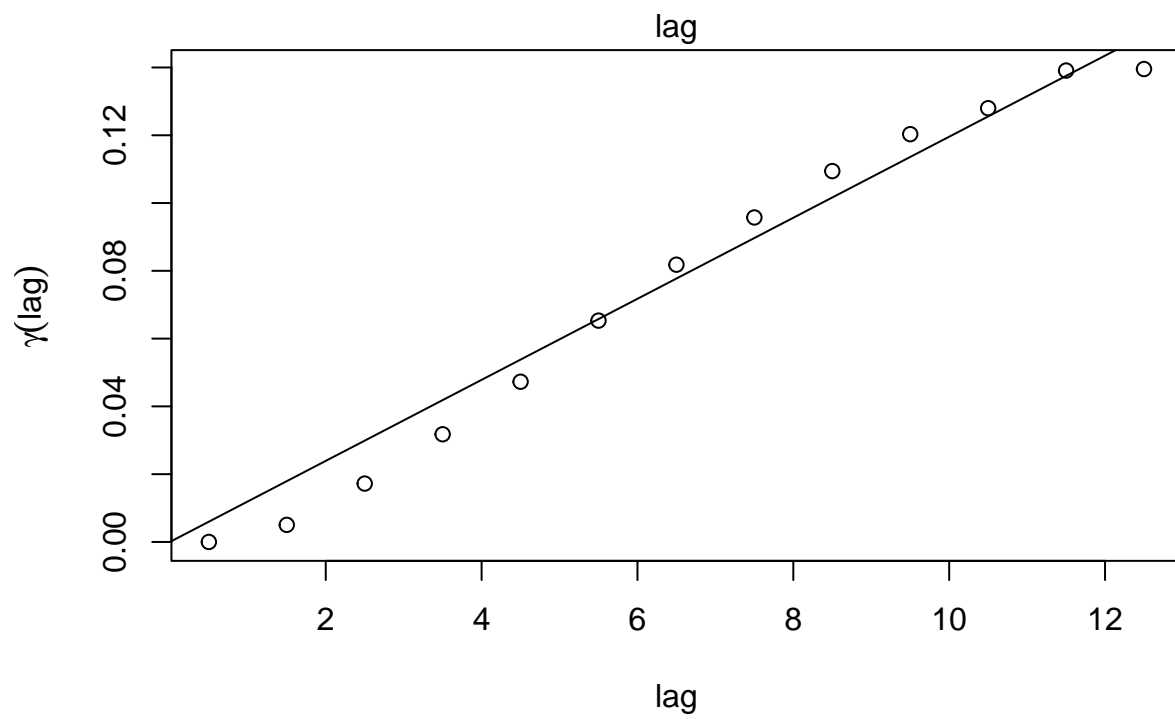
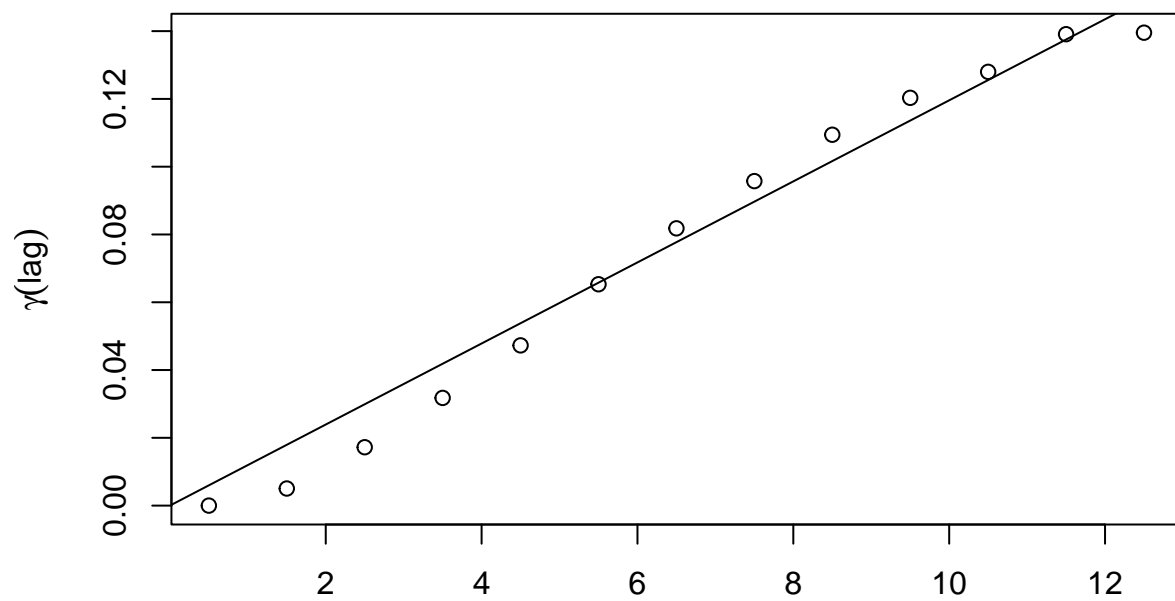




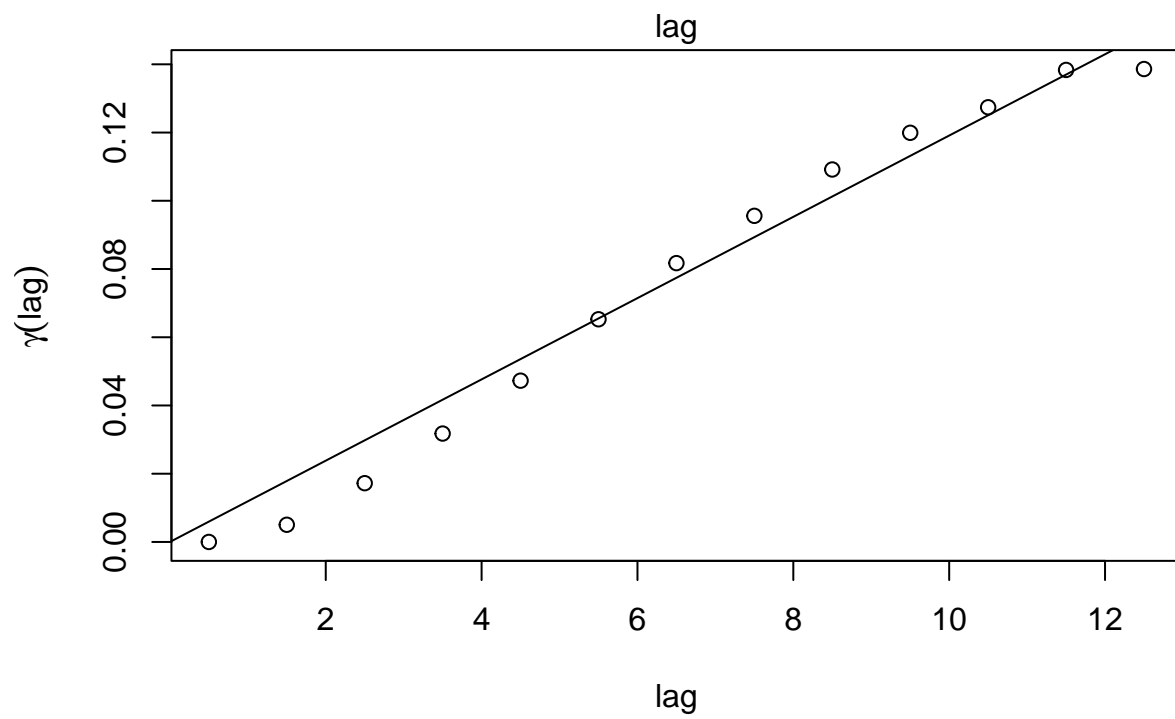
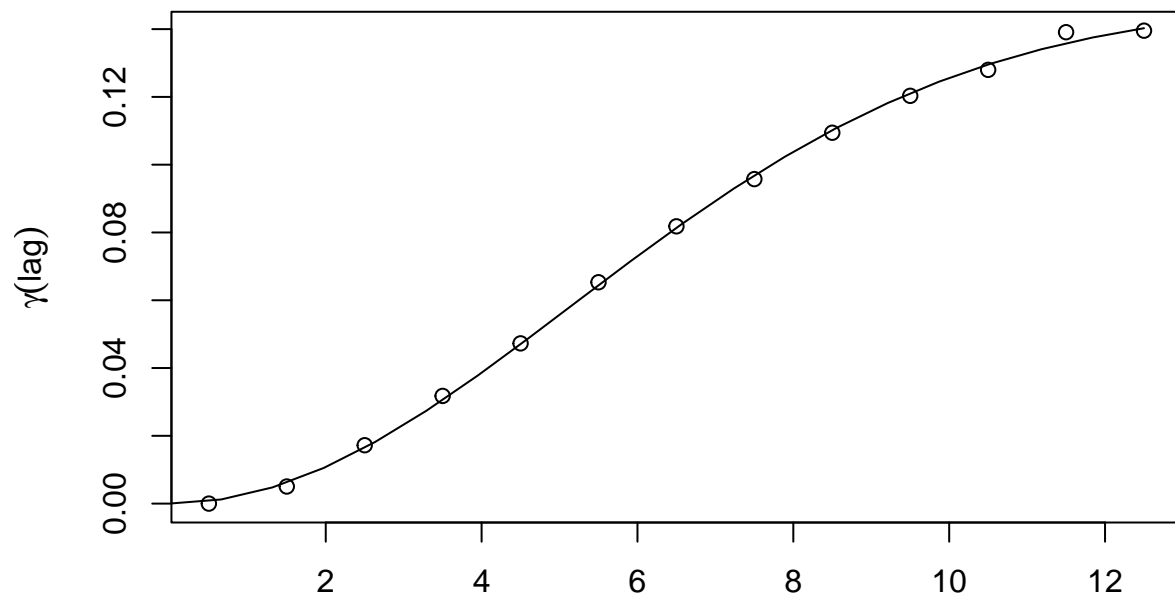


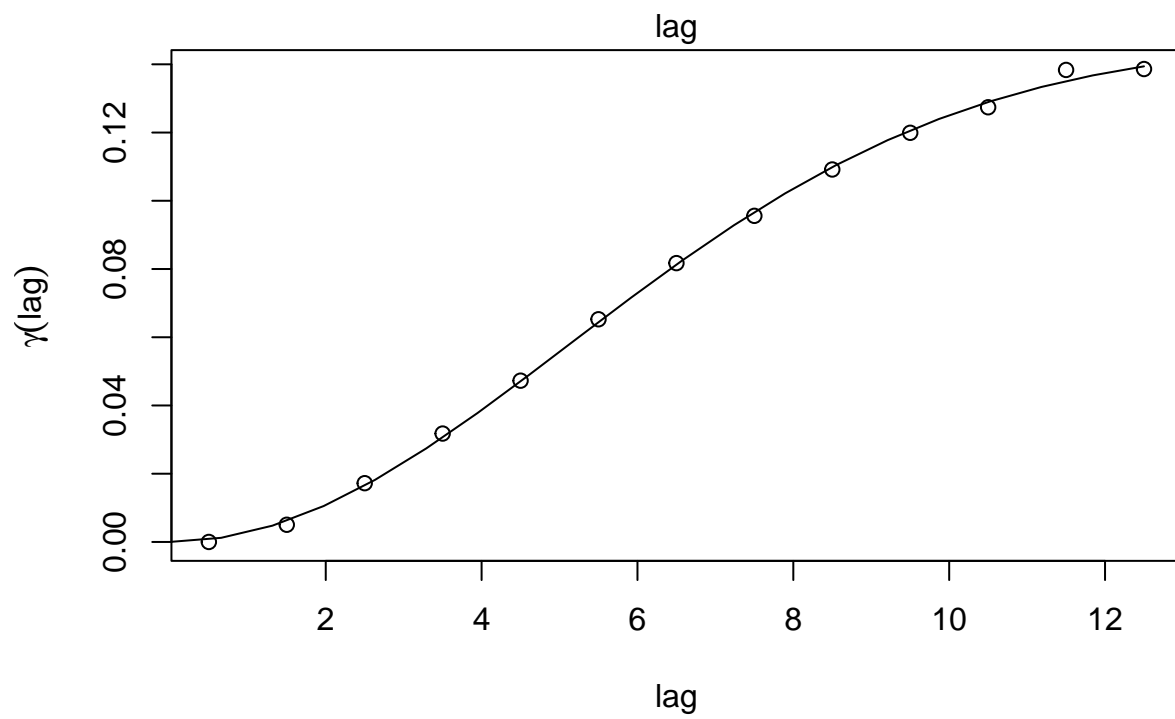
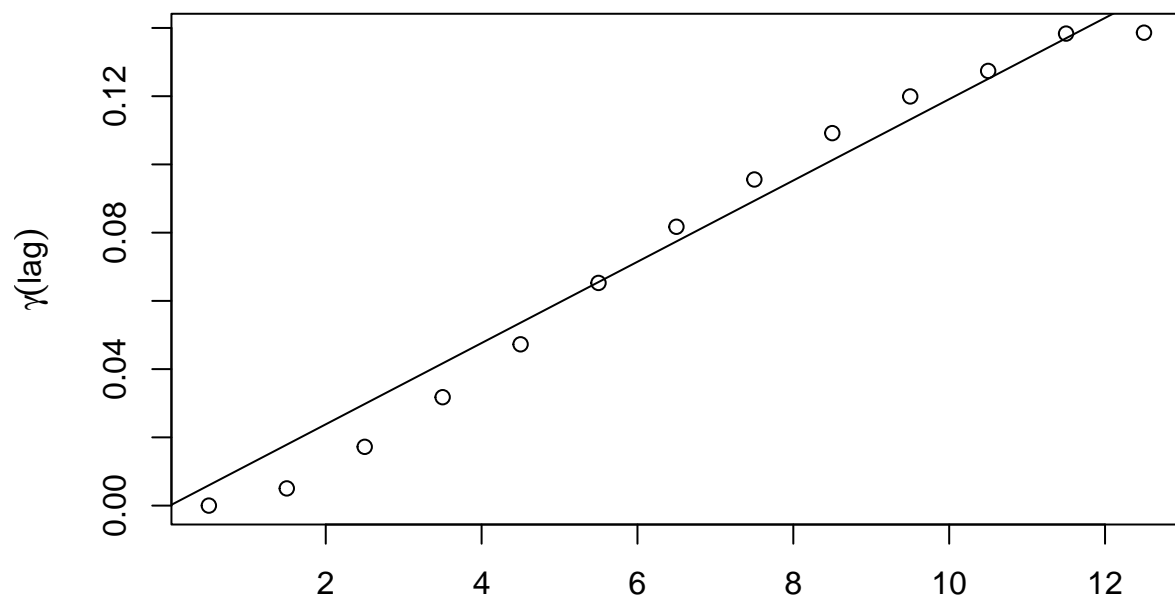


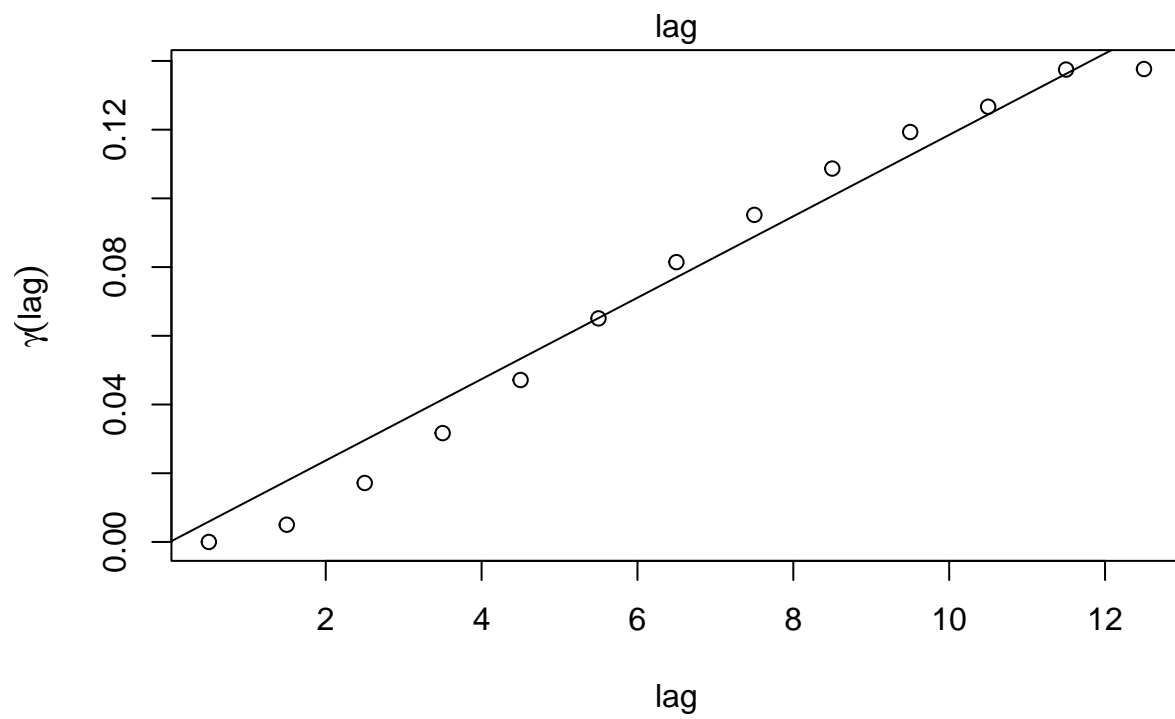
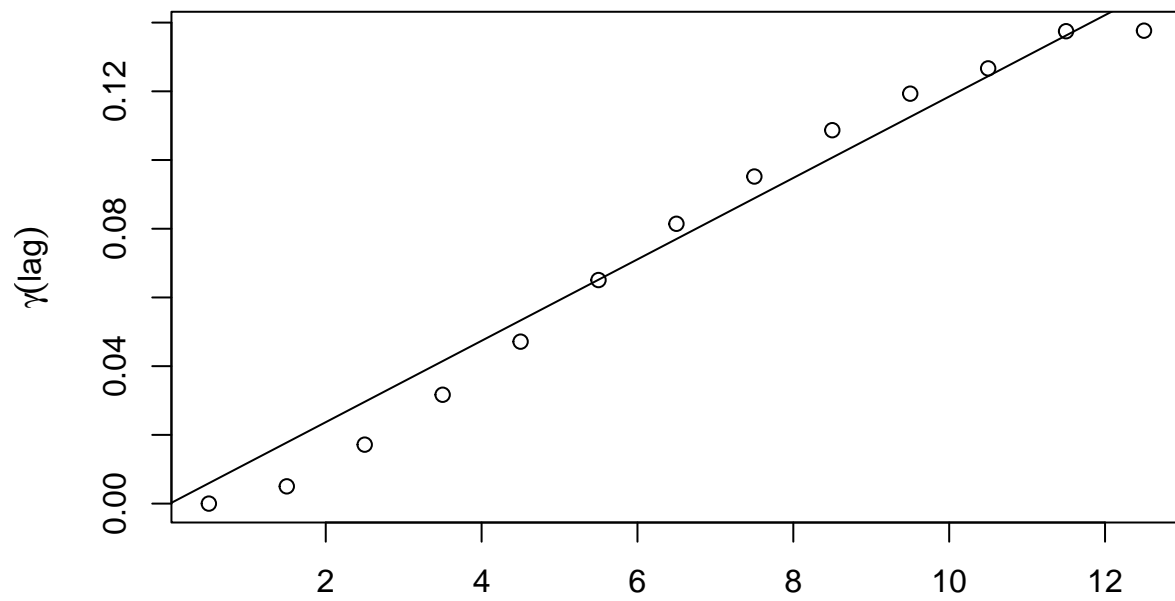


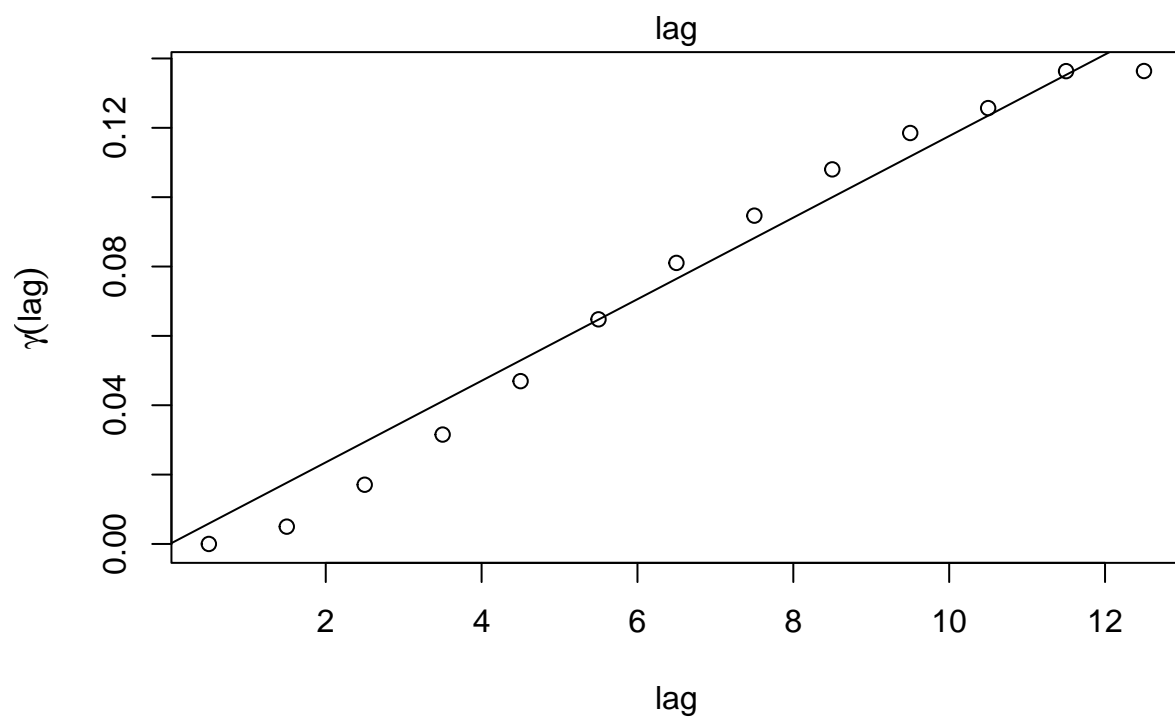
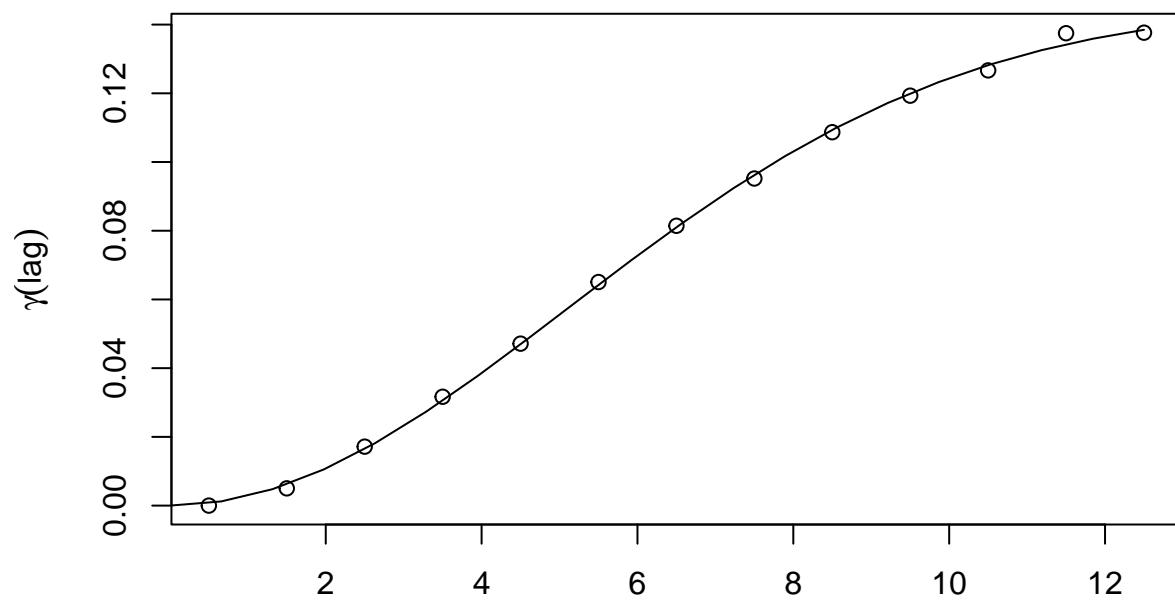


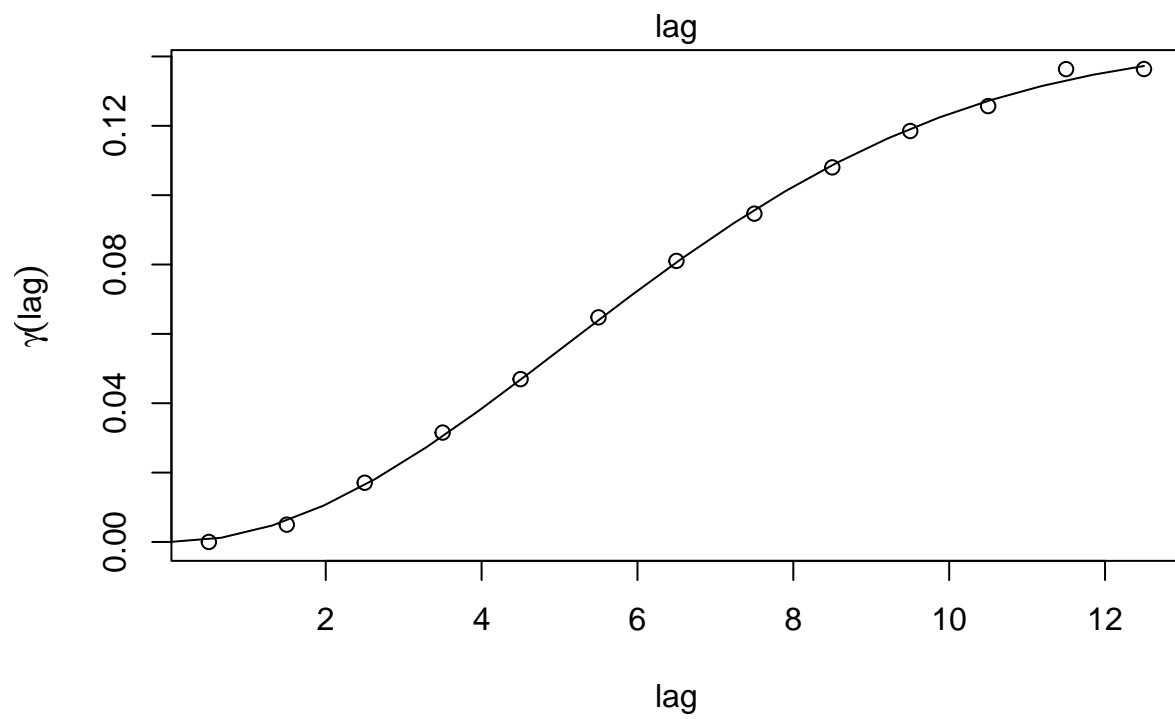
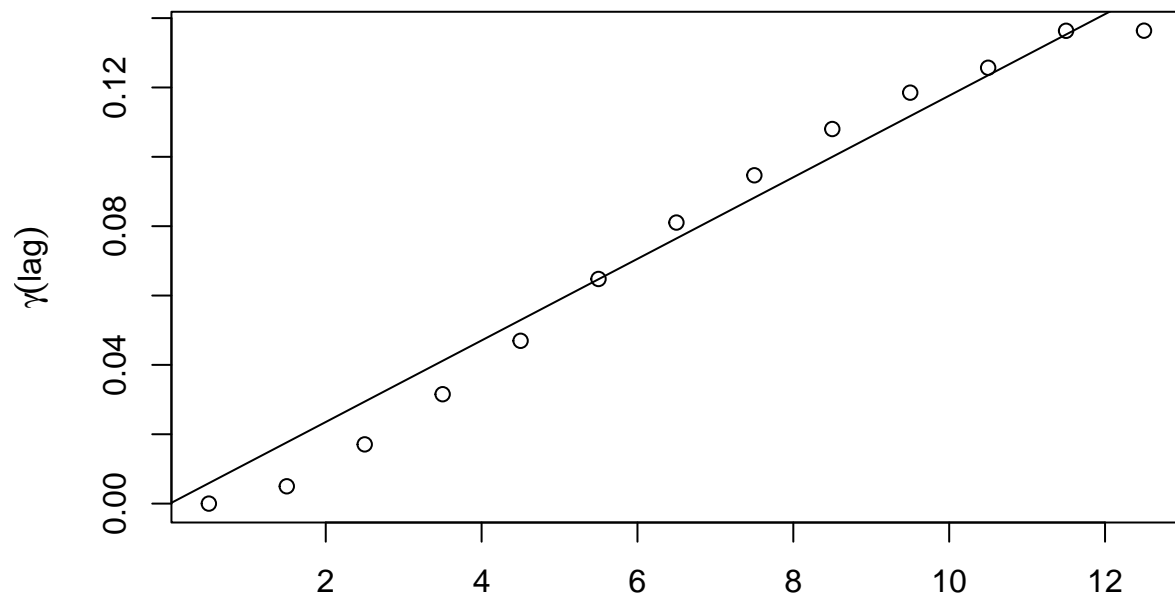


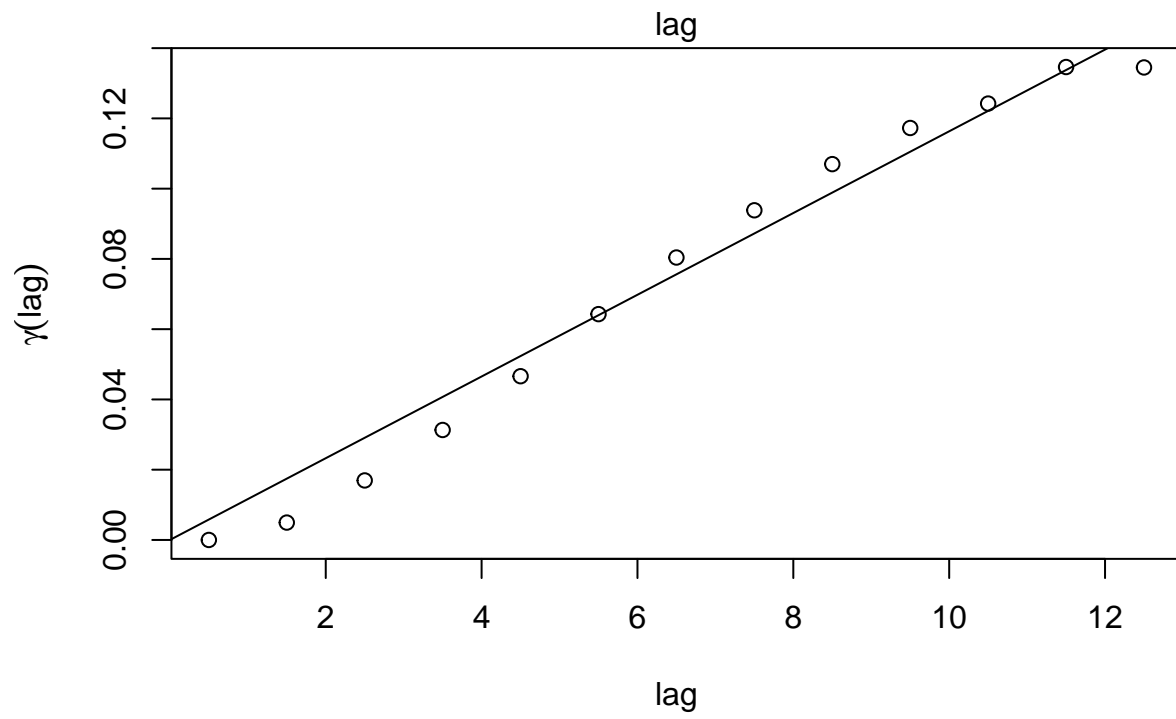
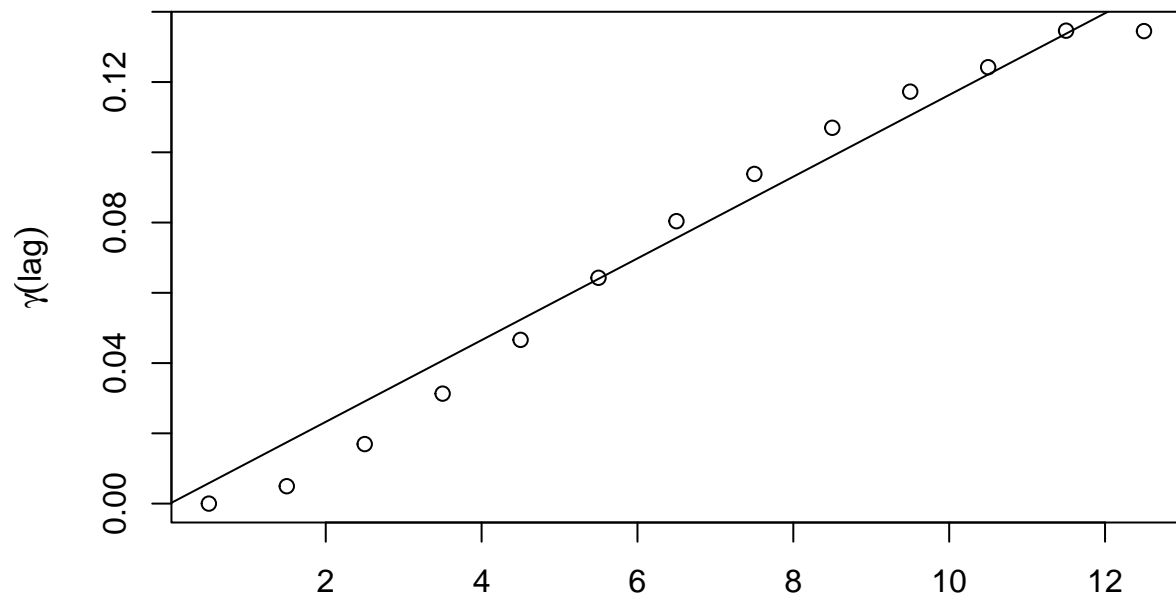


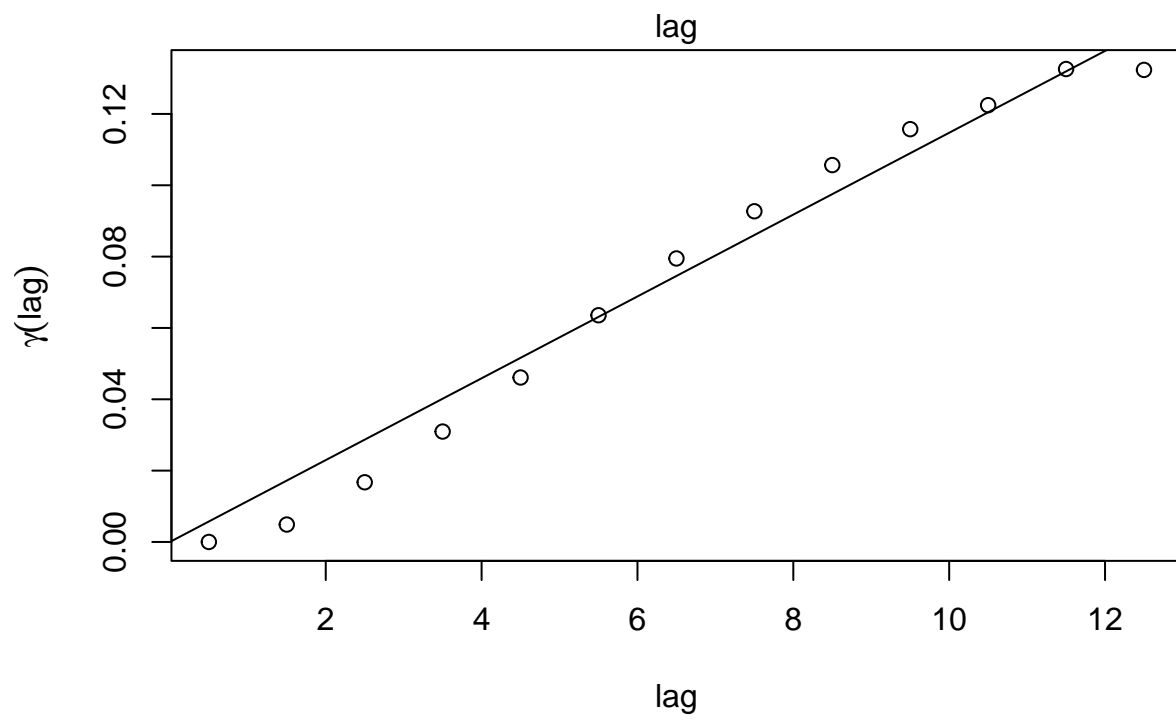
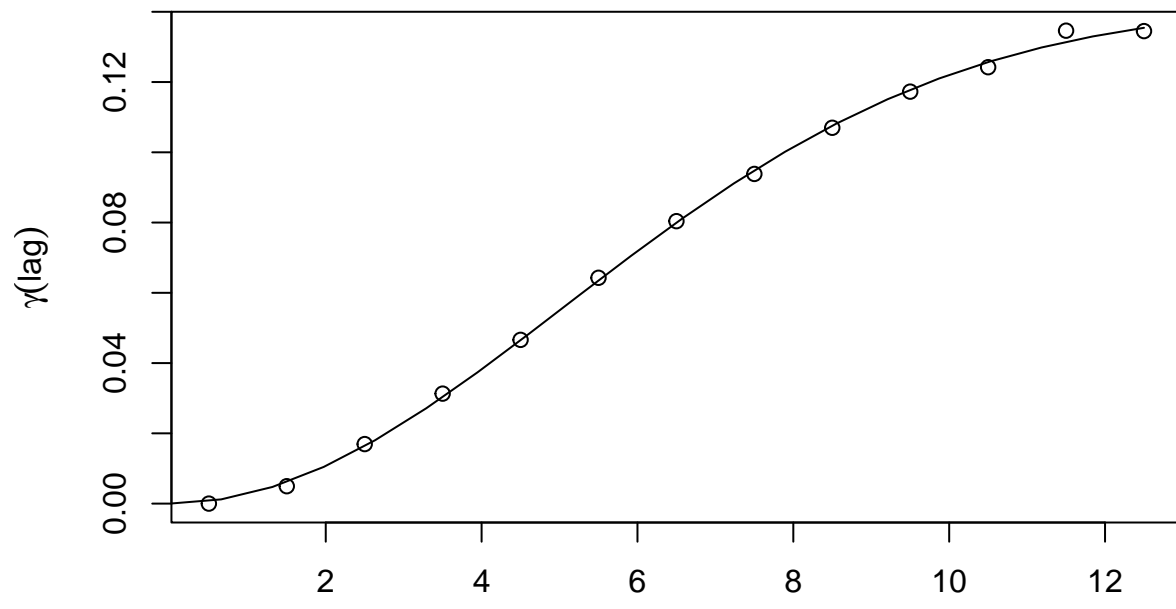


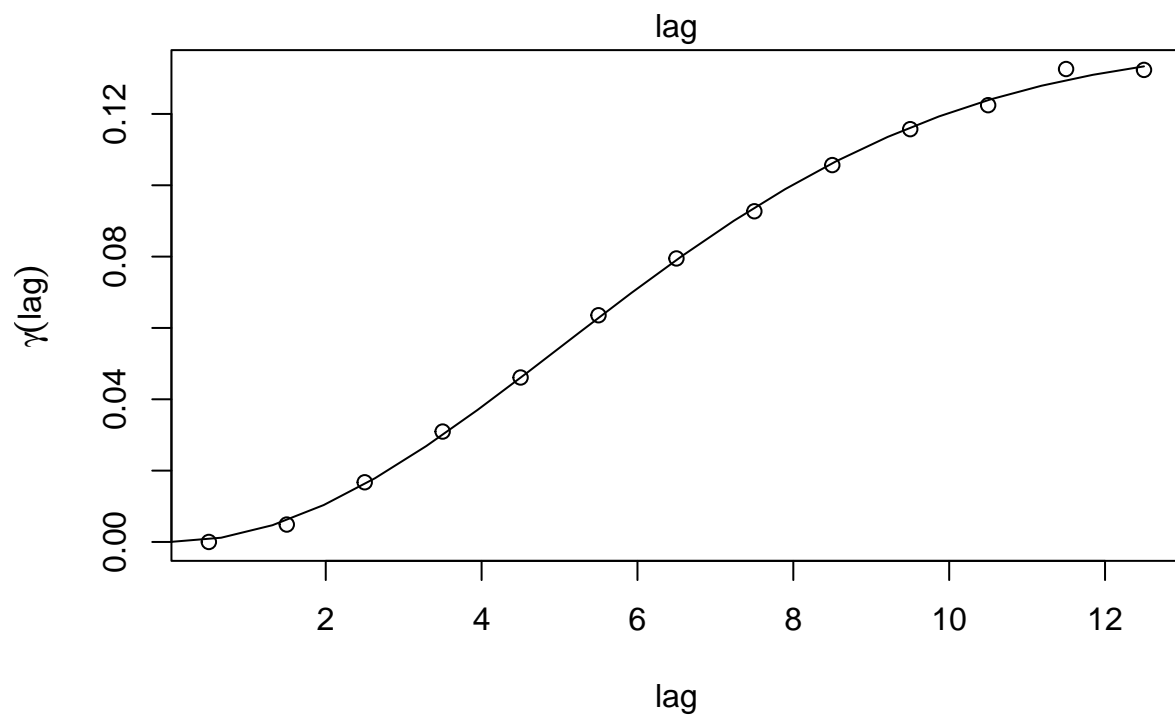
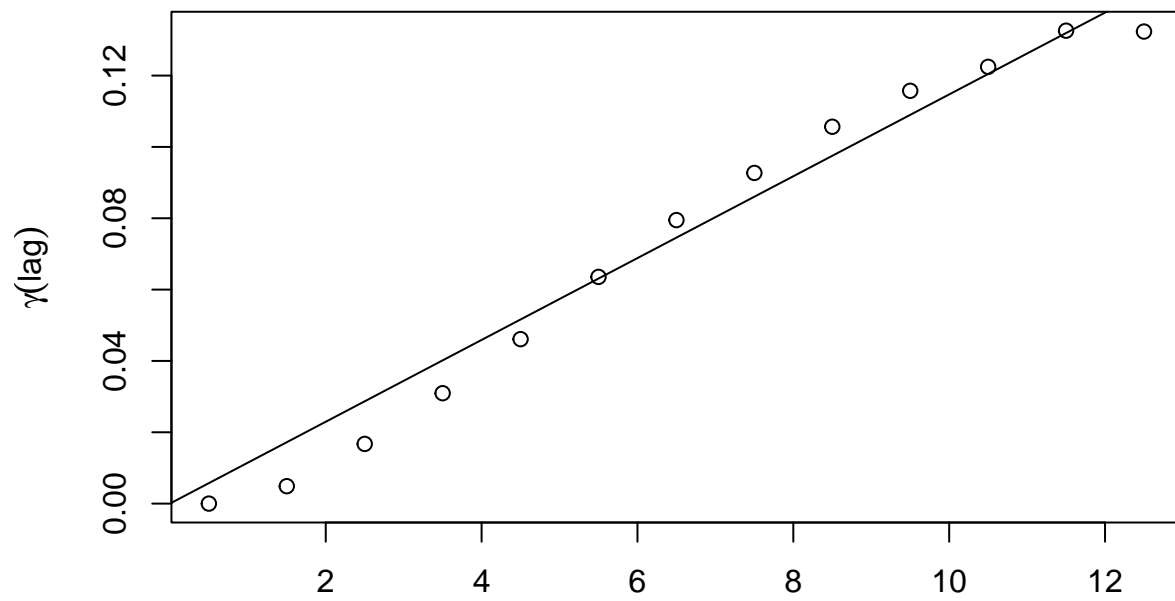




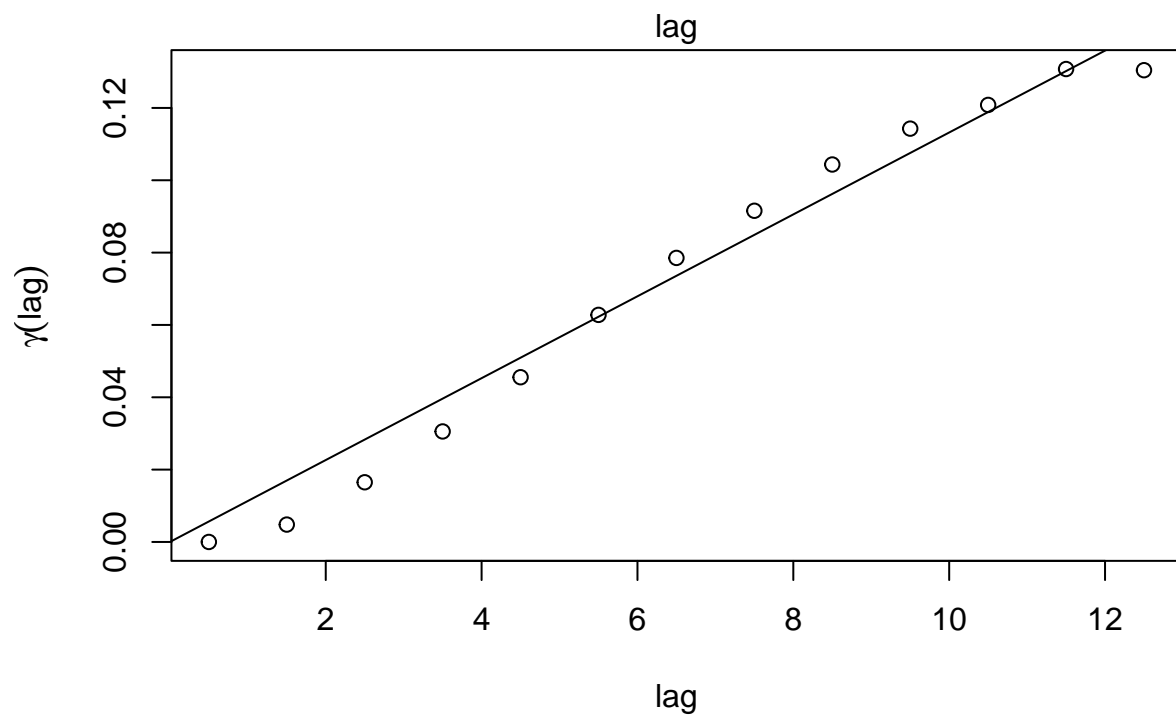
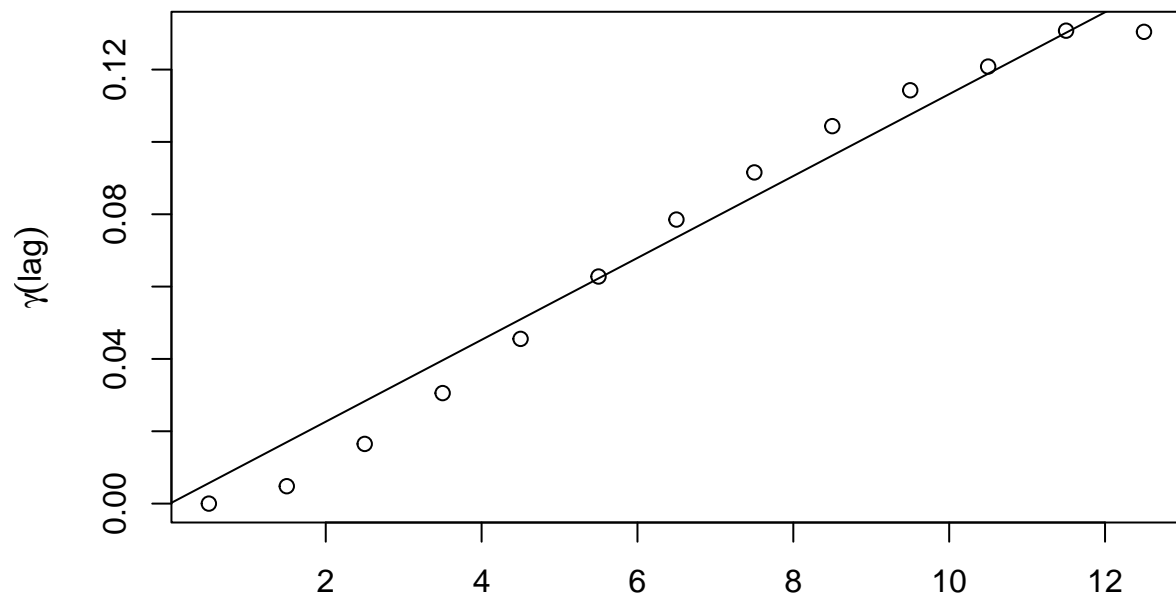


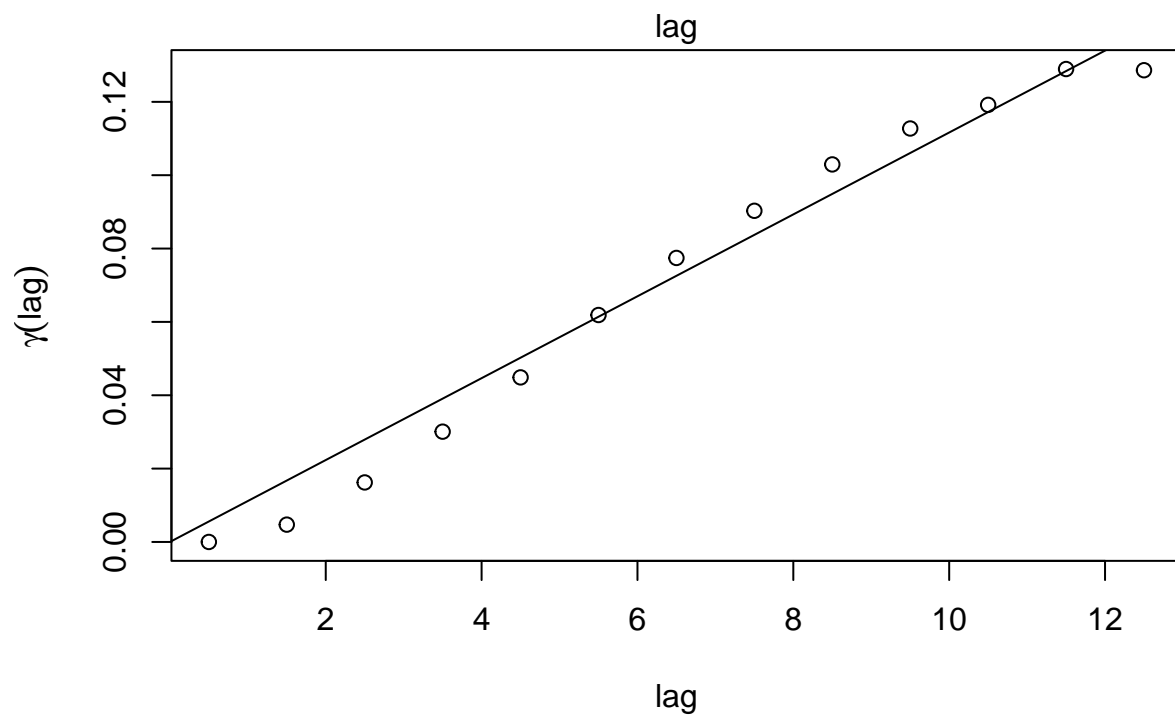
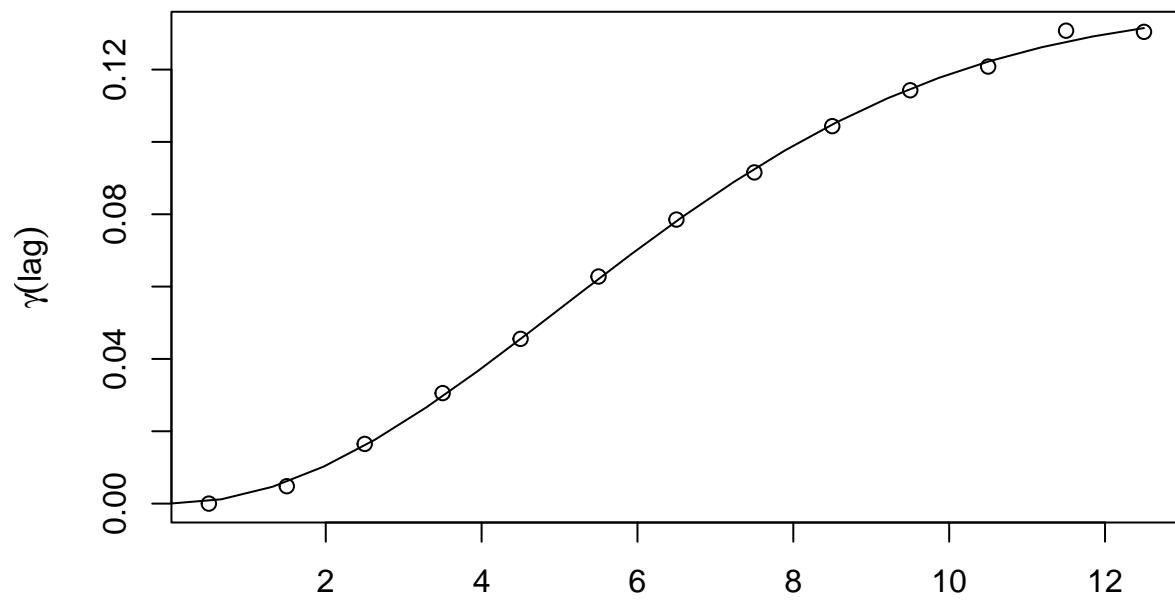


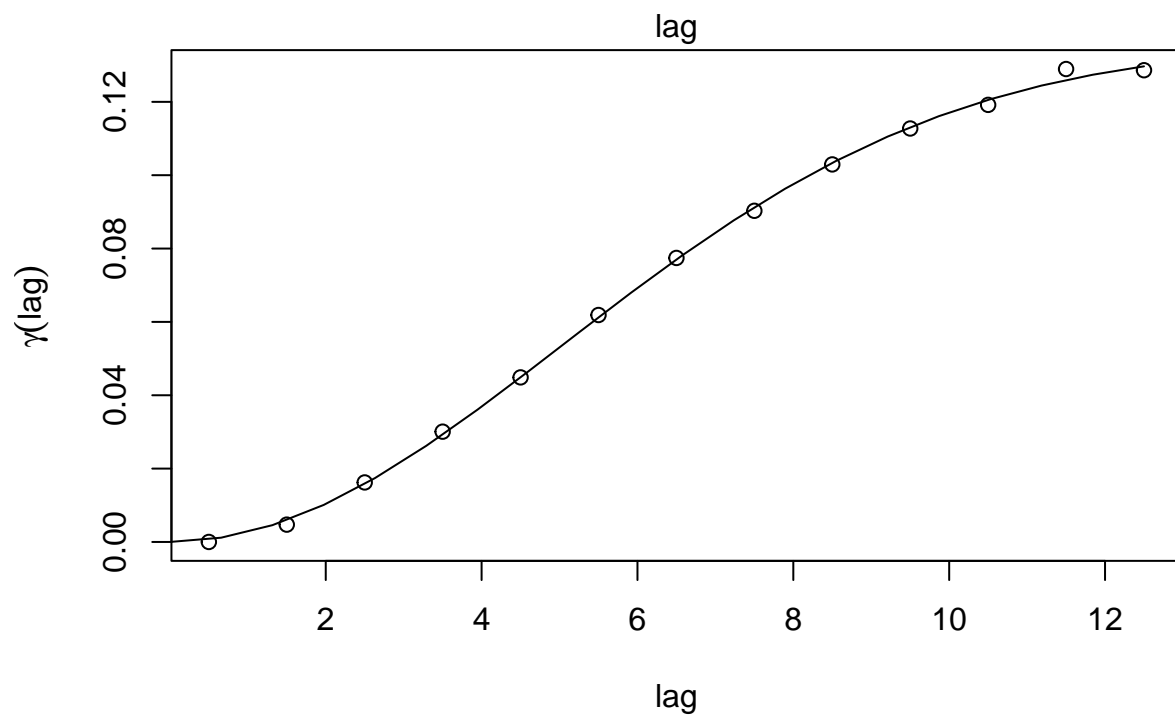
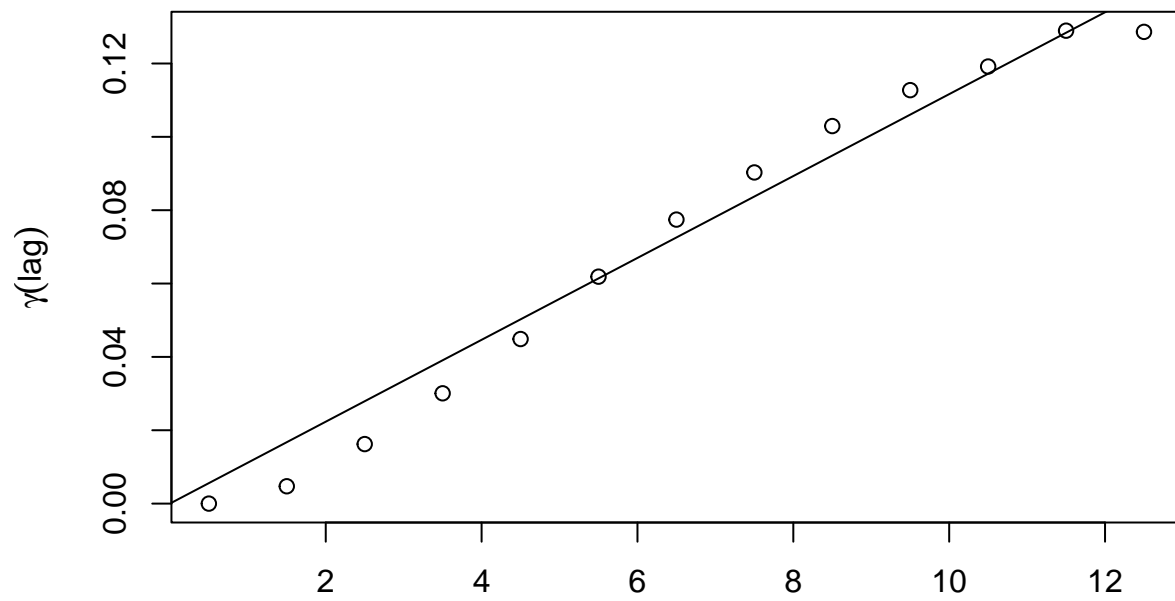


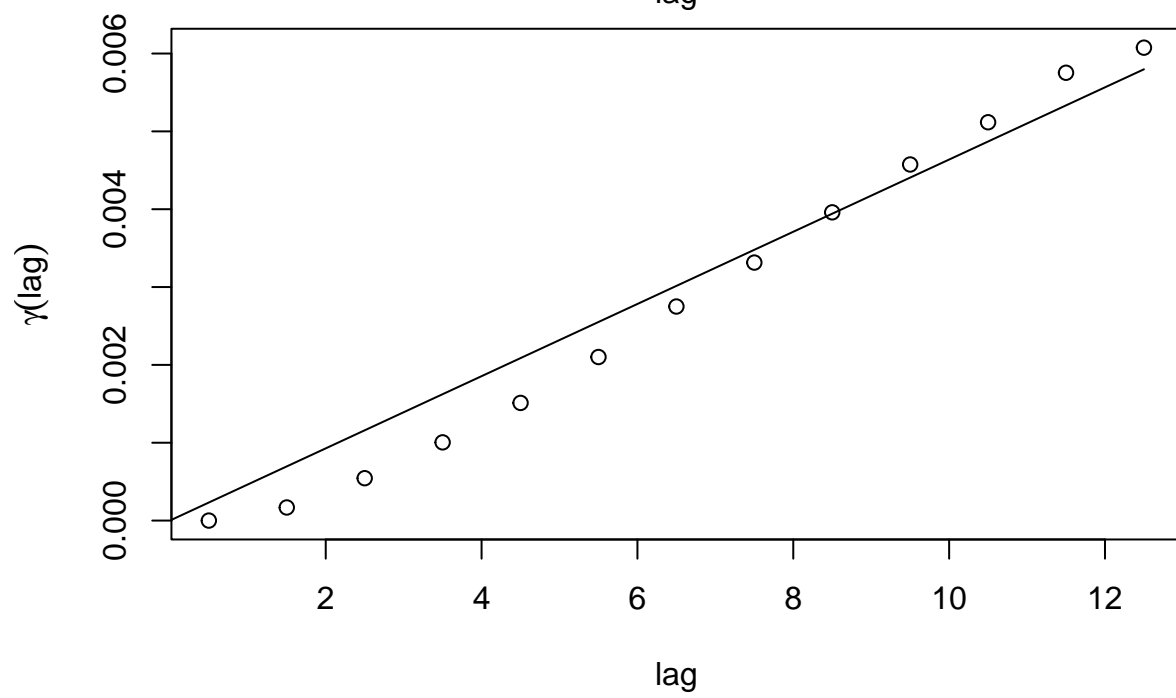
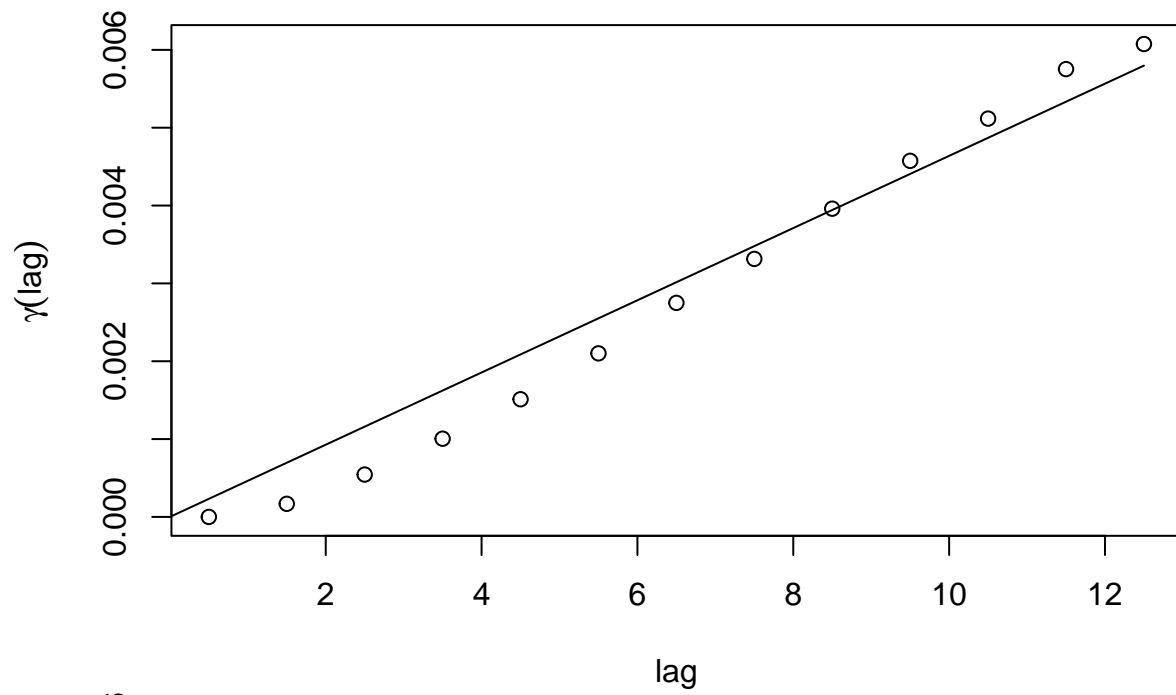


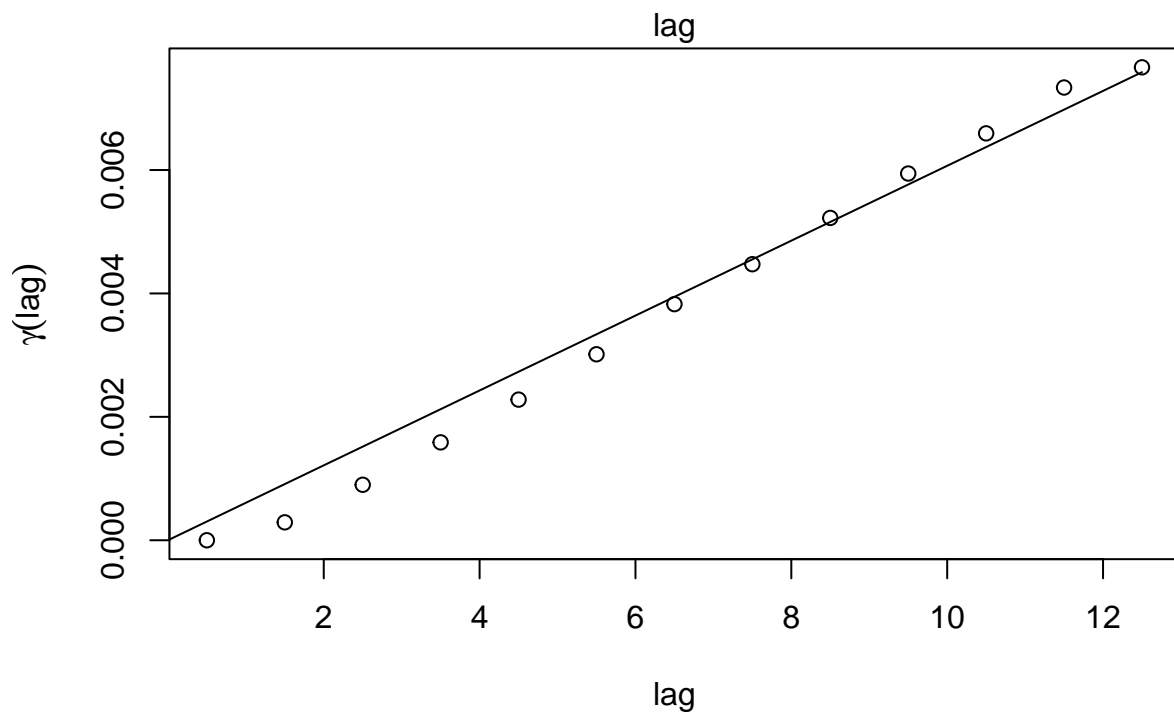
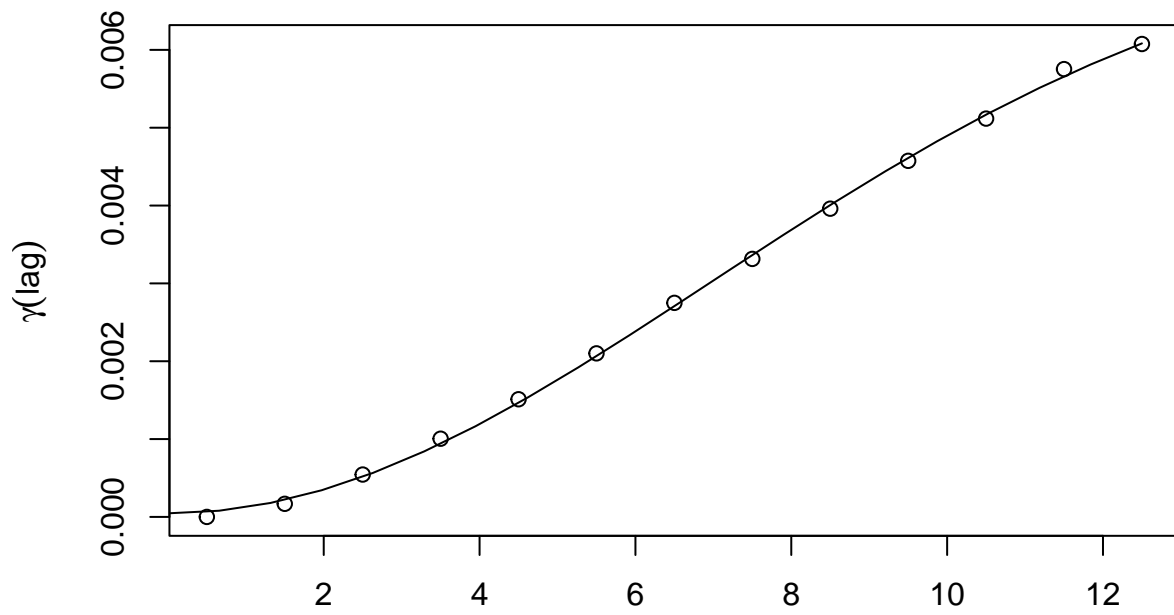


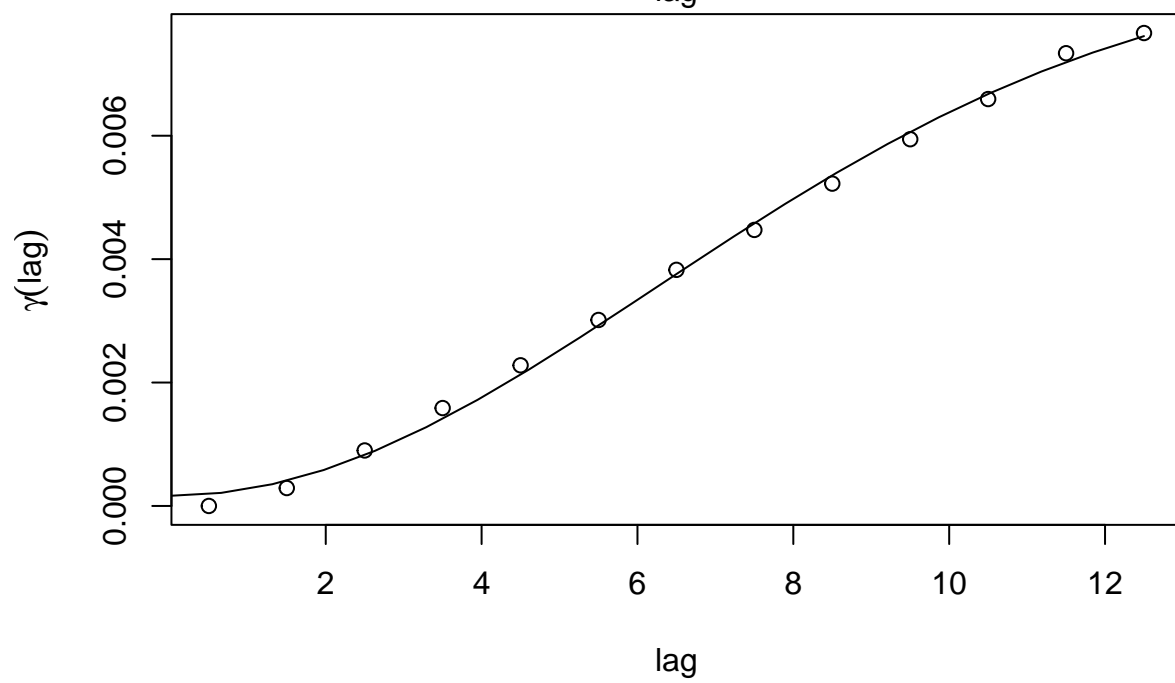
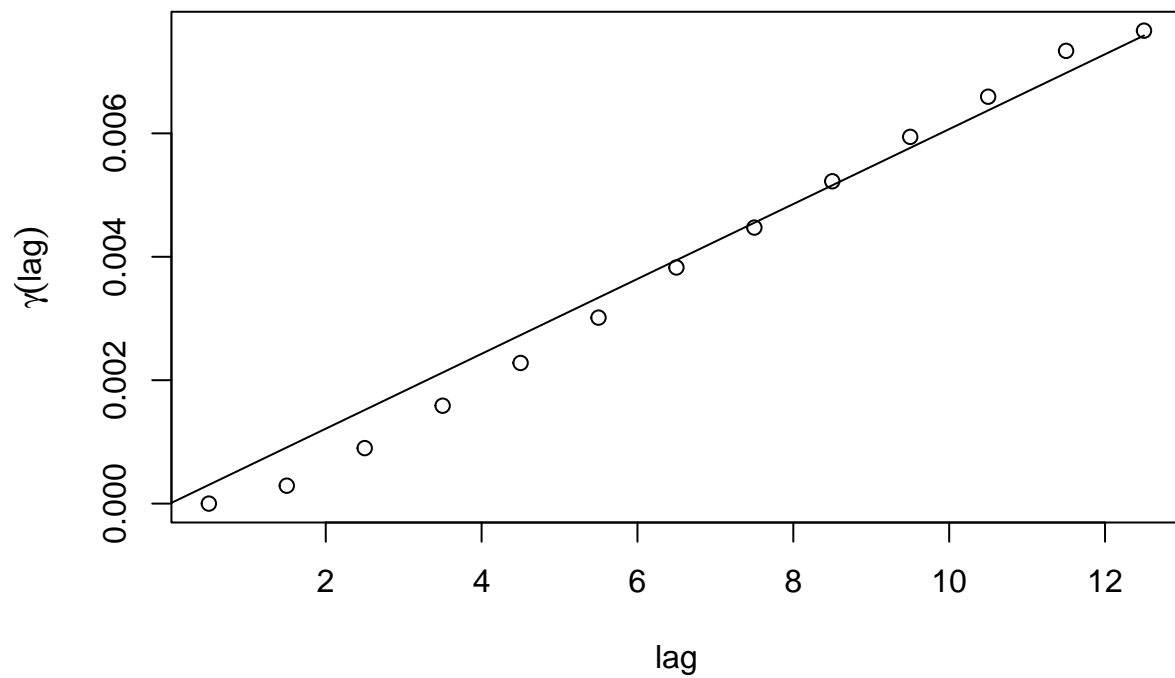


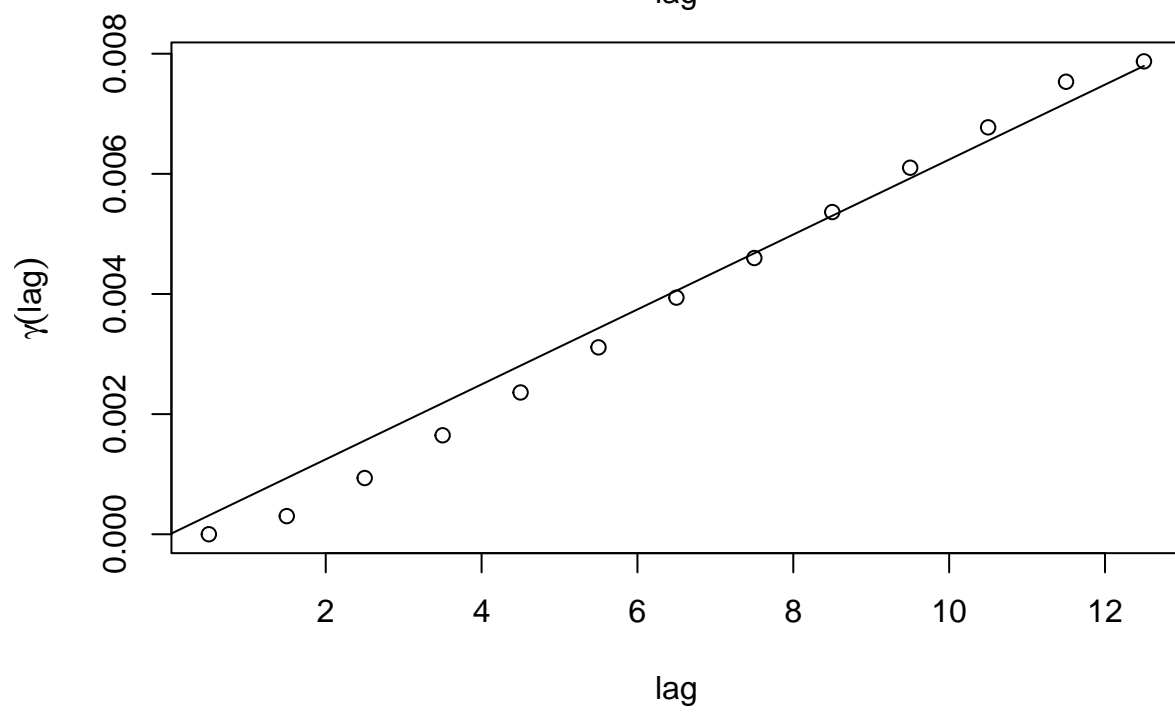
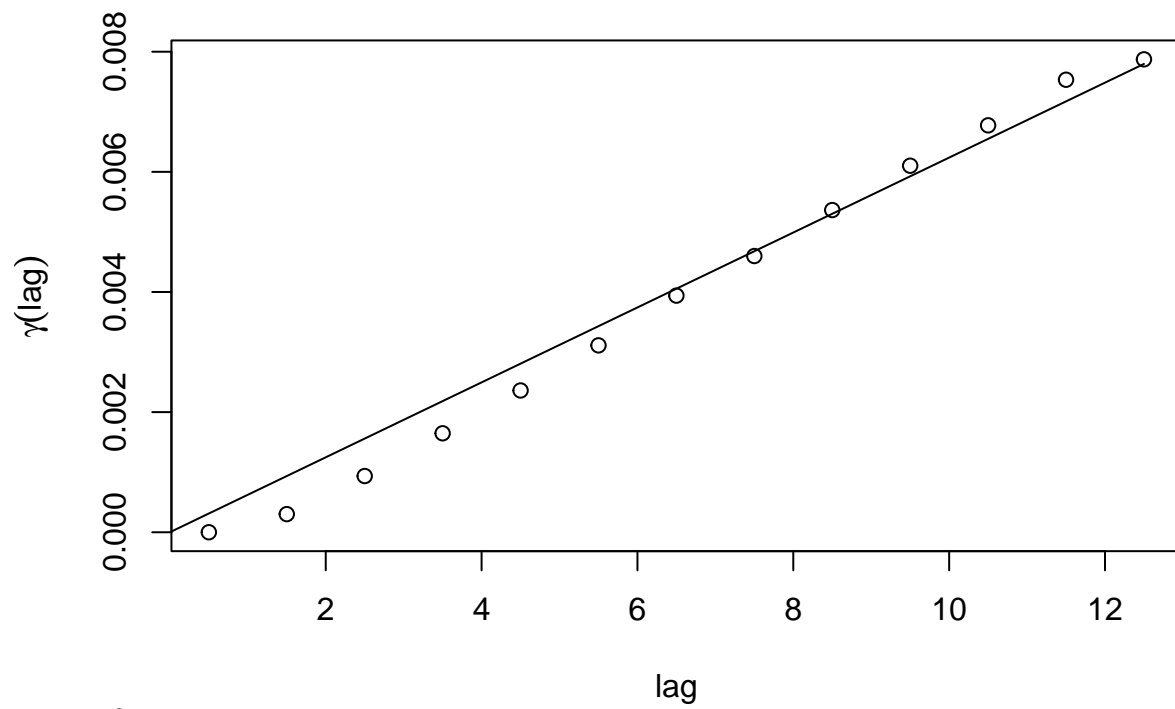


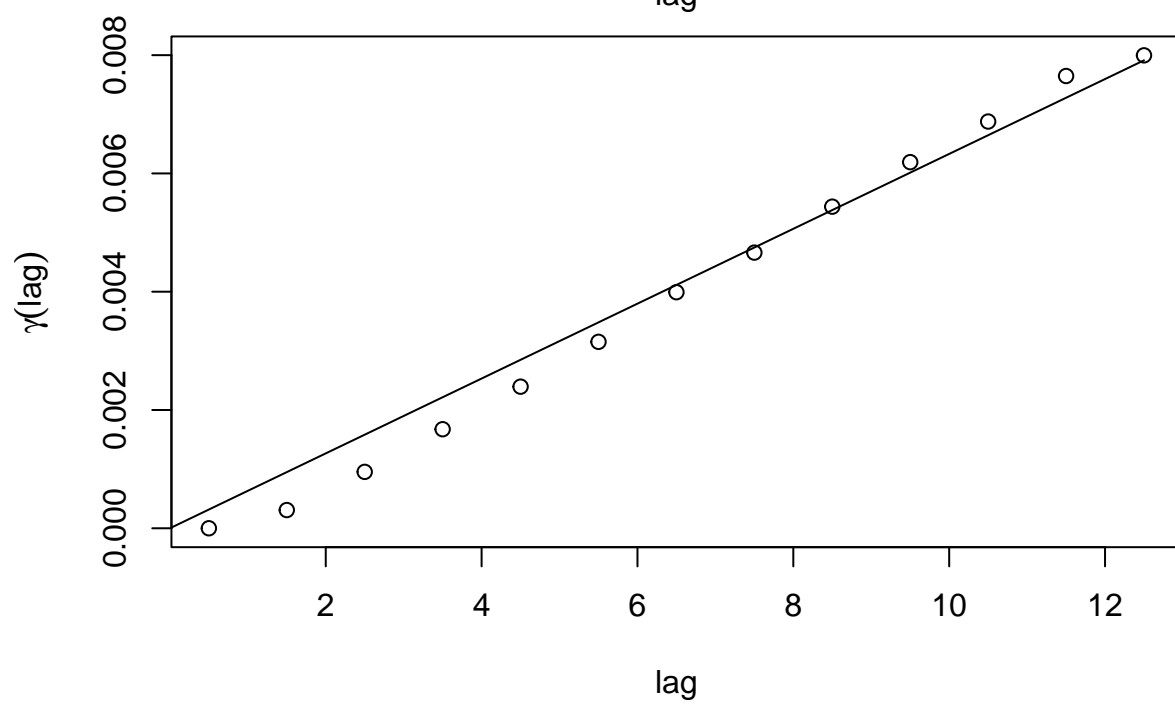
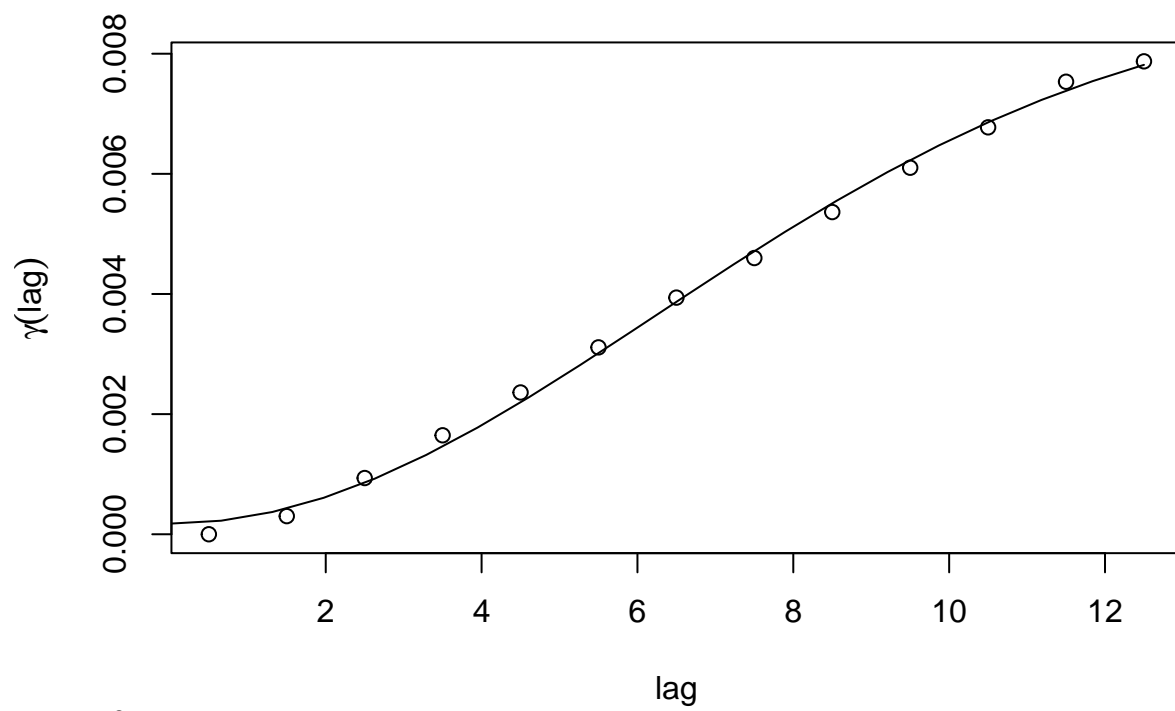




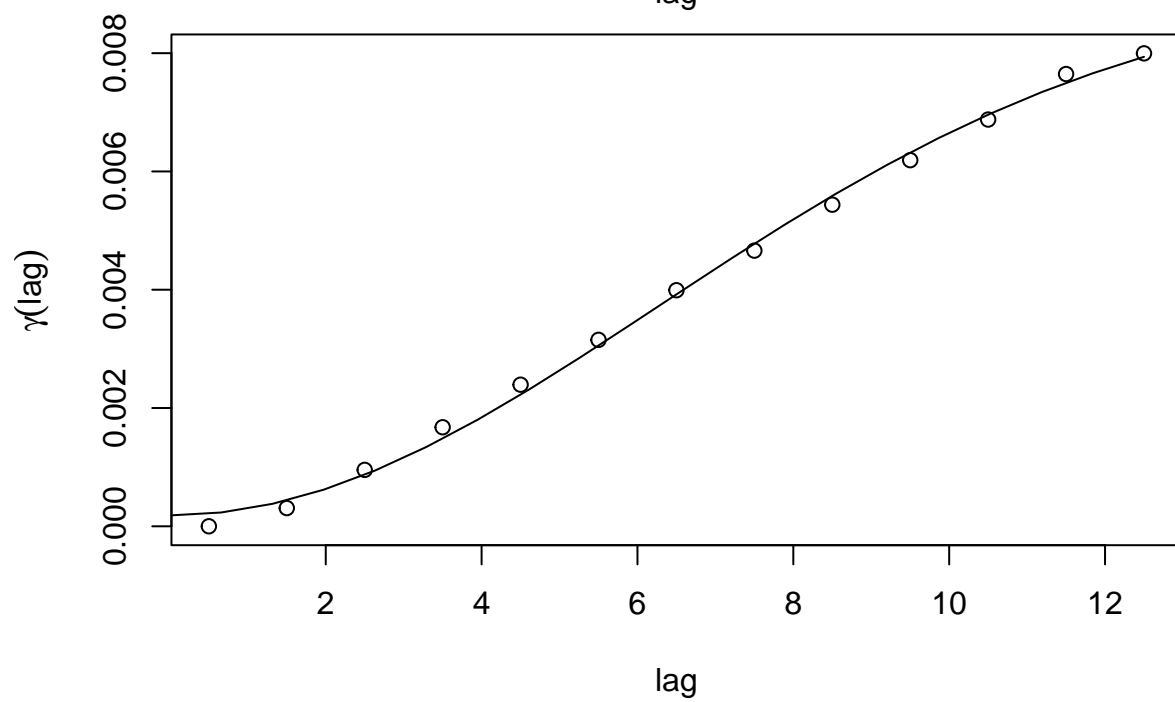
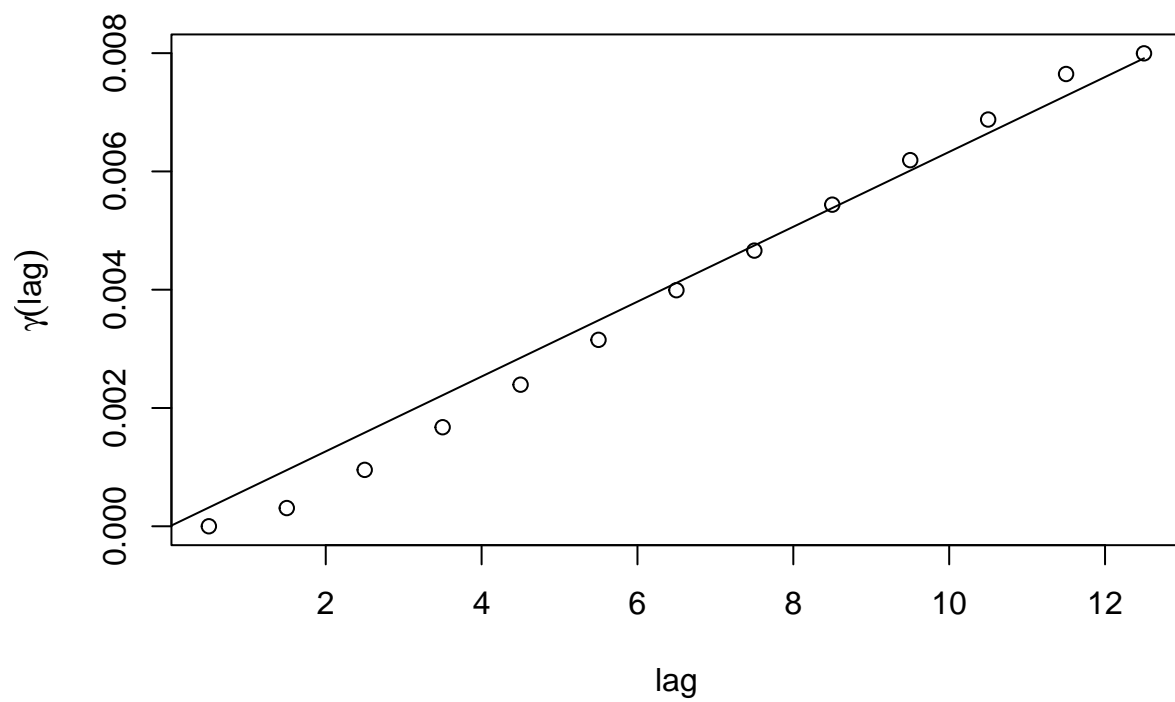


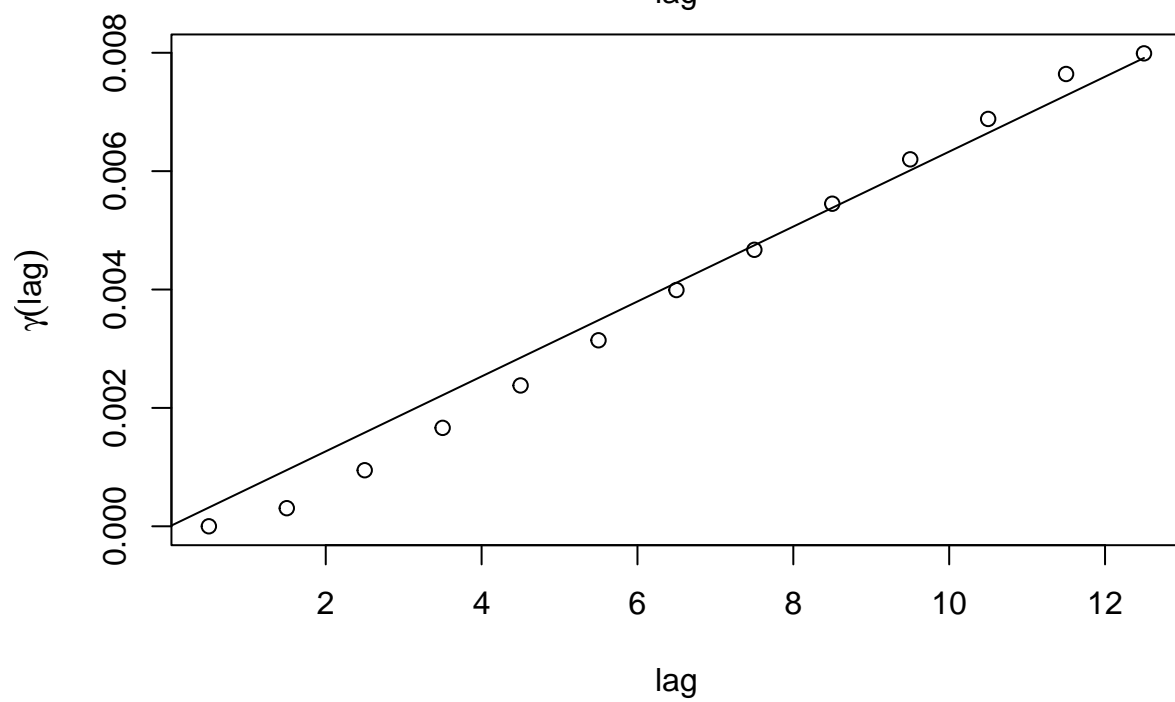
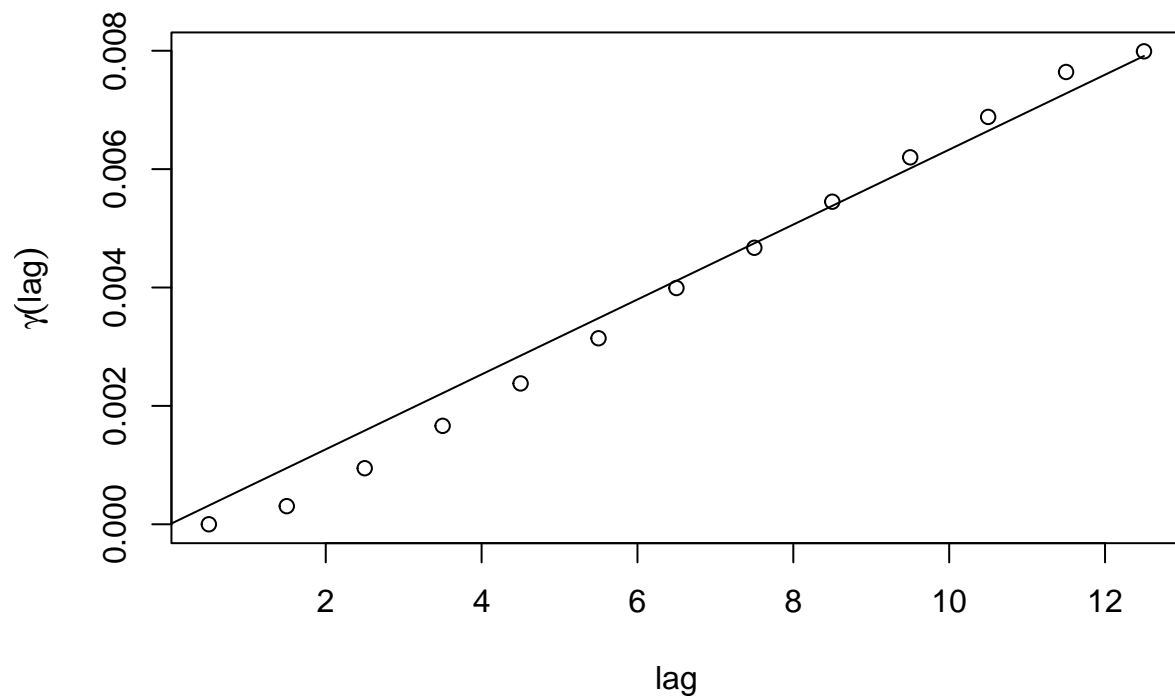


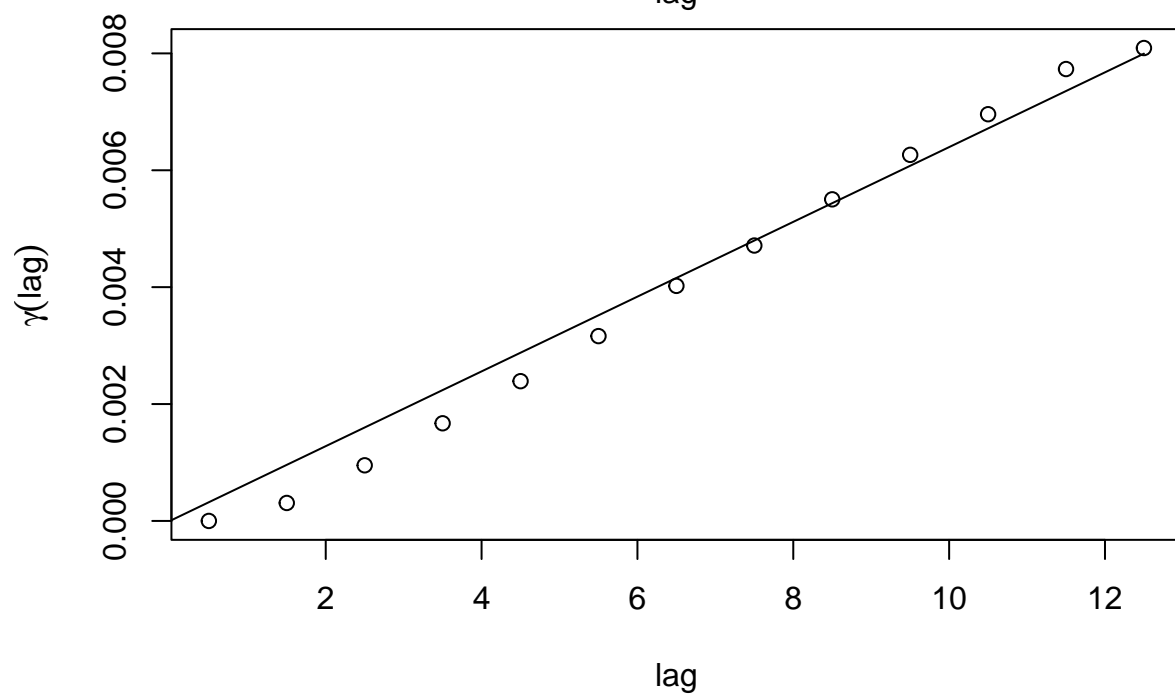
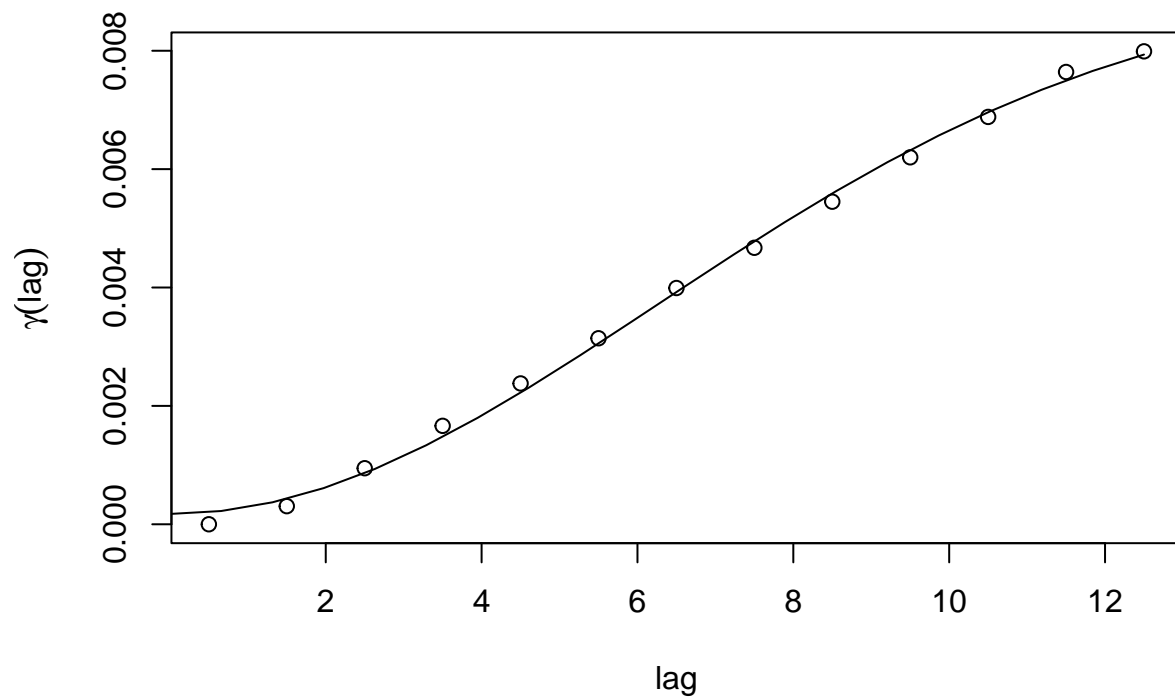


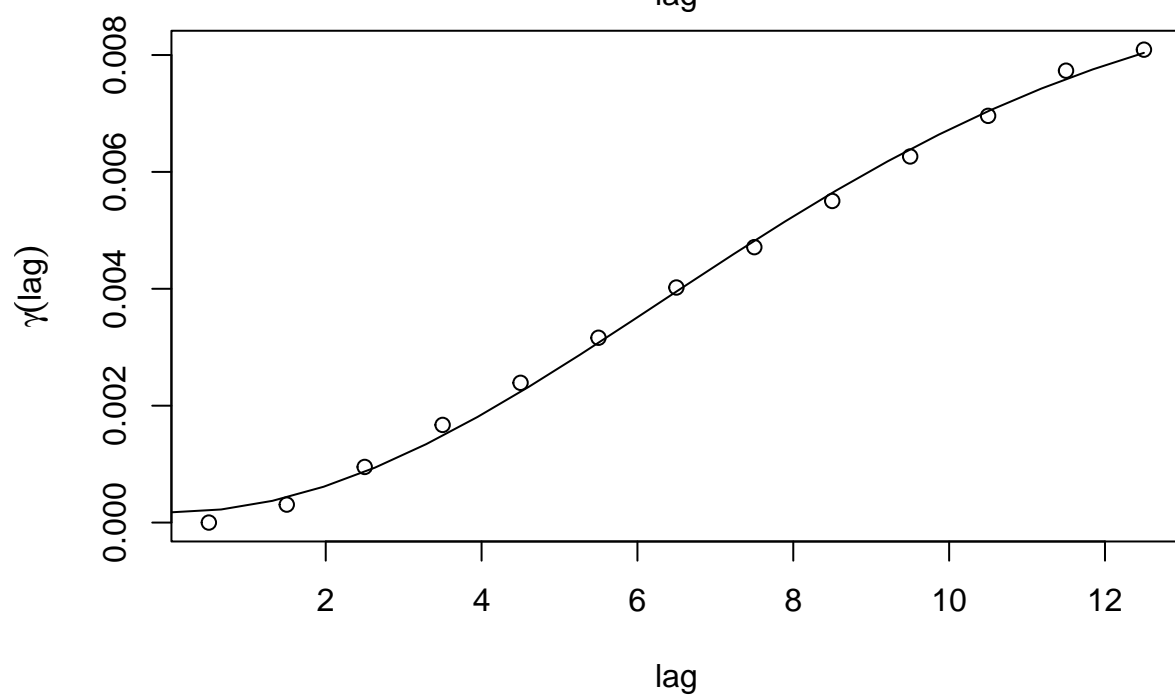
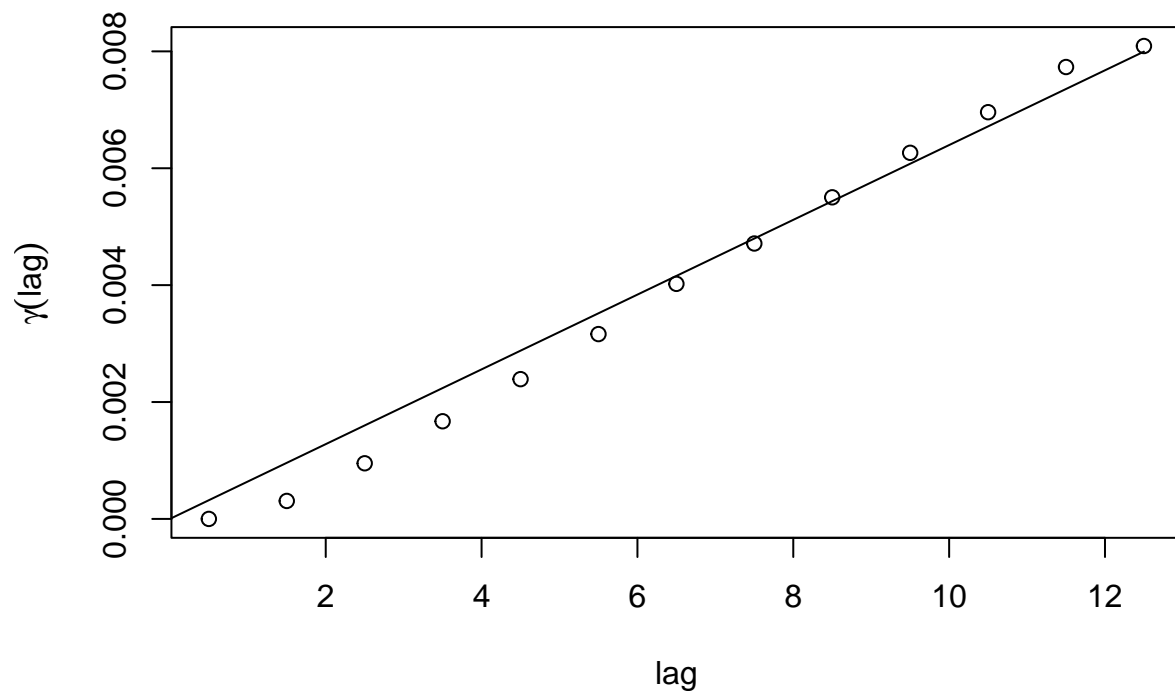


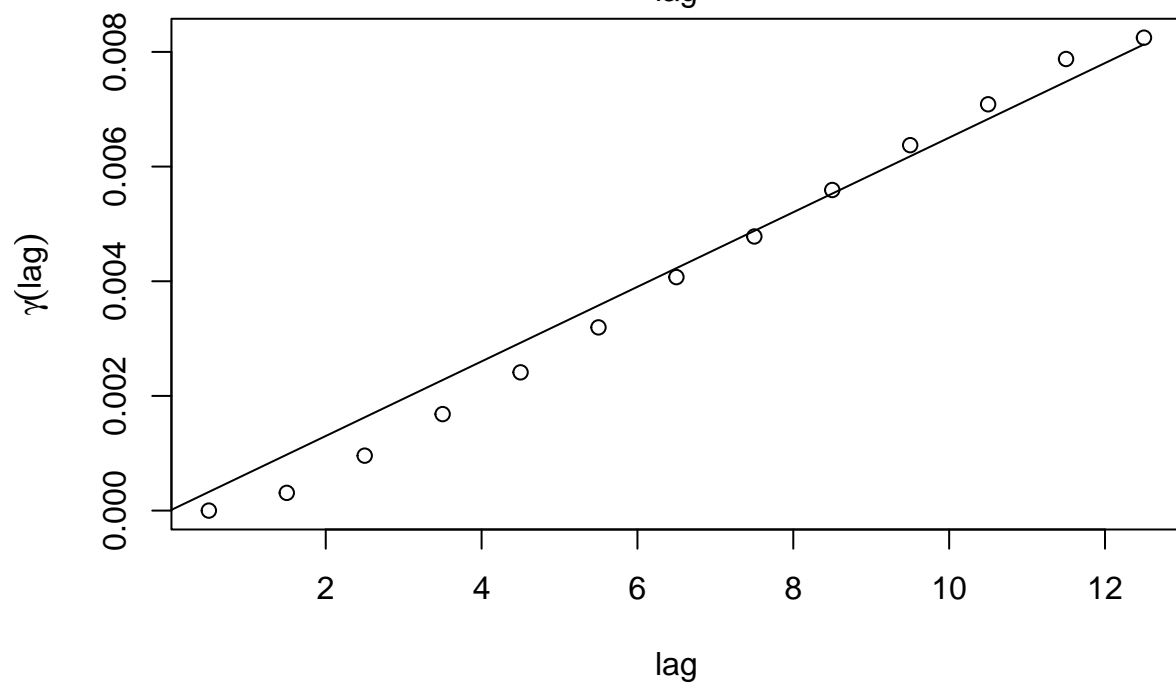
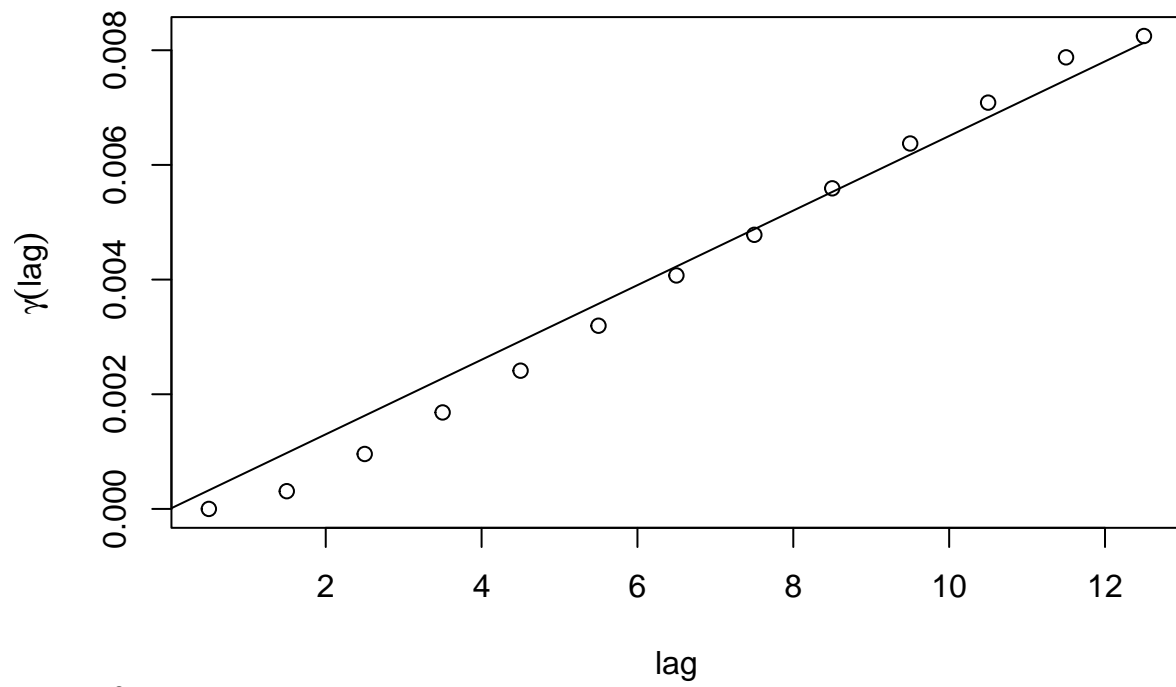


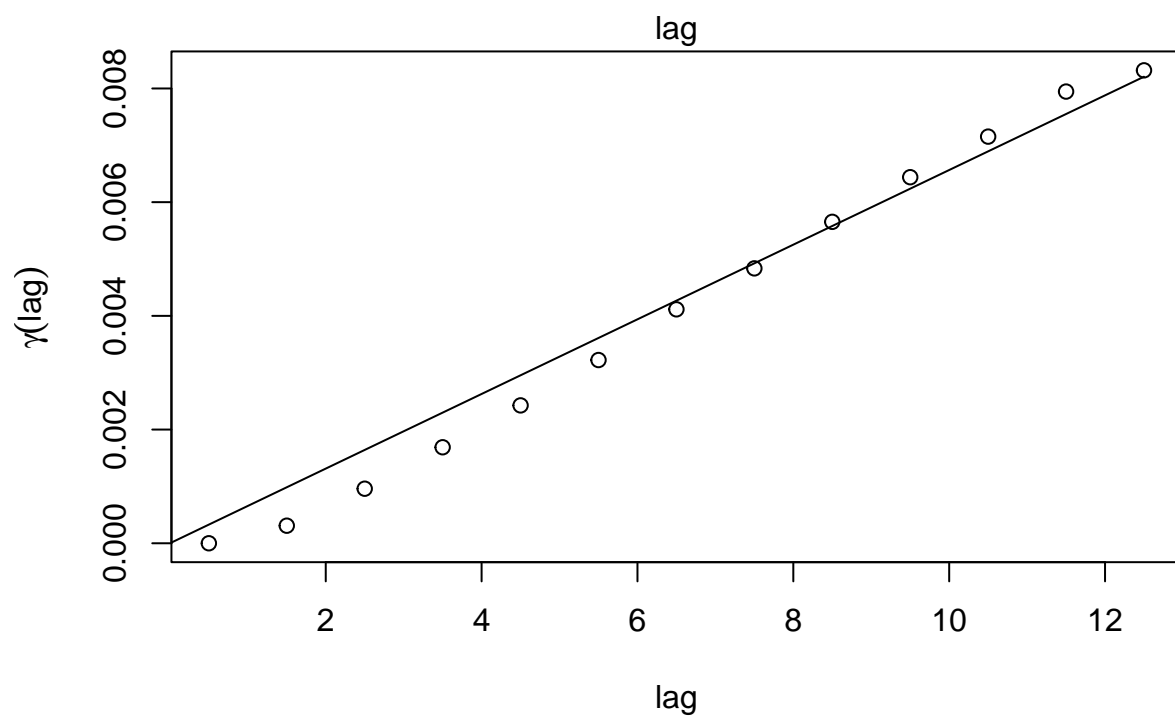
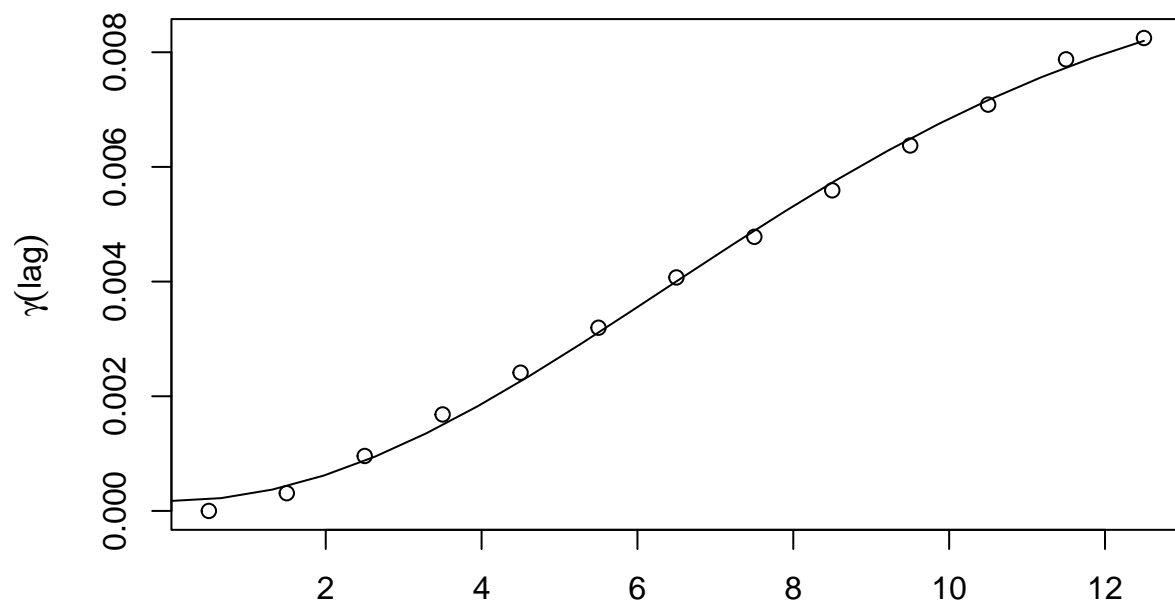


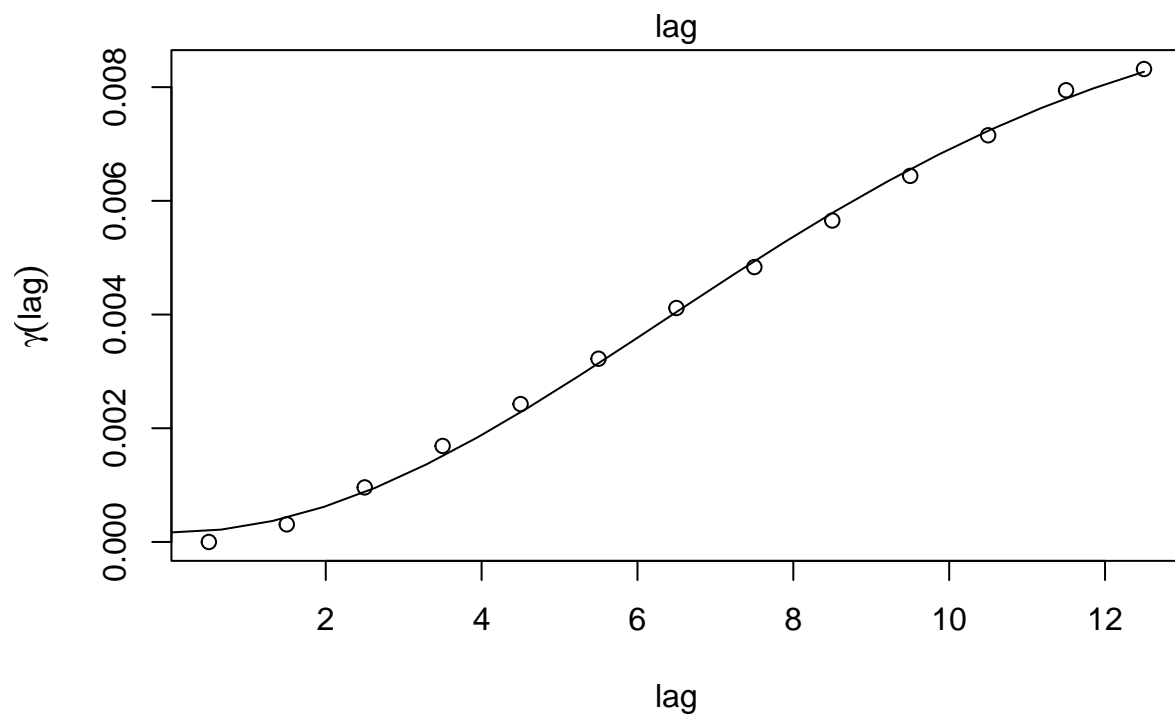
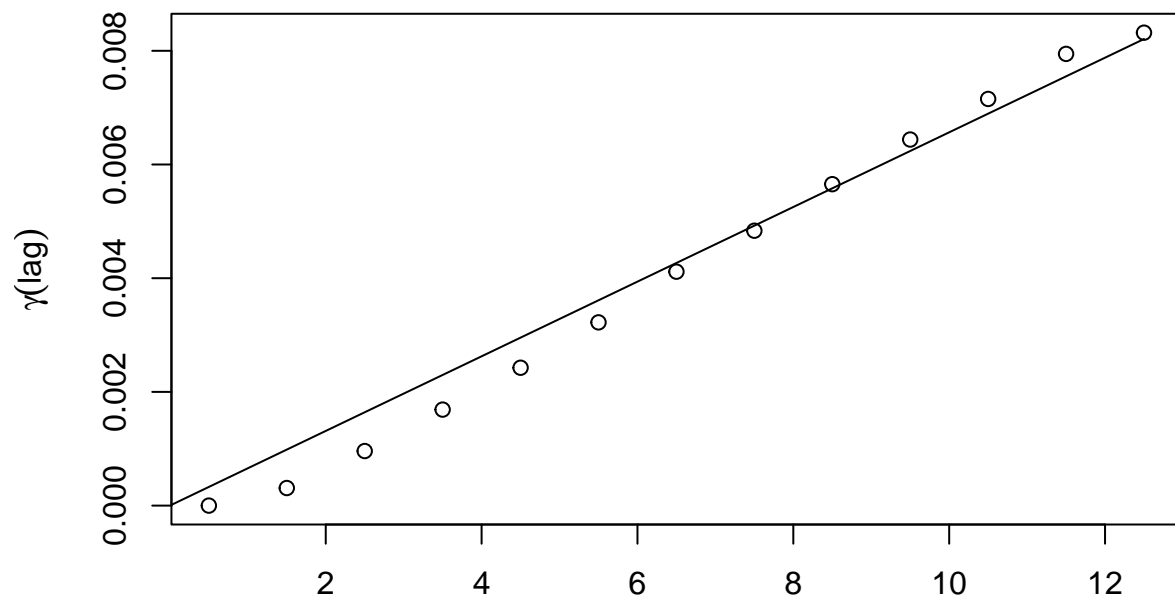


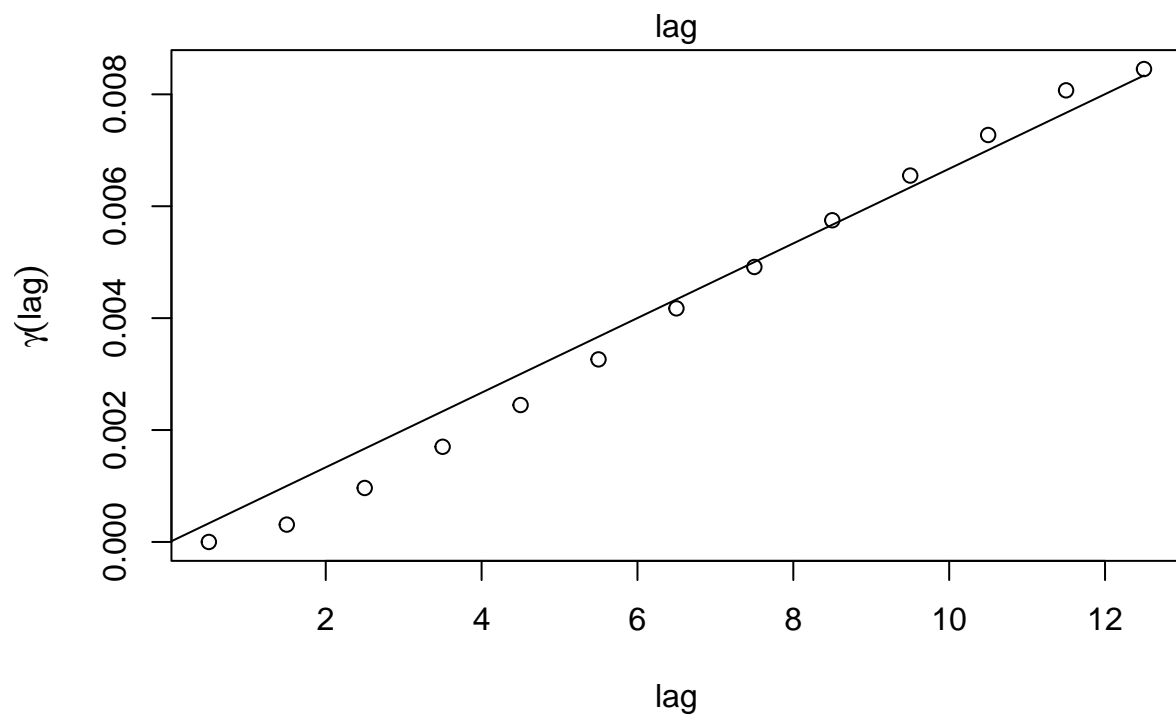
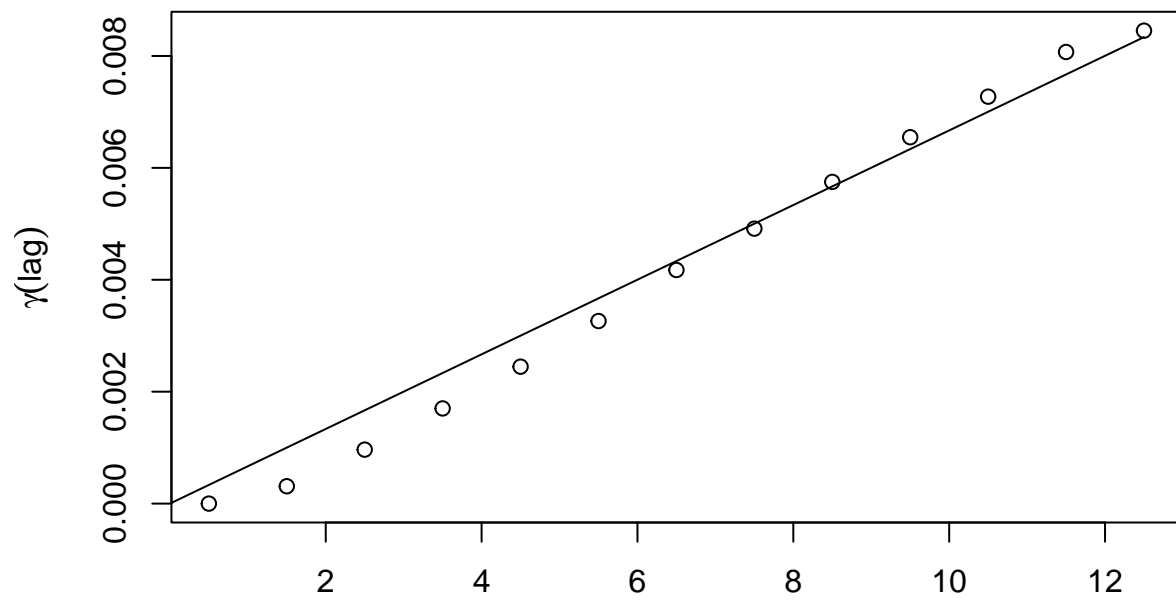




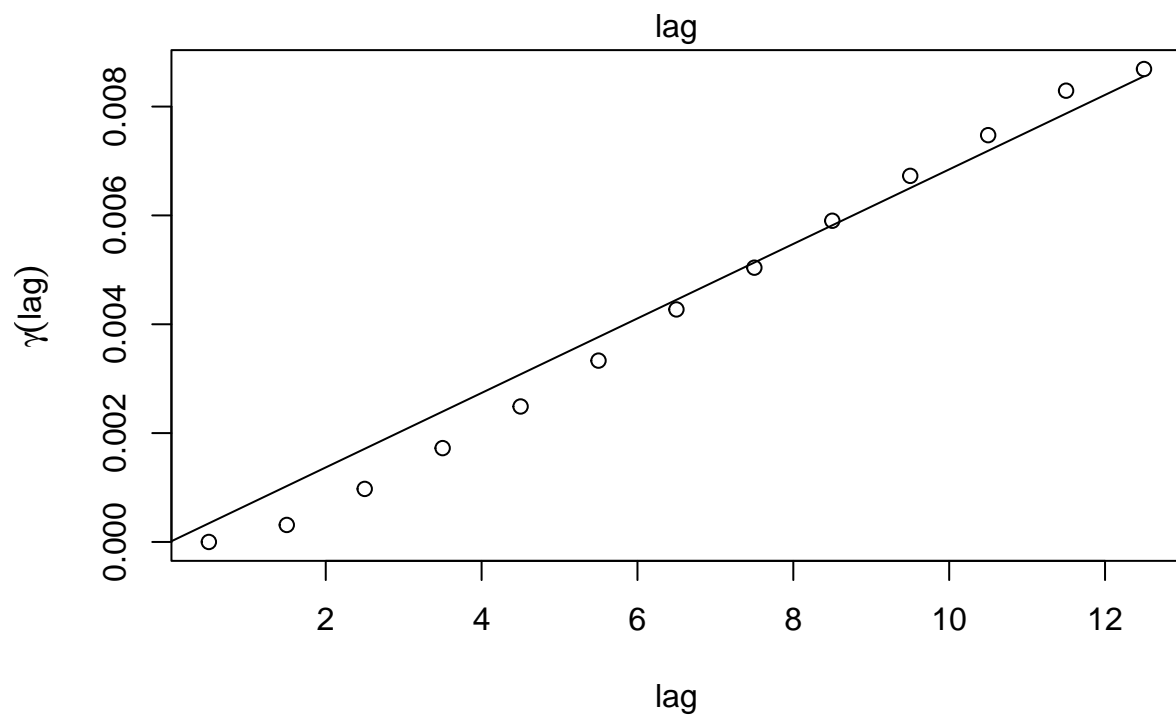
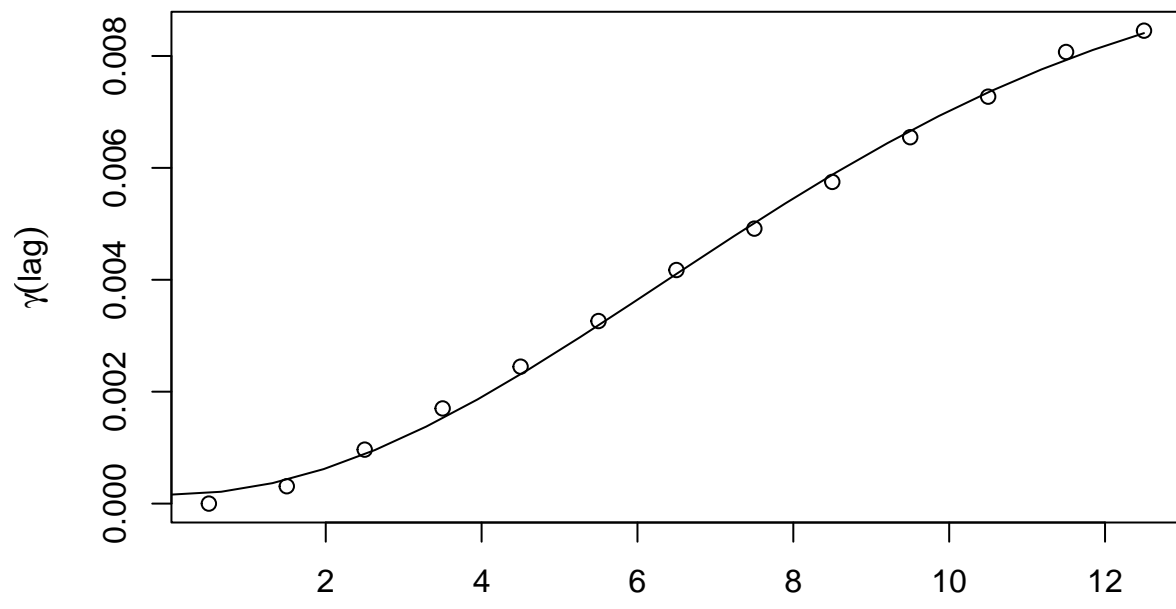


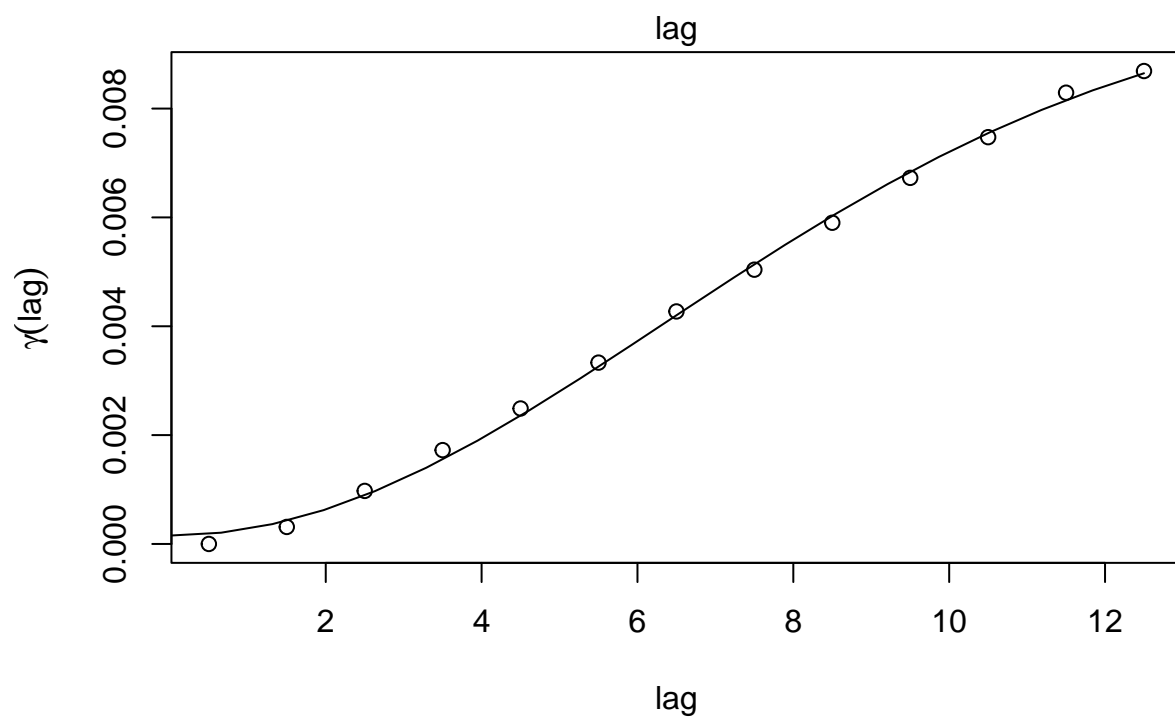
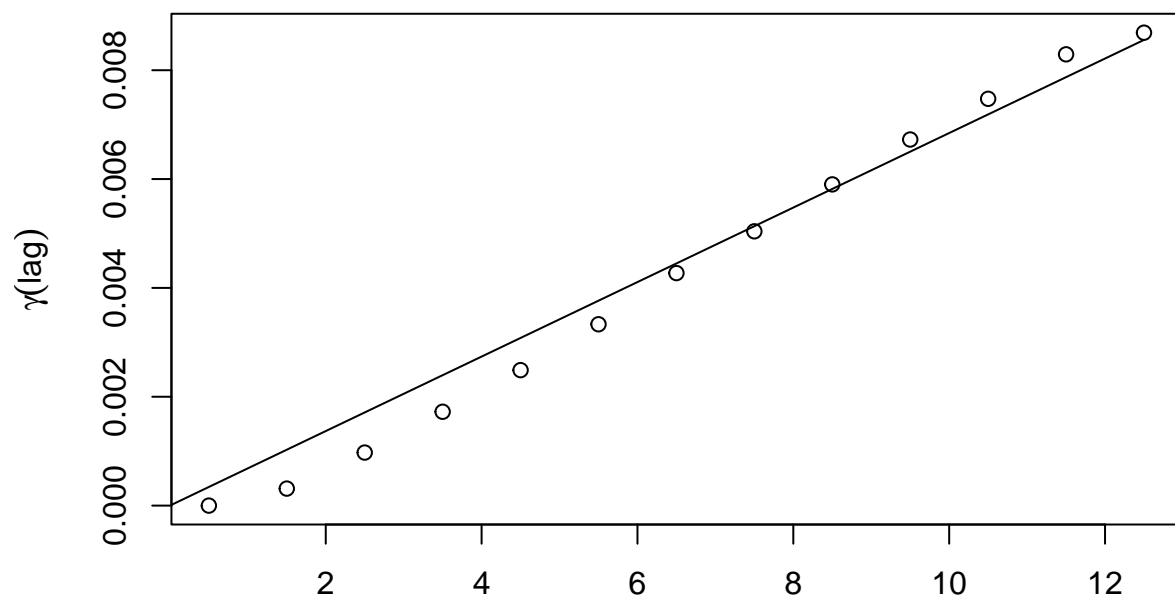


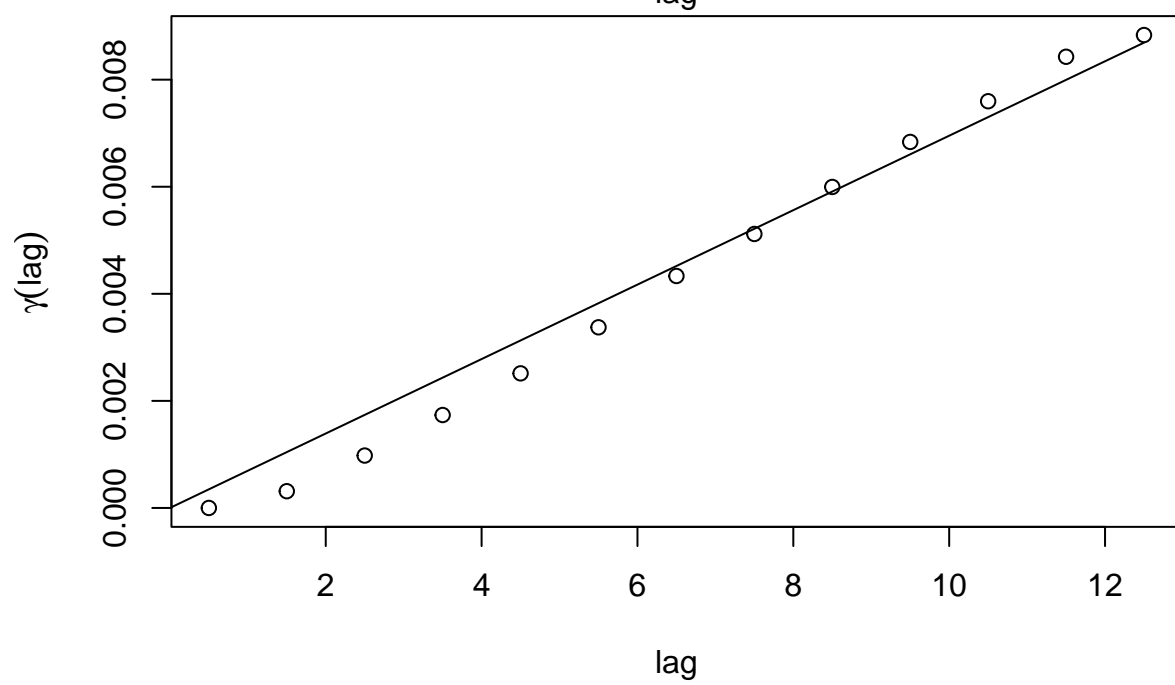
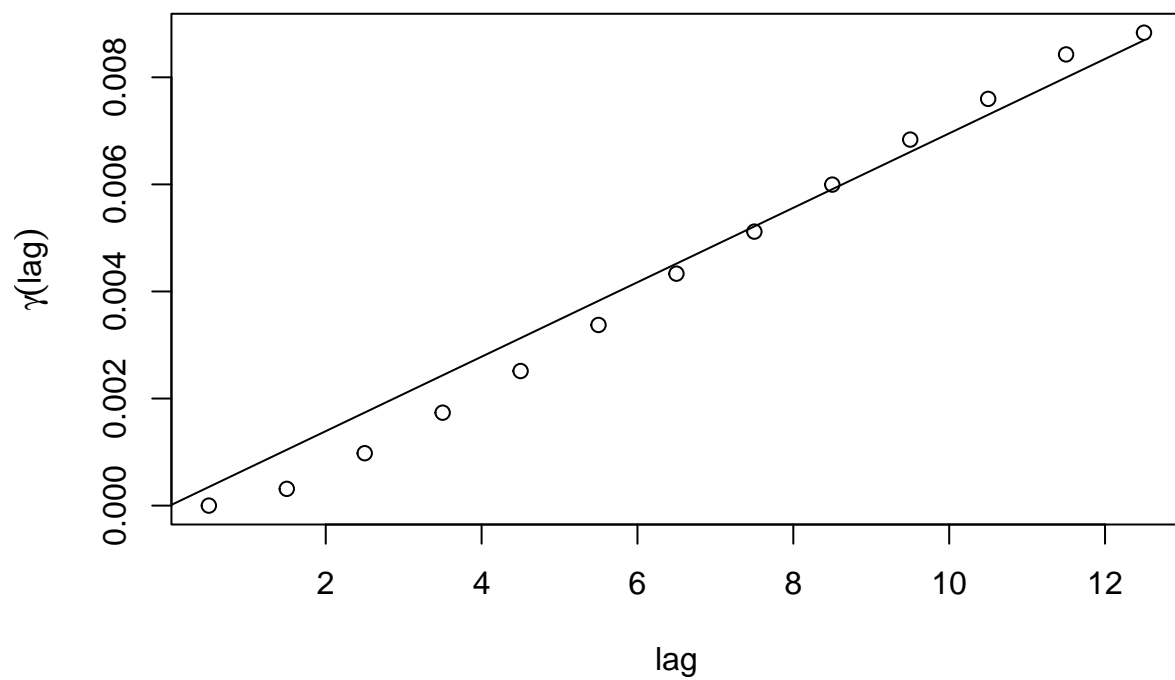


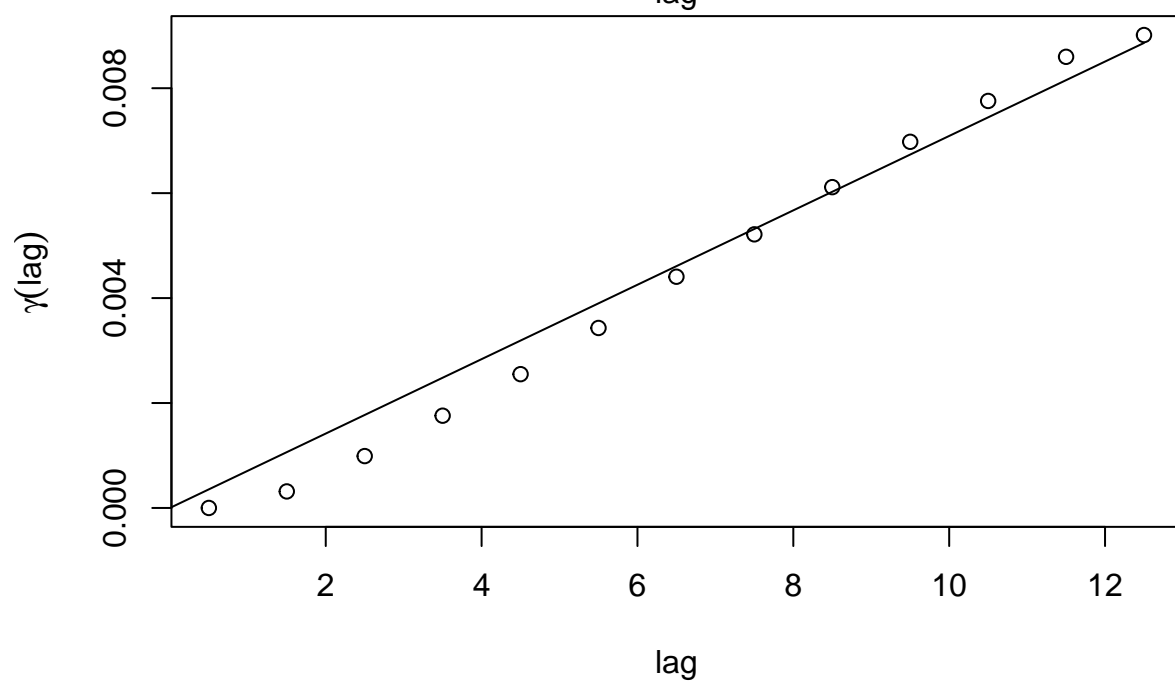
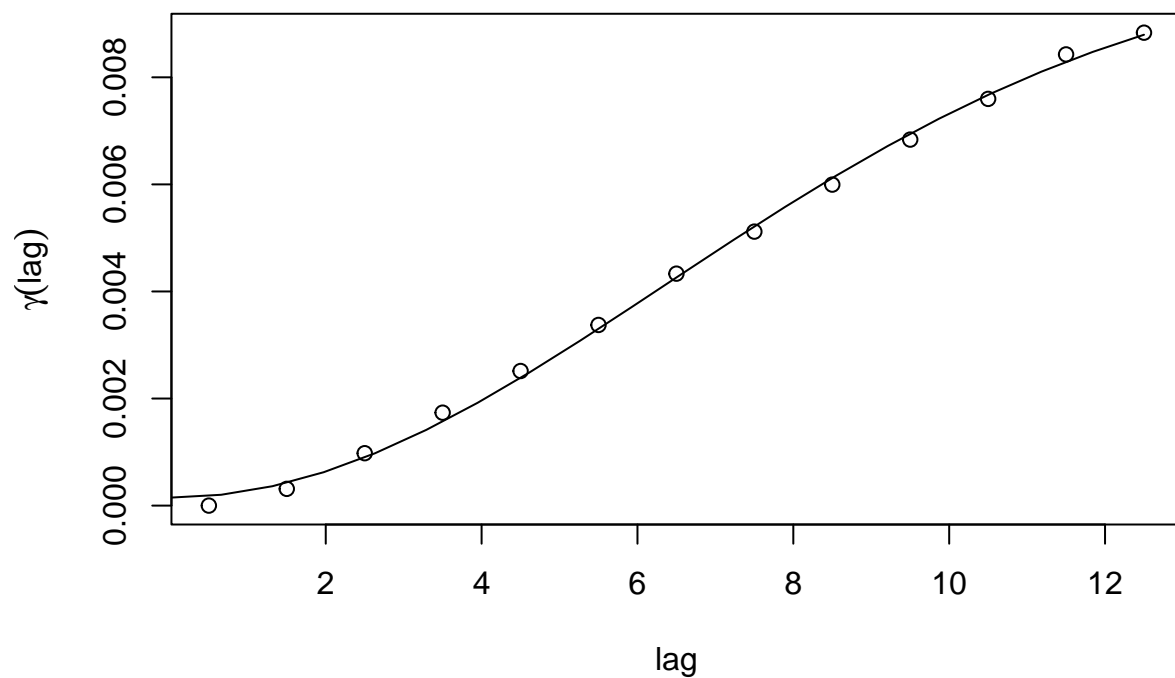


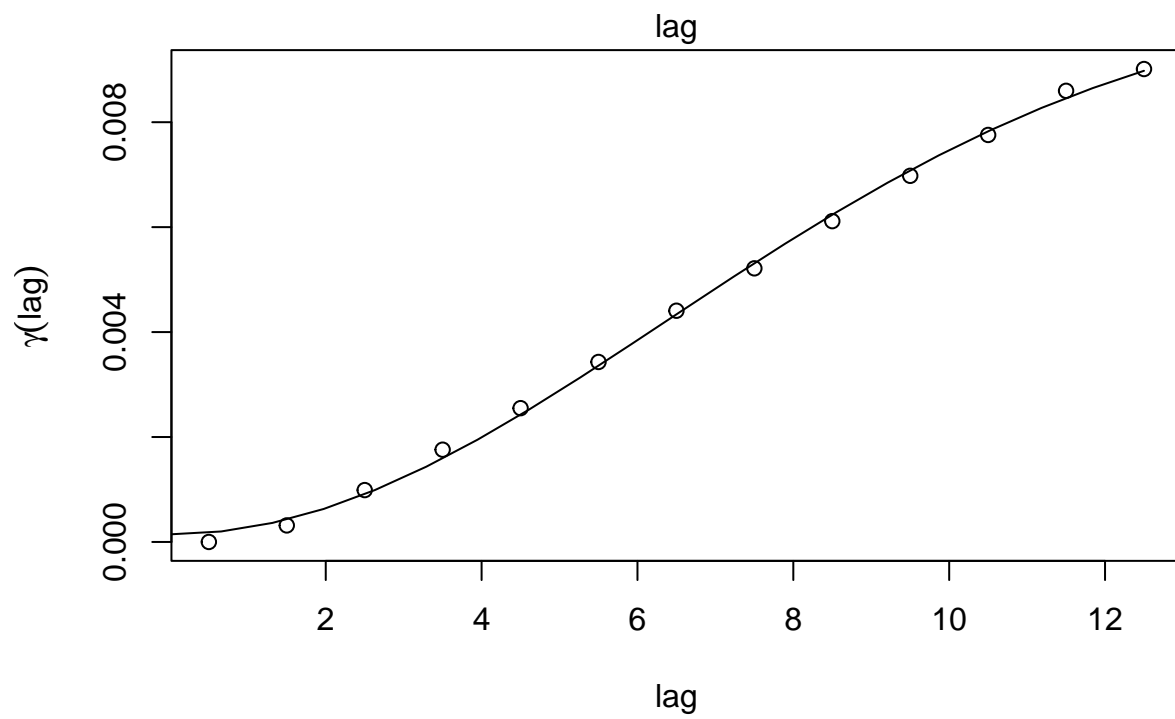
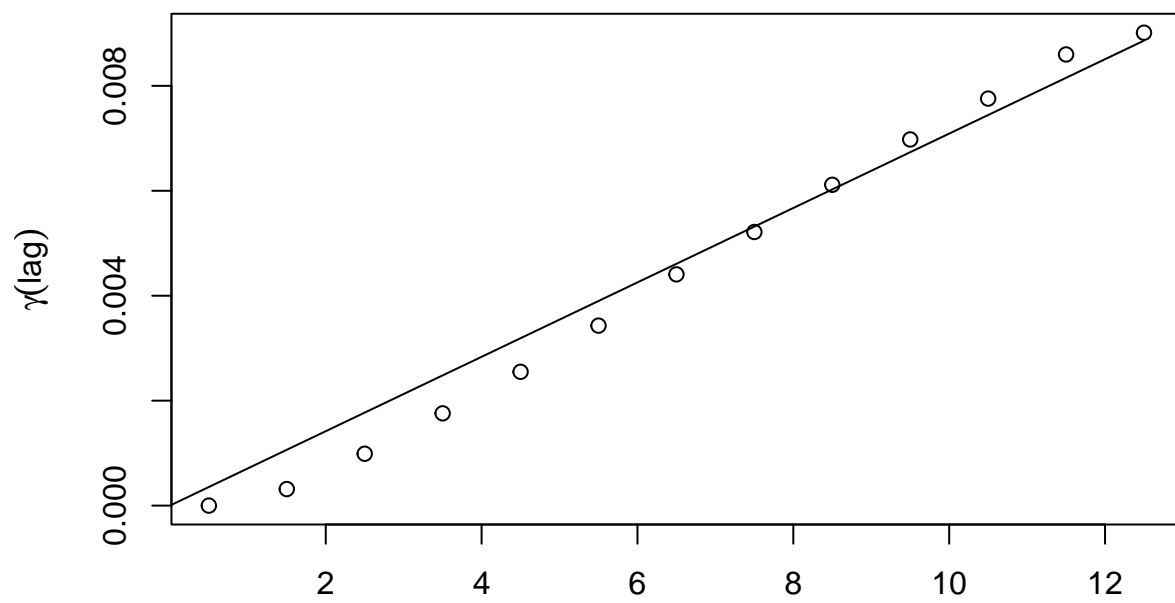


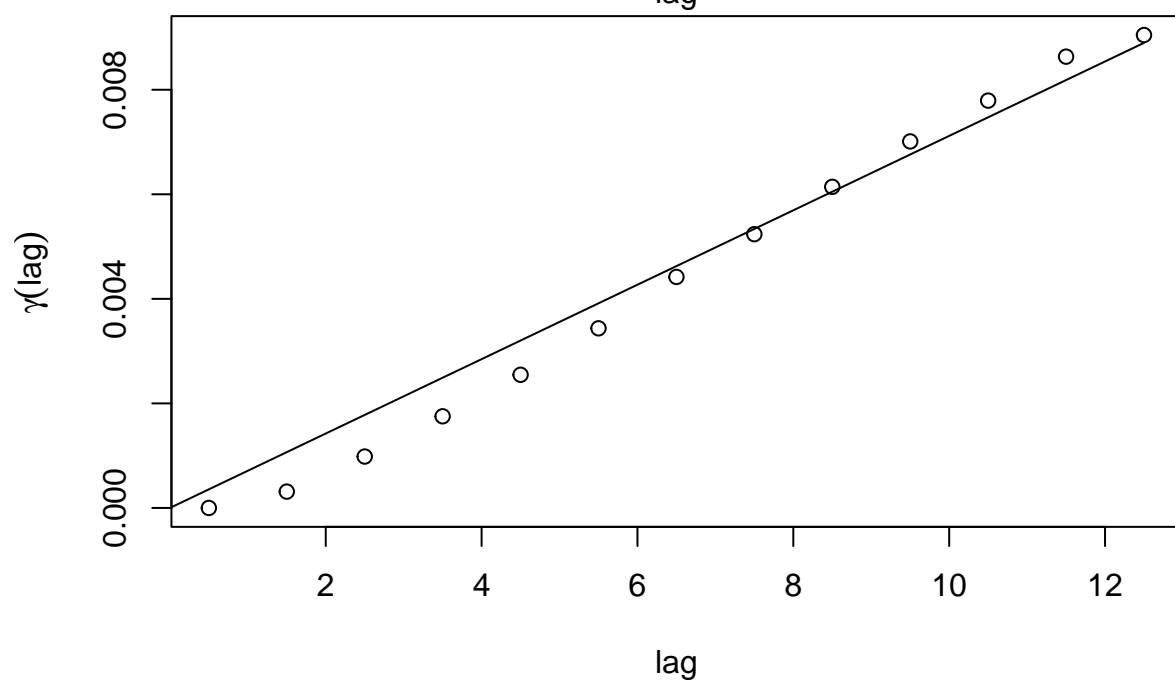
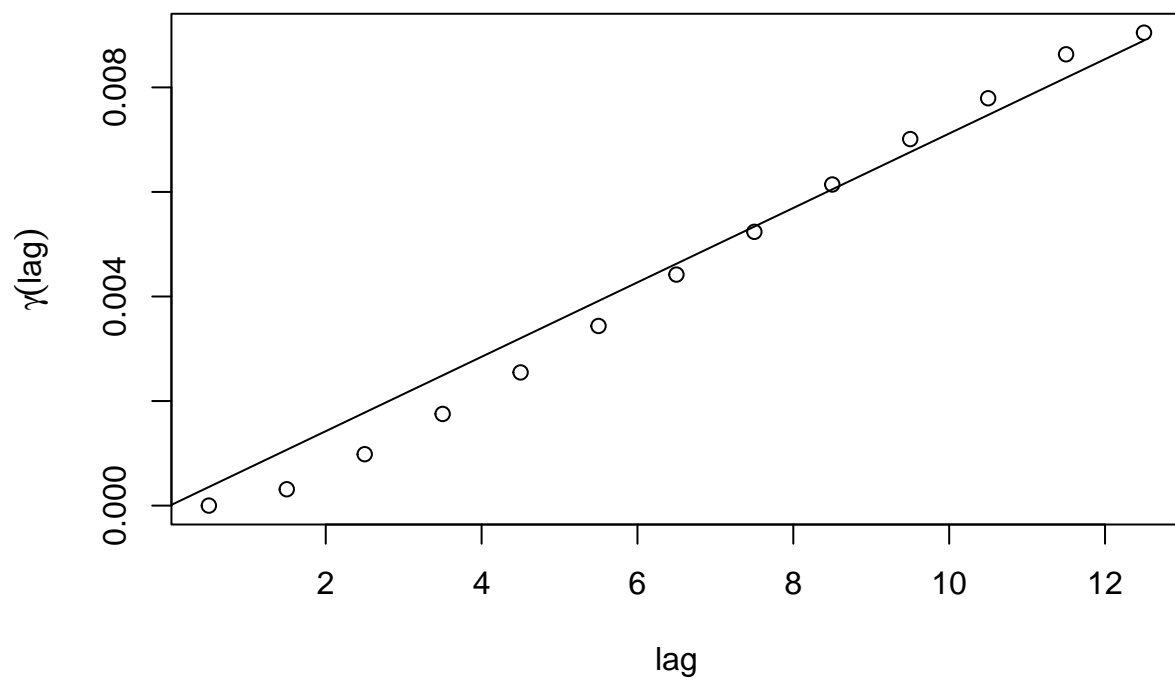


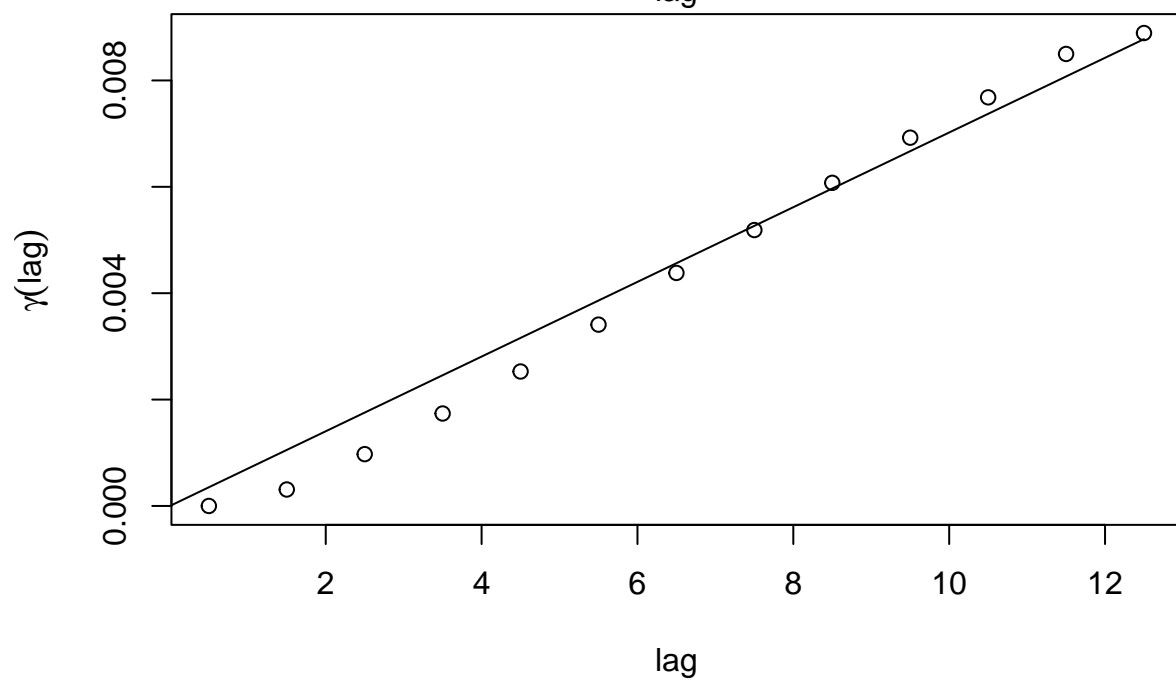
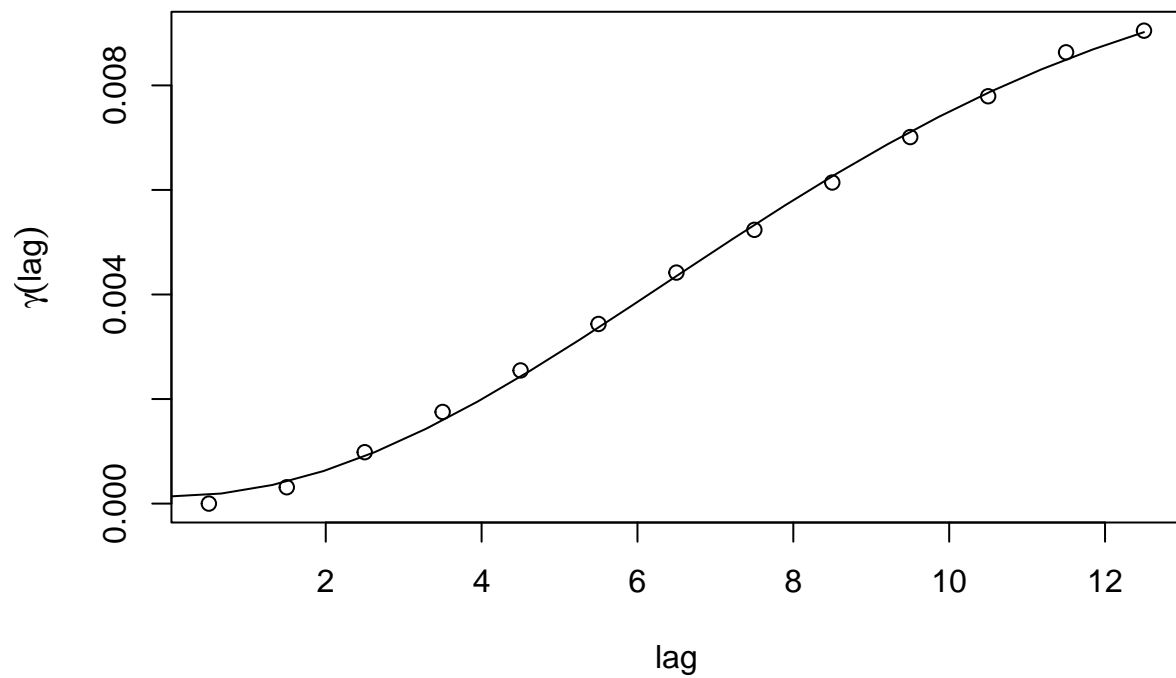


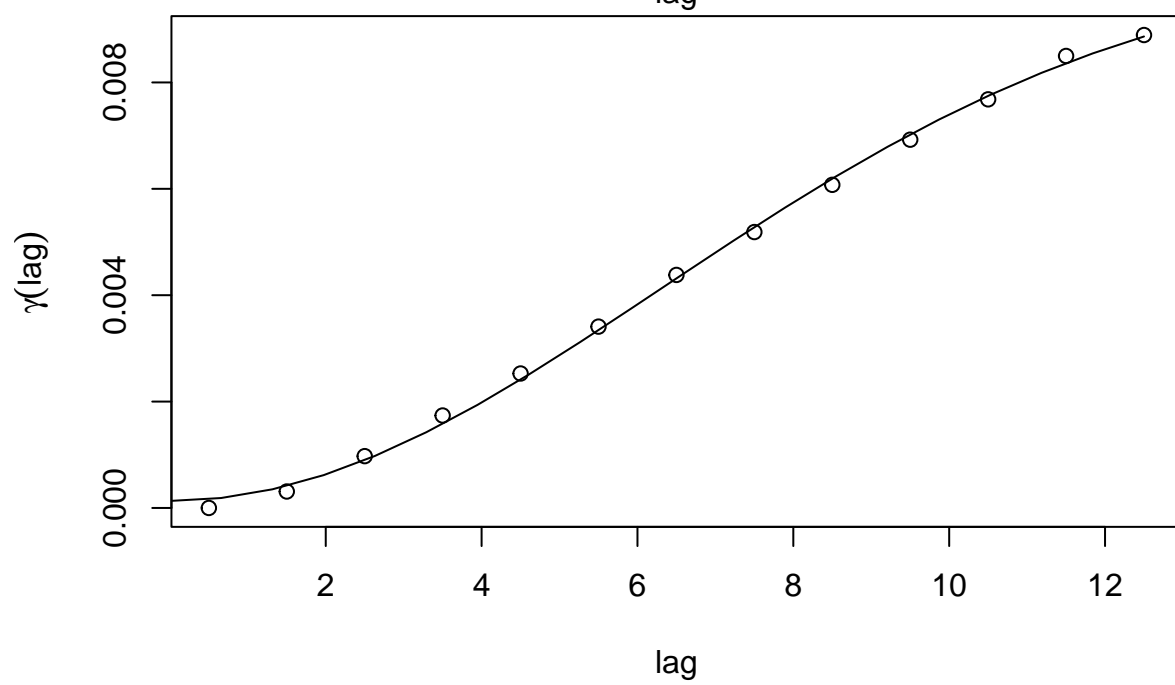
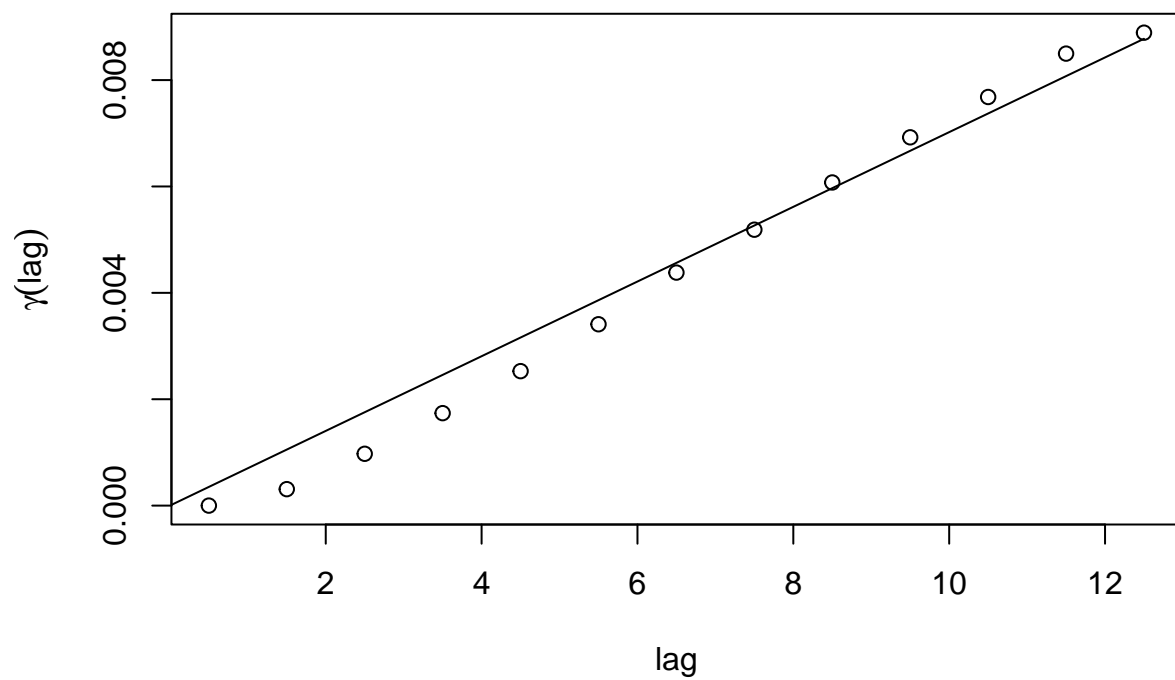




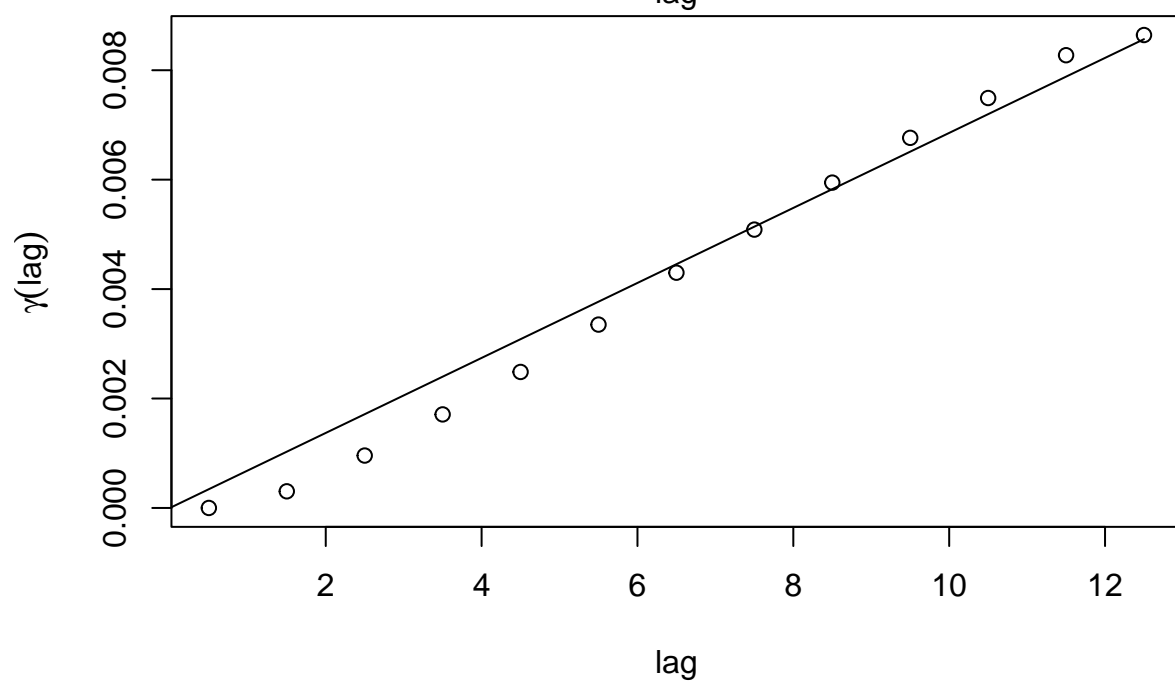
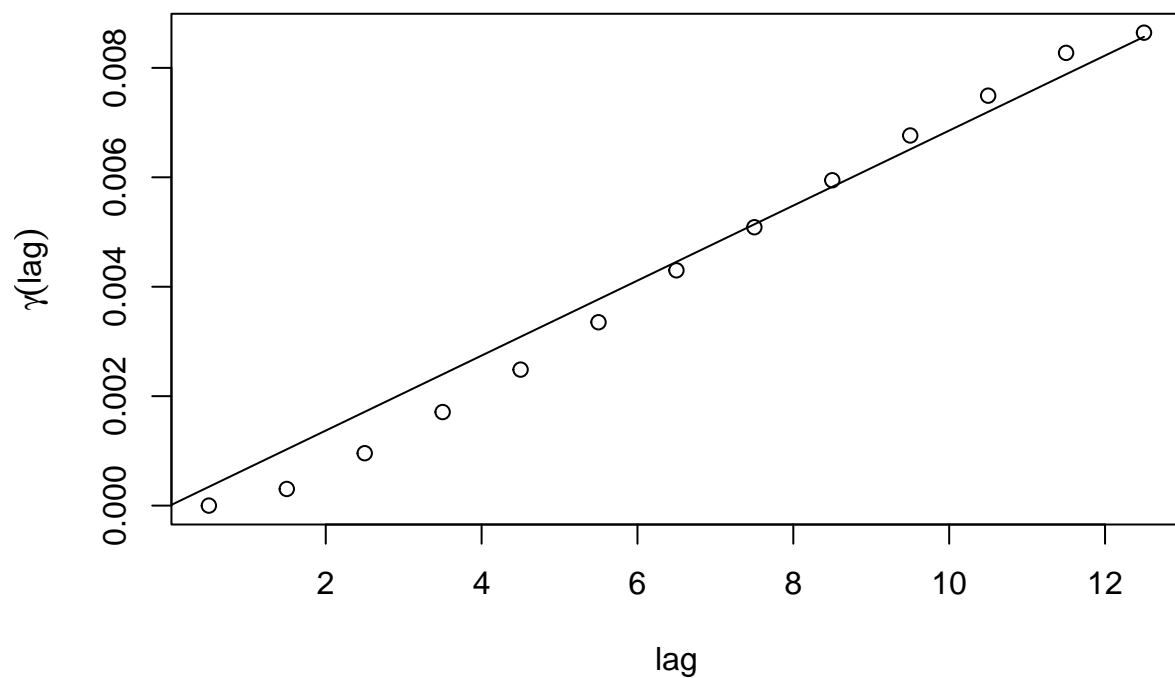


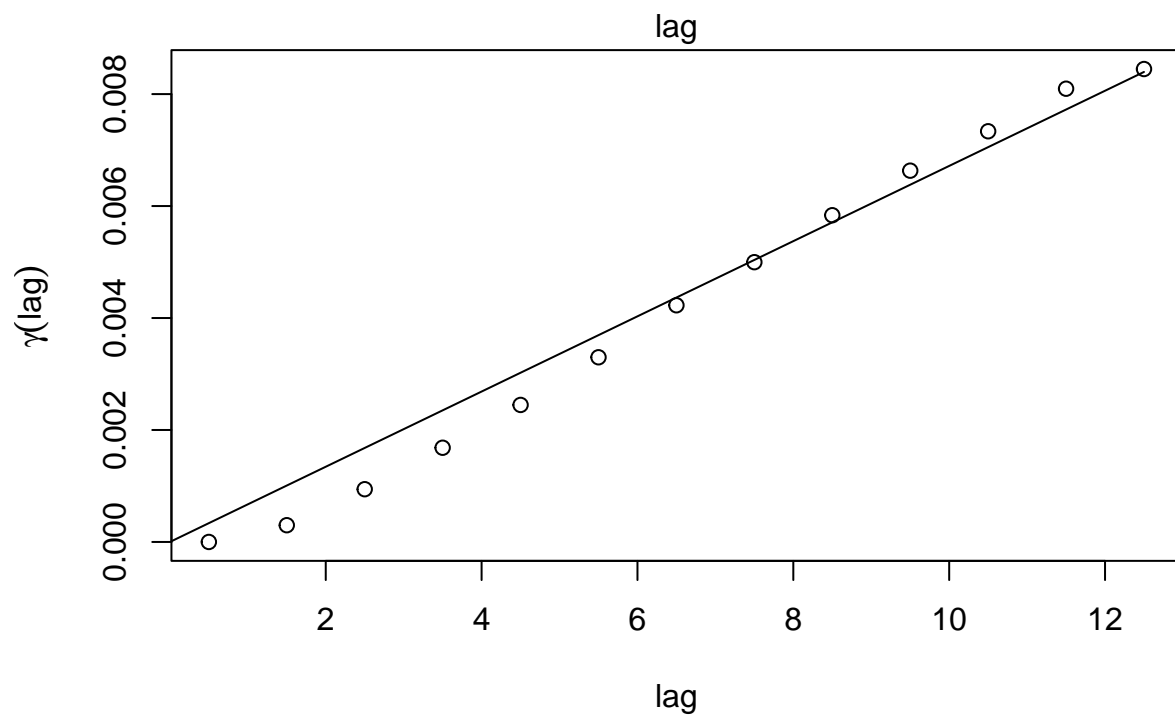
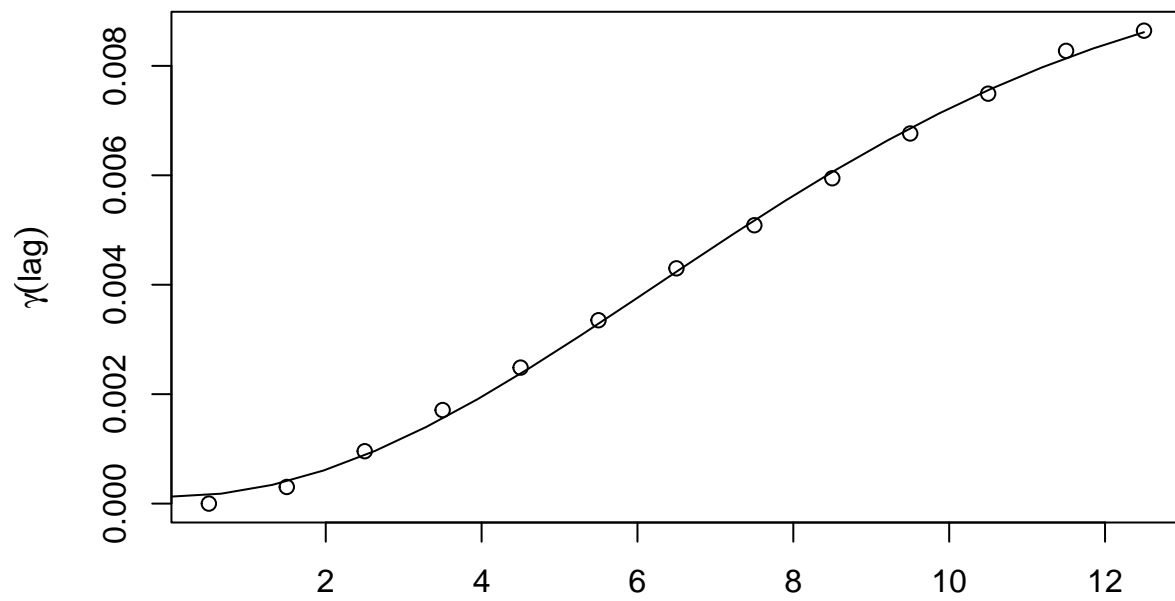


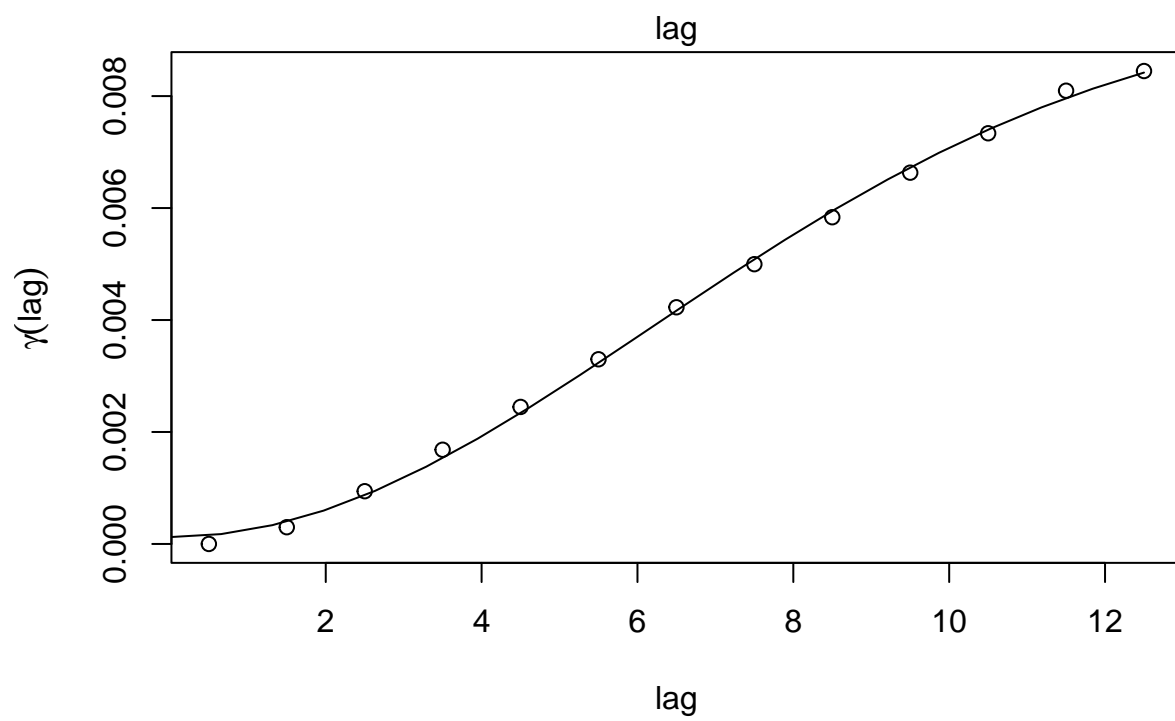
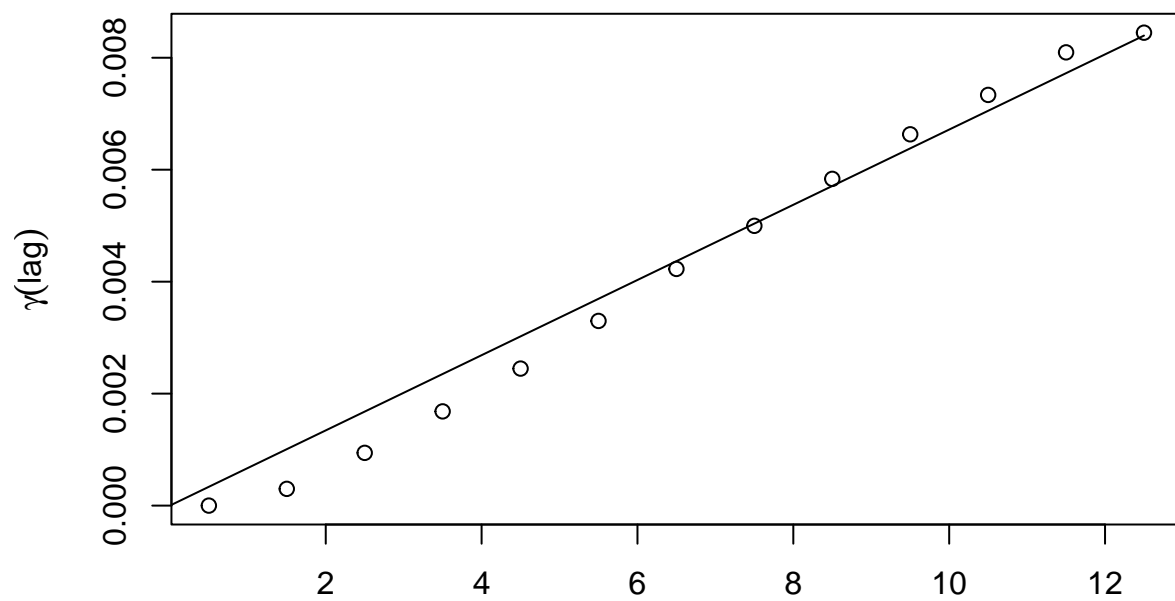


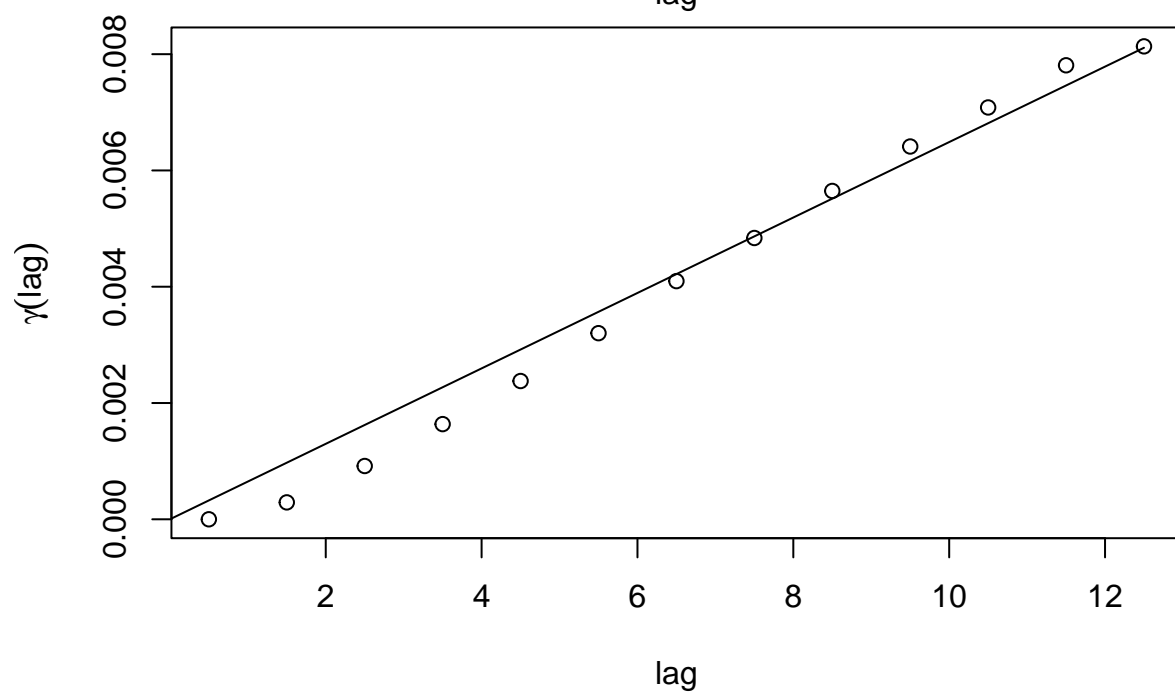
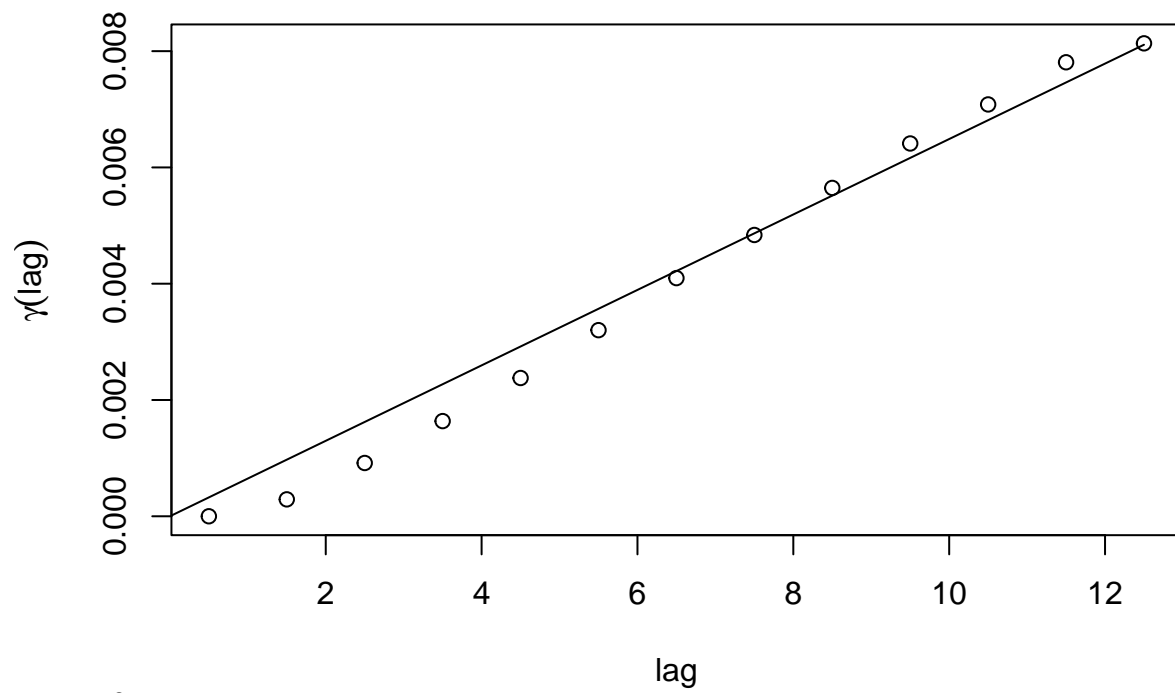


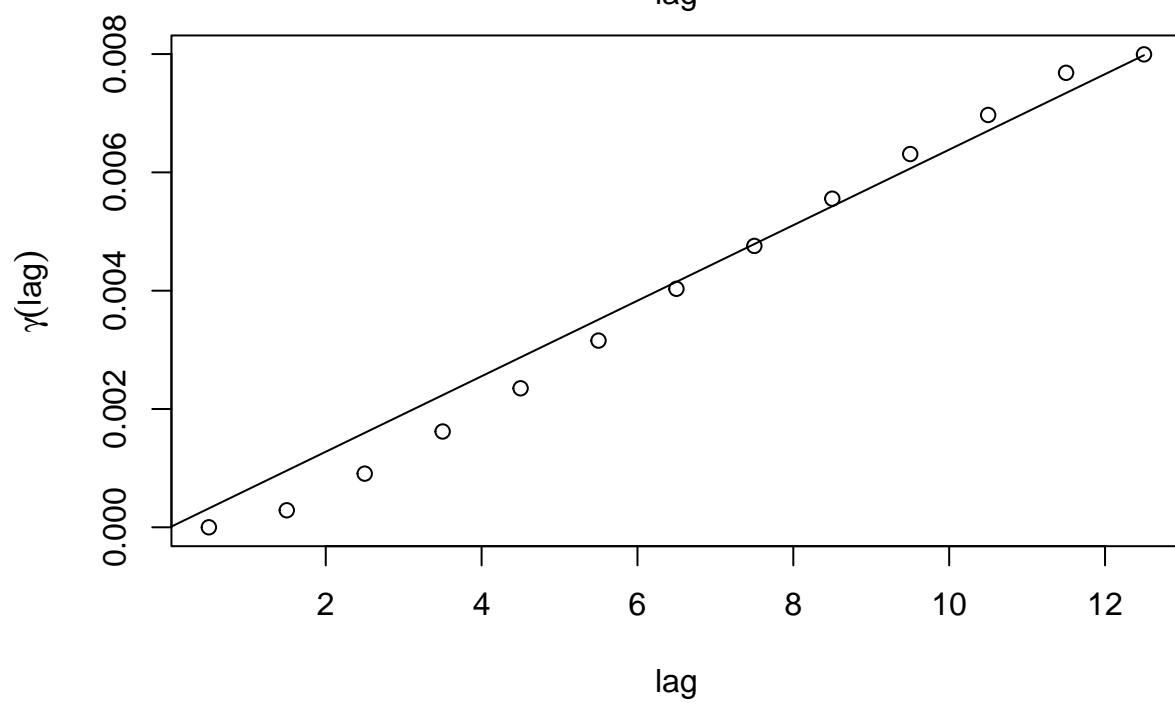
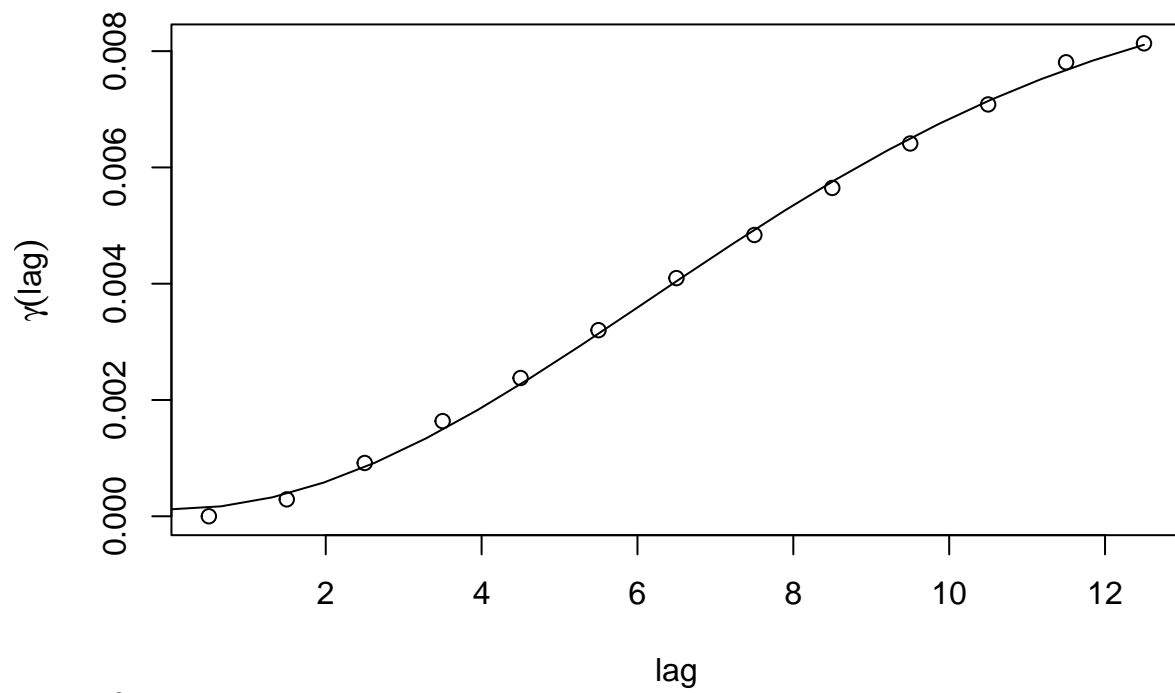


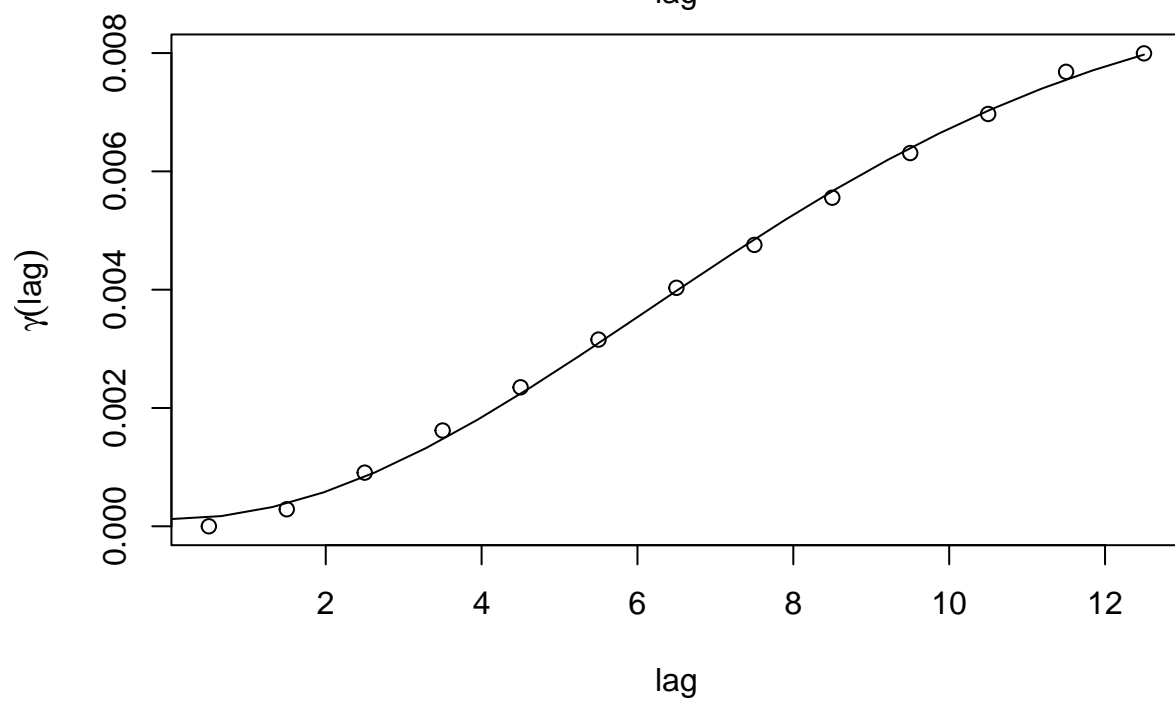
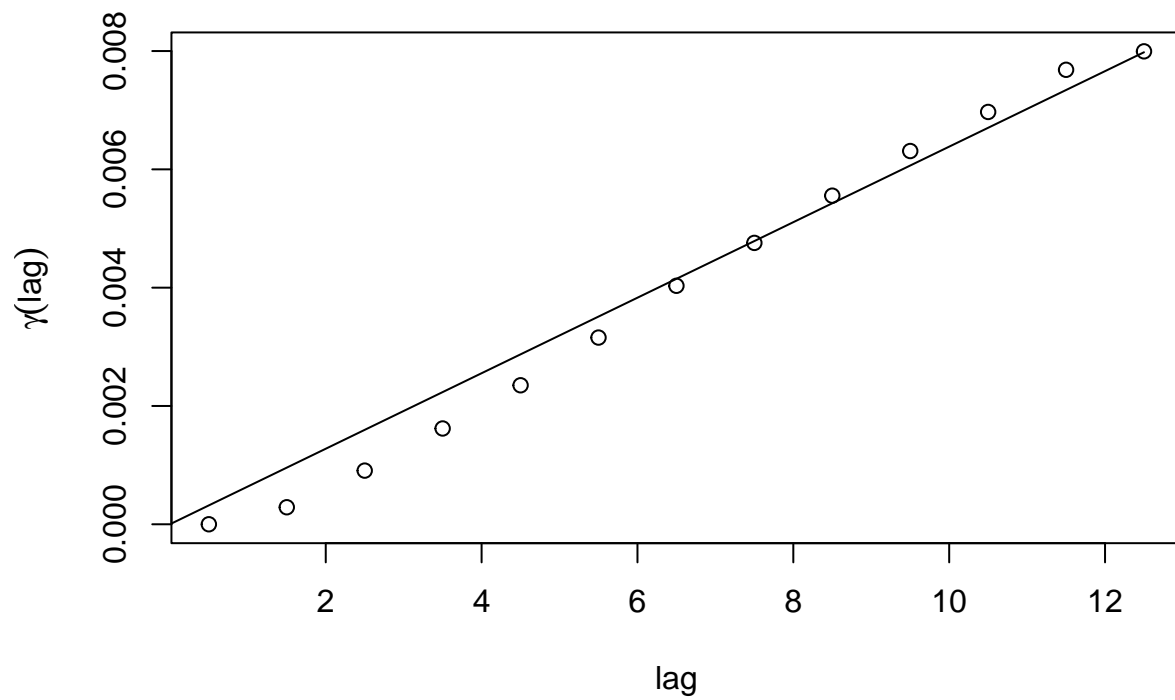


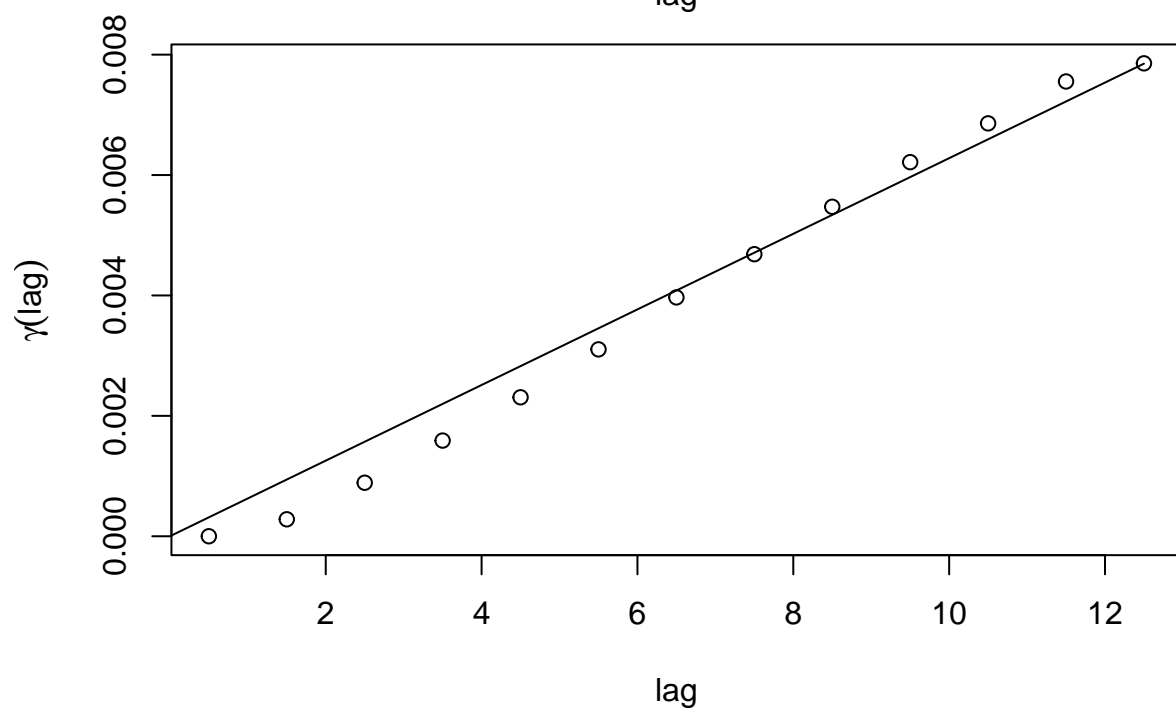
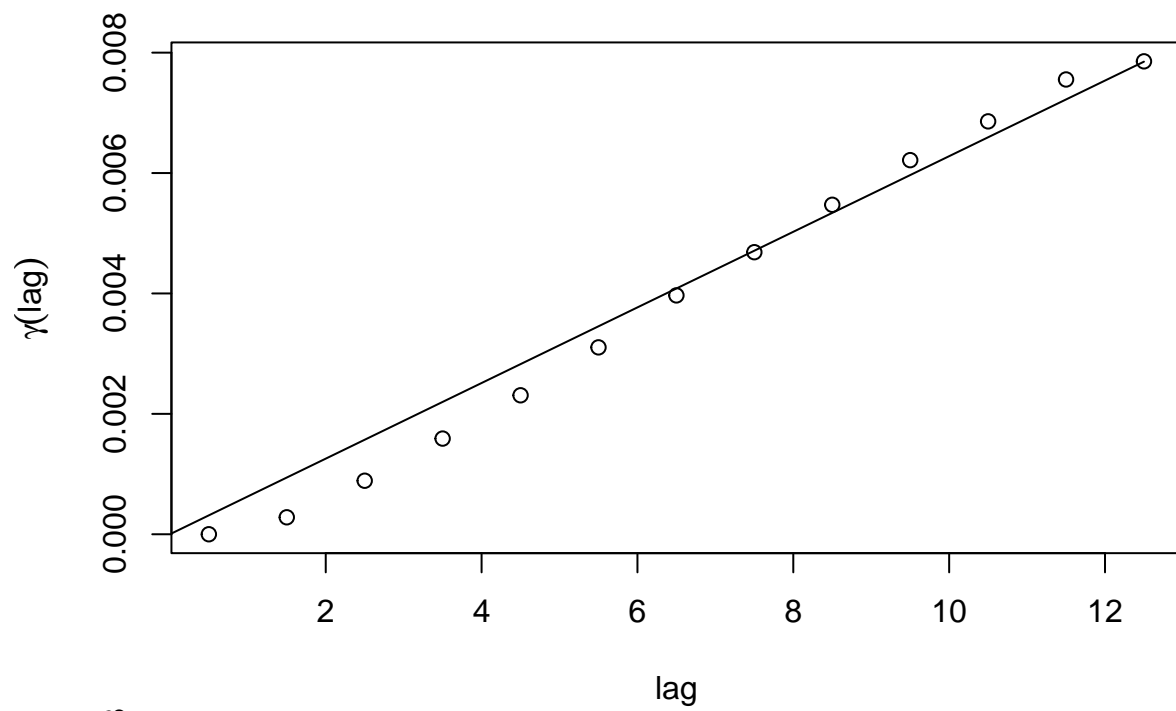


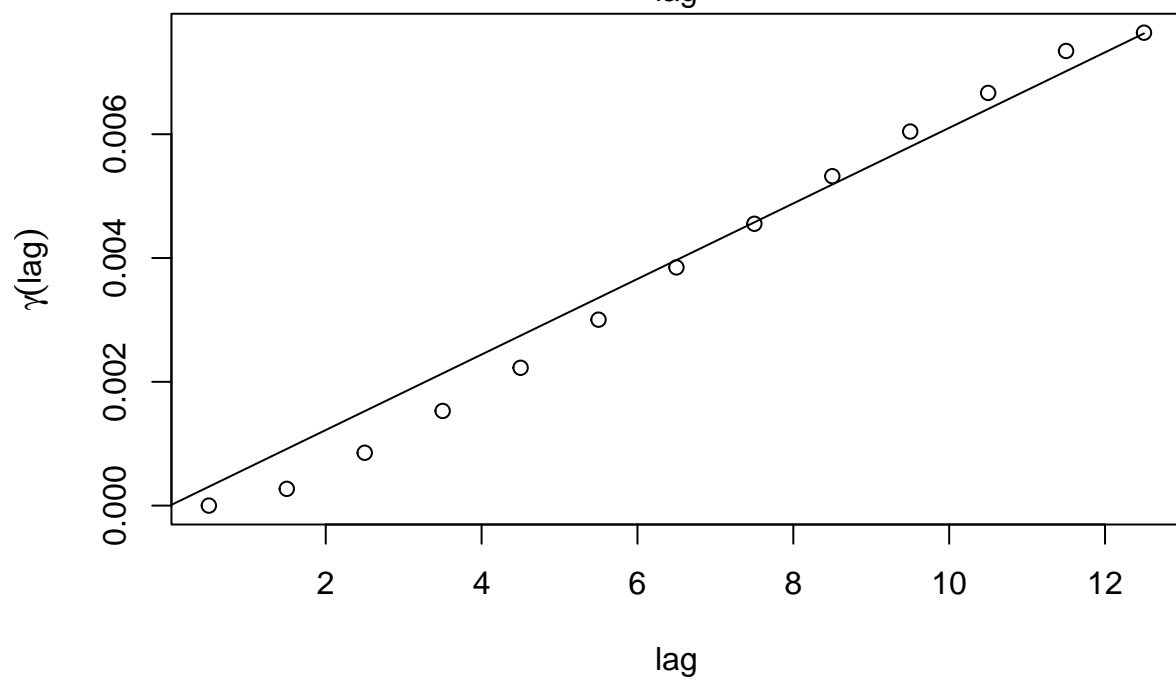
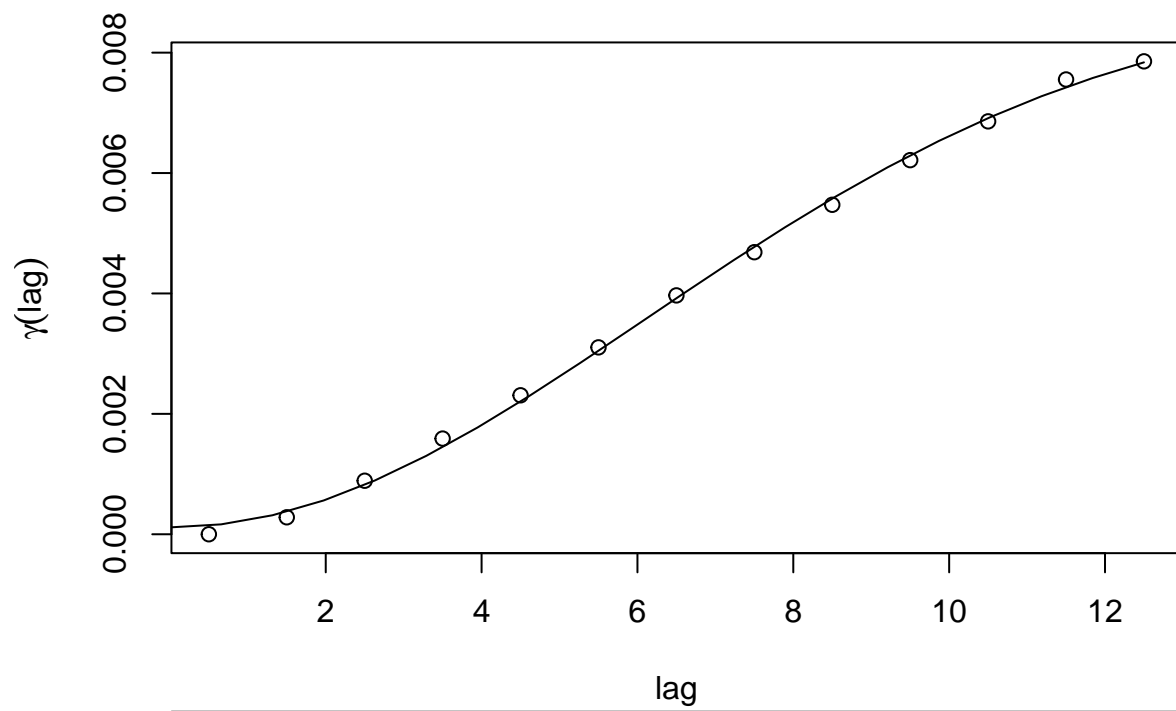




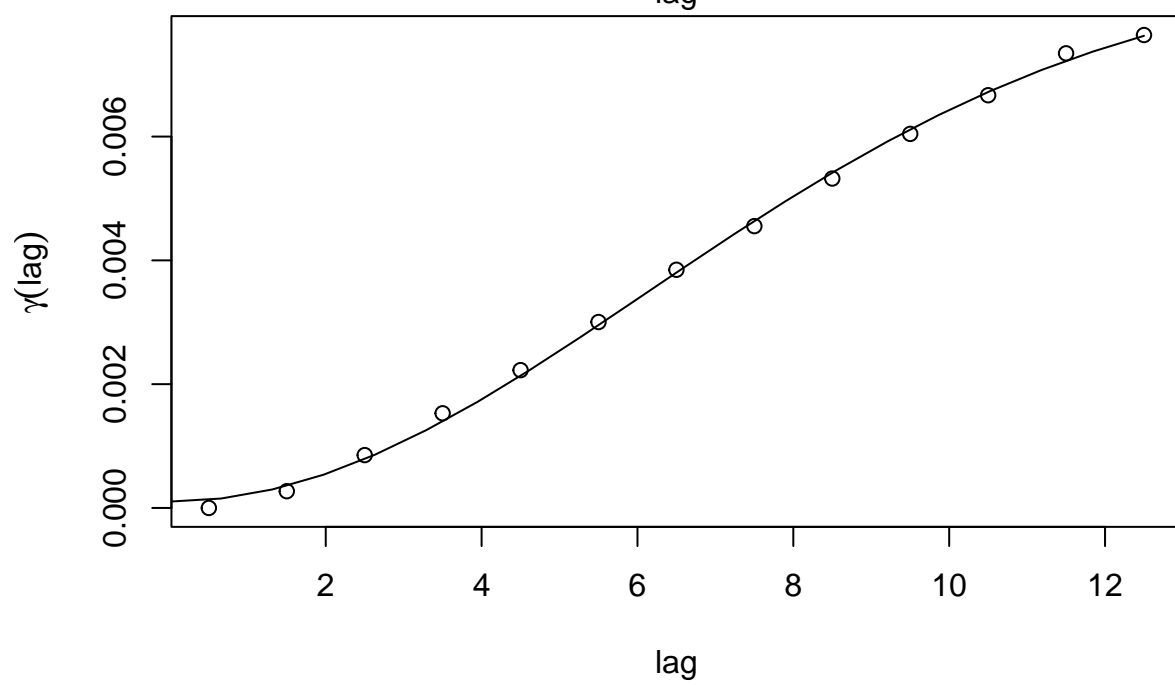
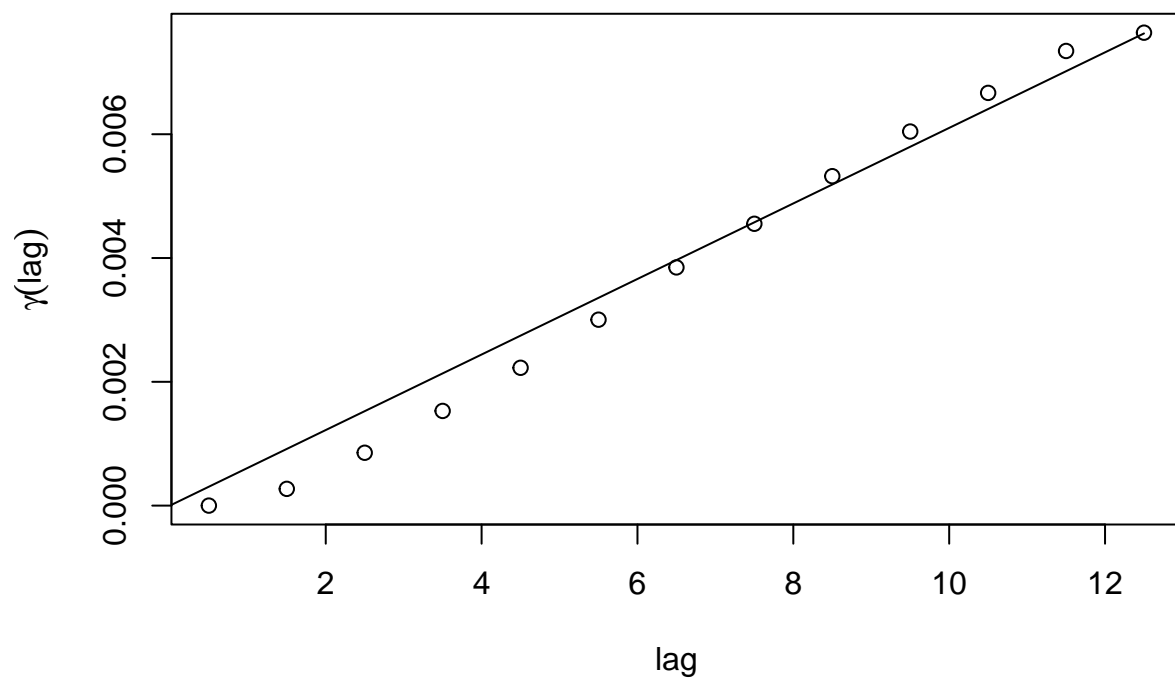


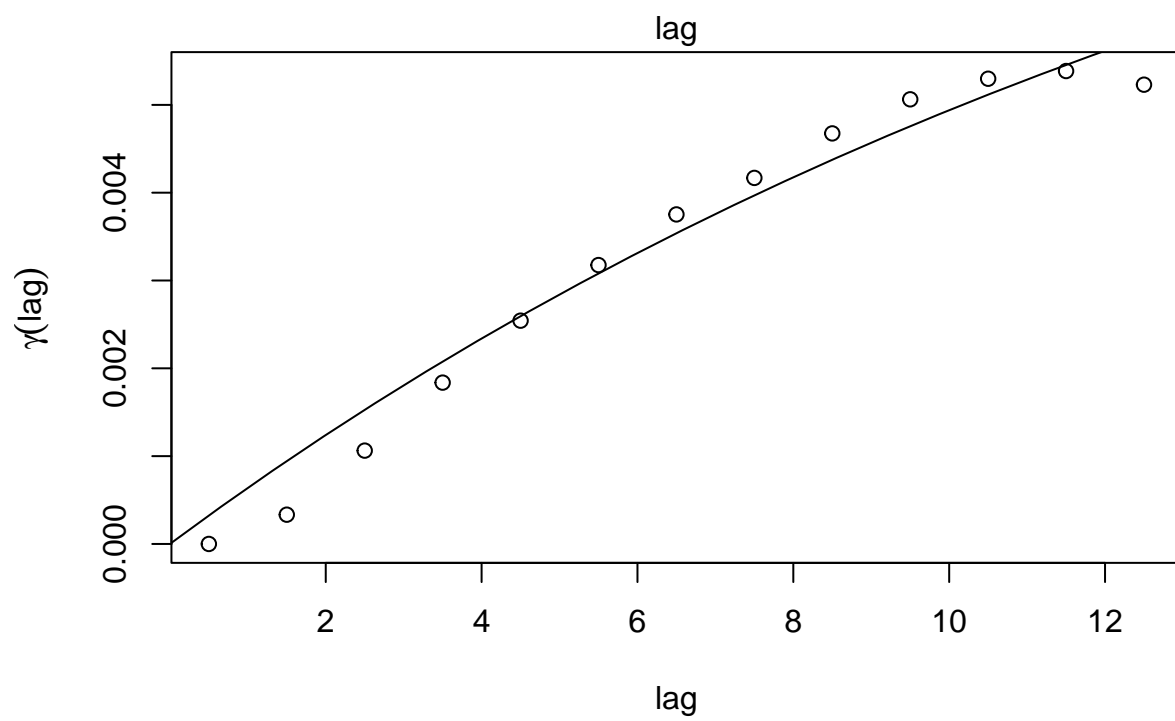
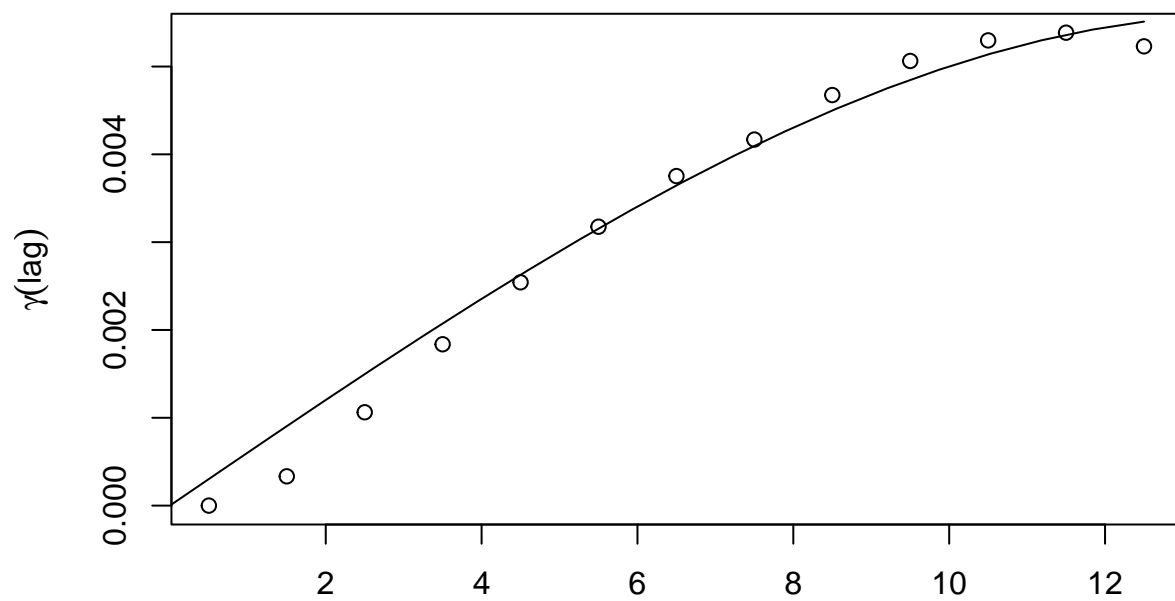


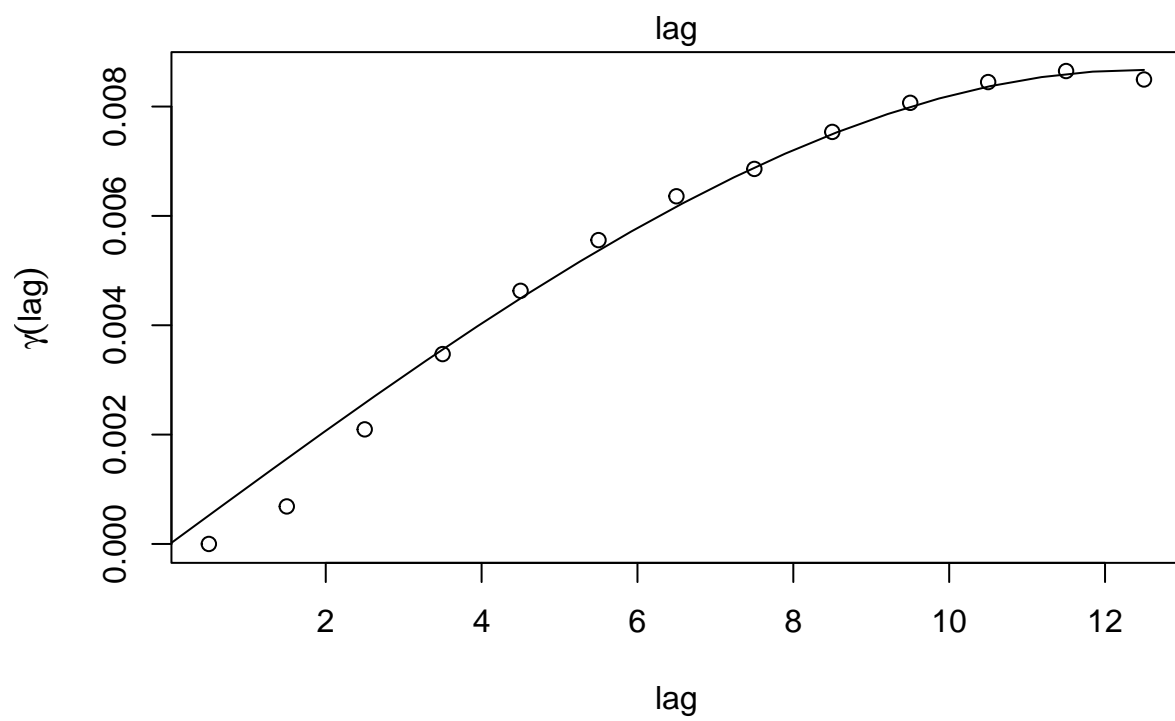
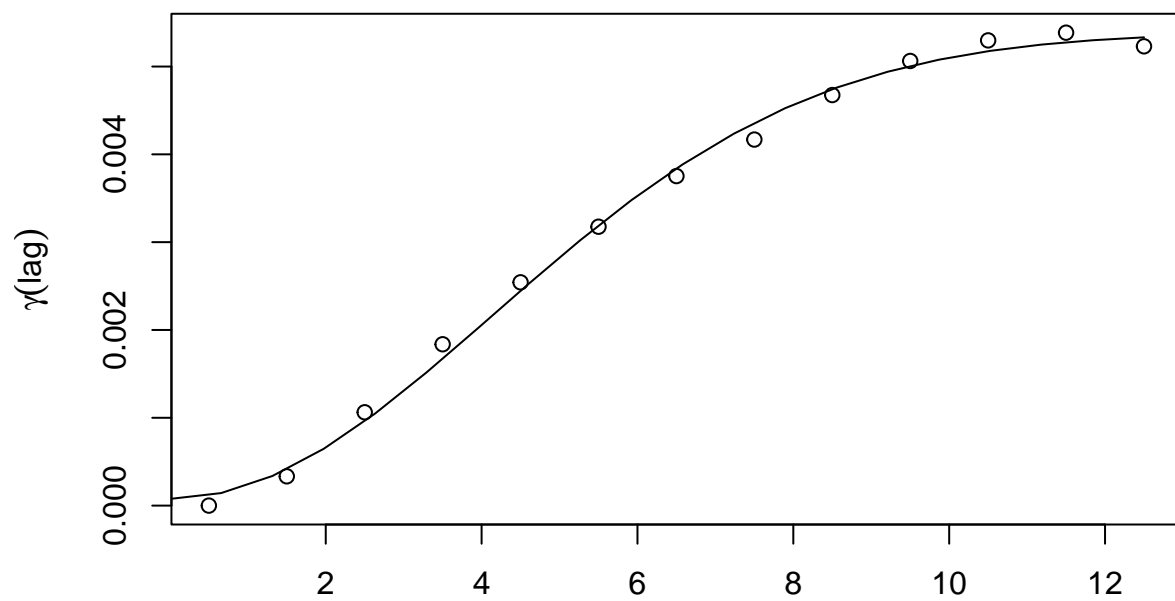


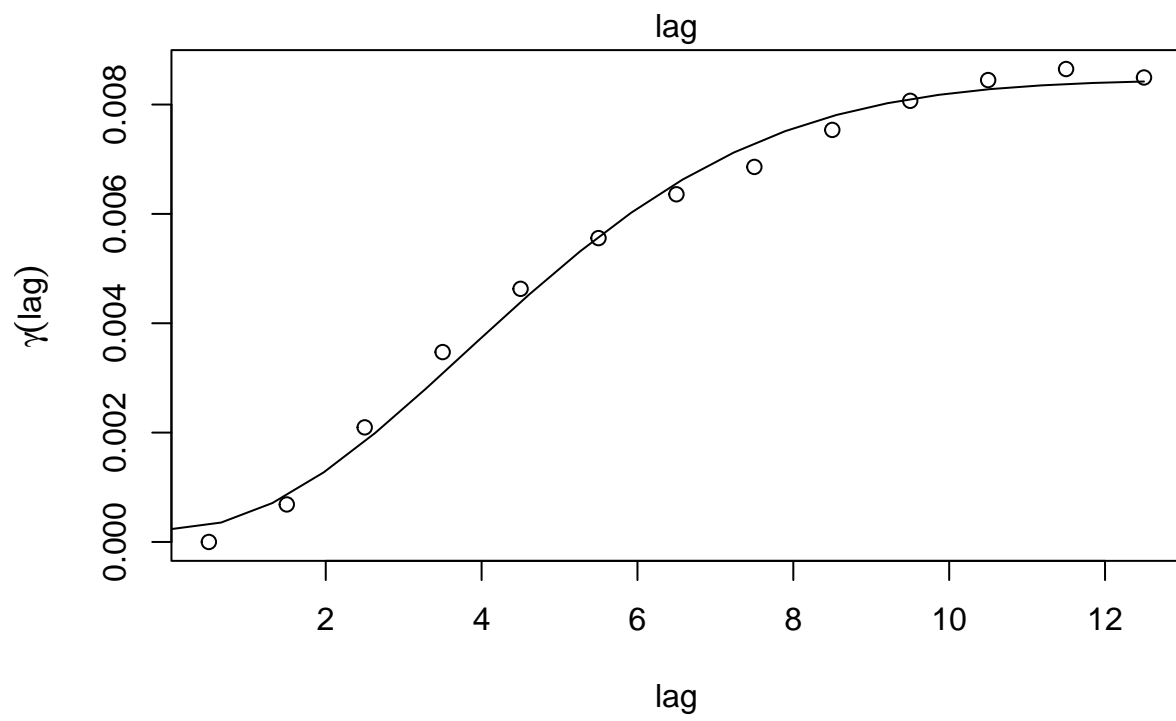
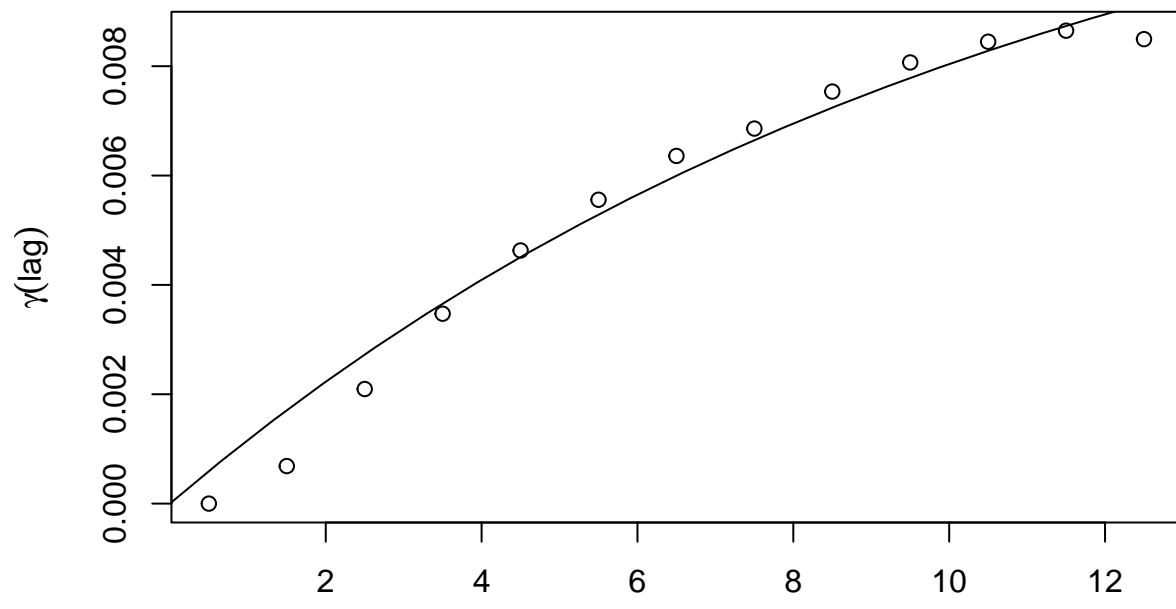


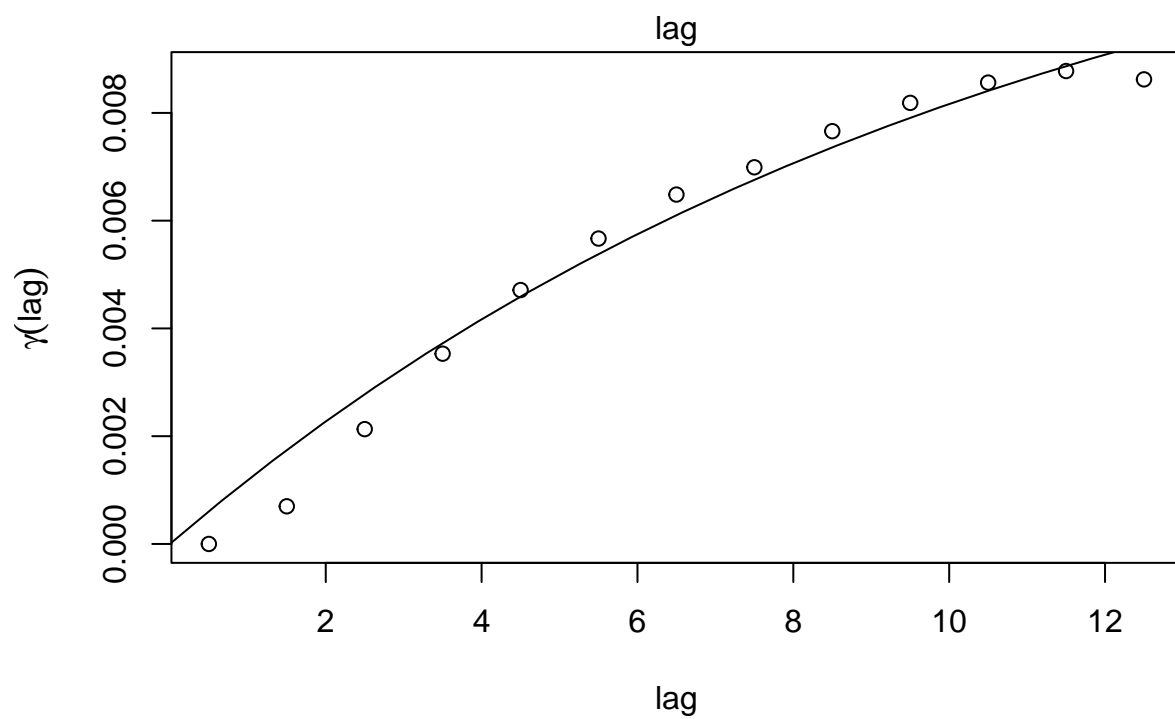
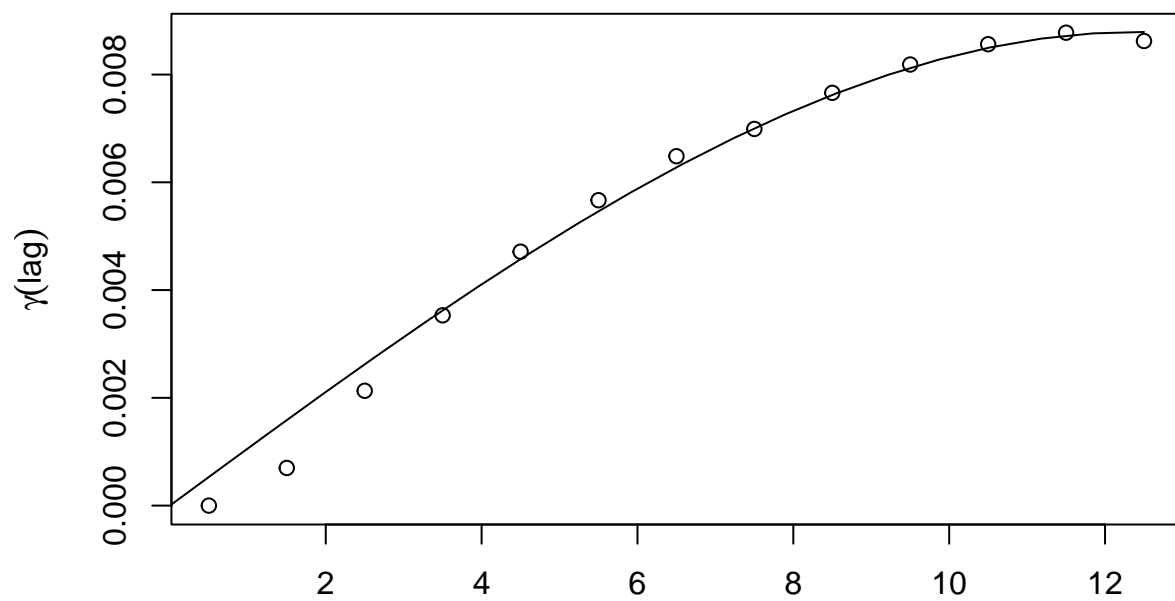


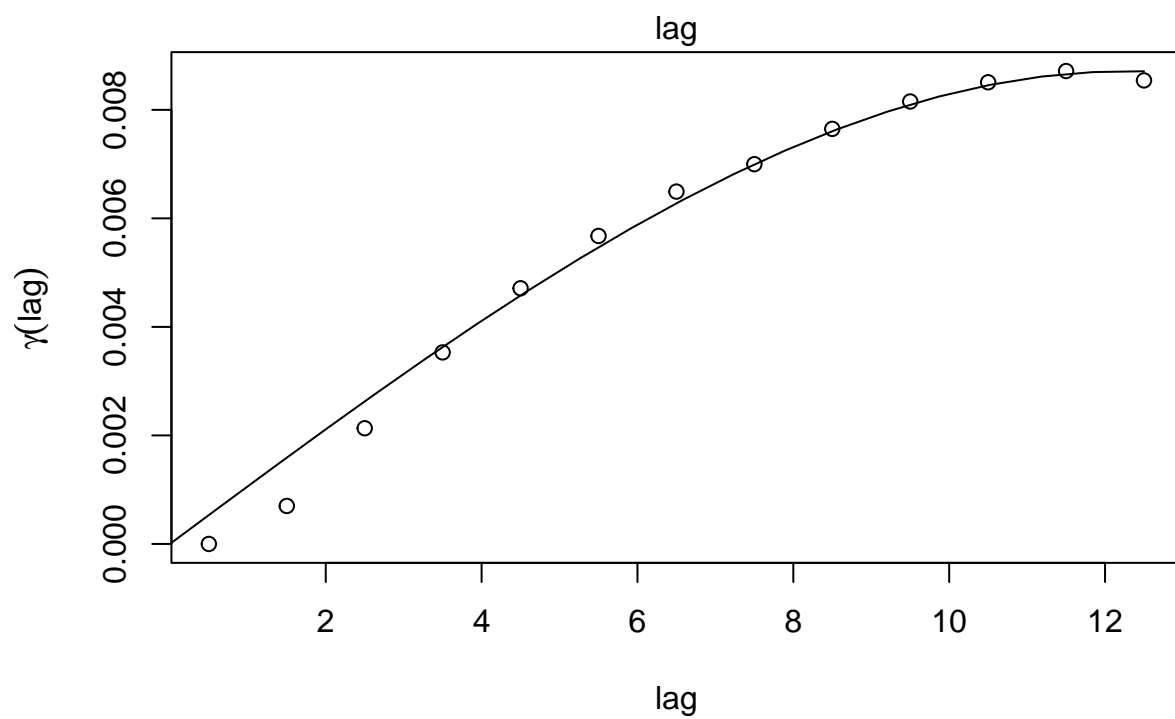
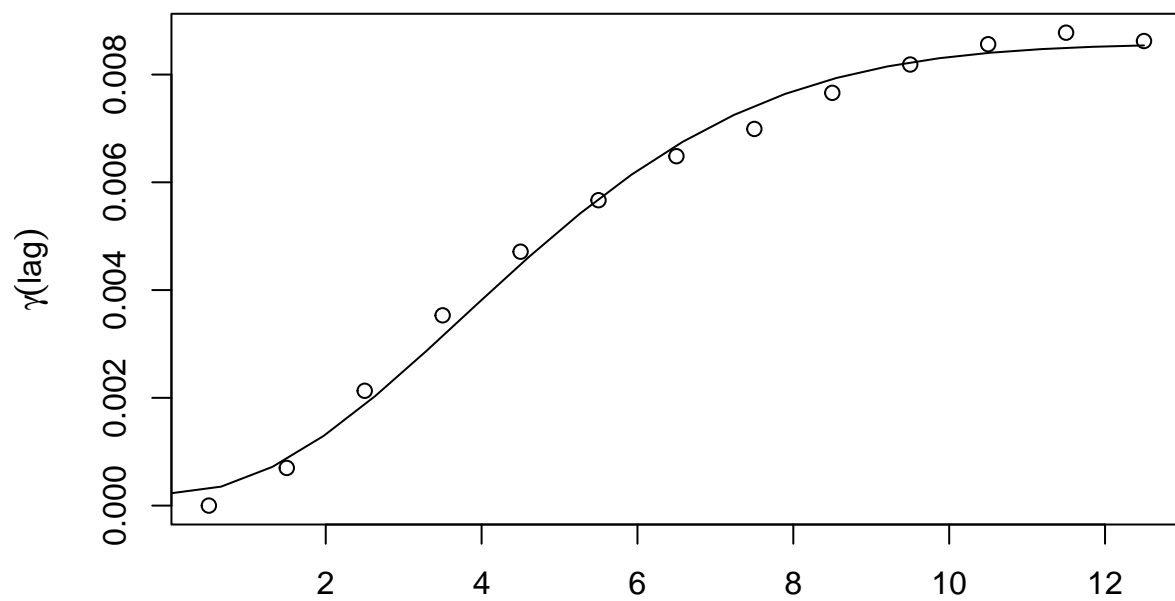


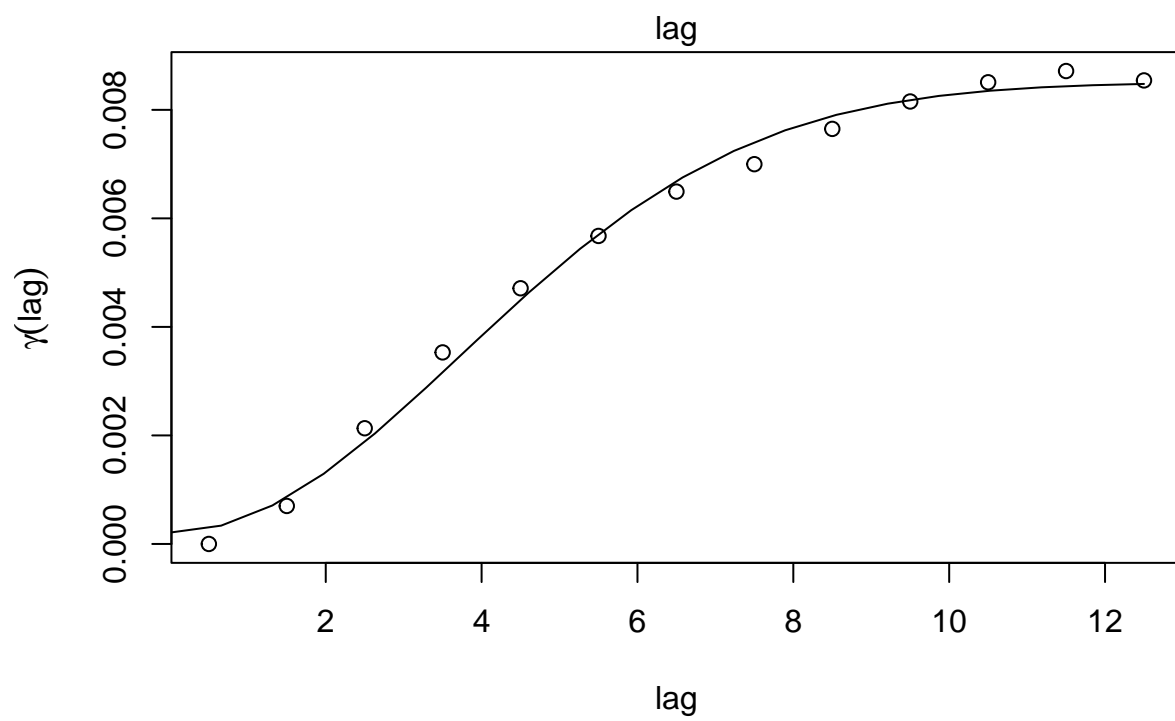
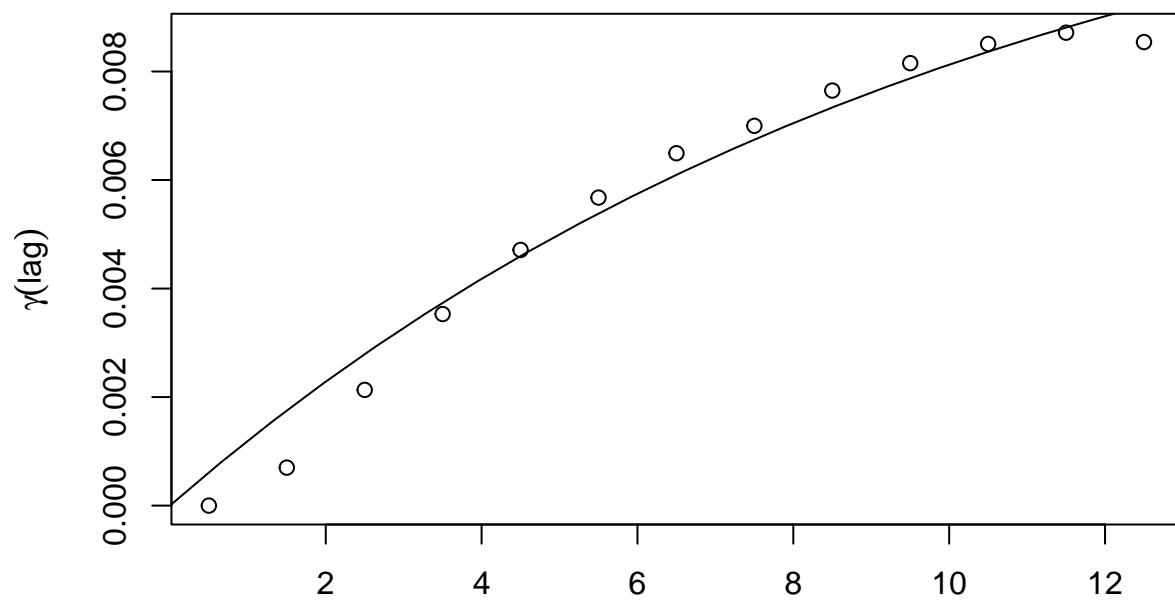


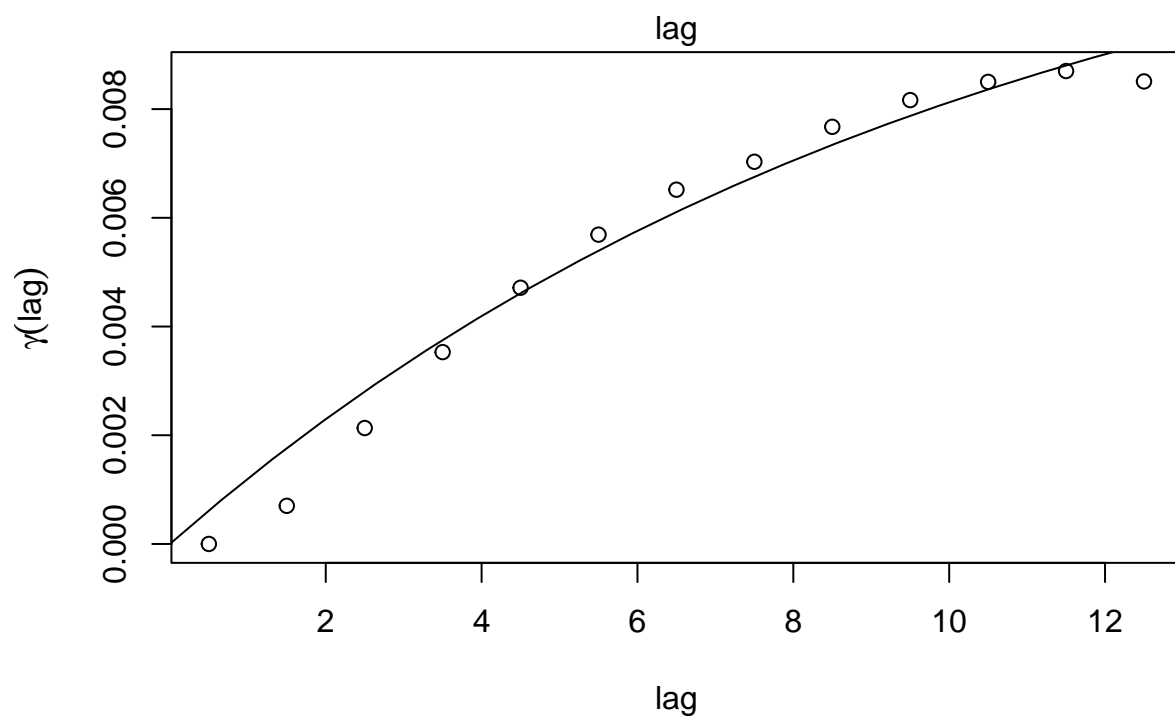
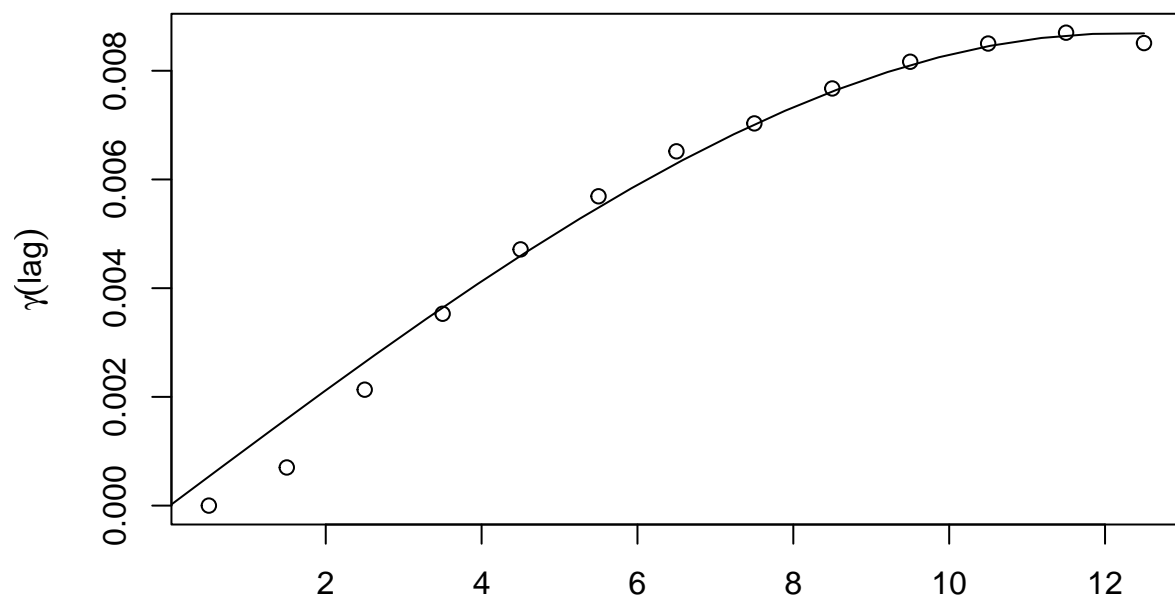




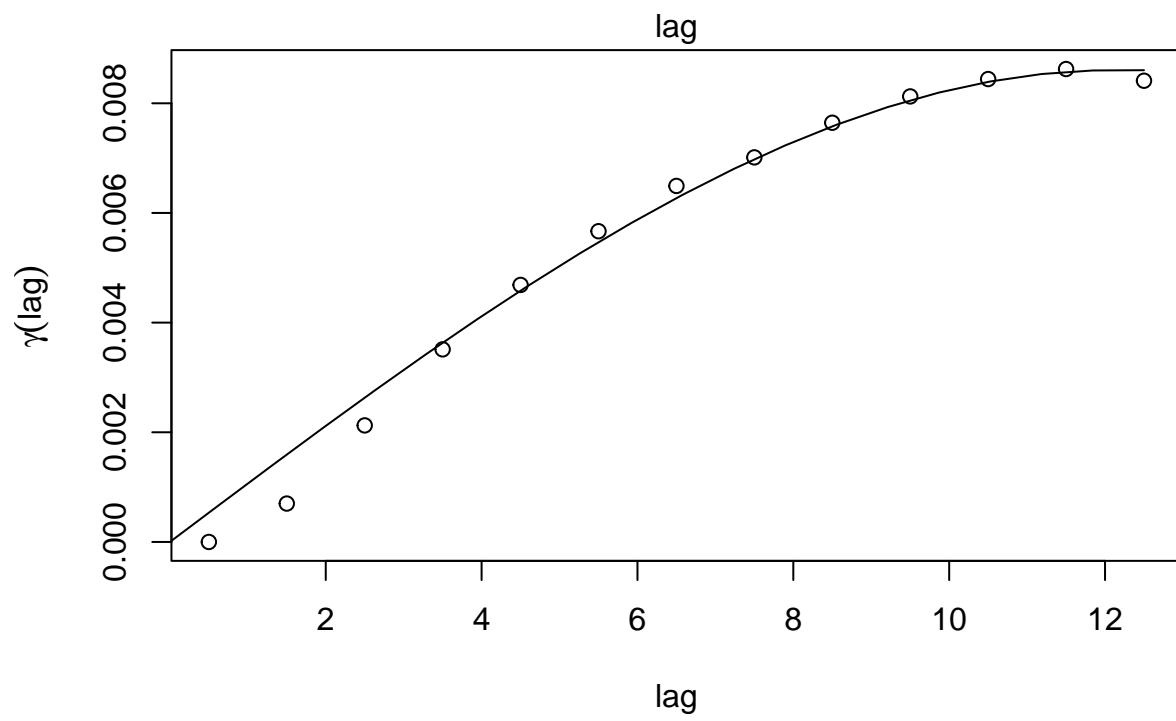
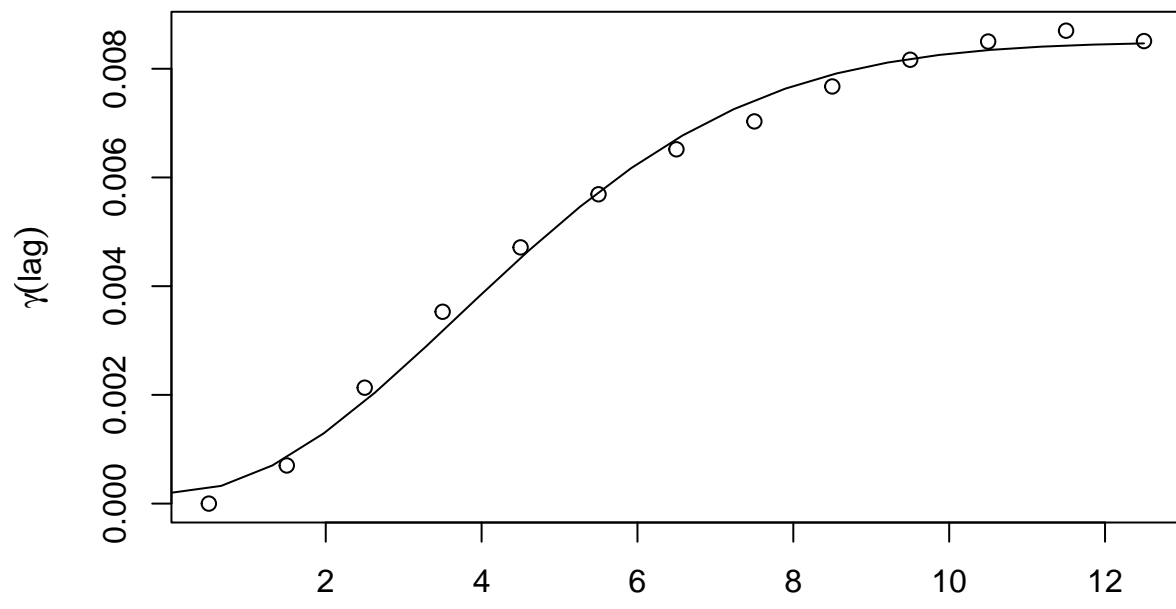


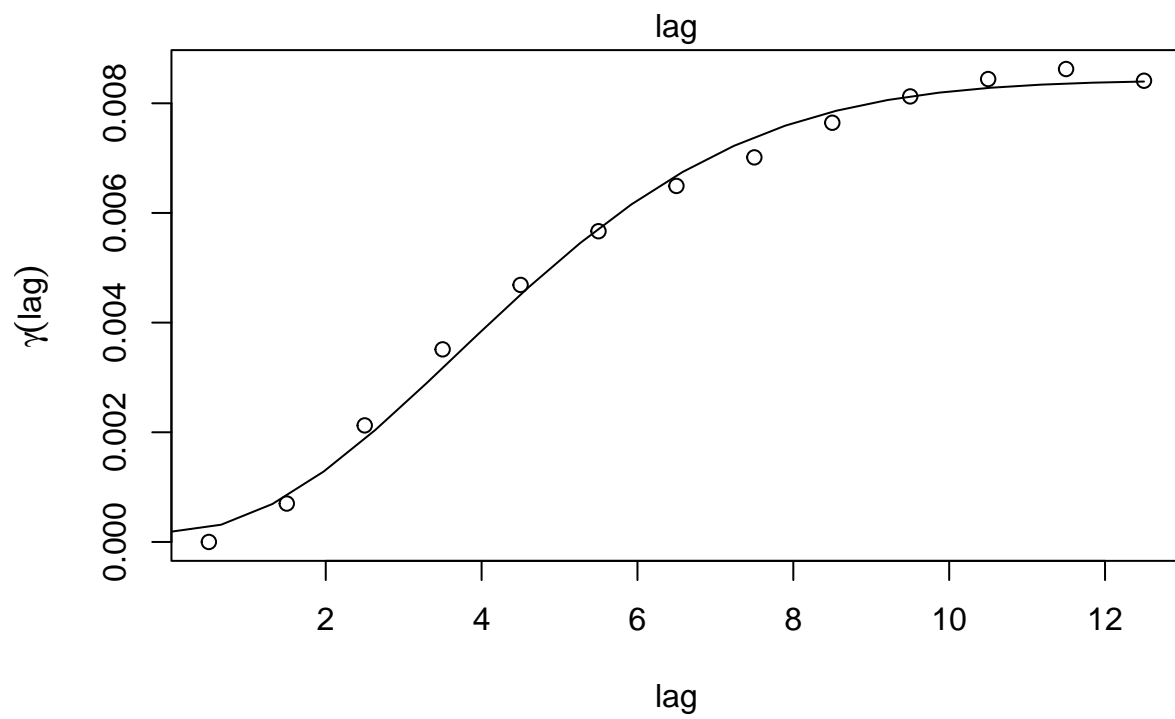
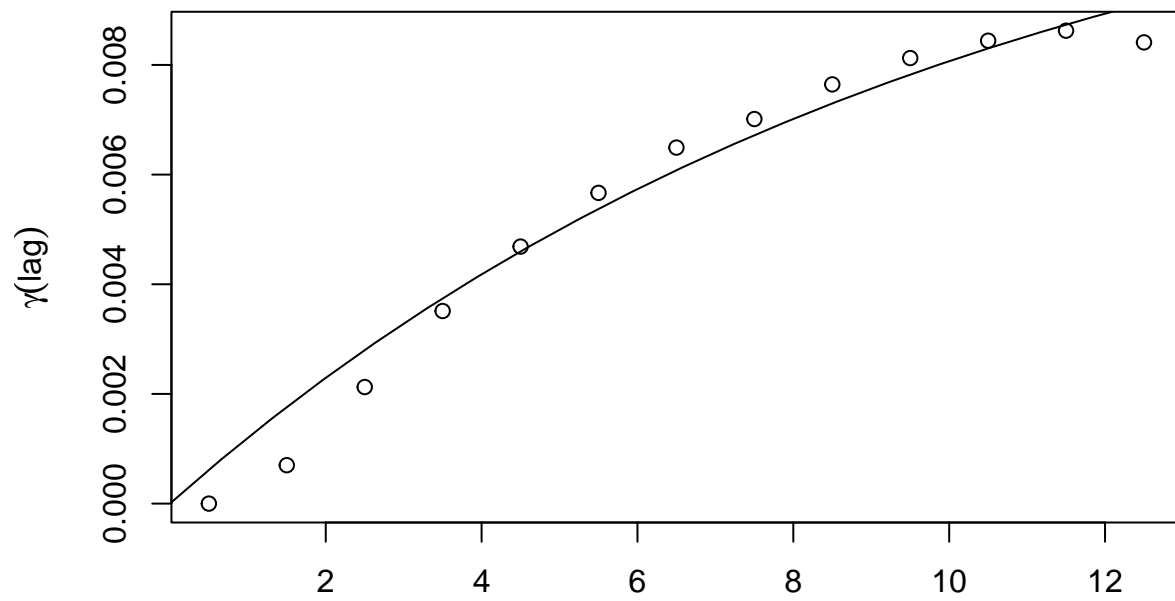


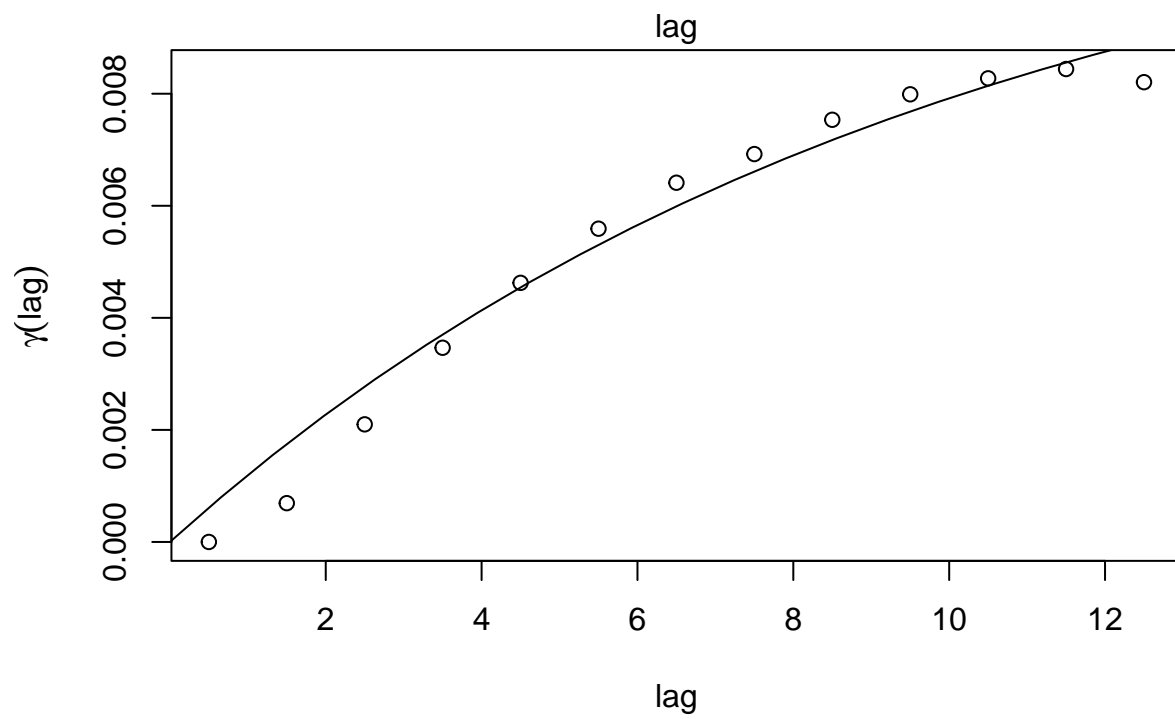
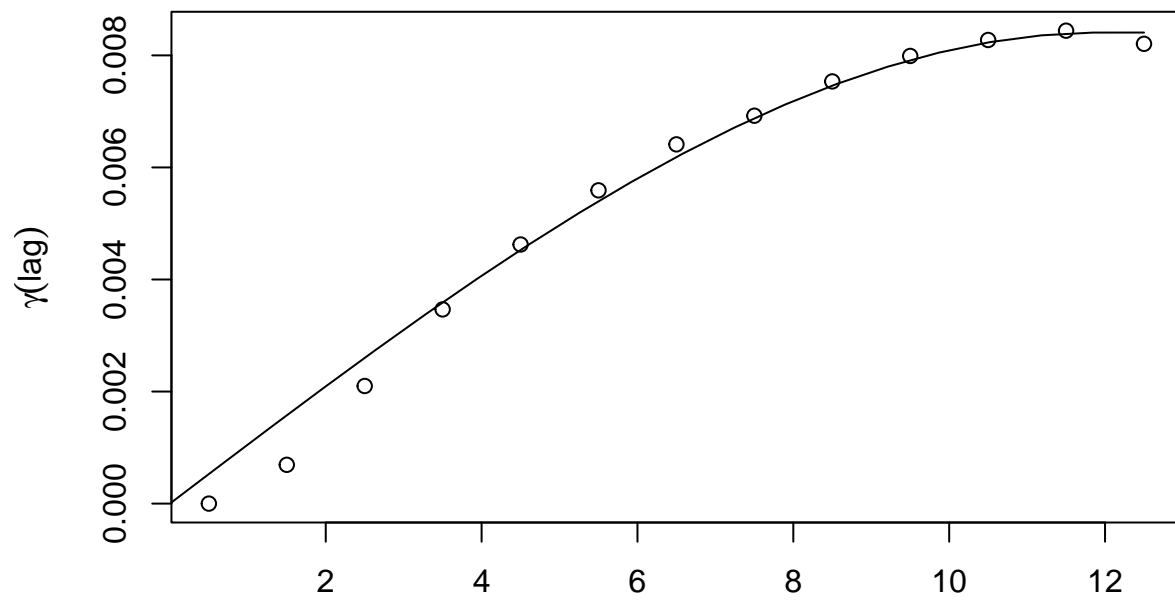


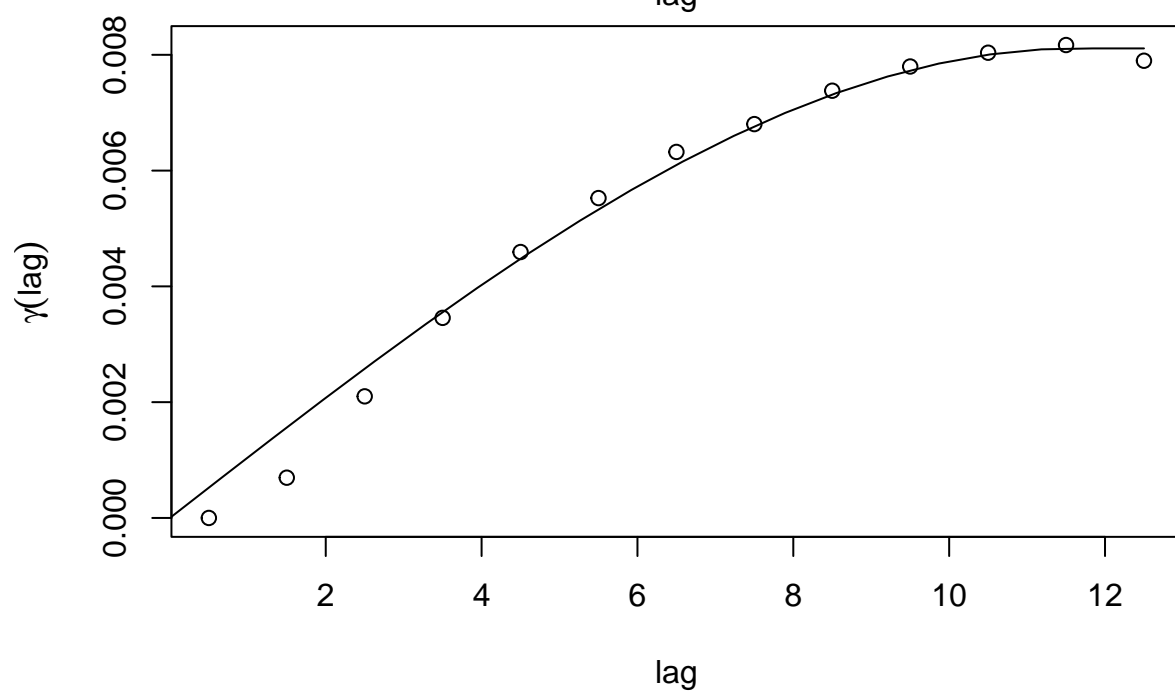
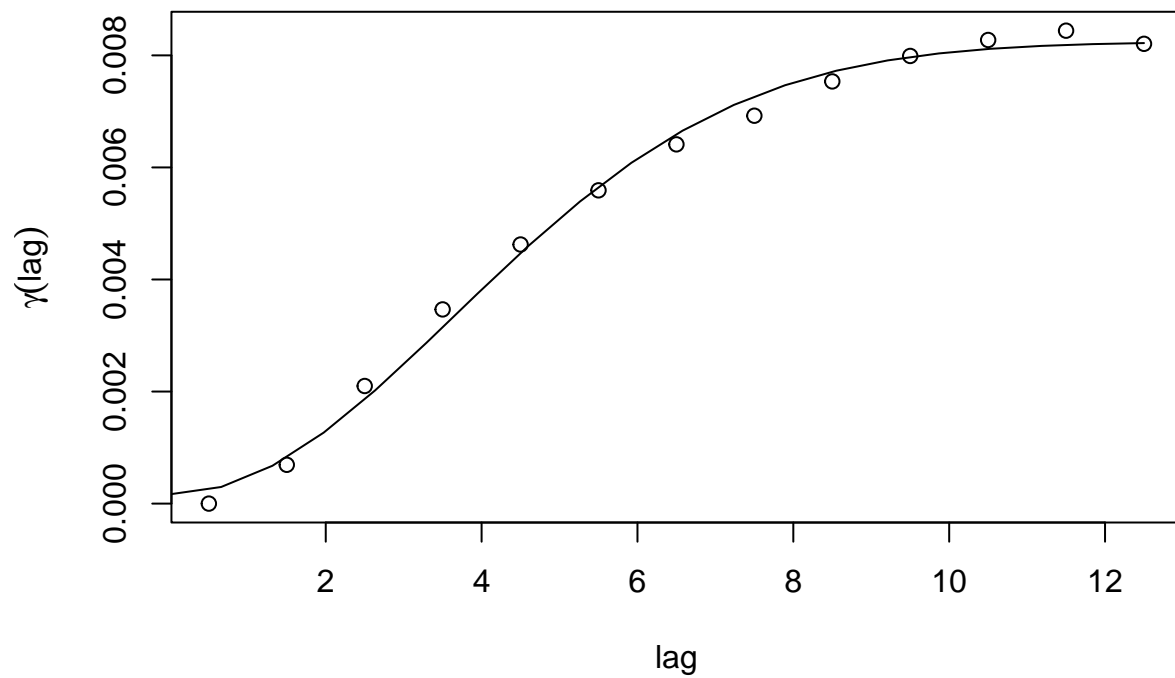


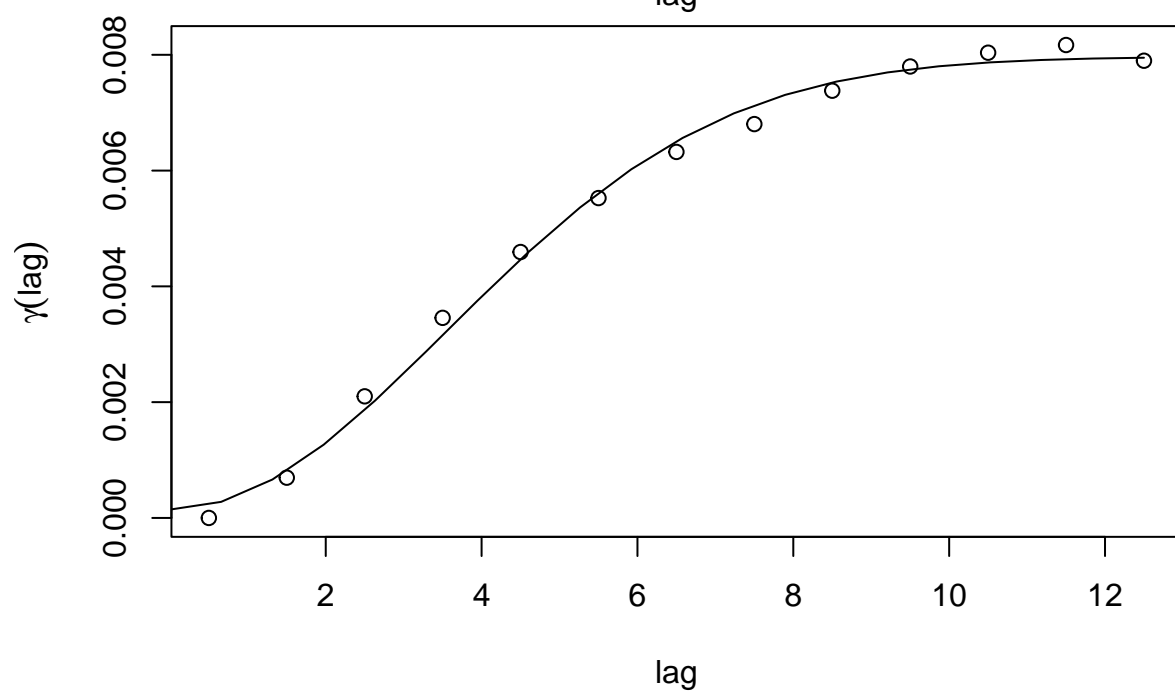
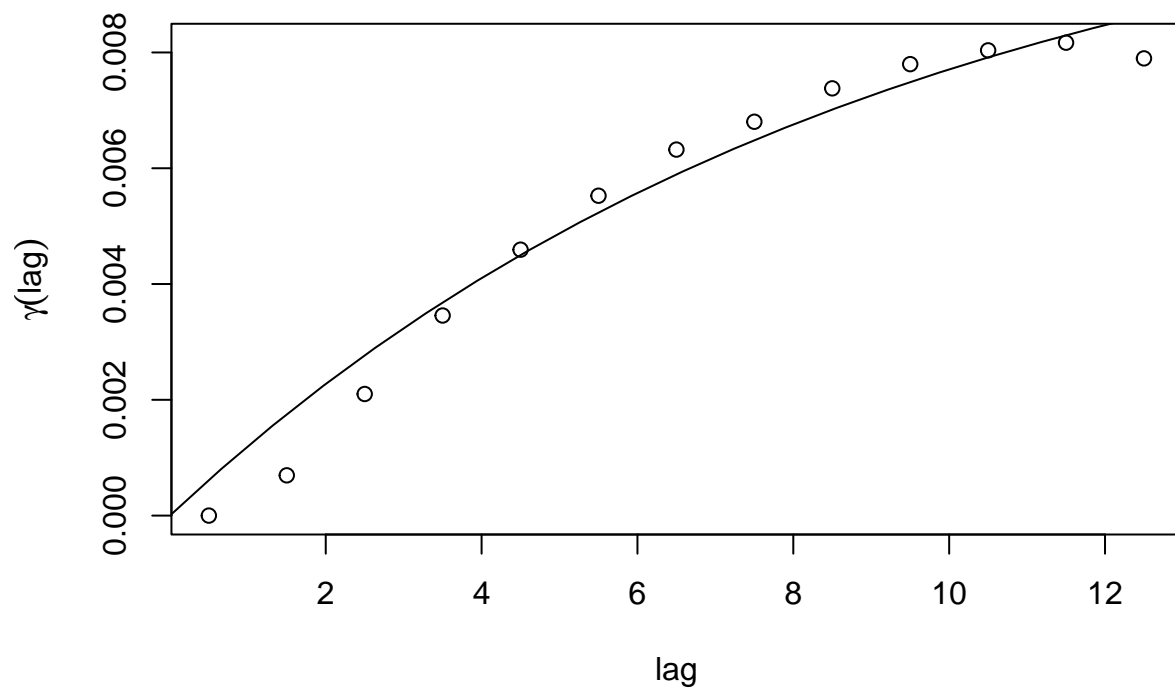


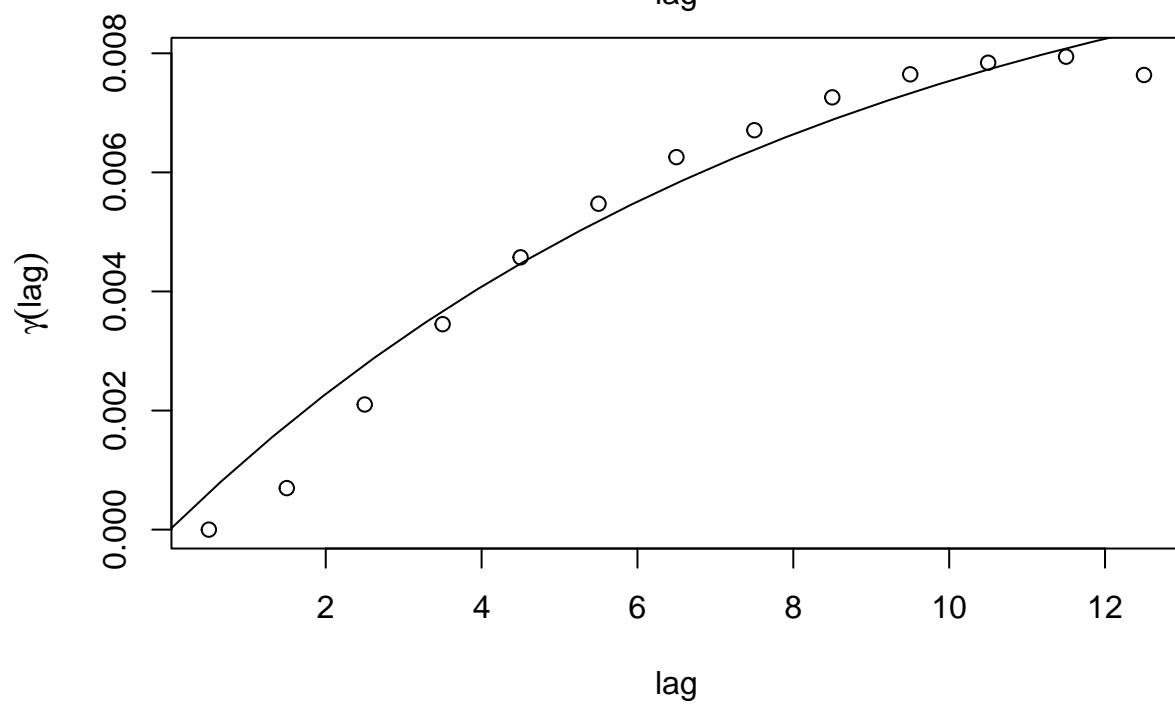
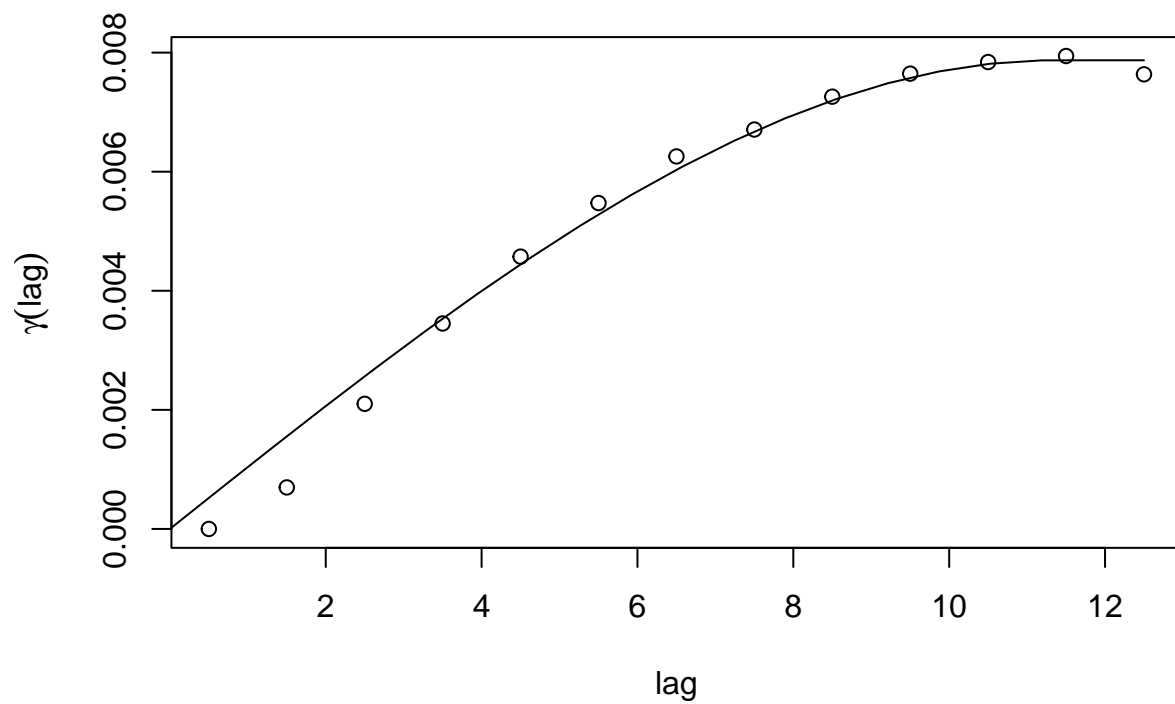


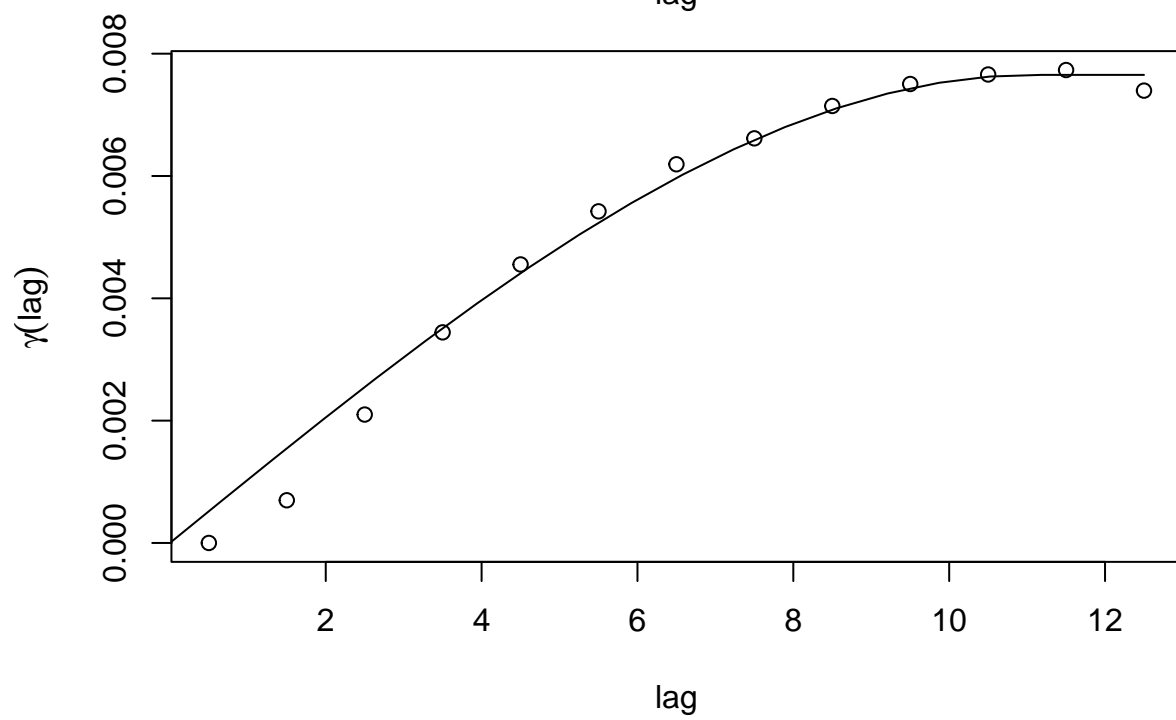
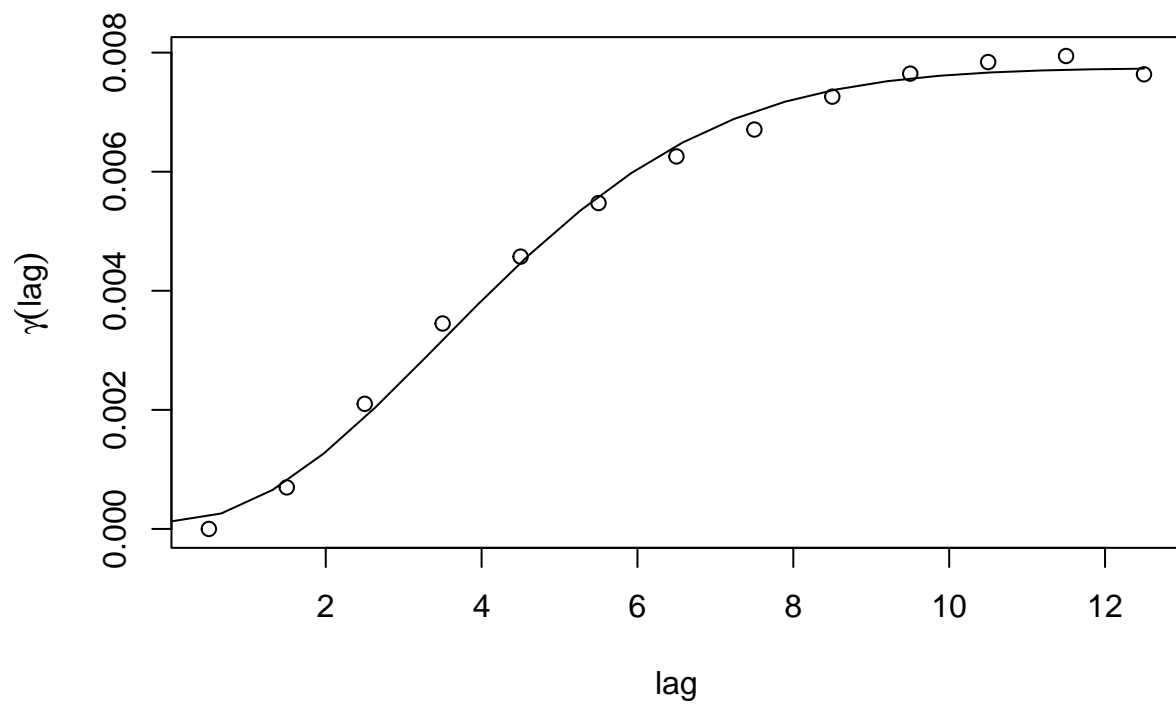


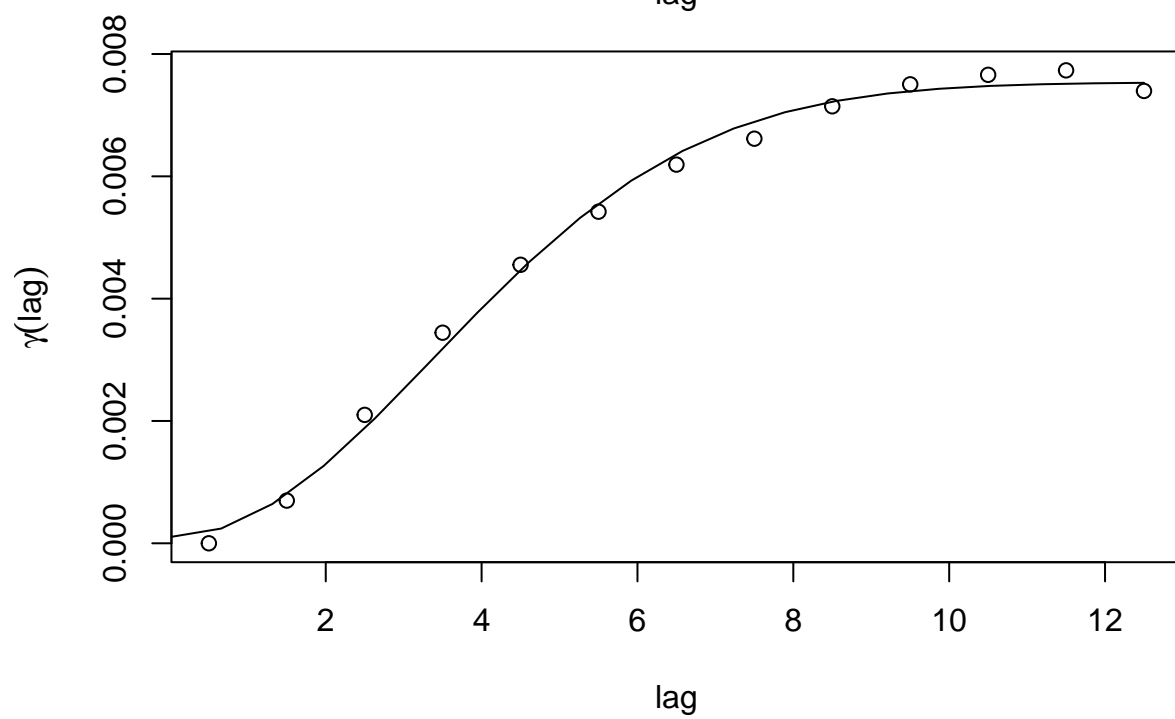
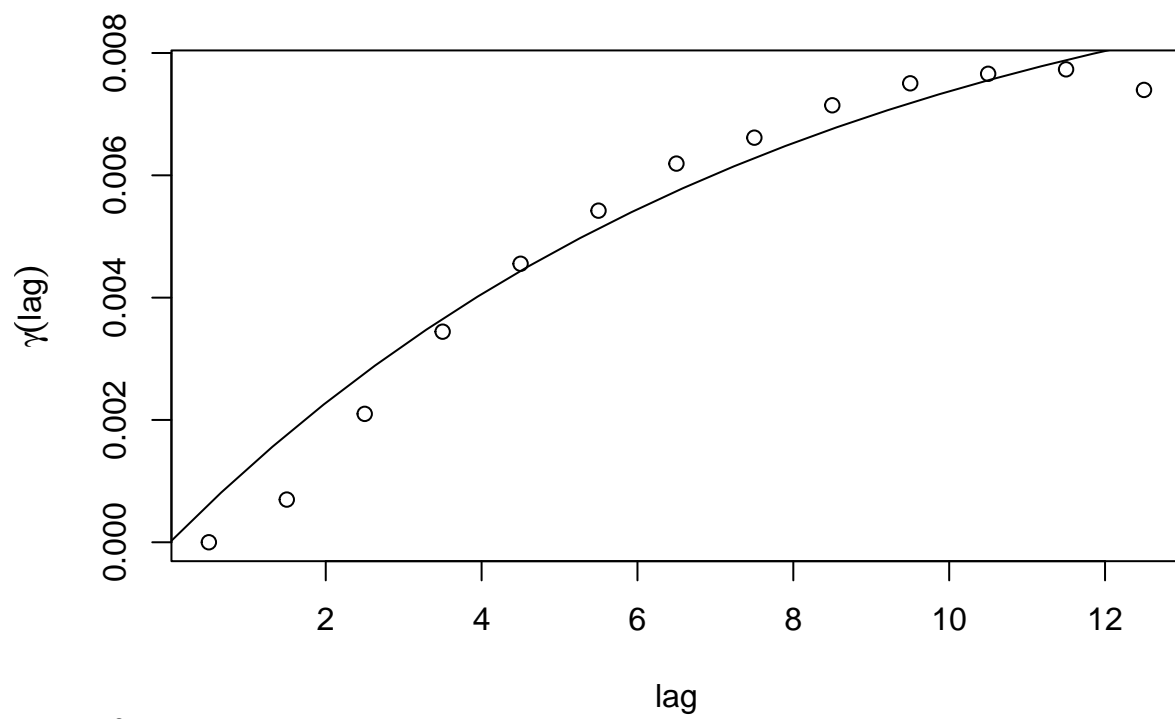




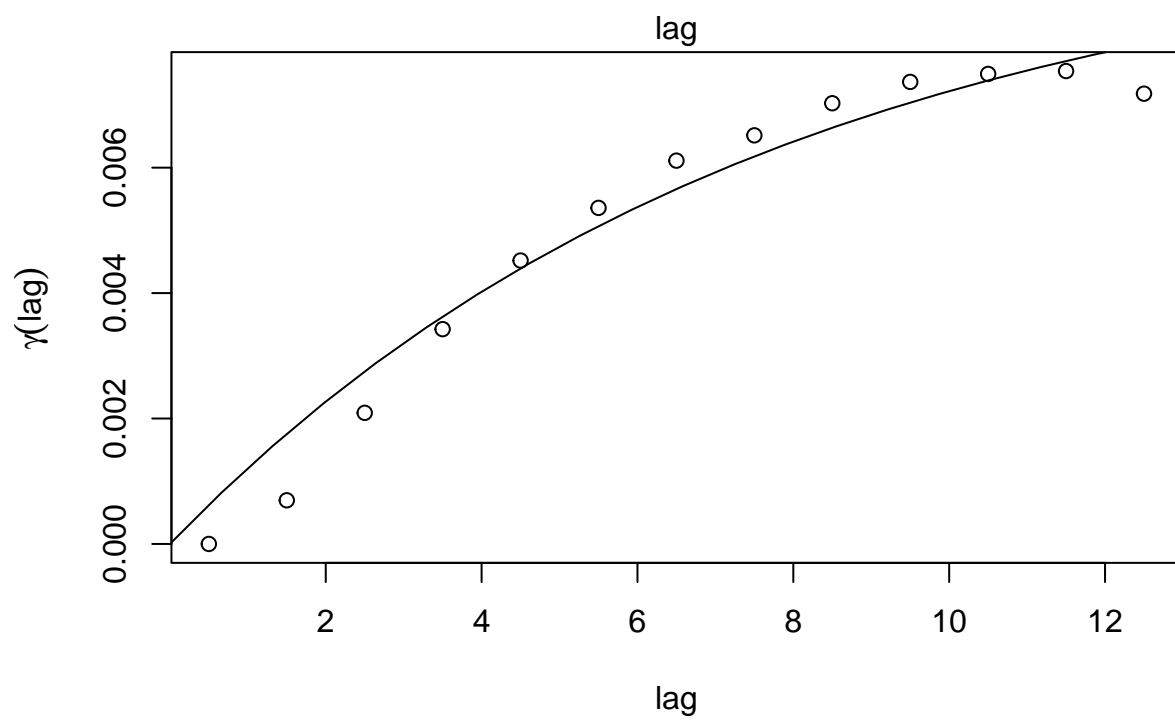
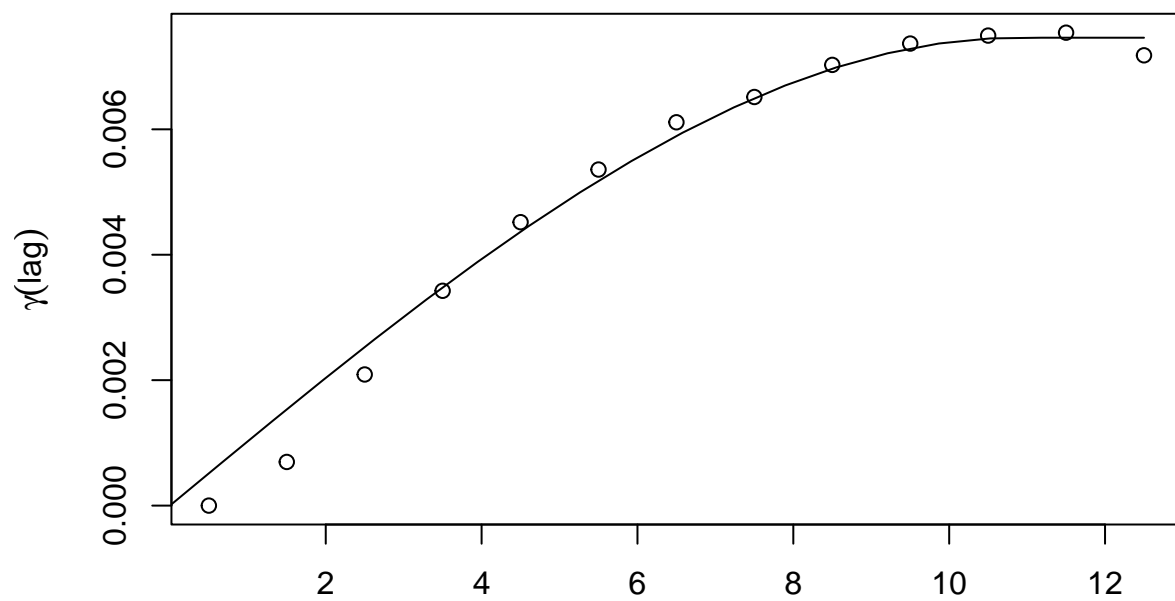


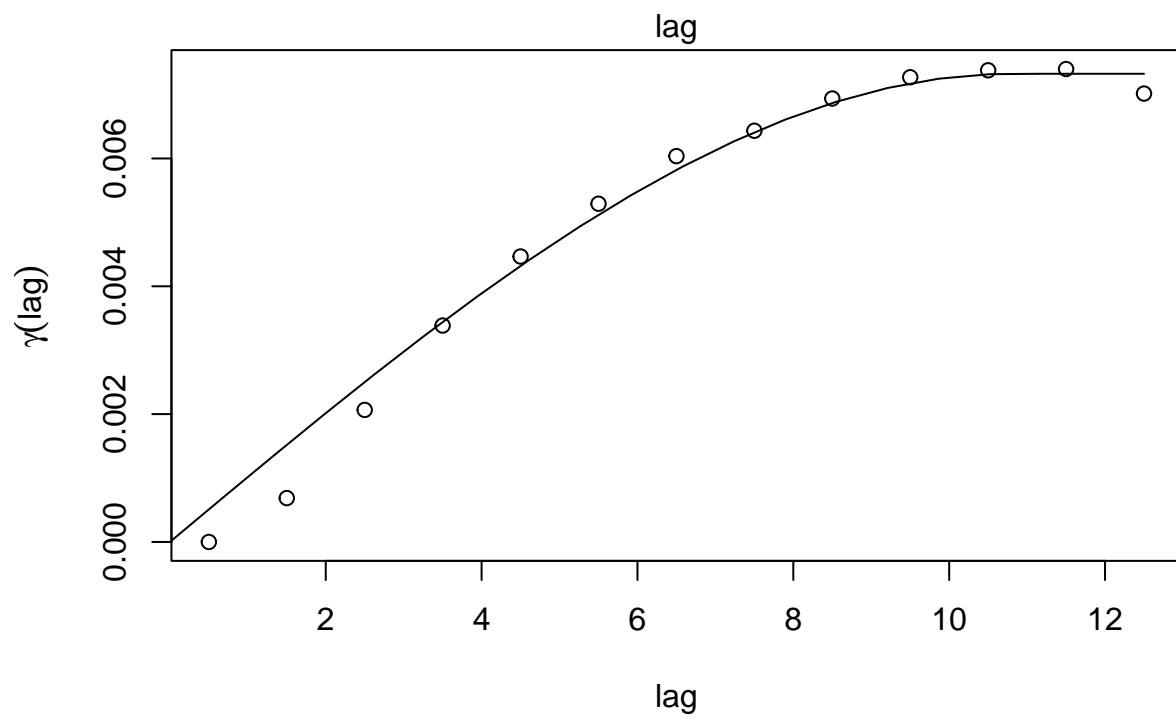
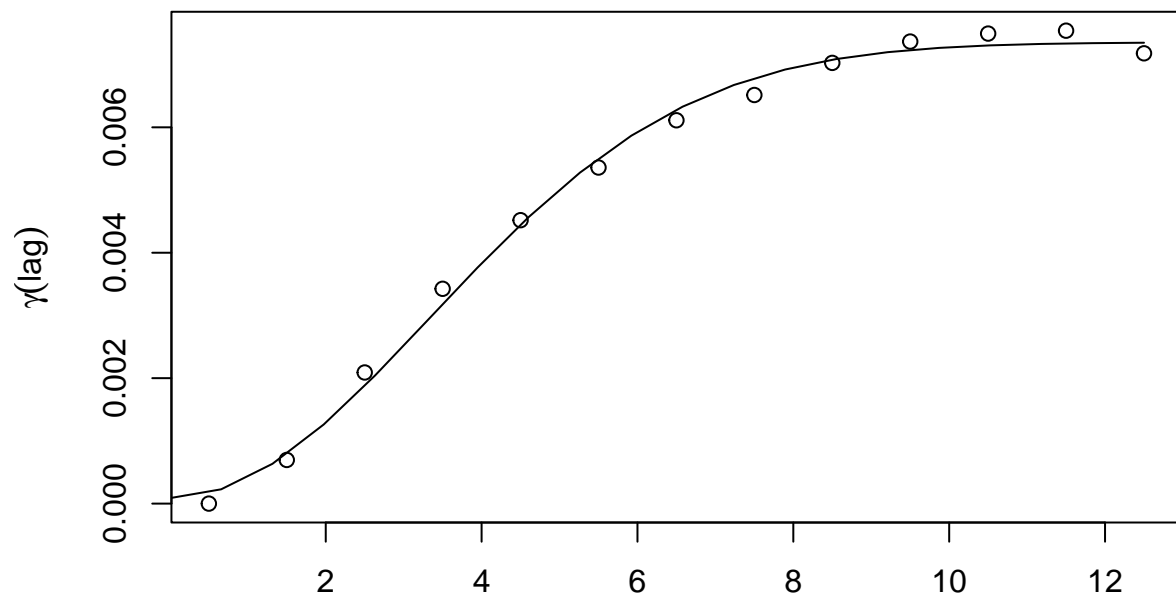


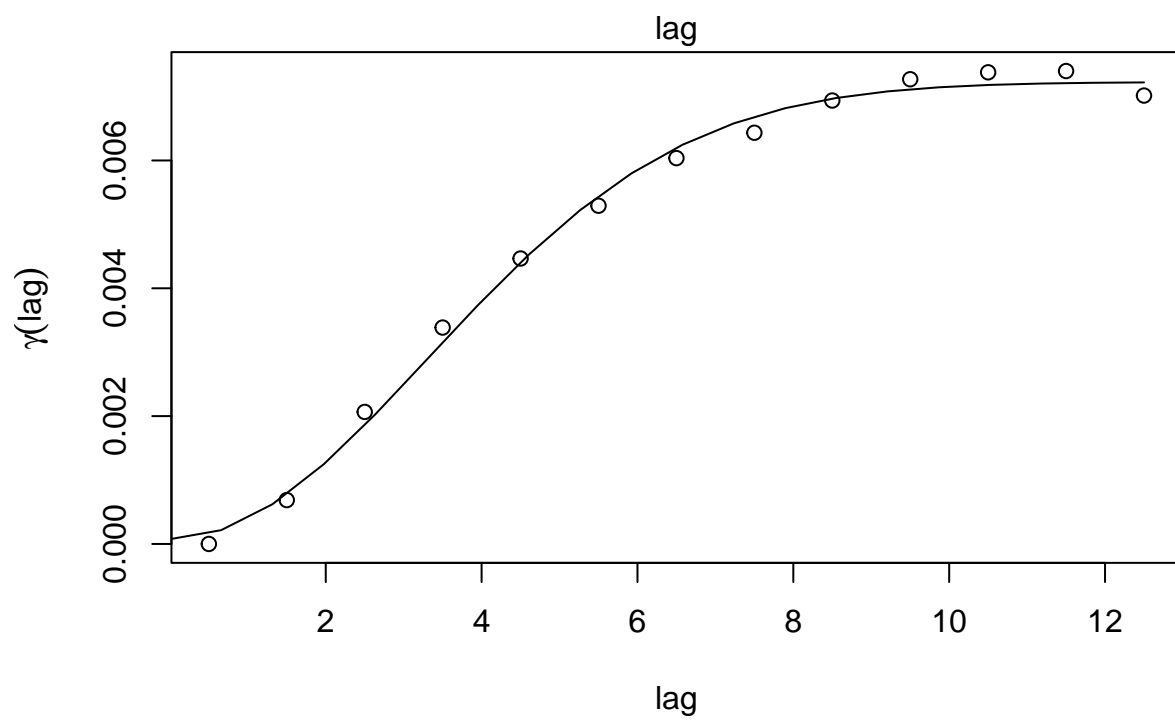
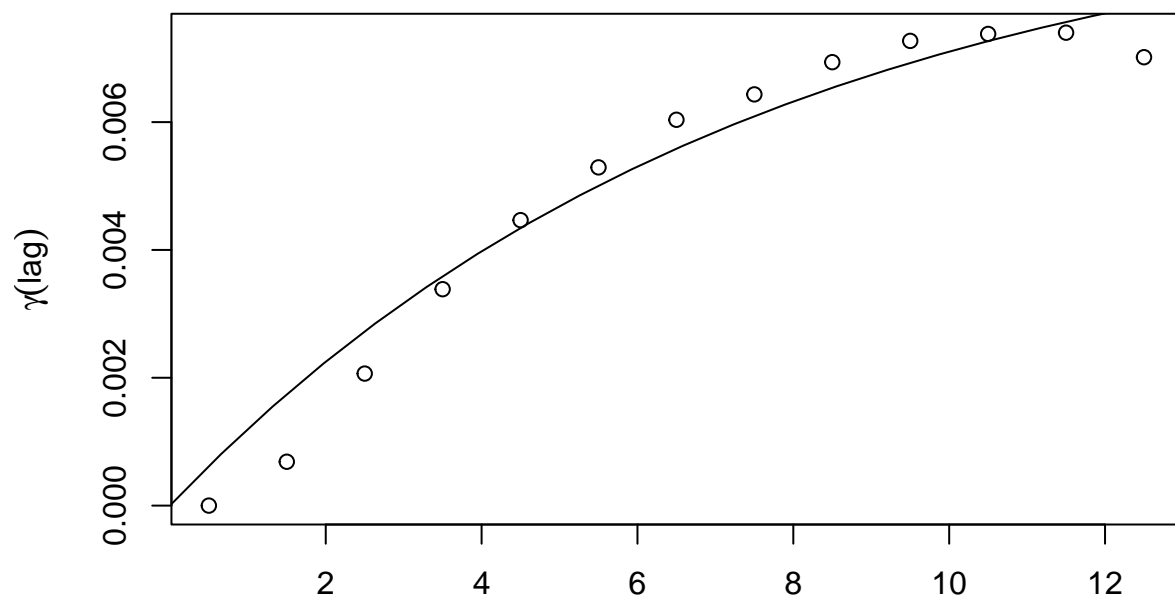


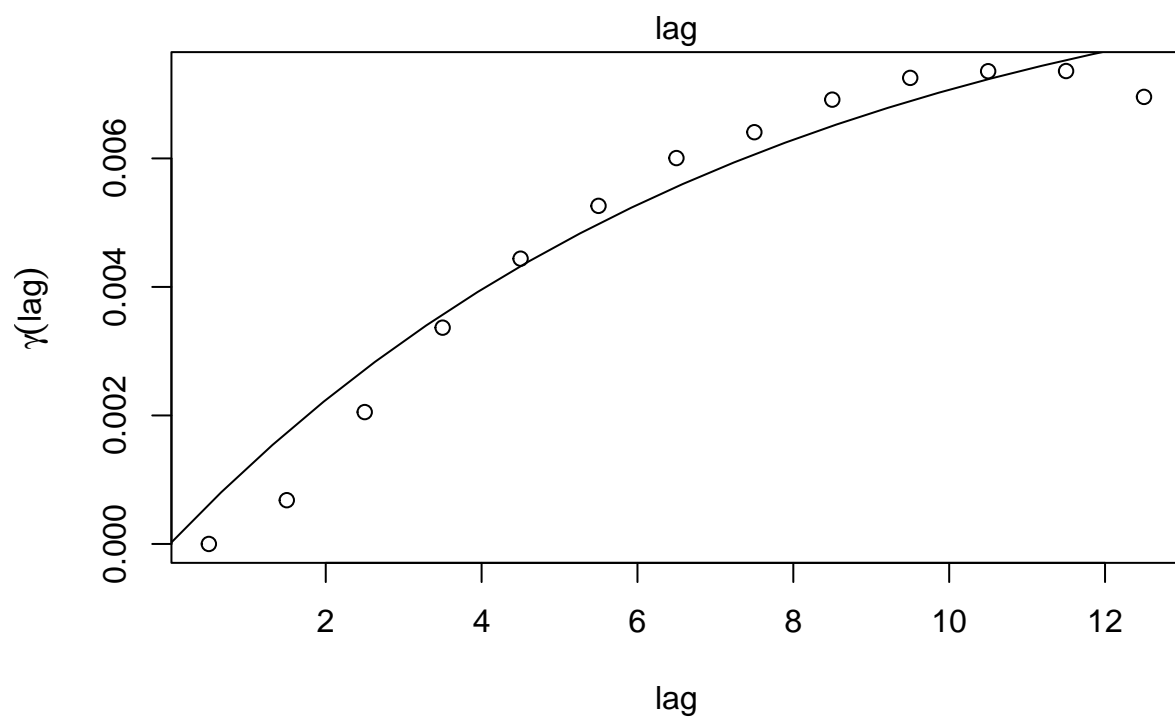
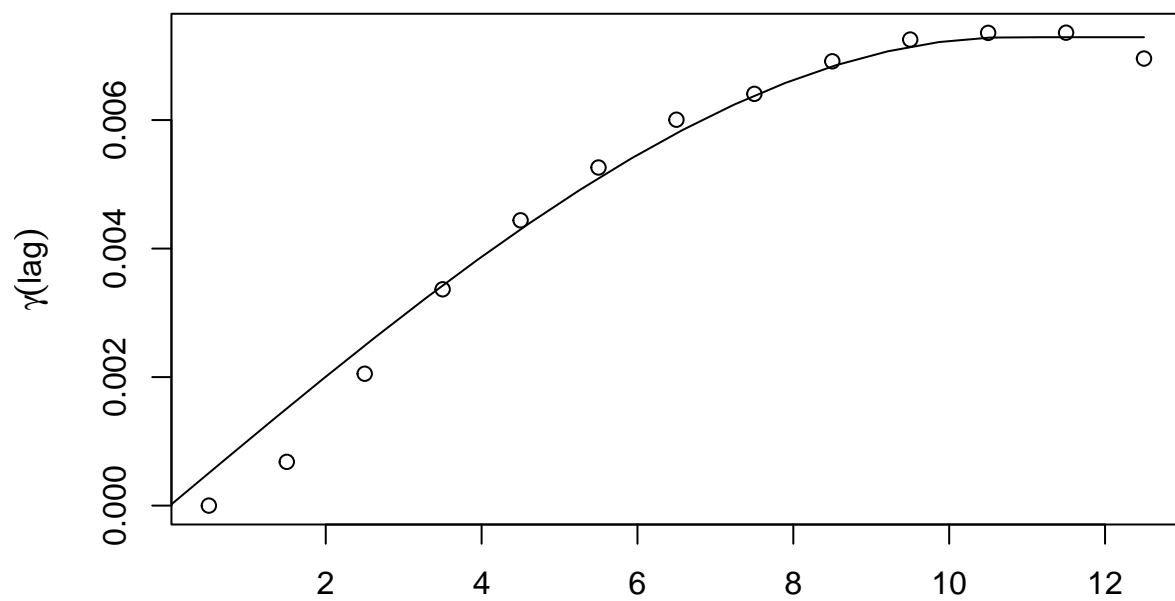


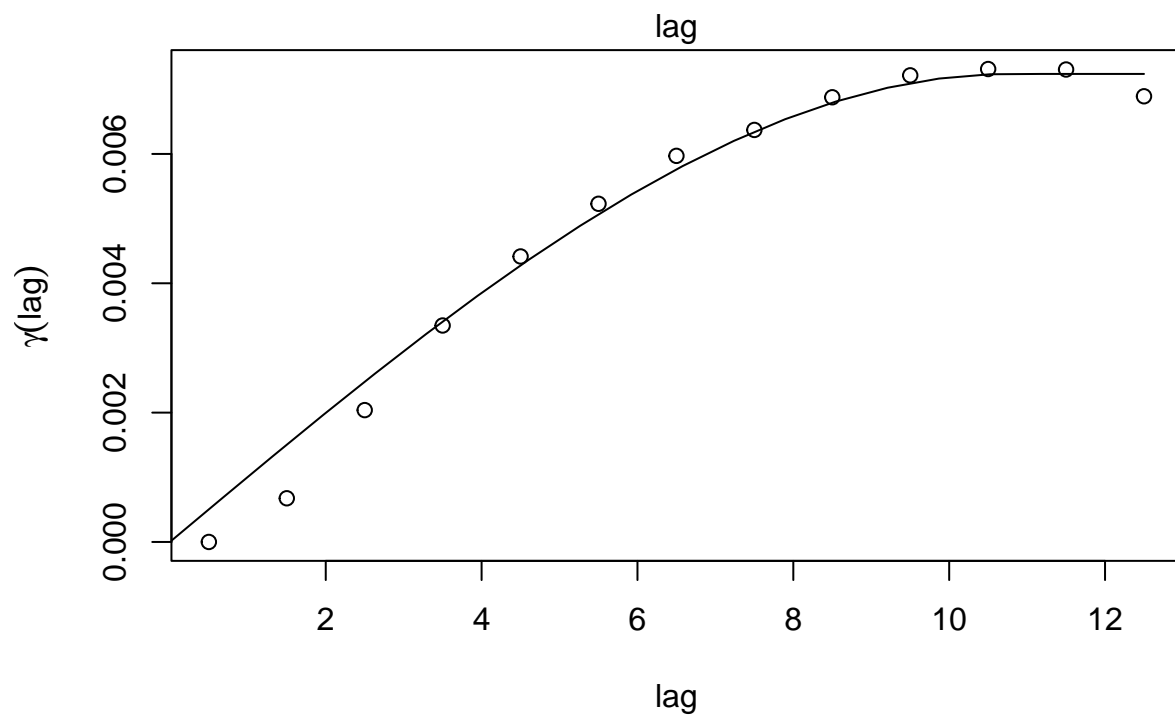
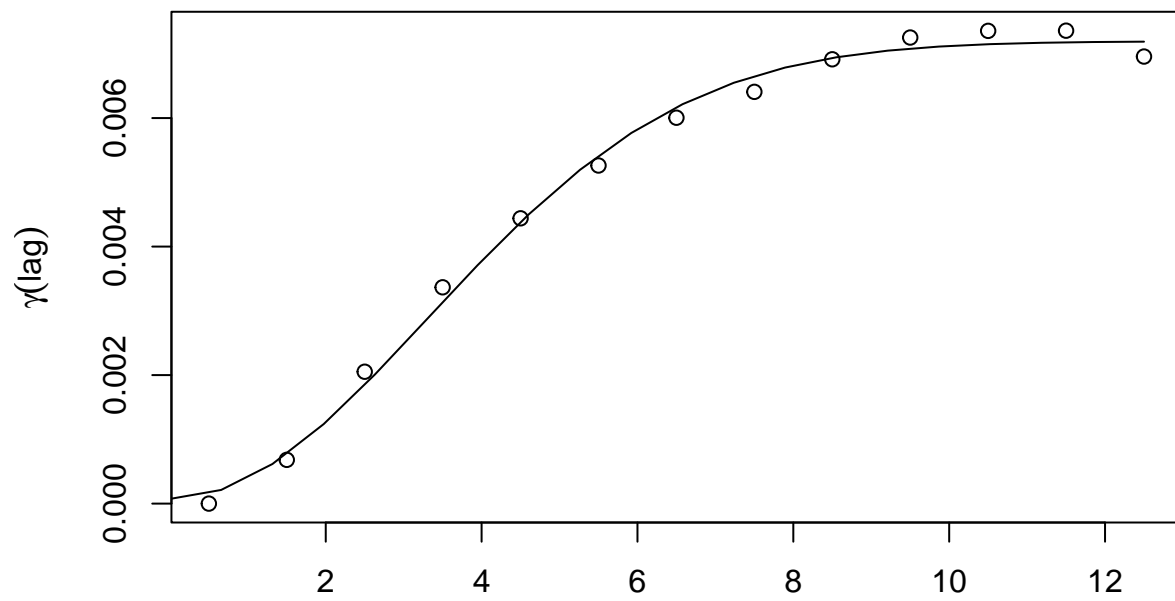


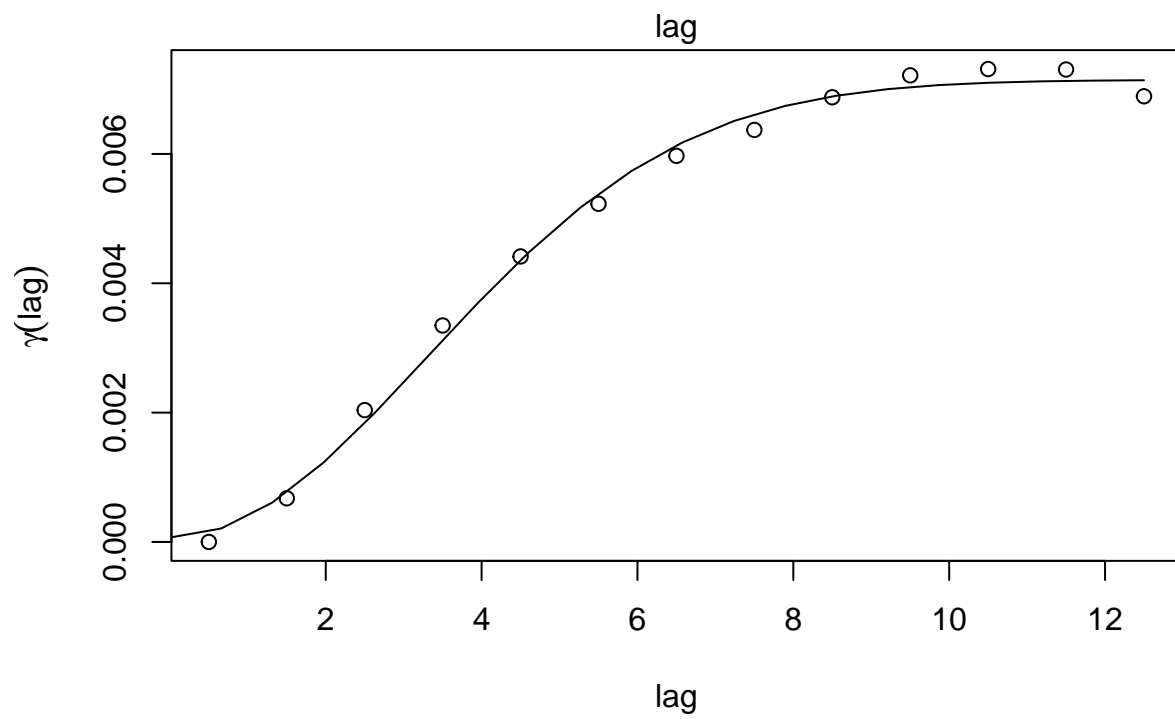
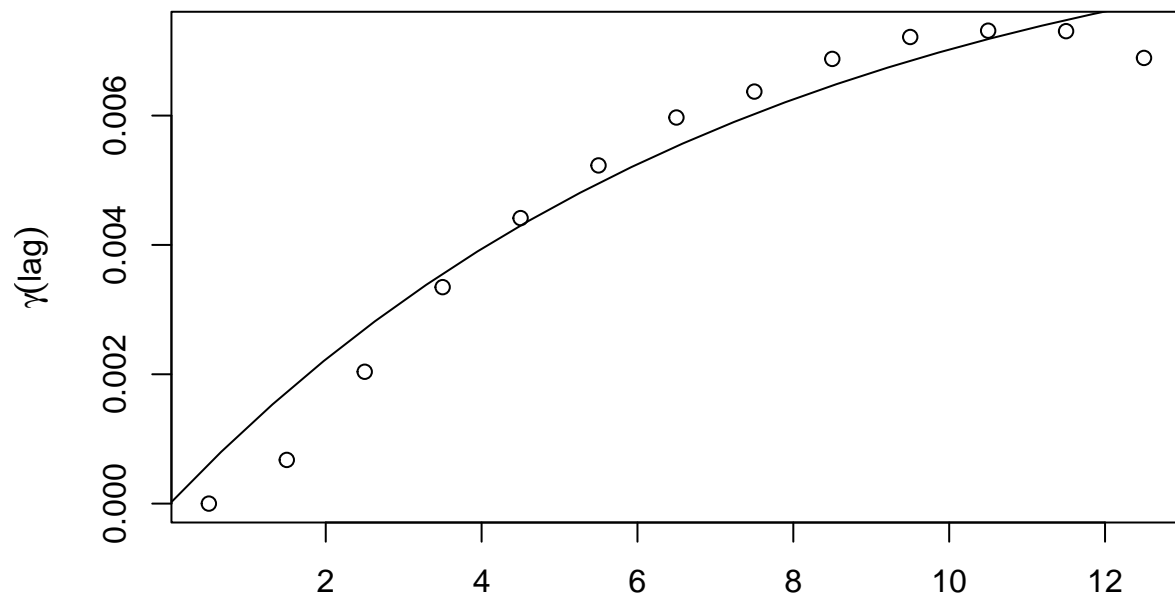


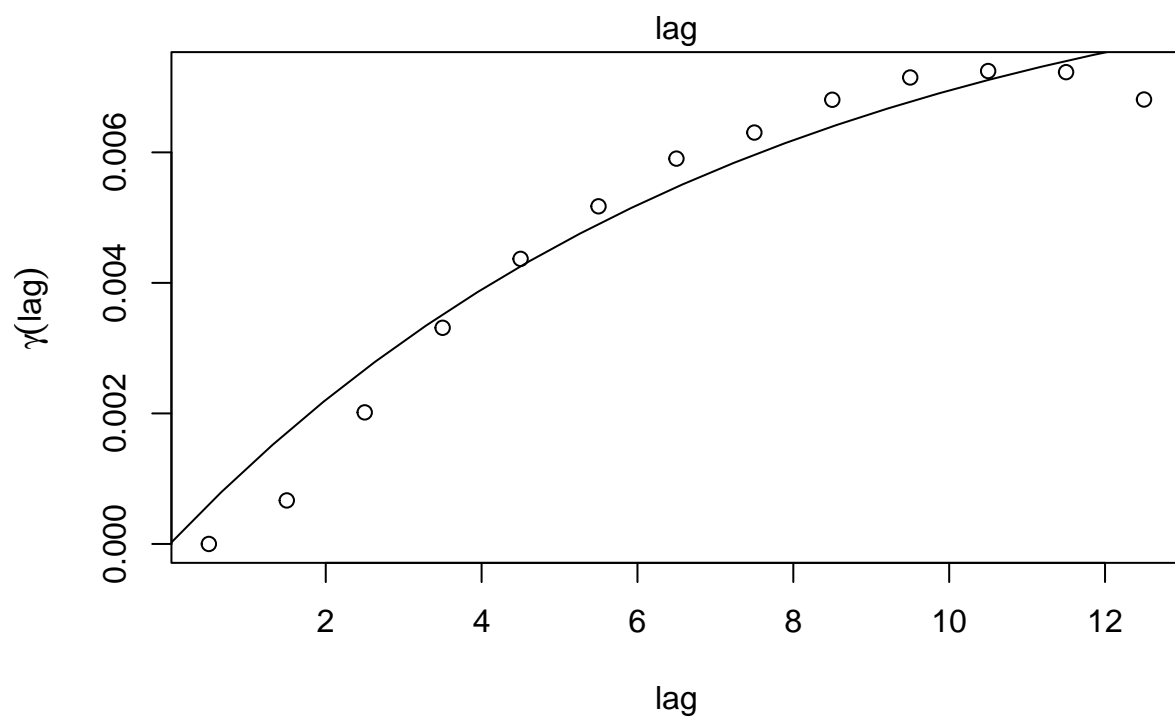
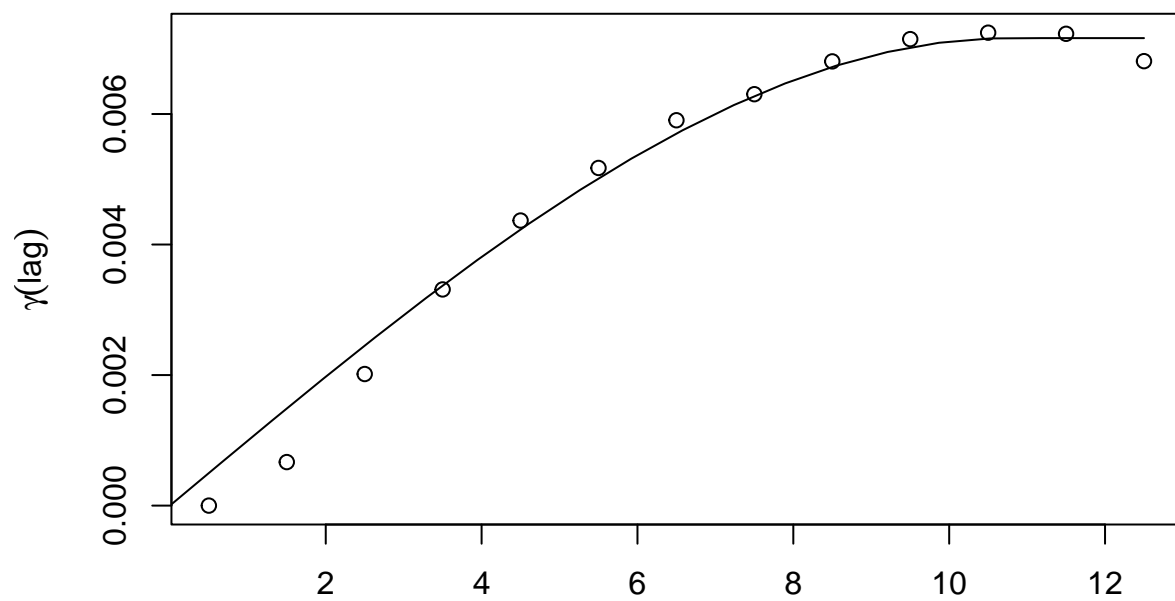


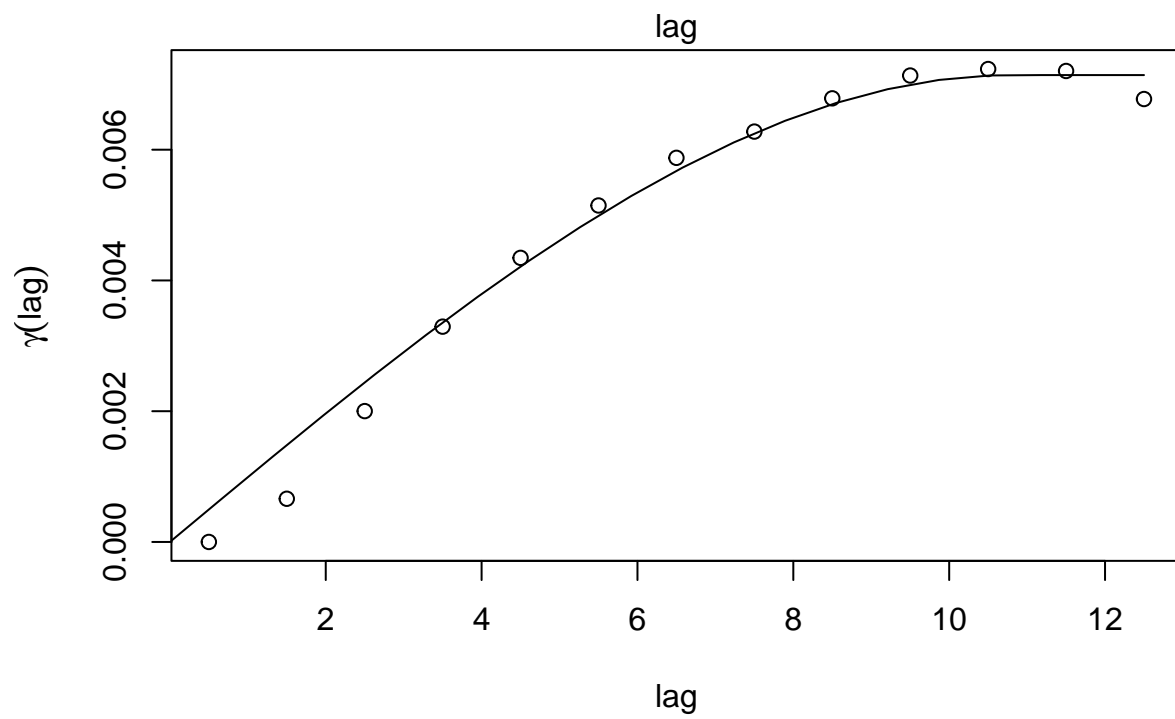
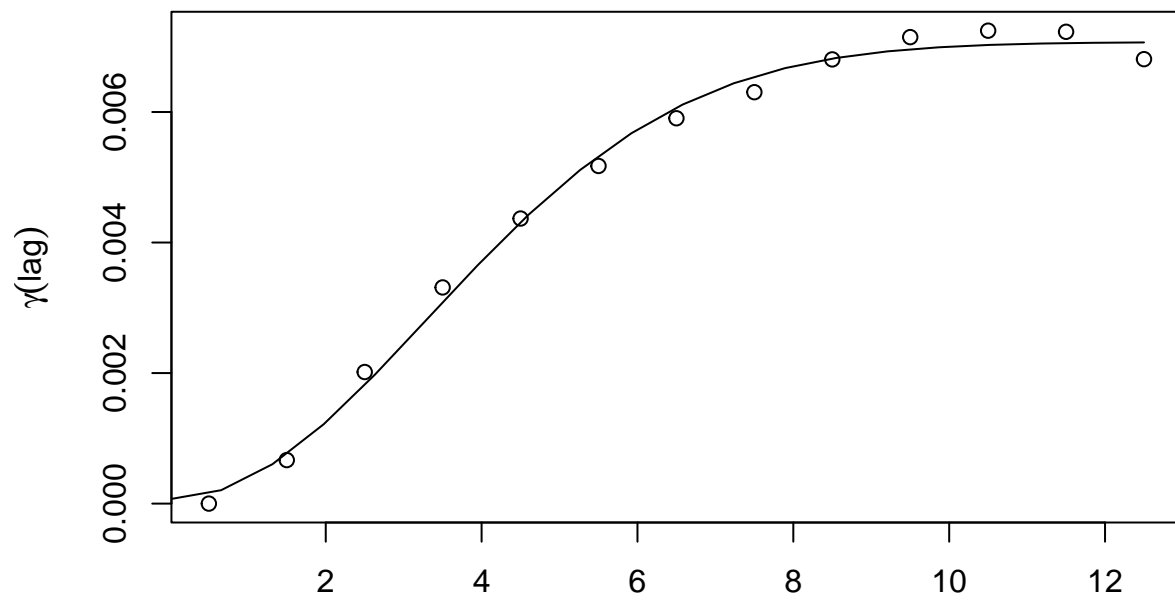




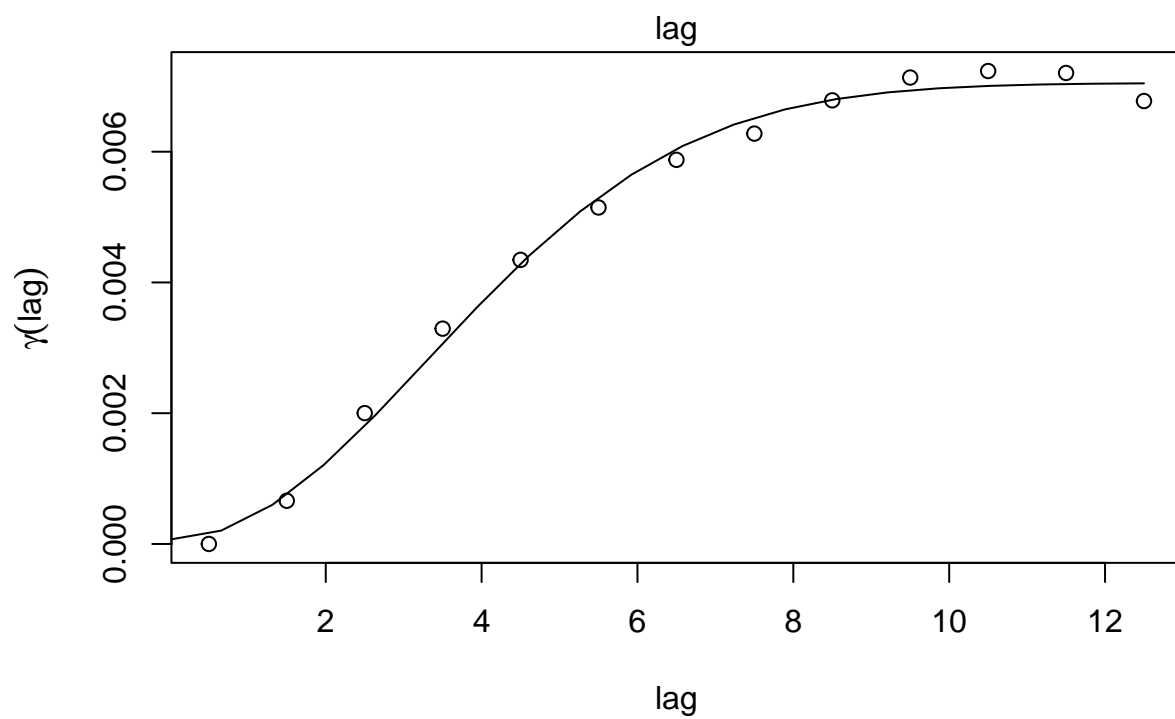
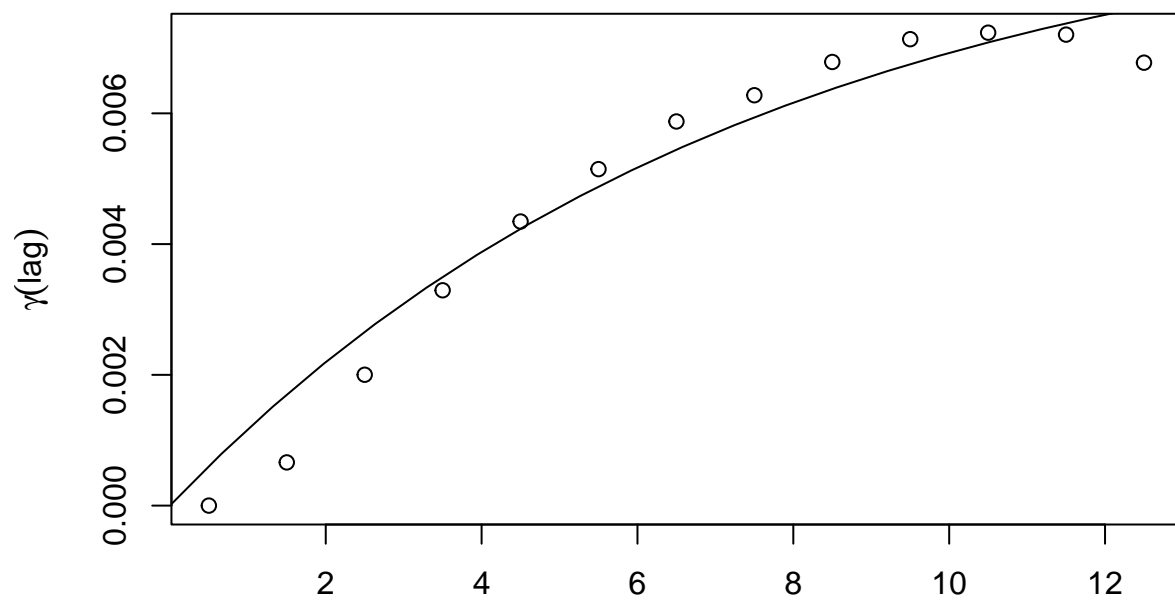


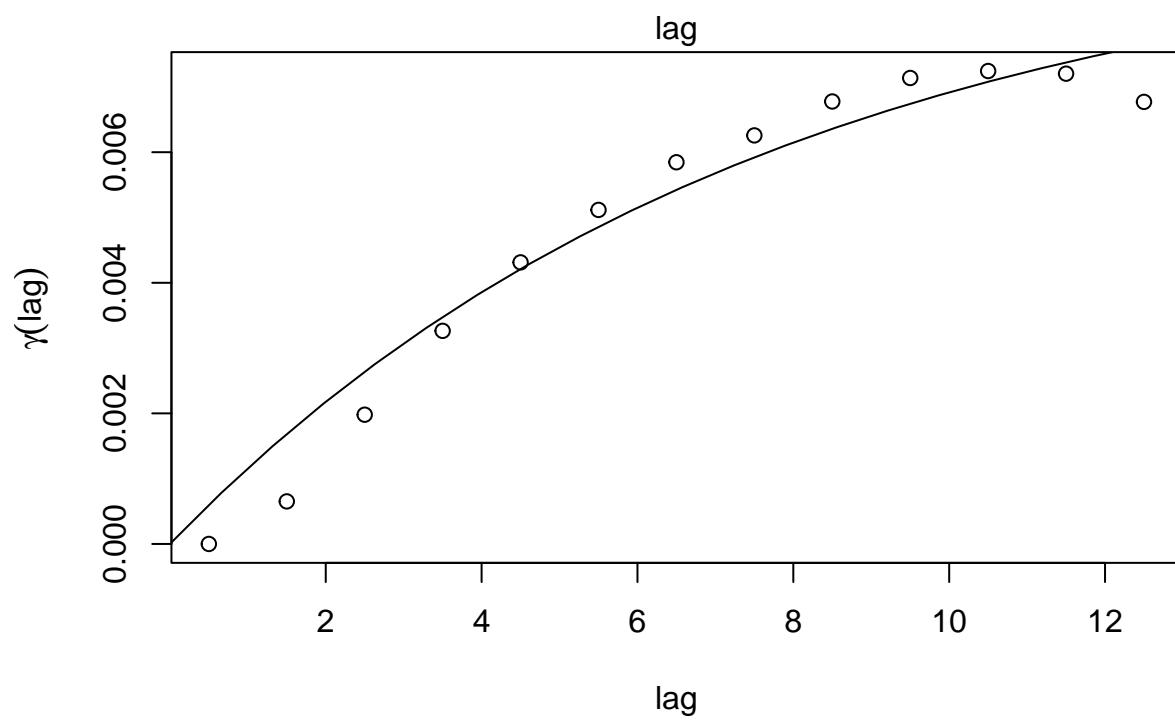
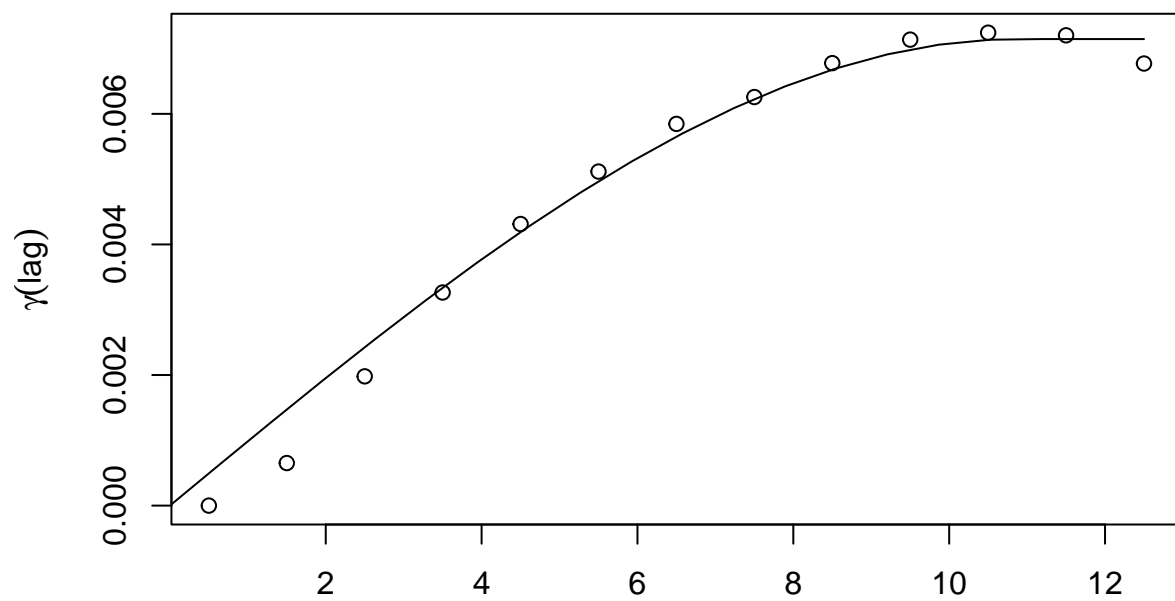


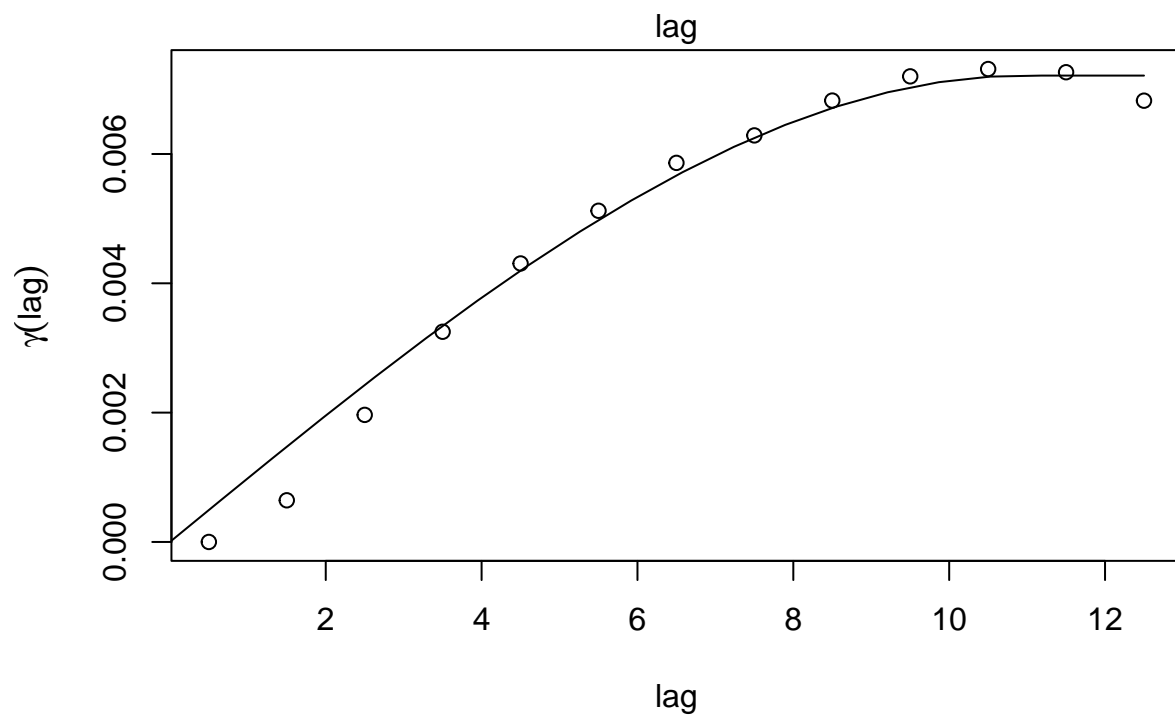
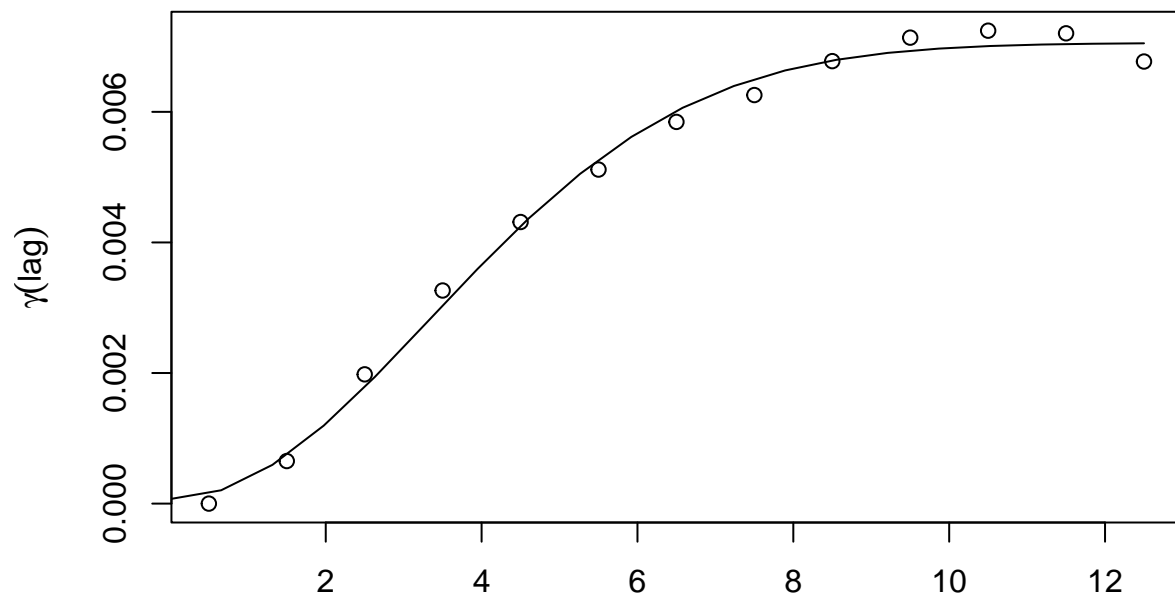


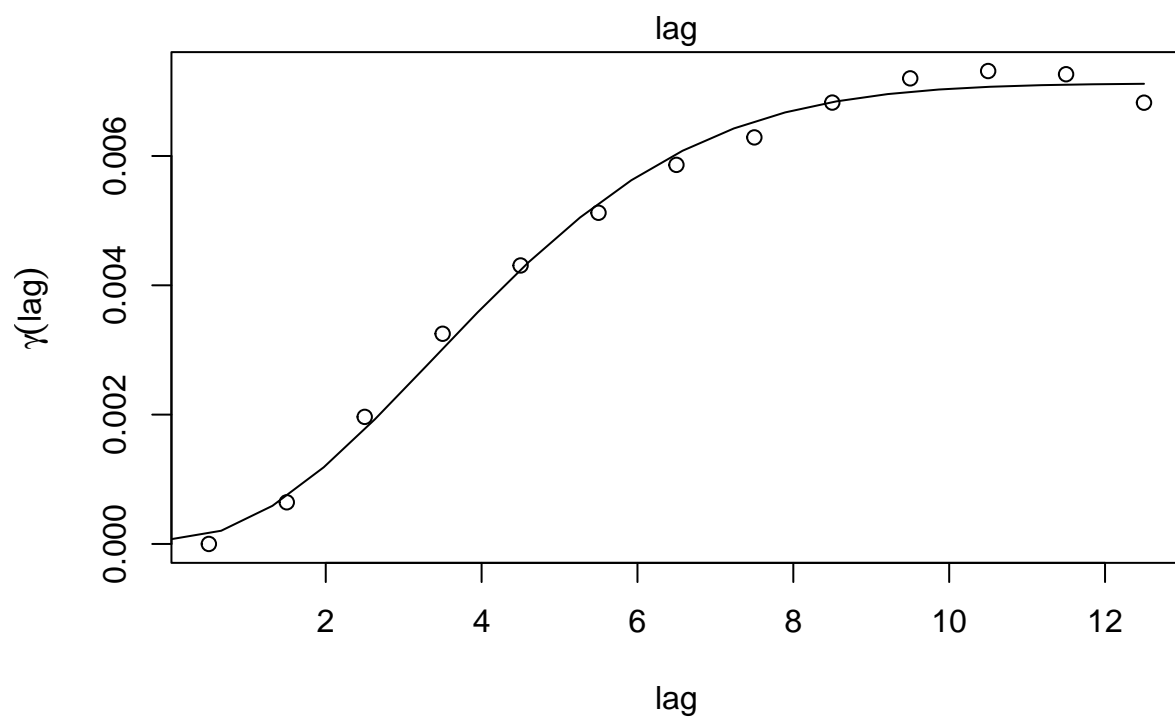
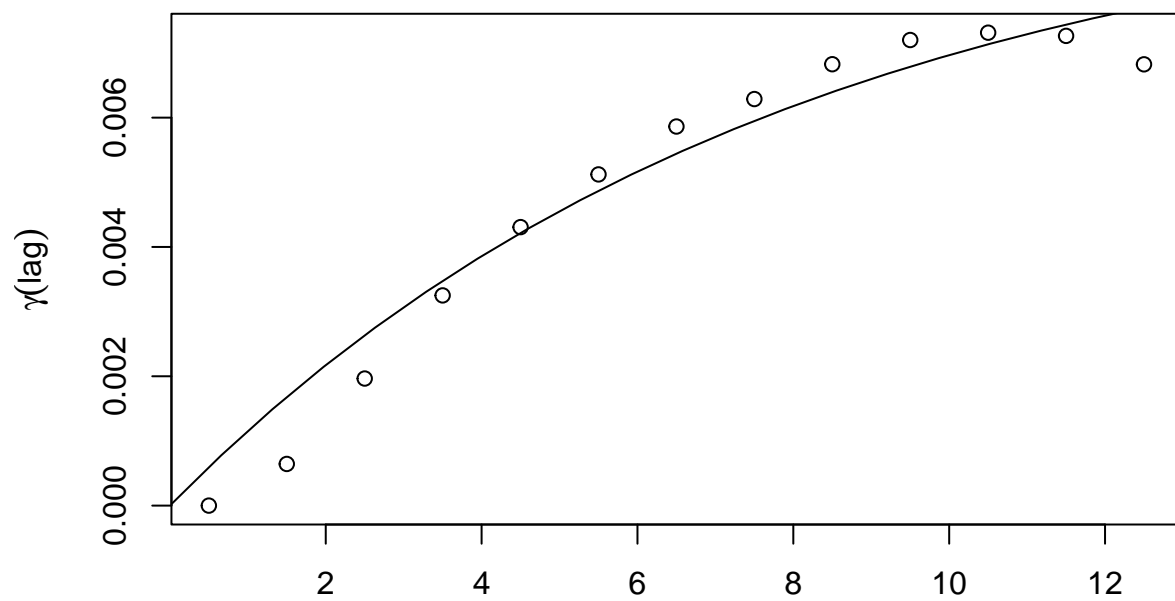


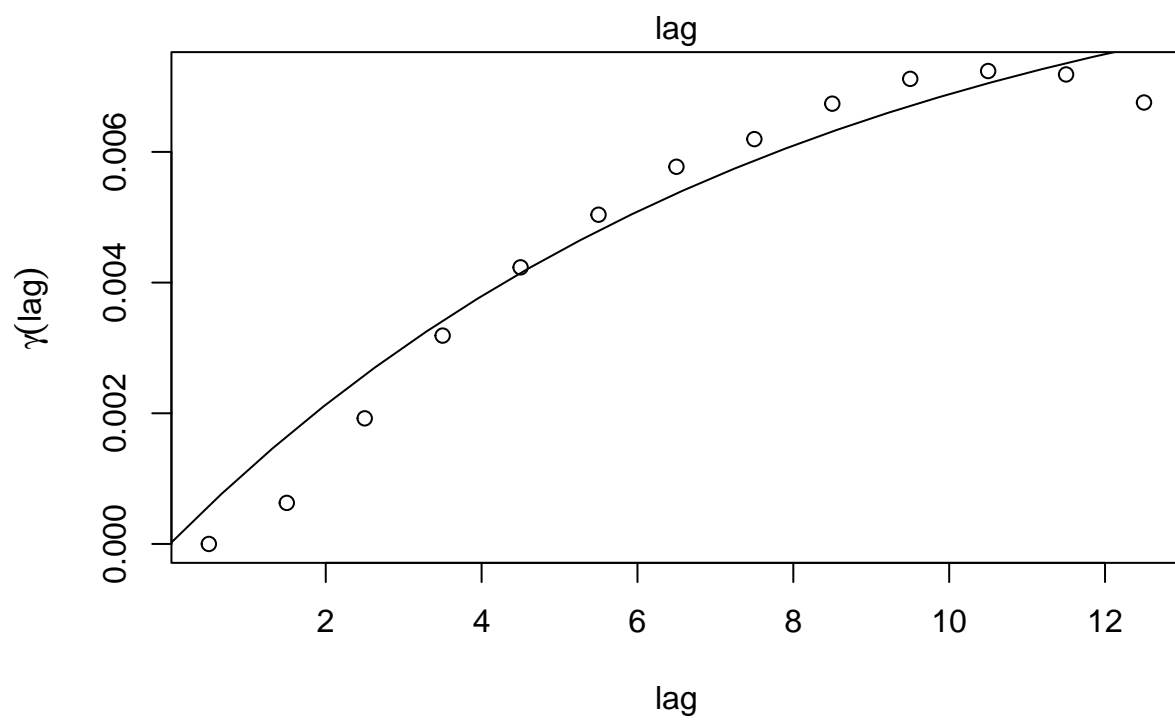
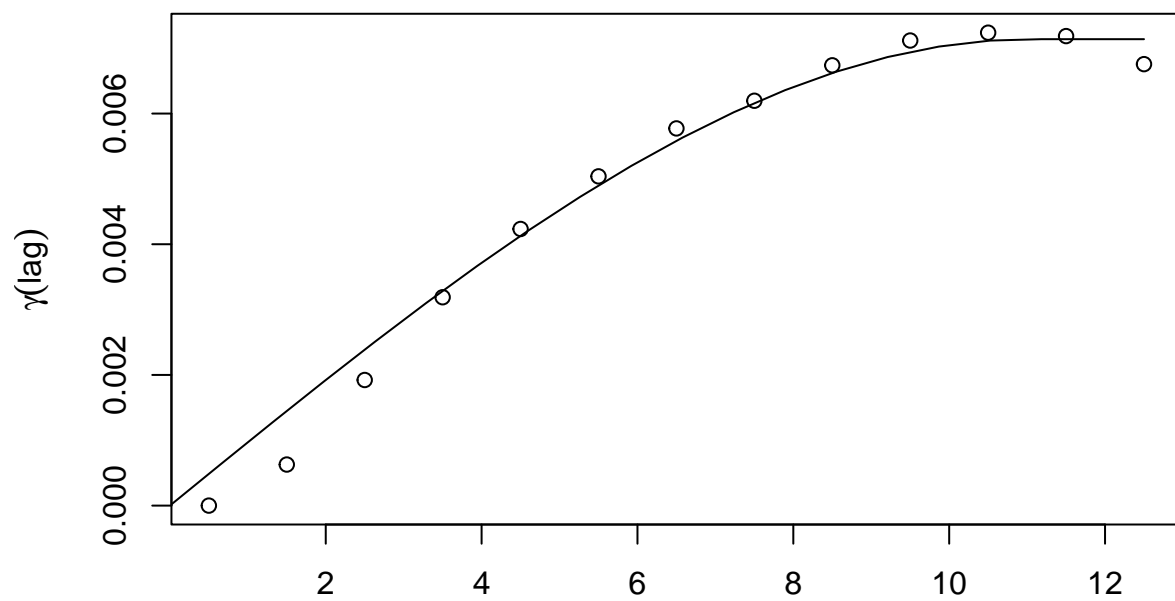


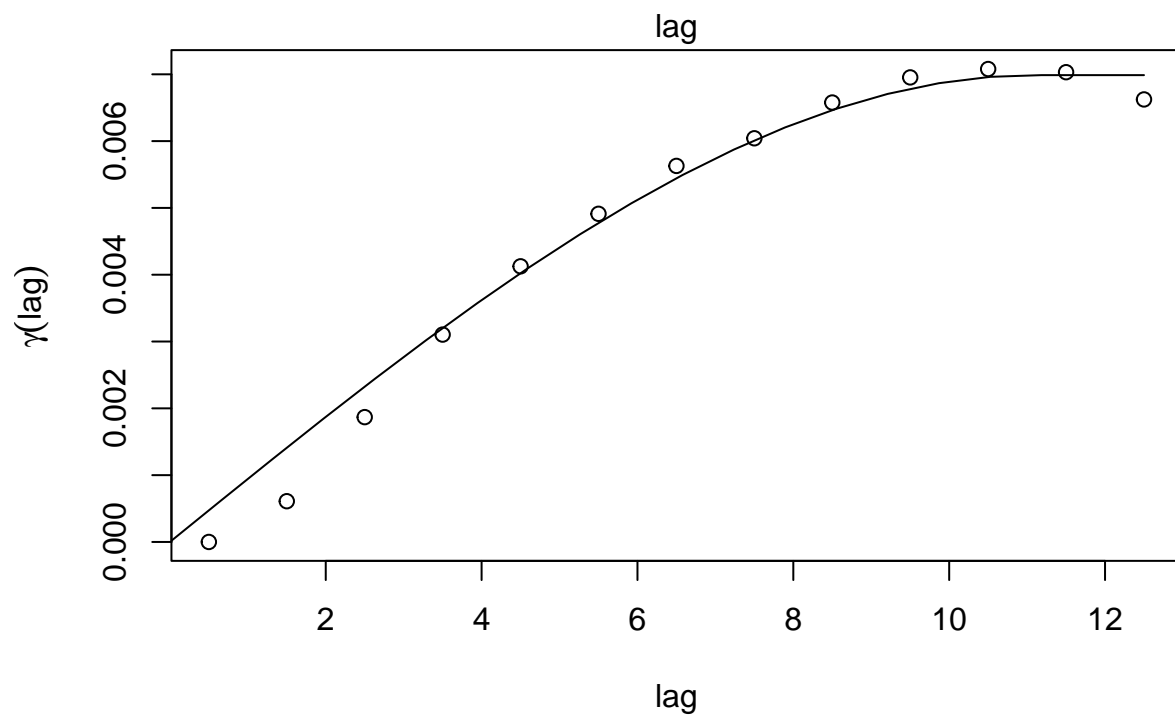
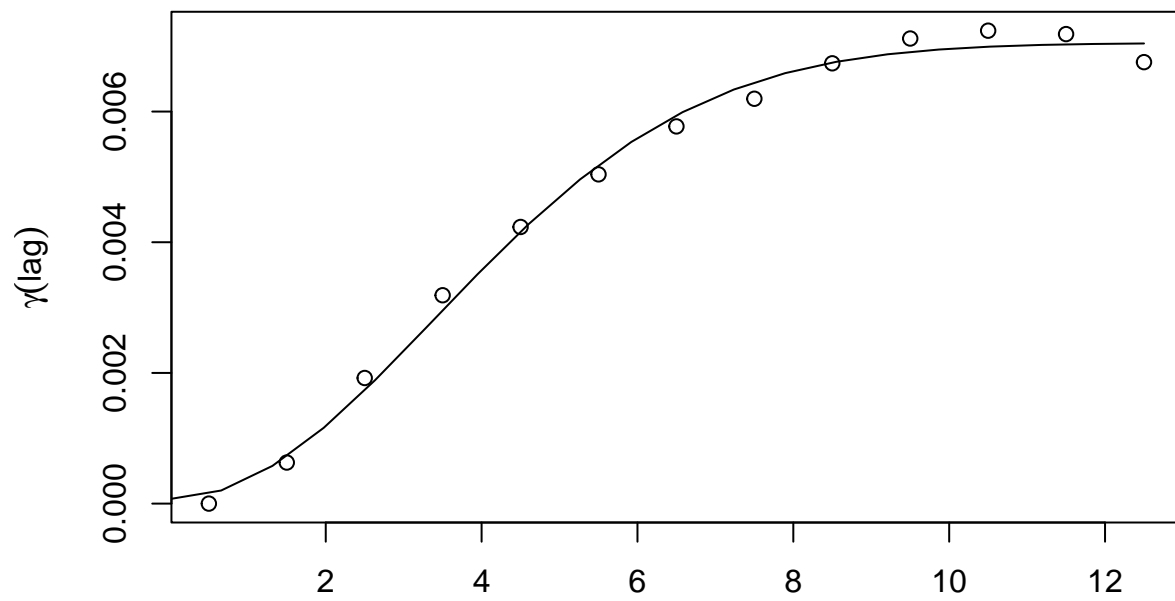


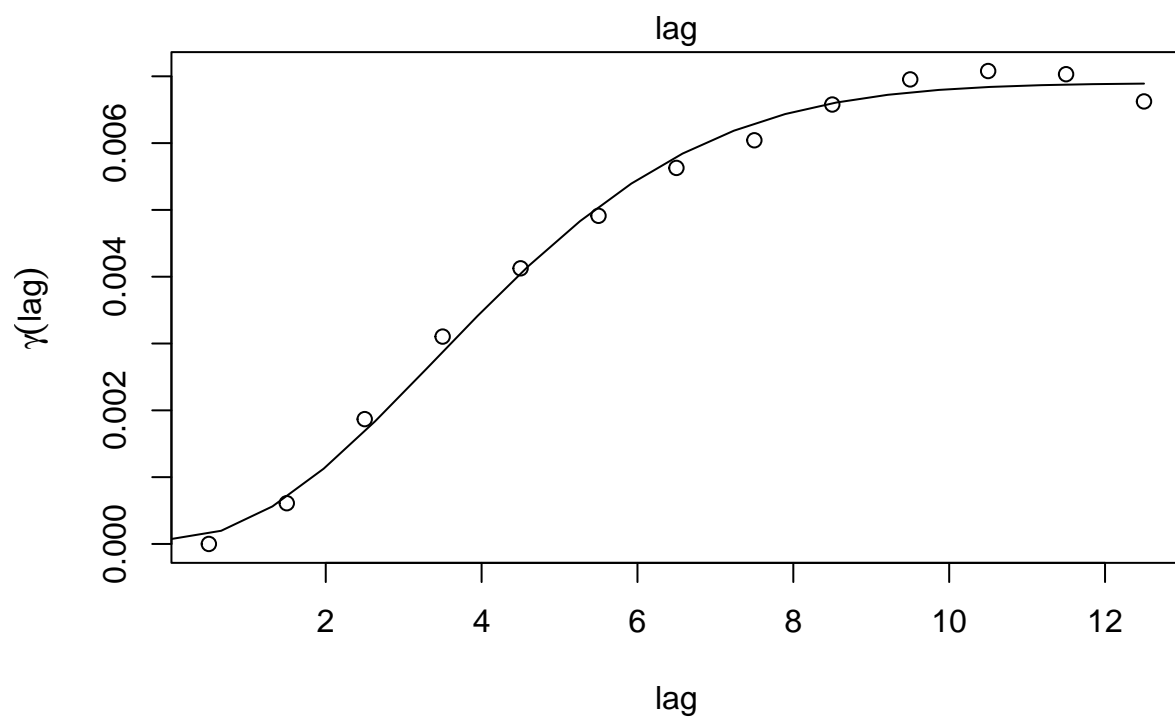
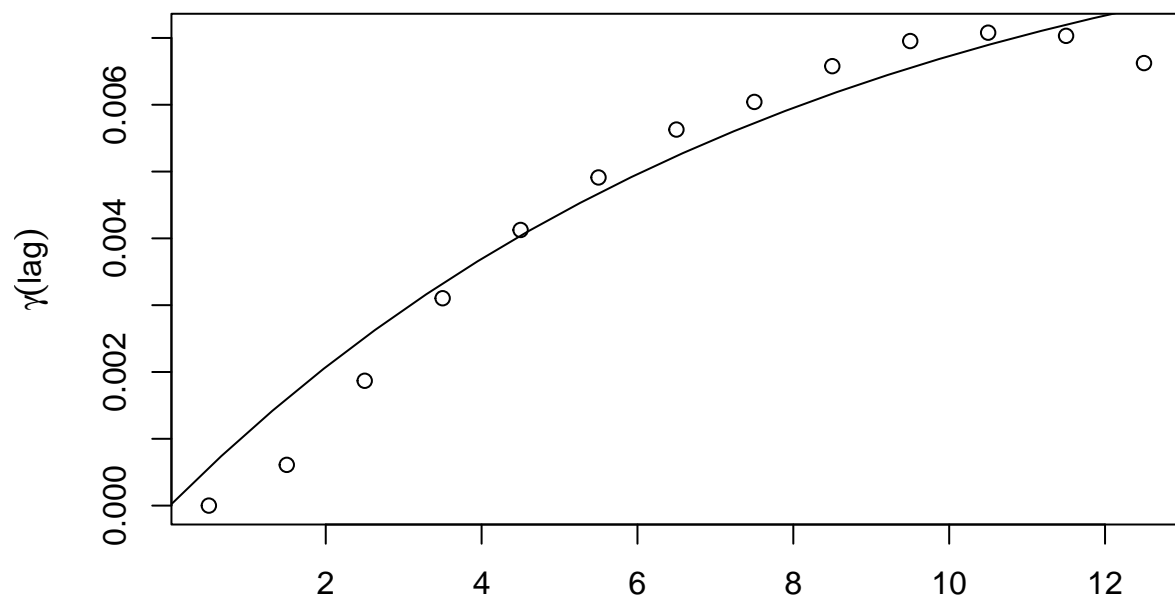


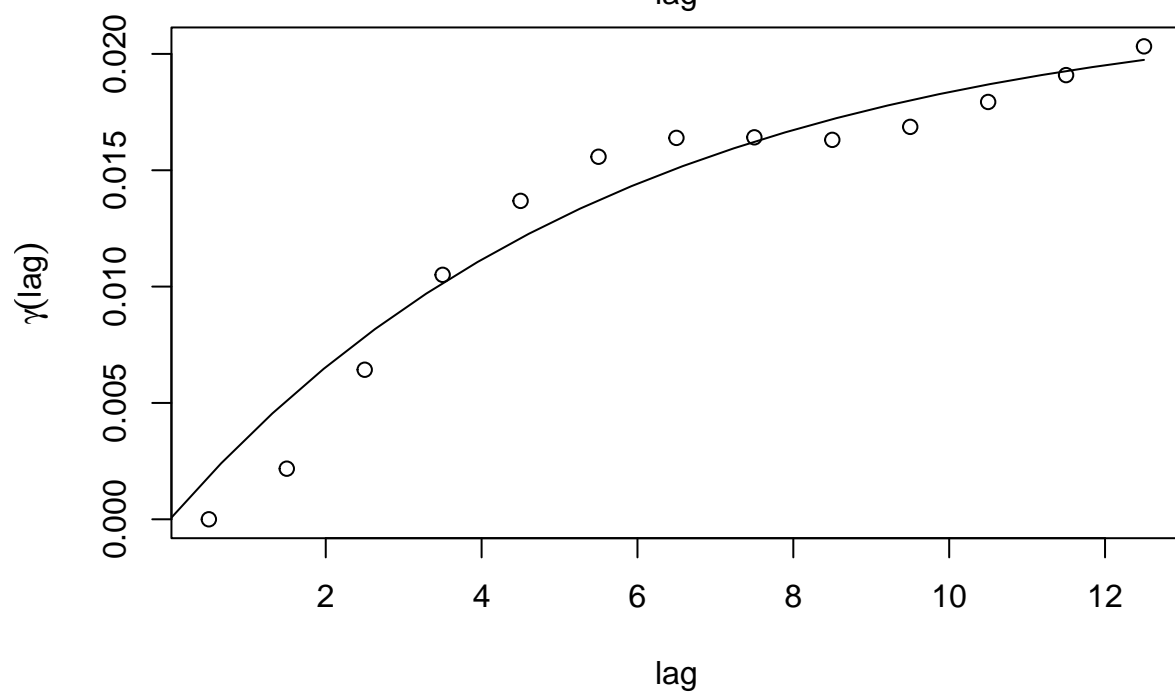
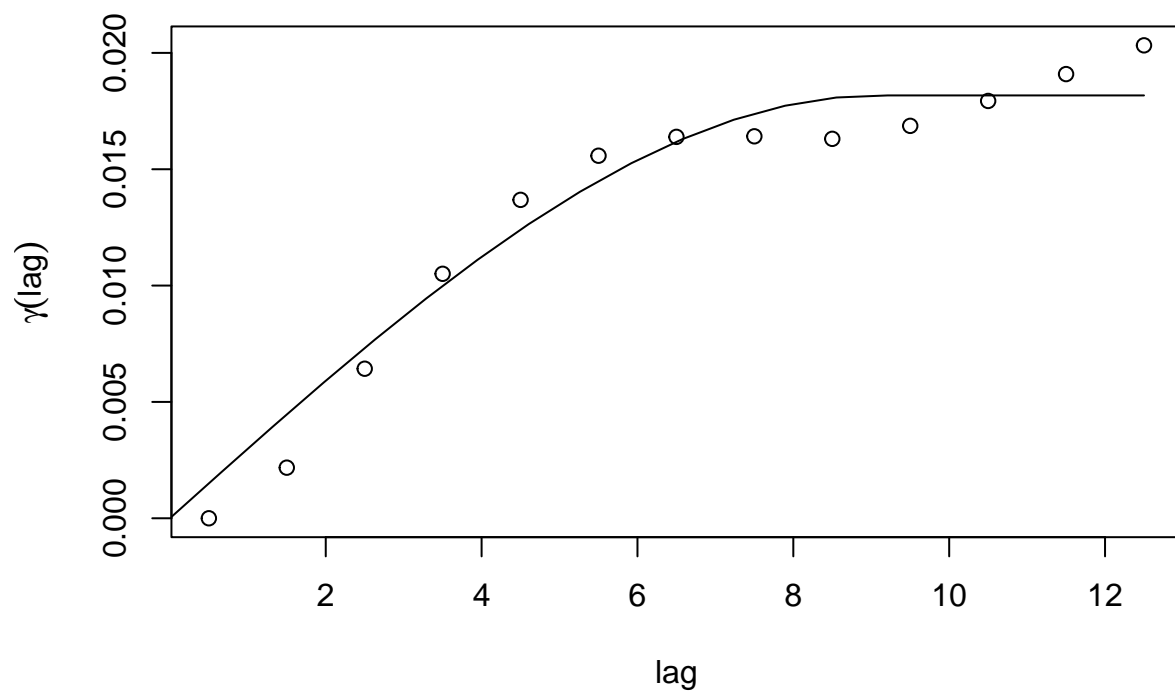




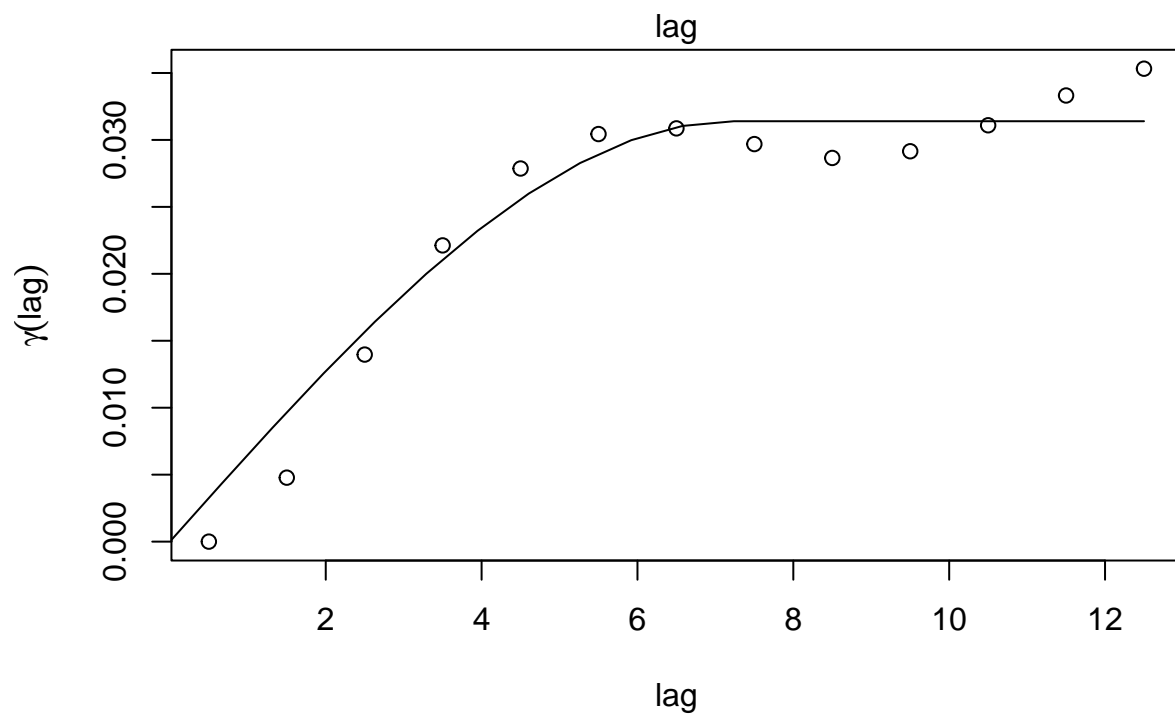
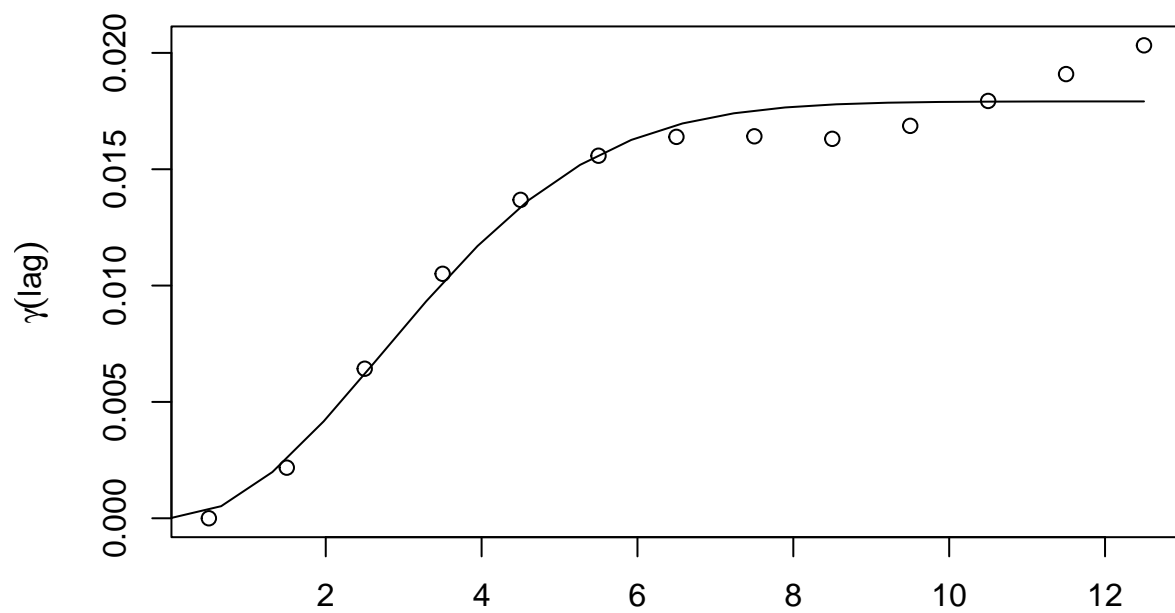


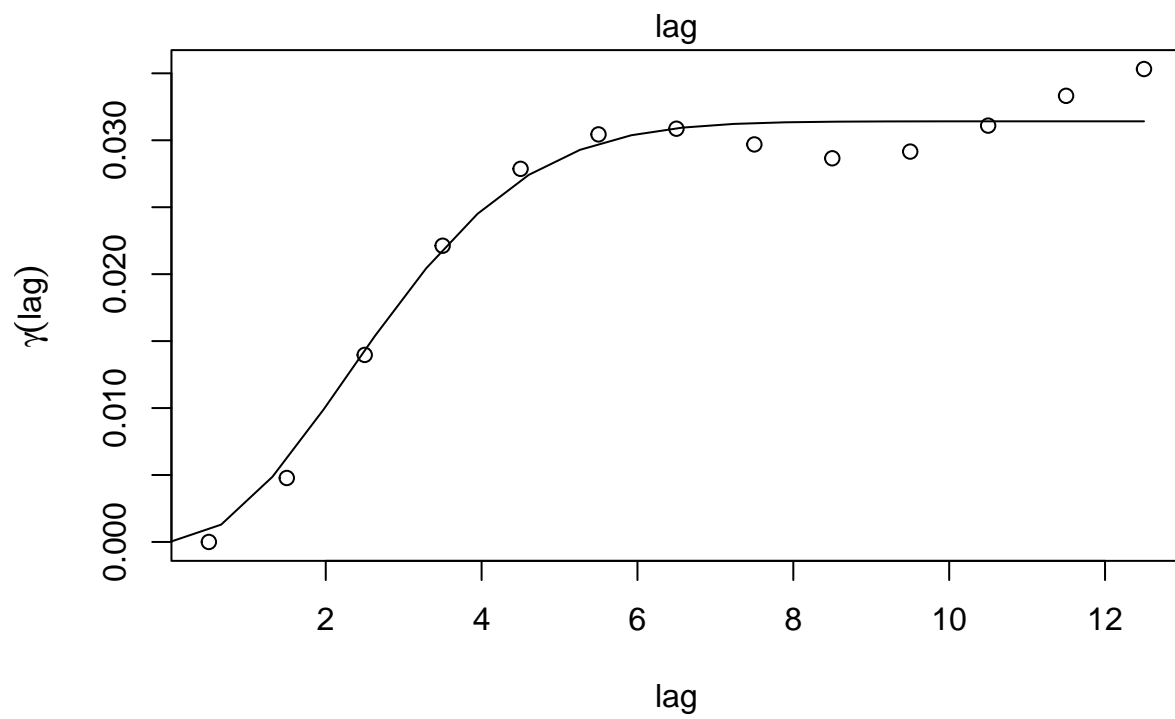
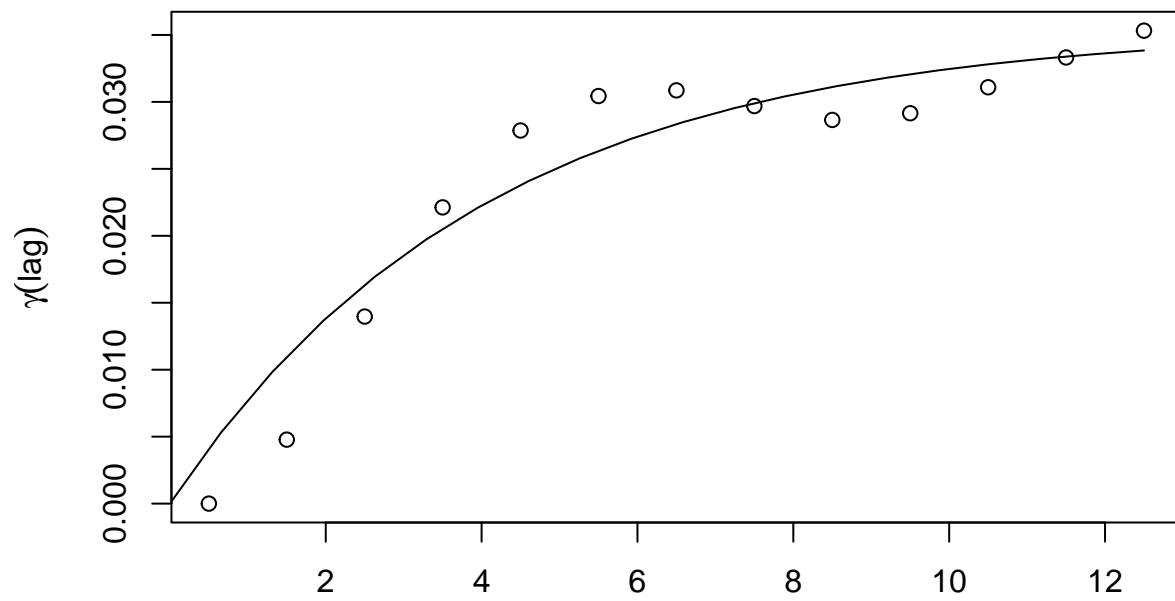


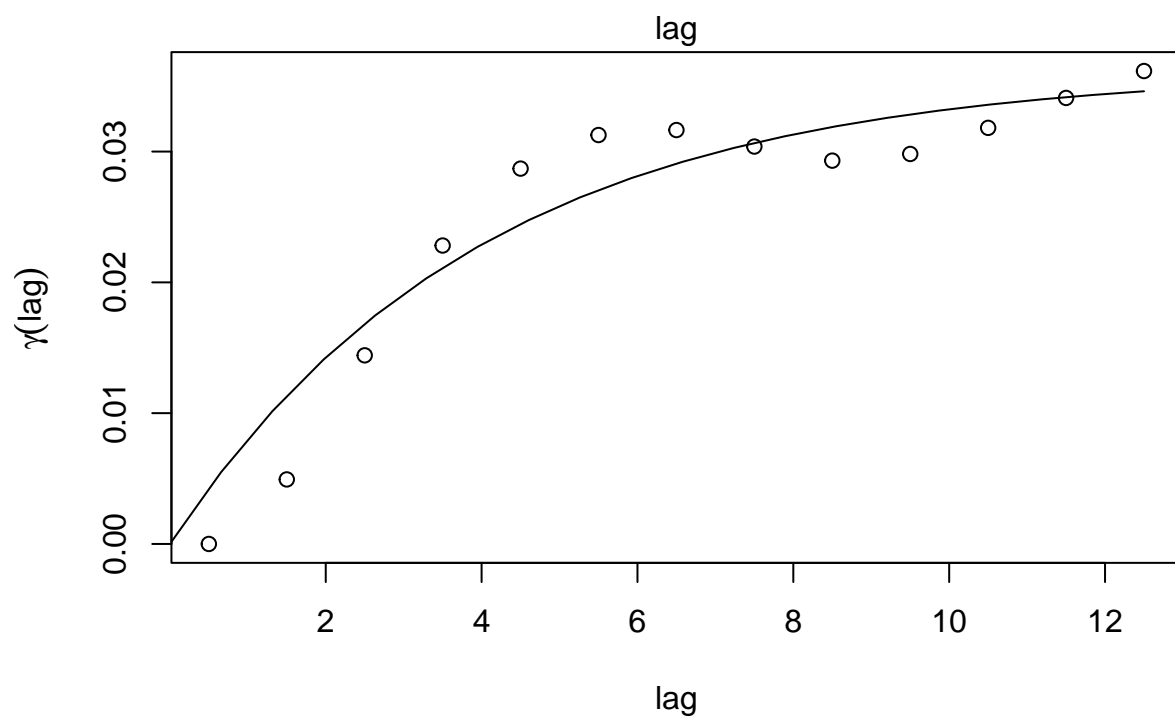
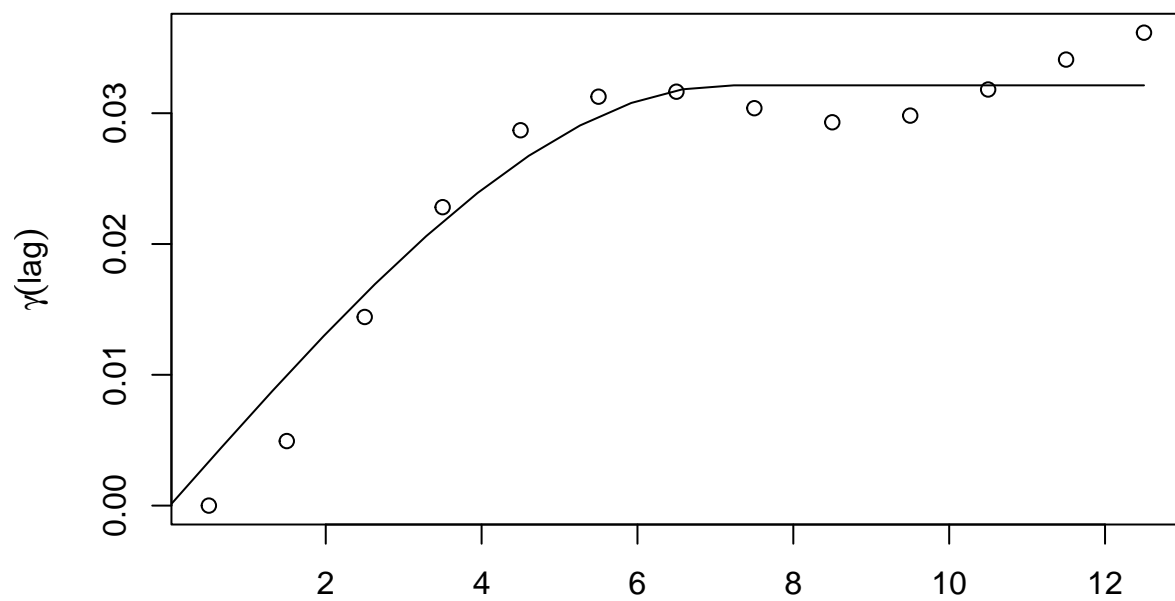


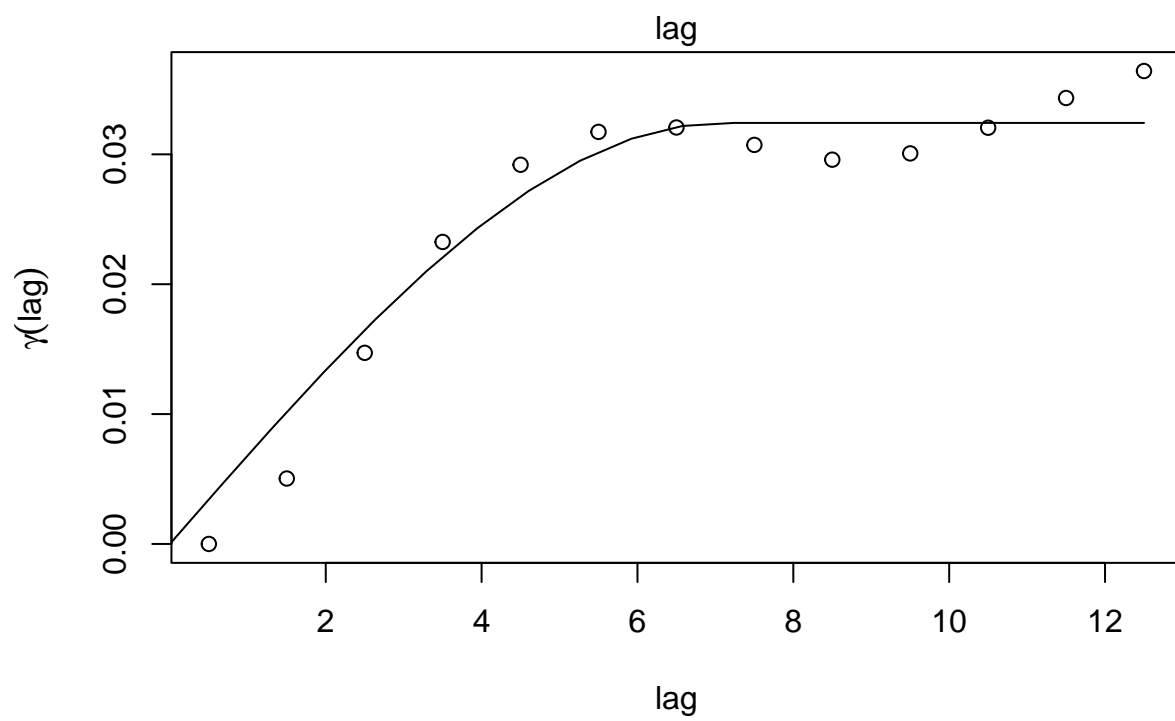
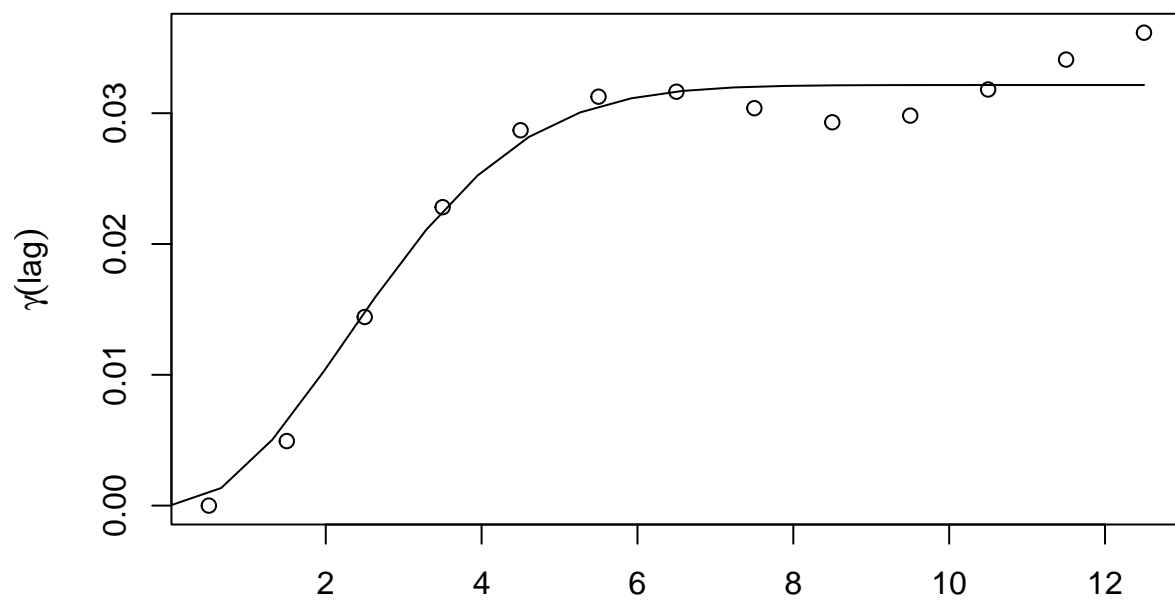


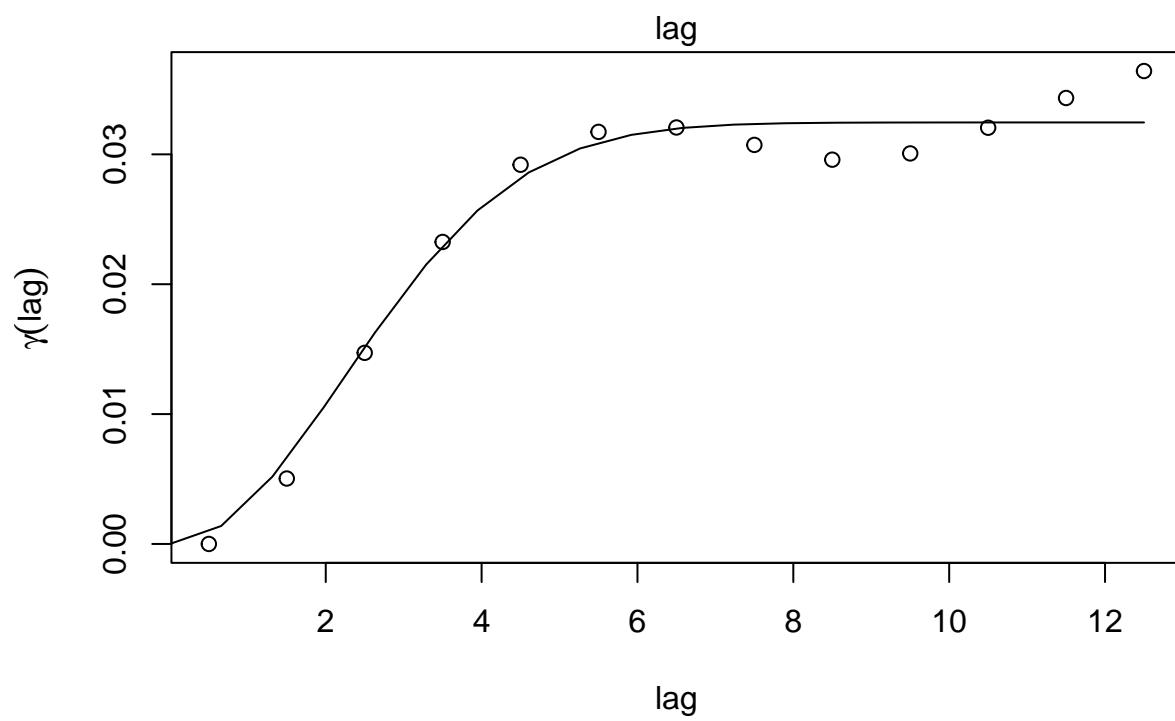
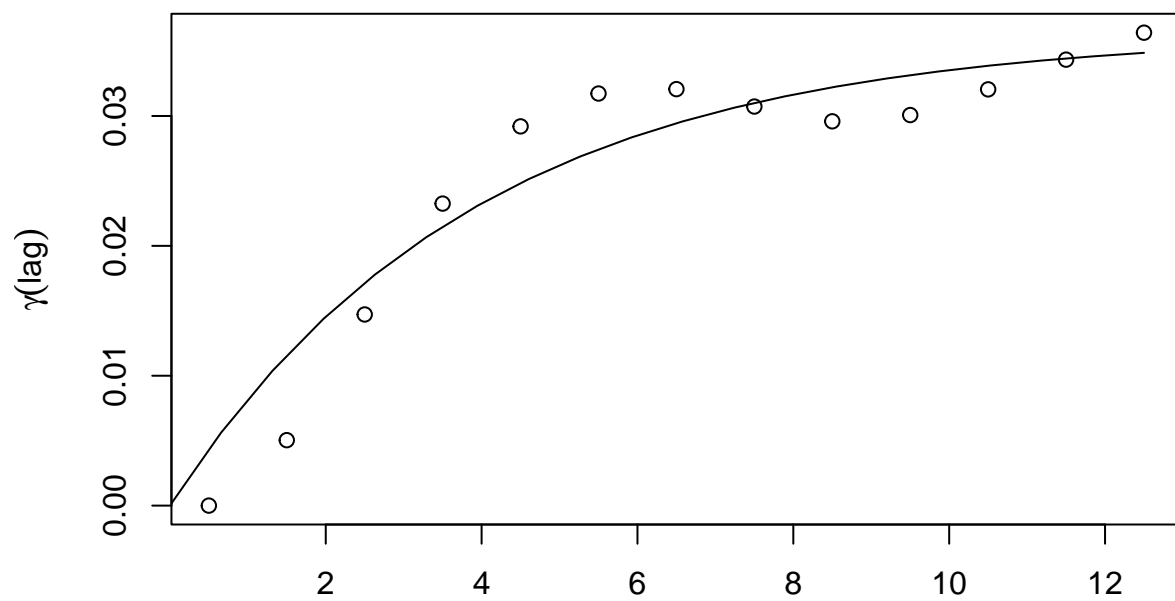


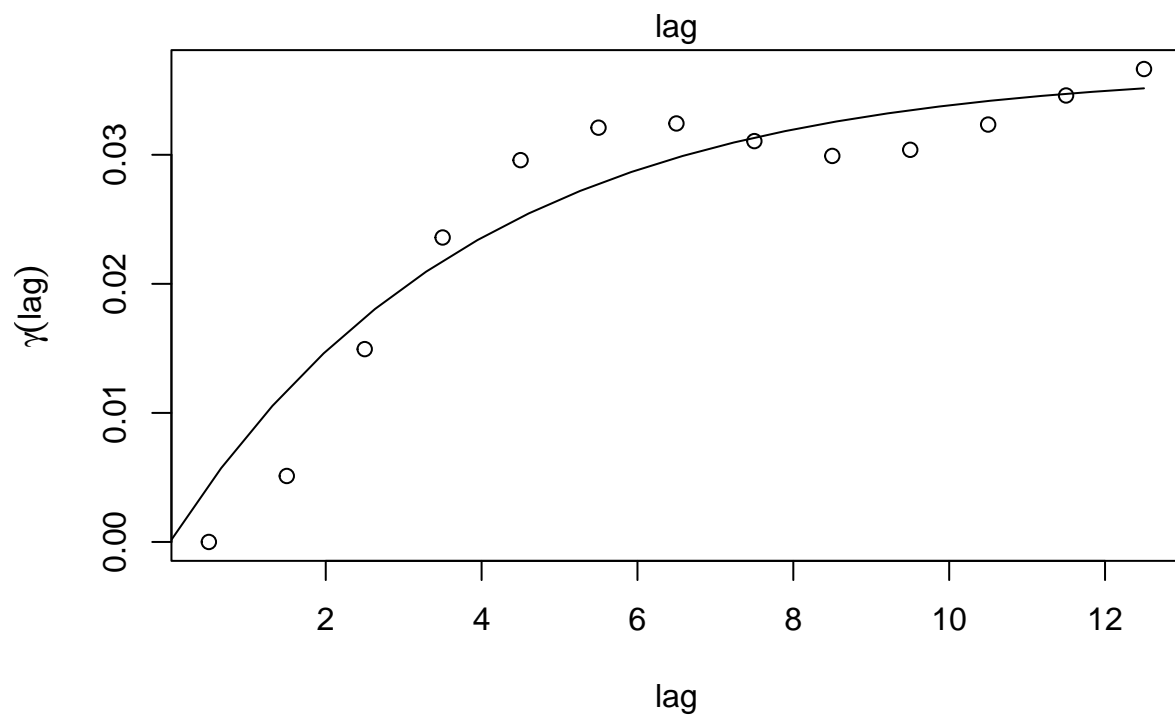
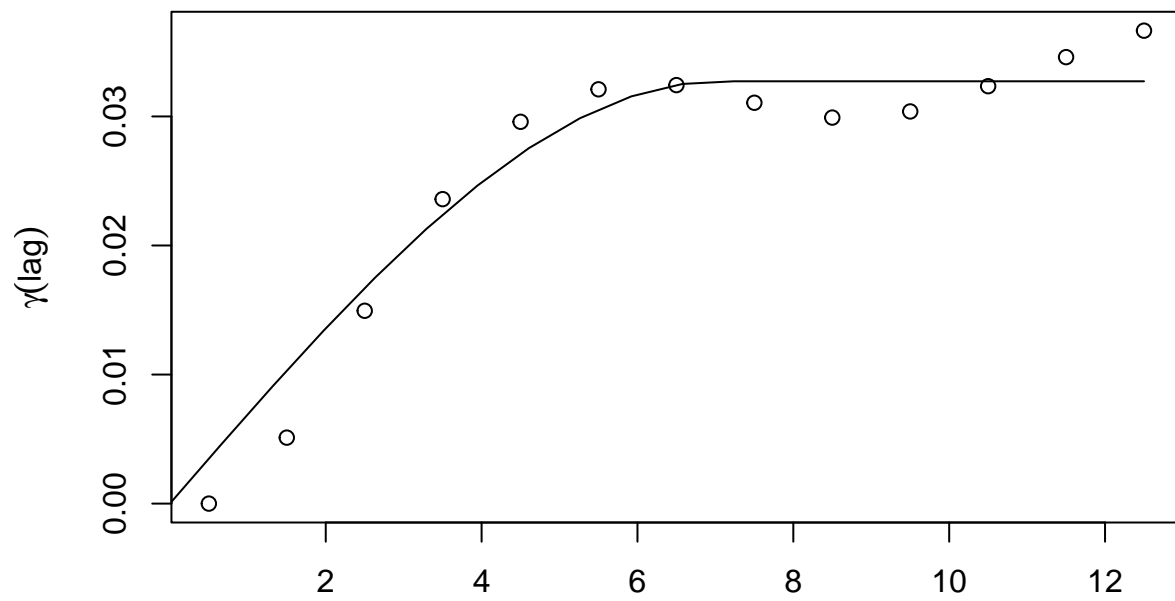


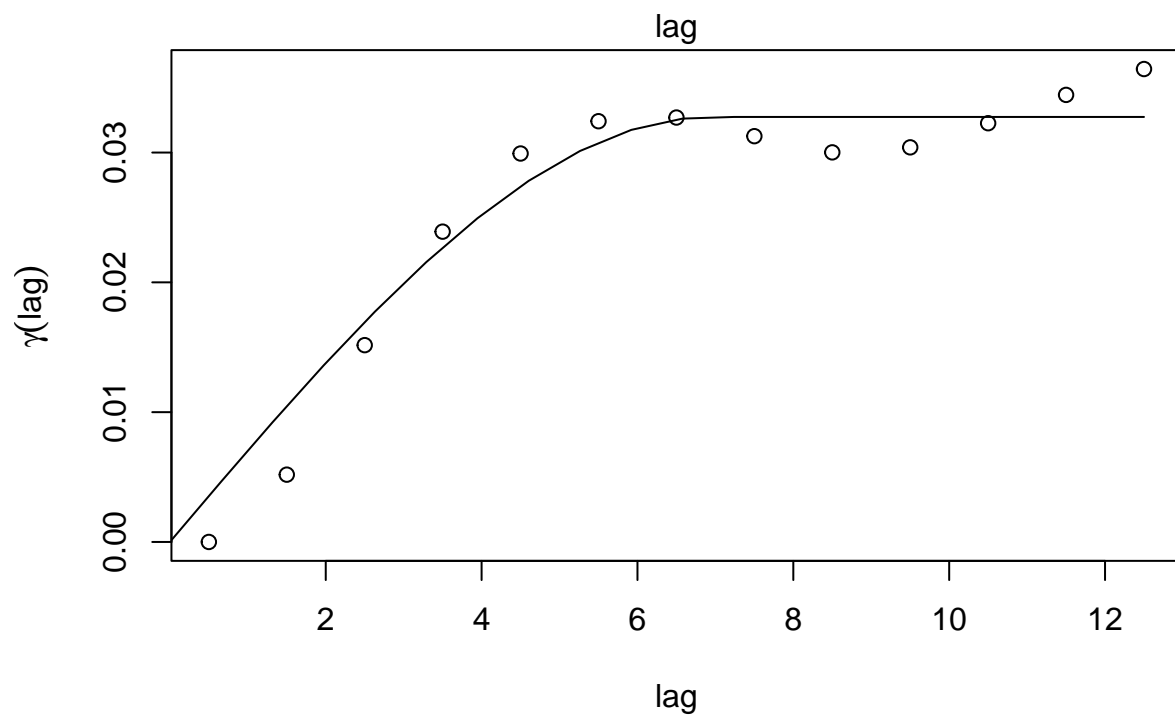
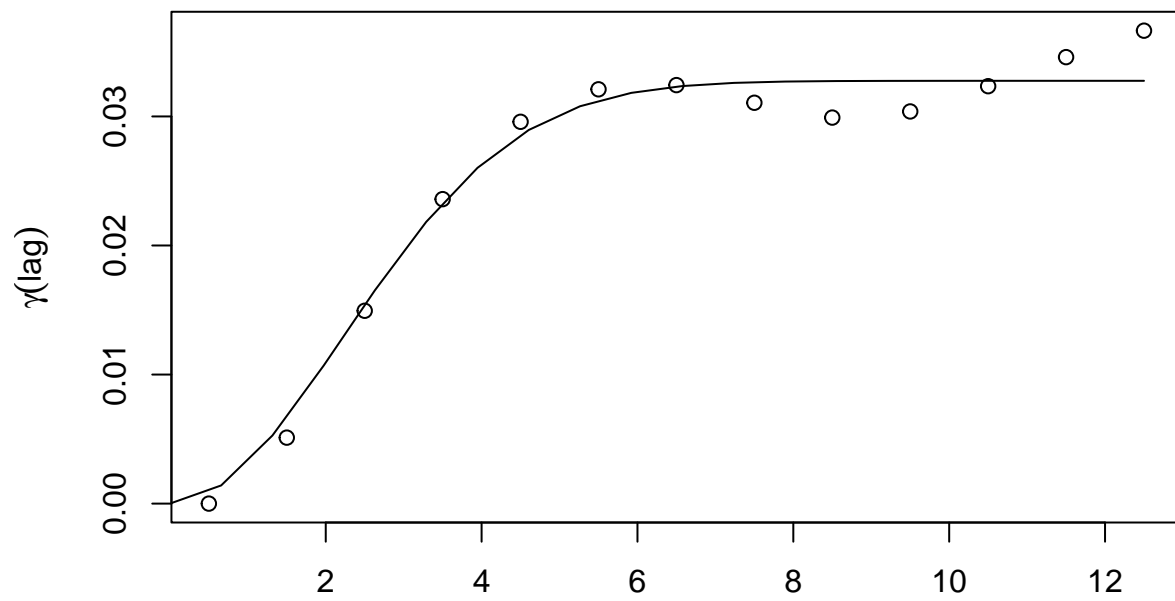


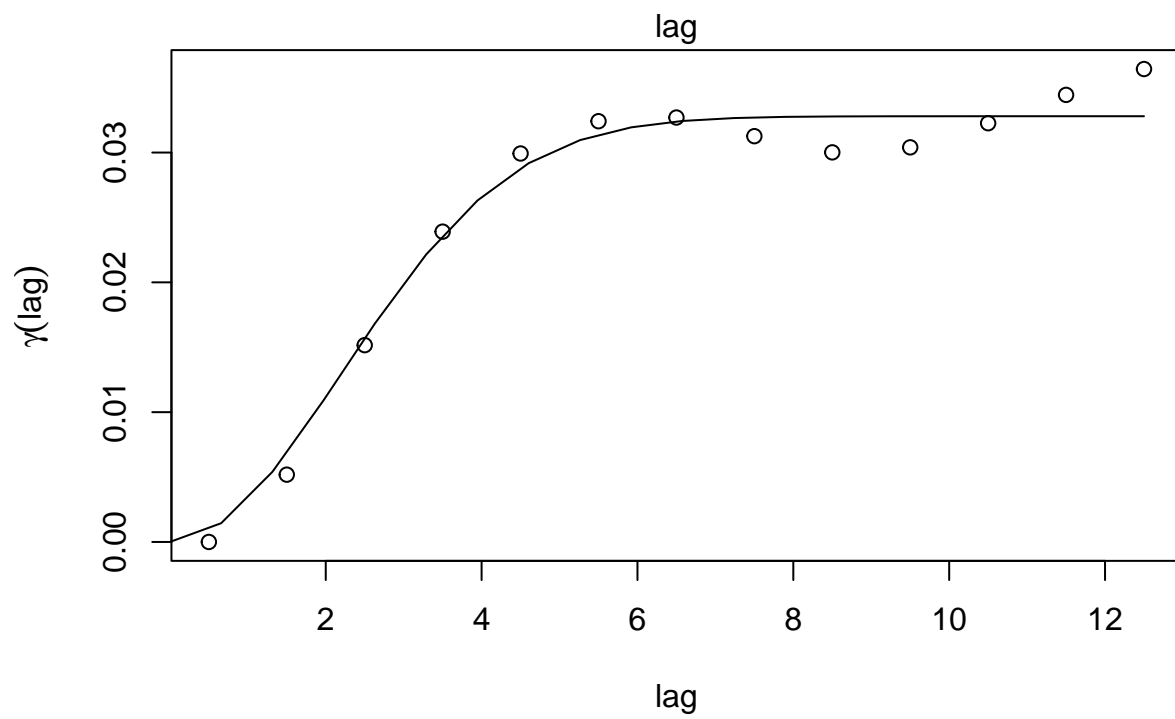
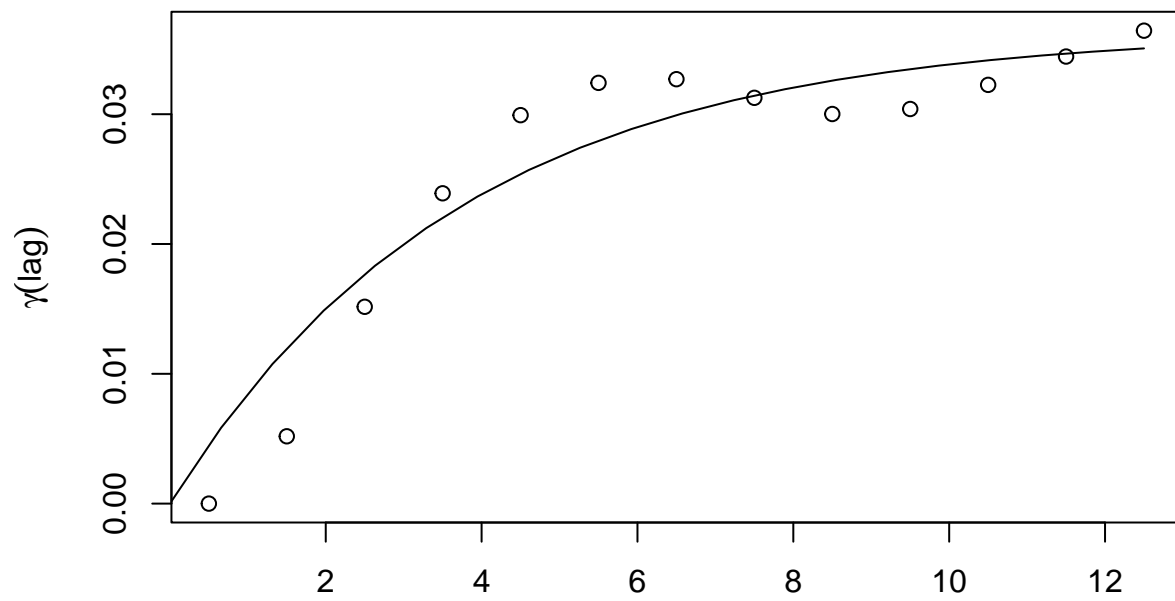




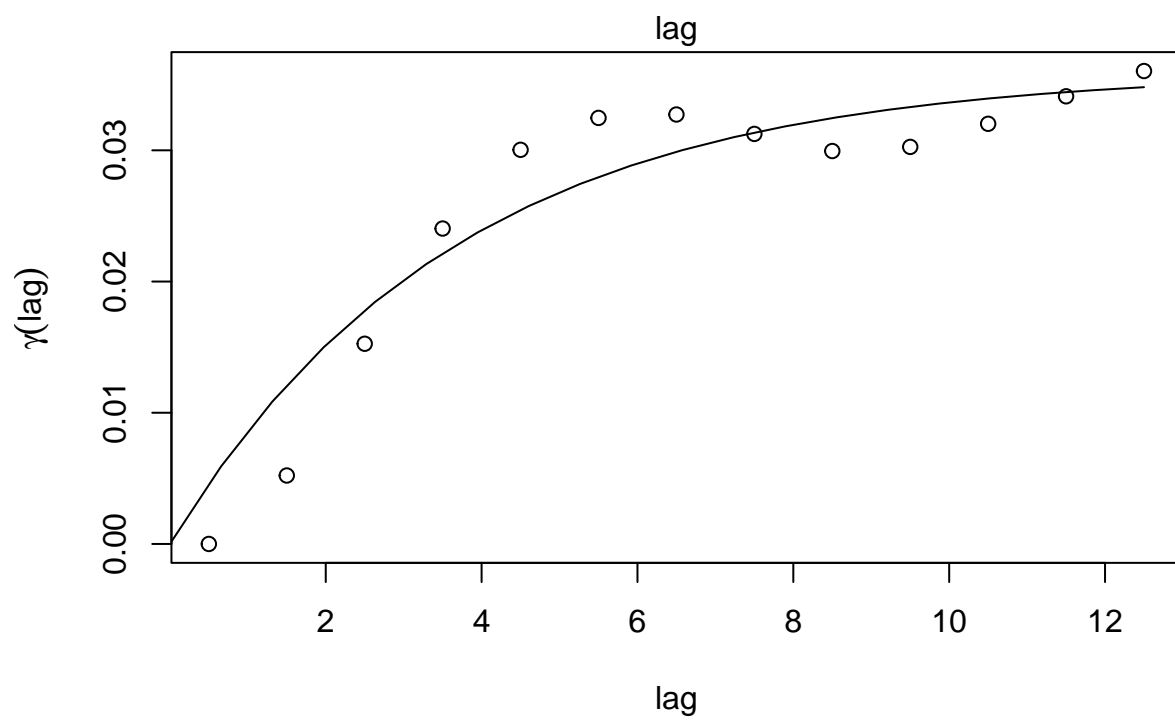
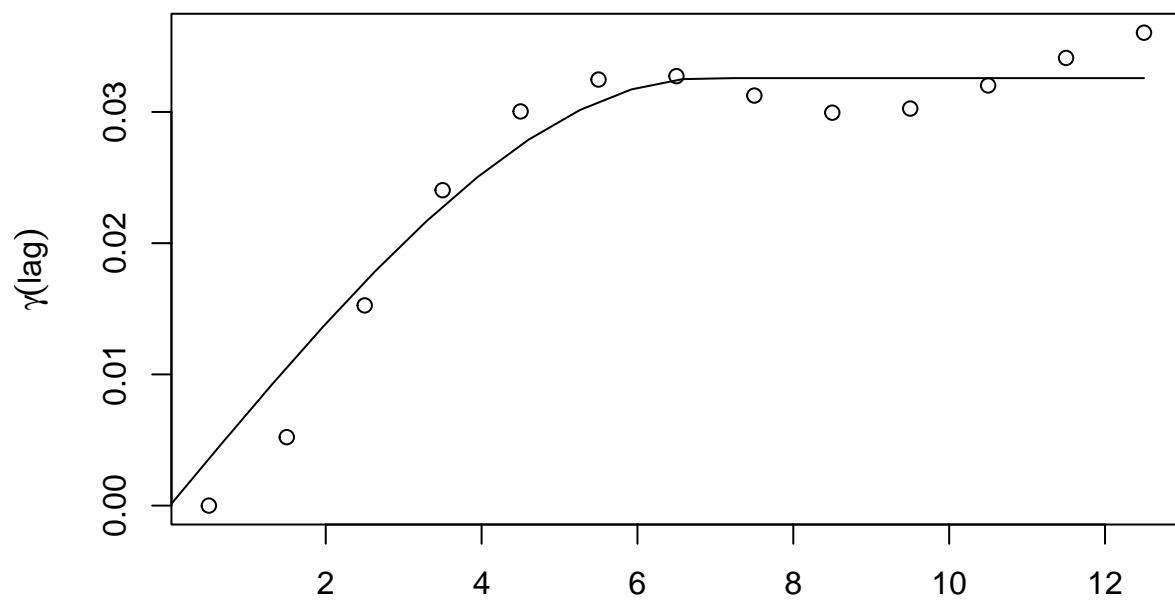


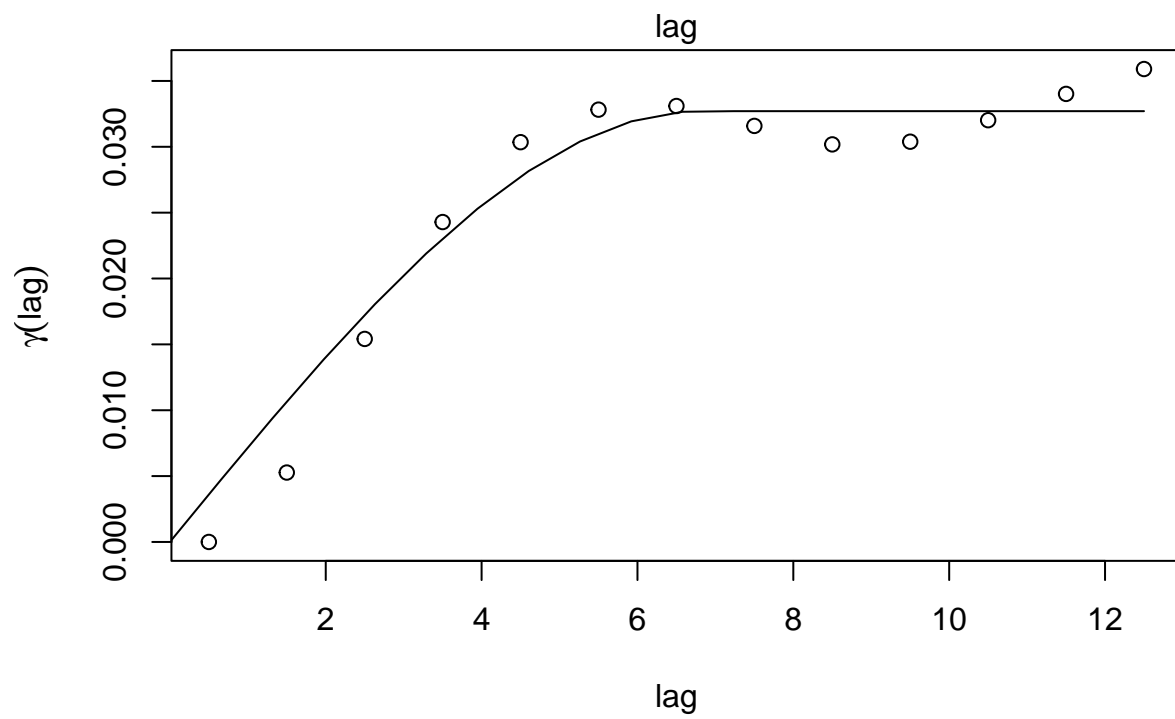
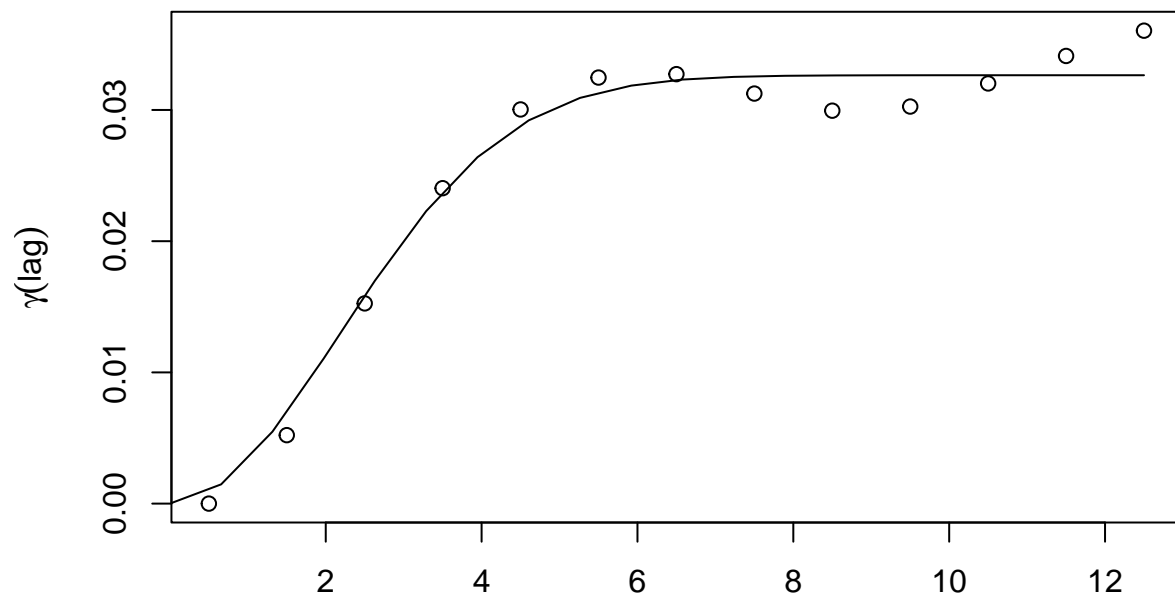


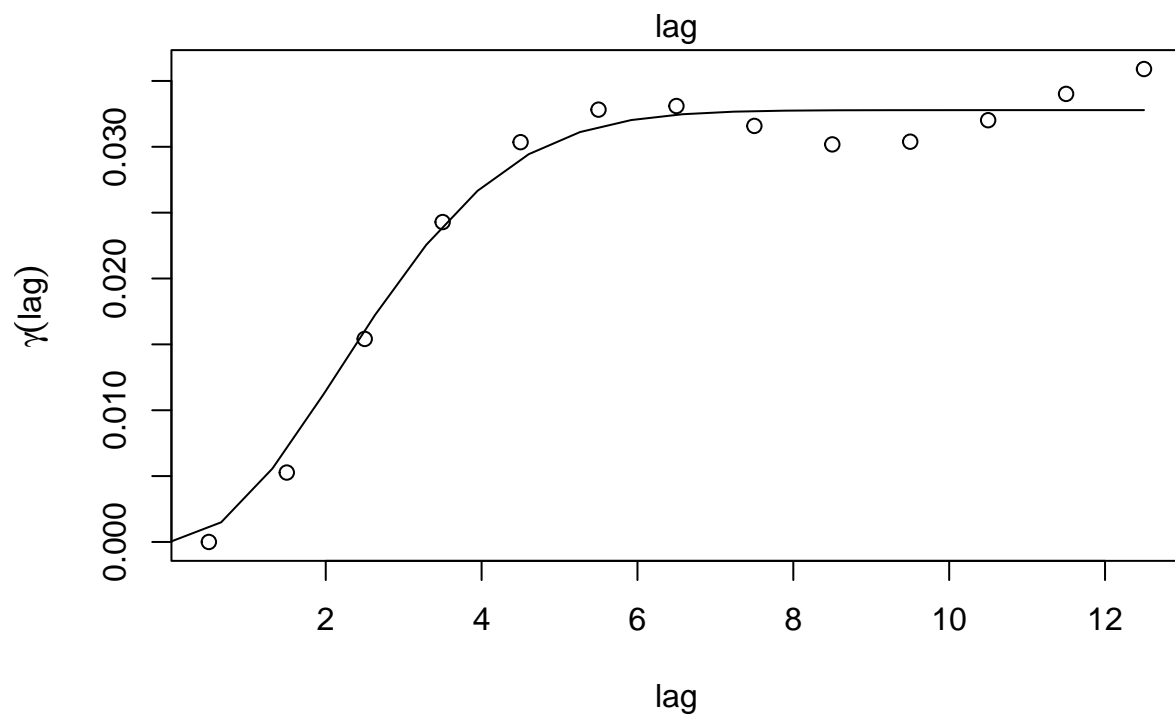
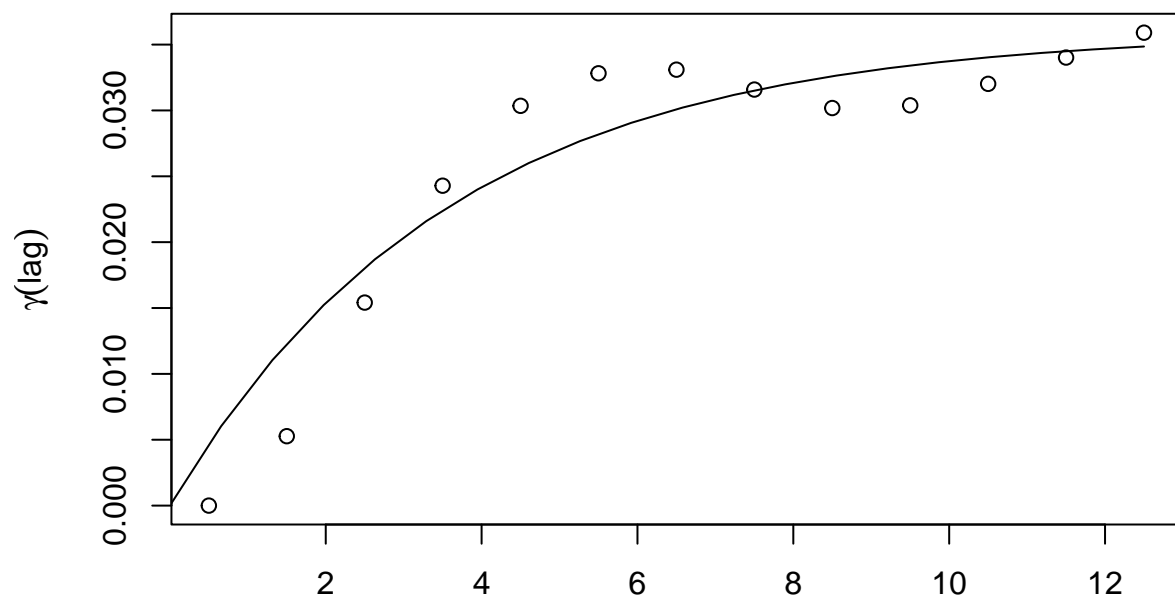


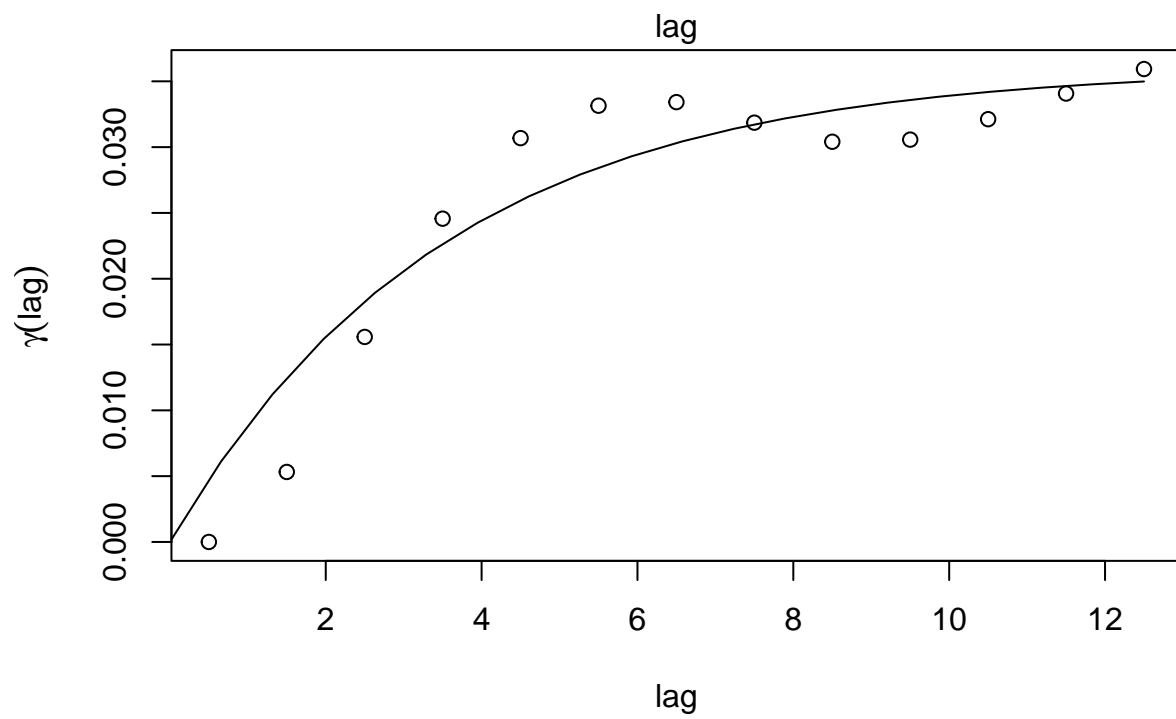
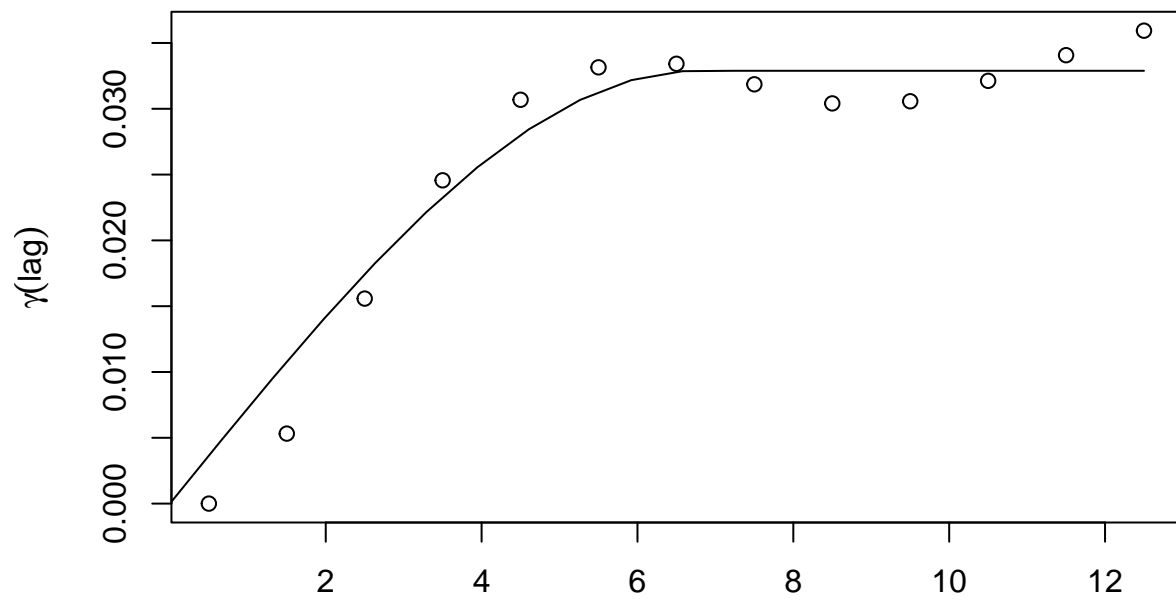


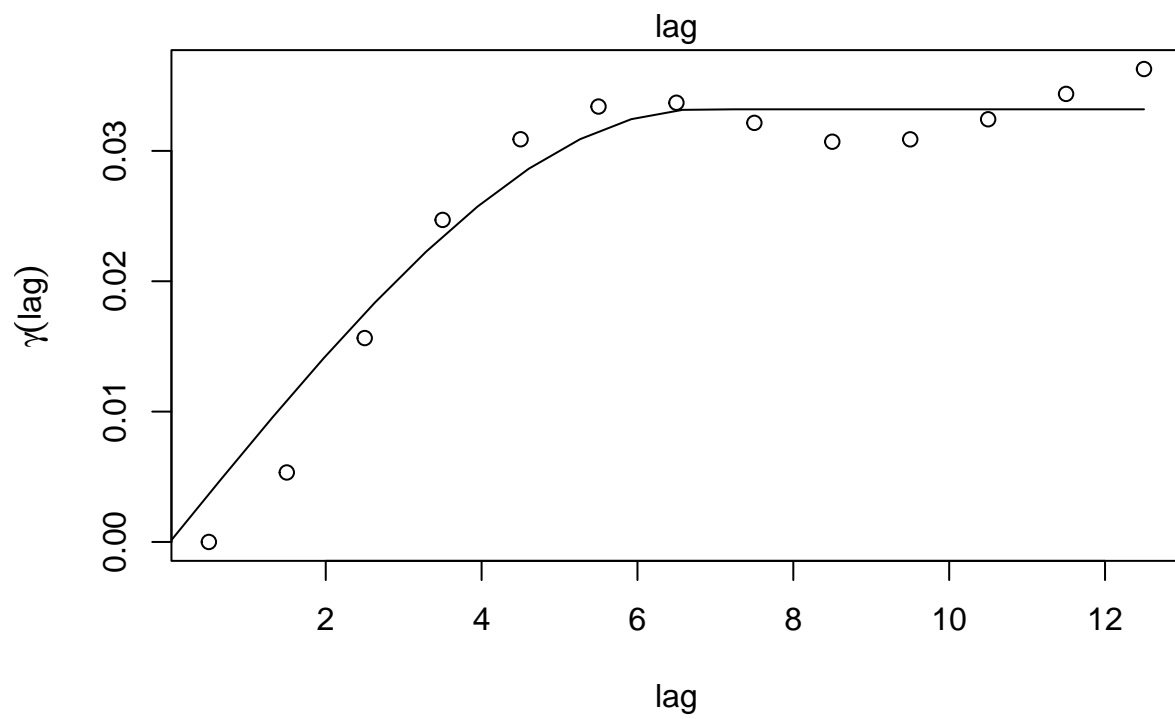
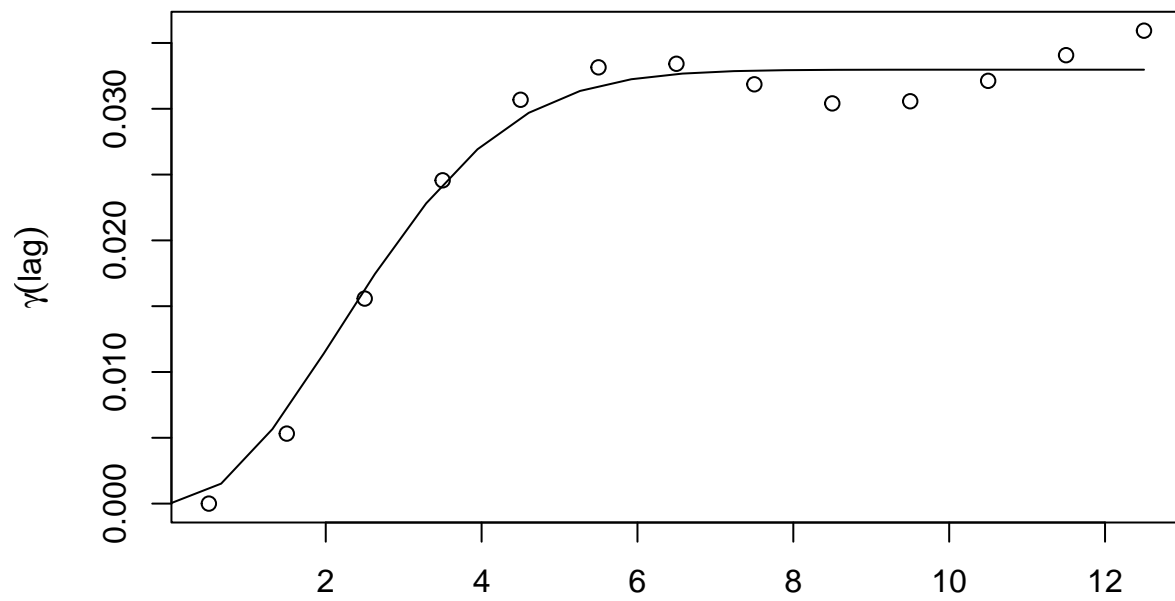


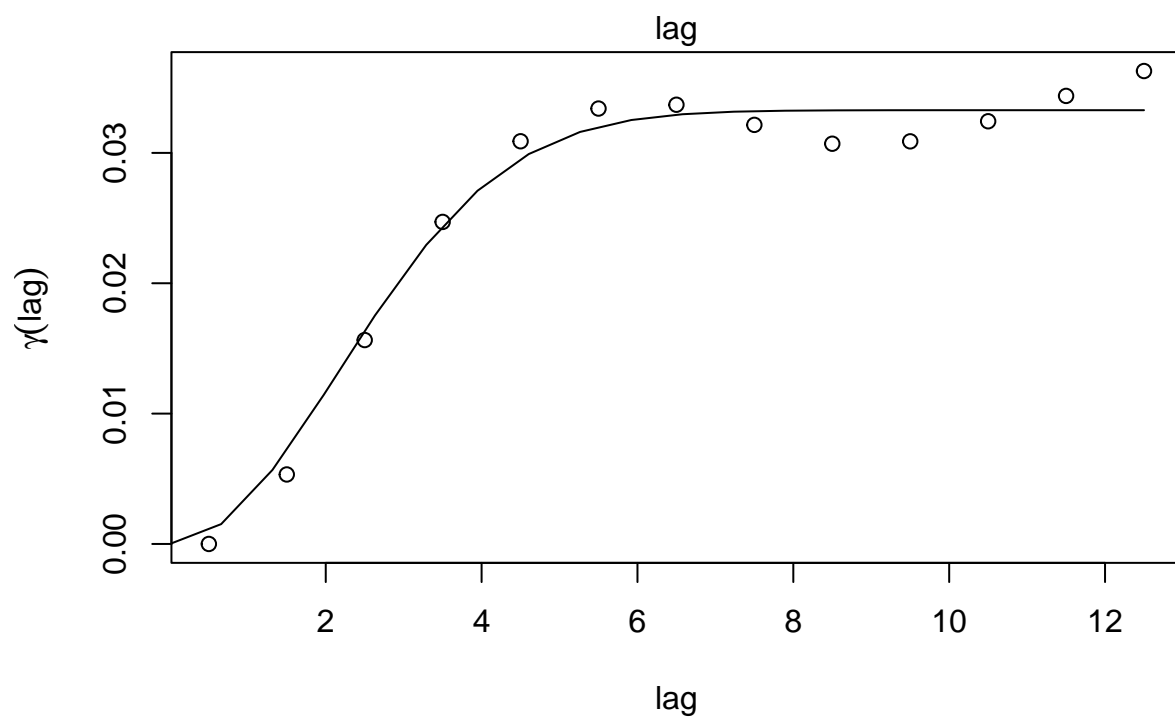
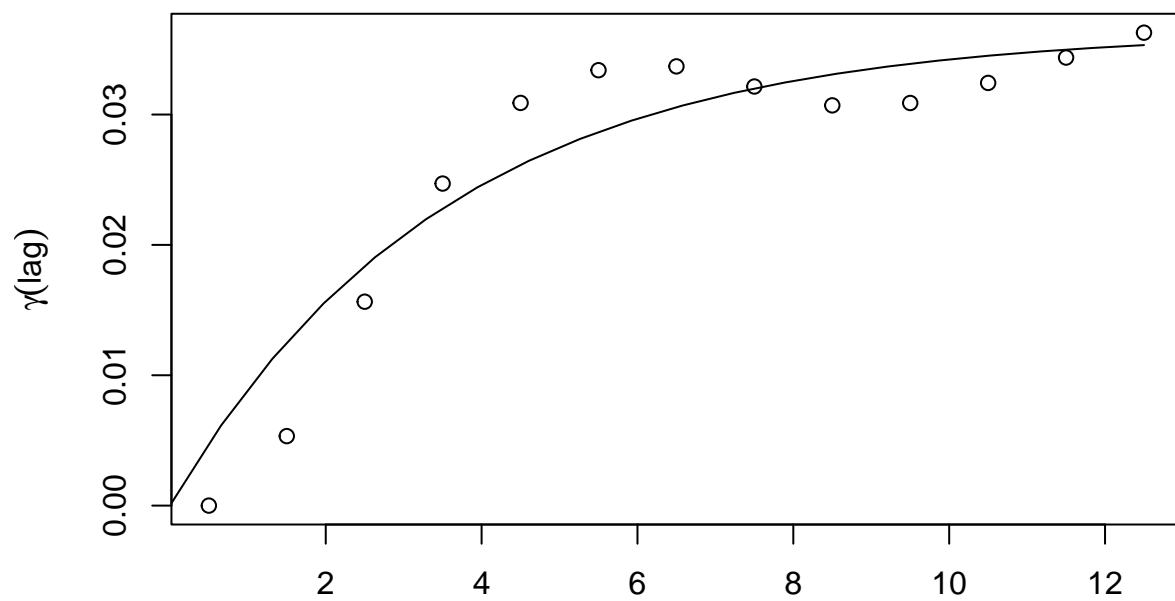


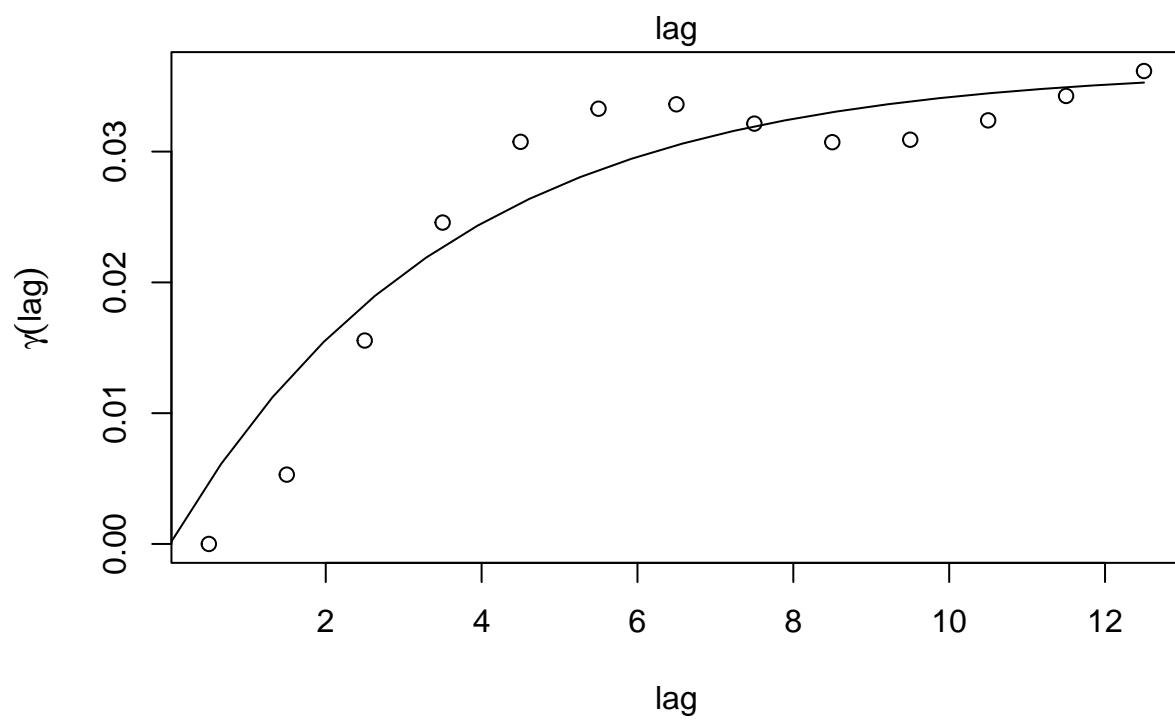
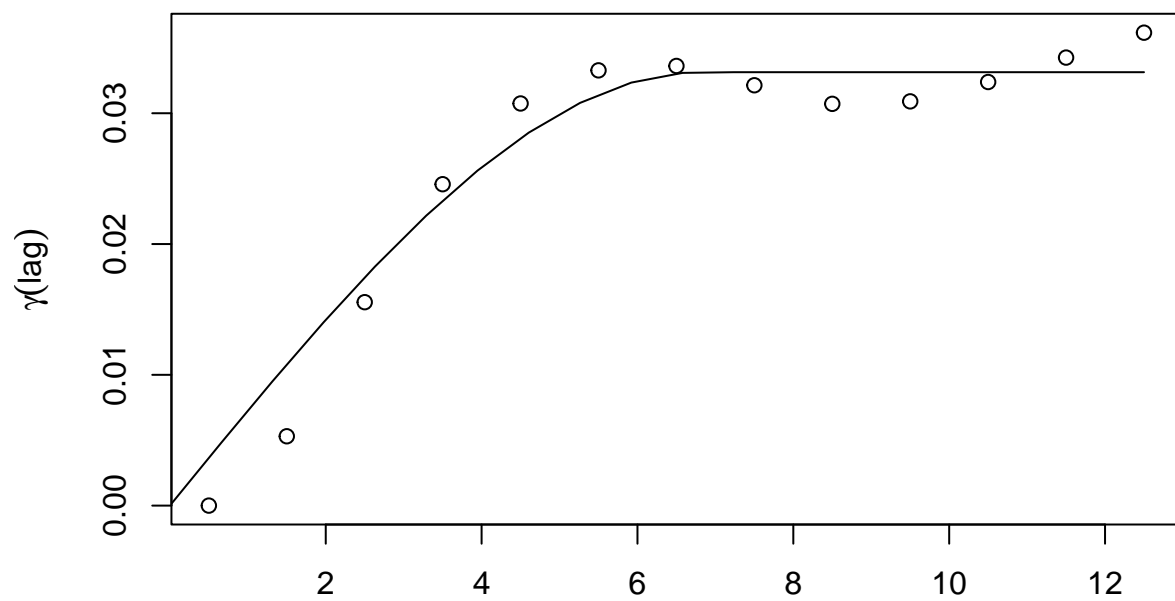


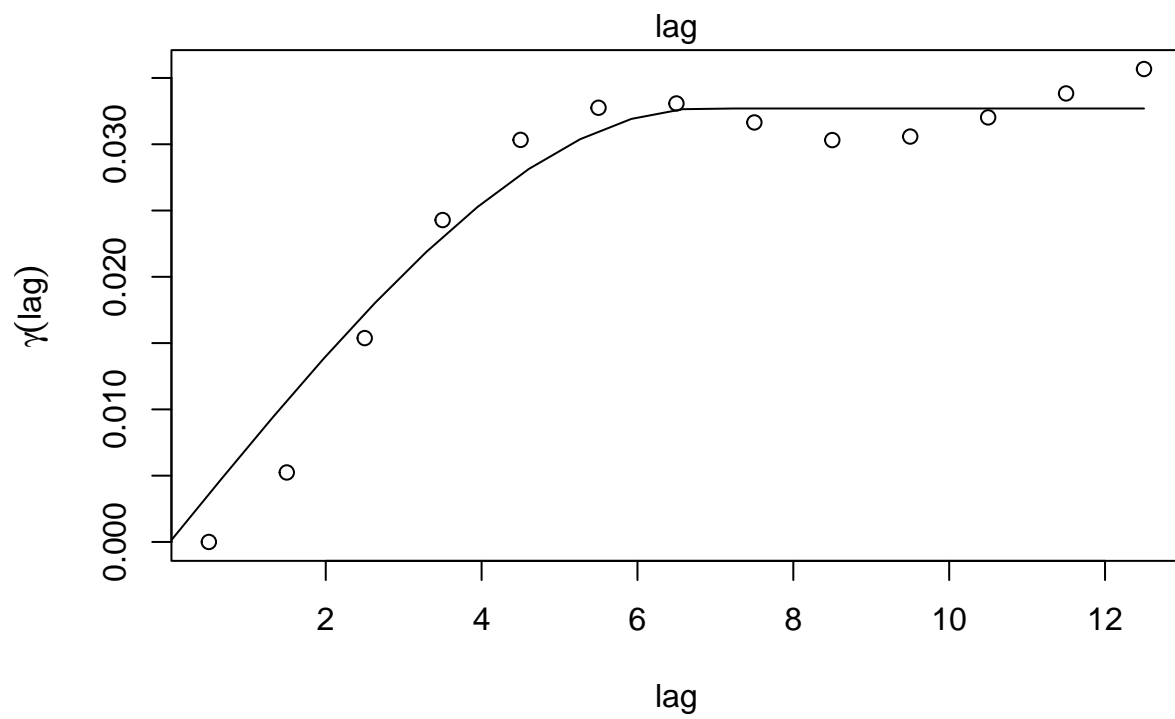
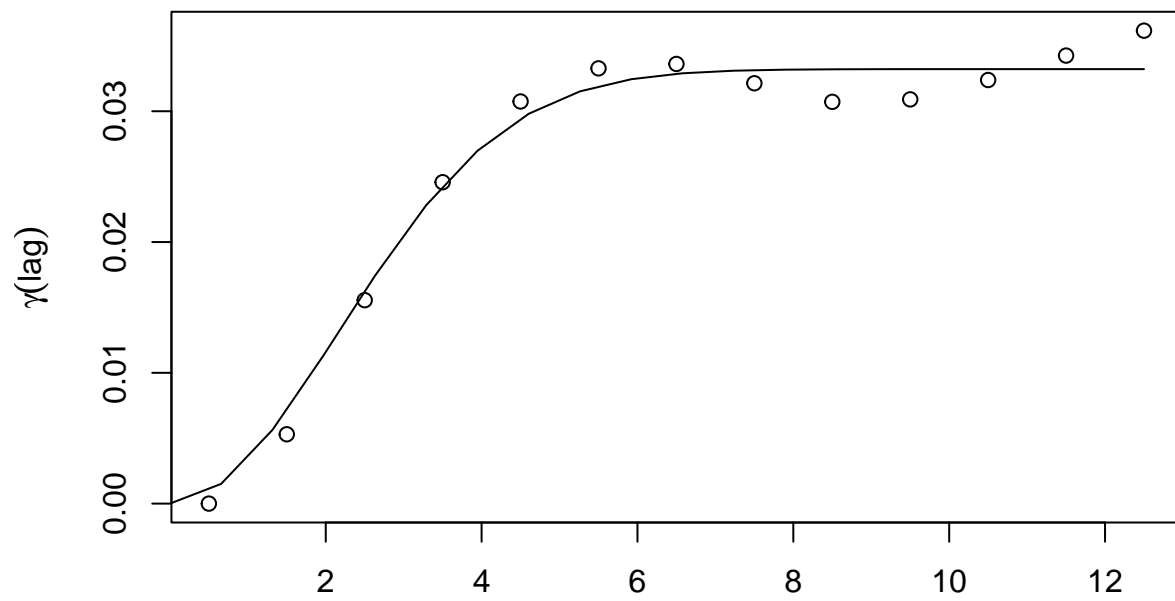




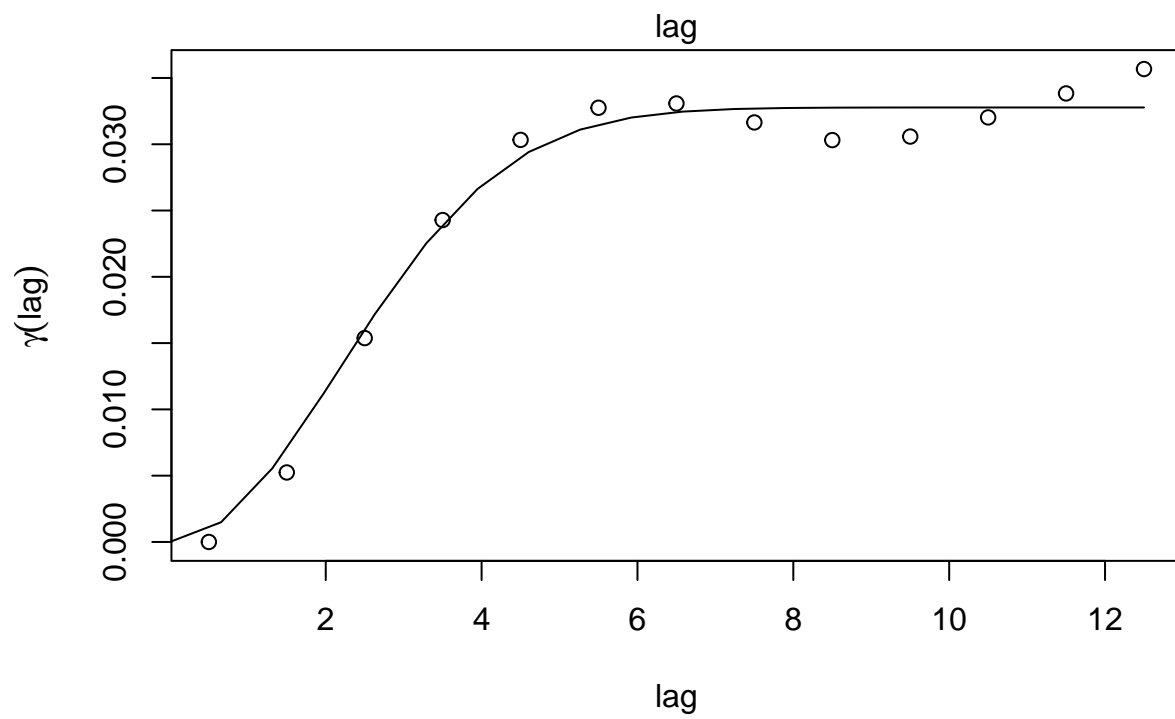
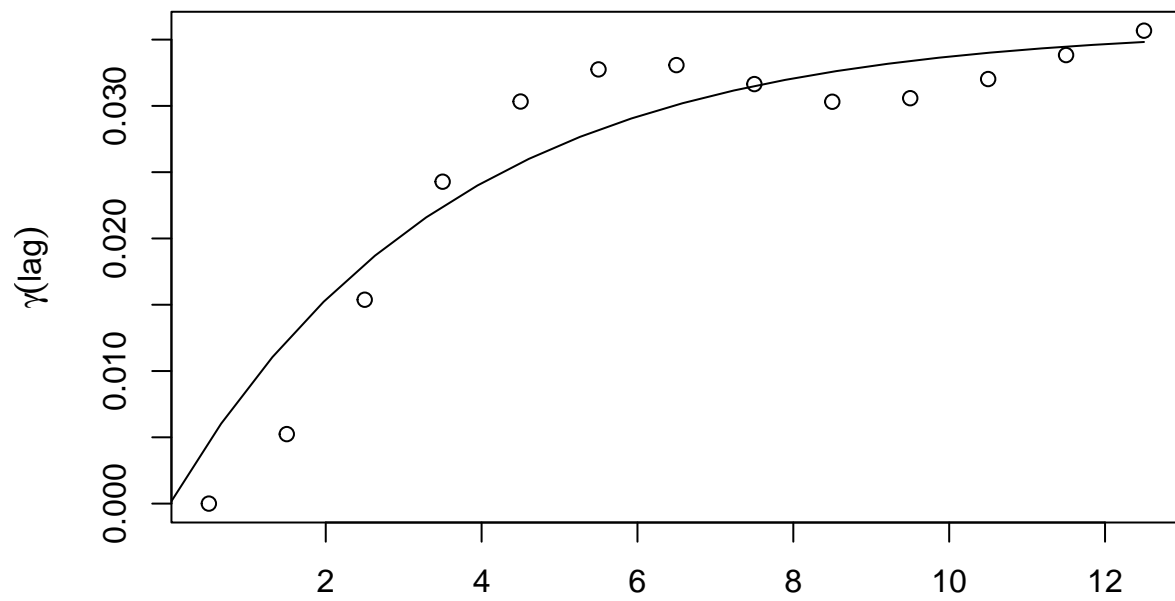


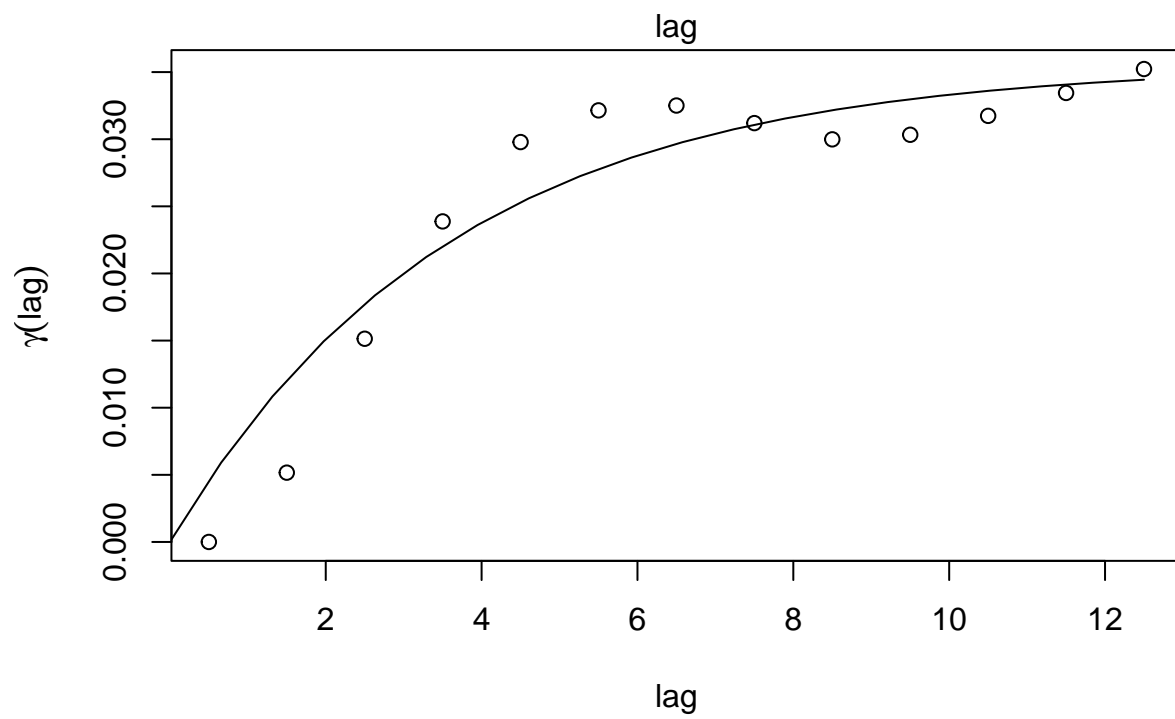
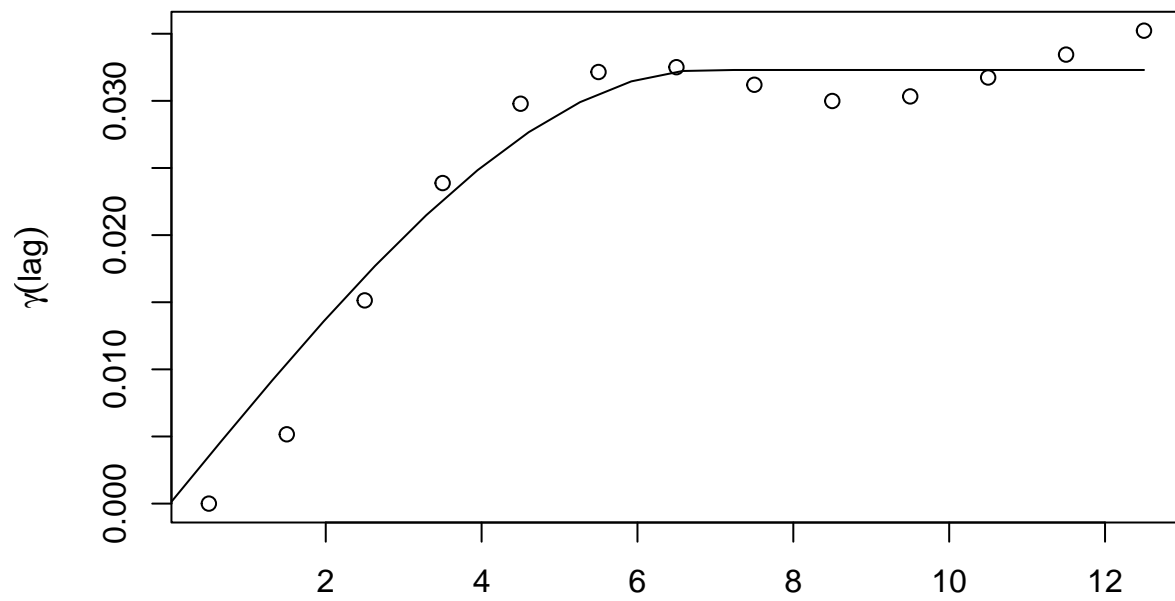


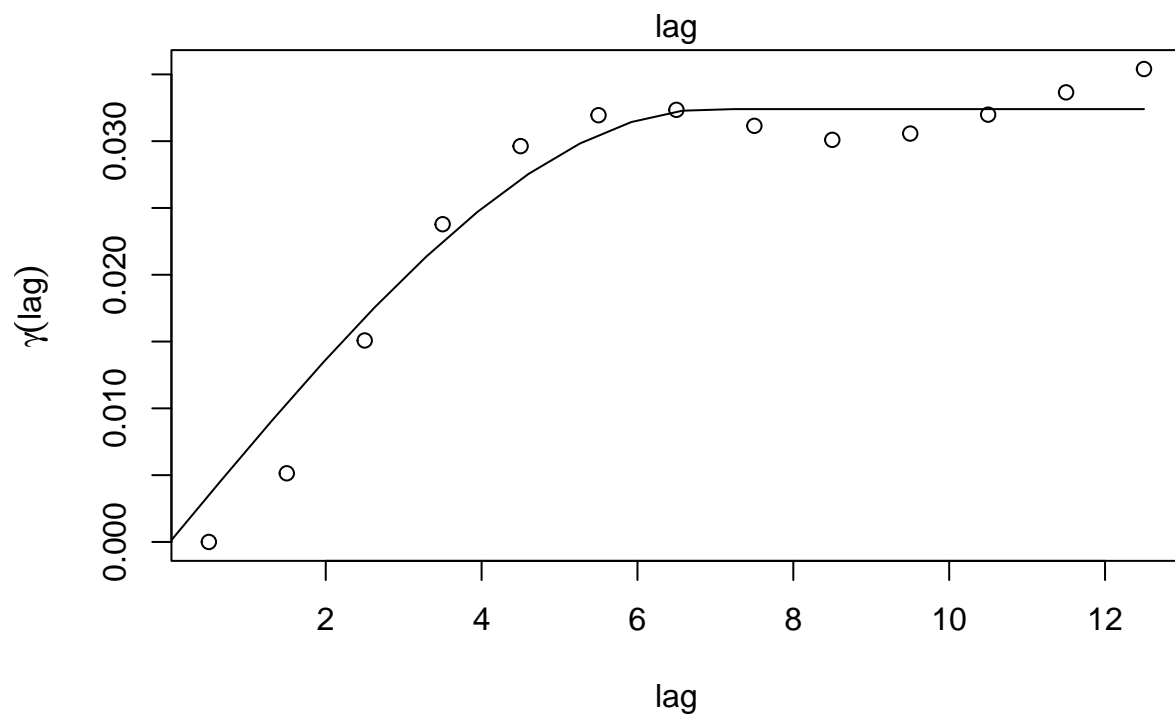
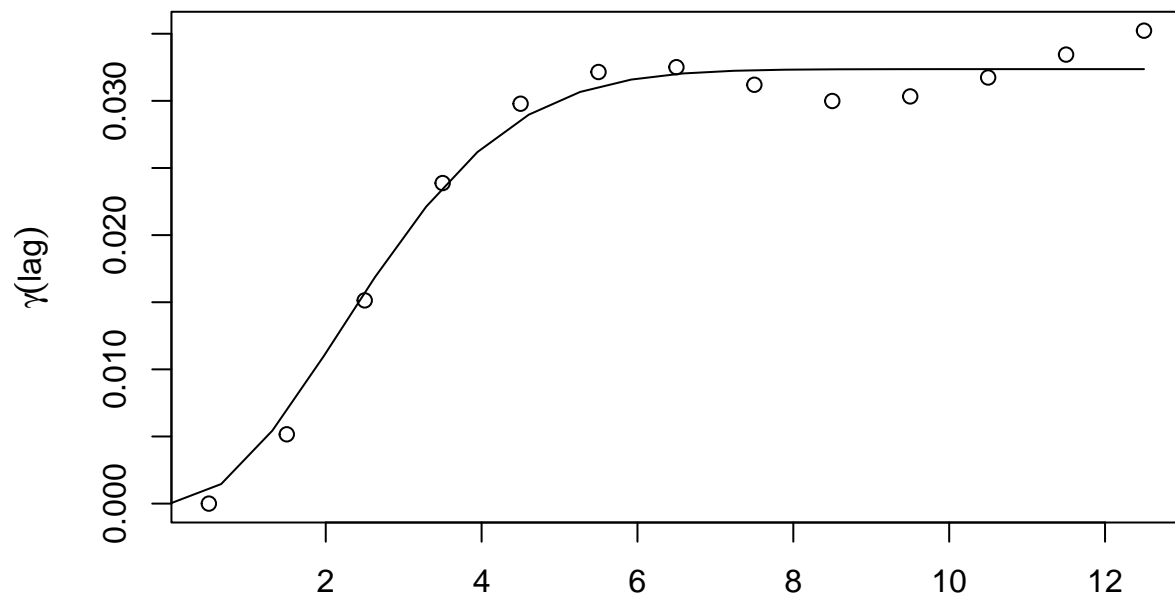


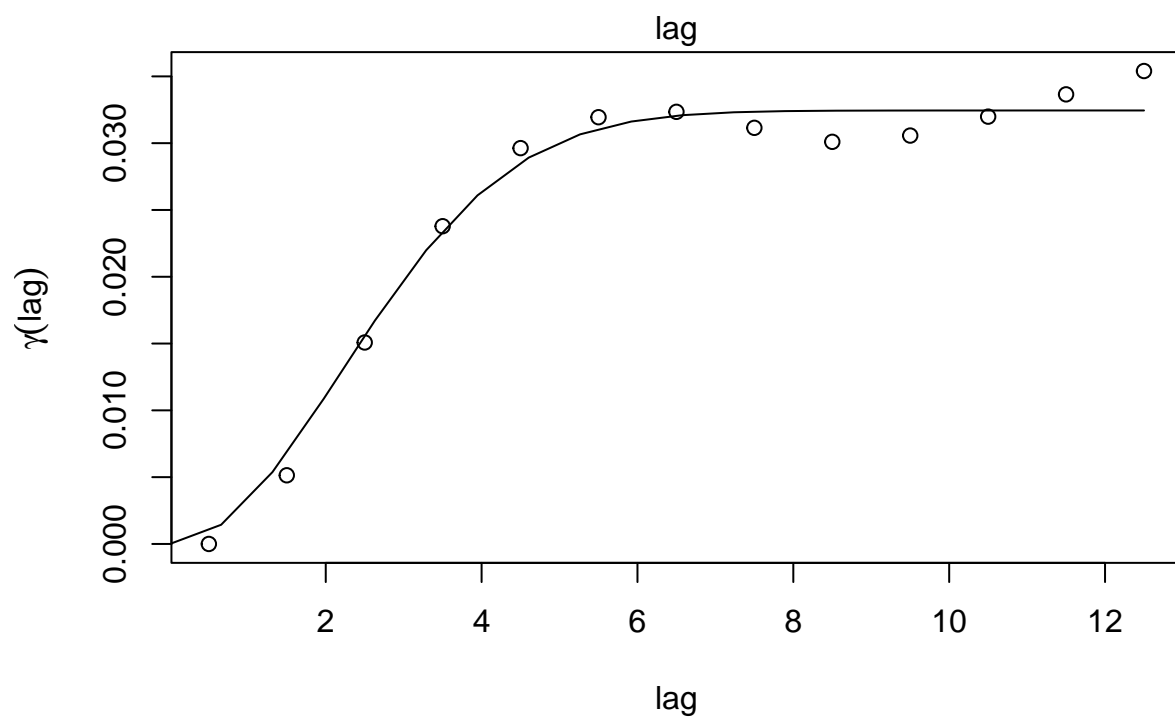
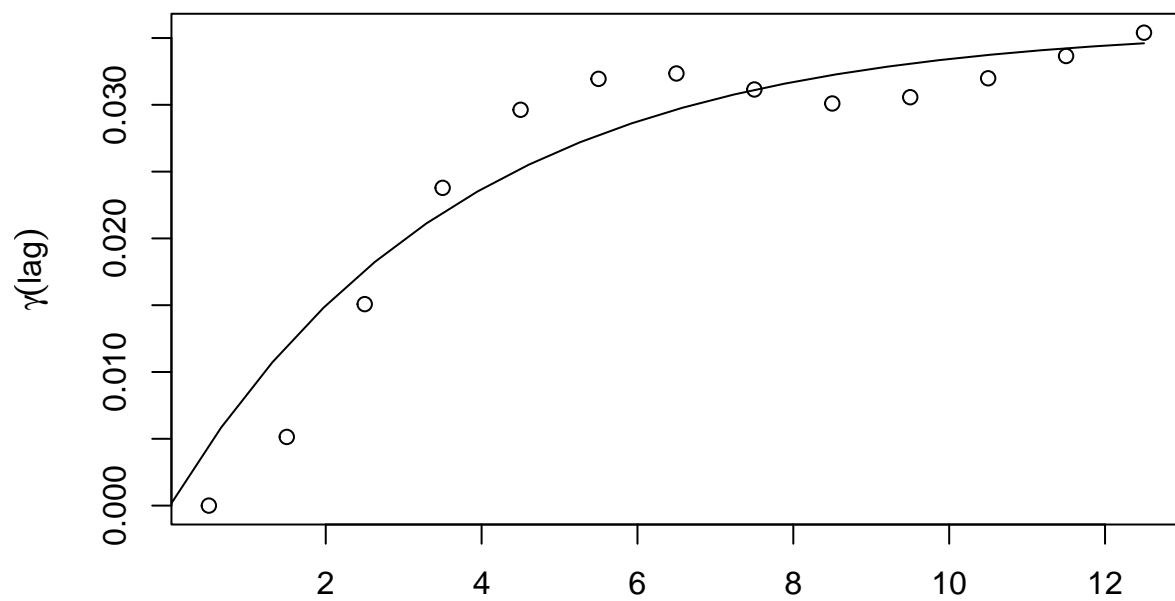


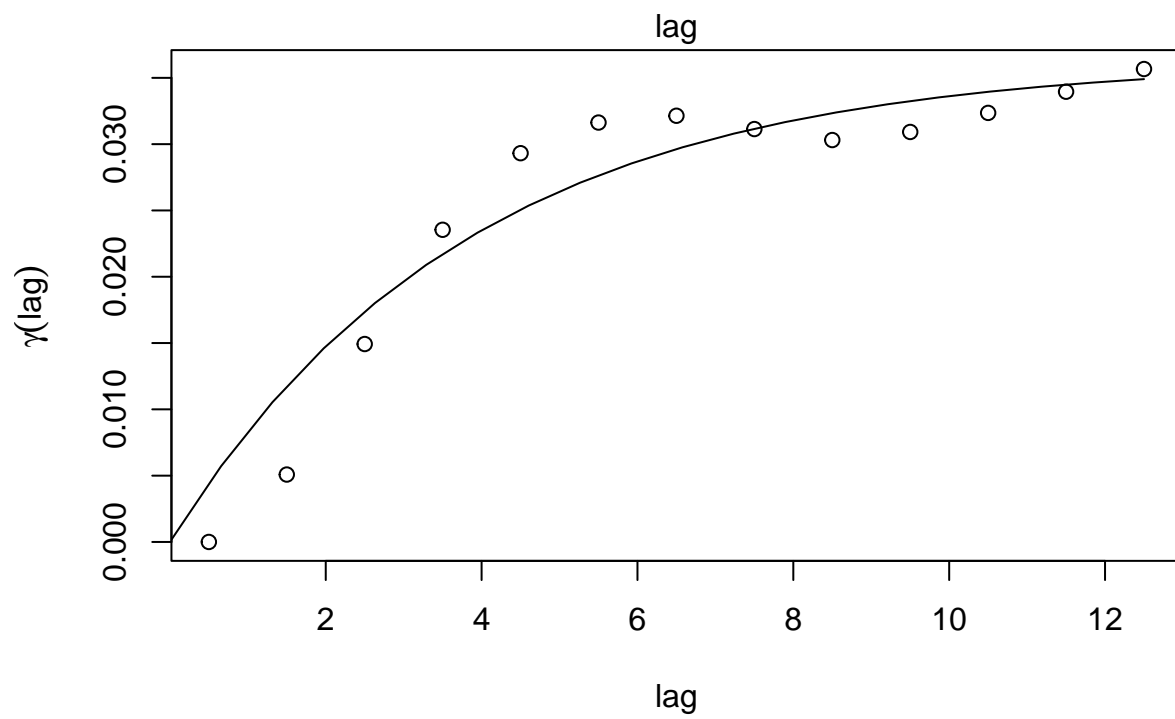
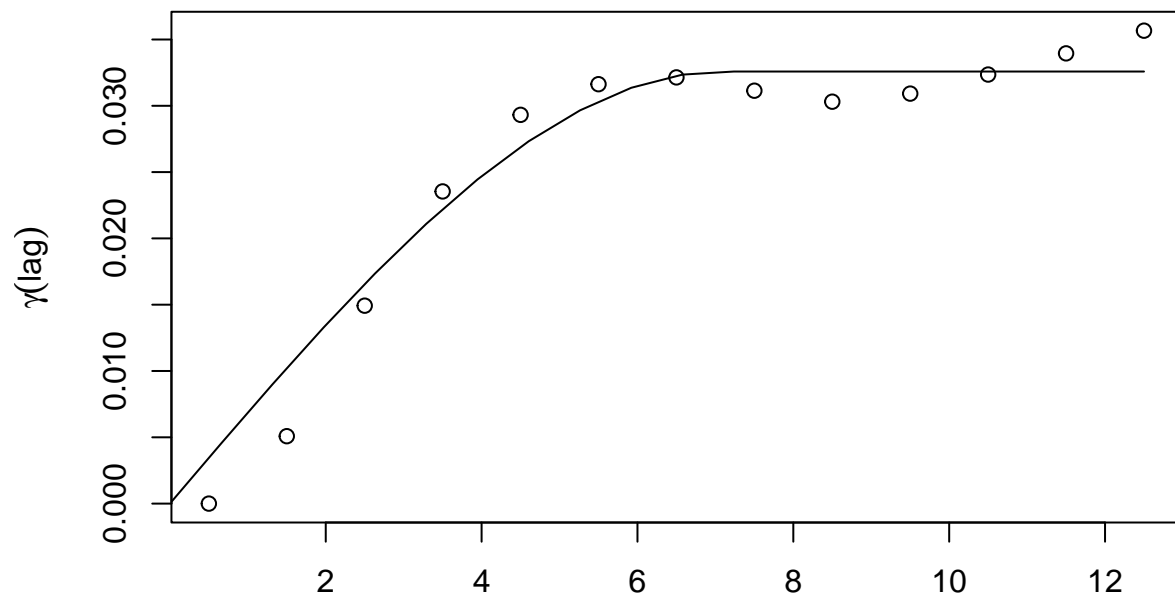


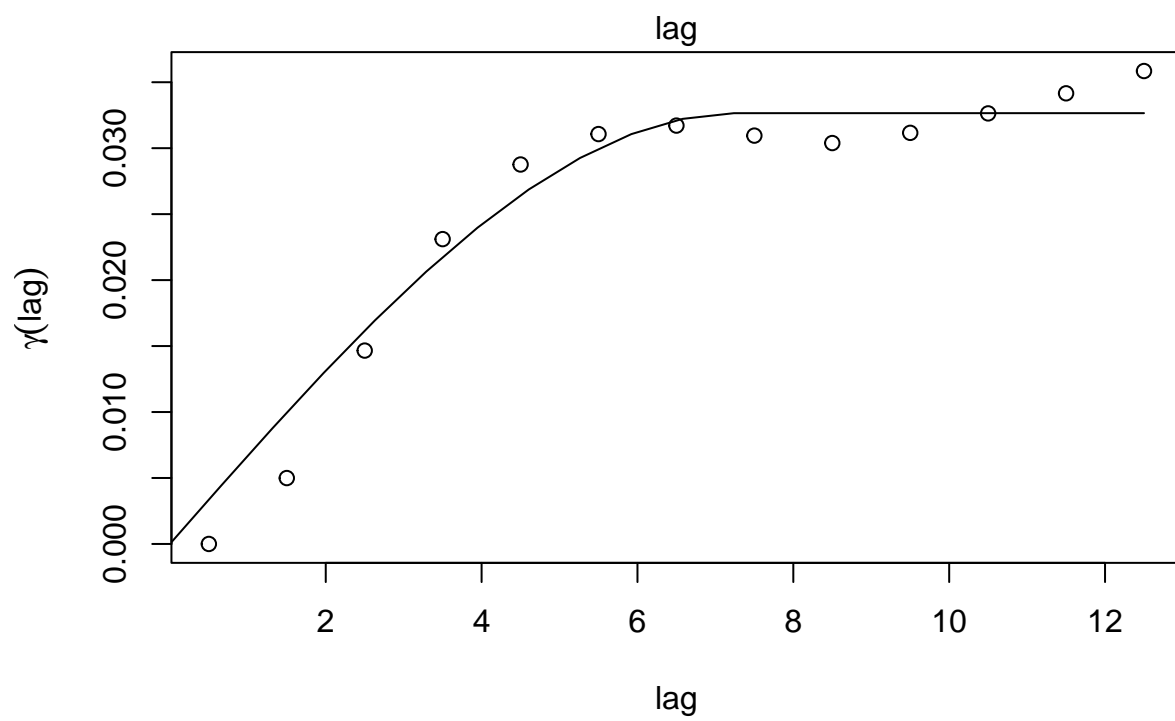
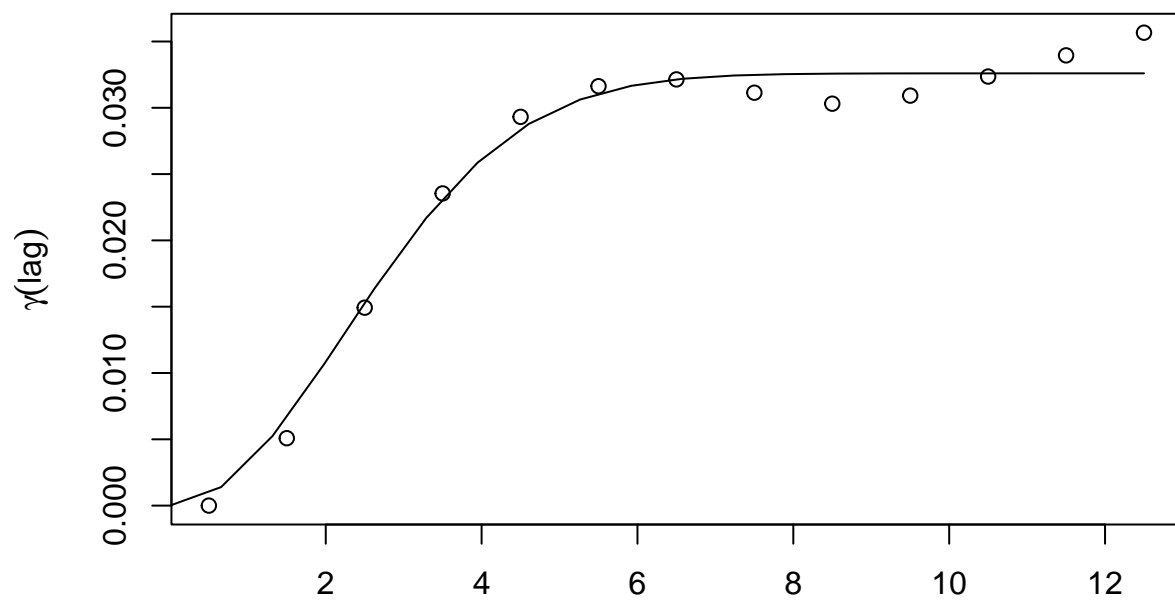


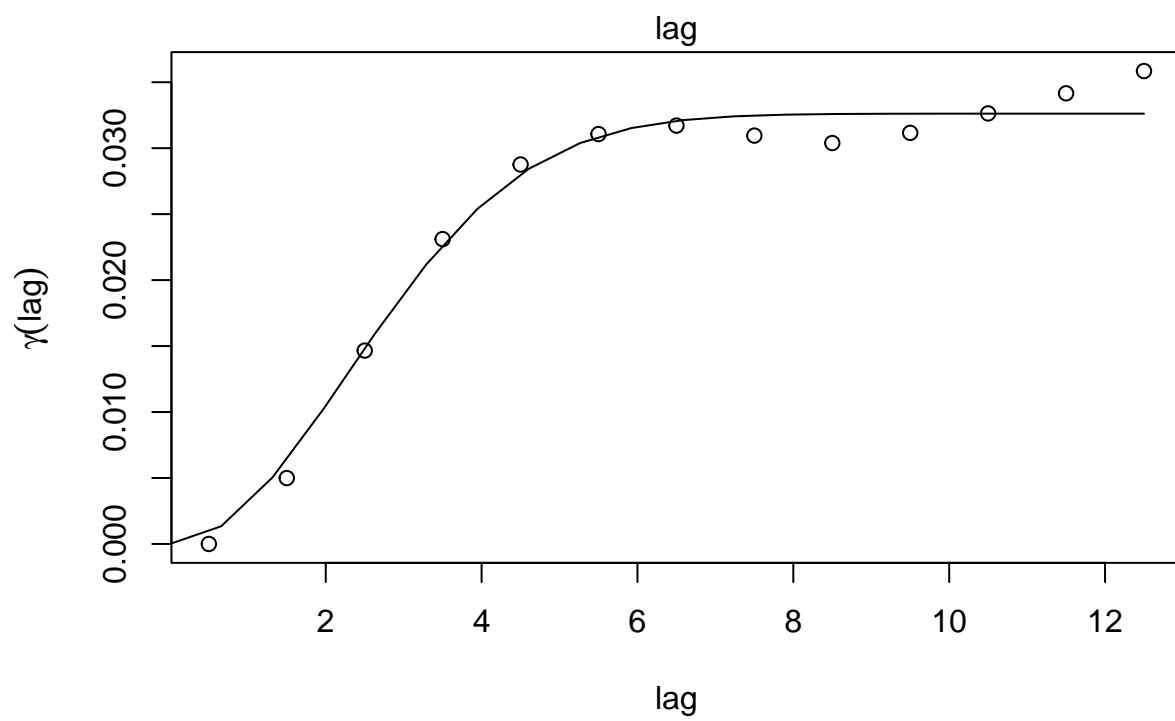
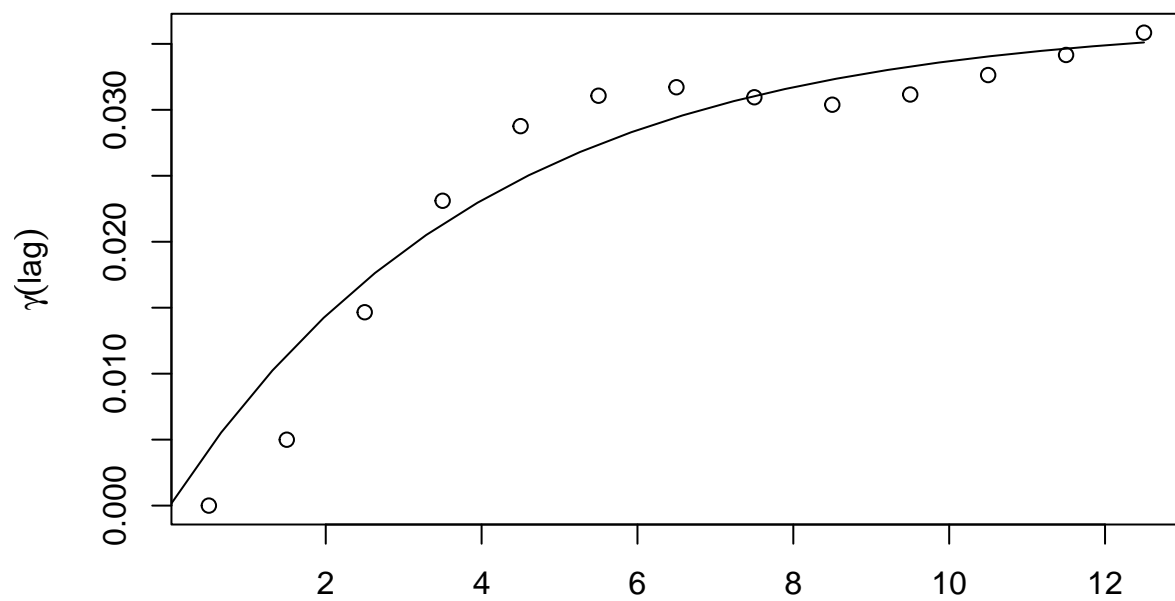


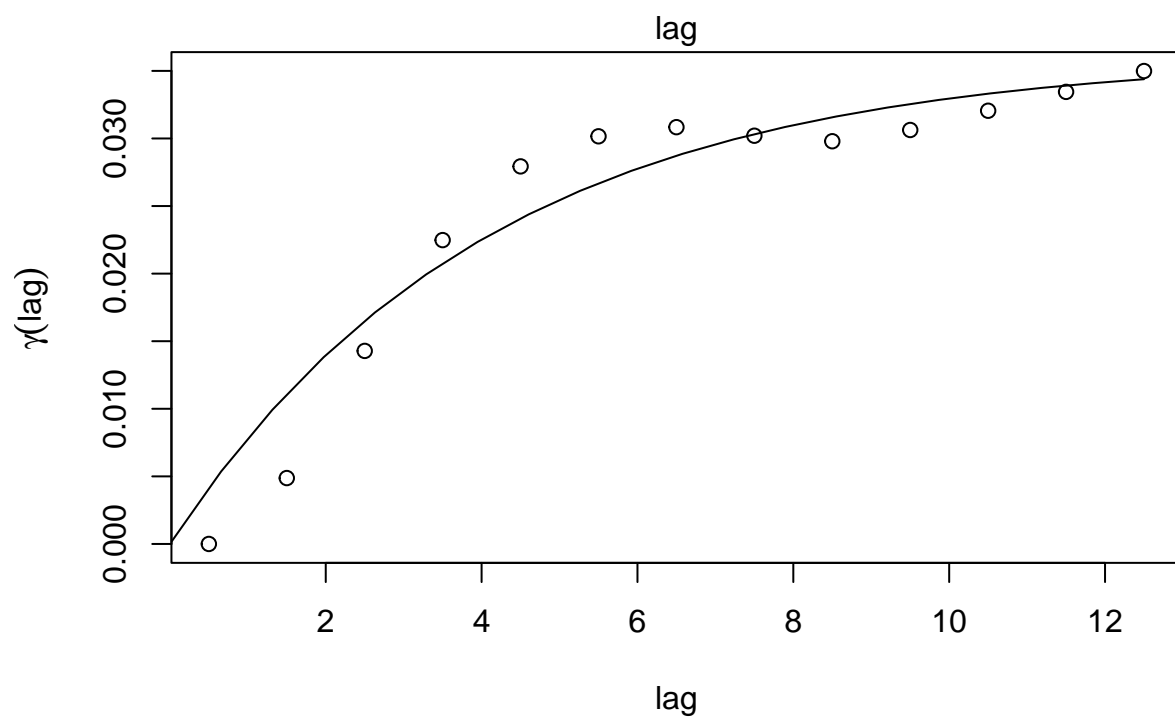
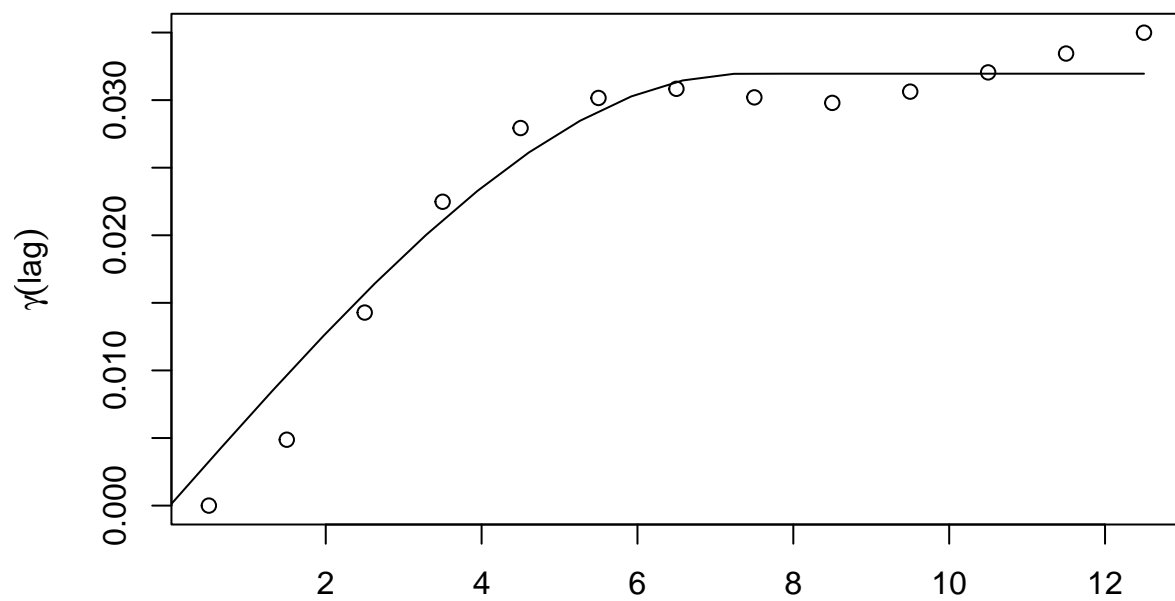




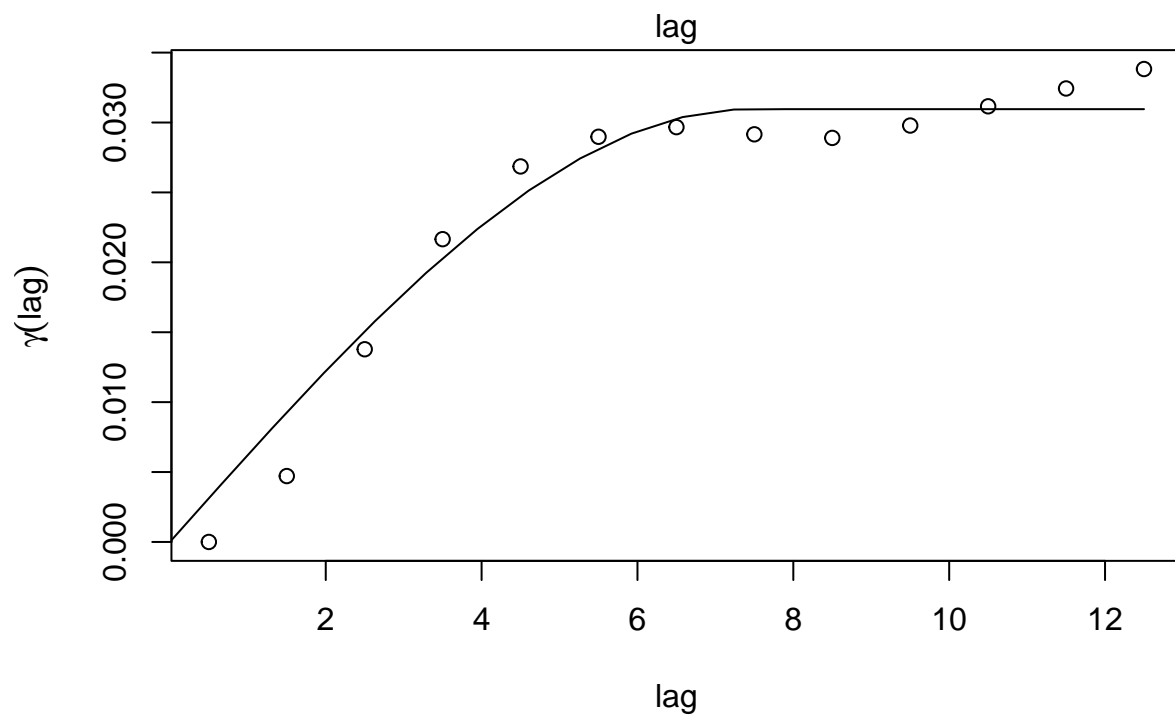
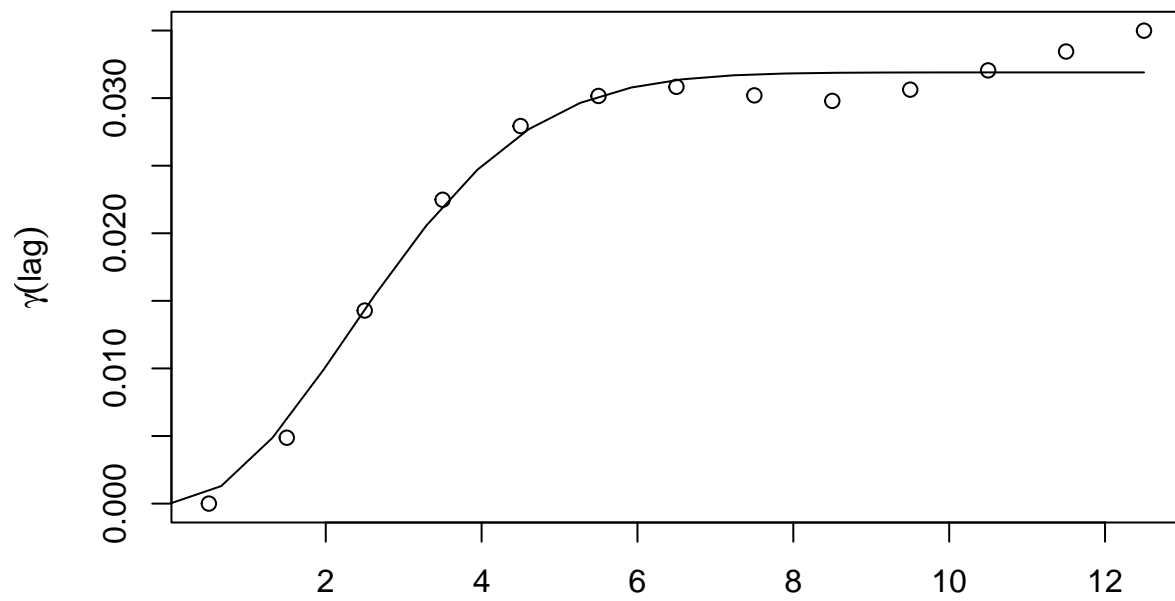


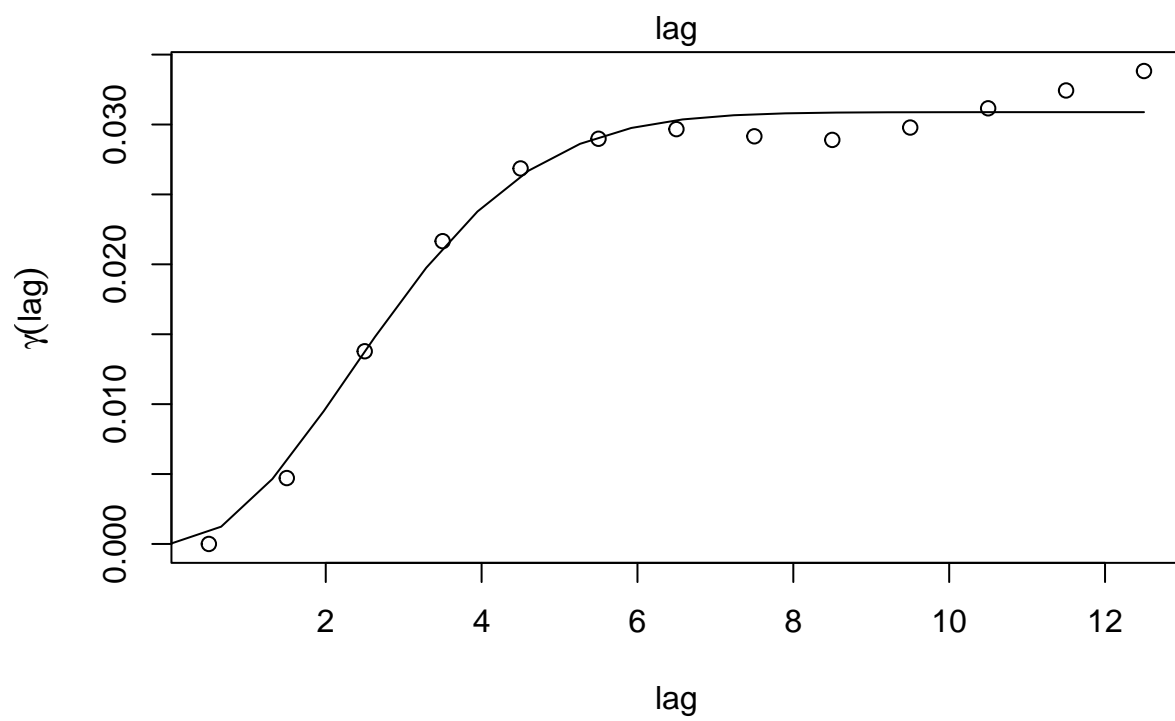
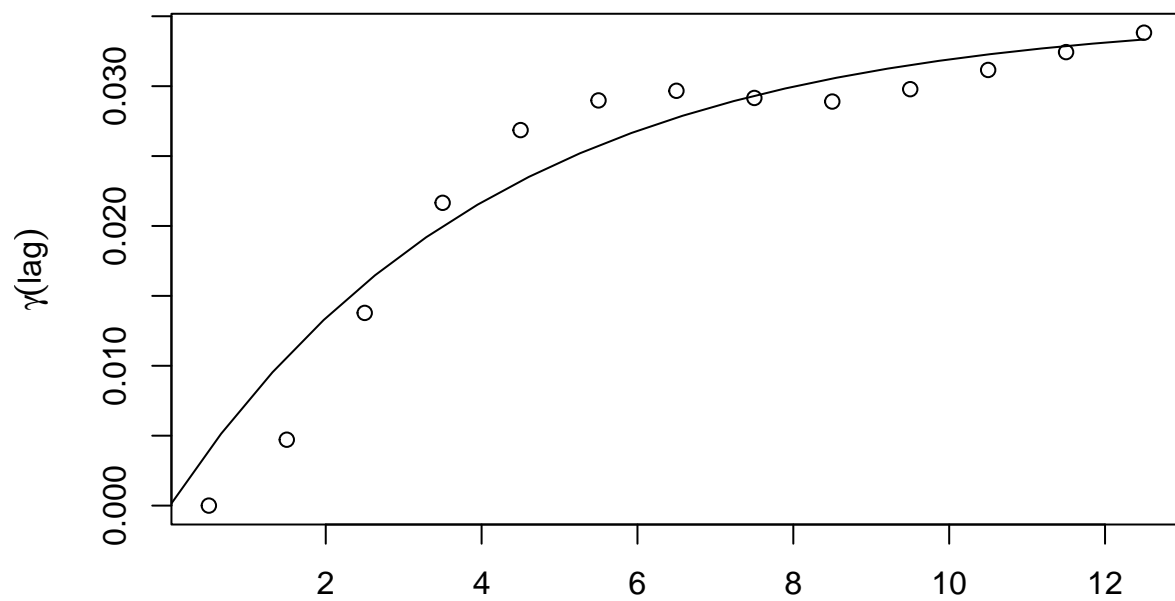


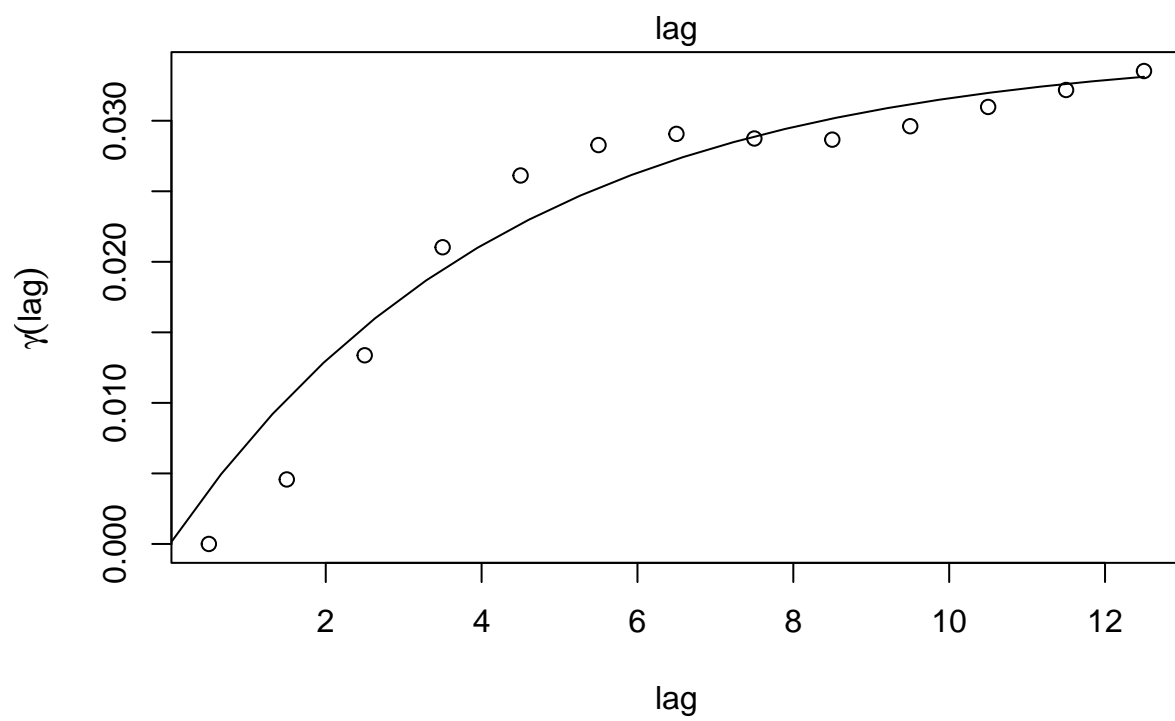
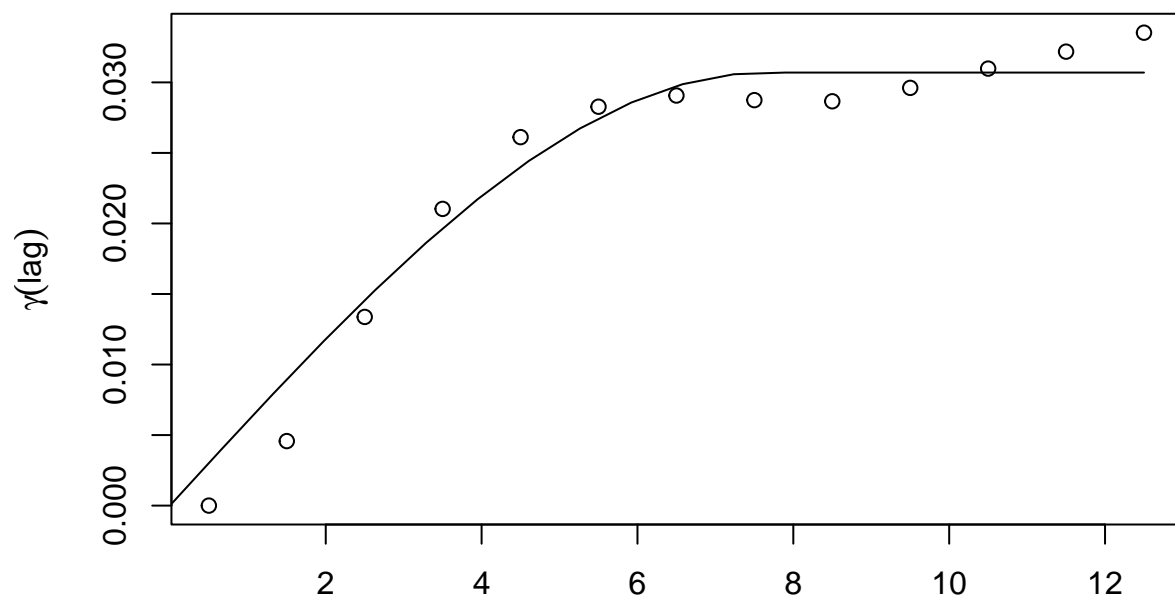


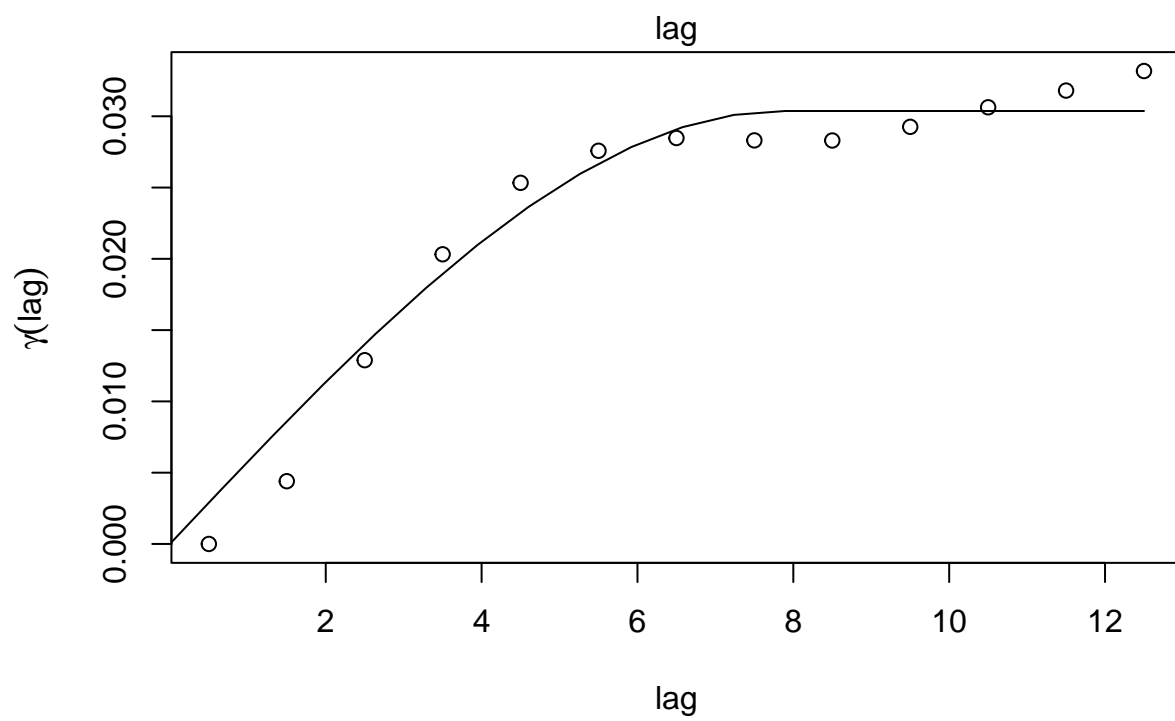
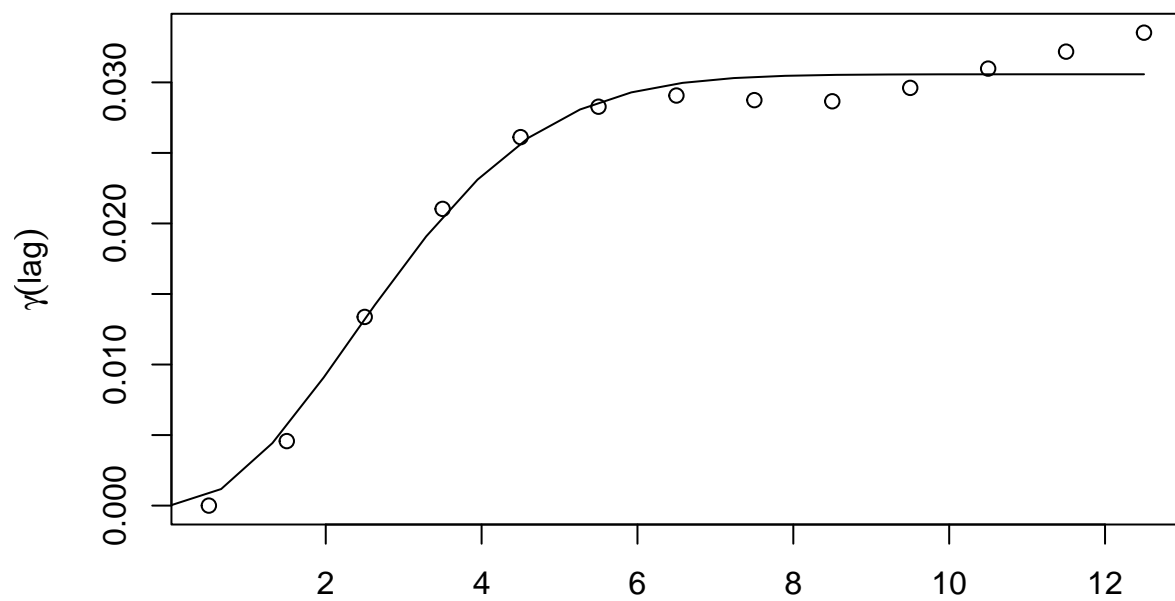


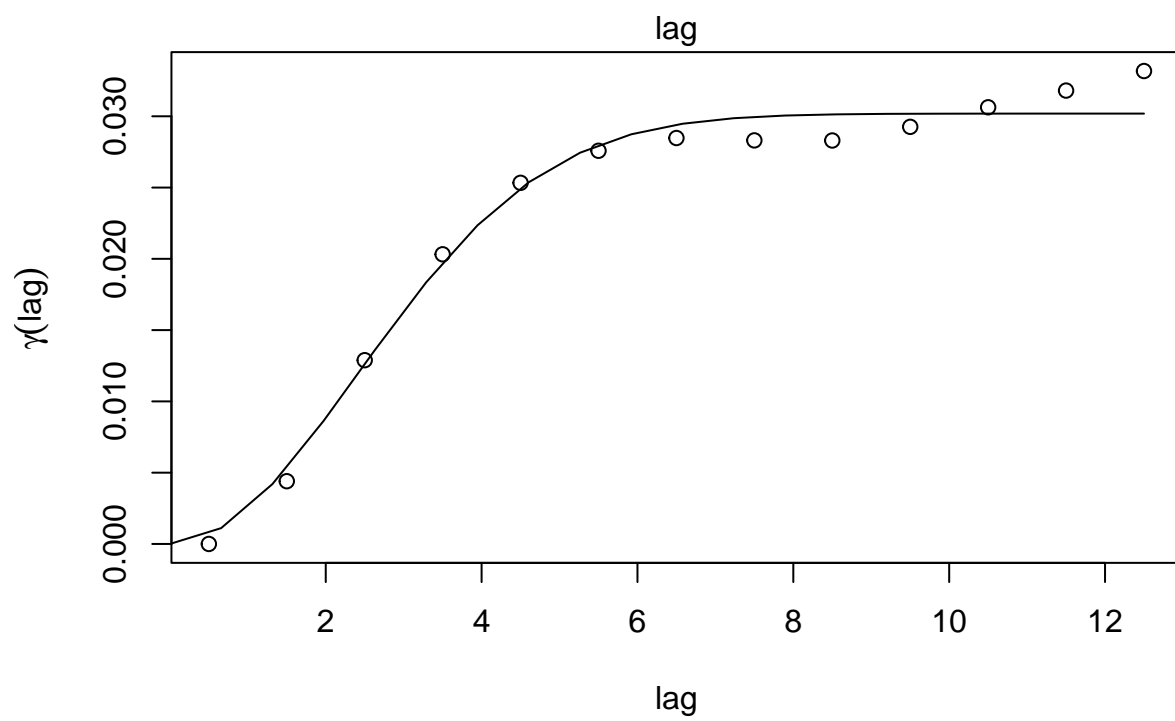
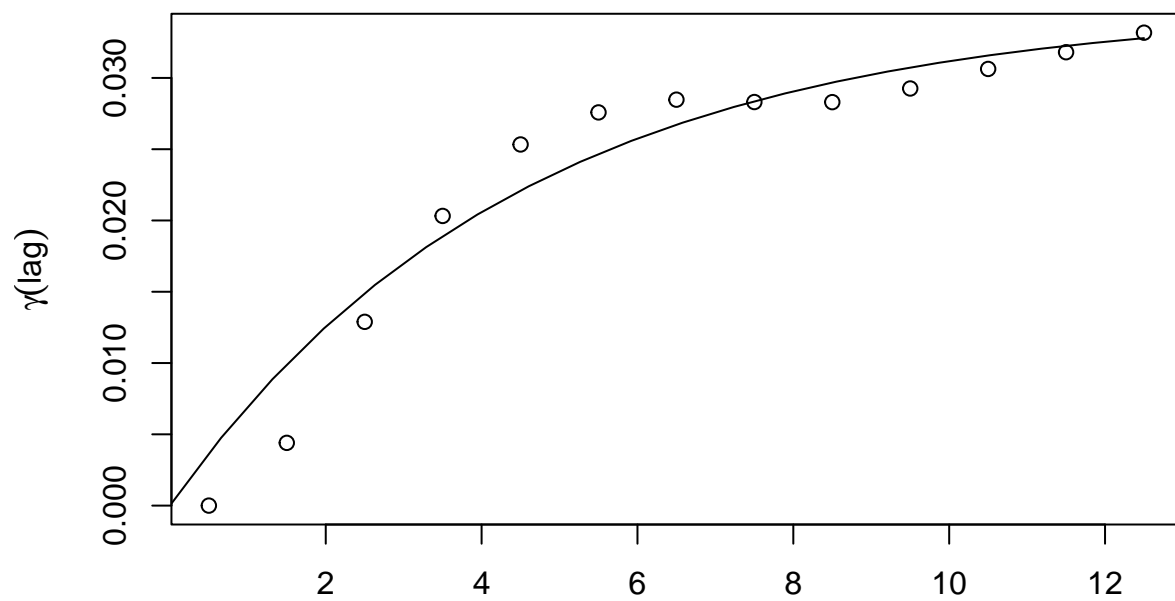


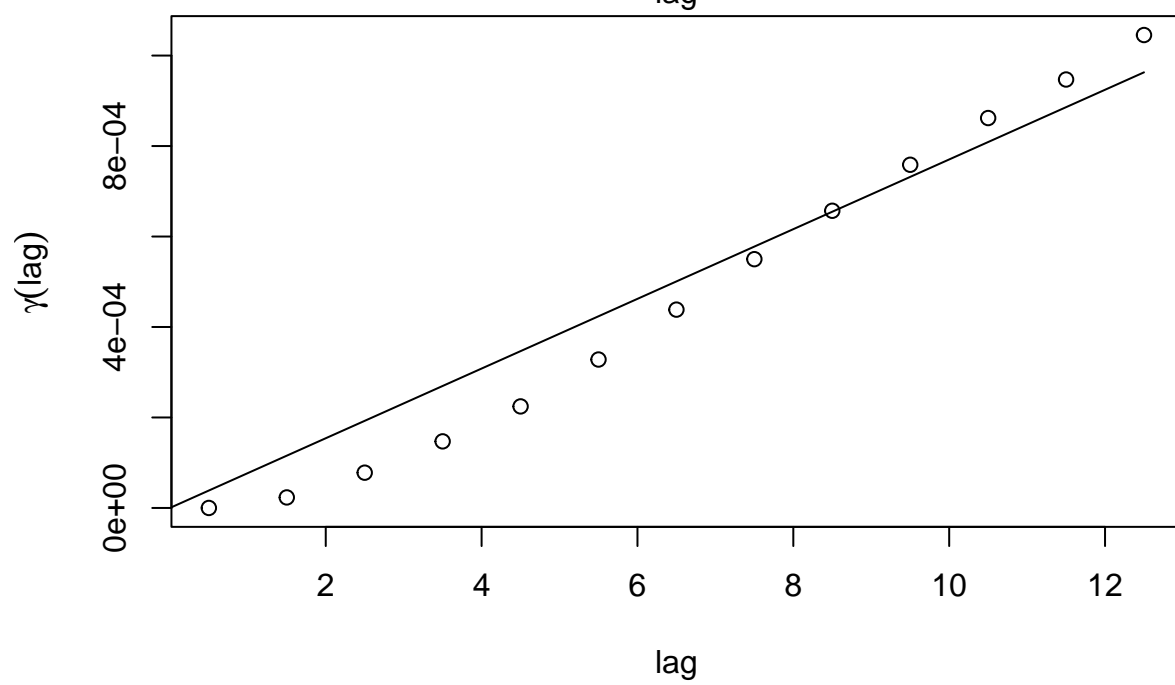
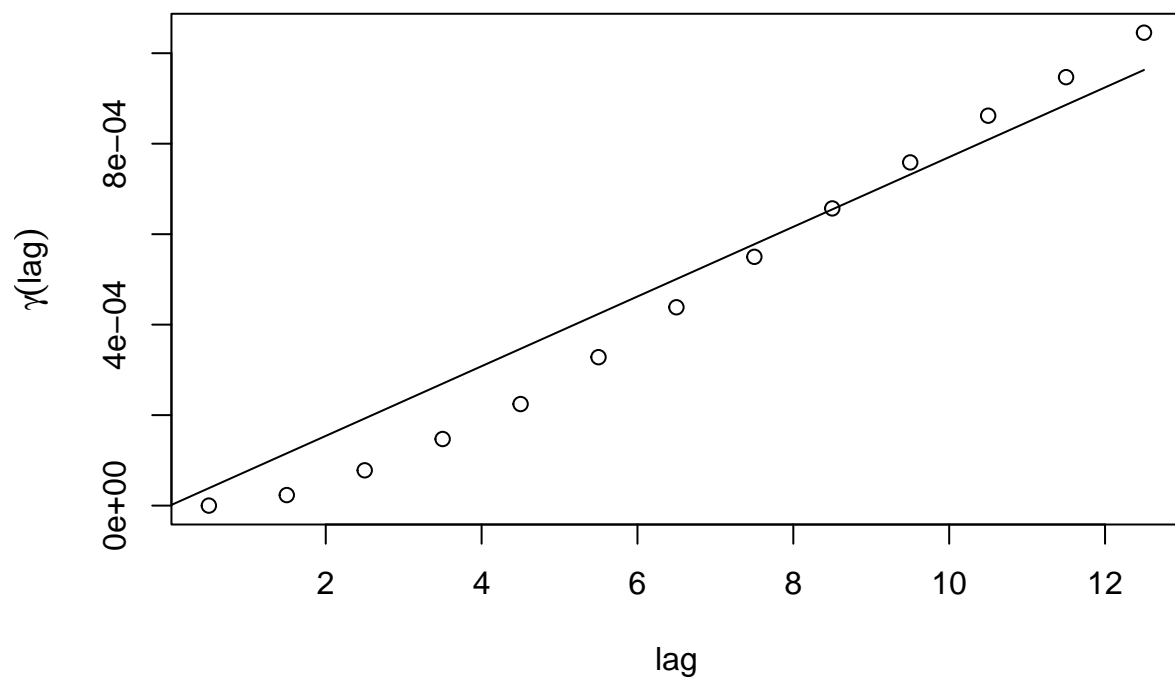


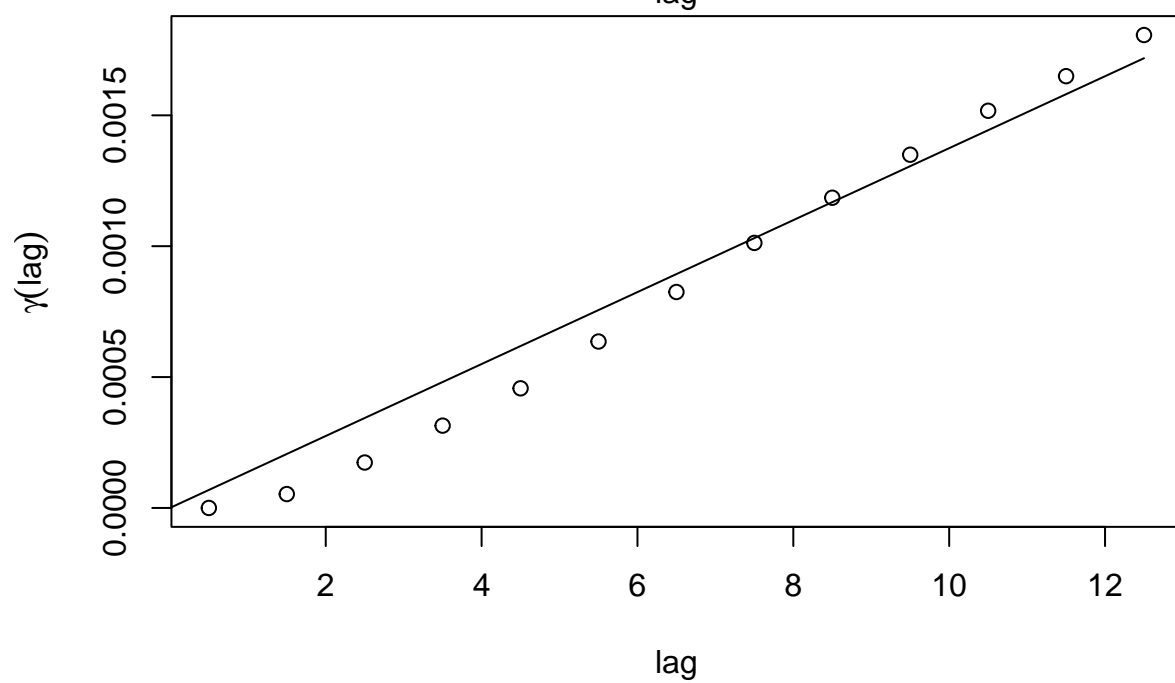
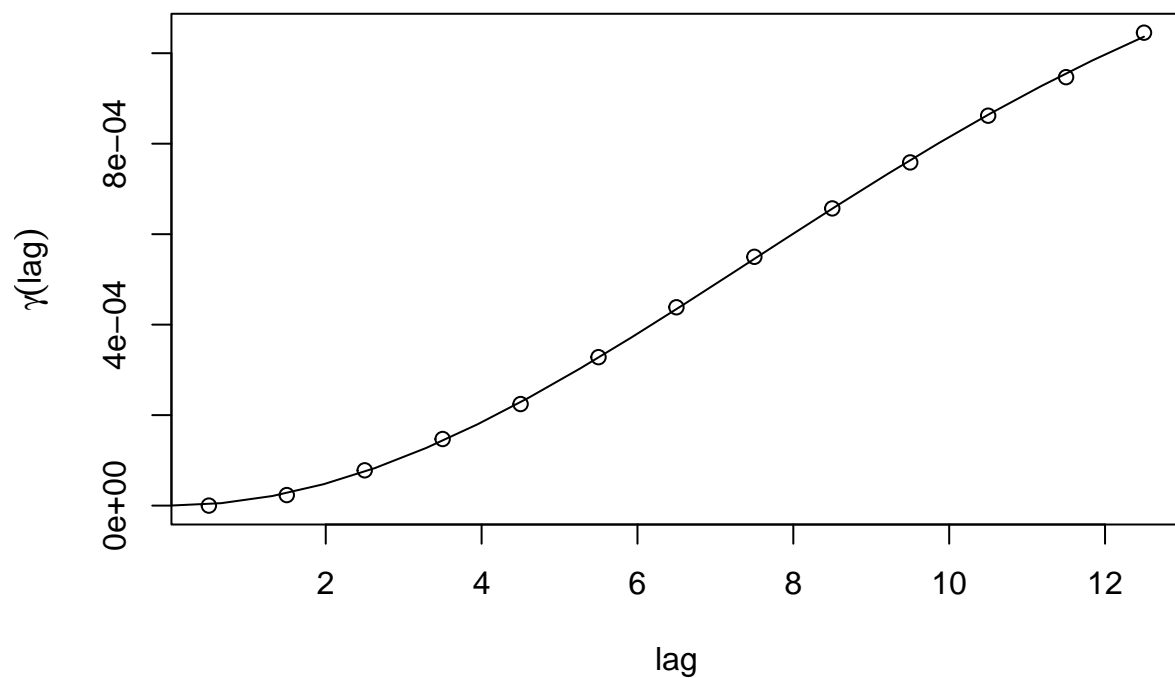


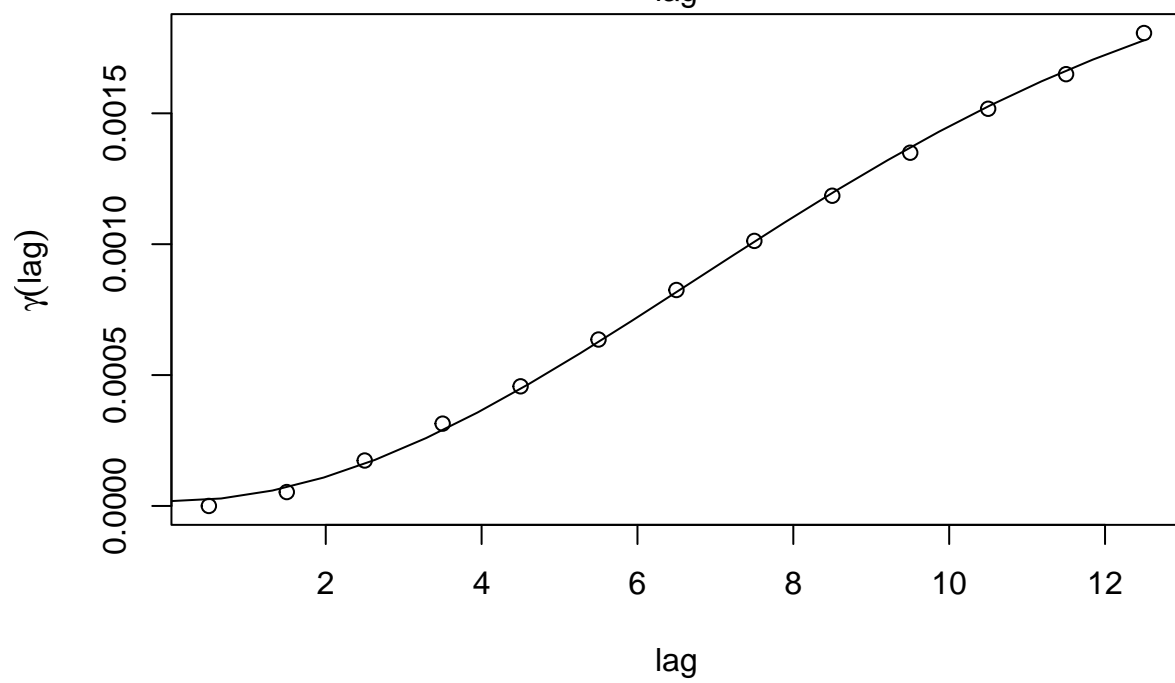
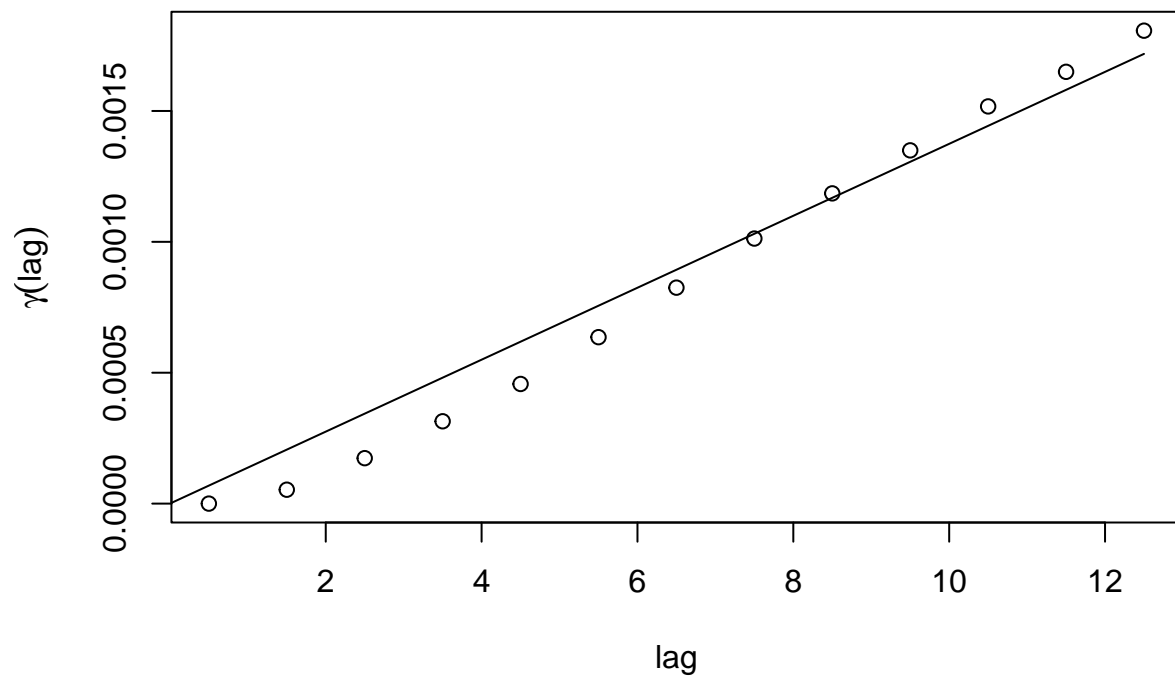




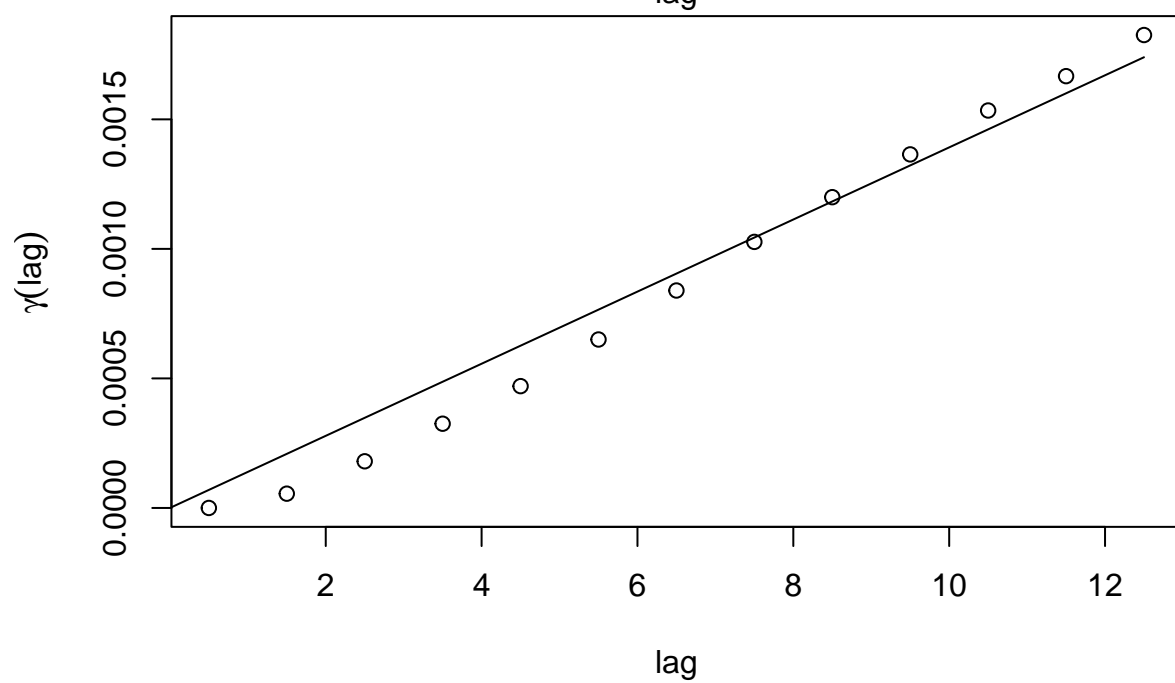
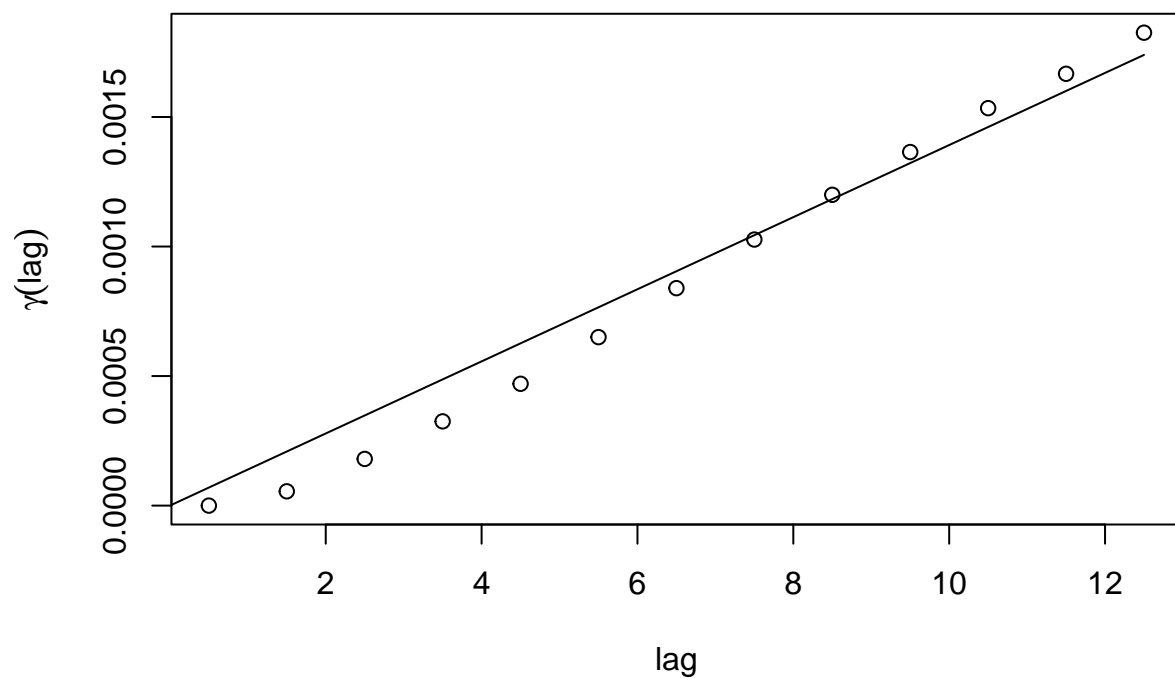


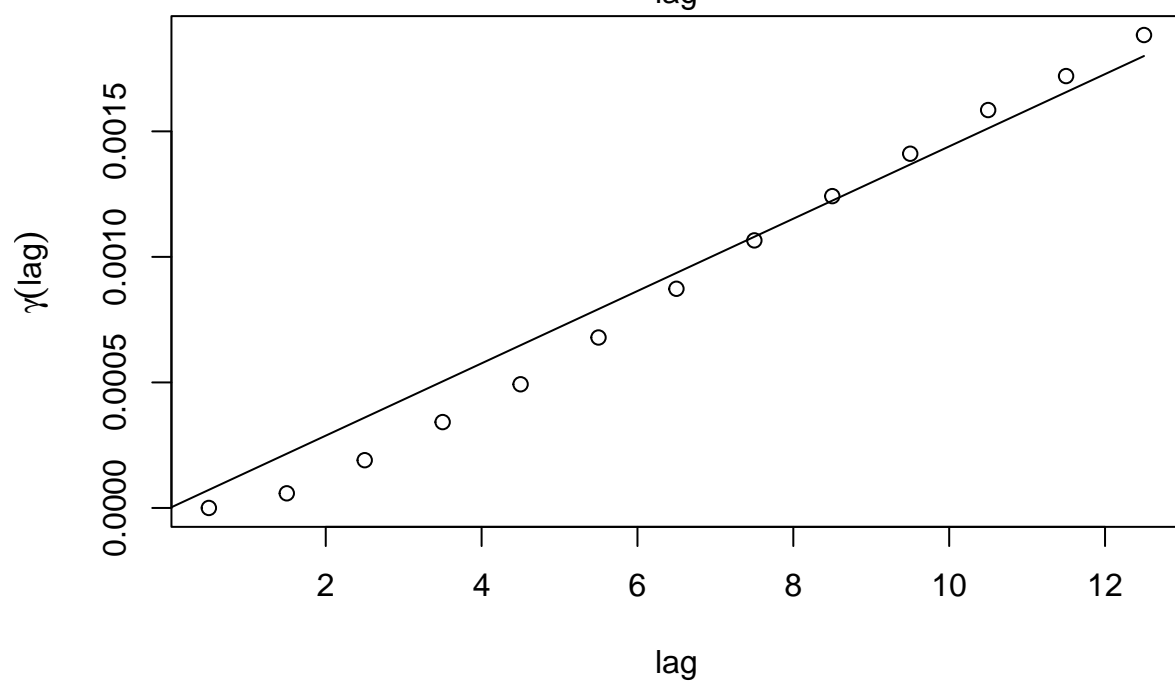
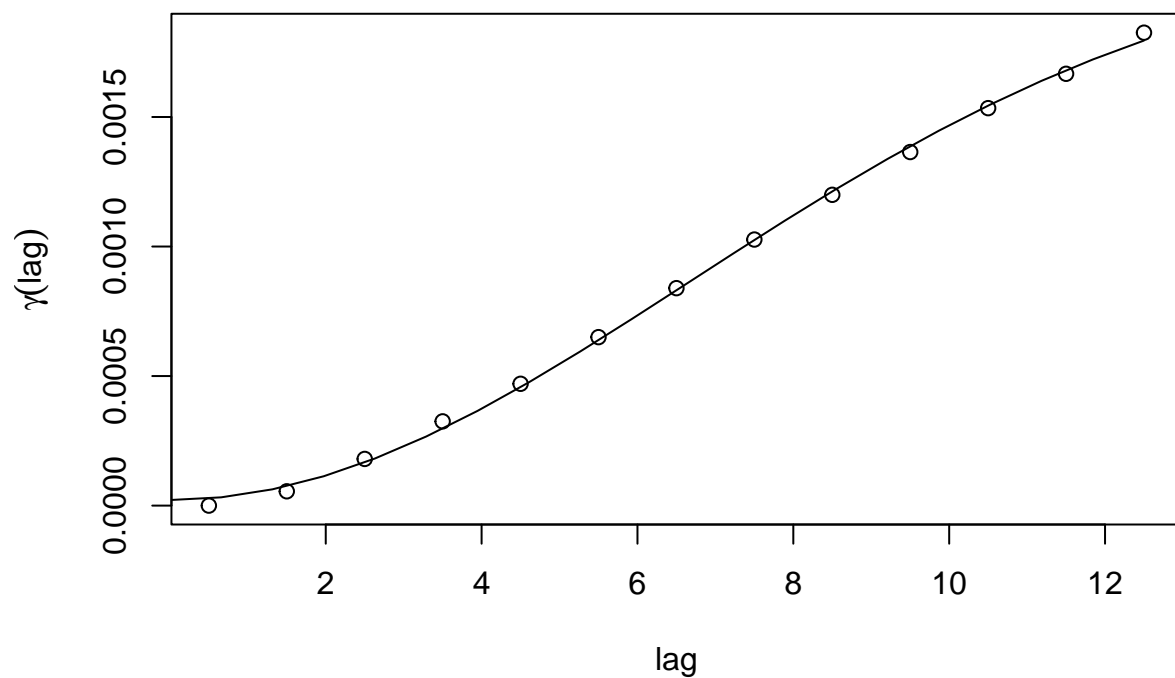


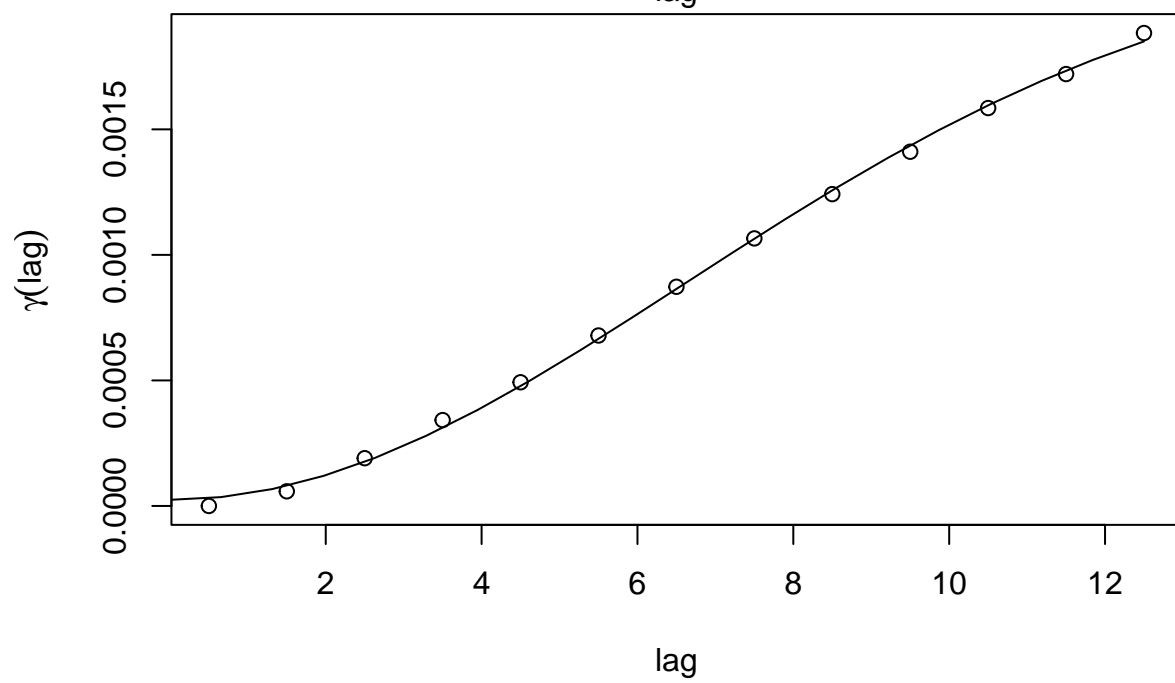
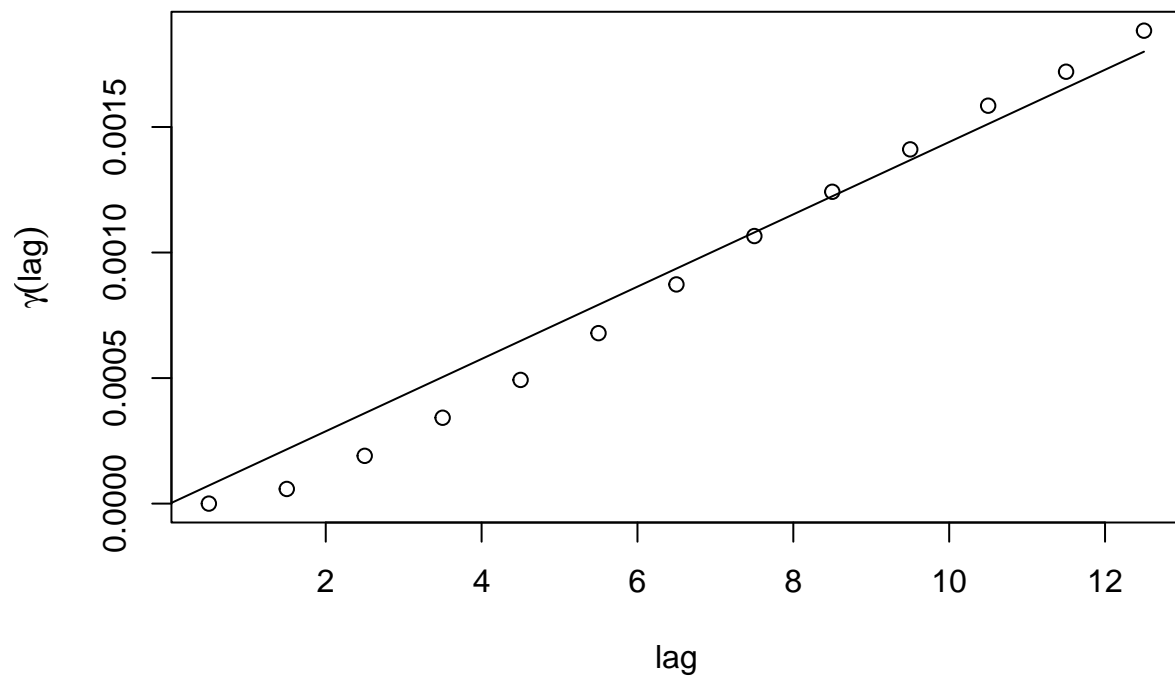


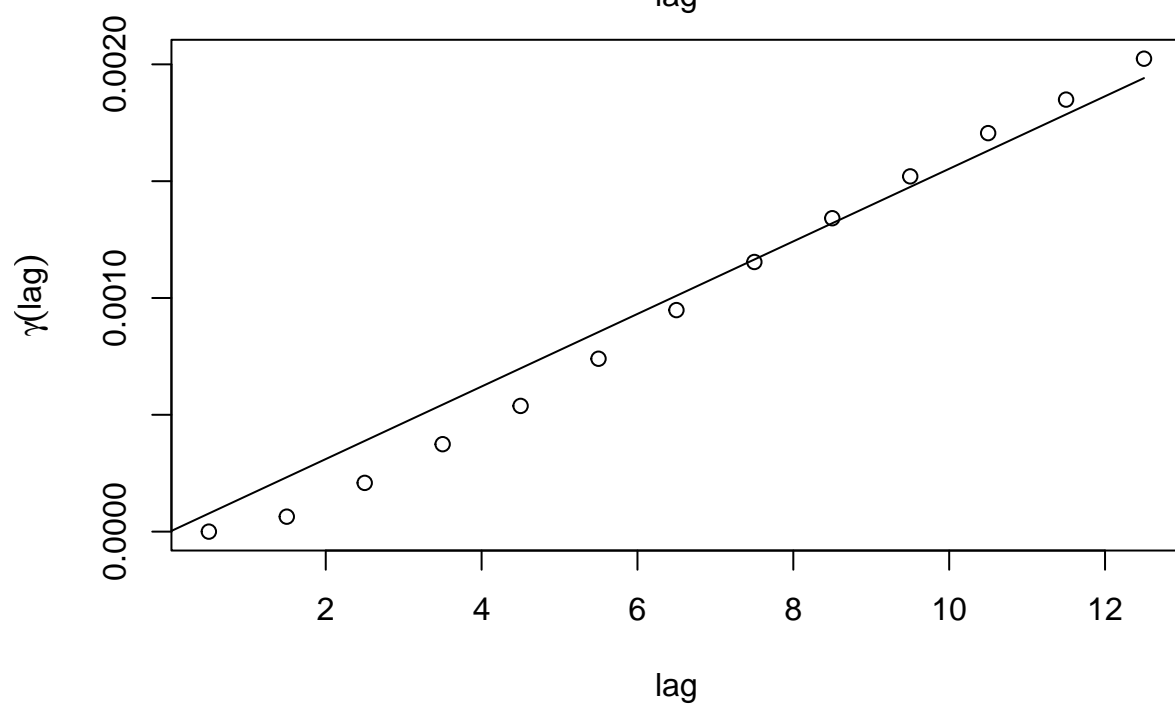
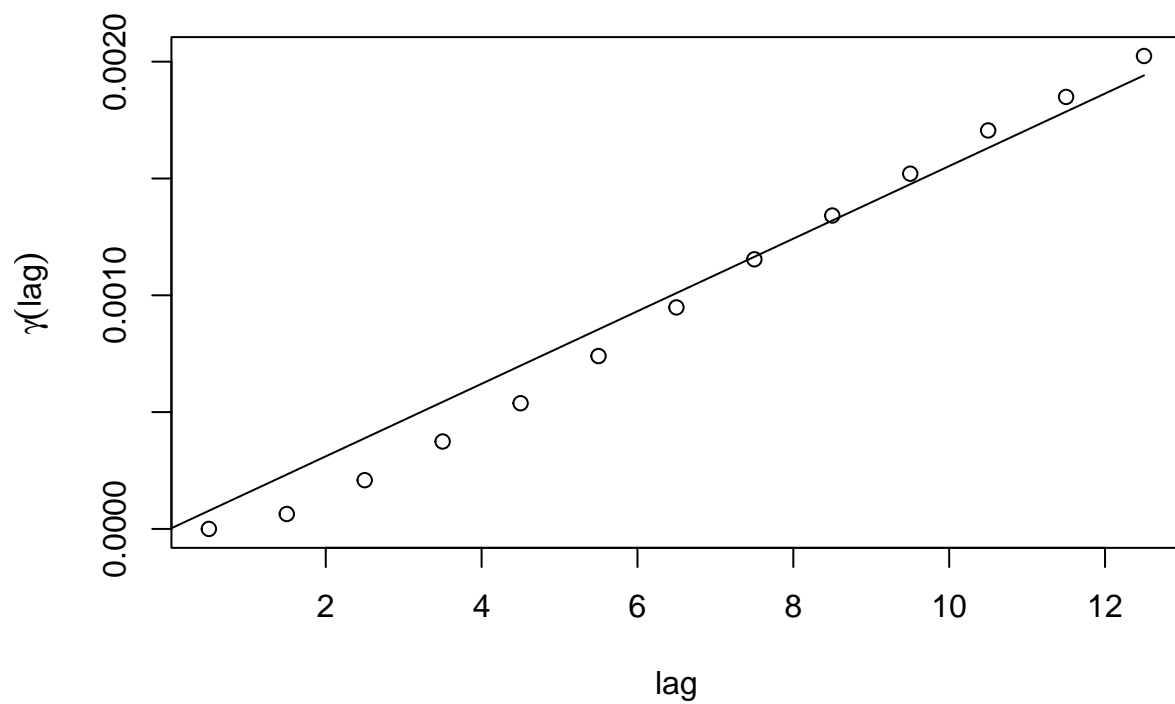


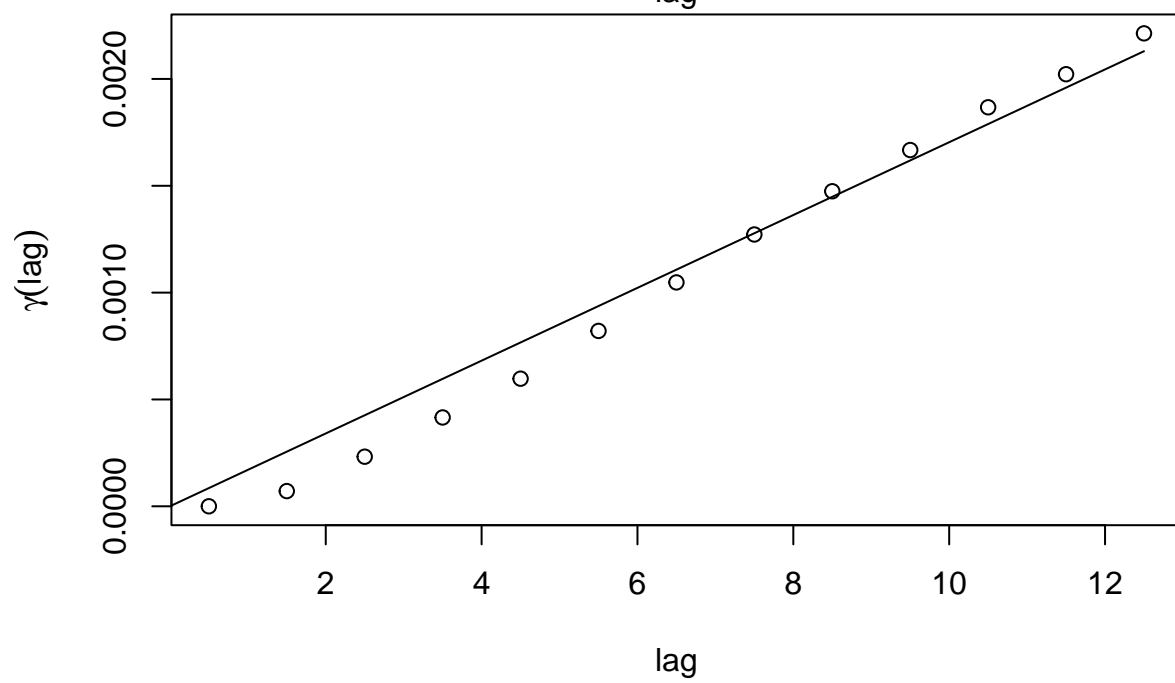
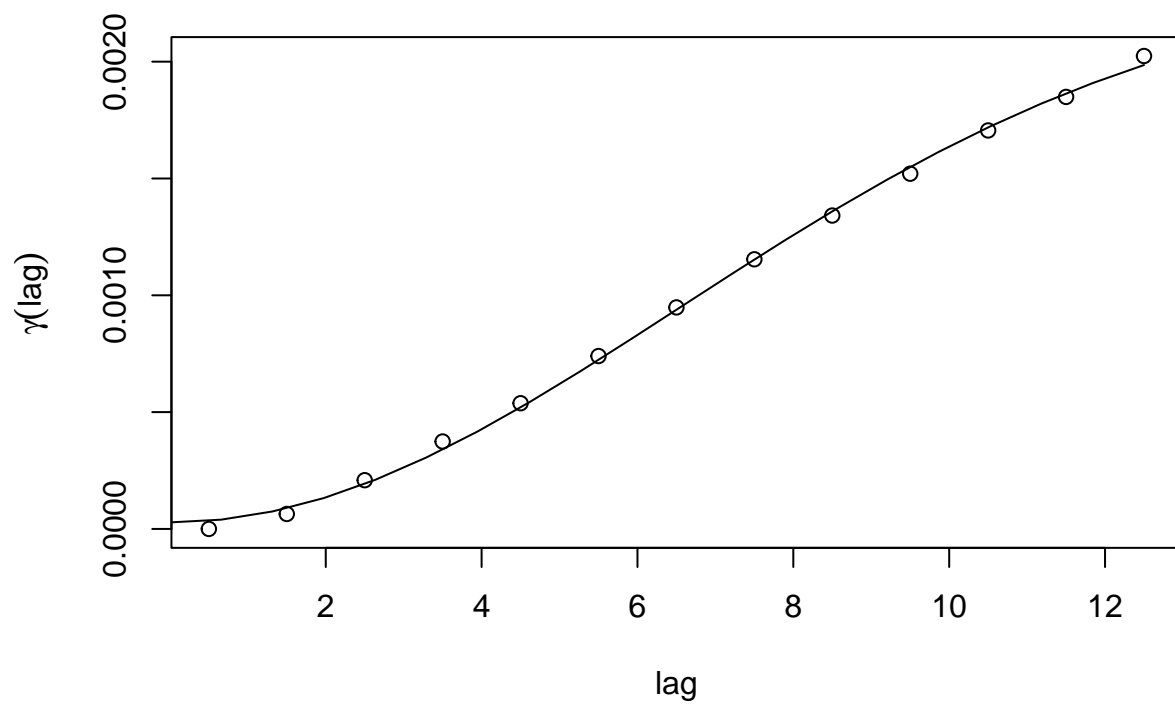


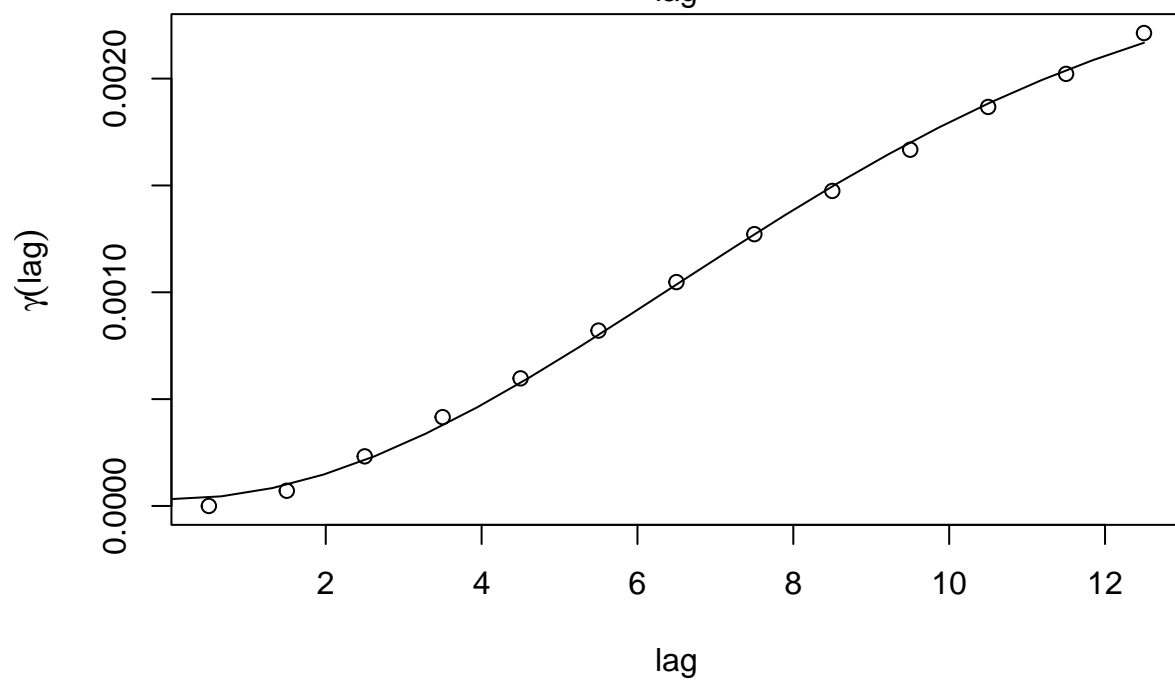
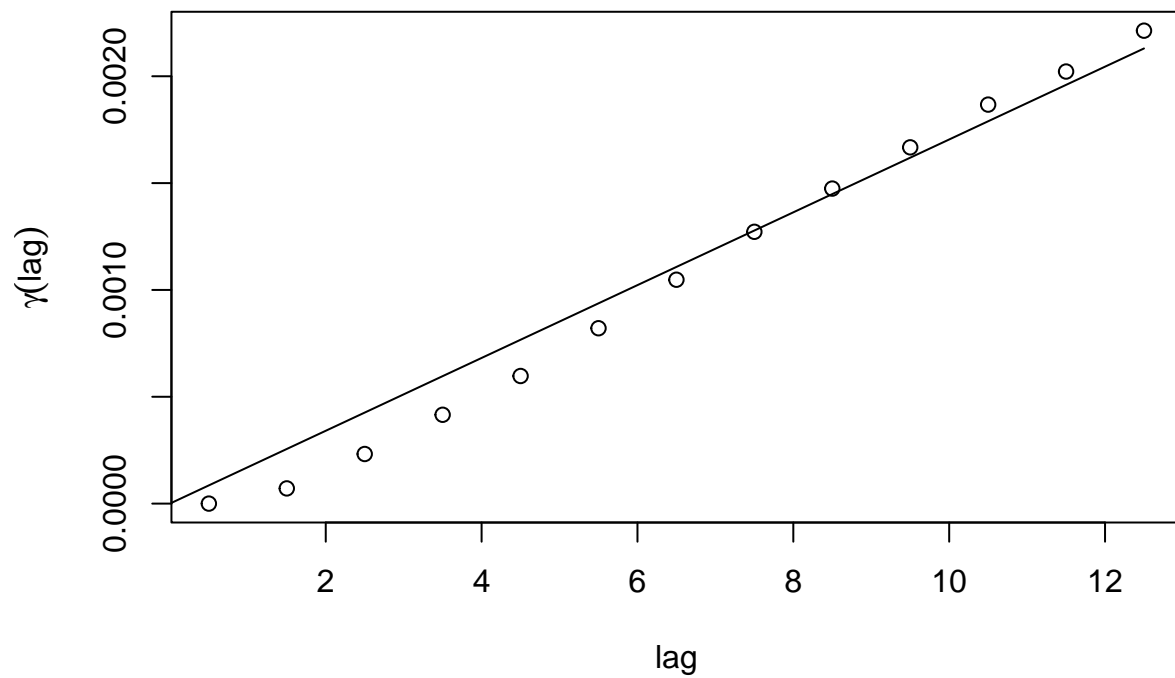


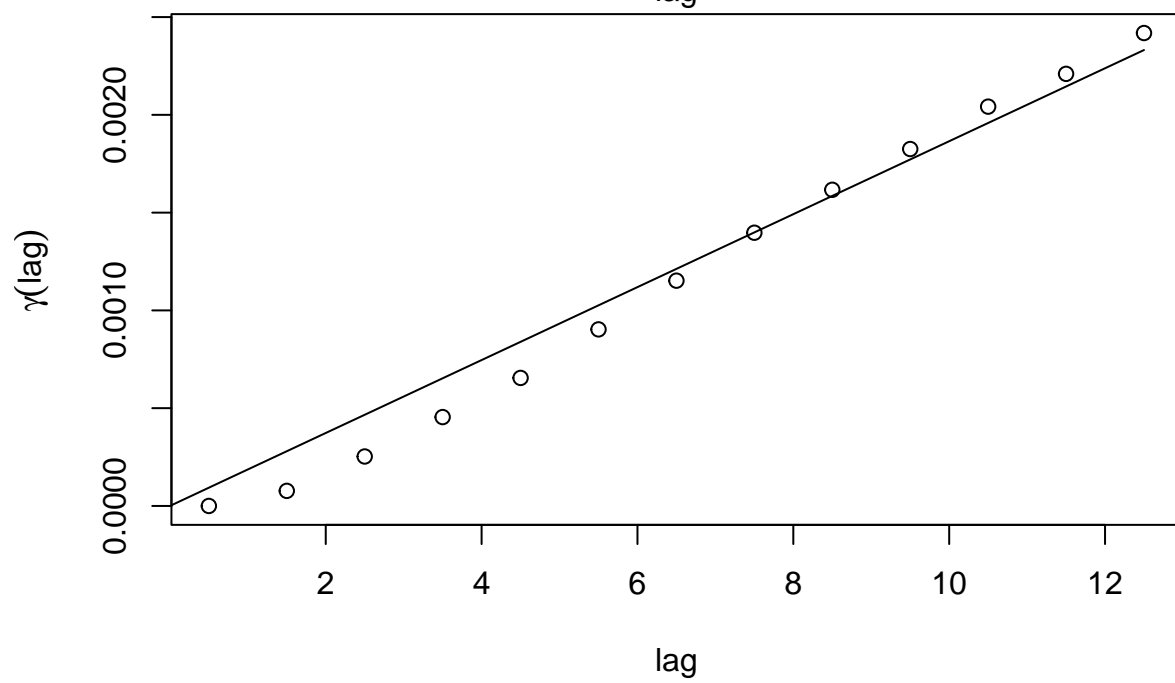
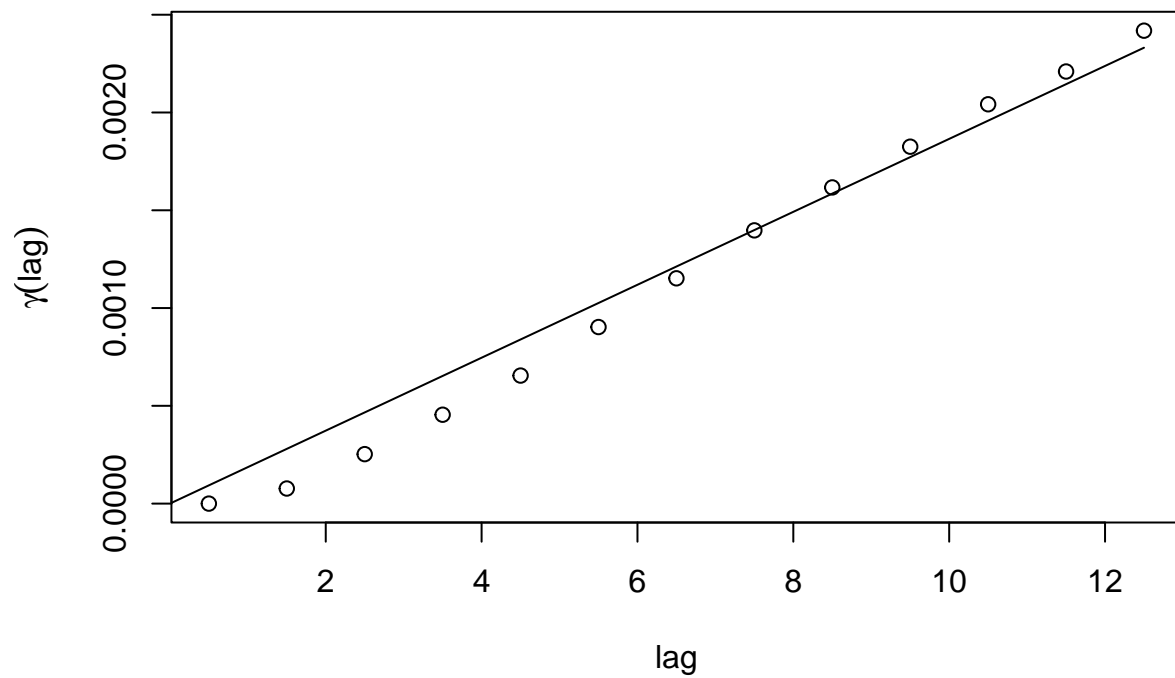


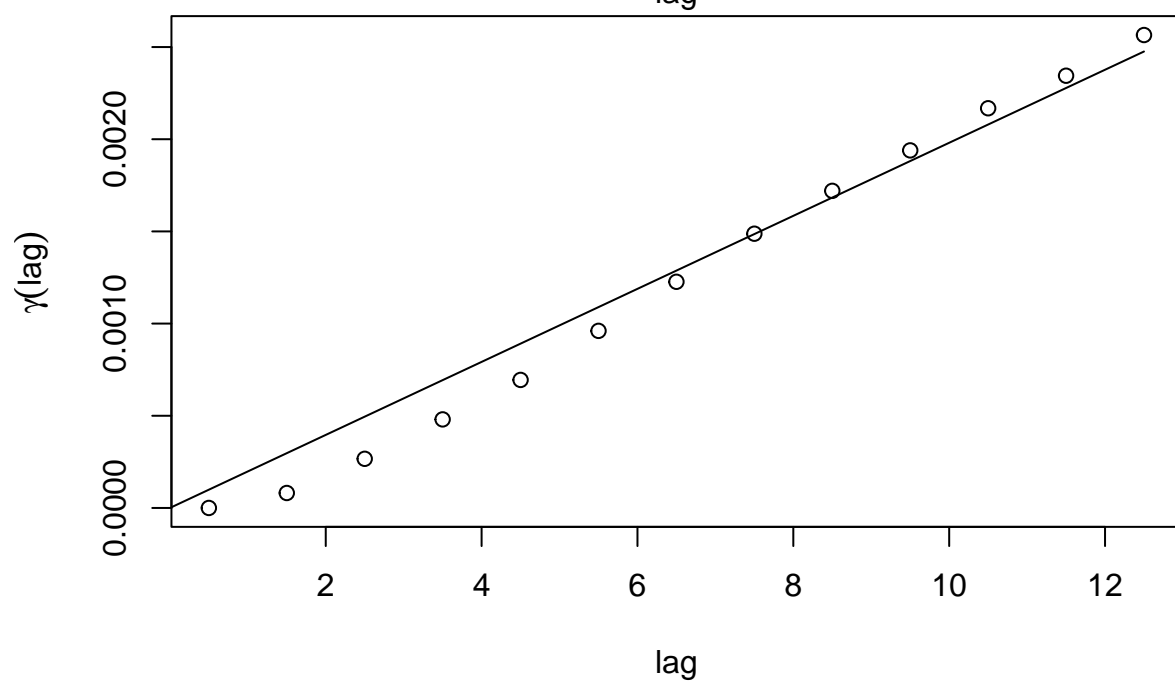
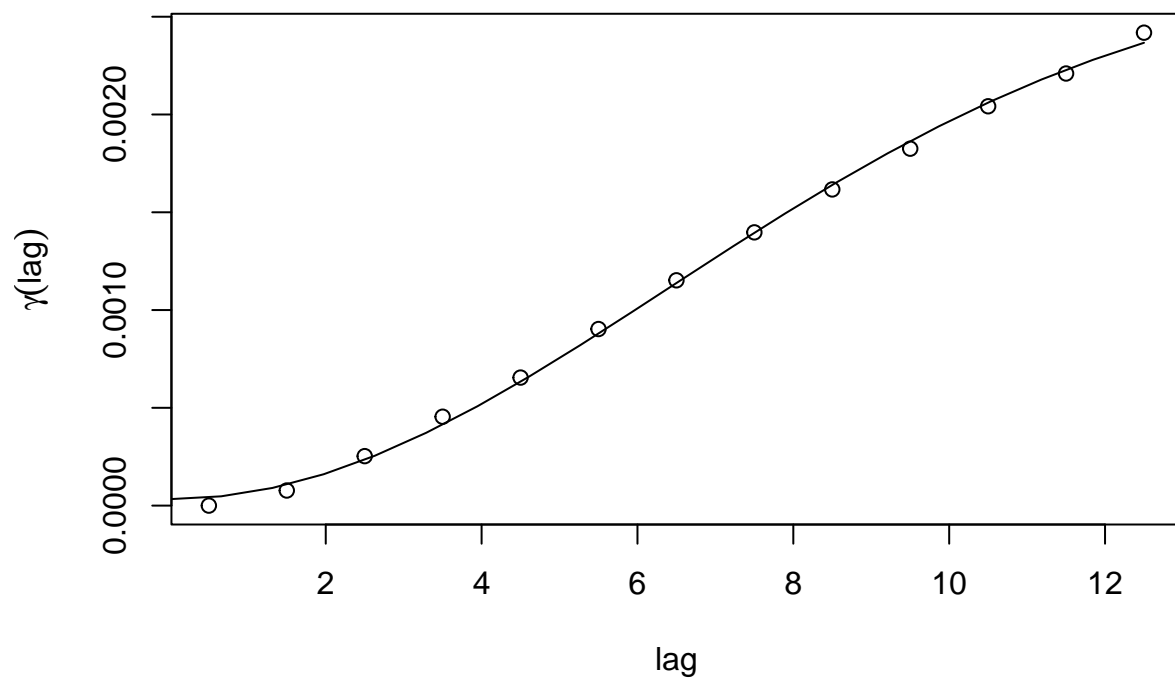




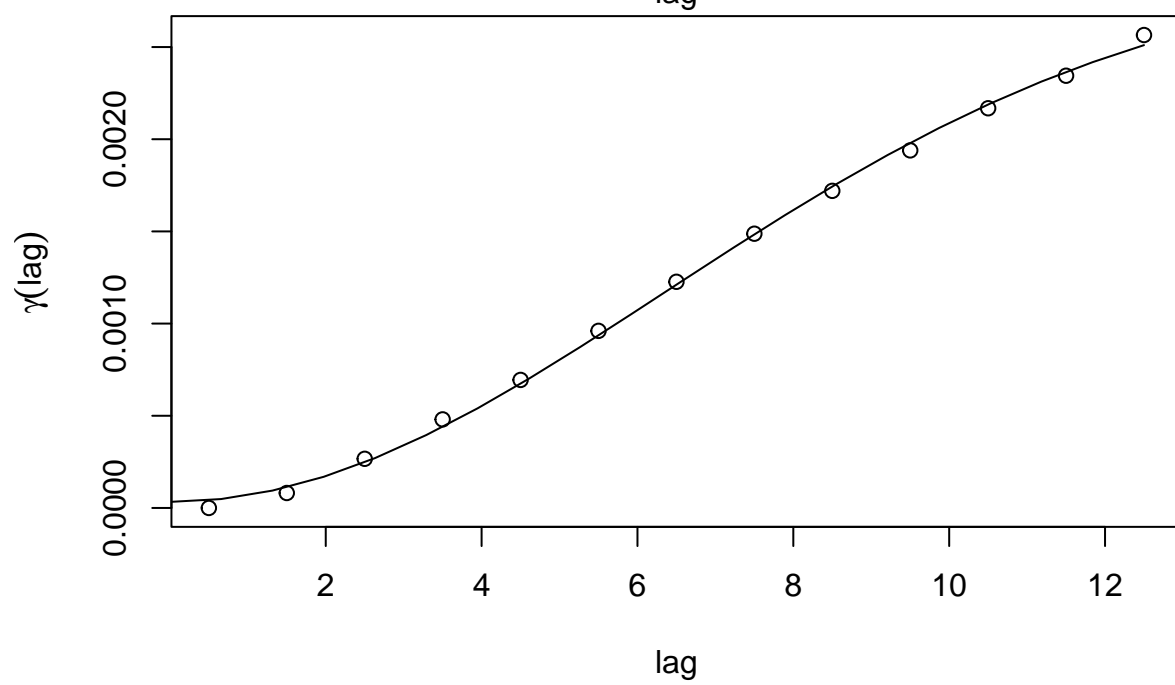
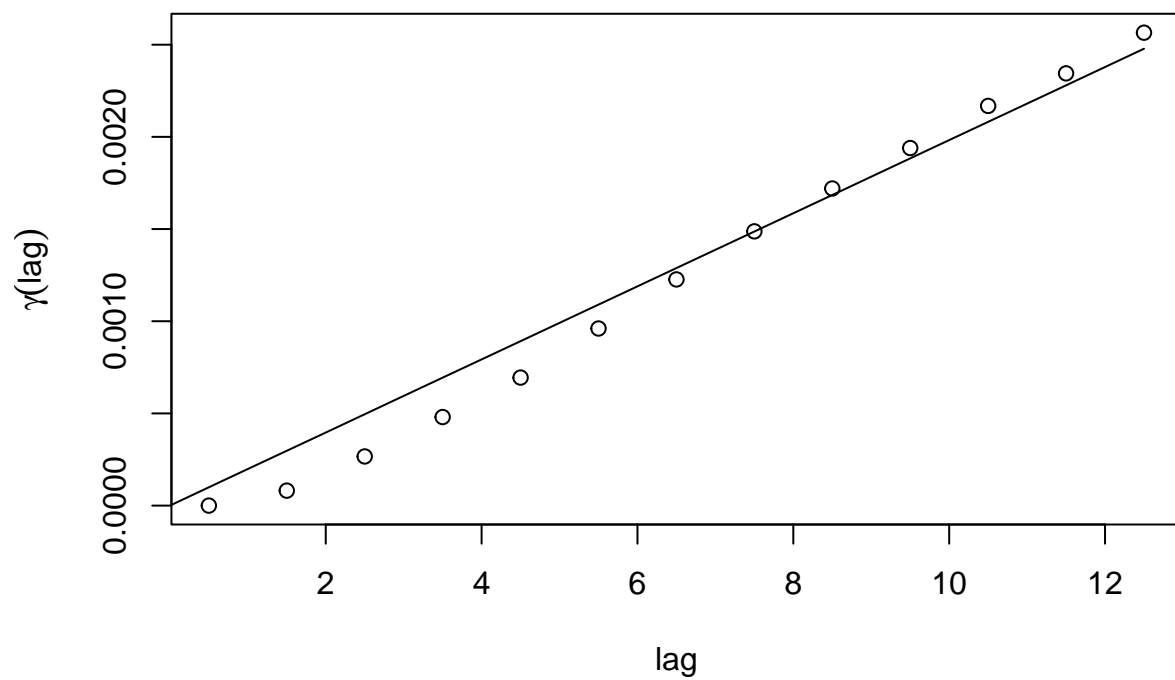


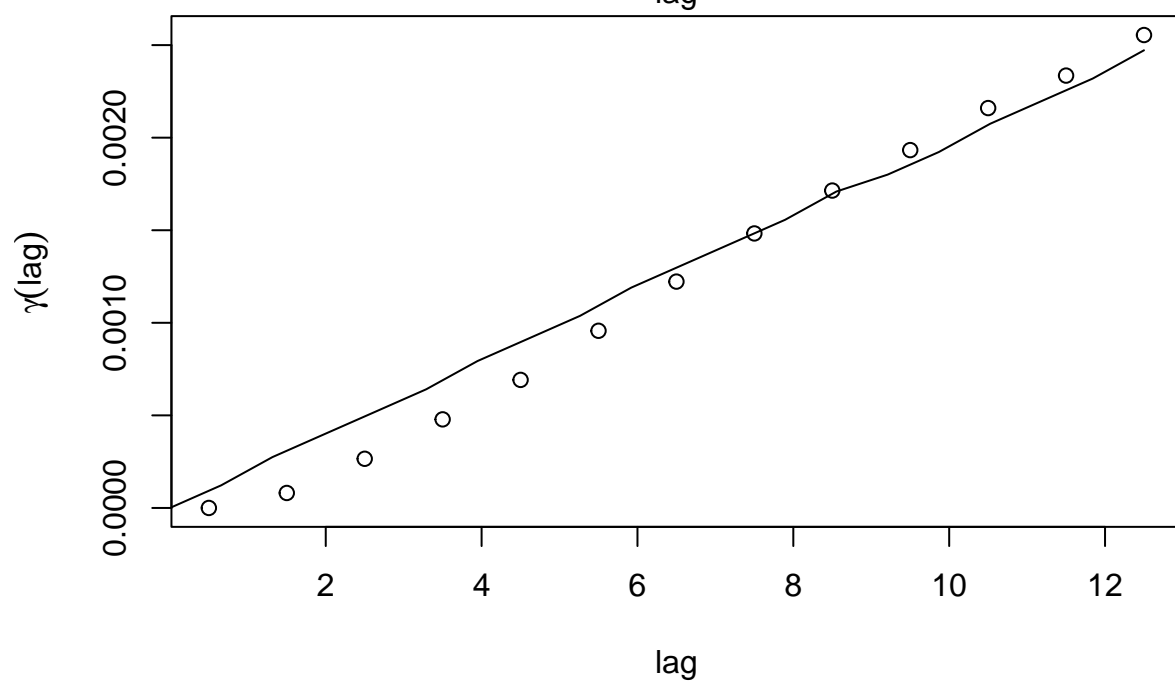
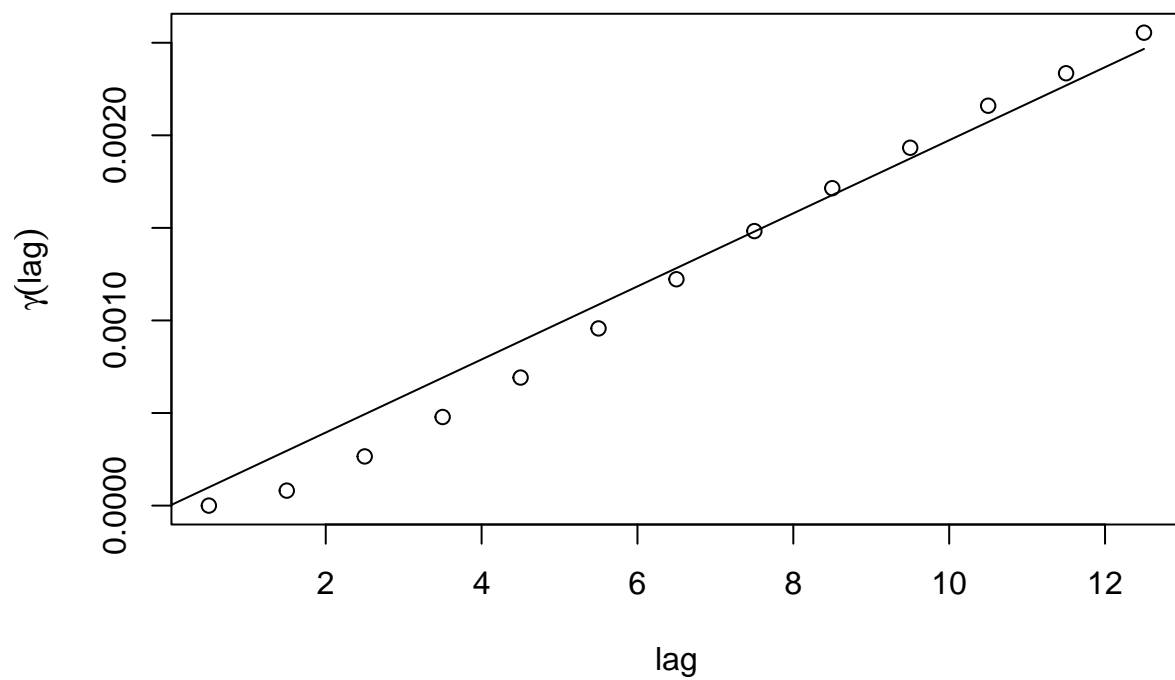


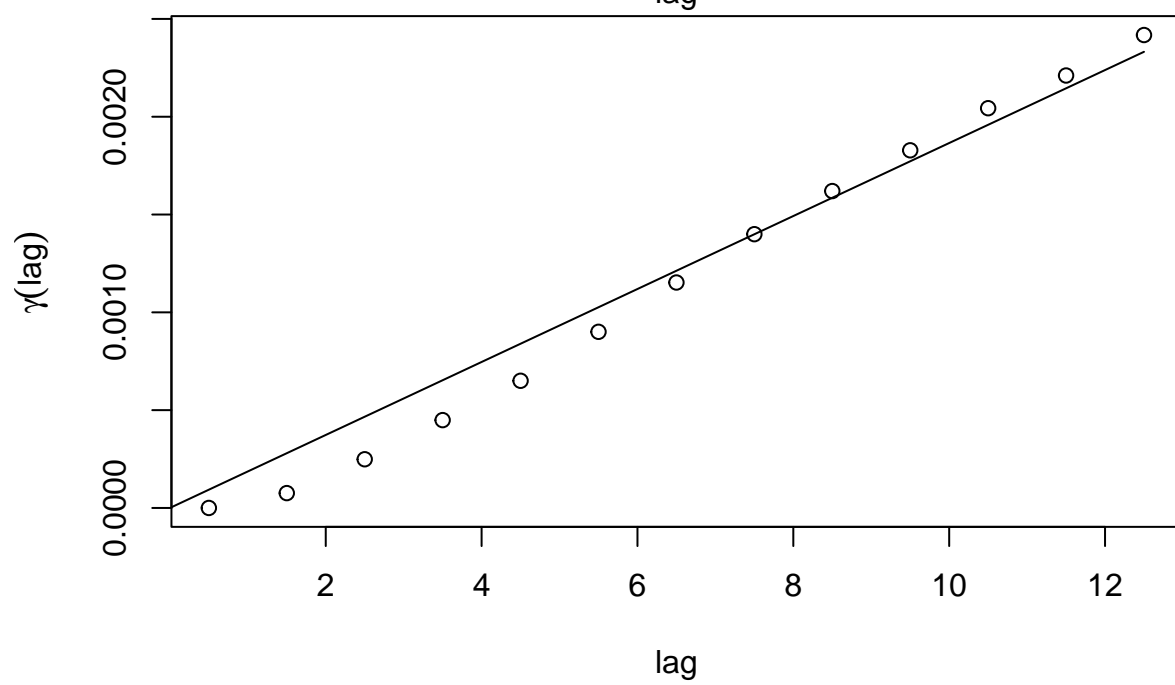
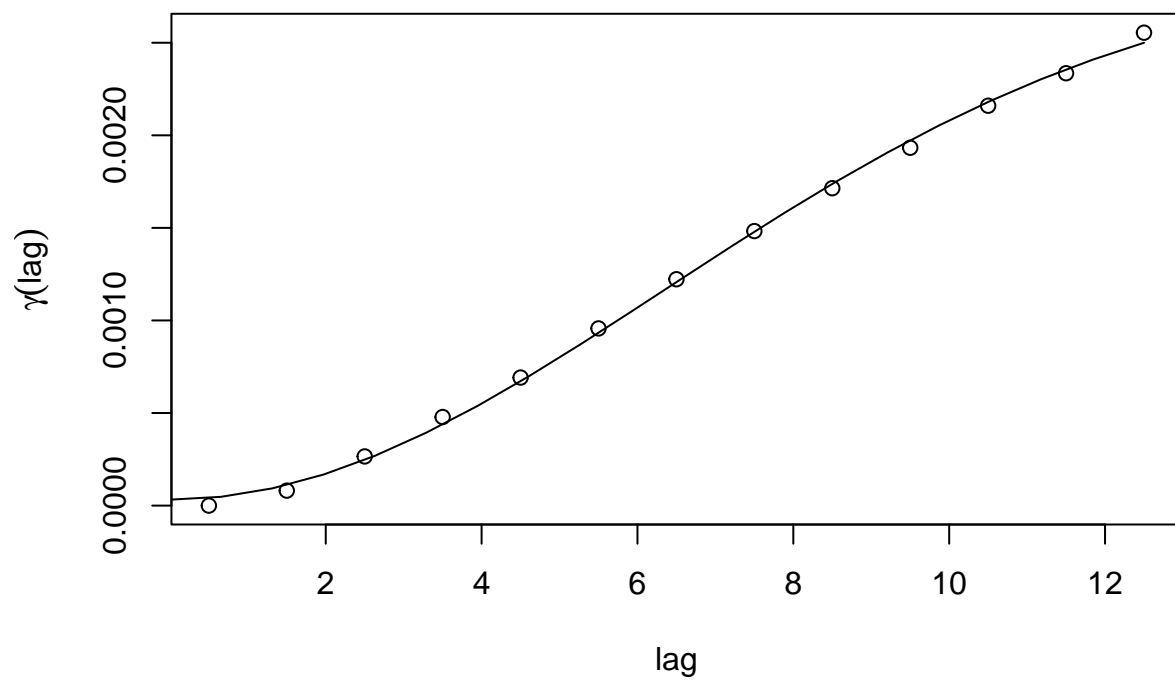


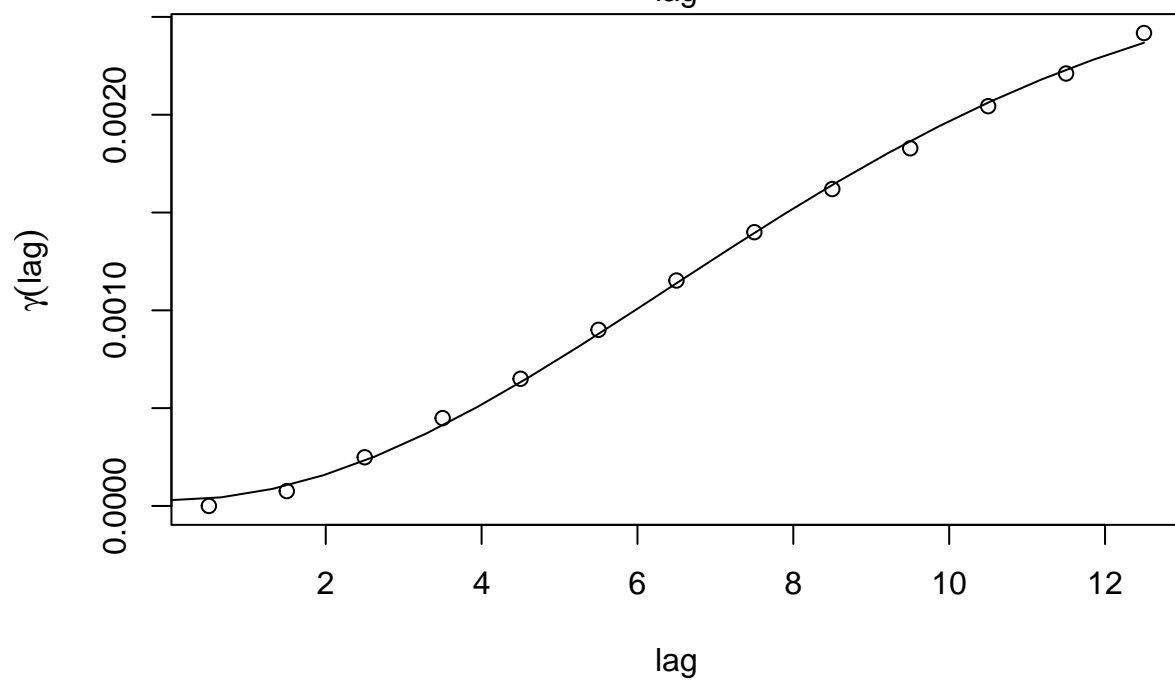
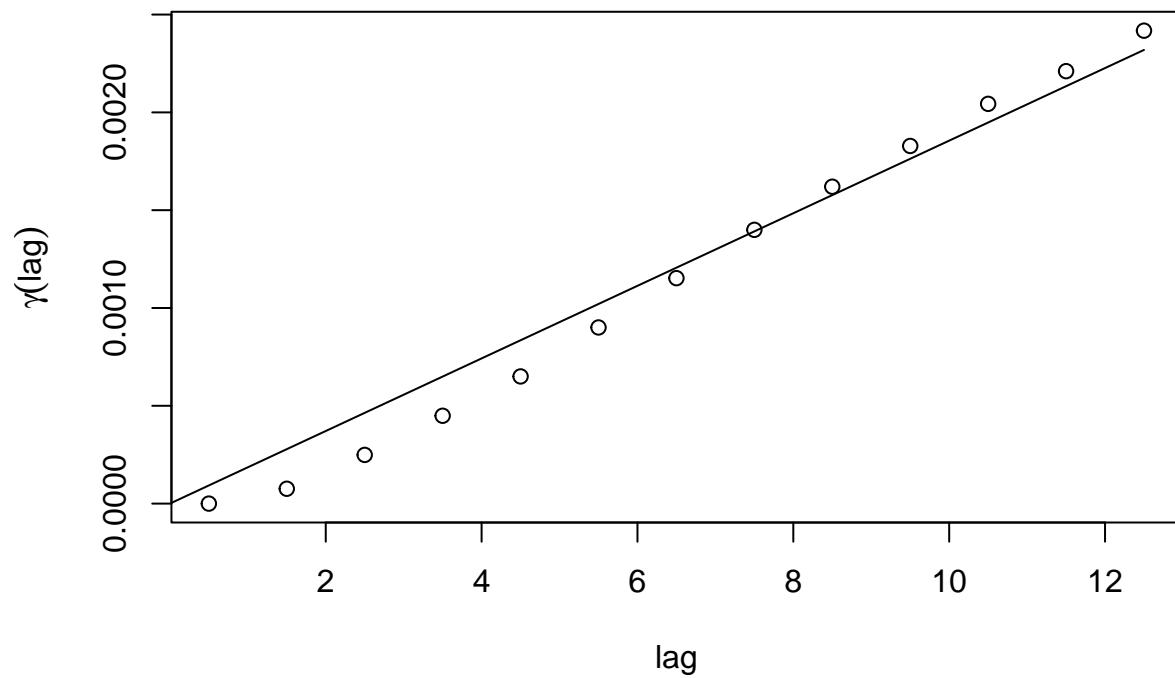


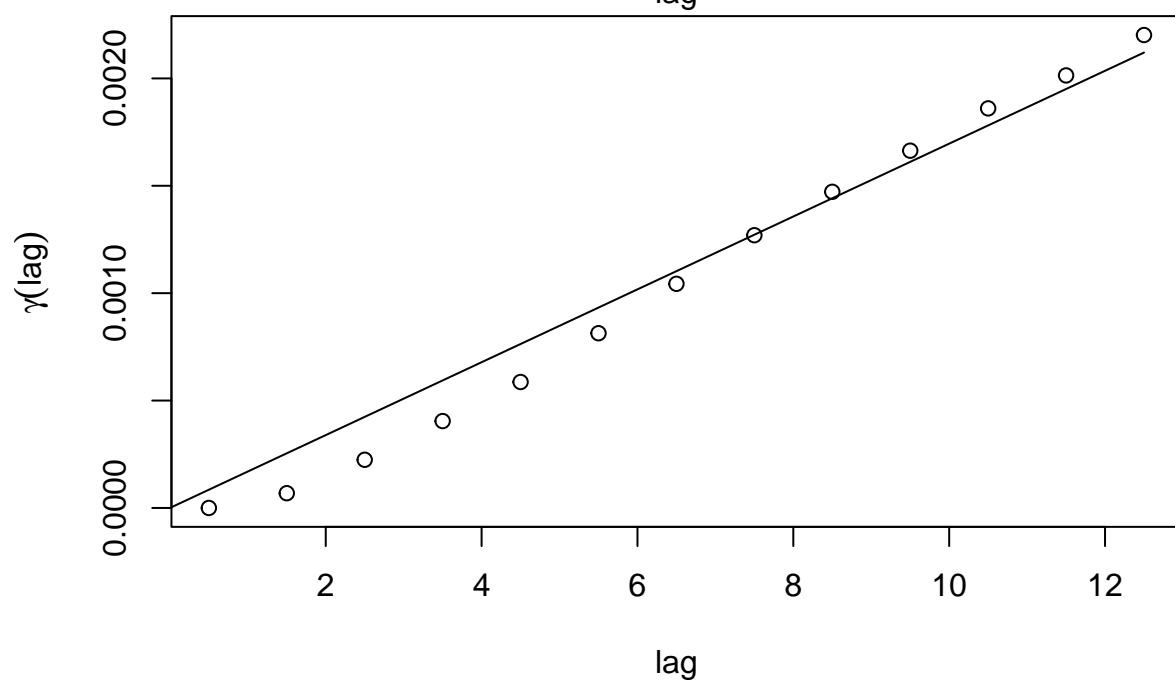
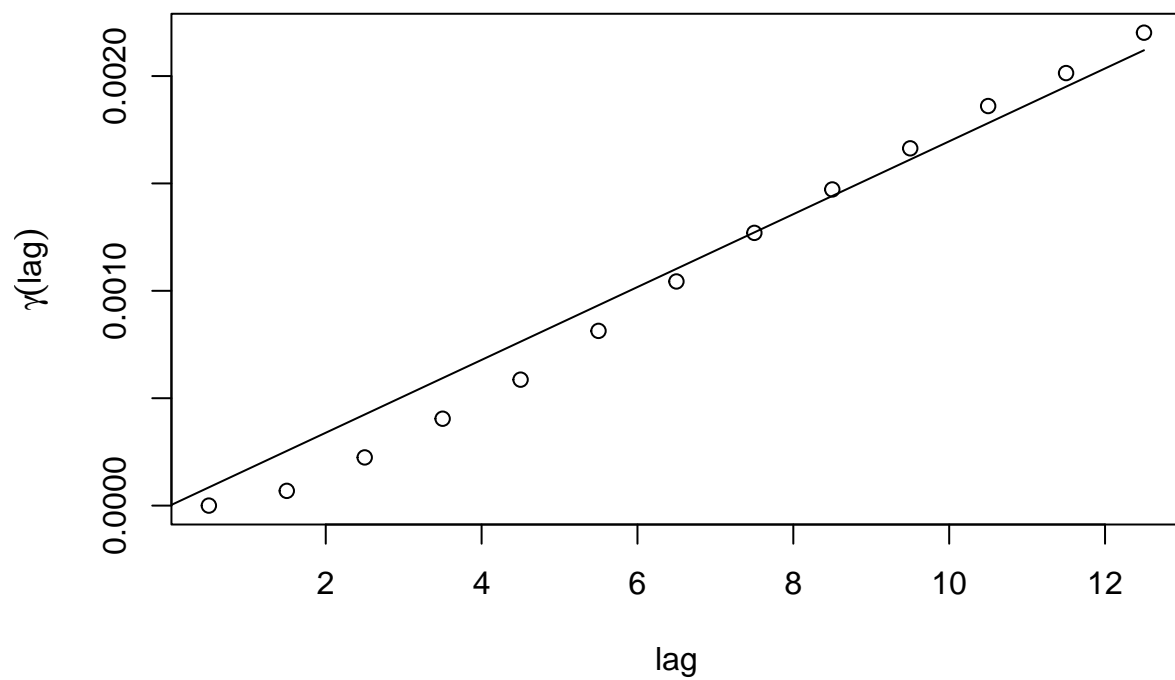


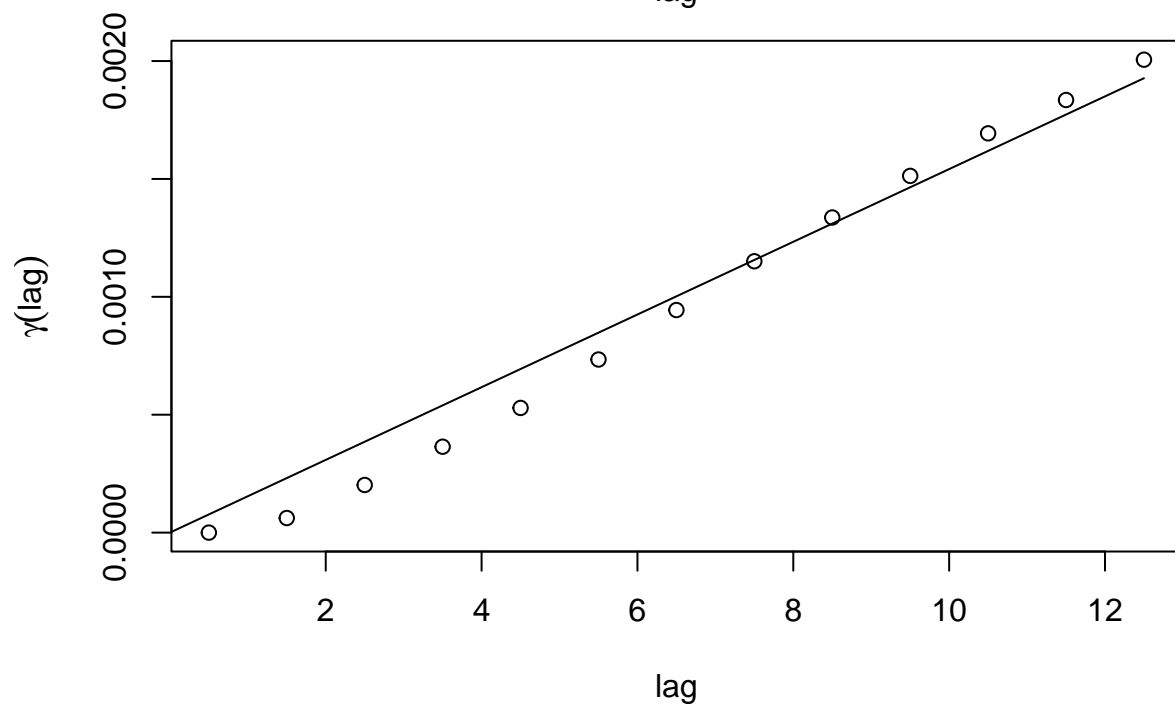
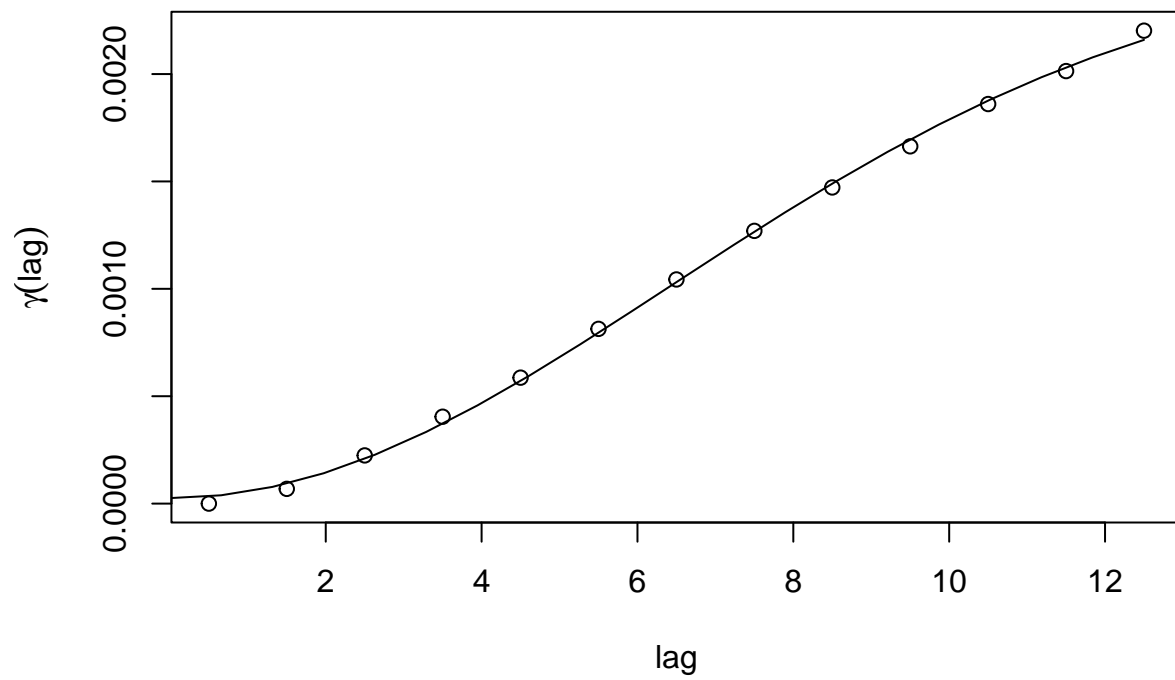


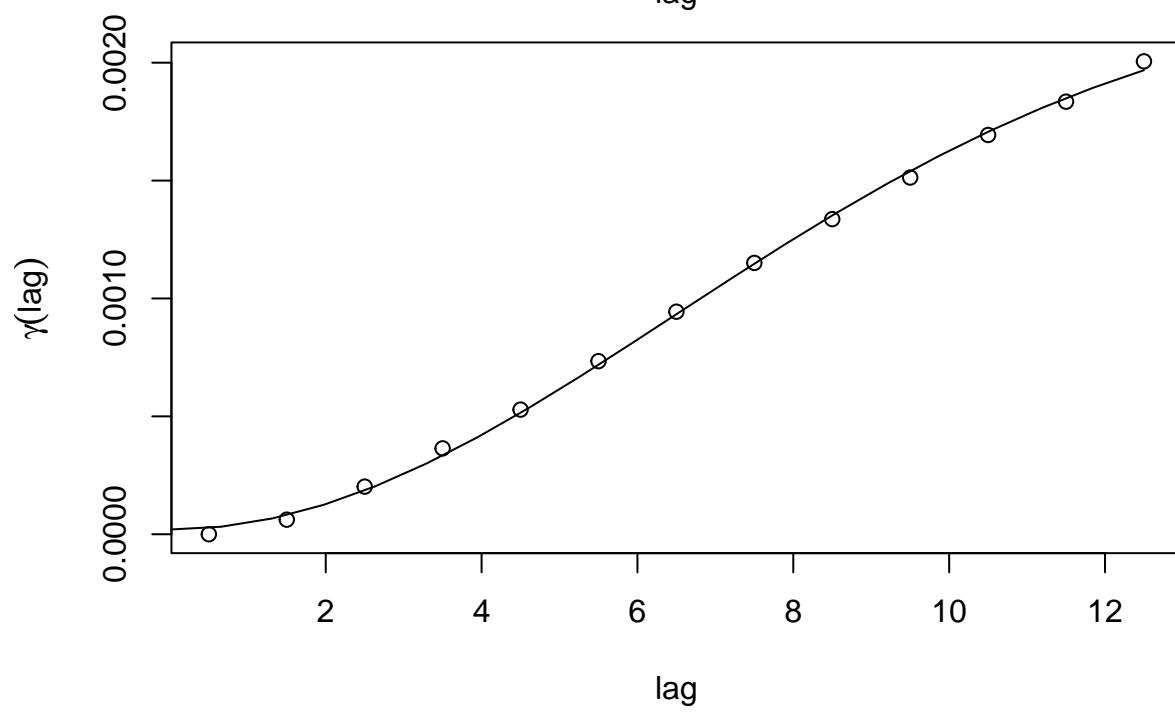
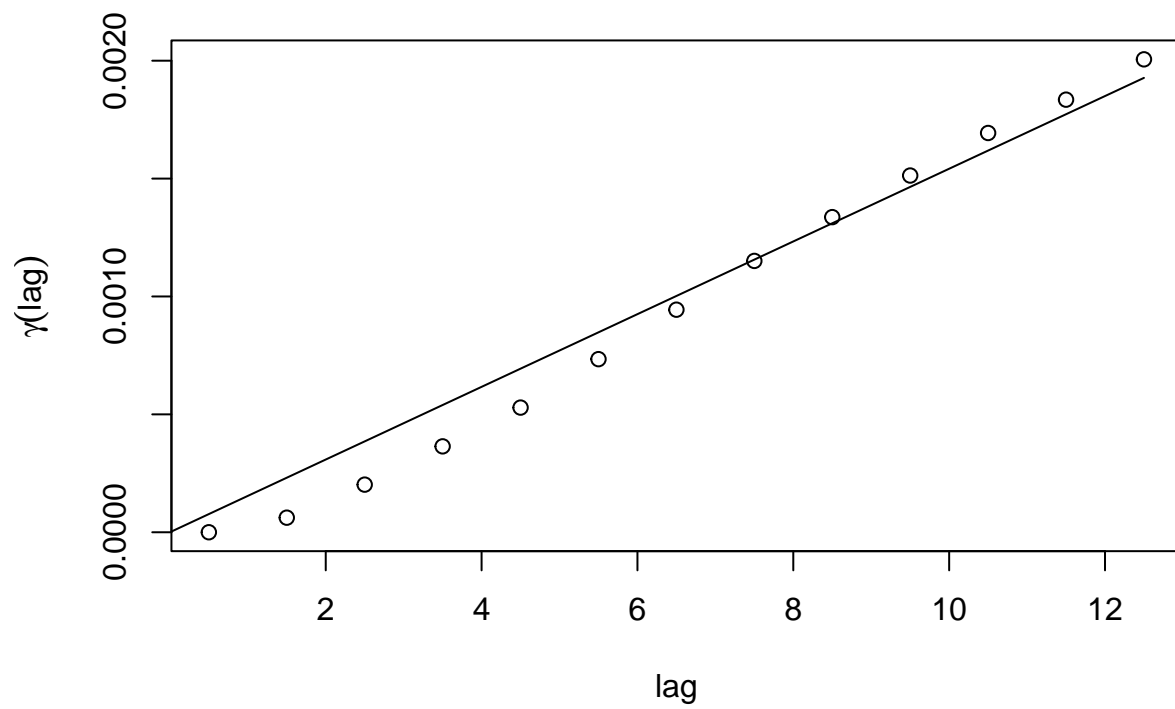


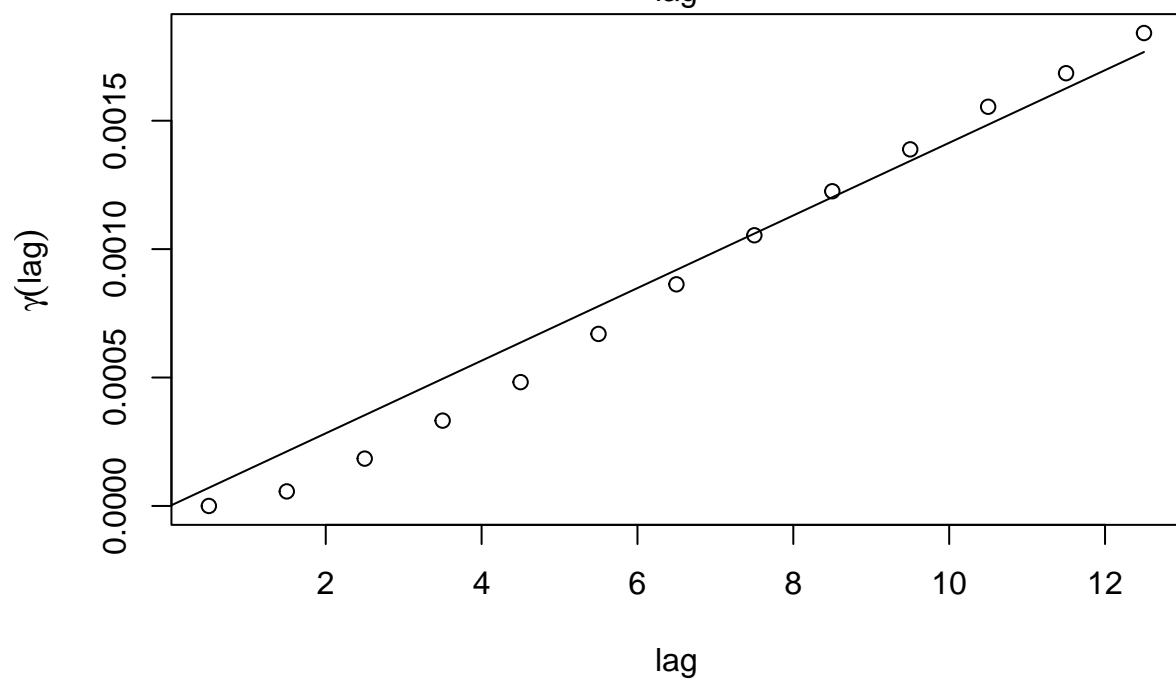
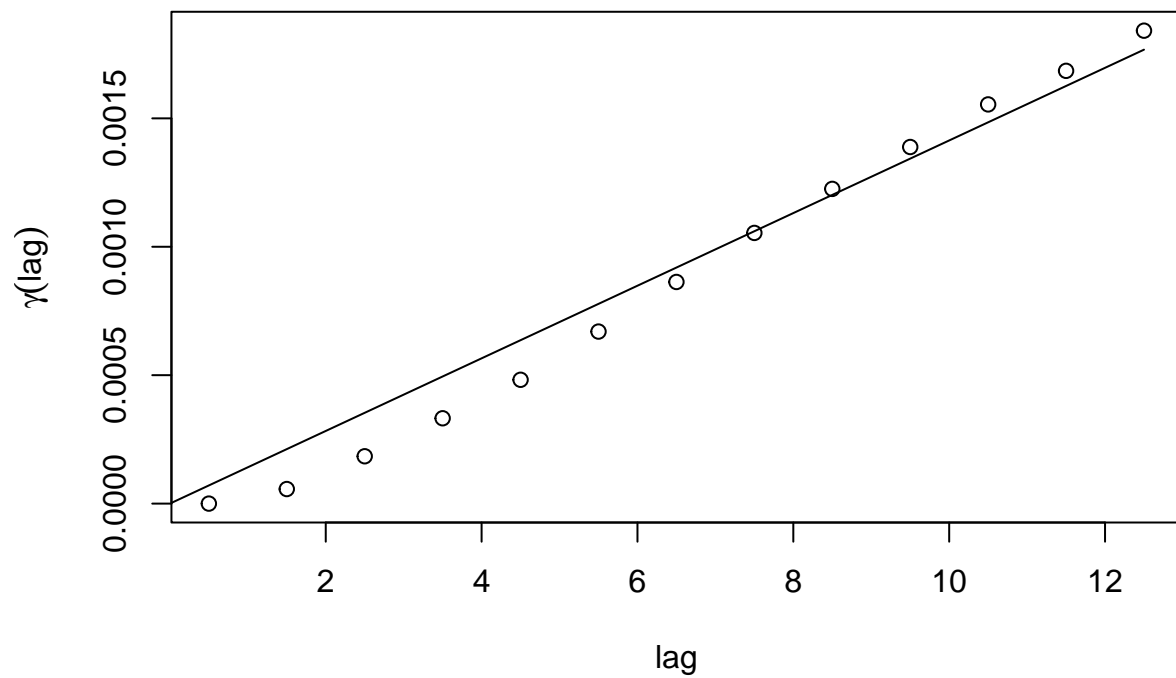




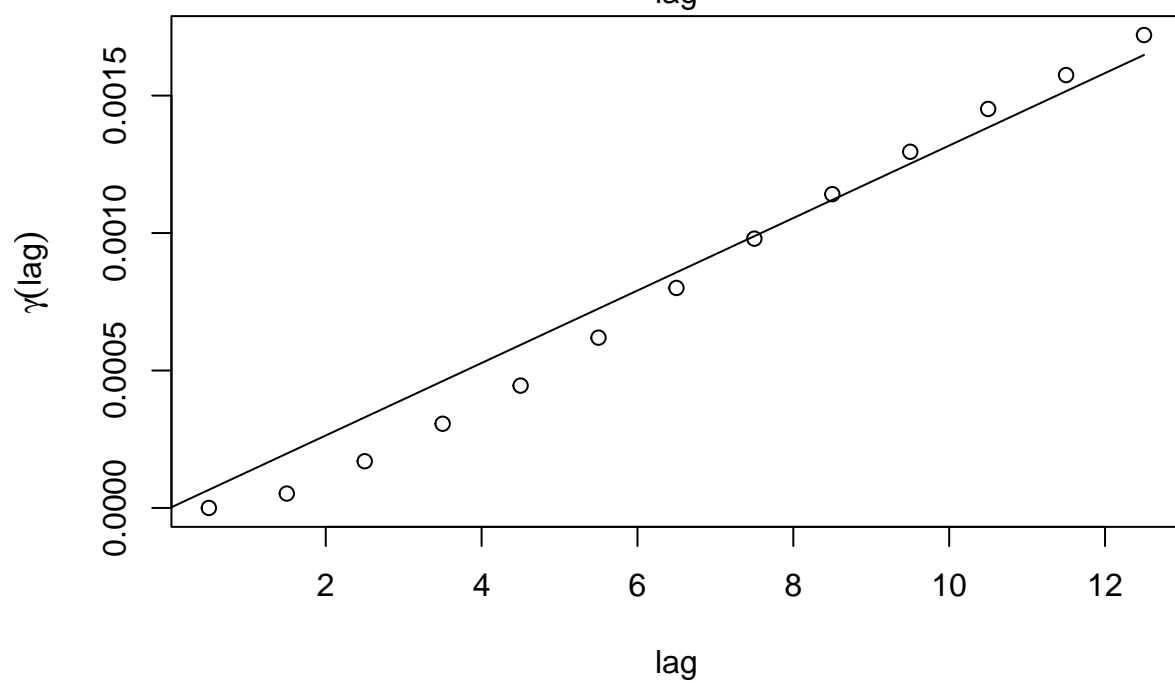
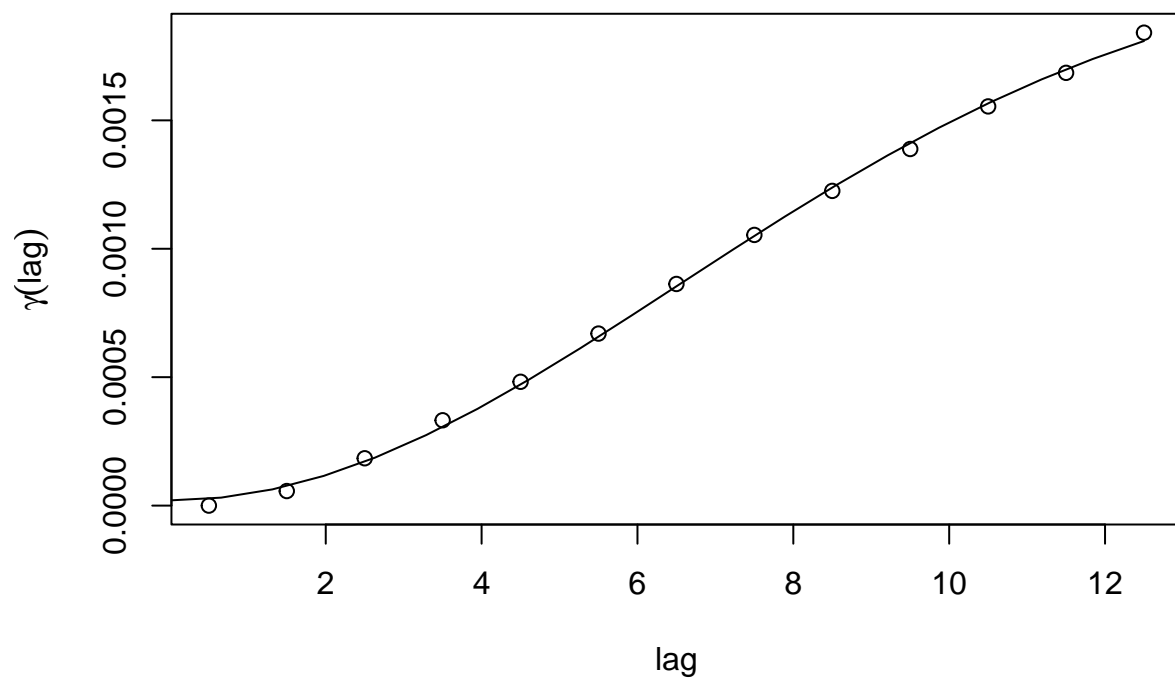


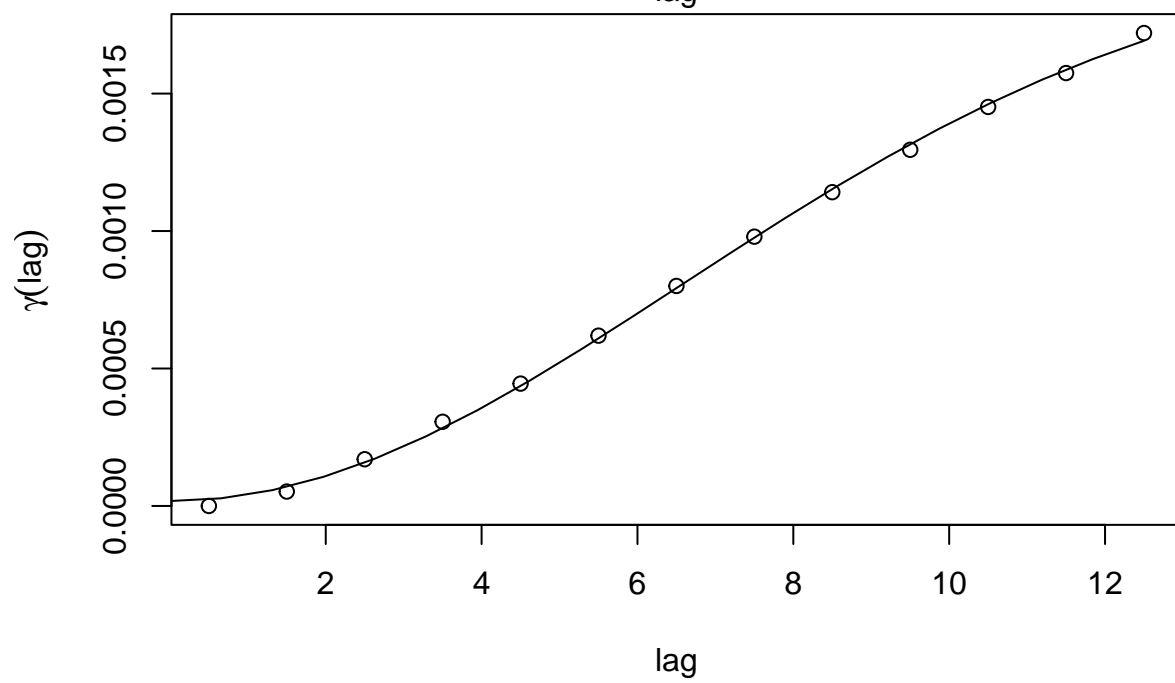
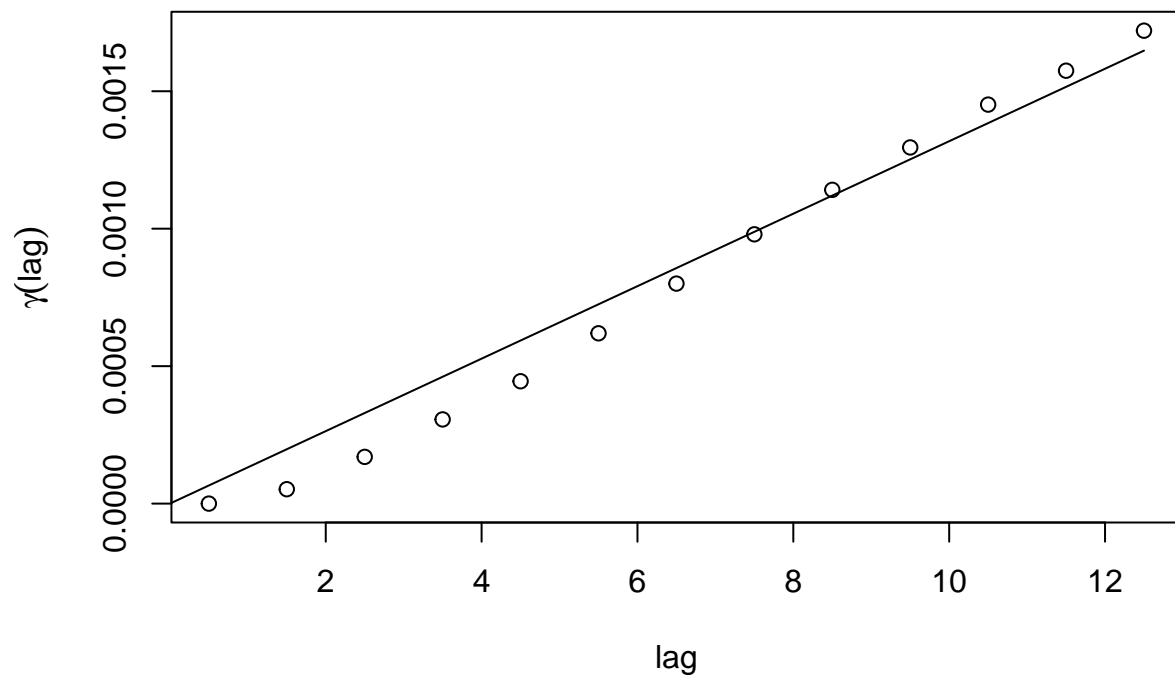


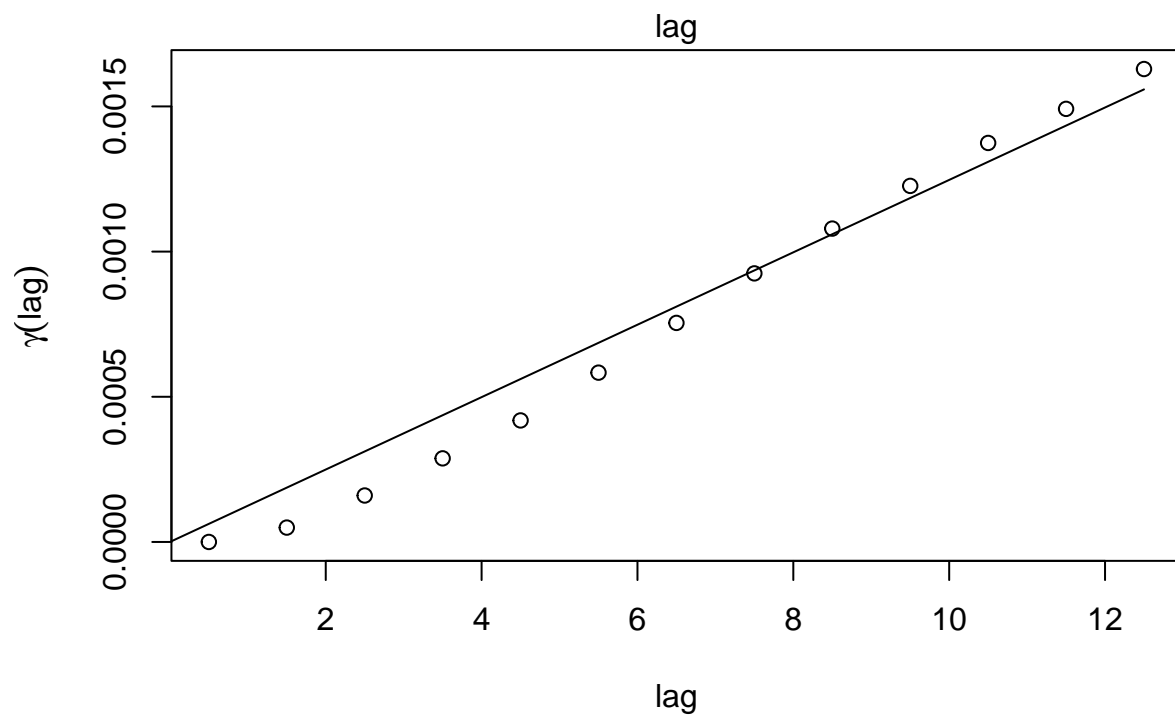
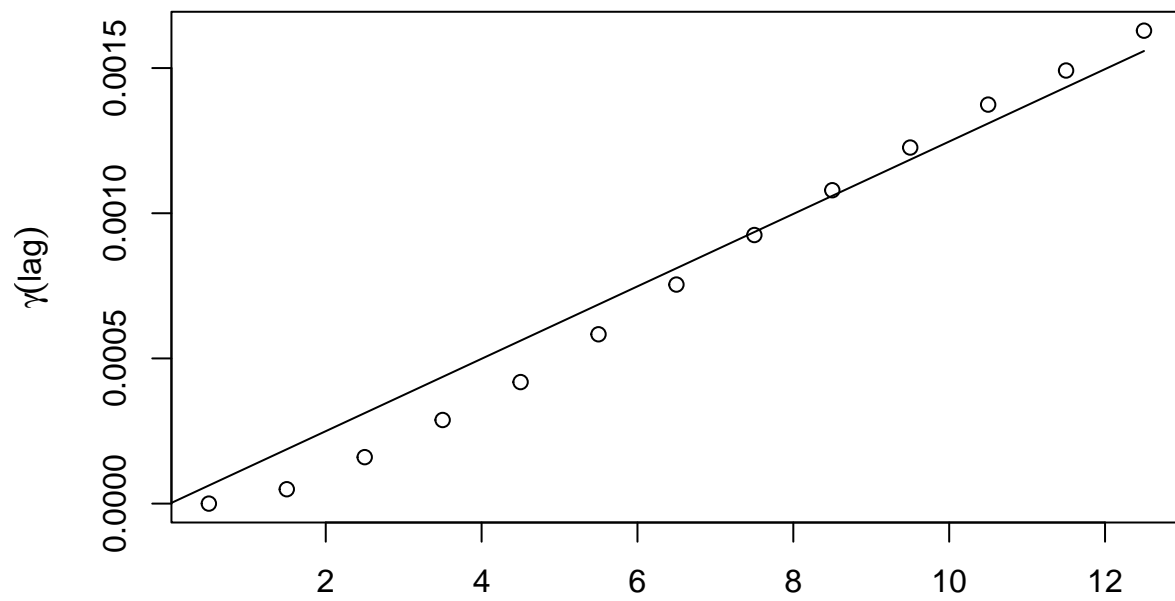


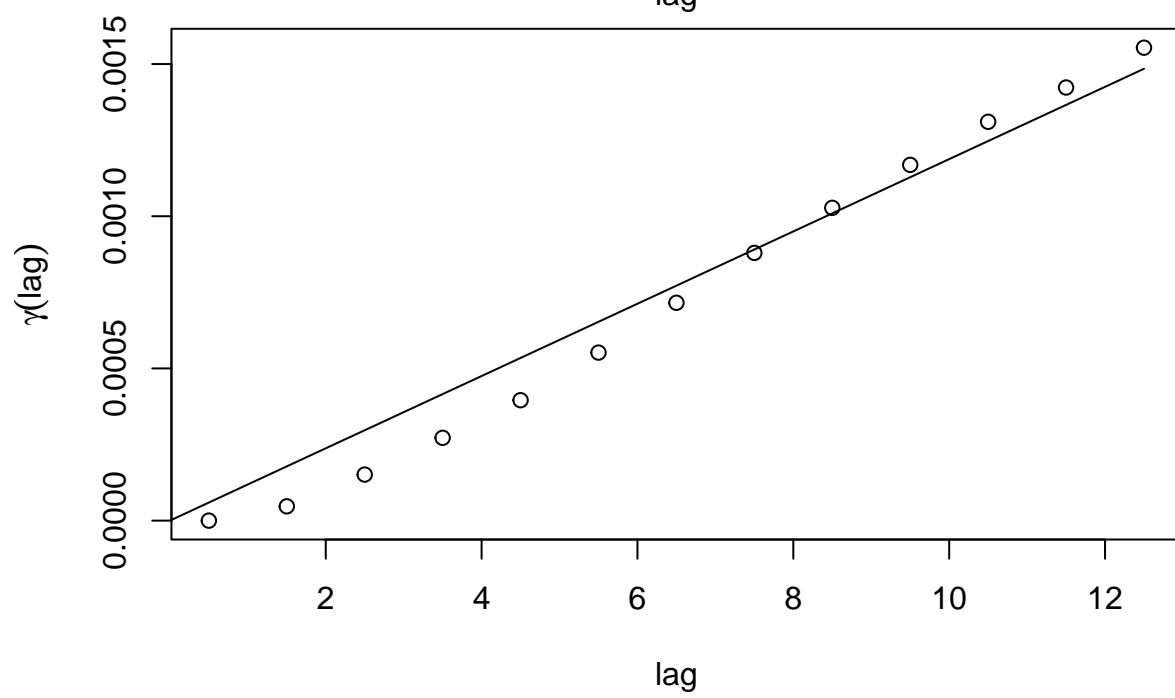
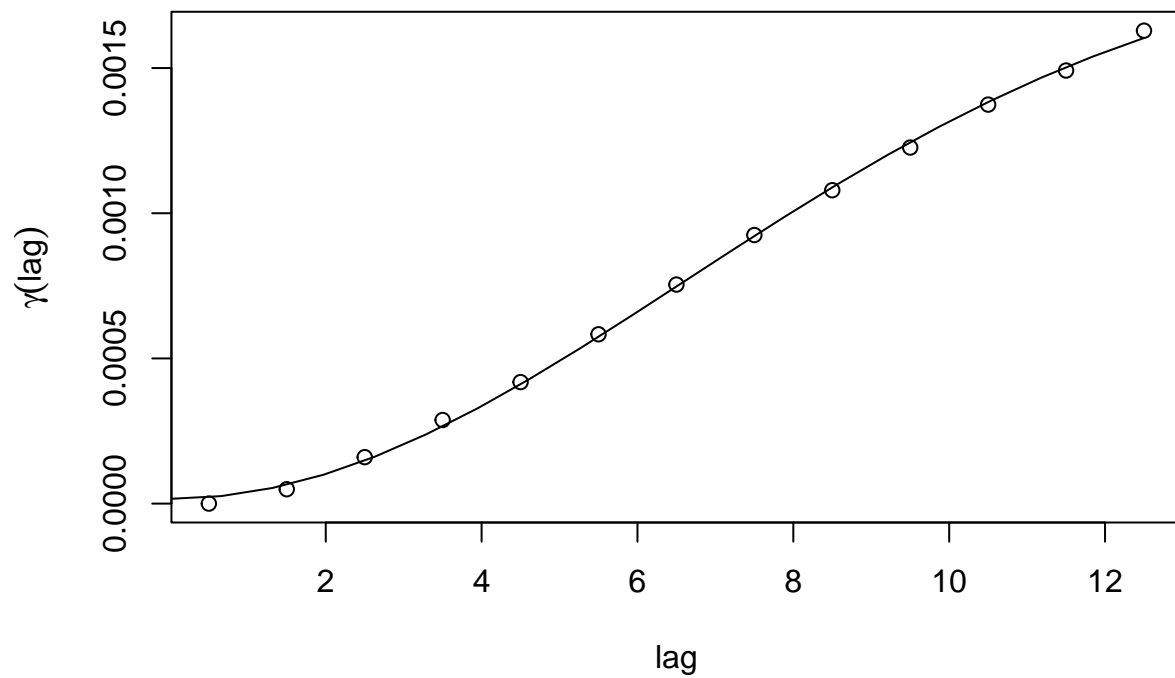


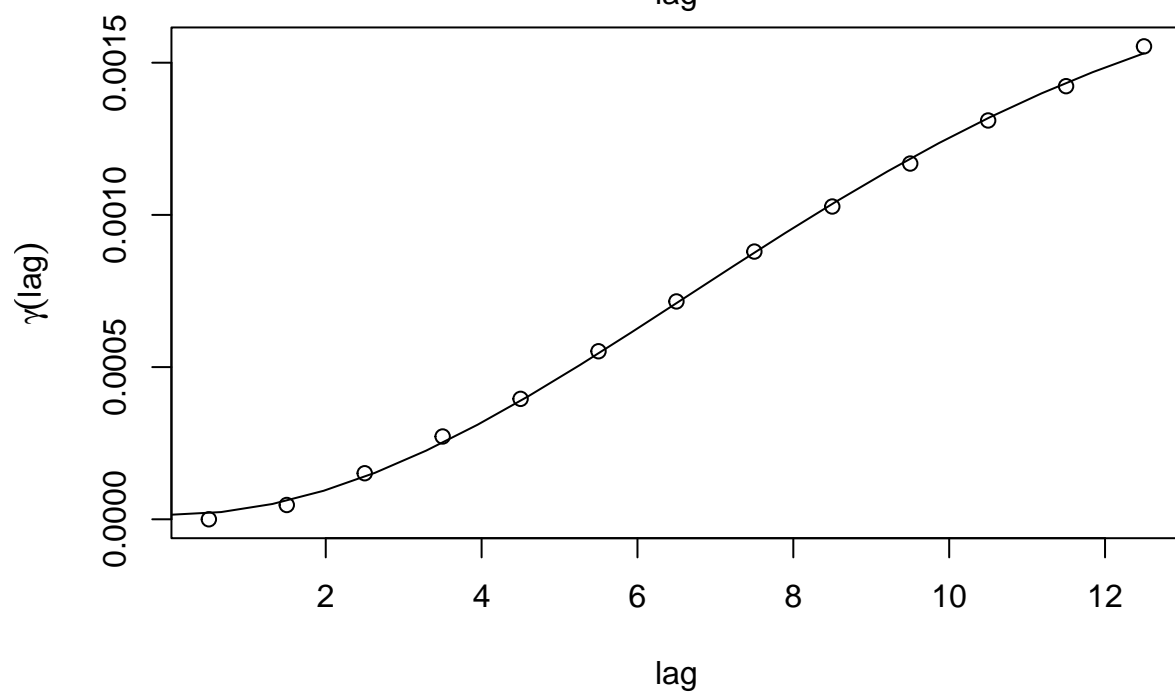
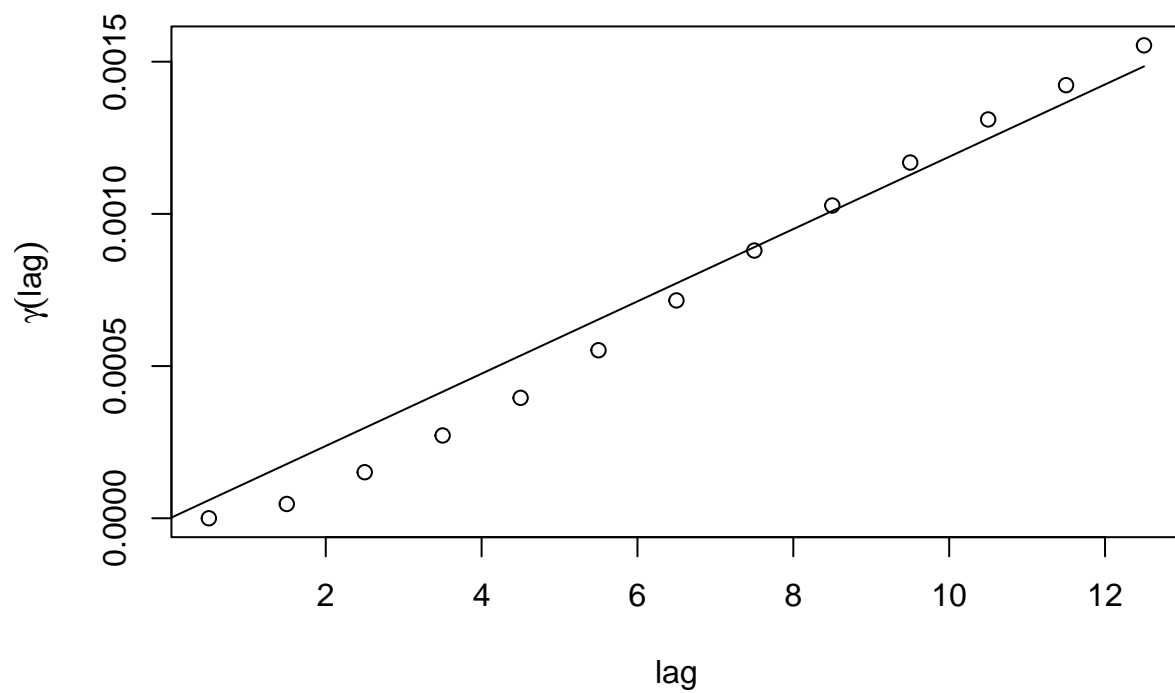


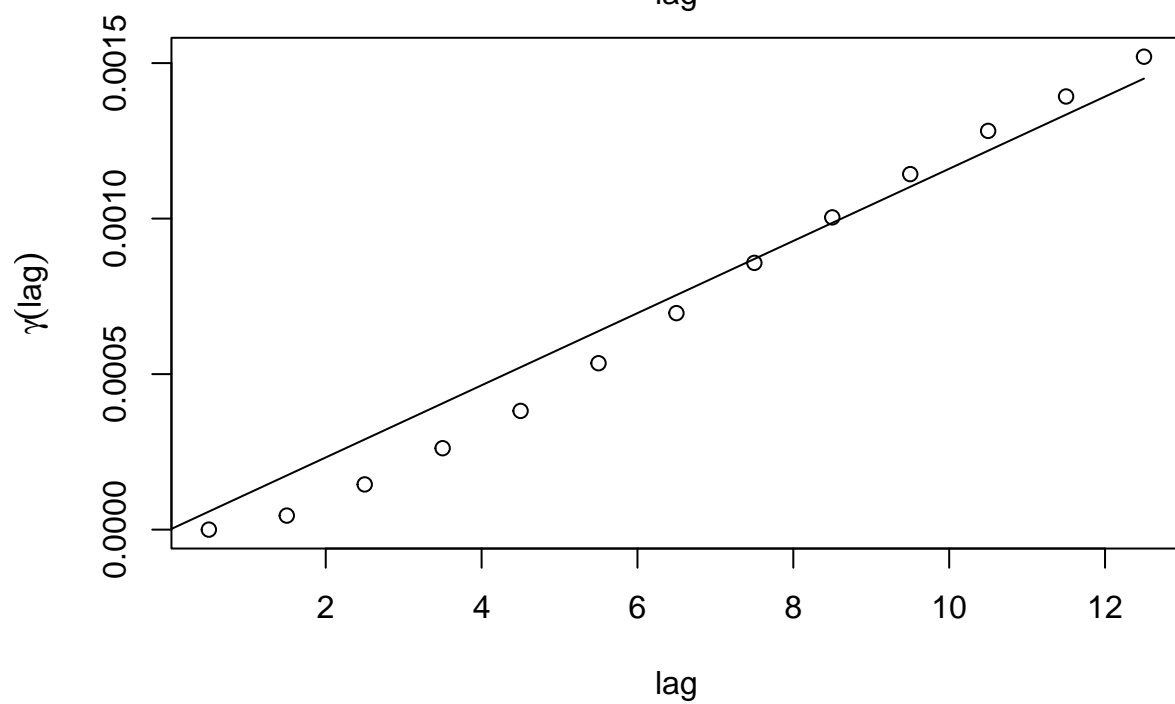
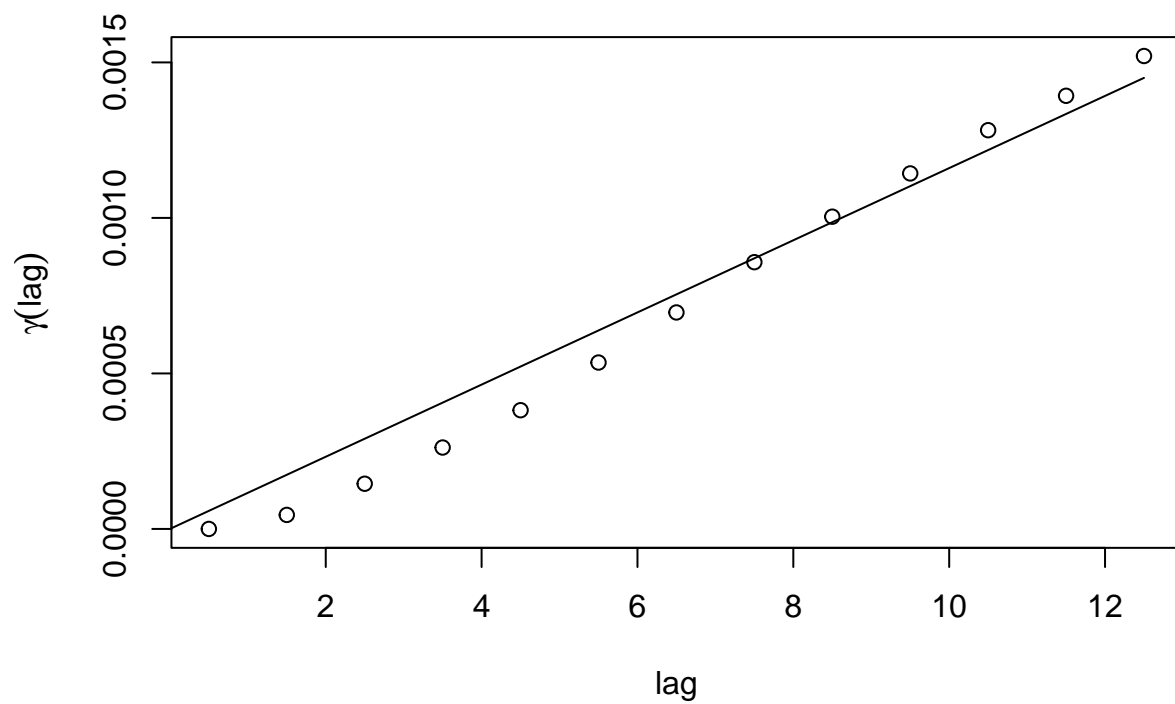


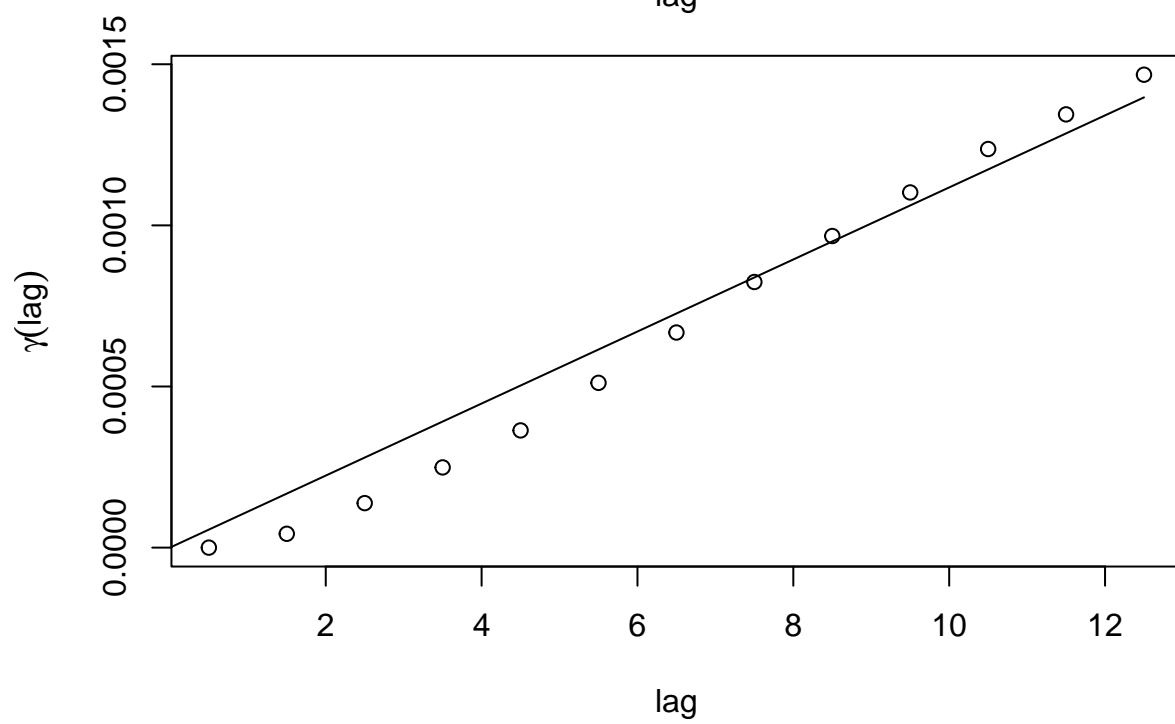
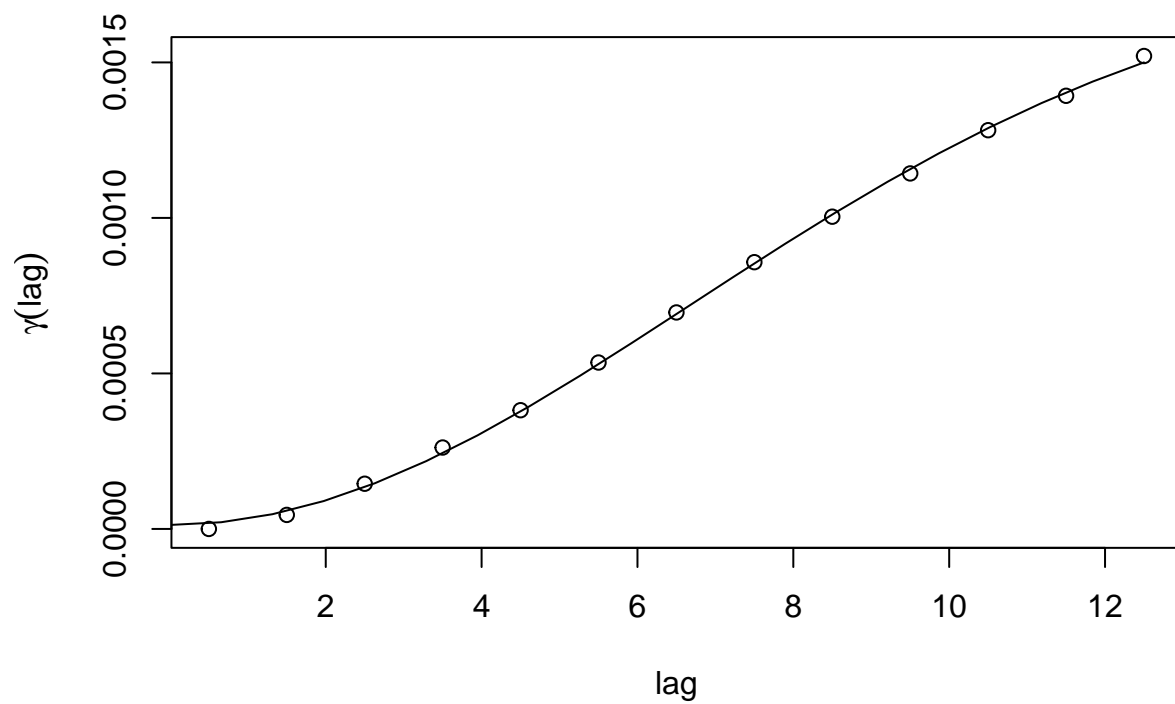


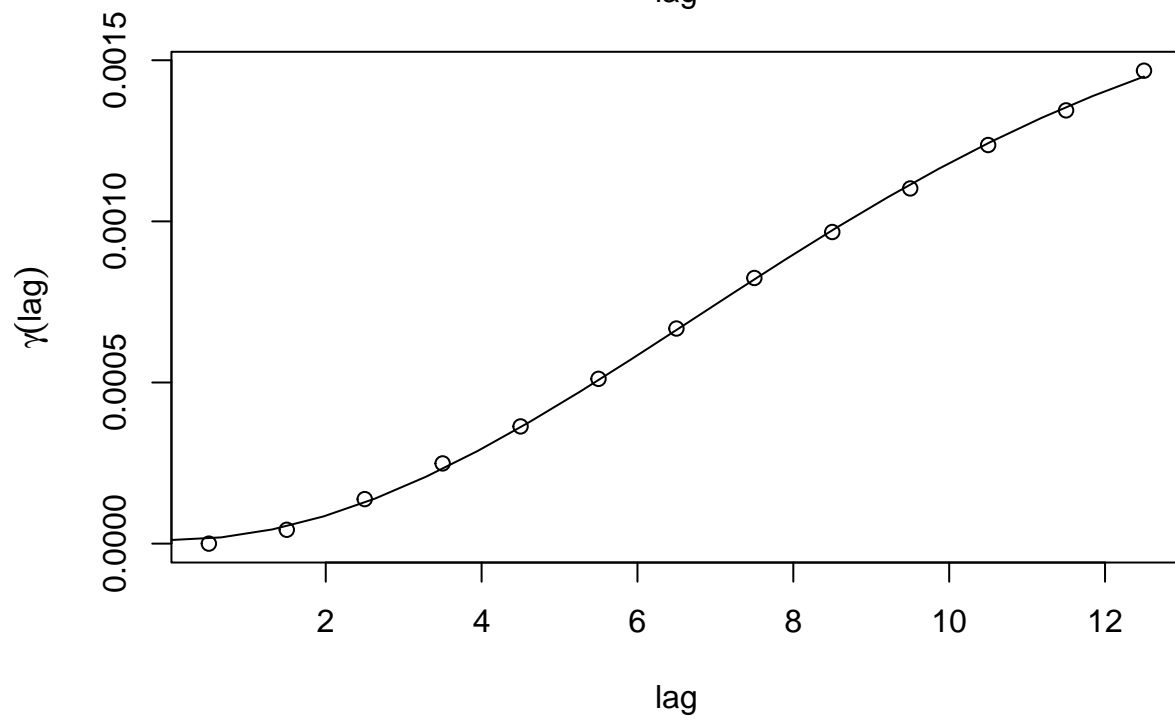
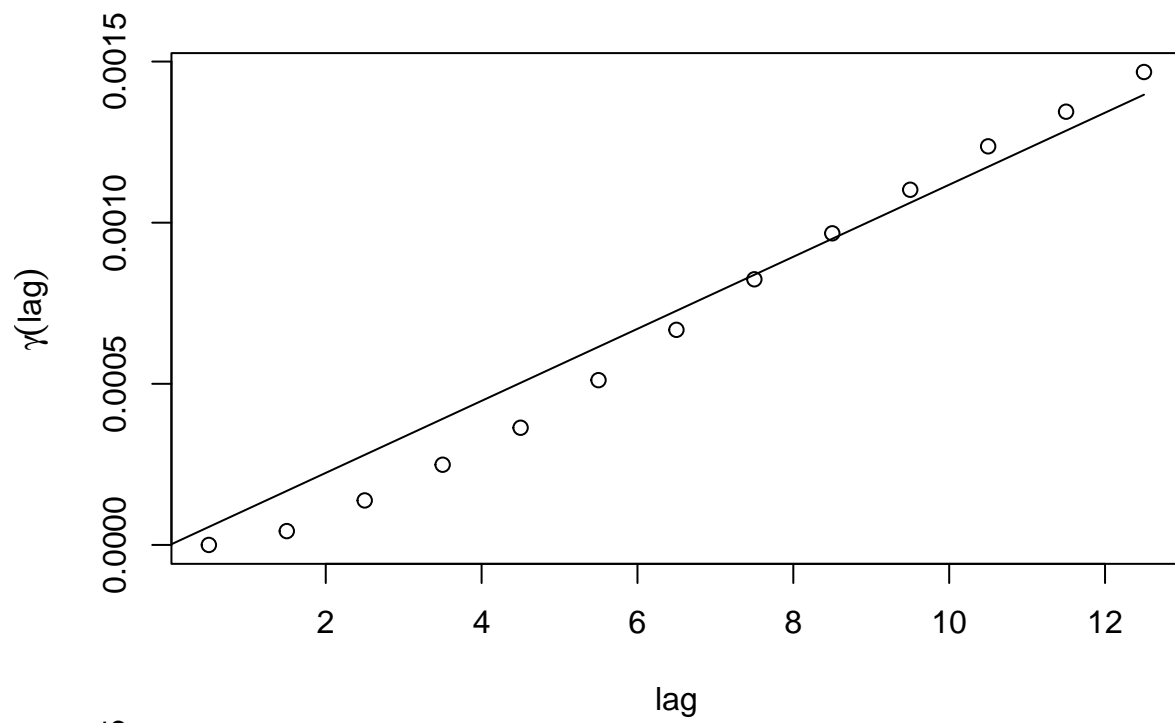




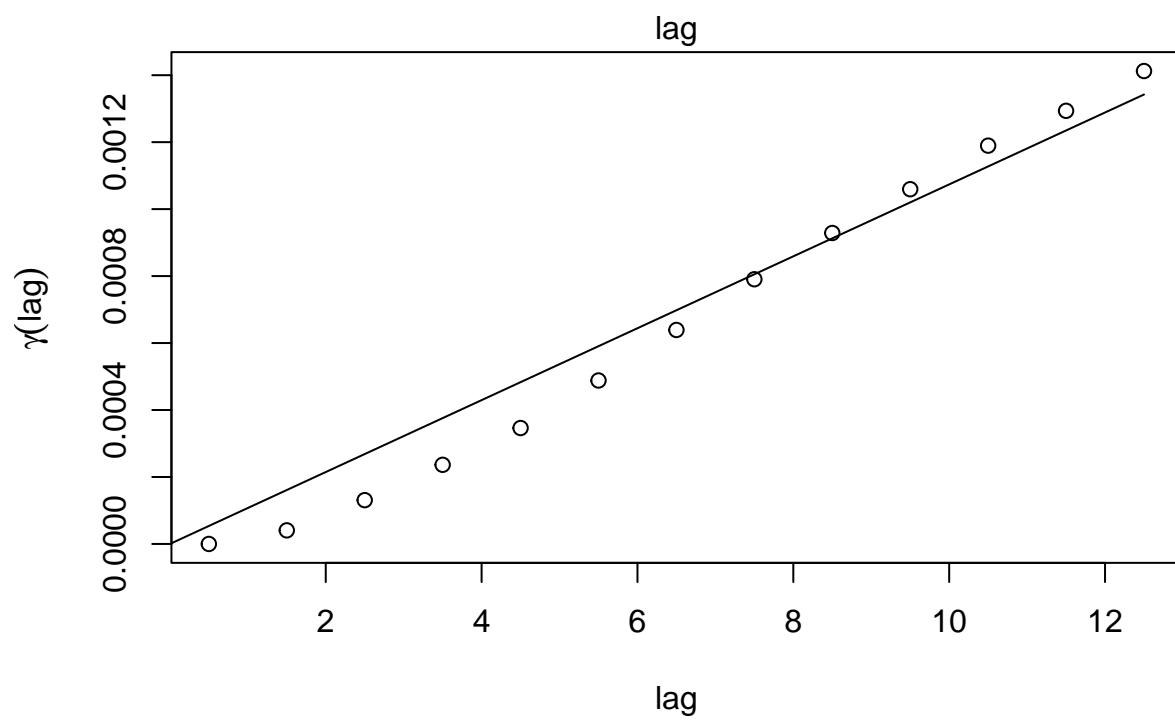
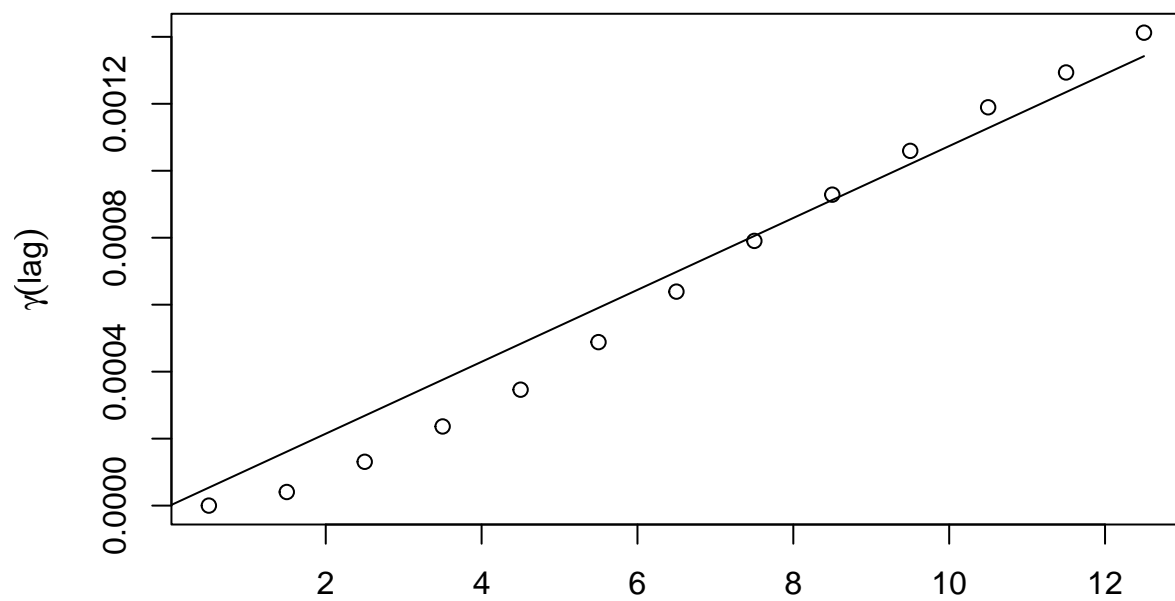


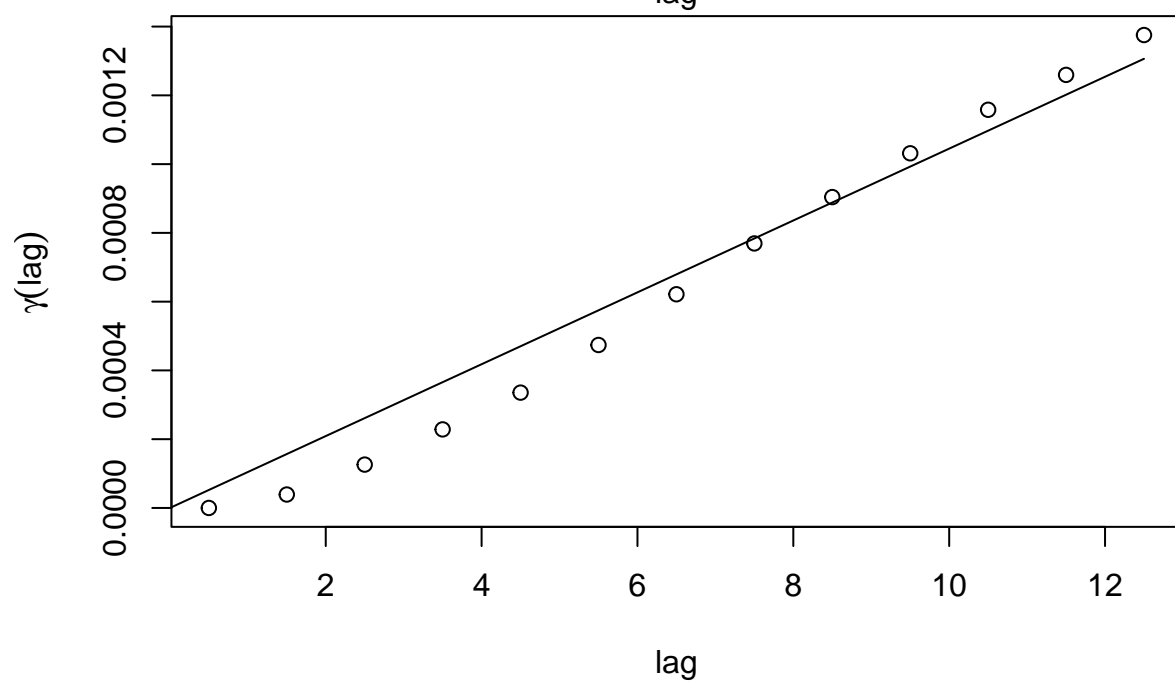
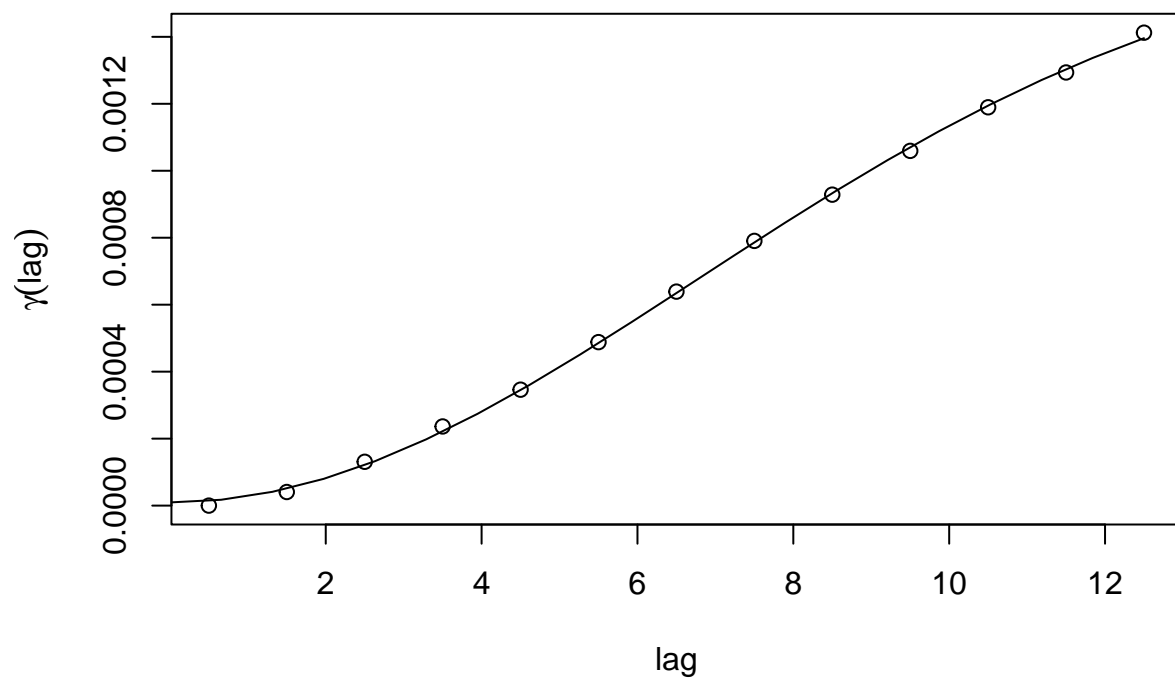


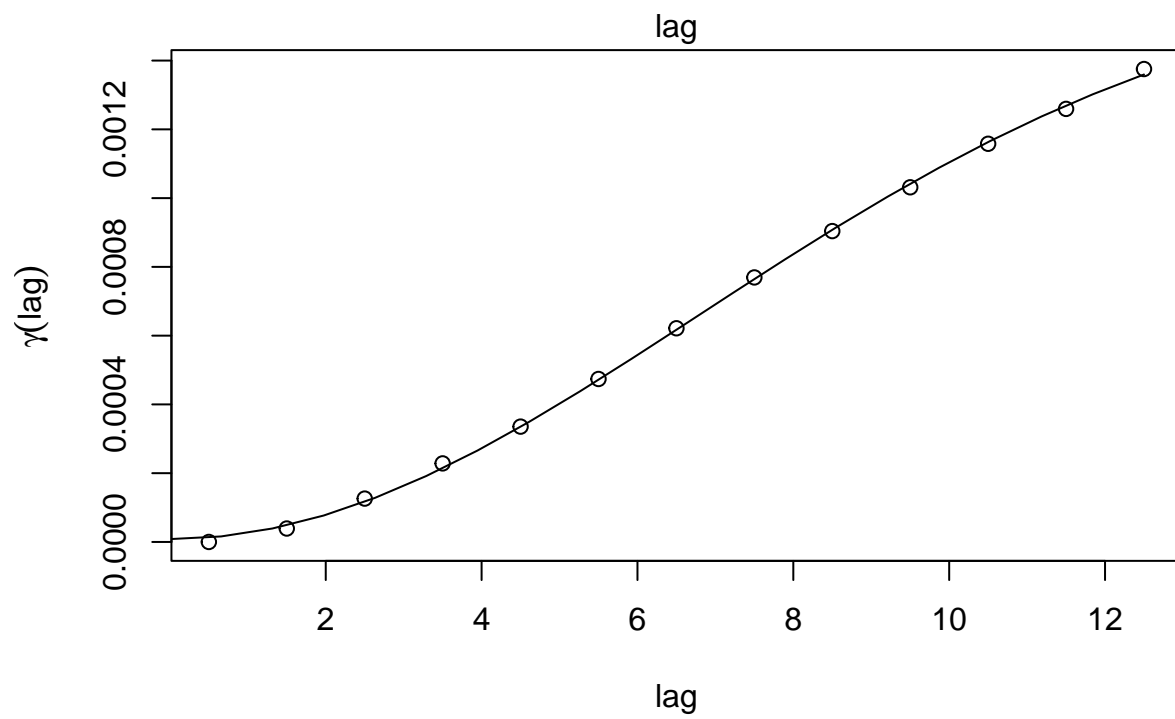
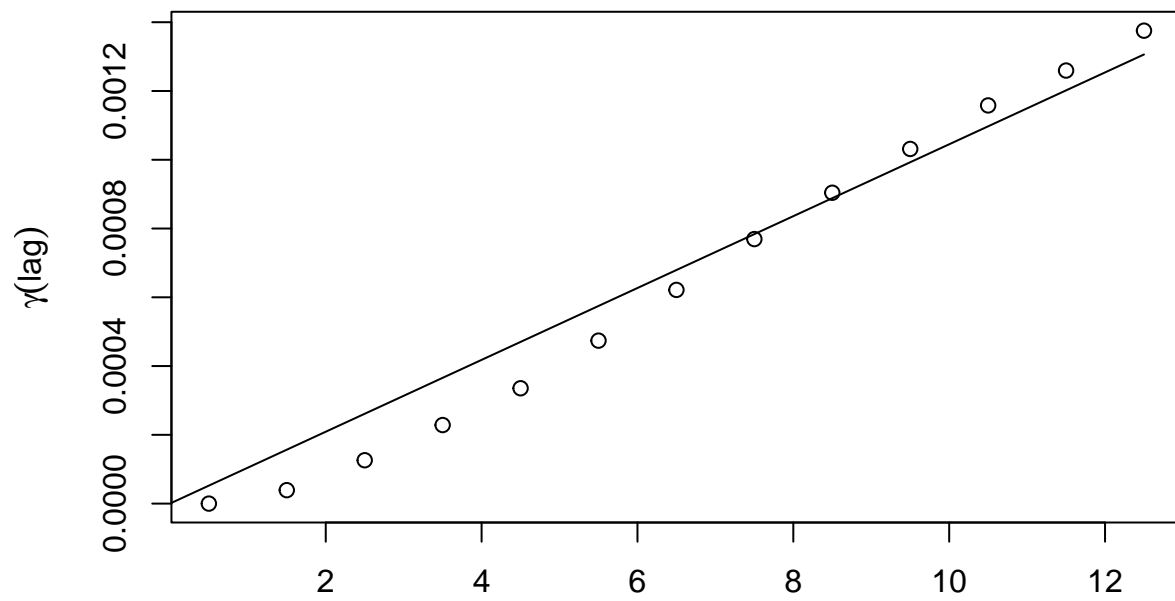


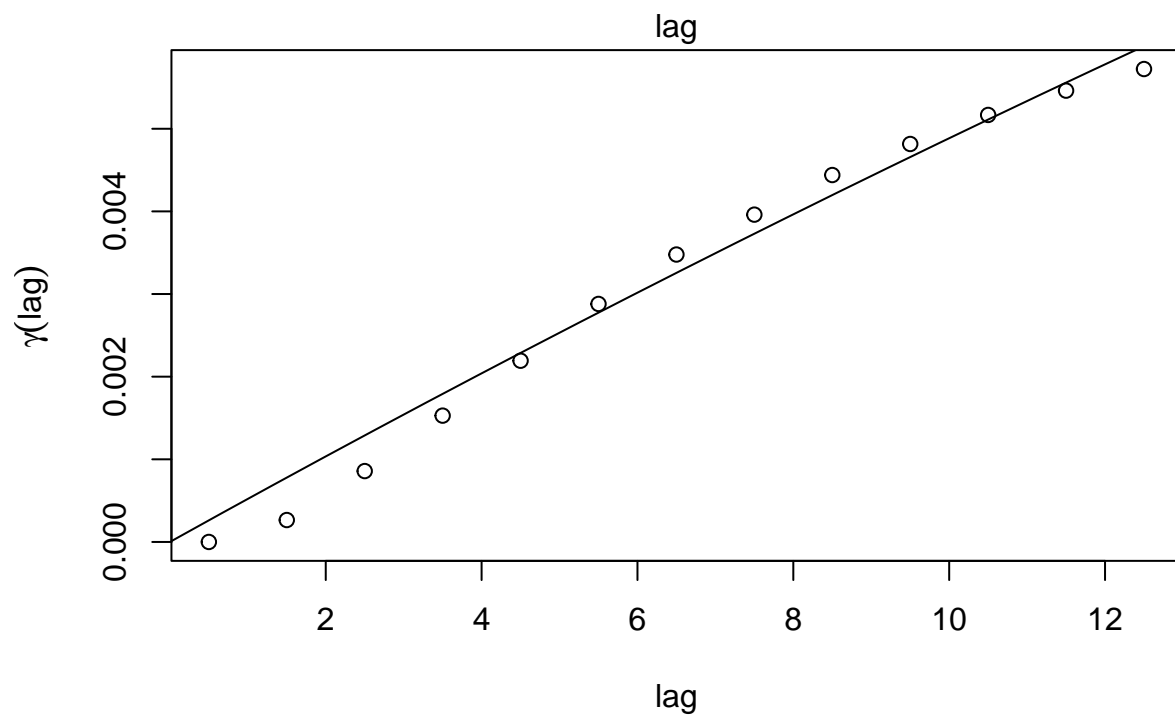
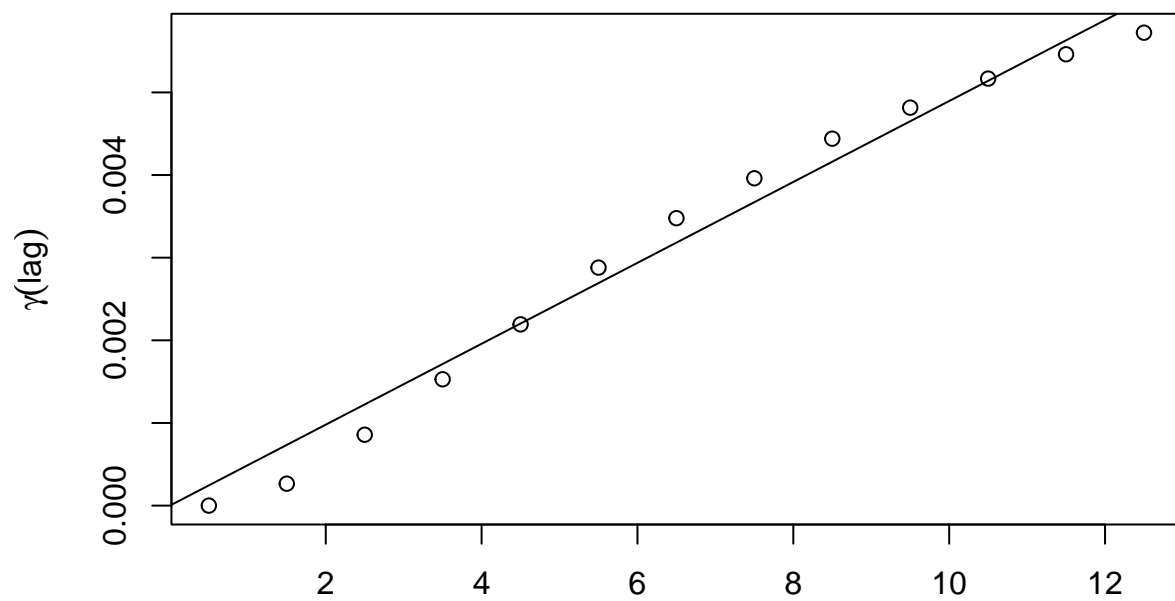


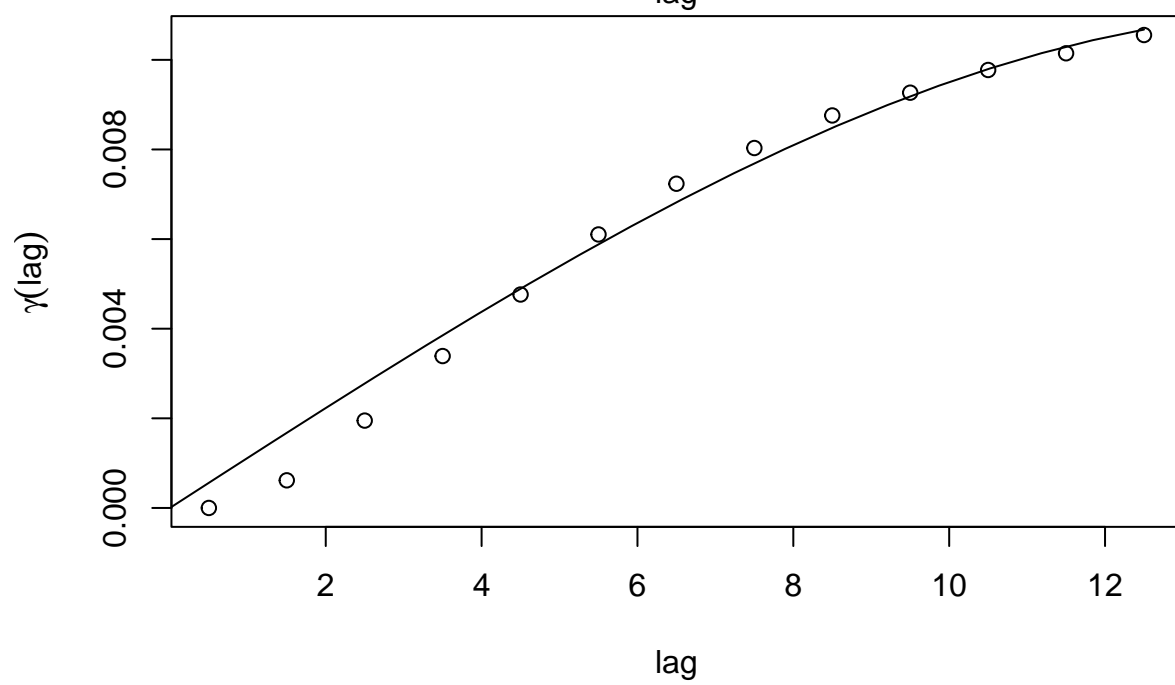
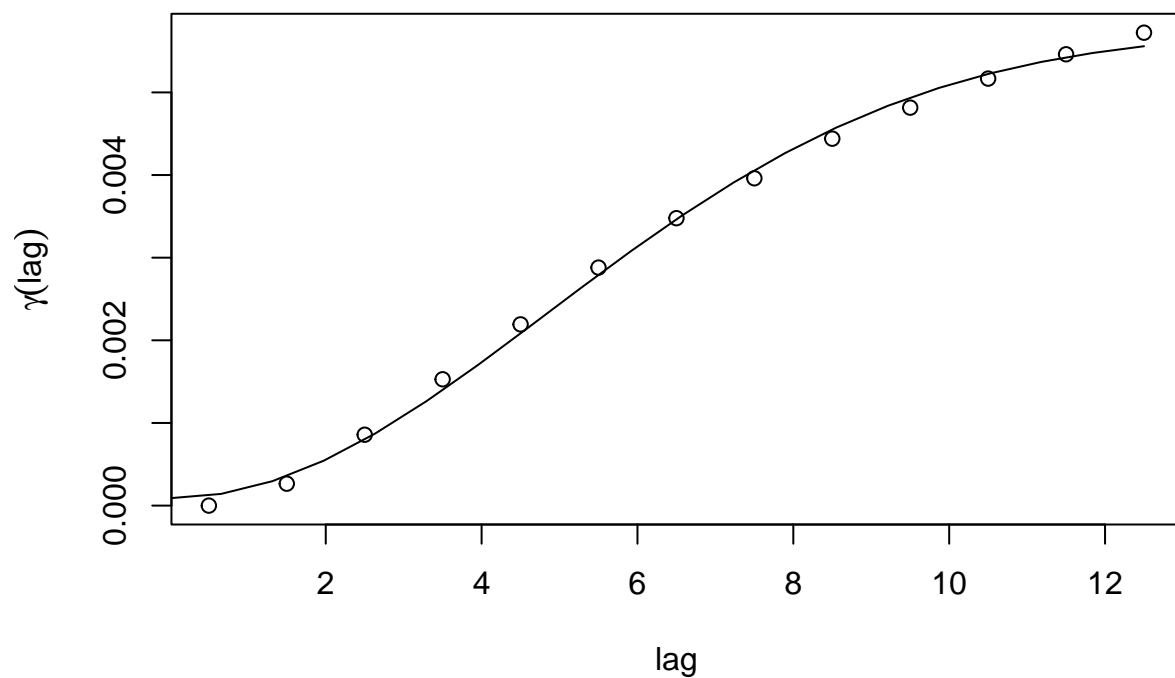


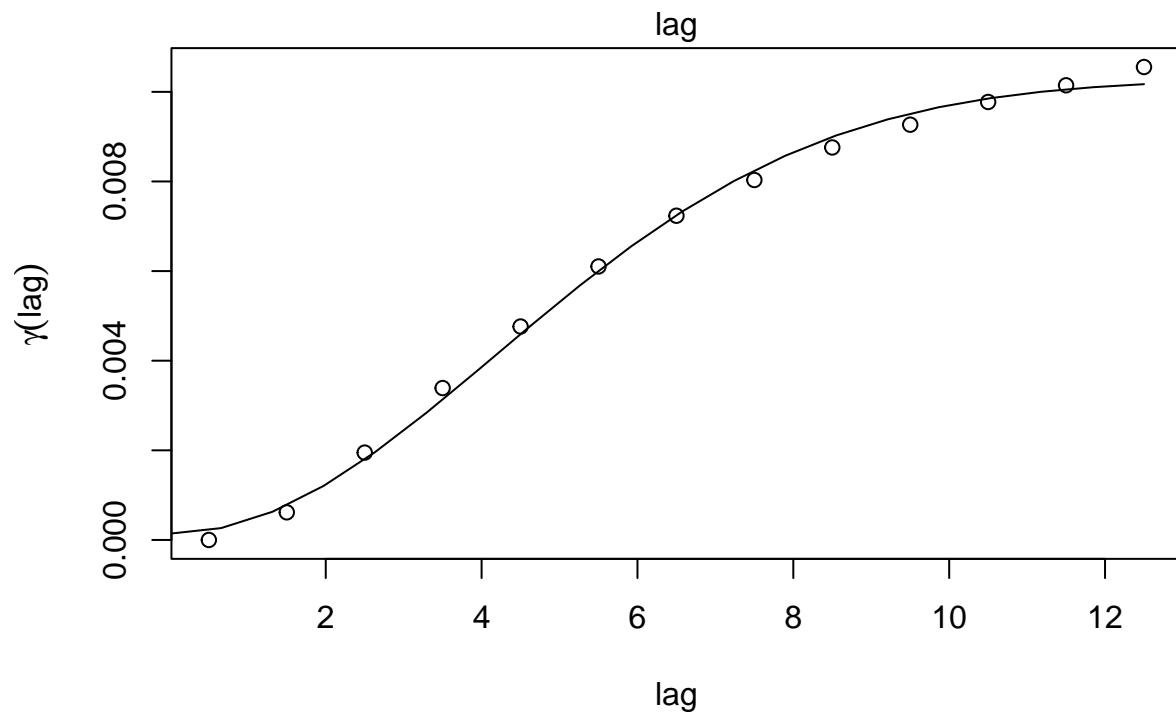
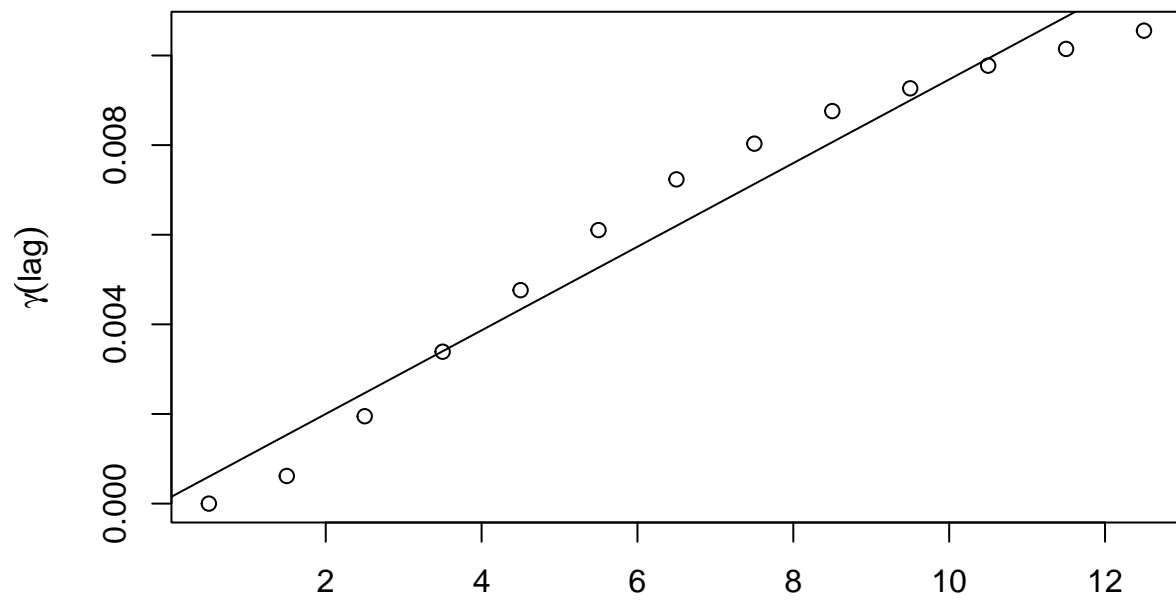


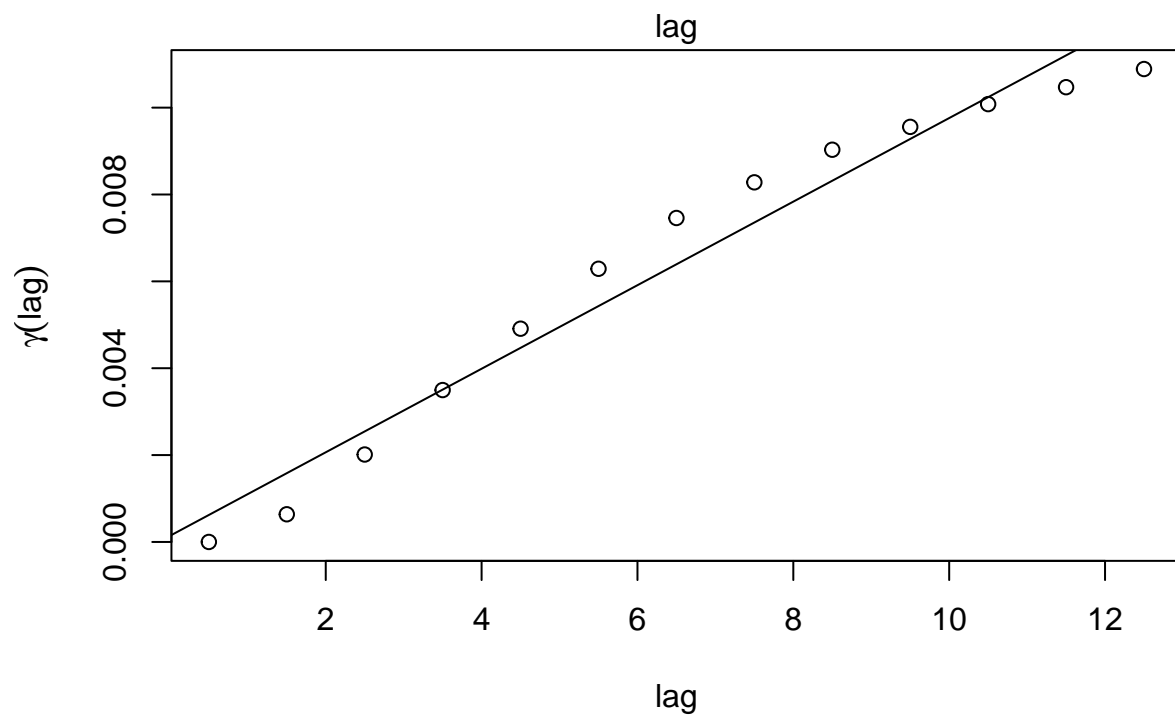
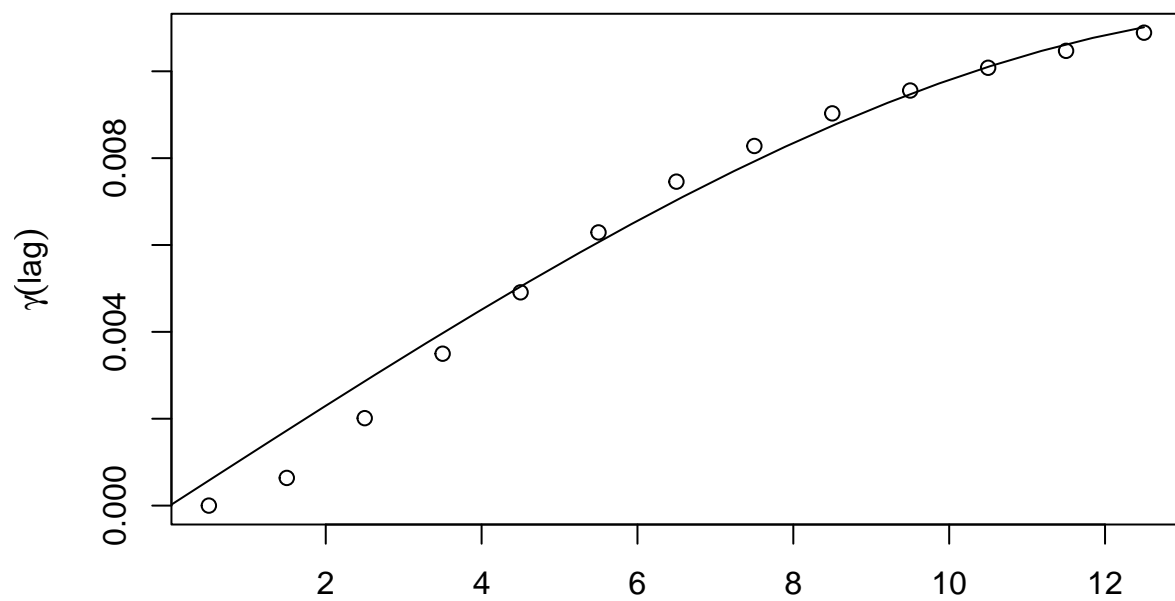


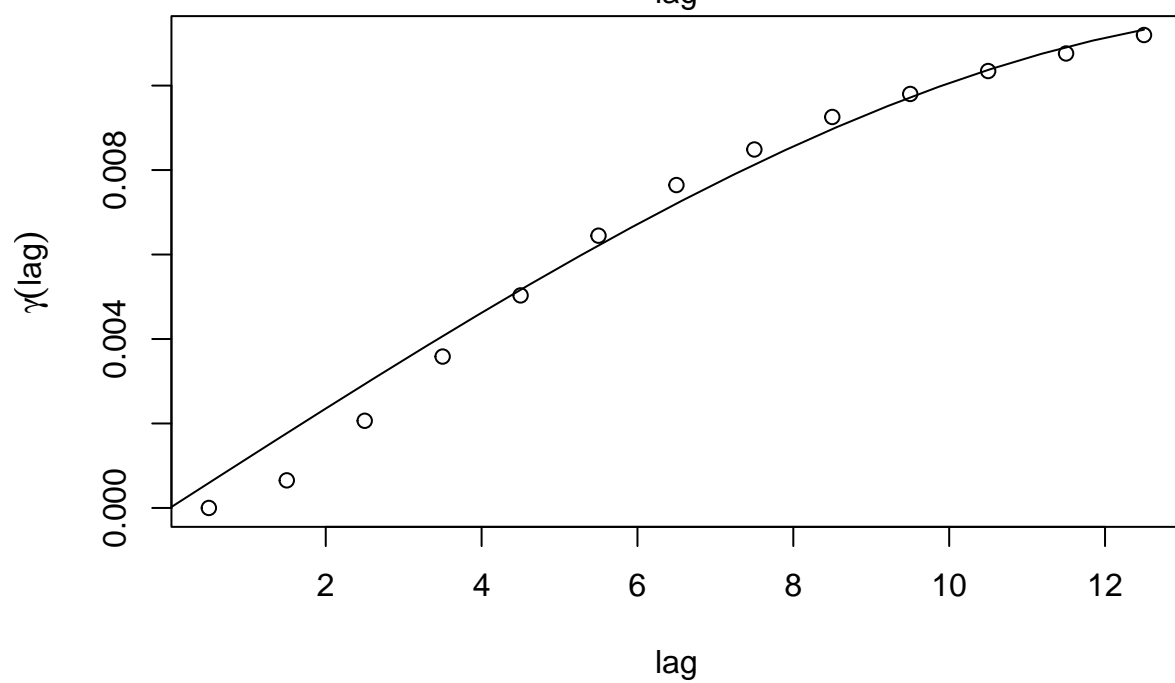
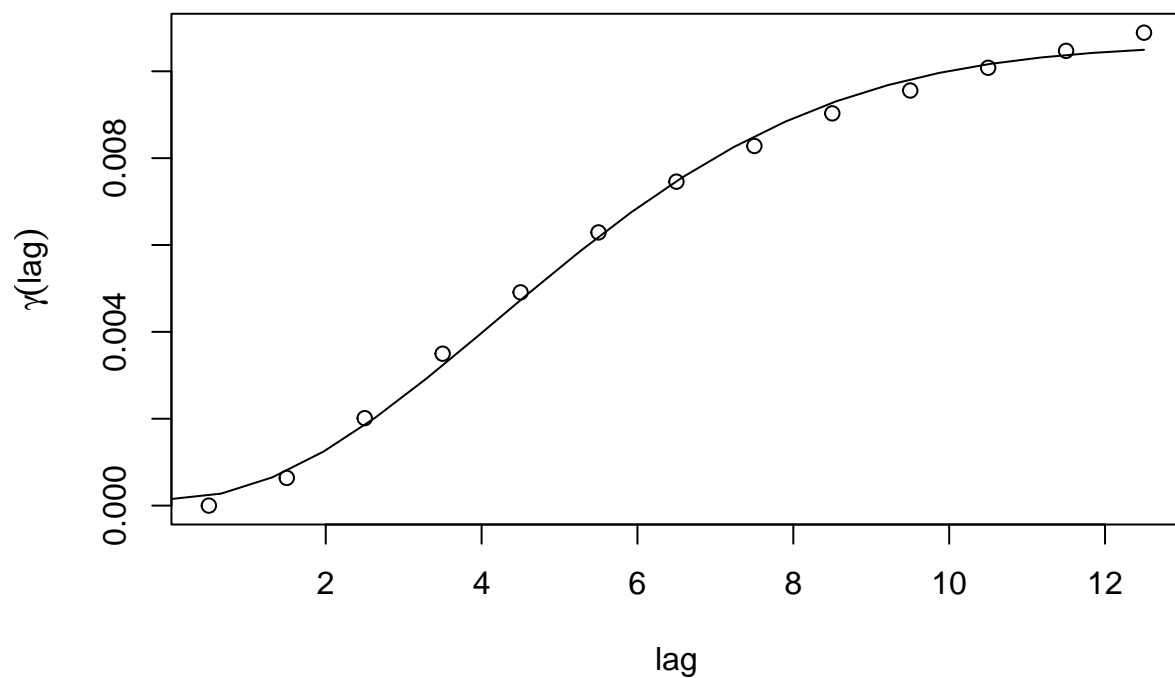




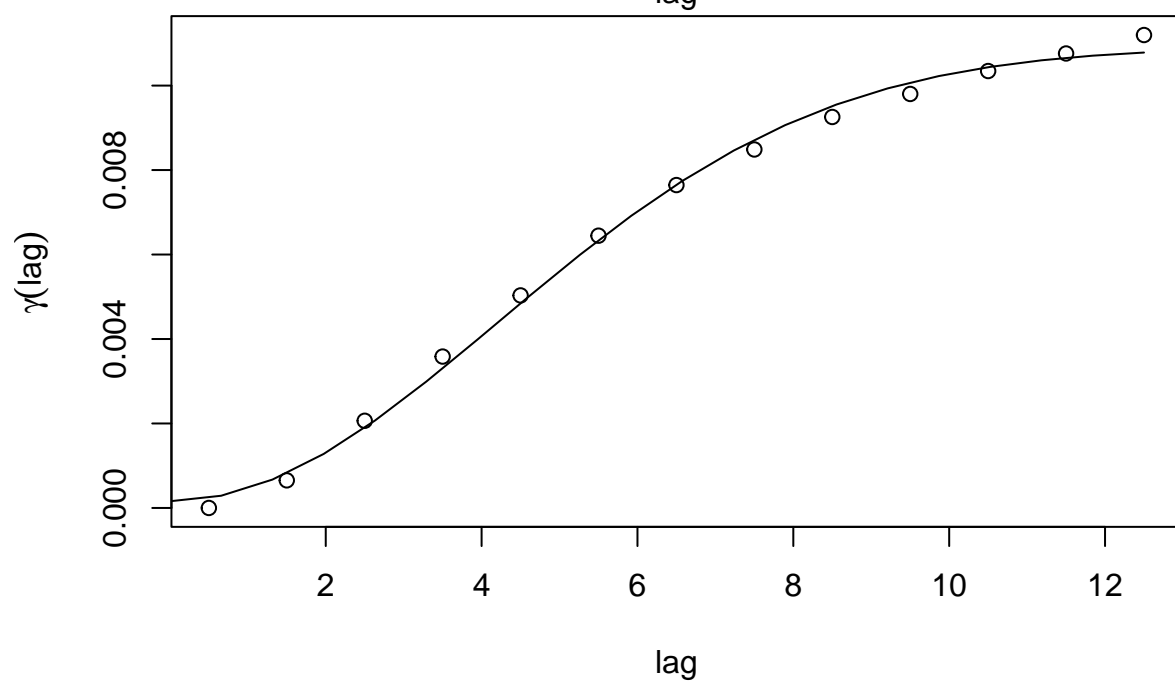
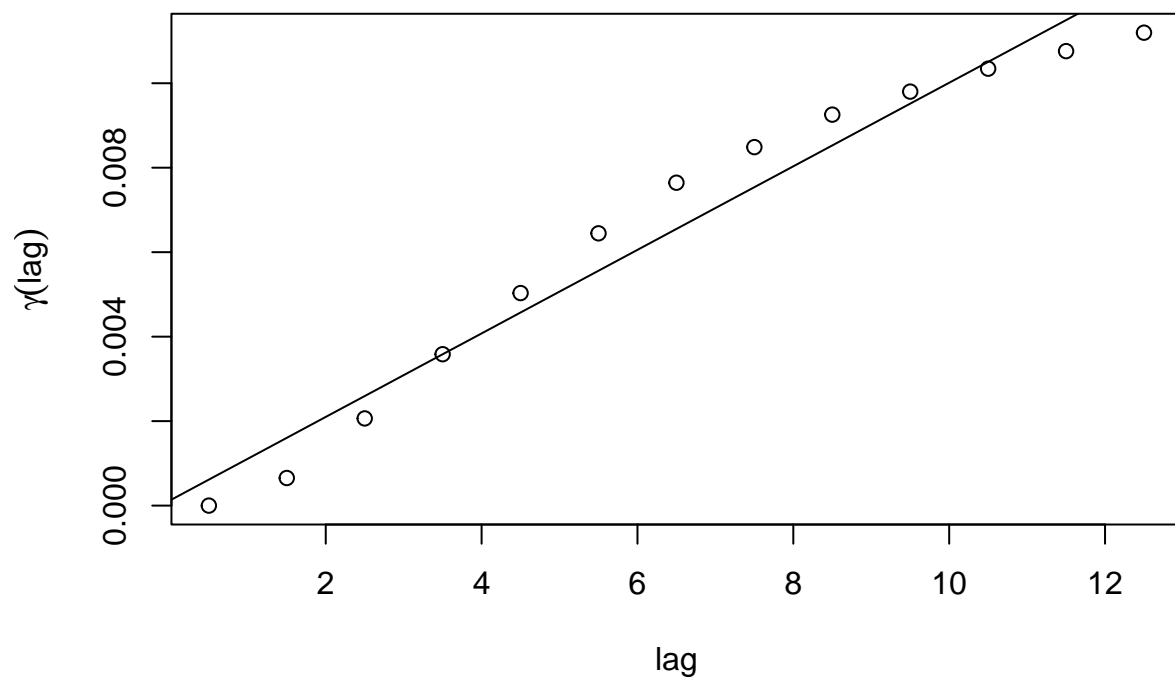


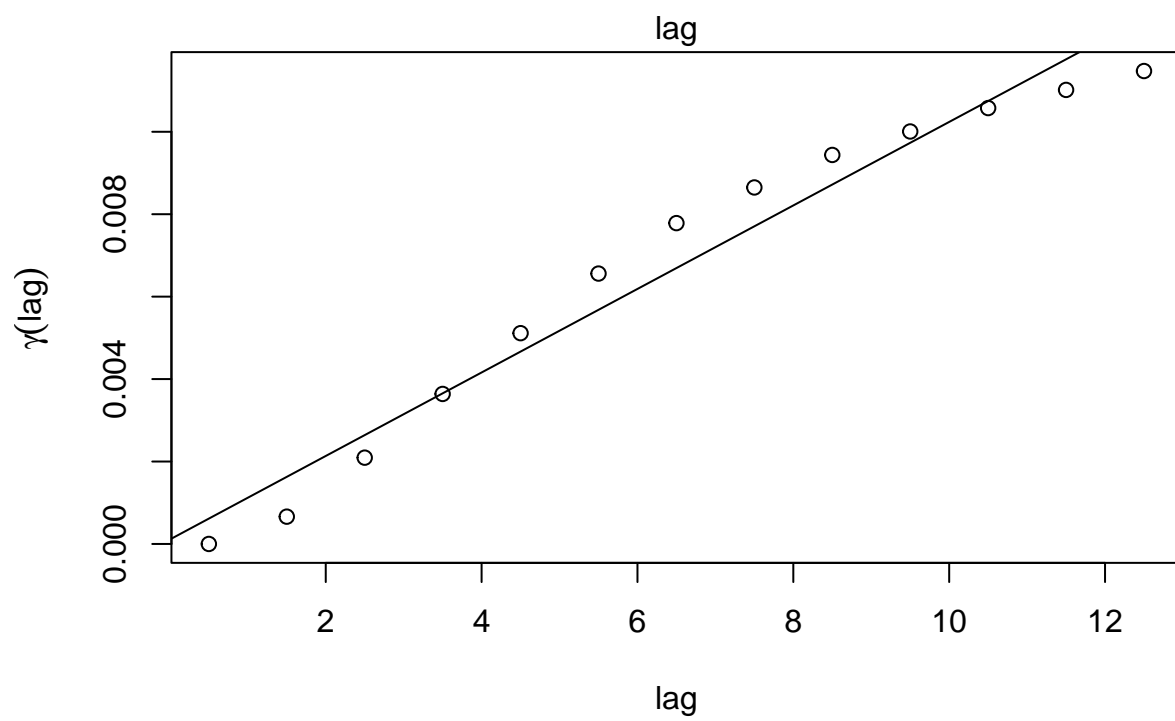
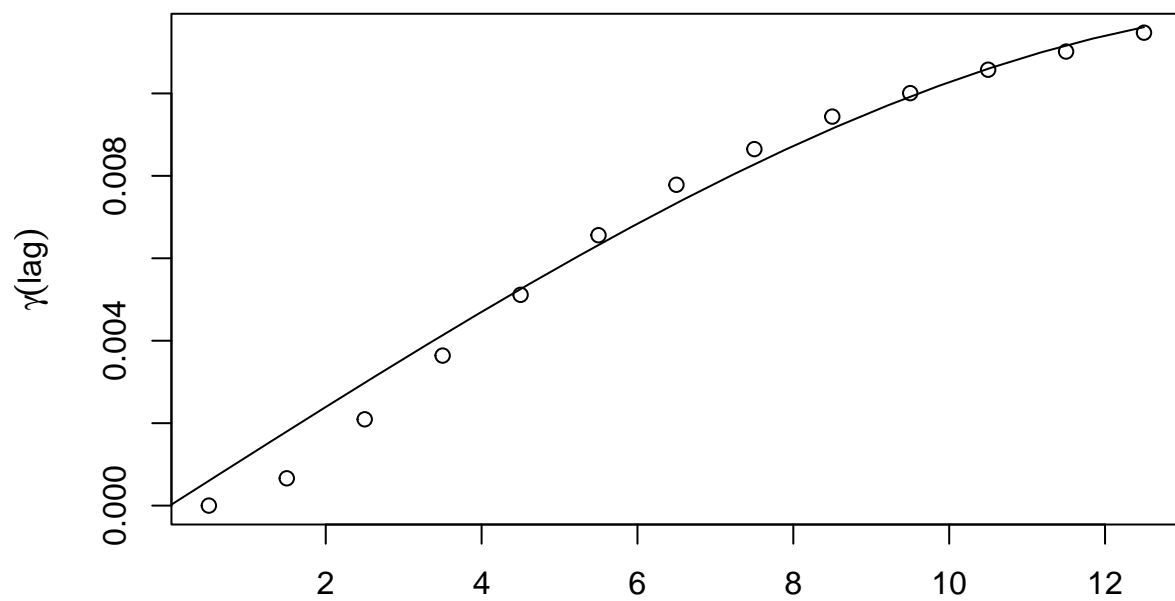


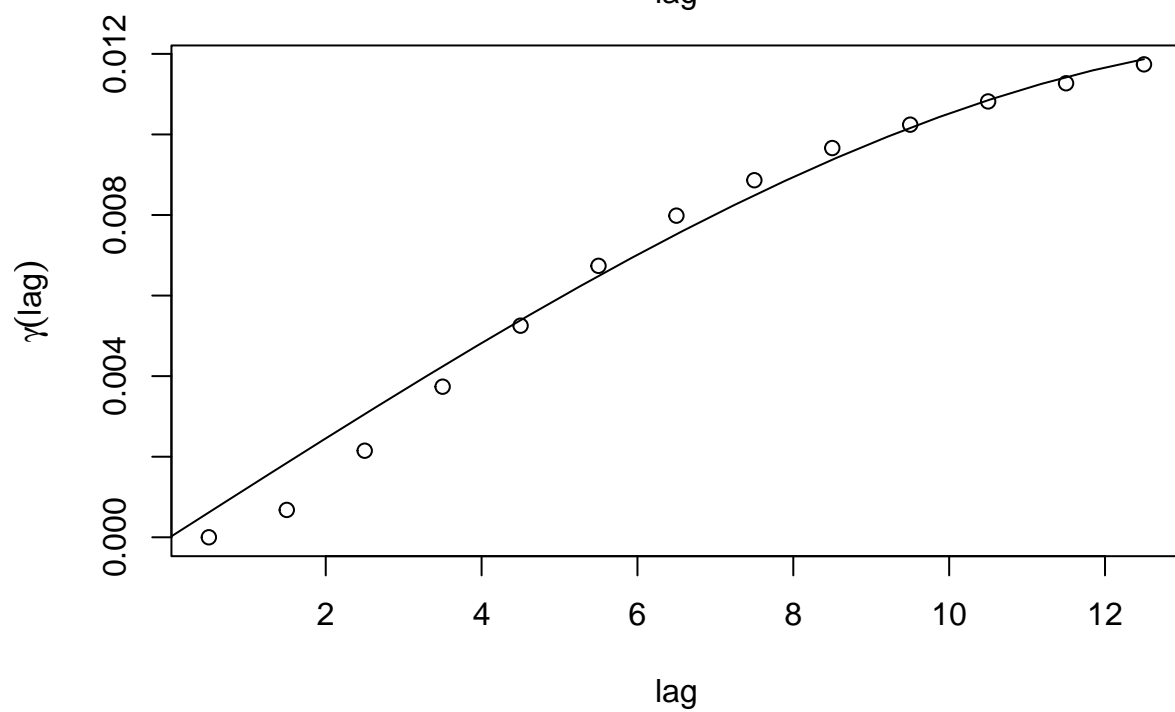
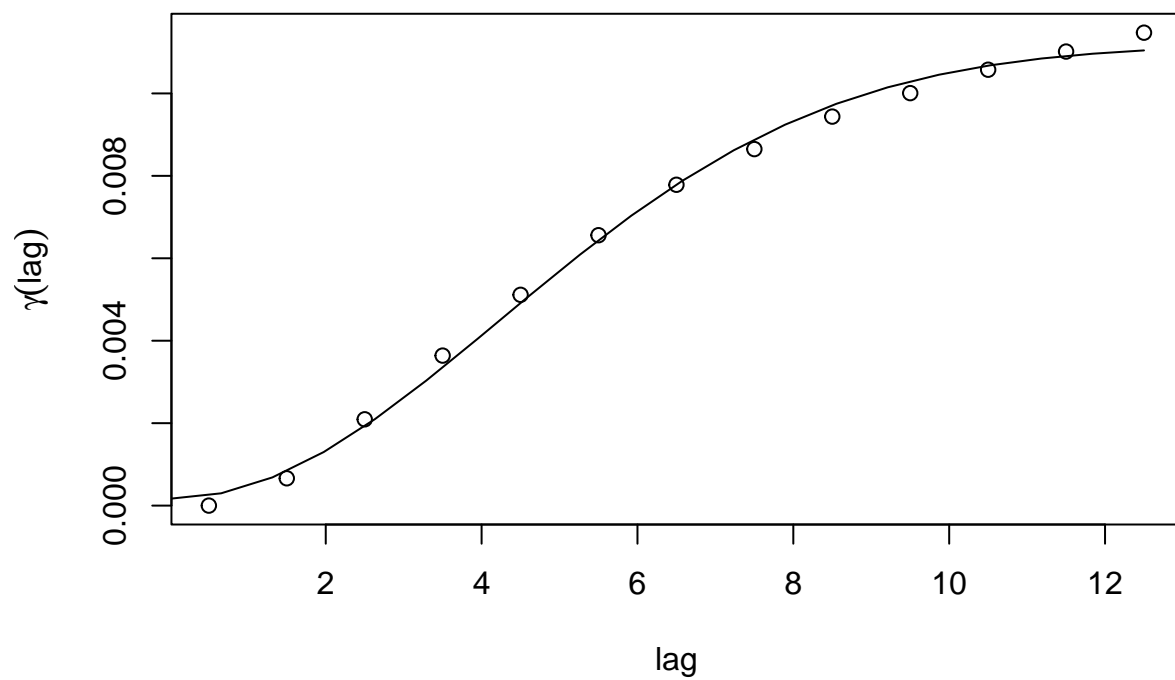


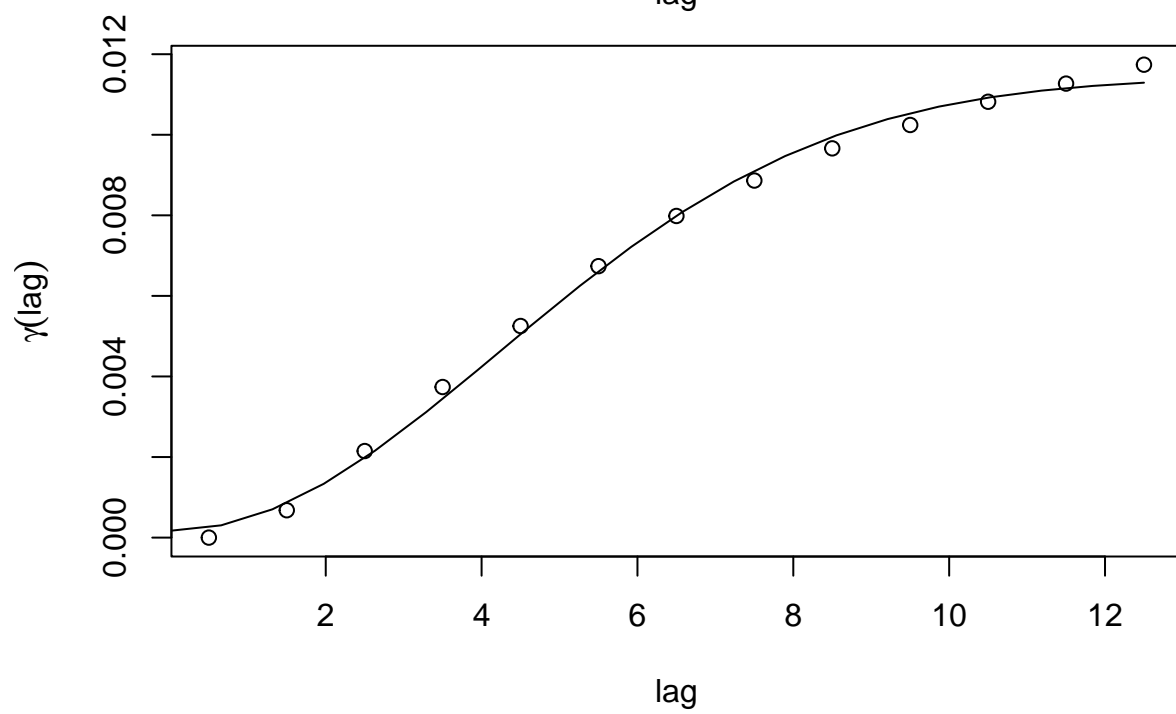
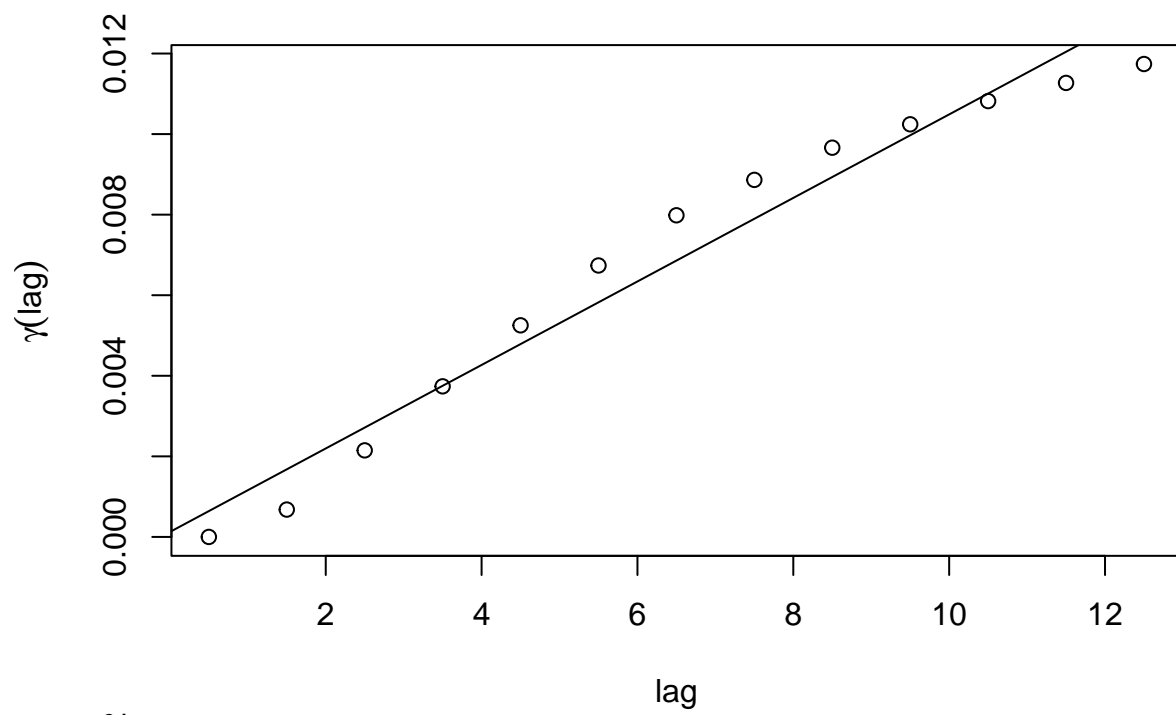


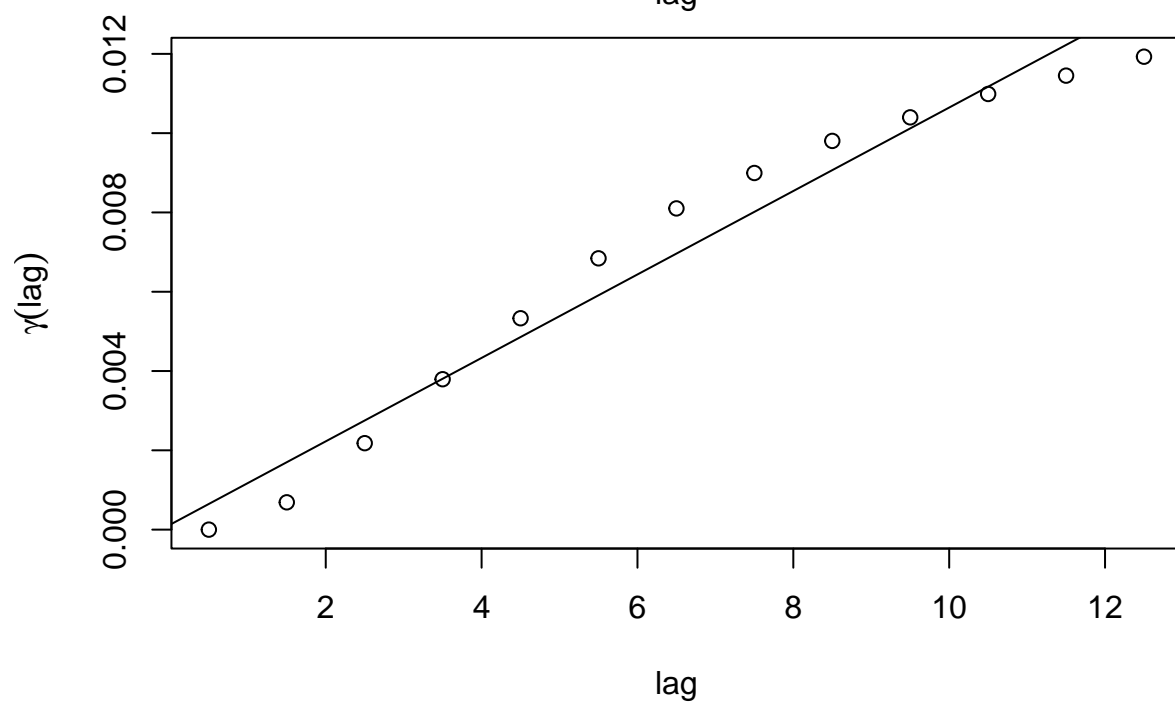
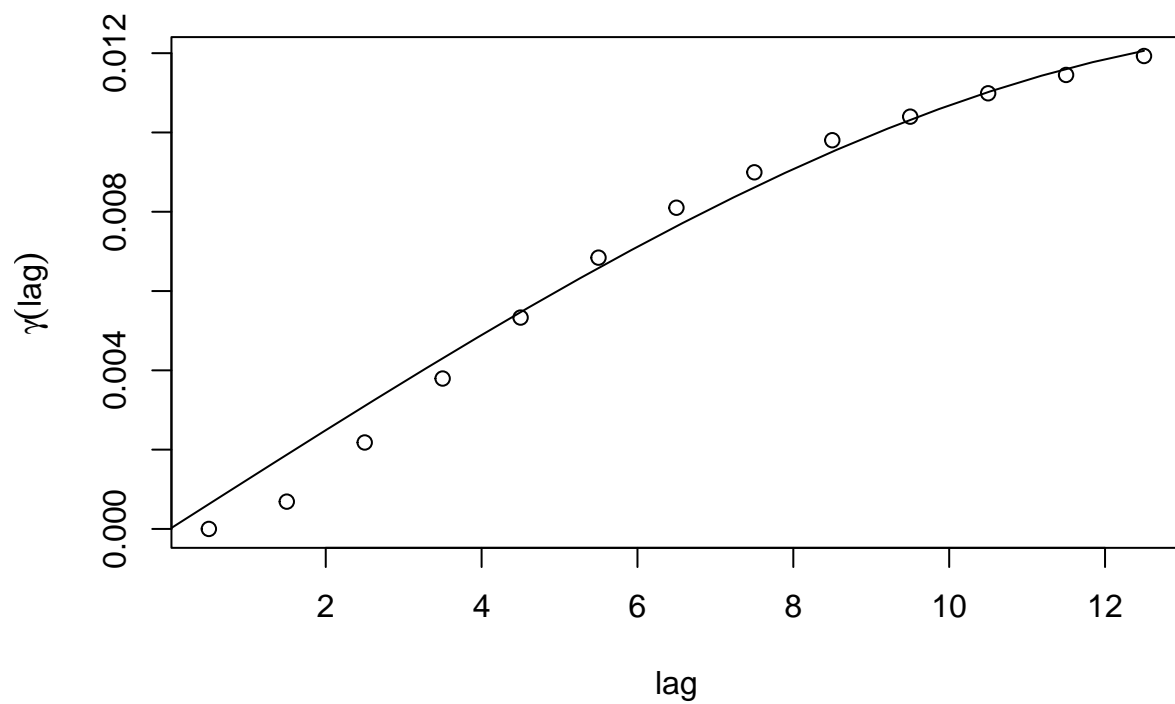


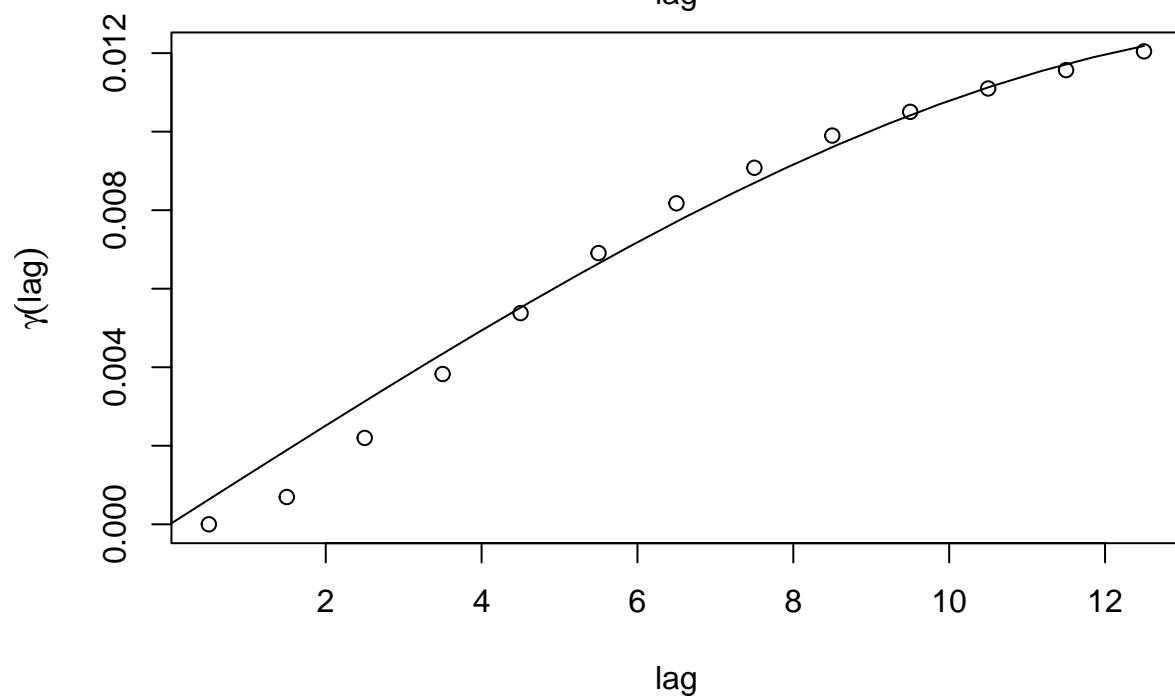
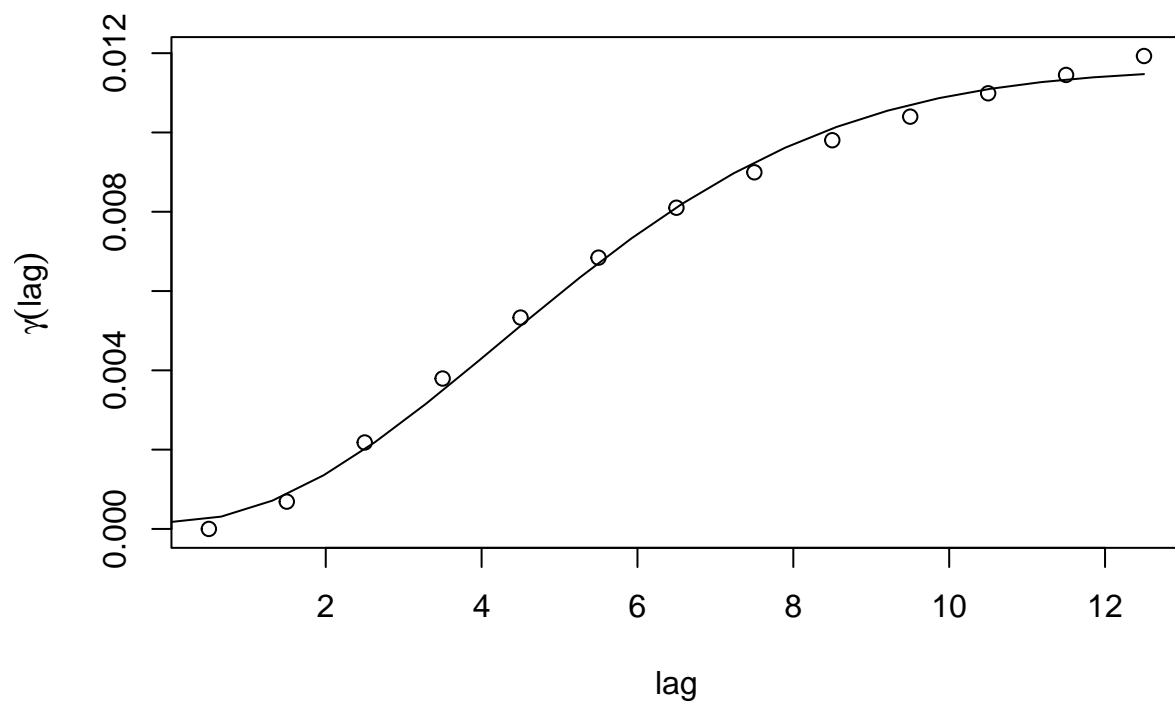


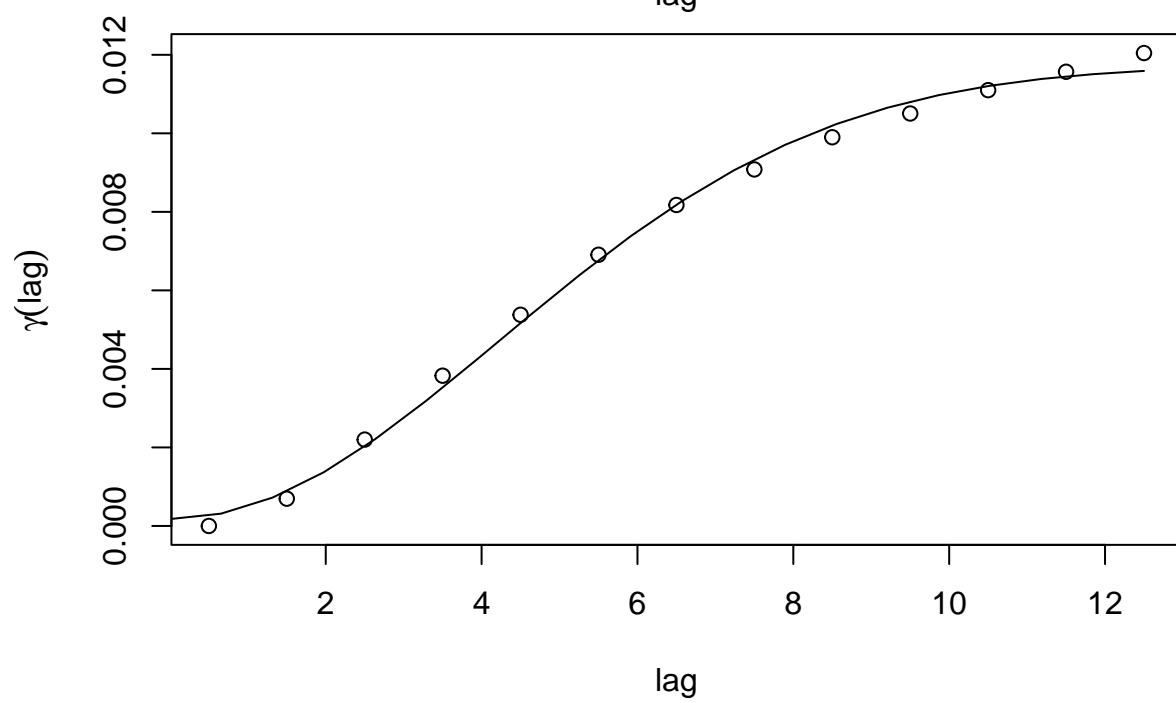
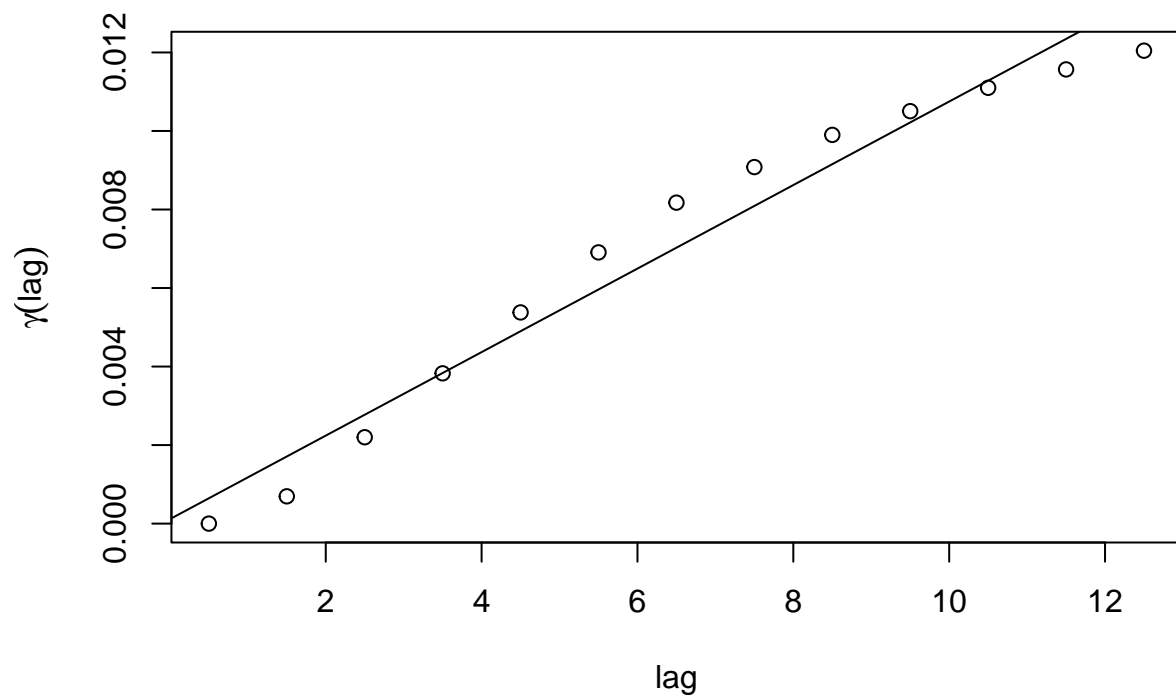


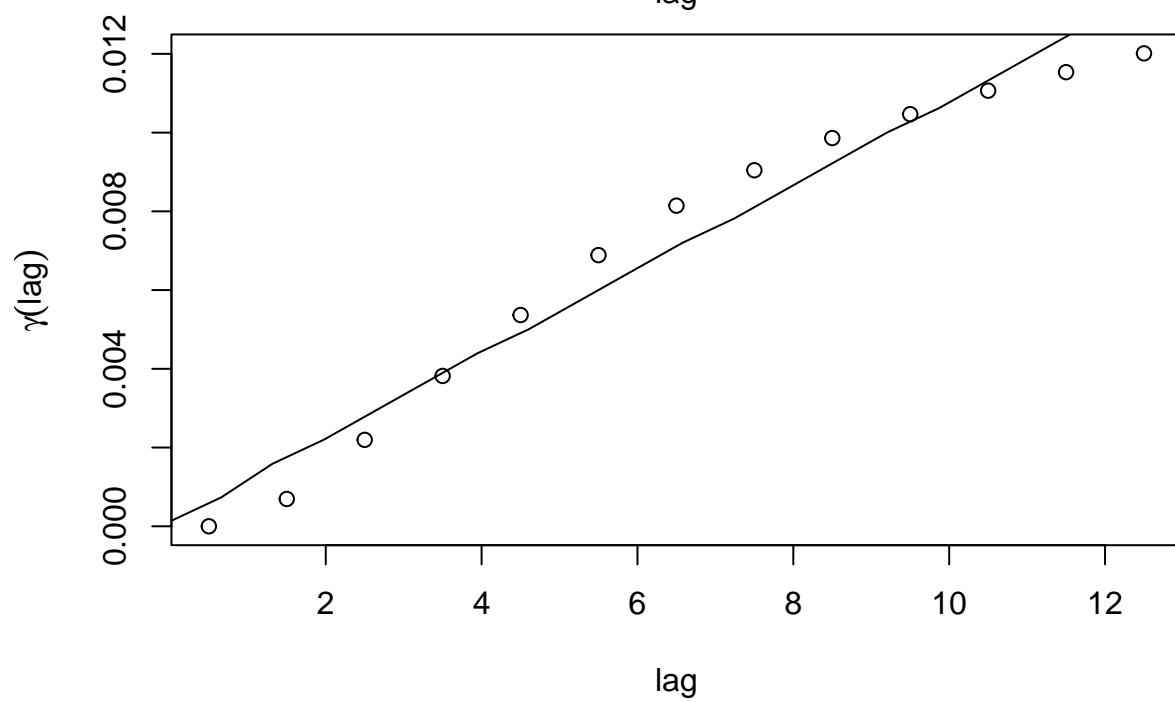
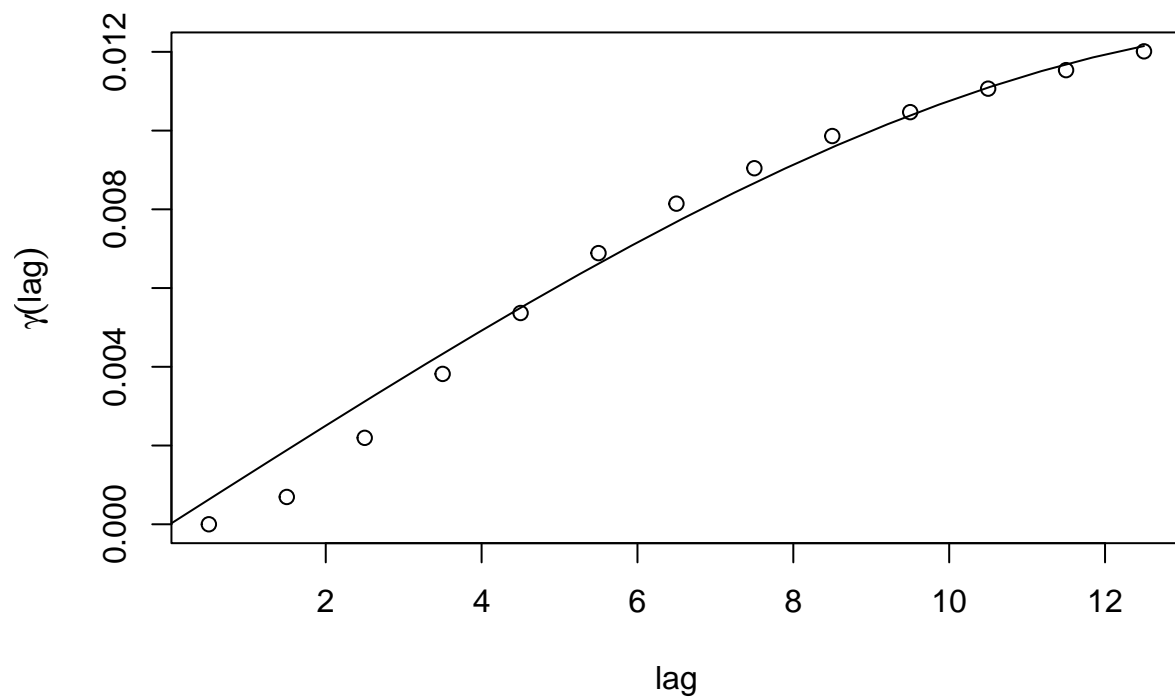




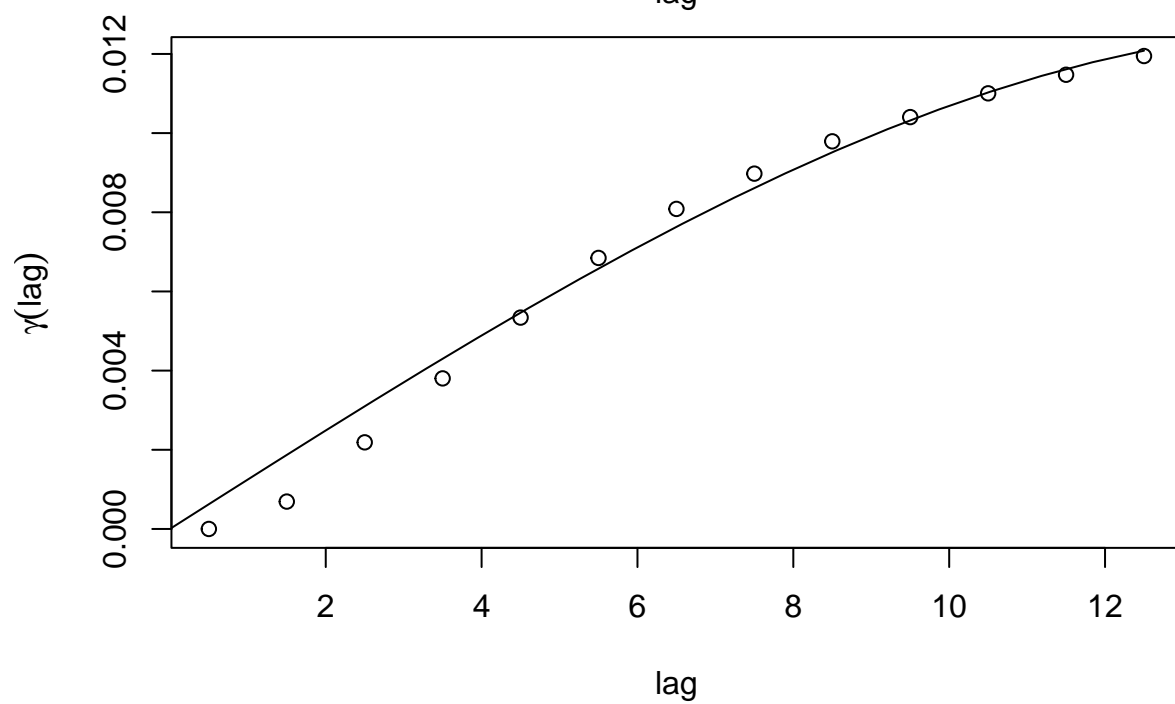
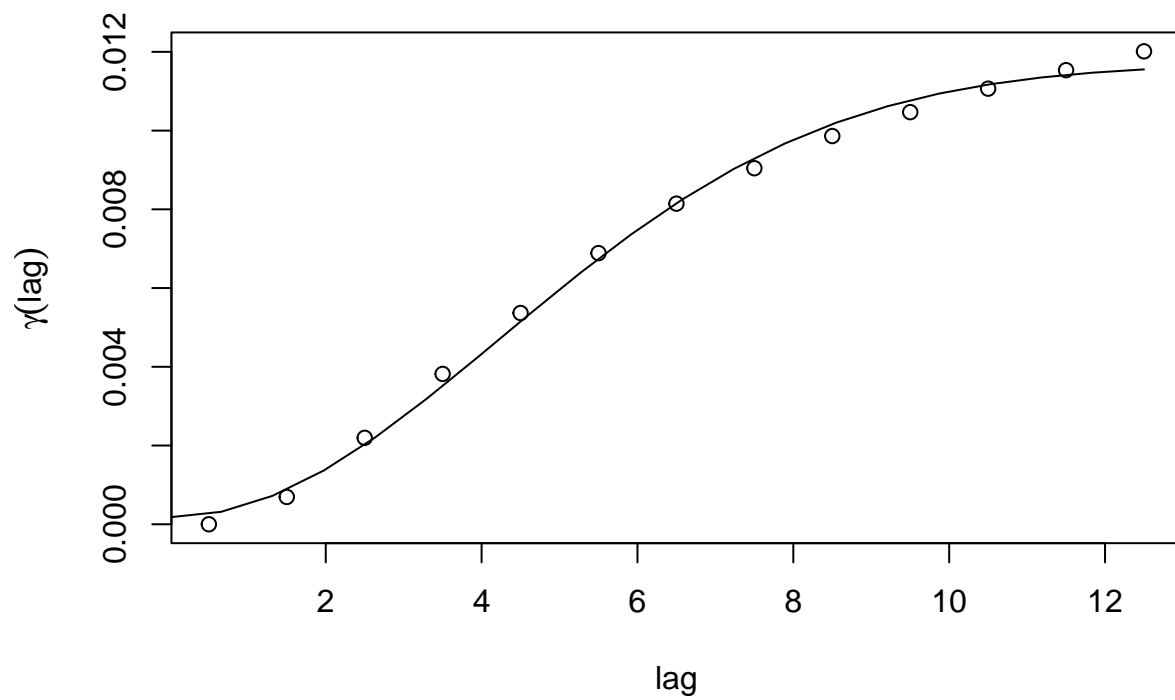


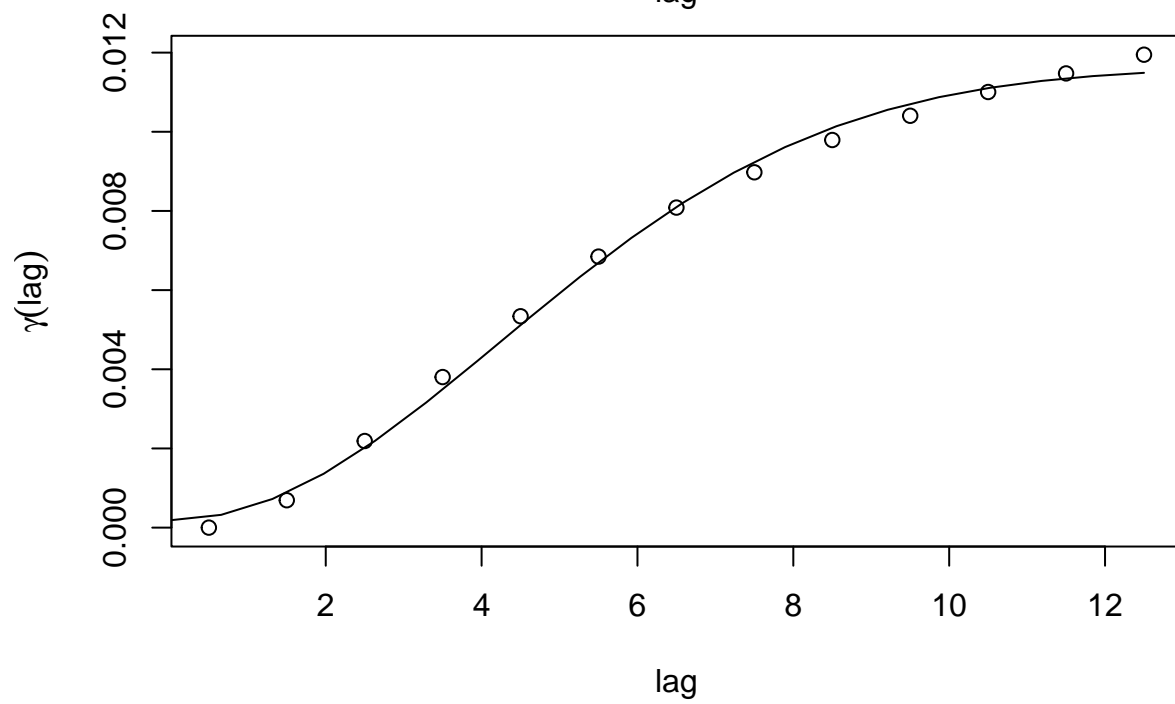
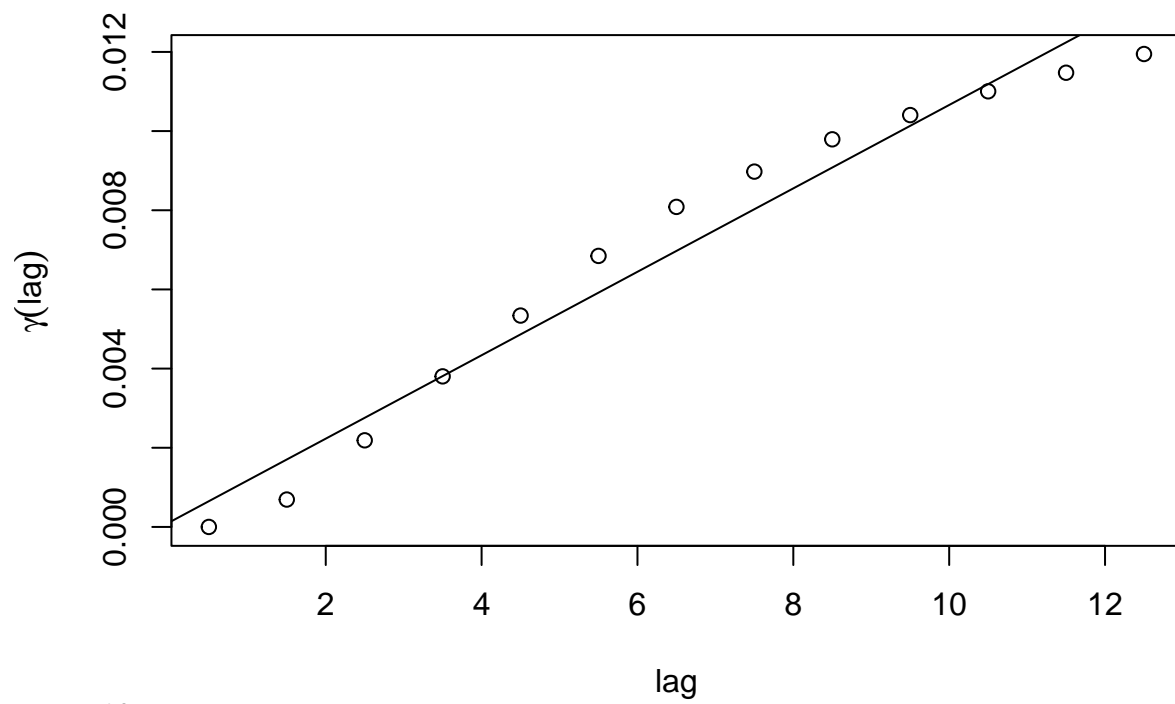


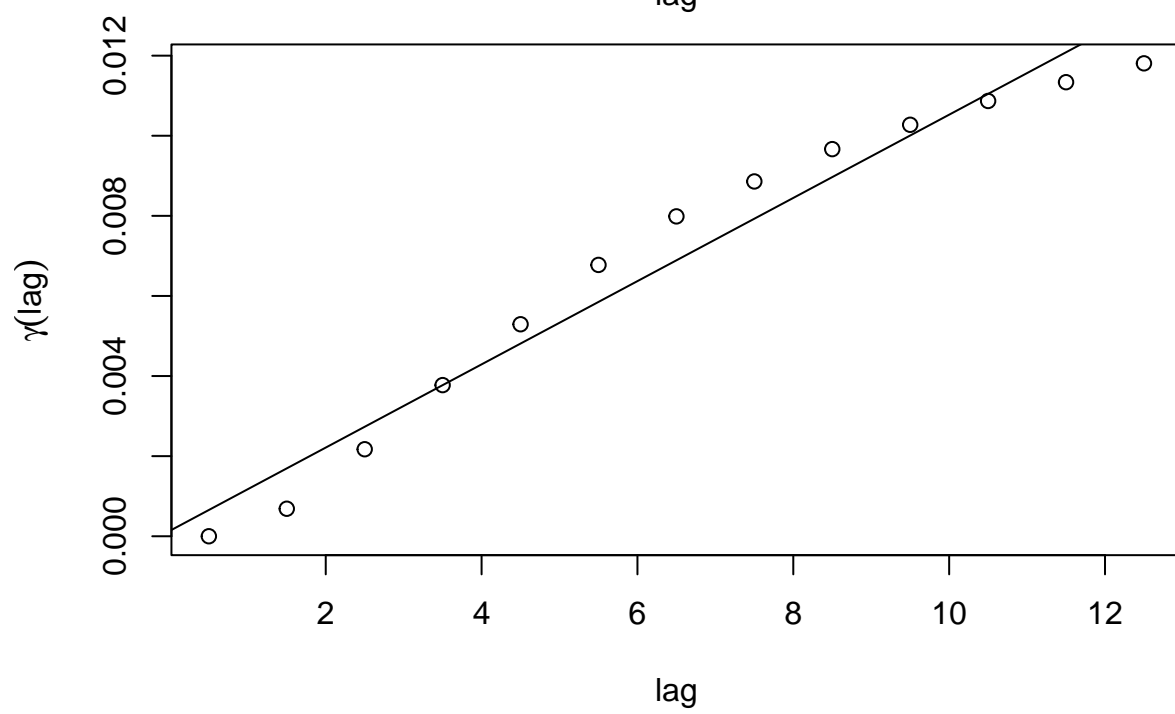
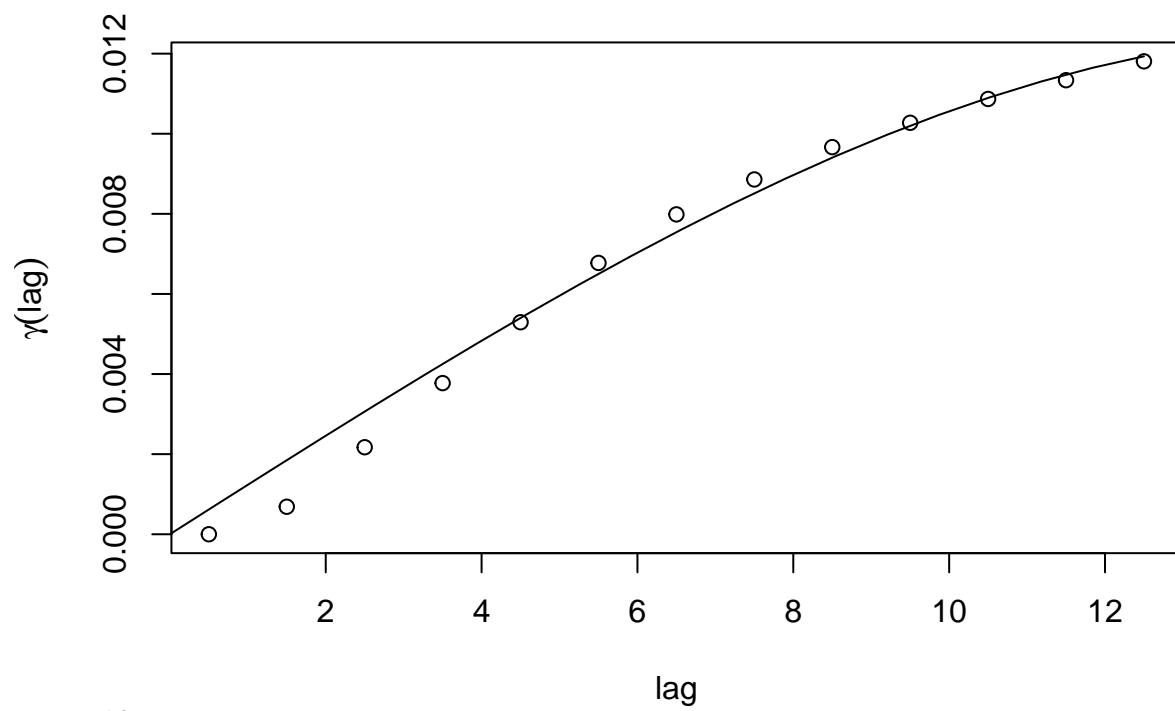


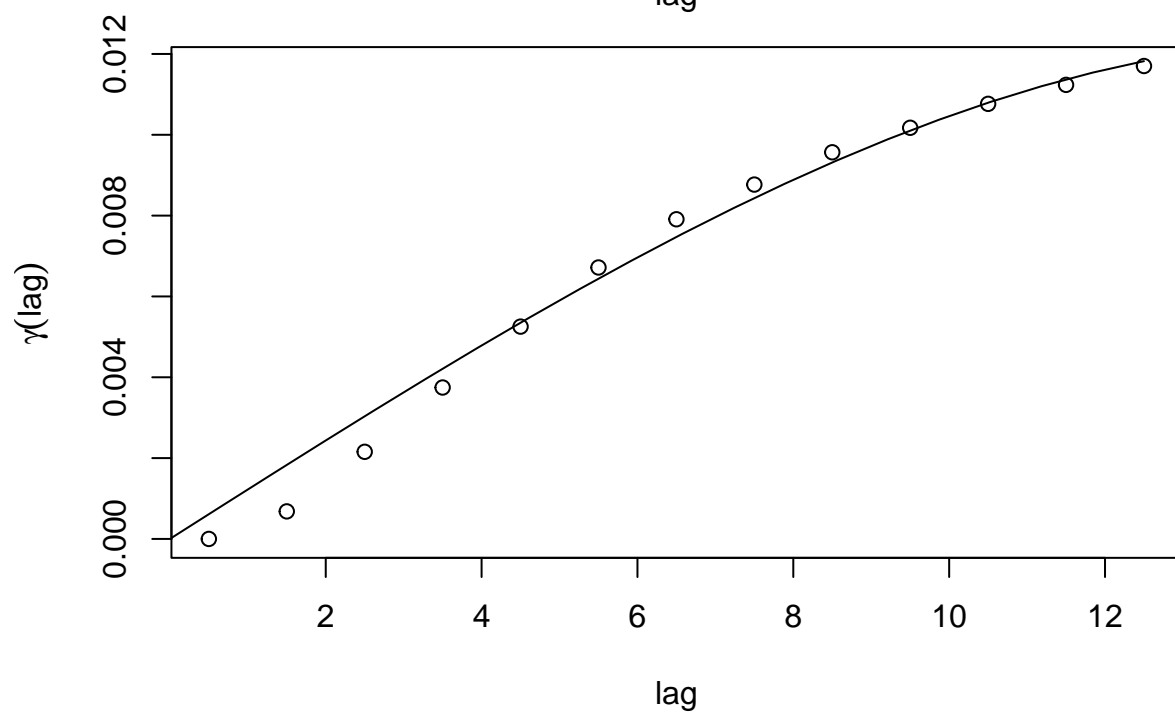
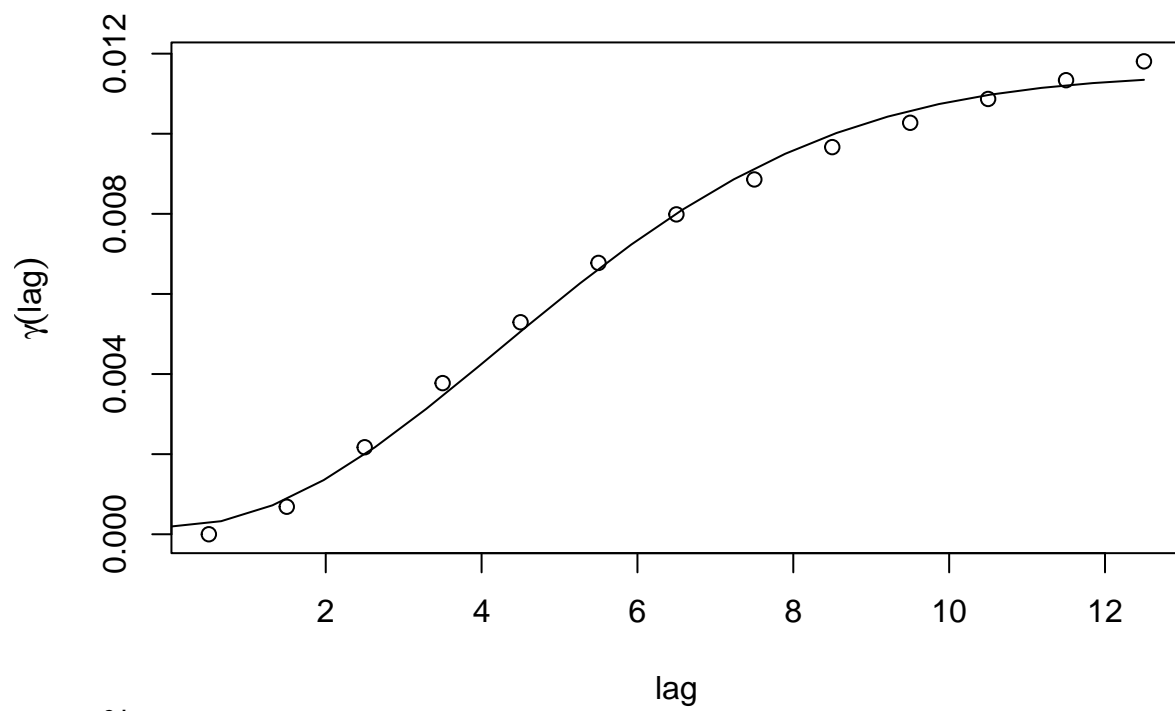


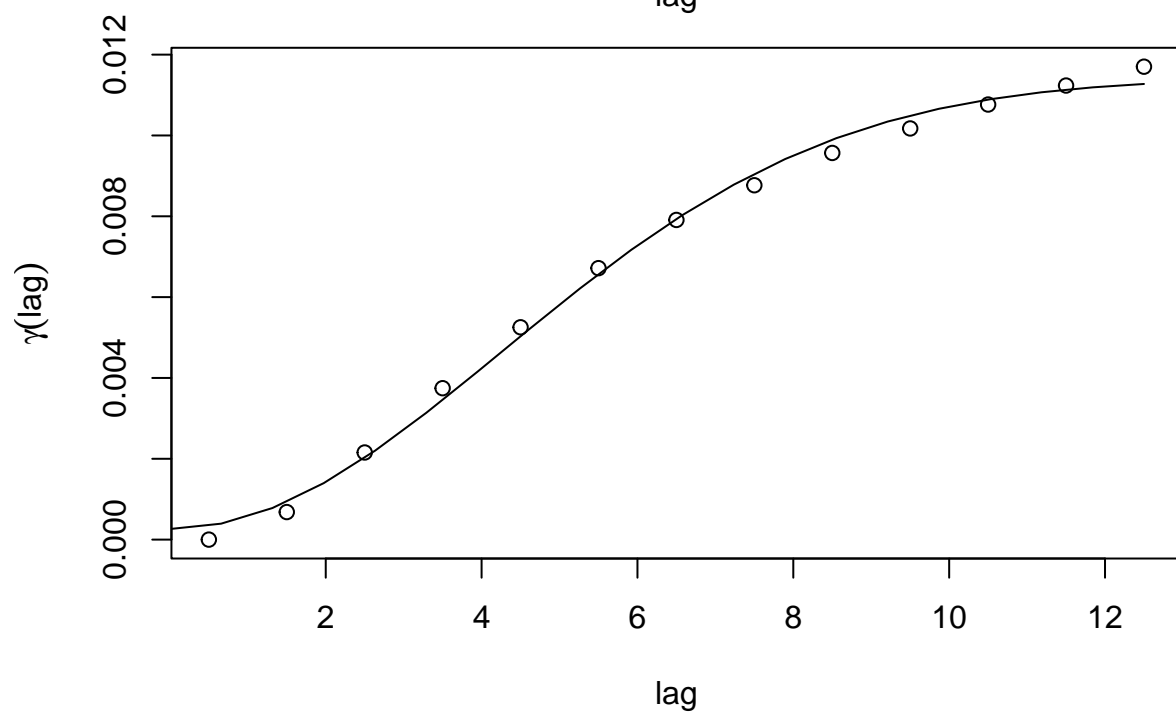
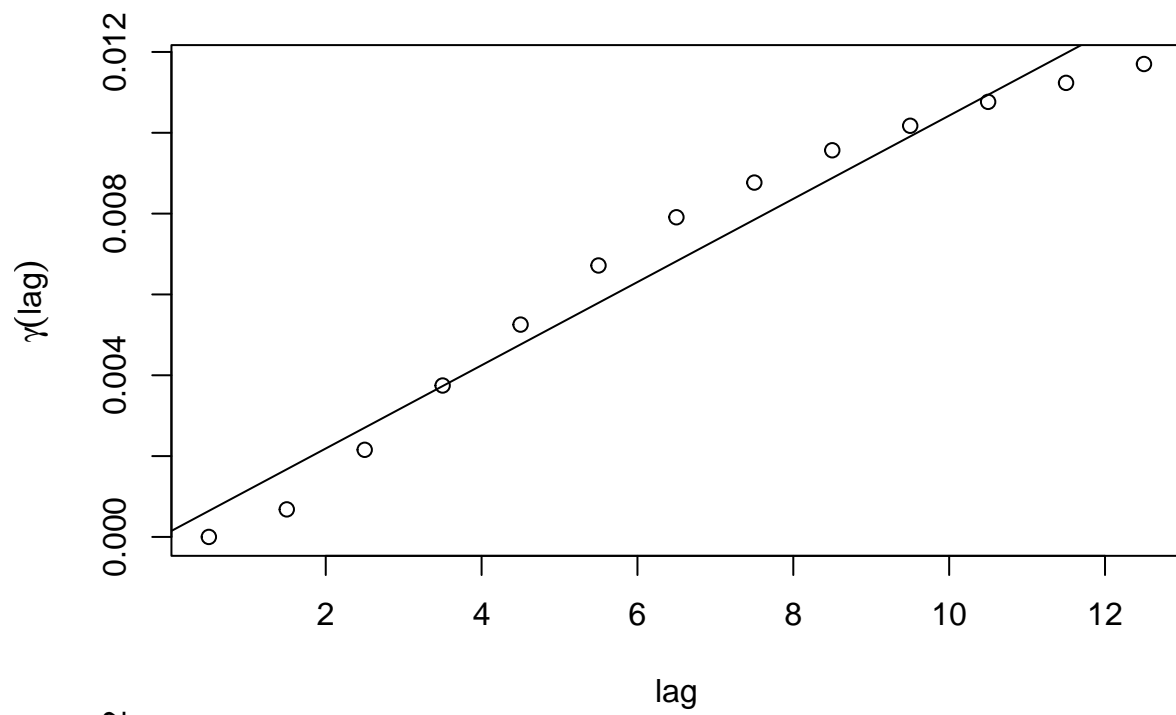


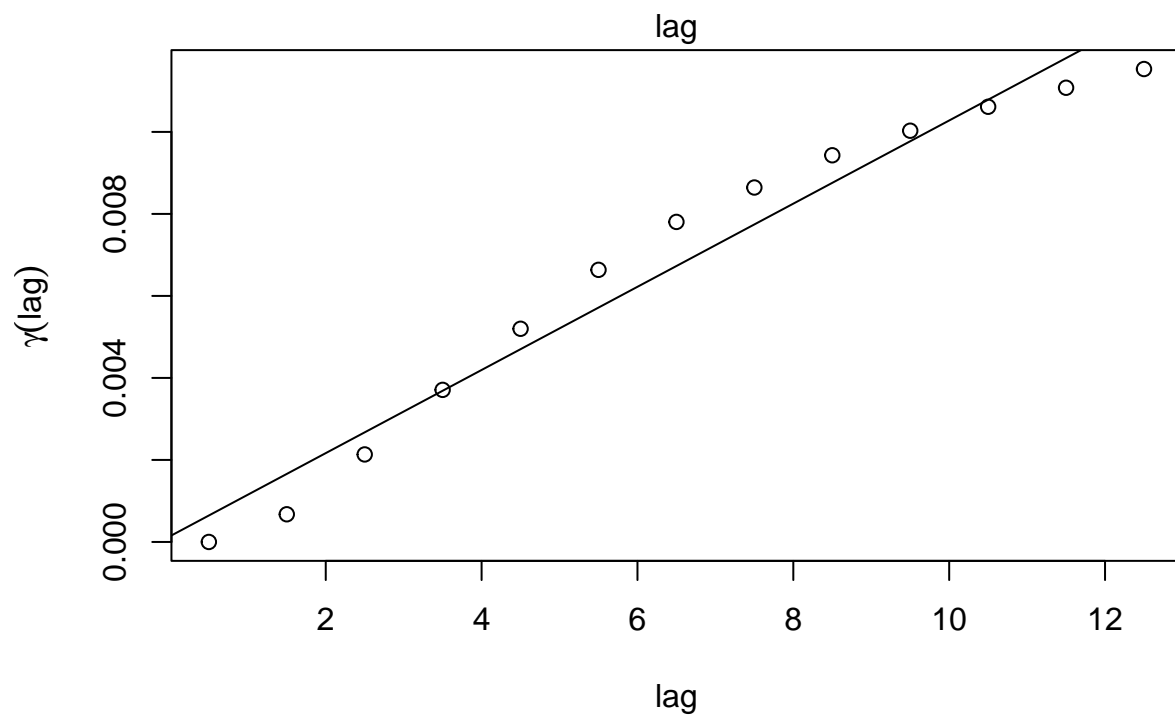
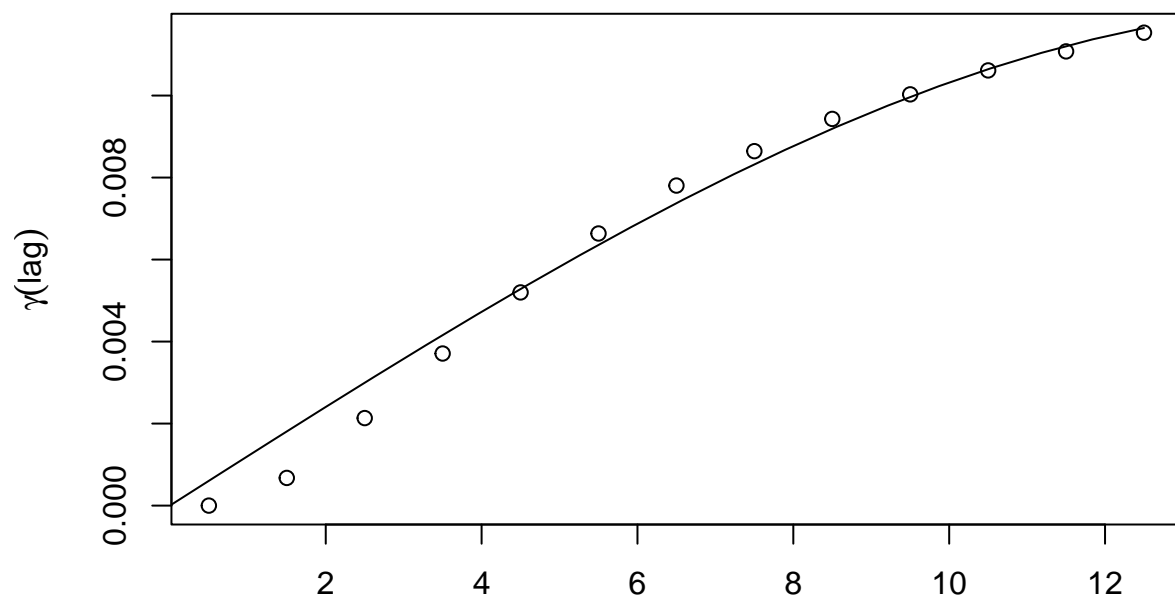


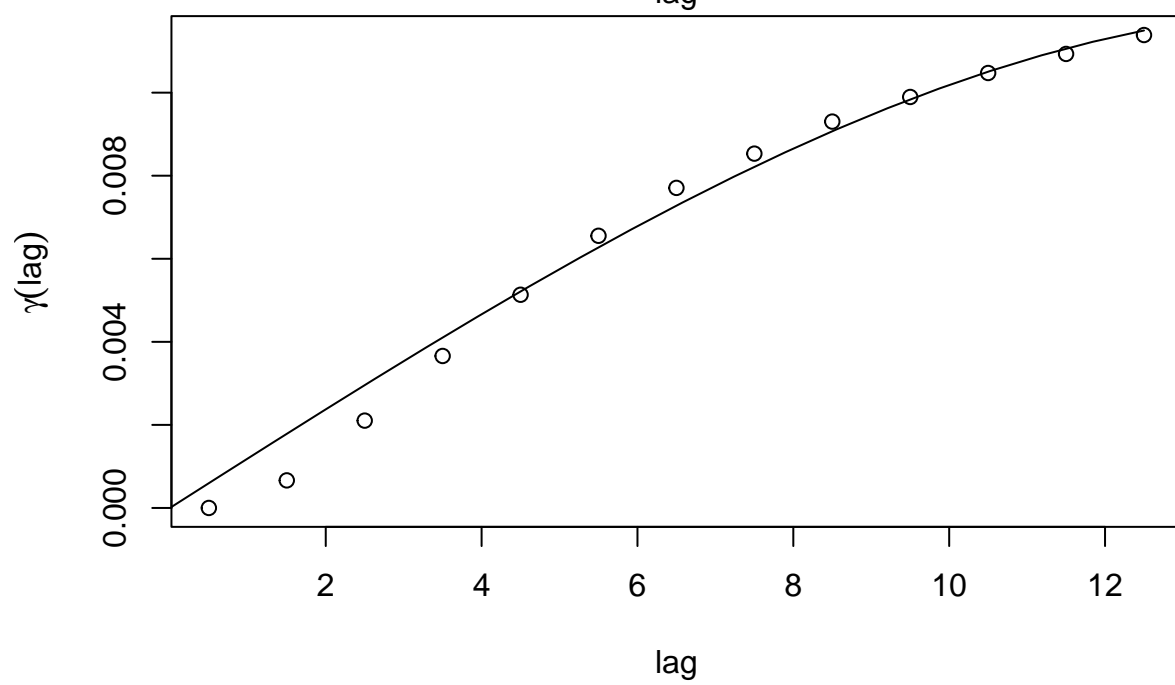
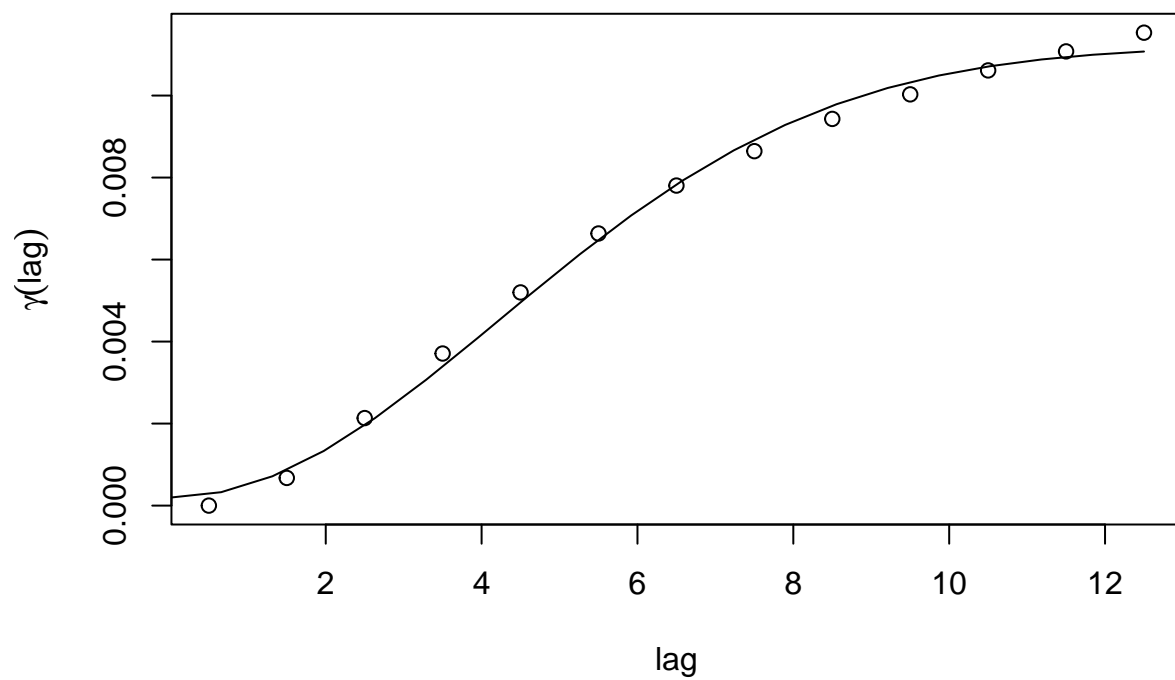


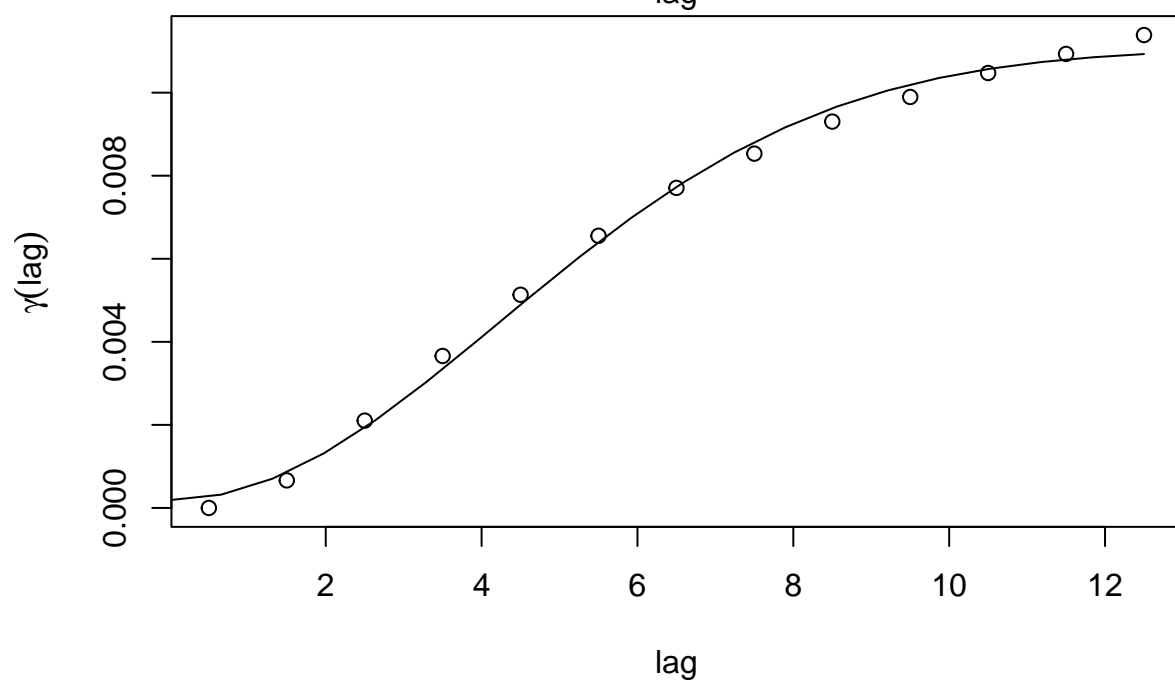
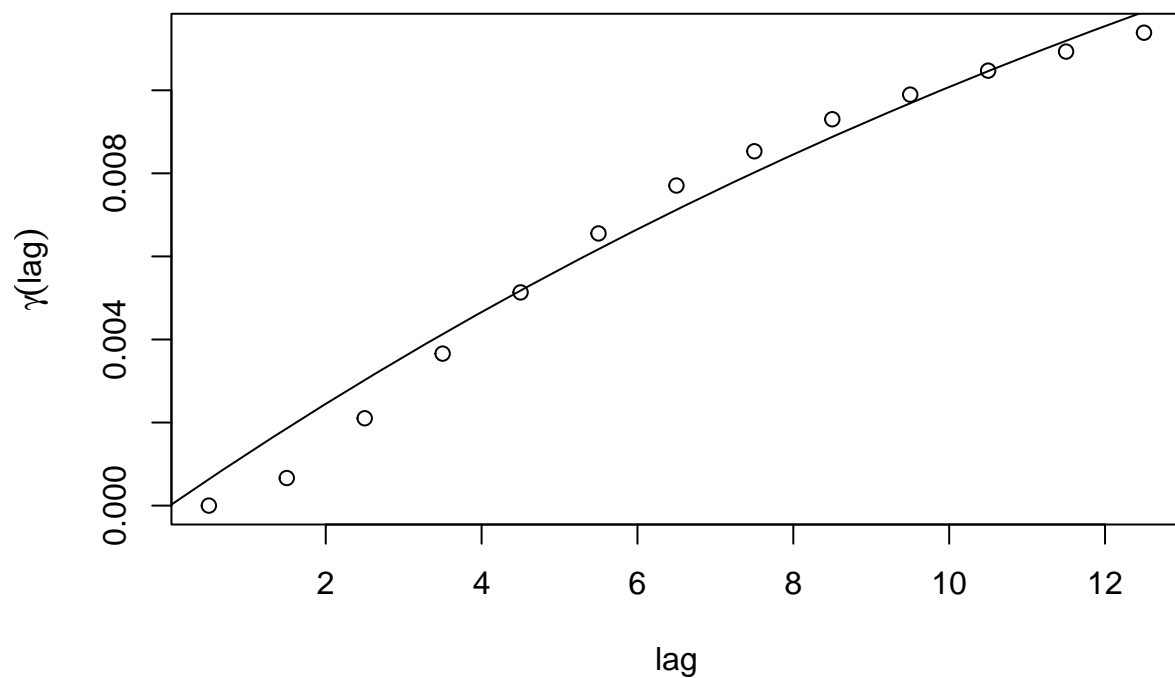




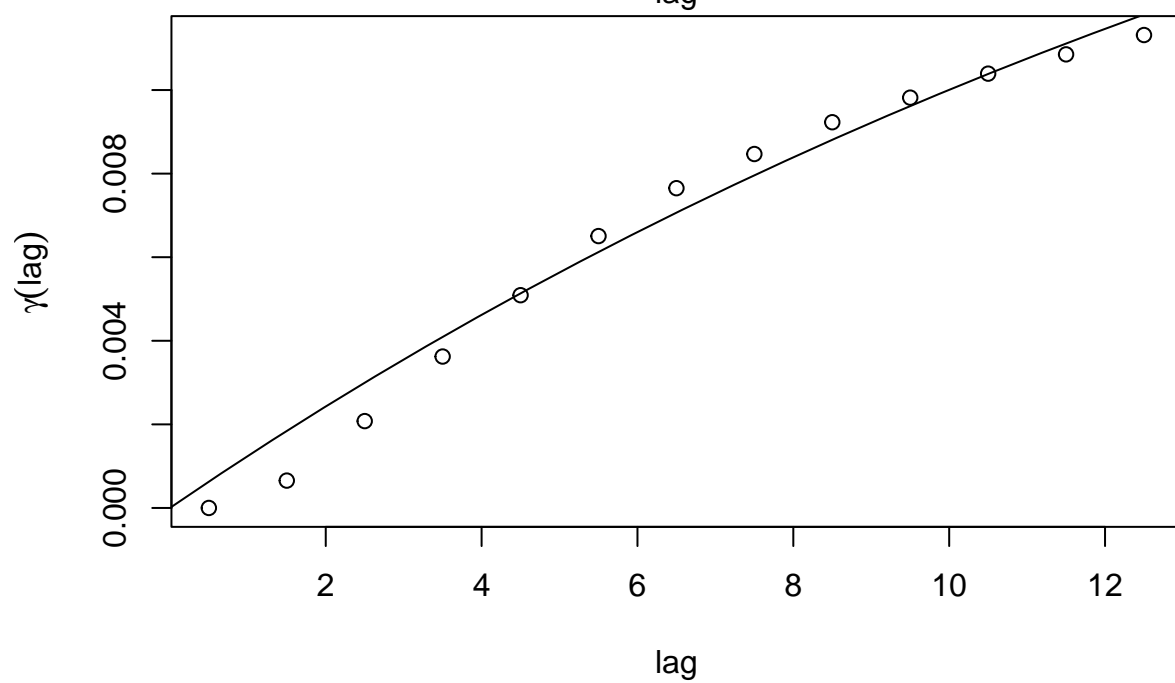
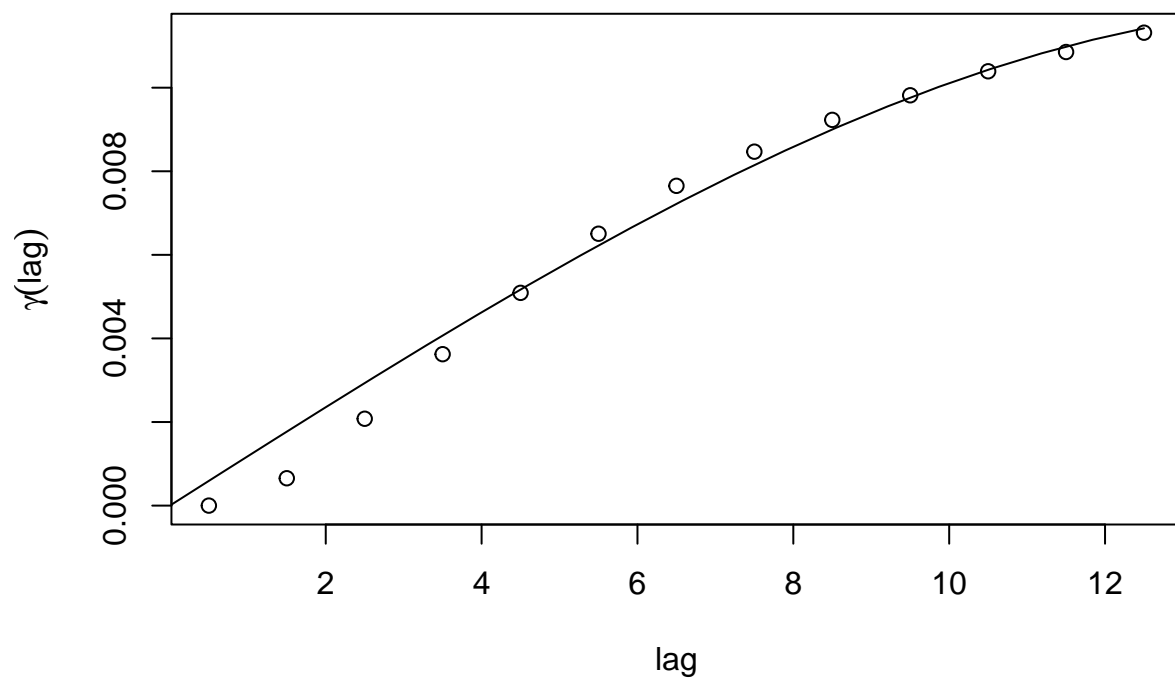


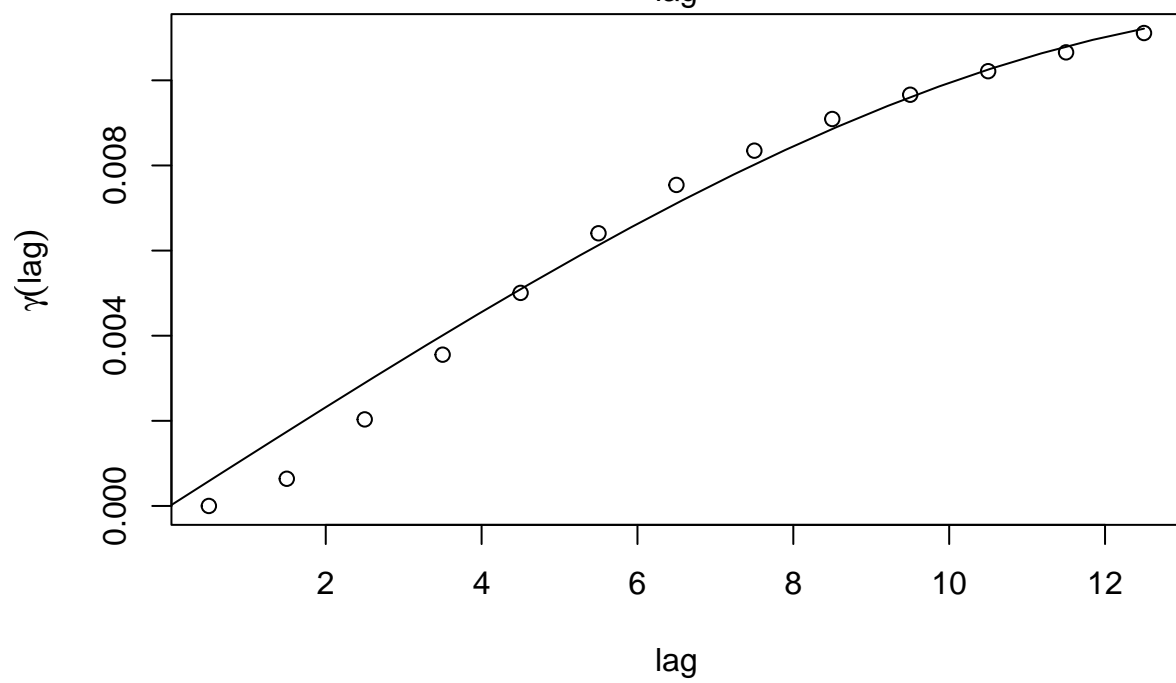
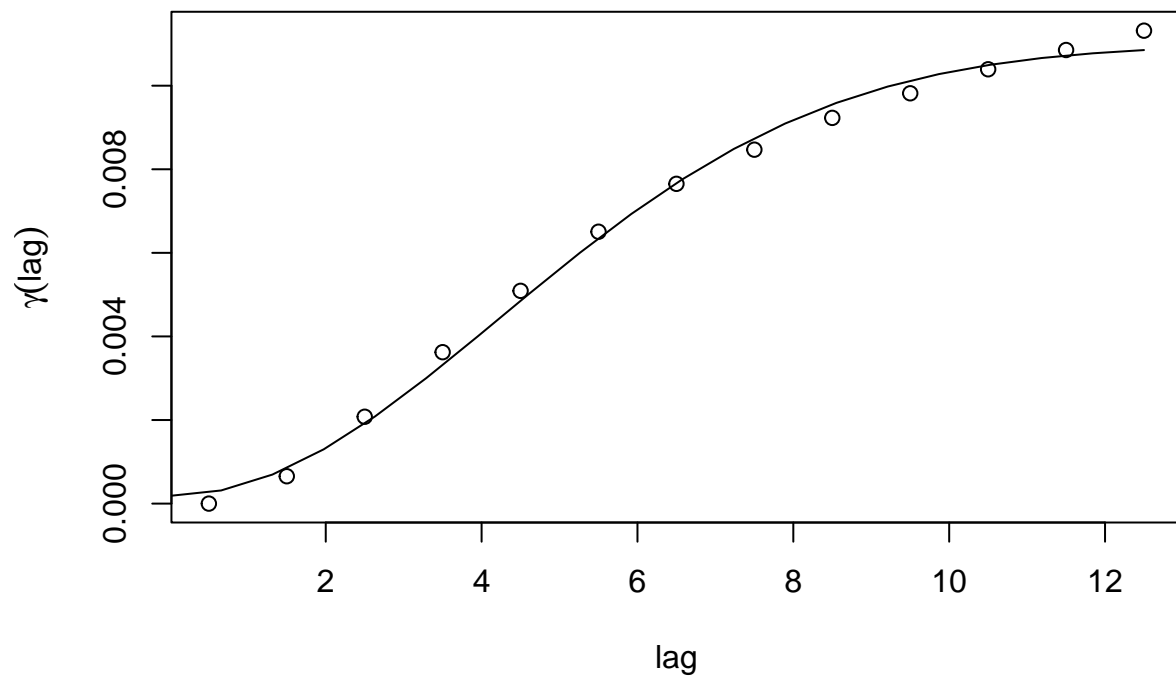


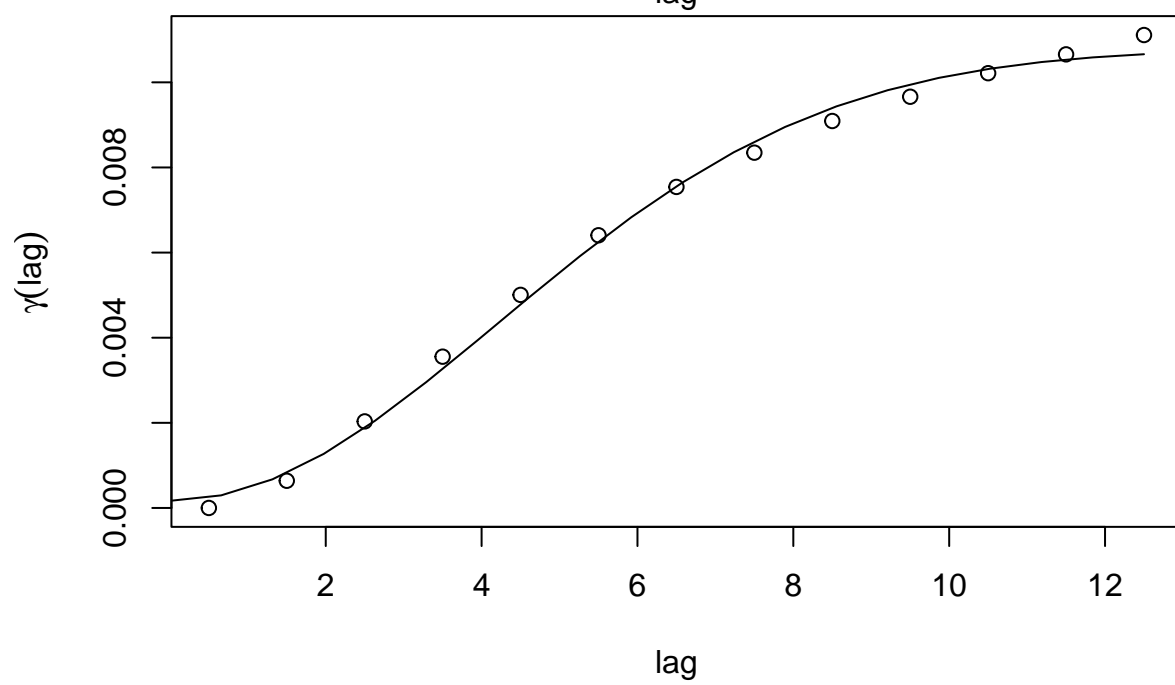
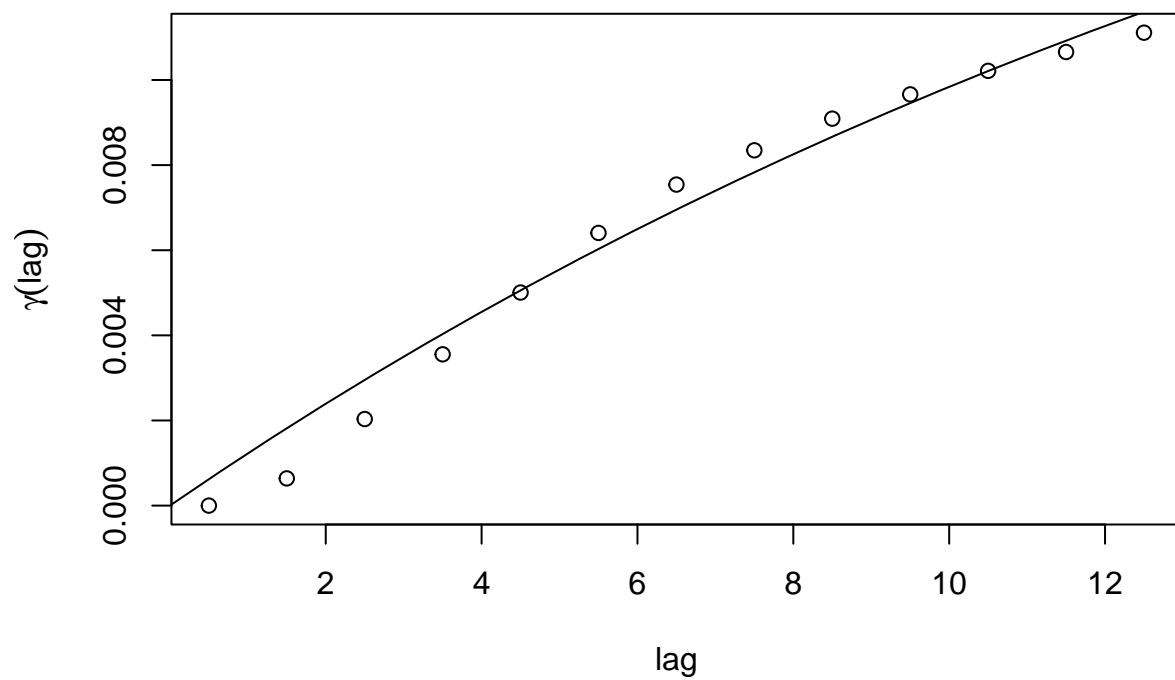


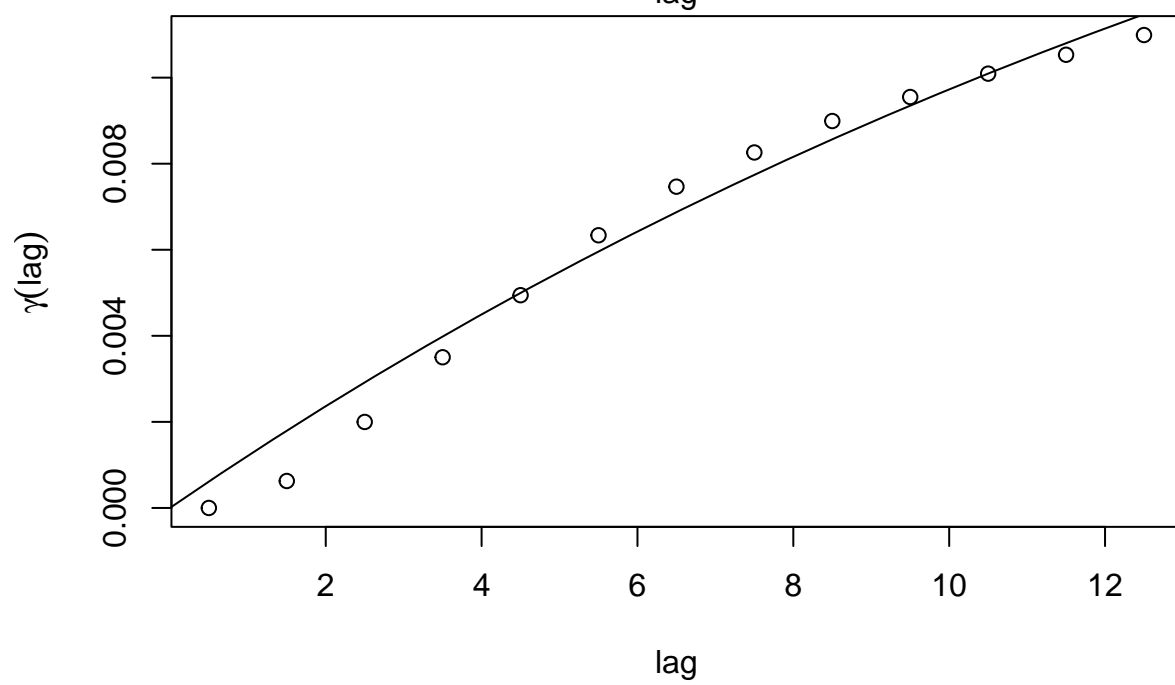
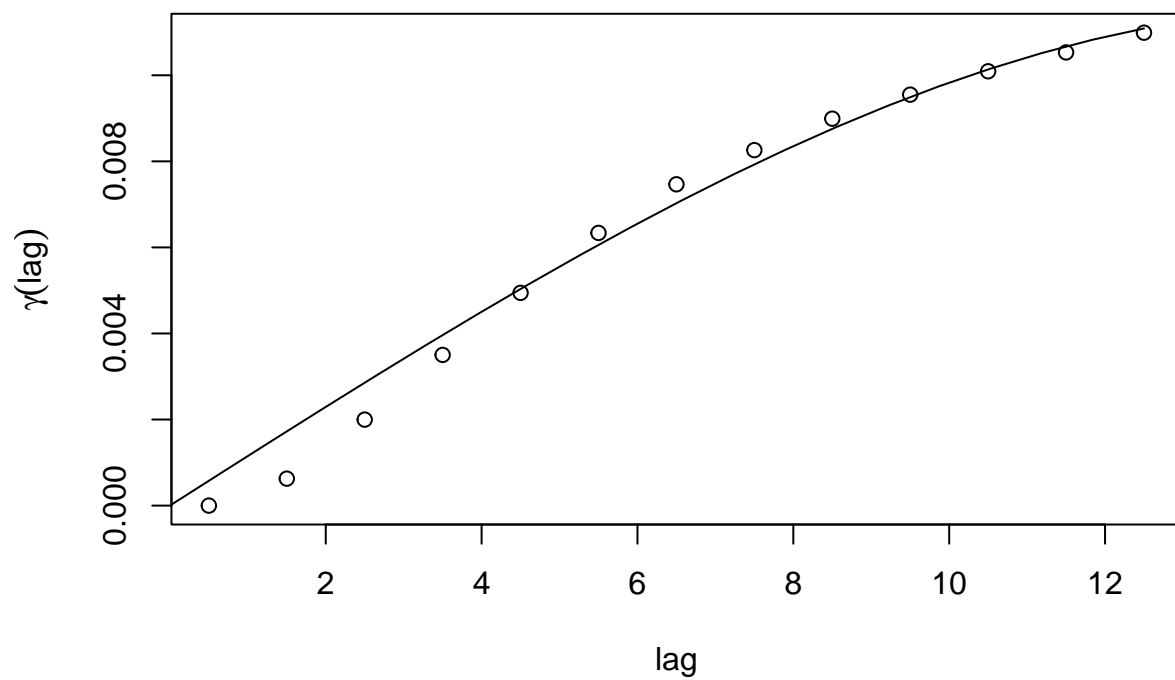


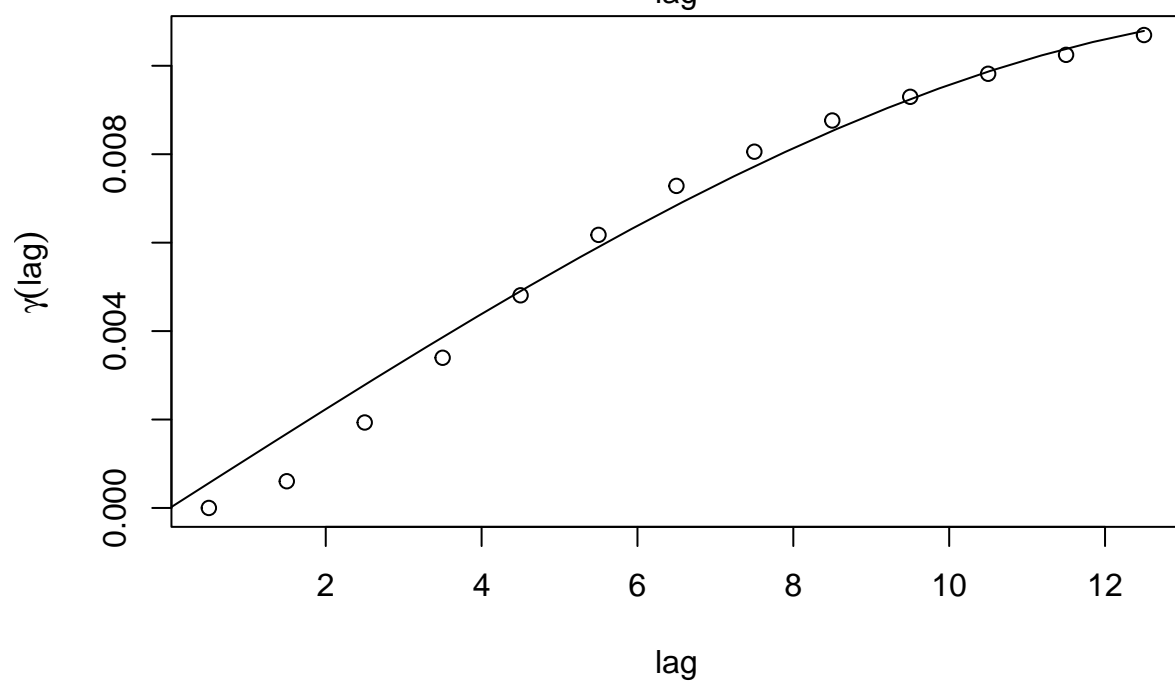
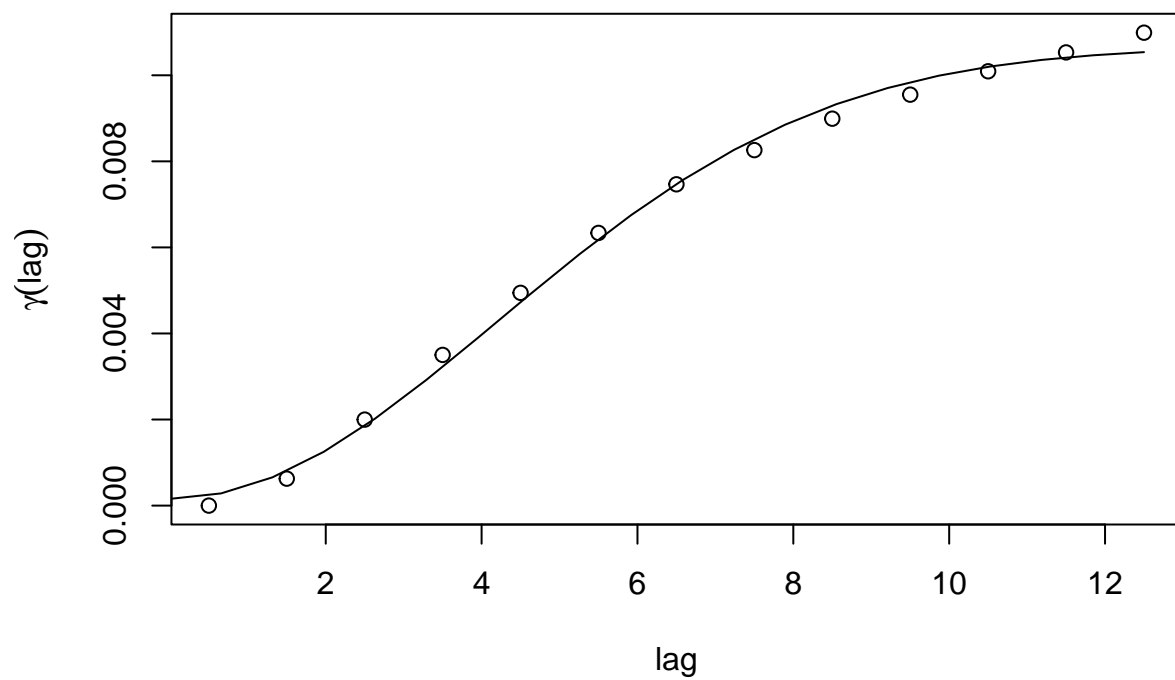


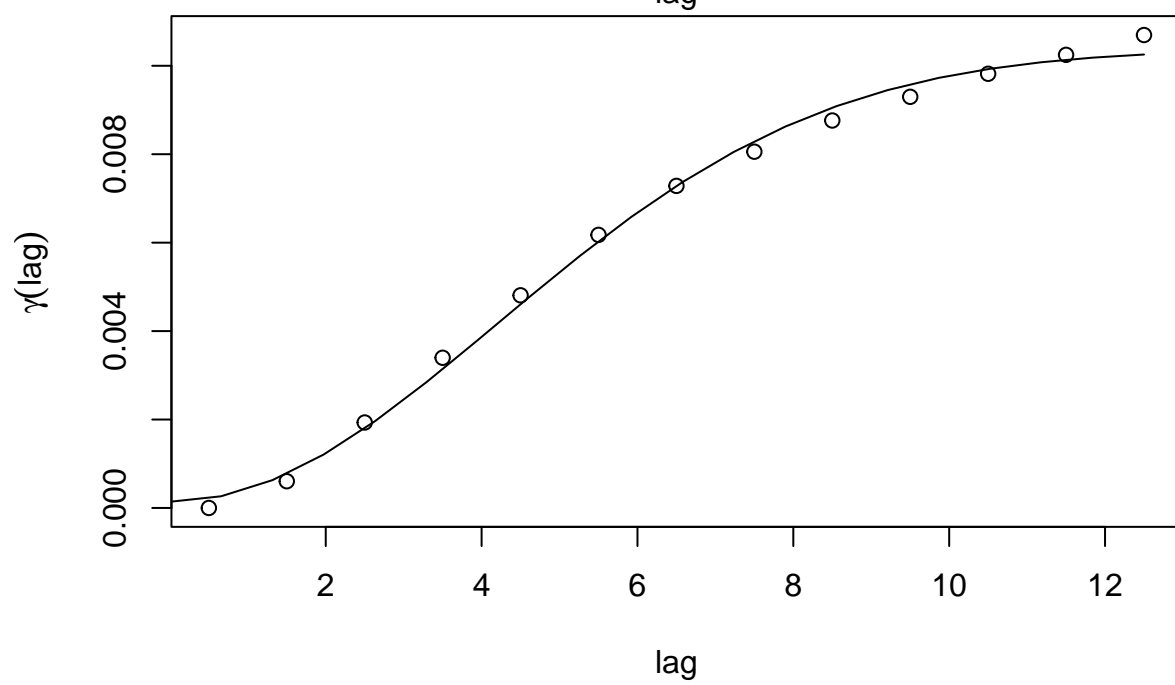
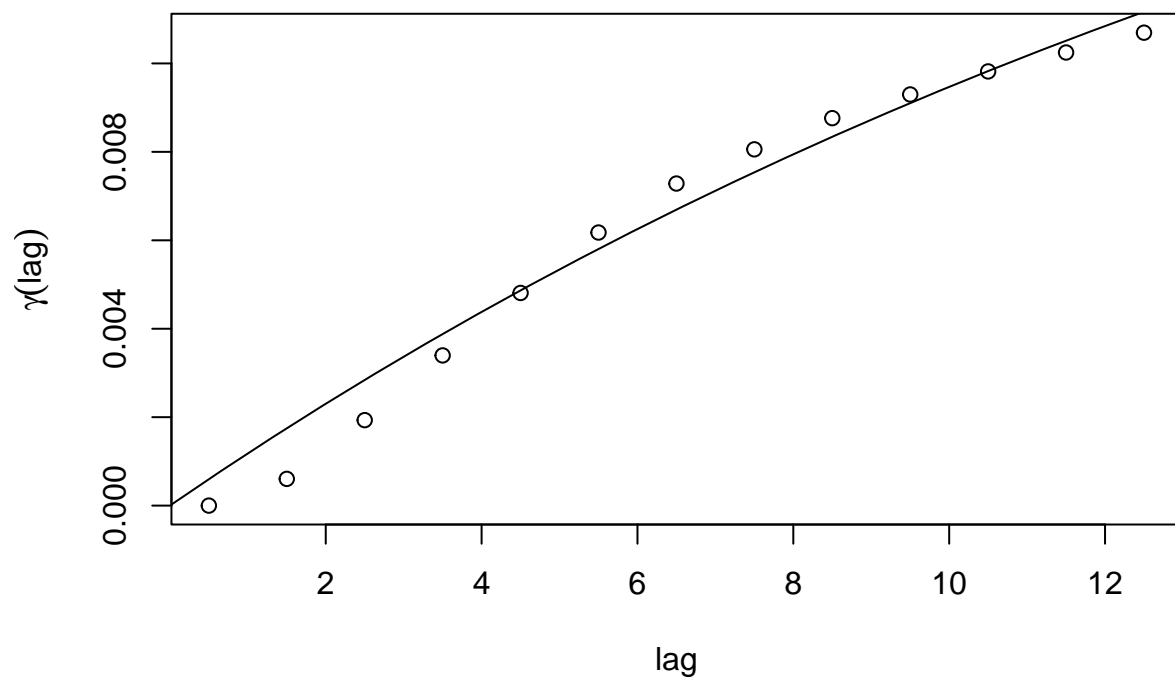


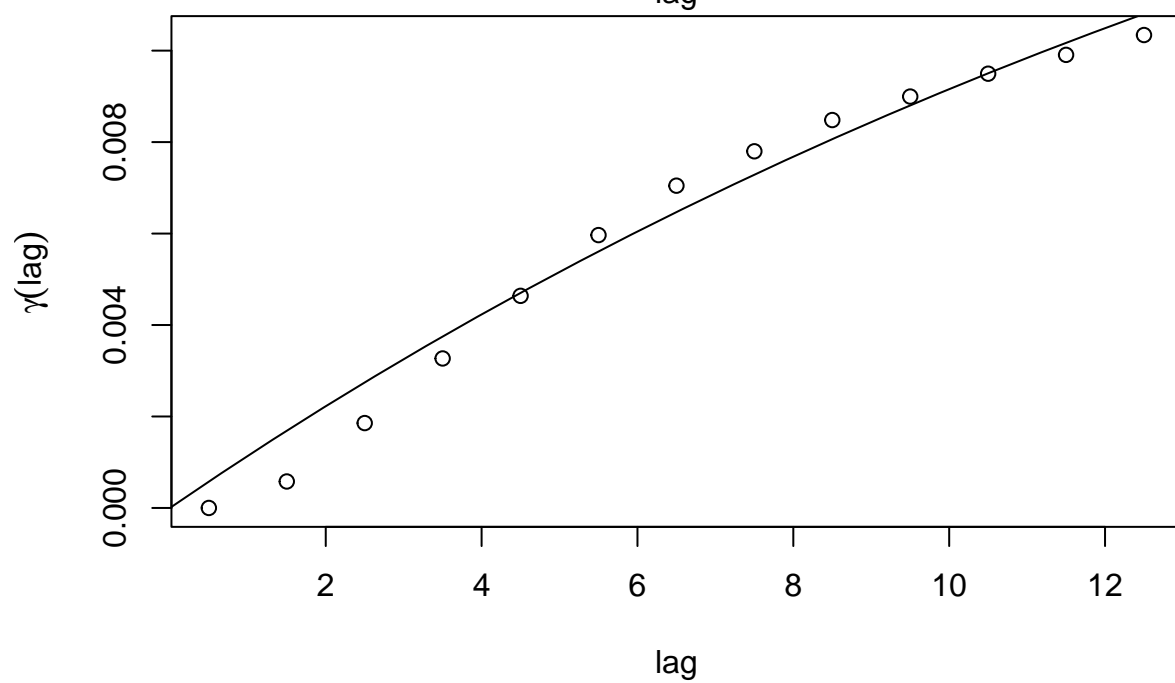
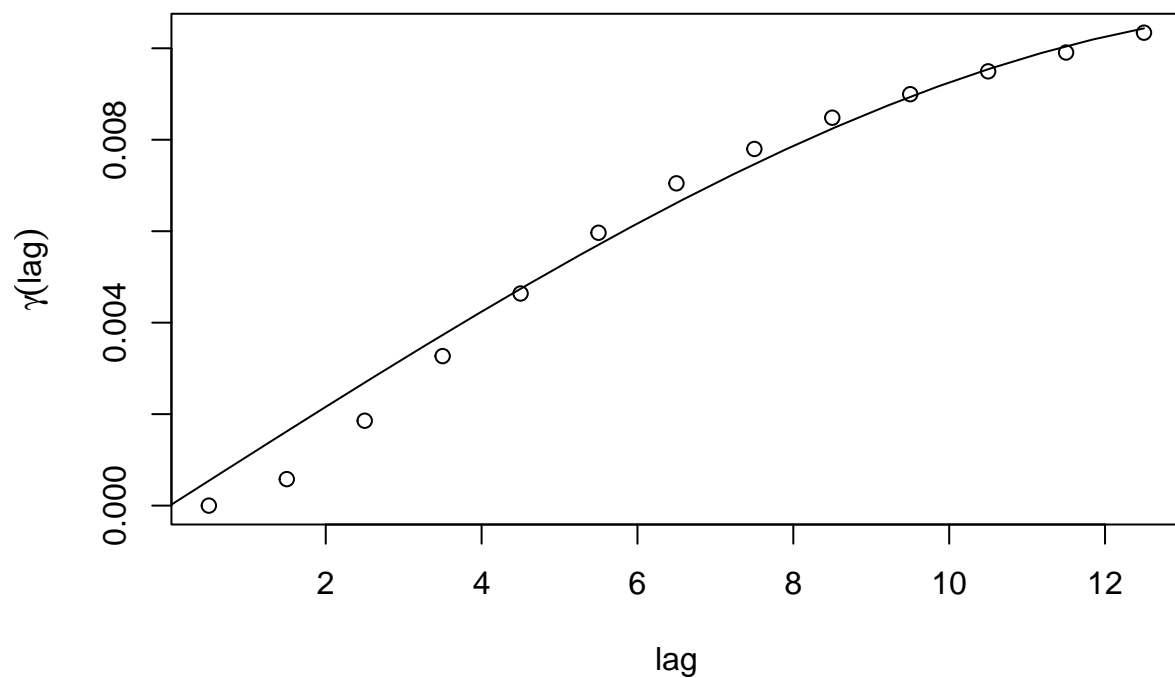


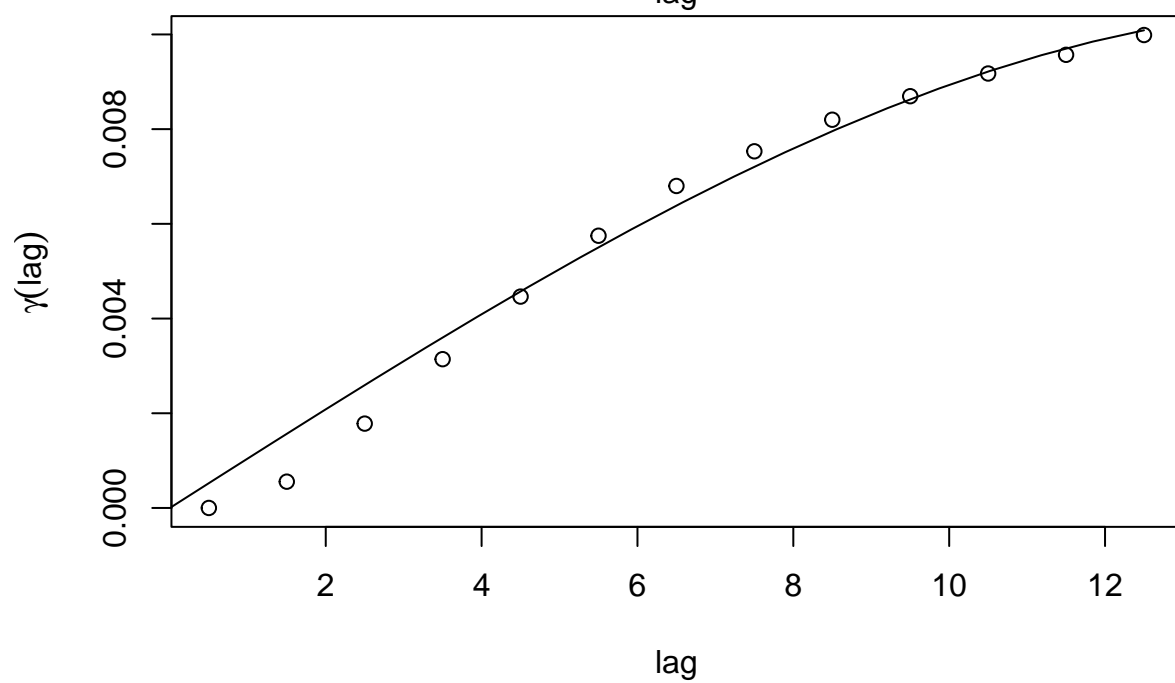
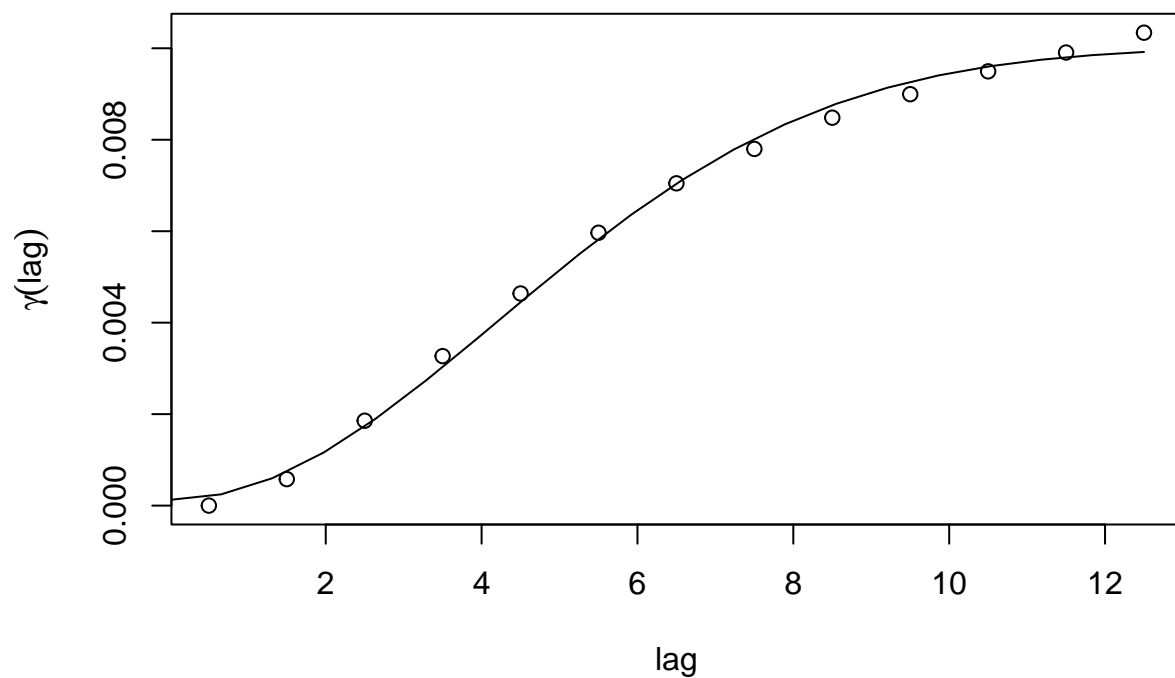




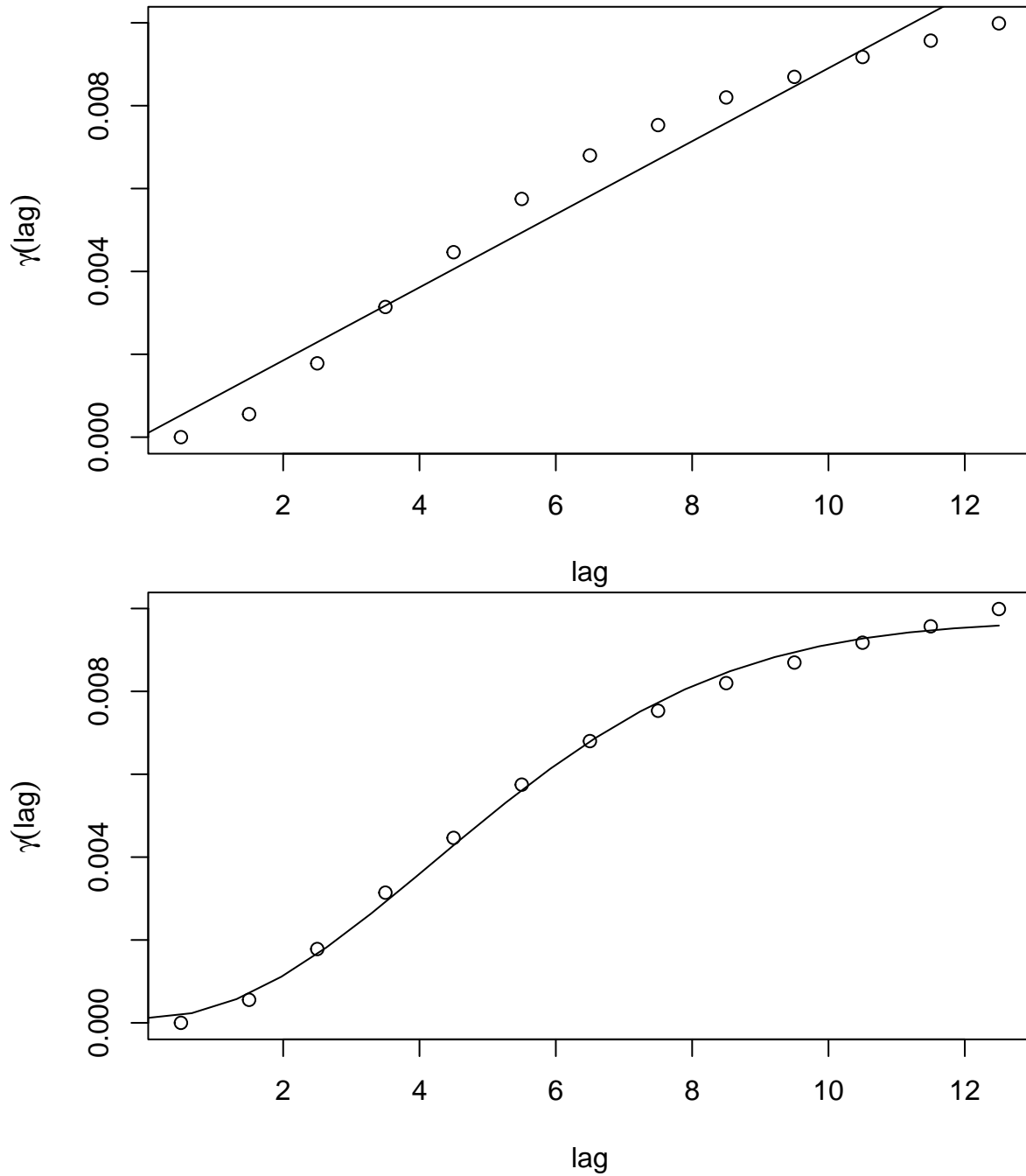












Based on visual assessment, the Gaussian model is the best fit to the relative abundance reconstructions. We can now use the parameters from this model to make inference about the distance of spatial correlation and its strength.

Here are the distances after which grid cells are deemed independent (in number of grid cells, the “range” parameter):

Taxon	Range (n. cells)
Ash	5.35352817075948
Beech	5.24993499783092
Birch	6.55520441471825
Elm	5.97101249033522
Hemlock	6.9855825624843
Maple	4.6476065817496
Oak	7.38899973865207
Other conifer	8.90685705597372
Other hardwood	4.96294809813878
Pine	3.18237895572842
Spruce	9.34620522357308
Tamarack	6.01398752765157

# Omnidirection variogram

Next, I will compute the omnidirectional variogram for each taxon at each time step. I do these at each time

step because I expect that the spatial correlation may change as a function of time.