



Common Practices

A. Maier, K. Breininger, L. Mill, N. Ravikumar, T. Würfl Pattern Recognition Lab, Friedrich-Alexander-Universität Erlangen-Nürnber May 16, 2018





Outline

Recap

Training Strategies

Optimization and Learning Rate

Architecture Selection and Hyperparameter Optimization

Ensembling

Class Imbalance

Evaluation





Recap





Training a Neural Network

- So far: all the nuts and bolts about how to train a network:
 - Fully connected and convolutional layers
 - · Activation function
 - Loss function
 - Optimization
 - Regularization
- Today: Common practices on how to choose an architecture, train and evaluate a deep neural network.



First Things First: Test Data



"Ideally, the test set should be kept in a "vault," and be brought out only at the end of the data analysis."

T. Hastie, R. Tibshirani, J. Friedman: The Elements of Statistical Learning



First Things First: Test Data (cont.)

- Overfitting is extremely easy with neural networks (see e.g. ImageNet with random labels [5]).
- True test set error/generalization error can be underestimated substantially when using the test set for model selection!
- Attention: Choosing the architecture is the first element in model selection
 → should never be done on the test set!
- Do initial experimentation on smaller subset of the dataset!





Training Strategies





Before Training: Gradient Checks

Own loss function, own layer implementation etc.: Check correct computation of gradient by comparing analytic and numerical gradient.

• Use centered differences for numeric gradient.





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- Use centered differences for numeric gradient.
- Use relative error instead of absolute differences.
- Numerics:
 - Use double precision for checking.
 - Temporarily scale loss function if you observe very small values (< 1e - 9).
 - Choose h appropriately.





Before Training: Gradient Checks (cont.)

Additional recommendations:

- Use only a few datapoints →less issues with non-differentiable parts of the loss function.
- Train the network for a short period of time before performing gradient checks.
- Check gradient first without, then with regularization terms.
- Turn of data augmentation and dropout.



Before Training: Check Initalization and Loss

- Goal: Check correct random initialization of layers.
- Compute the loss for each class on the untrained network, with regularization turned off.





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- Compute the loss for each class on the untrained **network**, with regularization turned off.
- Compare loss with loss achieved when deciding for a class randomly (chance).
- Repeat with multiple random initializations.





Before Training: Training!

- Goal: Check whether the architecture is **in general** capable to learn the task.
- Before training the network on the full training data set, take a small subset (5-20 samples) and try to overfit the network to get zero loss.
- Optionally: Turn off regularization that may hinder overfitting.



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- If the network cannot overfit:
 - Bug in the implementation.
 - Model too small →increase number of parameters.
 - Model not suitable for the task.



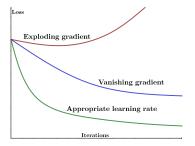
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 - Bug in the implementation.
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 - Model not suitable for the task.
- Also: Get a first idea about how the data, loss and network behave.



During Training: Monitor loss function

Recap:

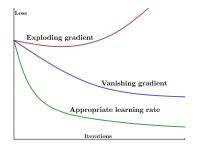


- Check learning rate (→more in a bit).
- Identify large jumps in the learning curve.



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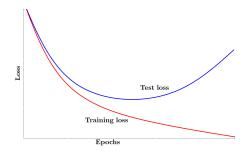
Recap:



- Check learning rate (→more in a bit).
- Identify large jumps in the learning curve.
- Very noisy curves →increase batch size.



During Training: Monitor Validation Loss

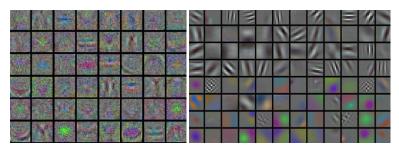


- Monitor amount of overfitting of the network.
- If training and validation loss diverge: overfitting → increase regularization/ early stopping
- If training and validation loss are close but high: underfitting → decrease regularization/ increase model size
- Save intermediate models if you want to use them for testing!



During Training: Monitor Weights and Activations

- Track relative magnitude of the weight update: Should be in a sensible range (approx. 1e-3).
- Convolutional layers: check filters of the first few layers. Should develop towards smooth and regular filters.
- Check for very large or saturated activations (→dying ReLUs)



Source: http://cs231n.github.io/neural-networks-3/





Optimization and Learning Rate





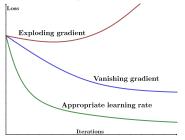
Choosing an Optimizer

- Batch gradient descent: Requires large memory, too slow, too few updates.
- Stochastic gradient descent (SGD): loss function and gradient become very noisy if only one/few samples are used.
- SGD with mini-batches: "best of both worlds"
 - Frequent, more stable updates.
 - Gradient noisy enough to escape local minima.
 - → Adapting mini-batch size yields smoother/more noisy gradient.
- Addition of momentum prevents oscillations and speeds up optimization.
- Effect of hyper-parameters relatively straight forward.
- Becommendation: Start with Mini-Batch SGD + momentum
- For faster convergence speed →ADAM.



Learning rate: Observing the loss curve

- Learning rate η has a large impact on the successful training of a network.
- For almost all gradient based optimizers, η has to be set.
- Effect of learning rate is often directly observable in the loss curve.



- → But this is a very simplified view!
- We want an adaptive learning rate: Progressively smaller steps to find the optimum
- → Annealing the learning rate.



Annealing the Learning Rate

- In deep learning context often known as learning rate decay.
- Decay means yet another hyper-parameter.
- Need avoid oscillation as well as a too fast cool down!
- · Decay strategies:
 - Stepwise decay: Every n epochs, reduce learning rate by a certain factor, e.g. 0.5, or by a constant value, e.g. 0.01.
 - Variant: Reduce learning rate when *validation error* stagnates.
 - Exponential decay: At epoch t: $\eta = \eta_0 e^{-kt}$ with k controlling the decay.
 - 1/*t*-decay: At epoch *t*: $\eta = \eta_0/(1 + kt)$.
- Stepwise decay most common: hyper-parameters are easy to interpret.
- Second-order methods are currently uncommon in practice, as they do not scale as well.





Architecture Selection and Hyperparameter Optimization





Reminder



Test data →vault!



Hyperparameter optimization

Neural networks have an enormous amount of hyperparameters.

- Architecture:
 - Number of layers & number of nodes per layer
 - Activation function
 - ...
- Optimization
 - Initialization
 - Loss function
 - Optimizer (SGD, Momentum, ADAM, ...)
 - Learning rate, decay & batch size
 - ...
- Regularization
 - Regularizer, e.g., L₂-, L₁-loss
 - · Batch Normalization?
 - Dropout?
 - ...
- . .



Choosing Architecture and Loss Function

- First step: Think about the problem and the data:
 - · How could the features look like?
 - What kind of spatial correlation do you expect?
 - What data augmentation makes sense?
 - How will the classes be distributed?
 - What is important regarding the target application?
- Start with simple architectures and loss functions.
- Do your research: Try well-known models first and foremost!
- If you change/adapt the architecture: Find reasons why the network should perform better.



- Learning rate, decay, regularization/dropout etc. can be tuned more easily.
- Still, networks can take days/weeks to train!



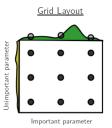
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- Options: Grid search or random search:



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- · Still, networks can take days/weeks to train!
- Search for hyperparameters using a log scale (e.g., $\eta \in \{0.1, 0.01, 0.001\}$).
- Options: Grid search or random search:
 - Use random search instead of grid search [2]:
 - → Easier to implement.
 - → Better exploration of parameters that have strong influence on the result.



Random Layout

Branch Strain S



Hyperparameter search: Coarse to fine search

- Hyperparameters highly interdependent.
- Optimize on a coarse to fine scale:
 - Training network only for a few epochs.
 - Bring all hyperparameters in sensible ranges.
 - Then refine using random/grid-search.





Ensembling





Concept

- So far we have always considered a single classifier. Can't we get better by using many?
- Assume N classifiers independently performing a correct prediction with probability 1 — p
- The probability to see *k* errors is:

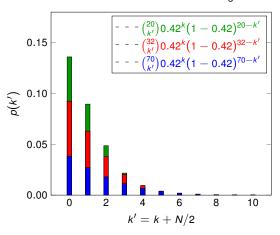
$$\binom{N}{k} p^k (1-p)^{N-k}$$
,

known as binomial distribution

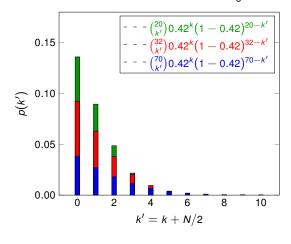
• So the probability of a majority $k > \frac{N}{2}$ to be wrong is:

$$\sum_{k>\frac{N}{2}}^{N} \binom{N}{k} p^{k} (1-p)^{N-k}$$



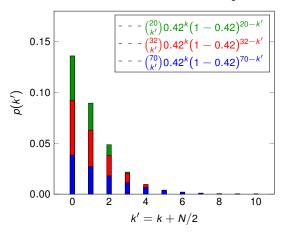






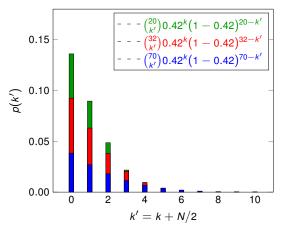
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 - Accuracy → 1!
- The big assumption here is independence



Ensembling

- Produce N independent classifiers/regressors
- Combine their predictions by majority/averaging



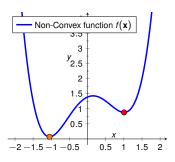
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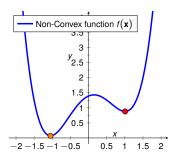
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Different models



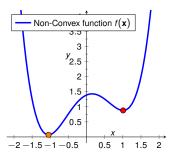






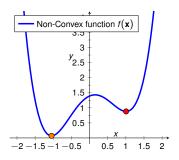
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- Combine models across optimization process
- Can be combined with a cylic learning rate



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- Different model checkpoints



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How to produce the components?

- Different models
- Different model checkpoints
- Moving average of w [6]
- Different methods
- → Easy performance boost if you need just a bit more

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Class Imbalance





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- Big challenge for machine learning algorithms.





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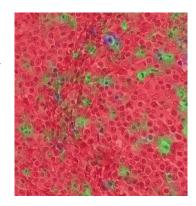
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 - → Misclassifying 1 out of 100 genuine transactions: 99% accuracy





Motivation (cont.)

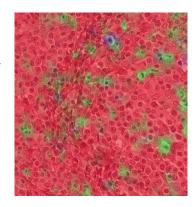
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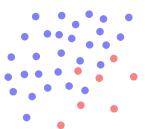
Motivation (cont.)

- Task: Detect mitotic cells for tumor diagnostics [1].
- Problem: Mitotic cells only make up a very small portion of cells in tissues.
- Data of a certain class is seen much less during training.
- Measures like accuracy, L₂ norm, cross-entropy do not show imbalance.



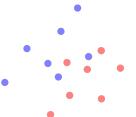


 Idea: Balance class frequencies by sampling classes differently.



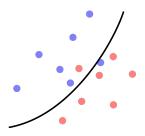


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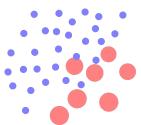
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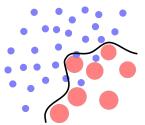
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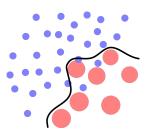
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- Disadvantage: Can lead to overfitting.
- Also possible: Combine Under- and Oversampling.





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- Data augmentation can help to reduce overfitting for underrepresented class.



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- Instead of class frequency, weights can be adapted with regards to other considerations.





Evaluation





Performance evaluation

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- Evaluate generalization performance on previously unseen data: the test set.
- → We can now open the vault!



Source: de.disney.wikia.com/wiki/Dagobert_Duck



Of All Things the Measure is Man [8]

- Protagoras of Abdera (c.490 c.420 BCE)
- Data is annotated and labeled by humans.
- During training, all labels are assumed to be correct f "to err is human"
- Additionally: Ambiguous data.



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May 16, 2018

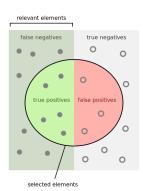


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- Multiple human voters: Take mean (if possible) or majority vote.
- Steidl et al. 2005: Entropy-based measure that takes "confusions" of human reference labelers into account.
 - Humans confuse certain classes with each other more (Angry vs. Happy/Angry vs. Annoyed)
 - Mistakes by the classifier are less severe if the same classes are confused by humans.

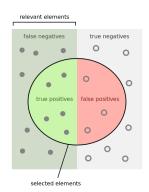


 Classification problem →classification measures:



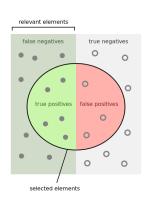


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 - True/False Positives: TP/FP
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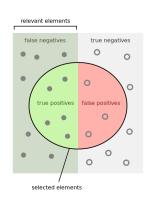


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- Precision/pos. predictive value: precision = $\frac{TP}{TP+FP}$
- Recall/true positive value: $recall = \frac{TP}{TP+FN}$
- Specificity/true negative value: specificity = TN TNI
 LEP
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- F1-score: F1 = $2 \cdot \frac{\text{TPV-TNV}}{\text{TPV+TNV}}$
- Receiver operating characteristic (ROC) curve.





Performance measures: Multiclass classification

- Adapted versions of measures mentioned above.
- Top-K error: True class label is not in the K classes with the highest prediction score.
- Common: Top-1 and Top-5 error.
- Example: ImageNet performance usually measured with Top-5 error.



- k-fold cross validation:
 - Split data in *k* folds
 - Use k − 1 folds as training data, test on fold k
 - Repeat k times.
- Rather uncommon in deep learning due to long training times.
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- Attention: almost always additional bias (architecture selection. hyperparameters).
- Even without cross-validation: Training is a highly stochastic process.
- → Retrain network multiple times and report average performance and standard deviation.



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- Run training for each method/network multiple times.
- → Determine whether performance is significantly different e.g. Student's t-test!
 - Compares two normally distributed data sets with equal variance.
 - Determines whether the means are significantly different with respect to a significance level α (e.g. 0.05 or 0.01).



Comparing Classifiers: Multiple testing

- Interpretation: The probability that this difference is caused by **chance** equals α .
- If we compare multiple classifiers, this chance can rise significantly due to multiple comparisons!



Comparing Classifiers: Multiple testing

- Interpretation: The probability that this difference is caused by **chance** equals α .
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- Correct for multiple tests using Bonferroni correction:
 - For *n* tests with significance level α , the total risk is $\alpha' = n \cdot \alpha$.
 - \rightarrow To reach a total significance level of α' , choose $\alpha' = \alpha/n$.



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 - For *n* tests with significance level α , the total risk is $\alpha' = n \cdot \alpha$.
 - ightarrow To reach a total significance level of lpha', choose lpha'=lpha/n.
- Assumes independence between tests: Pessimistic estimation of significance.
- More accurate, but incredibly time-consuming: Permutation tests [3].



Summary

- Check your implementation before training: Gradient, initialization, ...
- Monitor training process continuously: training/validation loss, weights, activations.
- Stick to established architectures before reinventing the wheel.
- Experiment with few data sets, keep your evaluation data safe until evaluation.
- Decay the learning rate over time.
- Do random search (not grid search) for hyperparameters.
- Perform model ensembling for better performance.
- Check for significance when comparing classifiers.

NEXT TIME

ON DEEP LEARNING



Coming Up

Evolution of neural network architectures:

- From deep networks to deeper networks.
- From "sparse" to dense connections.
- LeNet, GoogLeNet, ResNet, ...



Further Reading

- Link SGD Tricks by Leon Bottou.
- · Link: Interesting loss functions.
- Link: Practical recommendations by Yoshua Bengio (from 2012).





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