# Natural Language Processing for Law and Social Science

6. Sequence Embeddings

# Catching up from last week

- ▶ Presentation on Kozlowski et al
- ► Rest of word embedding slides

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- low-dimensional dense vectors rather than high-dimensional sparse vectors
- Embedding without neural nets:
  - ▶ PCA reductions of the document-term matrix
  - LDA topic shares

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- Embedding without neural nets:
  - ▶ PCA reductions of the document-term matrix
  - LDA topic shares
- Embedding with neural nets (today):
  - many useful ways to do this.

#### Outline

Embedding Sequences Without Word Order (CBOW)

**Embedding Sequences without Transformers** 

Transformers: Embedding Sequences with Attention

## Word Vectors can produce Document Vectors

$$\vec{D} = \sum_{w \in D} a_w \vec{w}$$

- The "continuous bag of words" (CBOW) representation for document D is the sum, or the average (potentially weighted by  $a_w$ ), of the vectors  $\vec{w}$  for each word w in the document.
  - $\blacktriangleright$  word vectors  $\vec{w}$  constructed using pre-trained GloVe or Word2Vec.
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  - word vectors  $\vec{w}$  constructed using pre-trained GloVe or Word2Vec.
  - "Document" could be sentence, paragraph, section, etc. (scales well to long docs)
- Arora, Liang, and Ma (2017) provide a "tough to beat baseline", the SIF-weighted ("smoothed inverse frequency") average of the vectors:

$$a_w = \frac{\alpha}{\alpha + p_w}$$

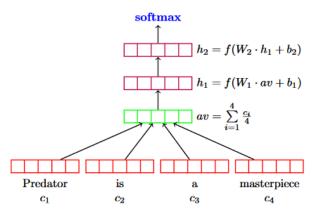
where  $p_w$  is the probability (frequency) of the word and  $\alpha = .001$  is a smoothing parameter.

# Deep Averaging Network (lyyer et al 2015)

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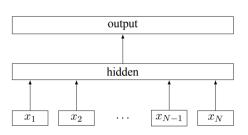
- 1. Trainable embedding layer for words, initialized with pre-trained embeddings
- 2. Average the embeddings, with dropout (sometimes words left out of average)
- 3. Average embedding fed into MLP with multiple hidden layers
- 4. MLP outputs used for classification or regression

# Hashed N-Gram Embeddings (Joulin et al 2016)

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**Figure 1:** Model architecture of fastText for a sentence with N ngram features  $x_1, \ldots, x_N$ . The features are embedded and averaged to form the hidden variable.

- 1. Allocate  $n_w \approx 10$  million rows to embedding matrix.
- 2. Assign n-grams to embedding indexes with hashing function.
- sentence embedding = average of n-gram embeddings
- 4. send to dense hidden layer(s)
- 5. send to output (e.g. classifier / regressor).

Captures local word-order information from n-grams without building vocabulary or costly training of Convolutional Neural Net.

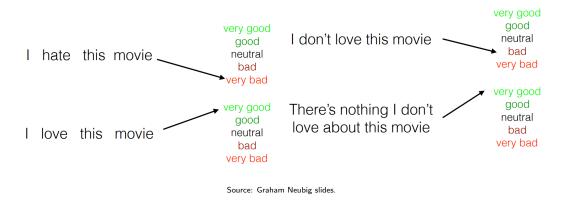
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Transformers: Embedding Sequences with Attention

#### The Classic Sentence Classification Problem



- bag-of-words models won't capture the importance of "don't love" or "nothing I don't love", even with interactions / hidden layers.
- ▶ N-grams have a large feature space (especially with 4-grams) and don't share information across similar words/n-grams.

## Sequence Data

- ▶ The real break-through from deep learning for NLP:
  - moving from bag-of-X representations to sequence representations.
  - ▶ Rather than inputting counts over words/n-grams x, take as input a sequence of tokens  $\{w_1,...,w_t,...w_n\}$ .

#### Sequence Data

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  - Rather than inputting counts over words/n-grams x, take as input a sequence of tokens  $\{w_1,...,w_t,...w_n\}$ .
- "Traditional" architectures:
  - Convolutional neural nets (CNNs)
  - Recurrent Neural Nets (RNNs)
- "Modern" architectures:
  - ► Transformers ("attentional" neural nets) and variants

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We saw this example last time, which produces document embeddings:

- ► Tokenize document to fixed length n<sub>L</sub>
- Inputs are each word position, input categorical (word) to  $n_E$ -dimensional embedding layer:

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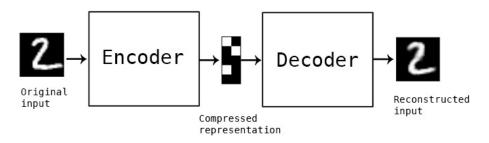
- $\triangleright$  Tokenize document to fixed length  $n_L$
- Inputs are each word position, input categorical (word) to  $n_E$ -dimensional embedding layer:

- pipe to further hidden layers of network.
- ightharpoonup document embedding =  $n_L n_E$ -dimensional vector of concatenated word embeddings.
  - computationally demanding and only works with short documents.

# Autoencoders: Optimal Compression Algorithms

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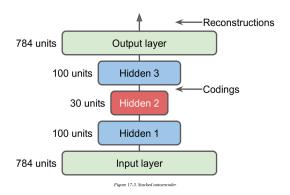
▶ Autoencoders = neural nets that perform domain-specific lossy compression:



- ► Learned encodings can be decoded back to a *reconstruction* a (minimally) lossy representation of the original data.
- AE's can memorize complex, unstructured data deep unsupervised learning.

#### Autoencoder Architecture – Neural net with output=input

- Stacked layers gradually decrease in dimensionality to create the compressed representation
- then gradually increase in dimensionality to try to reconstruct the input.



#### Reconstruction from encoded vector



Figure 17-4. Original images (top) and their reconstructions (bottom)

## Autoencoder Encodings are Embeddings

- ▶ Autoencoder compresses a document (e.g. a sentence) into a vector to be reconstructed.
  - Can use the compressed representation as a document embedding.
- ▶ Standard (that is, non-transformer) autoencoder embeddings don't tend to work well for sentence similarity tasks because autoencoders try to reproduce the specific wording (reconstruction objective), rather than the semantic meaning.
  - transformer-based autoencoders, i.e. BART, address this issue (next week)

#### Convolutional Neural Nets ↔ N-gram Detectors

A neural net architecture that constructs **filters** that slide across input sequences and extract **local predictive structure**.

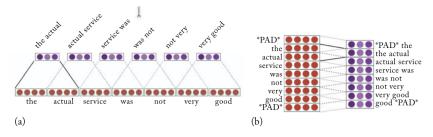


Figure 13.1: The inputs and outputs of a narrow and a wide convolution in the vector-concatenation and the vector-stacking notations. (a) A *narrow* convolution with a window of size k=2 and 3-dimensional output  $(\ell=3)$ , in the vector-concatenation notation. (b) A *wide* convolution with a window of size k=2, a 3-dimensional output  $(\ell=3)$ , in the vector-stacking notation.

➤ Overall, CNNs do not work well in NLP; use embedded hashed n-grams instead (Joulin et al 2016, Goldberg 2017).

In-Class Presentation Garg et al (2018), Word embeddings quantify 100 years of gender and ethnic stereotypes

## RNNs can input and output arbitrary-length sequences

- Downsides of previous approaches:
  - ► CBOW models (averaged word/phrase embeddings) lose any sequence information beyond local word order encoded by n-grams
  - ▶ all-token embedding, and CNNs, require fixed-length documents

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- Downsides of previous approaches:
  - ► CBOW models (averaged word/phrase embeddings) lose any sequence information beyond local word order encoded by n-grams
  - ▶ all-token embedding, and CNNs, require fixed-length documents
- Recurrent Neural Nets (RNNs) work with sequences of arbitrary length, both as inputs and outputs:
  - can encode sequences into vectors.
  - can decode vectors into sequences.
- therefore especially useful for language tasks such as translation.

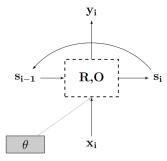
# Summary of RNN Architecture

- At each step *t*:
  - ▶ a recursion function  $R(s_{t-1}, x_t; \theta_R)$  computes the state vector  $s_t$  given current word  $x_t$  and previous state  $s_{t-1}$ .

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  - An output function  $O(s_t; \theta_O)$  computes an output vector  $y_t$  (to be compared to the outcome variable in the dataset).

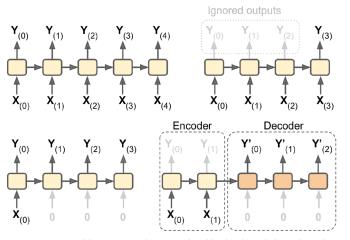
$$\hat{\boldsymbol{y}}_t = O(\boldsymbol{s}_t, \theta_O)$$
  
 $\boldsymbol{s}_t = R(\boldsymbol{s}_{t-1}, \boldsymbol{x}_t, \theta_R)$ 



▶ The parameters of those functions,  $\theta = (\theta_R, \theta_O)$  are learned during model training.

## RNN Encoding and Decoding

top left: sequence to sequence; top right: sequence to vector



Figure~15-4.~Seq-to-seq~(top~left),~seq-to-vector~(top~right),~vector-to-seq~(bottom~left),~and~Encoder-Decoder~(bottom~right)~networks

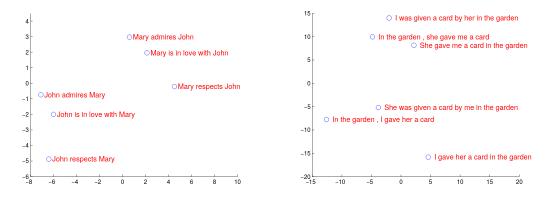
bottom left: vector to sequence; bottom right: encoder-decoder.

# Gated RNNs – LSTM (Long Short-Term Memory)

- Gating mechanisms prevent vanishing/exploding gradients.
- ▶ bidirectional LSTMs (trained backward and forward) get state-of-the-art performance on text classification of short documents (e.g. classifying sentences by sentiment), but rarely better than transformer models.
- ► See Goldberg (2017) if curious.

# RNN's (e.g. Machine Translation) Produce Document Embeddings

- ▶ RNN machine translators produce a sentence vector that must be decoded into another language.
- ▶ if the vector produces a good translation, it must contain the important information in the sentence.



Sutskever, Vinyals, and Le, "Sequence to sequence learning with neural networks."

#### Outline

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Transformers: Embedding Sequences with Attention

# Deep Learning with NLP $\approx$ Transformers

- ➤ Since a 2017 paper (Vaswani et al 2017), most deep learning for NLP uses the transformer architecture.
- Recurrent neural nets can process whole documents word-by-word, but they have to sweep through the whole document at each training epoch. They learn too slowly.
- Transformers overcome this limitation:
  - intuitively, they provide a way to efficiently read in an entire document and learn the meaning of all words and all interactions between words.

## Transformers = Attentional Neural Nets

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## Attention does two things:

- 1. On a technical level:
  - ▶ allows a neural net to build many implicit databases of key-value pairs (a la python dictionaries), and to efficiently query those databases.

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## Attention does two things:

- 1. On a technical level:
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- 2. On a linguistic level:
  - allows a neural net to build a set of implicit key-value databases:
    - the keys are pairs of words
    - the value is a learnable vector that helps in some prediction task, e.g. predicting the next word in a sequence.

#### Attention heads

Transformers consist of stacked blocks of parallel attention heads ► Attention heads are machine-reading filters, which allow each word to scan over every other word in the document and pick up predictive interactions.

Shortcut: Using huggingface Pre-Trained Models

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```
from transformers import pipeline
sentiment analysis = pipeline("sentiment-analysis")
pos text = "I enjoy studying computational algorithms."
neg text = "I dislike sleeping late everyday."
pos sent = sentiment analysis(pos text)[0]
print(pos sent['label'], 0 pos sent['score'])
neg sent = sentiment analysis(neg text)[0]
print(neg sent['label'], neg sent['score'])
```

- ▶ also straightforward to fine-tune BERT for your own classification tasks.
- see notebooks for full details / explanation.

## Queries, Keys, and Values

- Assume a database  $D = \{(k_1, v_1), ...(k_m, v_m)\}$ 
  - m tuples of keys and values.
  - ▶ Denote by *q* a "query".
  - ▶ e.g., a python dictionary; query is used to look-up; normally one of the keys.

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#### Define

$$\mathsf{Attention}(q) = \sum_{i=1}^m a(q, k_i) v_i$$

- ▶  $a(\cdot)$  are scalar "attention weights"; they give more weight ("pay more attention") to some items based on q and  $k_i$ .
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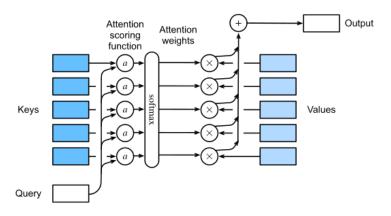
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- In a normal database query / dictionary, a(q, k) = 1 if q = k and zero otherwise.
- ▶ in a transformer, this is generalized such that  $a(\cdot) \ge 0$ ,  $\sum a(\cdot) = 1$ .
- ightharpoonup achieved for any weighting function  $a_0$  by a softmax operation:

$$a(q, k_i) = \operatorname{softmax}(a_o(q, k_i)) = \frac{\exp(a_0(q, k_i))}{\sum_j \exp(a_o(q, k_j))}$$

↑ differentiable and gradient never vanishes.

# Scaled dot product attention



- ightharpoonup let q and k be vectors with dimension d.
- scaled dot product attention:

$$a(q, k_i) = \operatorname{softmax}(\frac{q \cdot k_i}{\sqrt{d}})$$

# Self-Attention with word embeddings

- Consider a sequence of tokens with fixed length  $n_L$ ,  $\{w_1,...,w_i,...,w_{n_L}\}$
- ▶ We have (learnable) word embeddings  $x_i = \omega_E w_i$  with dimension  $n_E$ , producing a sequence of vectors

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▶ A **self-attention layer** transforms  $x_{1:n_L}$  into a second sequence  $h_{1:n_L}$  with

$$h_i = \sum_{j=1}^{n_L} a(x_i, x_j) x_j$$

- ▶ where  $a(\cdot)$  is an attention function such that  $a(\cdot) \ge 0$ ,  $\sum a(\cdot) = 1$ .
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- ightharpoonup each  $h_i$  becomes a weighted average of the whole sequence.
- ▶ if sequence length  $n < n_L$ , set  $a_i = 0$  for all i > n.
- $ightharpoonup h_{1:n_l}$  is flattened and piped to the network's hidden layers.

## **Basic** Self-Attention

## Setup:

- 1. Sequence of tokens  $\{w_1, ..., w_i, ..., w_{n_l}\}$
- 2. Sequence of (trainable) embedding vectors  $\{x_1,...,x_i,...,x_{n_L}\}$
- 3. Sequence of attention-transformed vectors  $\{h_1,...,h_i,...,h_{n_l}\}$  with

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**Basic self-attention** uses scaled dot product attention:

$$a(x_i, x_j) = \operatorname{softmax}(\frac{x_i \cdot x_j}{\sqrt{n_E}}) = \frac{\exp(\frac{x_i \cdot x_j}{\sqrt{n_E}})}{\sum_{k=1}^{n_L} \exp(\frac{x_i \cdot x_j}{\sqrt{n_E}})}$$

▶ the scaled dot-product  $\frac{x_i \cdot x_j}{\sqrt{n_E}}$ , normalized with softmax such that  $\sum_j a(\cdot) = 1$ .

► The self-attention transformation

$$h_i = \sum_{j=1}^{n_L} a(x_i, x_j) x_j$$

with

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- basic self-attention has no learnable parameters.
  - self-attention works indirectly through the word embeddings (more next slide)
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The big initial gain from transformers, relative to RNNs, came from basic self-attention.

▶ But the successful models (e.g. BERT, GPT) do add parameters and word order information to  $a(\cdot)$ .

# Why self-attention works

Consider a sentence

the, cat, walks, on, the, street

with embeddings

$$\mathbf{X}_{\text{the}}, \mathbf{X}_{\text{cat}}, \mathbf{X}_{\text{walks}}, \mathbf{X}_{\text{on}}, \mathbf{X}_{\text{the}}, \mathbf{X}_{\text{street}}$$

► Feeding this sentence into the self-attention layer produces

$$h_{\mathsf{the}}, h_{\mathsf{cat}}, h_{\mathsf{walks}}, h_{\mathsf{on}}, h_{\mathsf{the}}, h_{\mathsf{street}}$$

where

$$\mathbf{h}_i = a(x_i \cdot \mathbf{x}_{\mathsf{the}})\mathbf{x}_{\mathsf{the}} + a(x_i \cdot \mathbf{x}_{\mathsf{cat}})\mathbf{x}_{\mathsf{cat}} + ... + a(x_i \cdot \mathbf{x}_{\mathsf{street}})\mathbf{x}_{\mathsf{street}}$$

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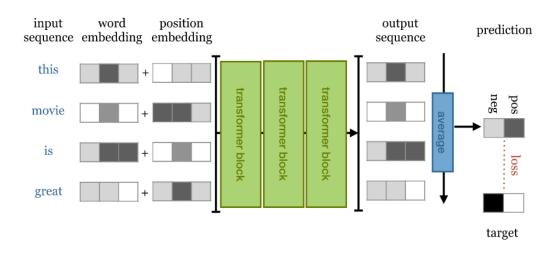
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Embedding layer will learn vectors **x** that tend to have **attention dot products** that contribute to the task at hand.

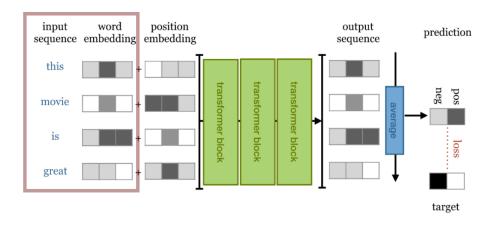
- ► For example, for most tasks, stopwords like "the" will not be helpful.
  - ightharpoonup the learned embedding  $x_{\text{the}}$  will tend to have a low or negative dot product with more informative words.

# In-Class Presentation Ash et al (2022), Gender attitudes in the judiciary

## Transformer Architecture: Sentiment Classification

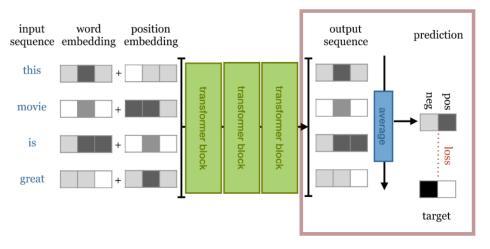


Input sequence → word embedding



- ▶ Input sequence of tokens  $\{w_1, ..., w_i, ..., w_{n_L}\}$
- ▶ Trainable embedding vectors  $[x_1...,x_i...x_{n_L}]$

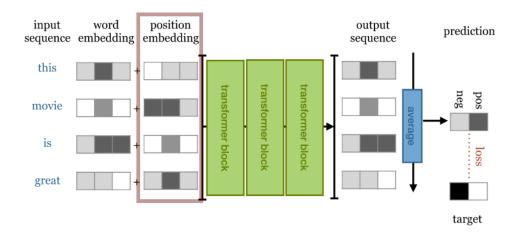
 $\dots \rightarrow \mathsf{document} \ \mathsf{embedding} \rightarrow \mathsf{sentiment} \ \mathsf{score}$ 



- ightharpoonup output sequence  $\{h_1^y,...,h_i^y,...,h_{n_l}^y\}$
- ightharpoonup averaged to produce **document vector**  $\vec{d}$
- final output layer with sigmoid activation to produce probabilities  $\hat{y}$  across positive and negative output classes.

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 $\dots \rightarrow \mathsf{position} \; \mathsf{embedding} \rightarrow \dots$ 

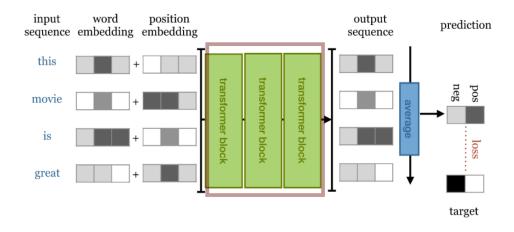


# Position Embeddings

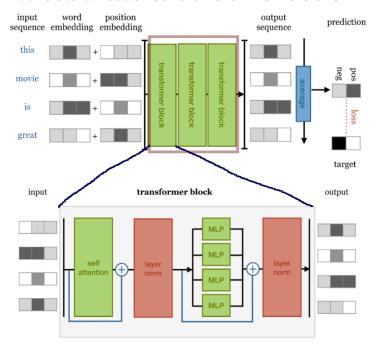
- ► To add word order information, transformers add a **position embedding** along with the **word embedding** as input to the attention layer.
- we have
  - word embeddings  $\{x_1,...,x_i,...,x_{n_l}\}$  each with dimension  $n_E$
  - ▶ position embeddings  $\{t_1,...,t_i,...,t_{n_L}\}$ , categorical embeddings for each position index i, also with dimension  $n_E$ .
- input to the first attention layer is element-wise addition of these embeddings,

$$h_{1:n_L=}^0\{x_1+t_1,...,x_{n_L}+t_{n_L}\}$$

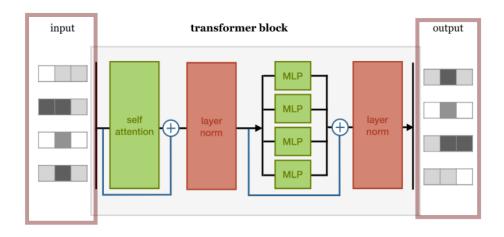
 $\dots \rightarrow \mathsf{transformer} \; \mathsf{blocks} \rightarrow \dots$ 



## A transformer consists of stacked transformer blocks



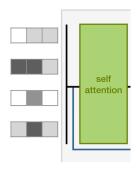
# Transformer block (input and output)



▶ Each transformer block  $l \in \{1,...,n_y\}$  takes as input a sequence of vectors  $h_{1:n_L}^{l-1}$  and outputs a sequence of vectors  $h_{1:n_L}^{l}$ , which become the input for the next transformer block.

# Transformer Block (Self-Attention Layer)

input



the "self attention" layer:

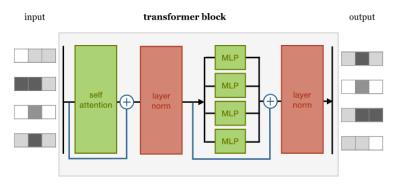
- ▶ input:
  - for the first block, includes the word embeddings summed with the position embeddings

$$h_{1:n_L=}^0\{x_1+t_1,...,x_{n_L}+t_{n_L}\}$$

- for the later blocks, includes the output of the previous block  $h^{l-1}$
- output:
  - matrix of self-attention-transformed vectors where item i is

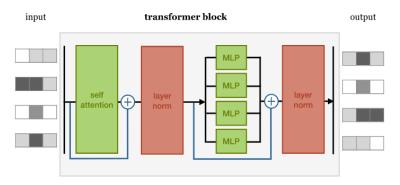
$$\sum_{i=1}^{n_L} a(h_i^{l-1}, h_j^{l-1}) h_j^{l-1}$$

# Transformer Block (Residualization and Normalization)



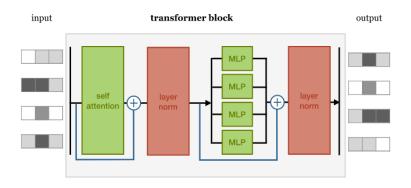
- self-attention layer's outputs are normalized
  - residual connections (blue line with  $\oplus$ ) means that the input  $h^{l-1}$  is added element-wise to the output of the attention layer
    - model can "bypass" layer if its not adding value.
    - helps deep models learn faster.

# Transformer Block (Residualization and Normalization)

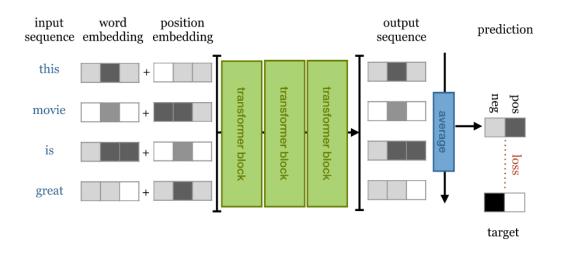


- self-attention layer's outputs are normalized
  - residual connections (blue line with  $\oplus$ ) means that the input  $h^{l-1}$  is added element-wise to the output of the attention layer
    - model can "bypass" layer if its not adding value.
    - helps deep models learn faster.
  - "layer normalization": normalize the input vector for each data point to unit variance across dimensions.
    - distinct from batch normalization, which normalizes a feature to unit variance across a batch sample of data points.

# Transformer Block (Dense MLP Layers)



- normalized self-attention outputs are piped to a multi-layer perceptron (MLP) with two hidden layers, with ReLU activation after the first layer.
- ▶ normalized again then output to  $h^{l+1}$ :
  - ightharpoonup either to the next transformer block, or to the output layer  $h^{n_y}$ .



will get state-of-the-art performance, and much faster to train than a bidirectional LSTM.

# Check for Understanding: True/False

- 1. A limitation of the Arora et al (2017) "tough-to-beat" sentence embeddings is that the vectors do not contain any information about word order.
- 2. Doc2Vec addresses the limits of the Arora et al (2017) embeddings by adding information on word order.
- 3. Unlike the other document embeddings, FastText embeddings (averaged hashed n-gram embeddings) do not have a geometric interpretation.