# Latent Representation of Topographic Classes in Remote Sensing Image Data using Autoencoders

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#### 5.1 Data

The available data are 1024x1024 images of the two United States cities Jacksonville in Florida and Omaha in Nebraska taken from the US3D Dataset that was partially published to provide research data for the problem of 3D reconstruction (Bosch et al. 2019). The images for each recorded area cover one square kilometer and can be divided into four categories with the first one being optical satellite images with three channels (RGB). Secondly visible and near infrared satellite images with eight channels (VNIR). Thirdly digital surface models (DSM). And lastly semantic labeling with five different categories.

The optical images were taken by the WorldView-3 satellite of Digital Globe from 2014 to 2016 and contain seasonal and daily differences in vegetation and sun positions. Each pixel of an image is described by three bytes representing the intensity of either red, green or blue.

Also collected by WorldView-3 were the VNIR images which contain eight channels for eight different bands of the spectrum with a ground sample distance of 1.3 meters. These images were taken over the course of all twelve months making them usable for training models that can handle seasonal appearance differences which are even more distinct than in the RGB data because certain wavelengths capture shadows and vegetation especially well. Overall this data offers more detail than the three channel RBG pictures. The eight channels of the imagery correspond to the following wavelengths:

• Coastal: 400 - 450 nm 1. Red: 630 - 690 nm

• Green: 510 - 580 nm 3. Near-IR1: 770 - 895 nm

• Yellow: 585 - 625 nm 4. Near-IR2: 860 - 1040 nm

The given DSMs were collected using light detection and ranging technology (Lidar). They have a single channel that describes the height of each pixel with a greater number representing a higher distance to the ground.

Lastly there are semantic labeled pictures with one channel of a single byte encodes one of five different topographic classes. Those classes are vegetation, water, ground, building and clutter. The semantic labeling was done automatically from lidar data but manually checked and corrected afterwards.

For all four categories of data the area covered in a single image is one square kilometer and they contain a lot of oblique view of buildings, often with sunshine casting good shadows making the data ideal for training models that should detect them.

### 5.2 Experiments

## 6 Architecture

## 6.1 Loss Function

#### Entropy

A part of the loss function used in the variational autoencoder is based on Kullback-Leibner divergence. To understand Kullback-Leibler divergence it seems necessary to explain entropy from the field of information theory. In short, entropy is a measure for the minimum average size an encoding for a piece of information can possibly have.

Suppose there is a system S1 that can have four different states a, b, c, d and every one of those states is equally likely to occur, that means the probability P(x) of each state x is 1/4. Now the goal is to losslessly transmit all information about that system with the minimum average amount of bits. That can be done with only two bits for example like this

$$a:00$$
  $b:01$   $c:10$   $d:11$ 

However, if P(a) = 1 and P(b) = P(c) = P(d) = 0, zero bits will suffice to encode the information since it is always certain that the system is in state a. So the entropy of the system clearly depends on the probabilities of each state. To see in which way, one can consider the system S2 with P(a) = 1/2, P(b) = 1/4, P(c) = 1/8 and P(d) = 1/8. In that case it would be best to encode the state with the highest probability with as few bits as possible since it has to be

transmitted the most often. That means a is encoded with one bit as 0. When decoding the information there must be no ambiguities so while the encoding for b has to start with a 1 it cannot be 1 since we need to encode two more states so b:10. Additionally if c:11 there would be no space left for d: say d:111 then if the transmitted information is 111111... it could either be decoded to ccc... or dd... So c should rather be encoded as 110 which way d:111 works. In the end a valid encoding that can transmit all information with the minimum average amount of bits is

$$a:0$$
  $b:10$   $c:110$   $d:111$ 

Here the states c,d are encoded with three bits instead of the two bits in the first example. But c and d are transmitted far less often than a which now only needs one bit. To be more precise half of all transmissions have one bit. Additionally a quarter of all transmissions have two bits. The sum of those probabilities multiplied with the respective amount of bits is the average amount of bits needed to transfer the information in a given encoding. So in the example, with f(x) as the number of bits that encode a state x, that turns out to be P(a)f(a) + P(b)f(b) + P(c)f(c) + P(d)f(d) = 1.75. That means for S2 on average you only need 1.75 bits to encode a state and since that is also the minimum 1.75 is the entropy of S2.

In general in an optimal encoding f(x) is the same as  $\log_2(\frac{1}{P(x)})$ . For S1 P(x) is 1/4 so the number of bits for x is  $\log_2(4) = 2$  what matches the two bits the first encoding uses for the states of S1.

The entropy of a system S with a set of discrete events X and the probability distribution P(x) for each  $x \in X$  is

$$\sum_{x \in X} P(x) \log_2(\frac{1}{P(x)}) = -\sum_{x \in X} P(x) \log_2(P(x))$$

Intuitively if a system has high entropy, the size of the encodings are high on average and many states have small probabilities. This means it is hard to predict what state the system will be in at a given time since there is no state that can be guessed with high confidence. If entropy is low, zero for example, one can be confident that the system is in a certain state like in the previous example with P(a) = 1.

#### Cross Entropy

- 7 Future Work
- 8 Conclusion

# References

Bosch, Marc et al. (2019). "Semantic Stereo for Incidental Satellite Images". In: 2019 IEEE Winter Conference on Applications of Computer Vision (WACV). IEEE, pp. 1524–1532.