

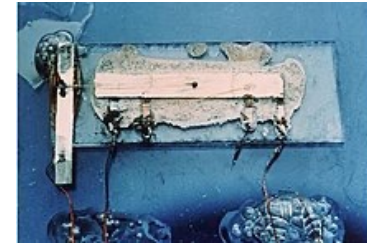
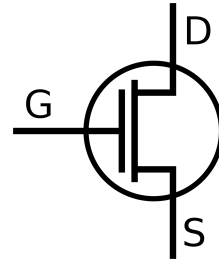
# Enabling Deeper Quantum Compiler Optimizations at High Level

Gushu Li  
11/10/2022



# The Quantum Revolution

1<sup>st</sup> Quantum  
Revolution



Classical  
Computer

1900

Quantum  
Mechanics

1947

Transistor

1956

MOSFET

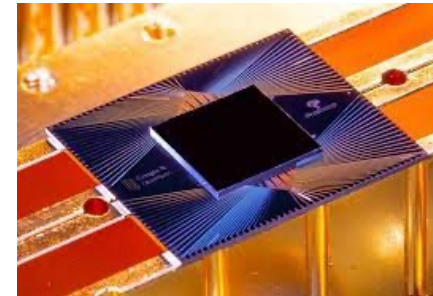
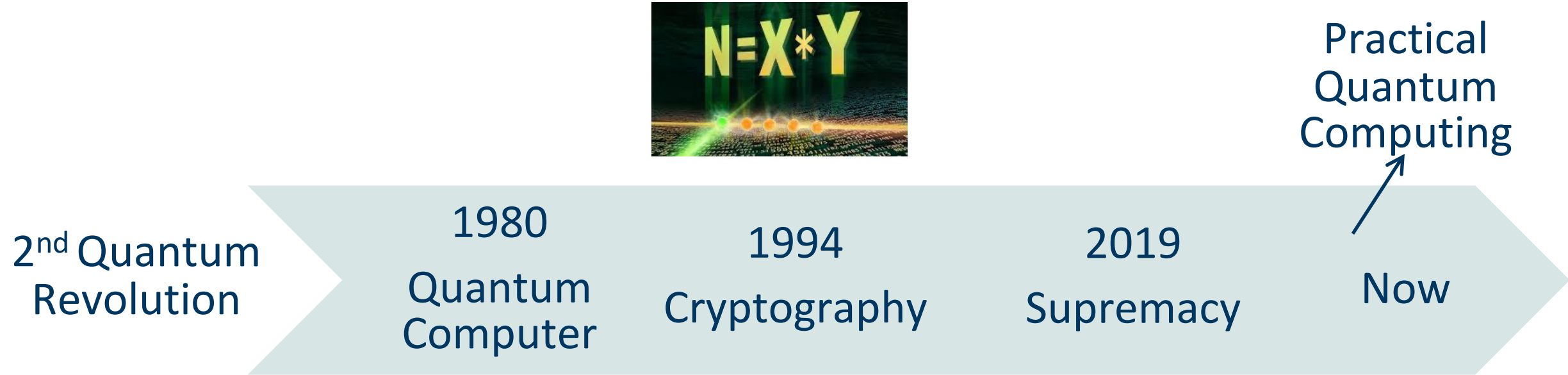
1958

Integrated  
Circuit

1980

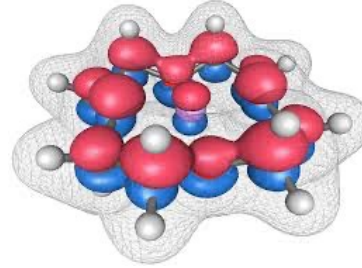
2<sup>nd</sup> Quantum Revolution: the power of  
quantum is not fully exploited

# The Quantum Revolution

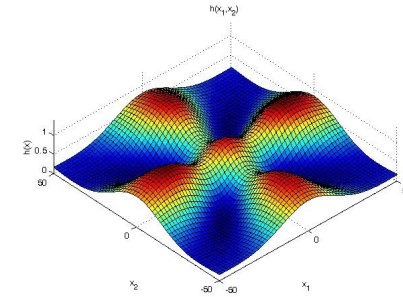


# Quantum Applications

Application



Simulation



Optimization



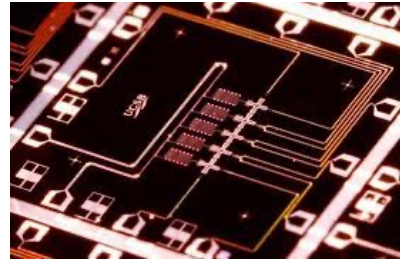
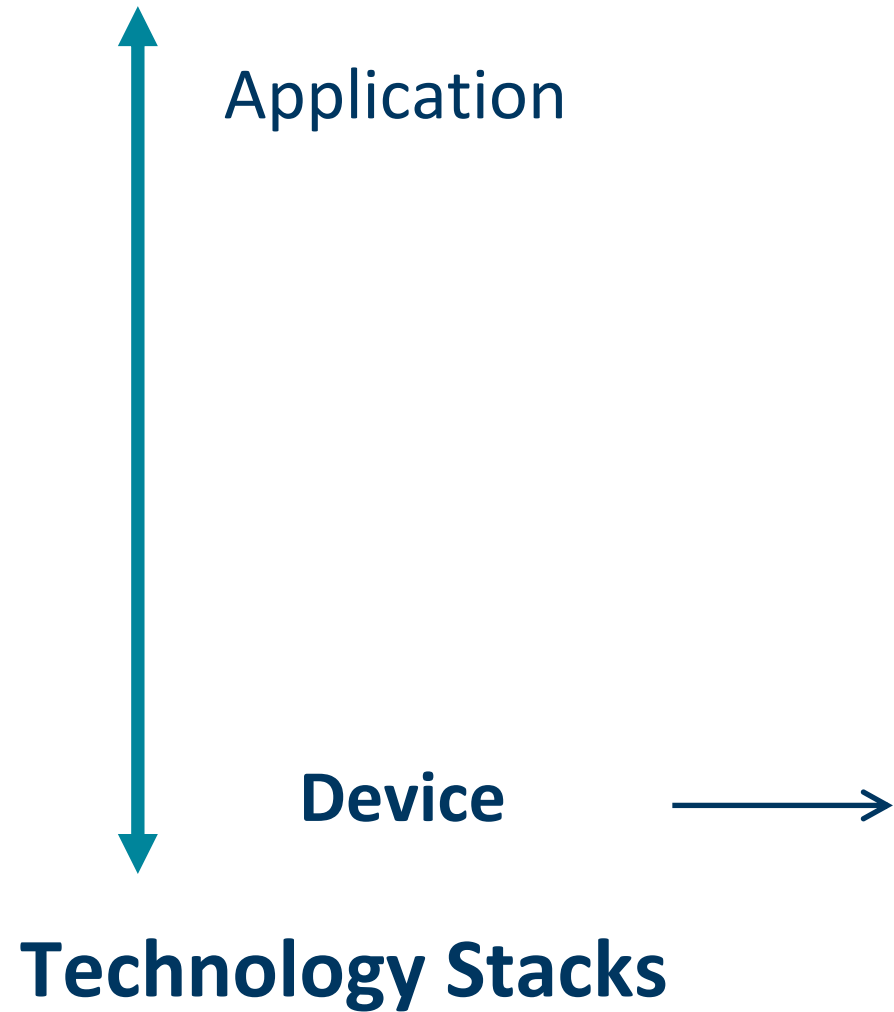
Machine Learning



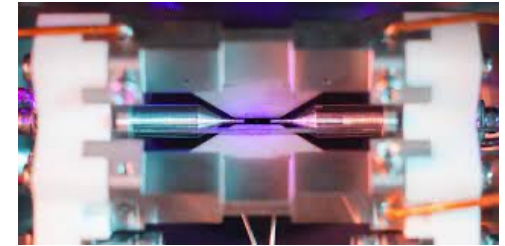
Cryptography

Technology Stacks

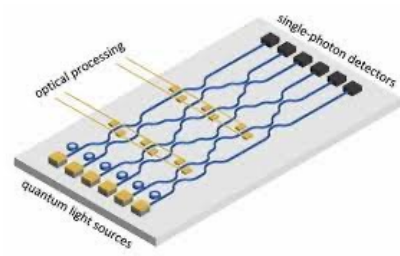
# Quantum Devices



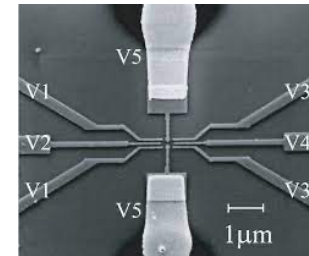
Superconducting



Ion Trap

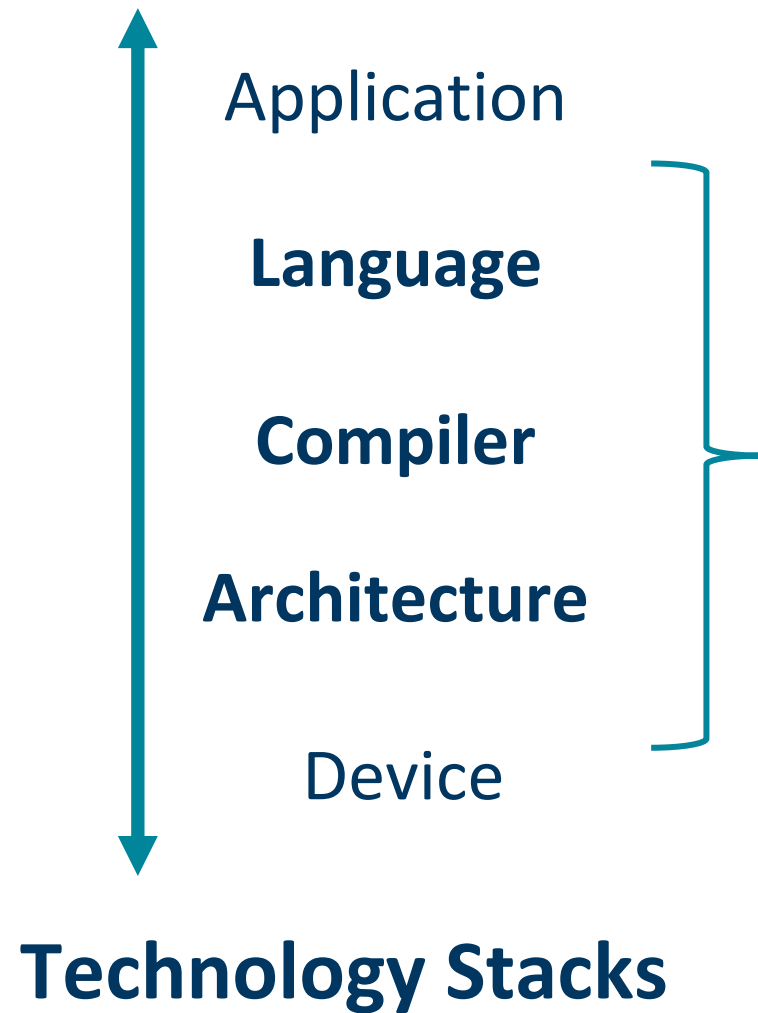


Photonics

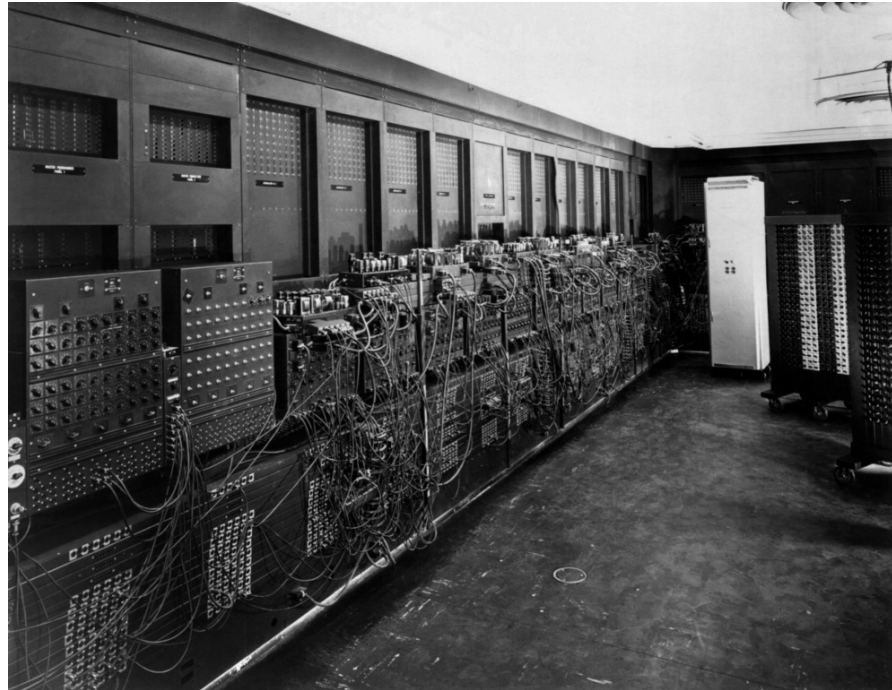


Quantum Dot

# Quantum Computer System

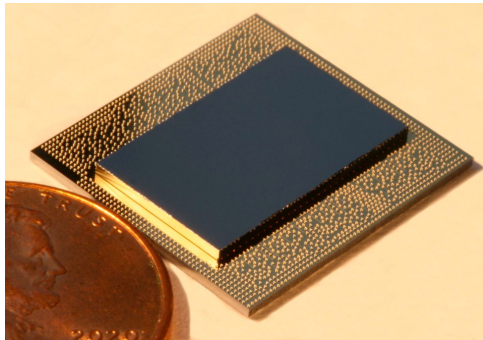


ENIAC, the first electronic general purpose digital computer, 1945

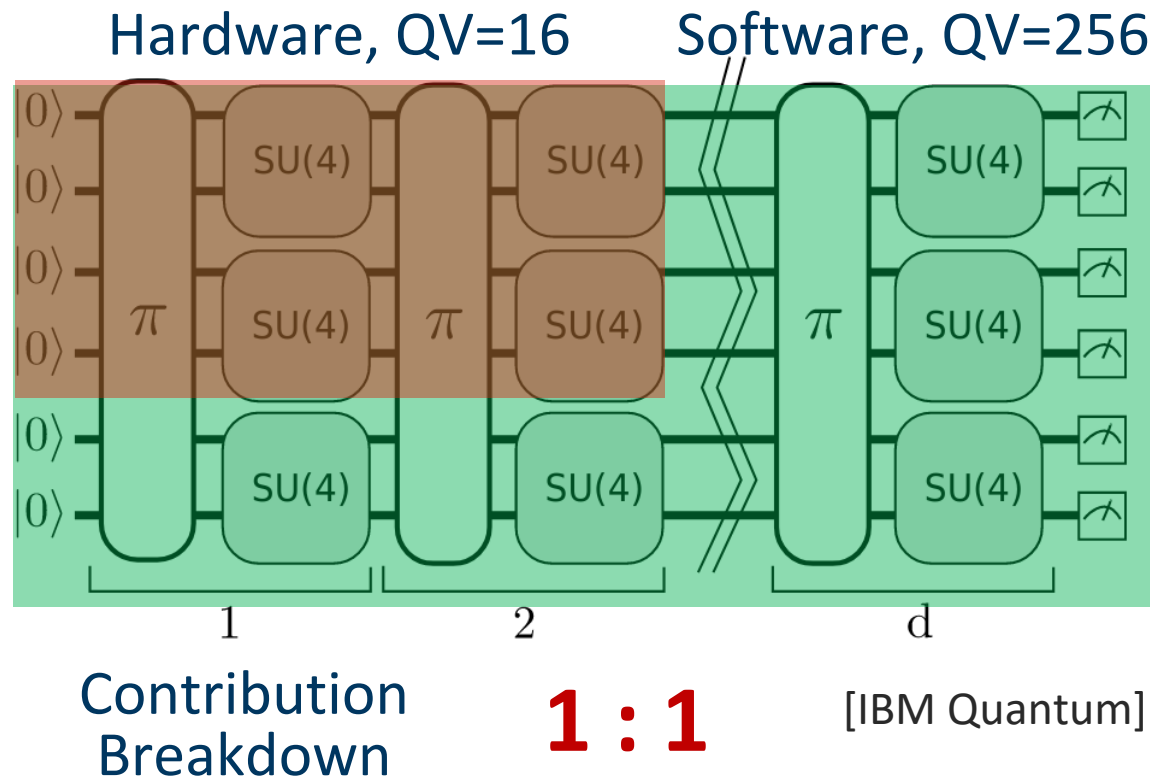


# Hardware vs Software

- IBM benchmarking results



IBM Q Montreal

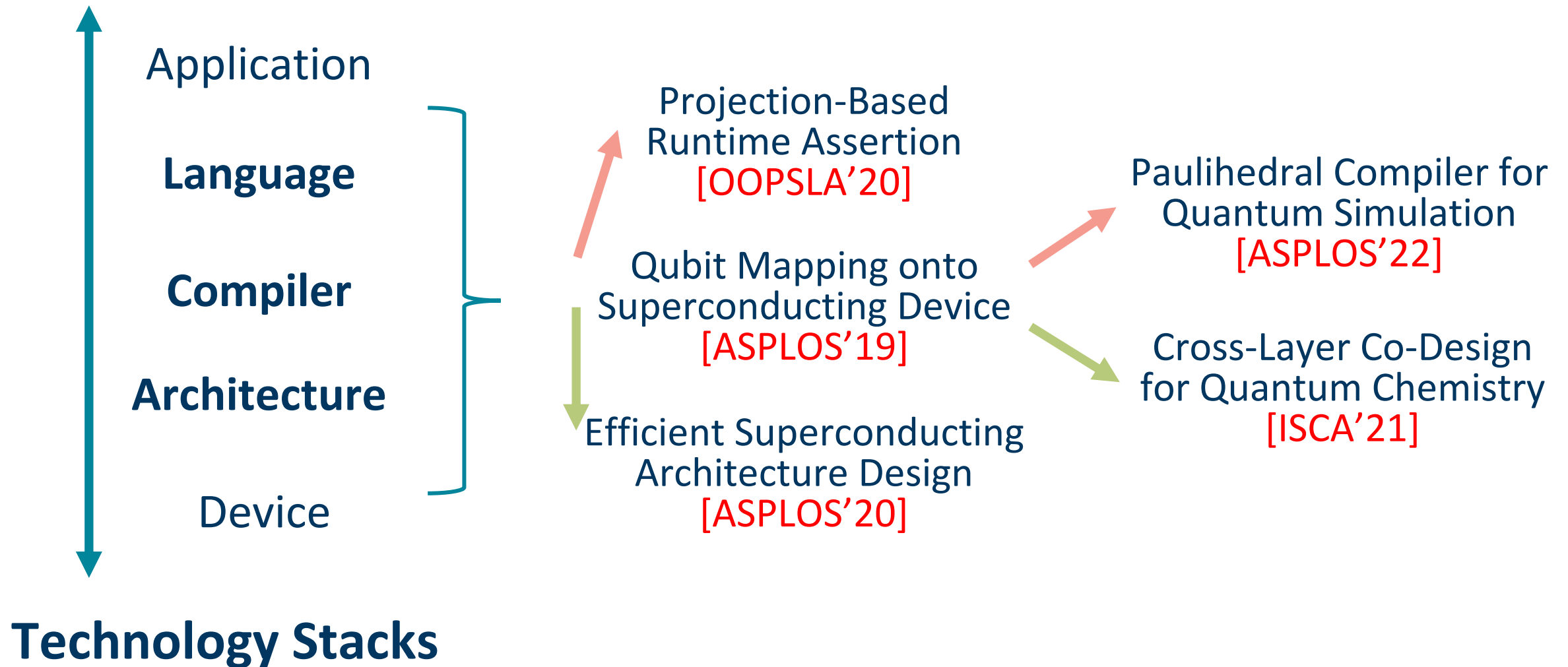


Quantum system research extends the computation capability!

And both software and hardware are important

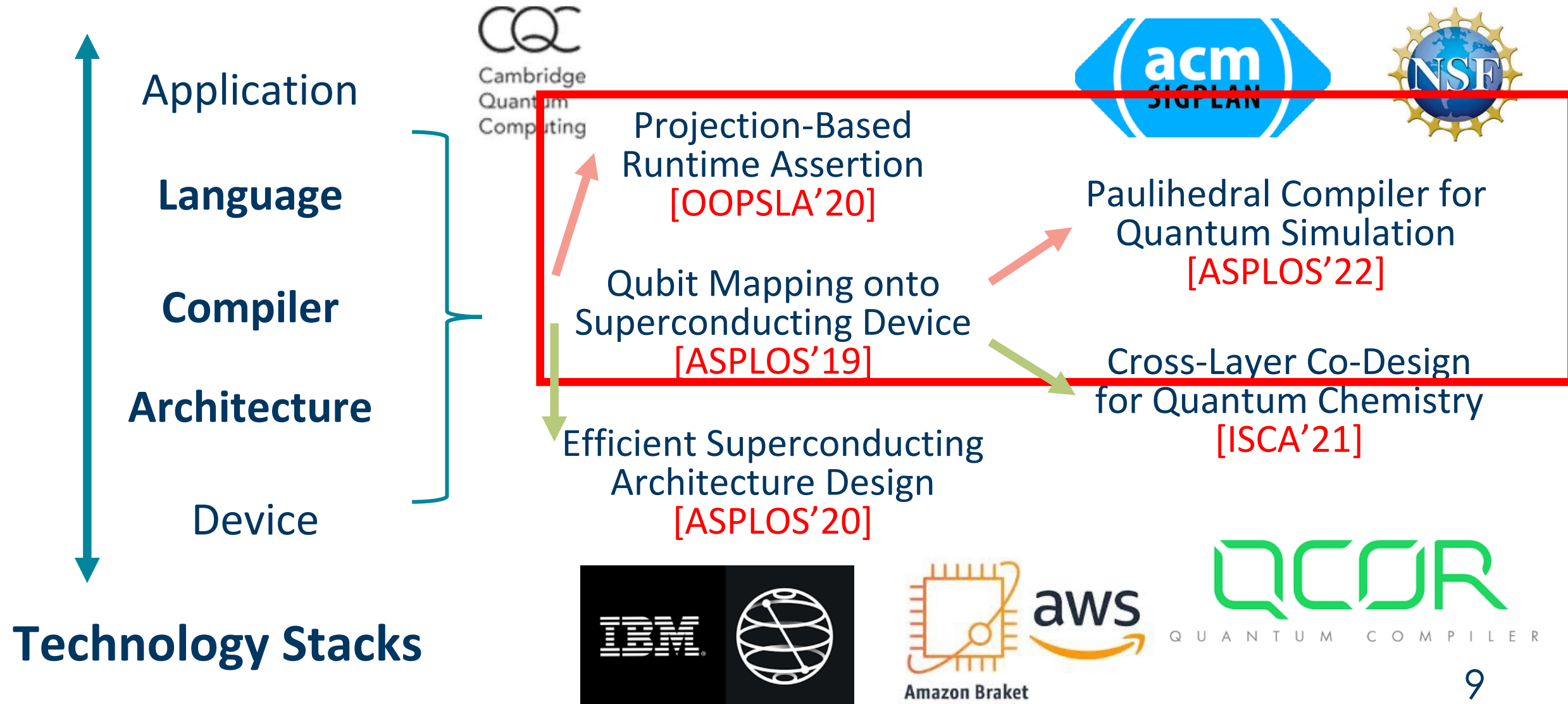
Quantum Volume (QV): the size of Hilbert space that a quantum processor can explore reliably

# My Research Overview



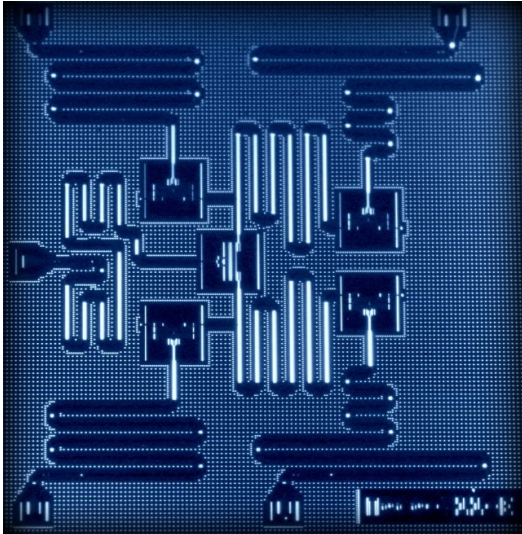


# Industry Adoptions & Awards

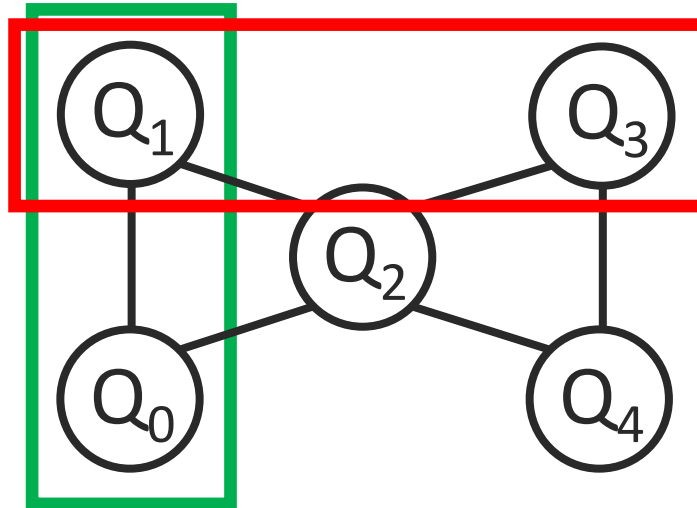


# Background

- Limitation of the superconducting architecture



IBM's 5-qubit  
superconducting  
quantum chip



Coupling graph – limited  
qubit connection

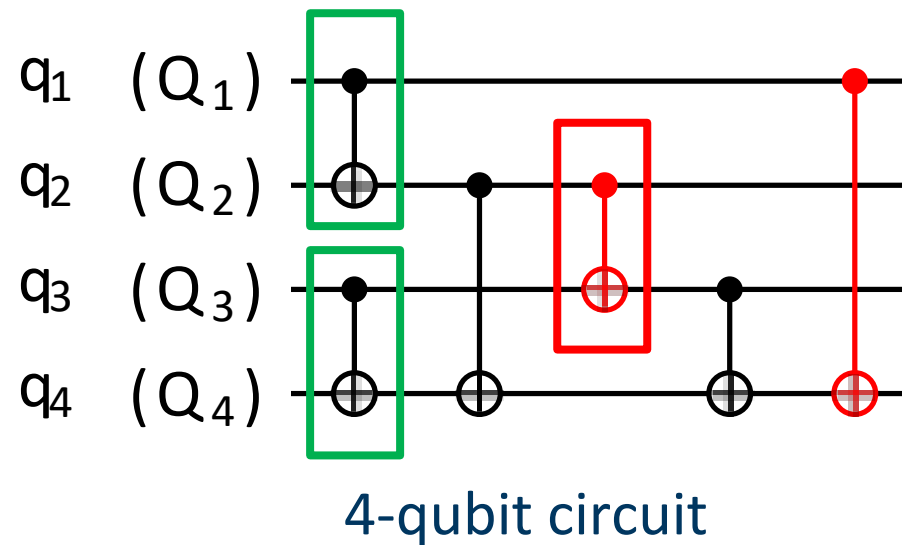
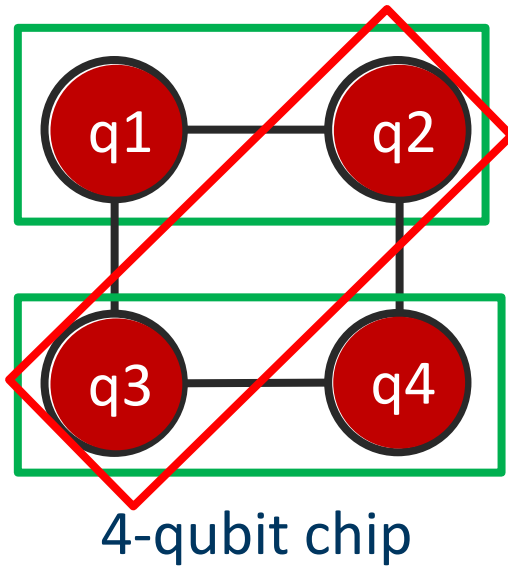
CNOT gates only  
allowed on the  
connected edges

CNOT Q0, Q1 😊

CNOT Q1, Q3 😞

# Qubit Mapping

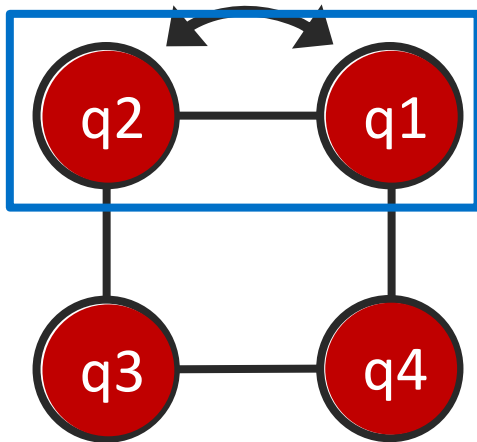
- An example



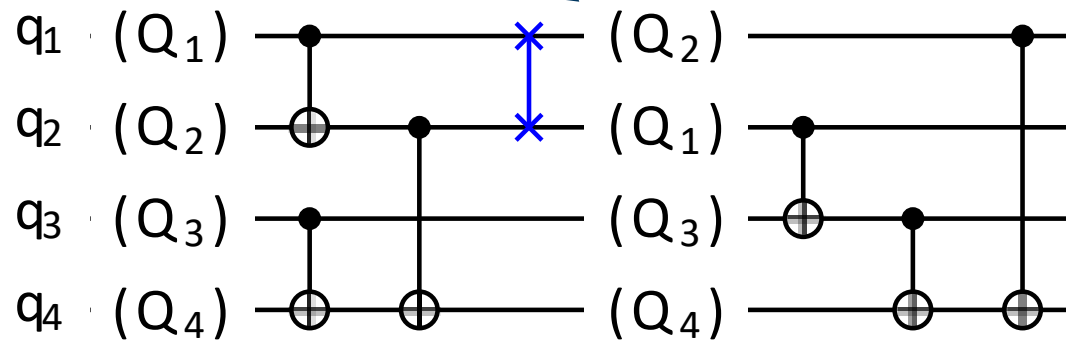
Some CNOTs  
are executable

# Qubit Mapping

- An example

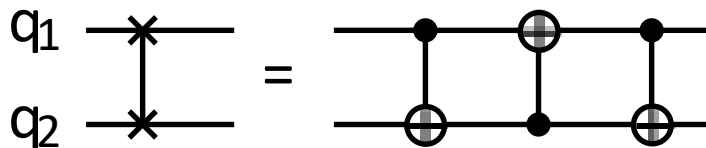


4-qubit chip



4-qubit circuit

Insert additional gate SWAP:  
exchange the mapping

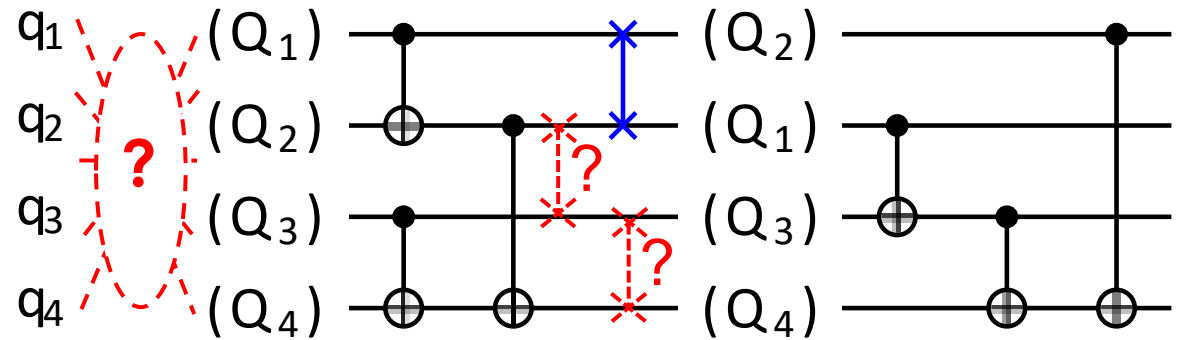


1 SWAP = 3 CNOT

Each additional SWAP leads to more noise

# Qubit Mapping

- Output:  
Initial mapping & SWAPs for remapping
- Constraint:  
Satisfy all two-qubit gate dependencies
- Optimization objectives:  
Compilation quality: Gate count, Circuit depth  
Compilation time



Quantum 'register allocation'  
but with different constraints



# Qubit Mapping

- Output:  
Initial mapping & SWAPs for remapping
- Constraint:  
Satisfy all two-qubit gate dependencies
- Optimization objectives:  
Compilation quality: Gate count, Circuit depth  
Compilation time

Qubit Mapping onto  
Superconducting Device  
[ASPLOS'19]

- **The default mapping method in Qiskit**



QCOR  
QUANTUM COMPILER

hardware-independent  
quantum program

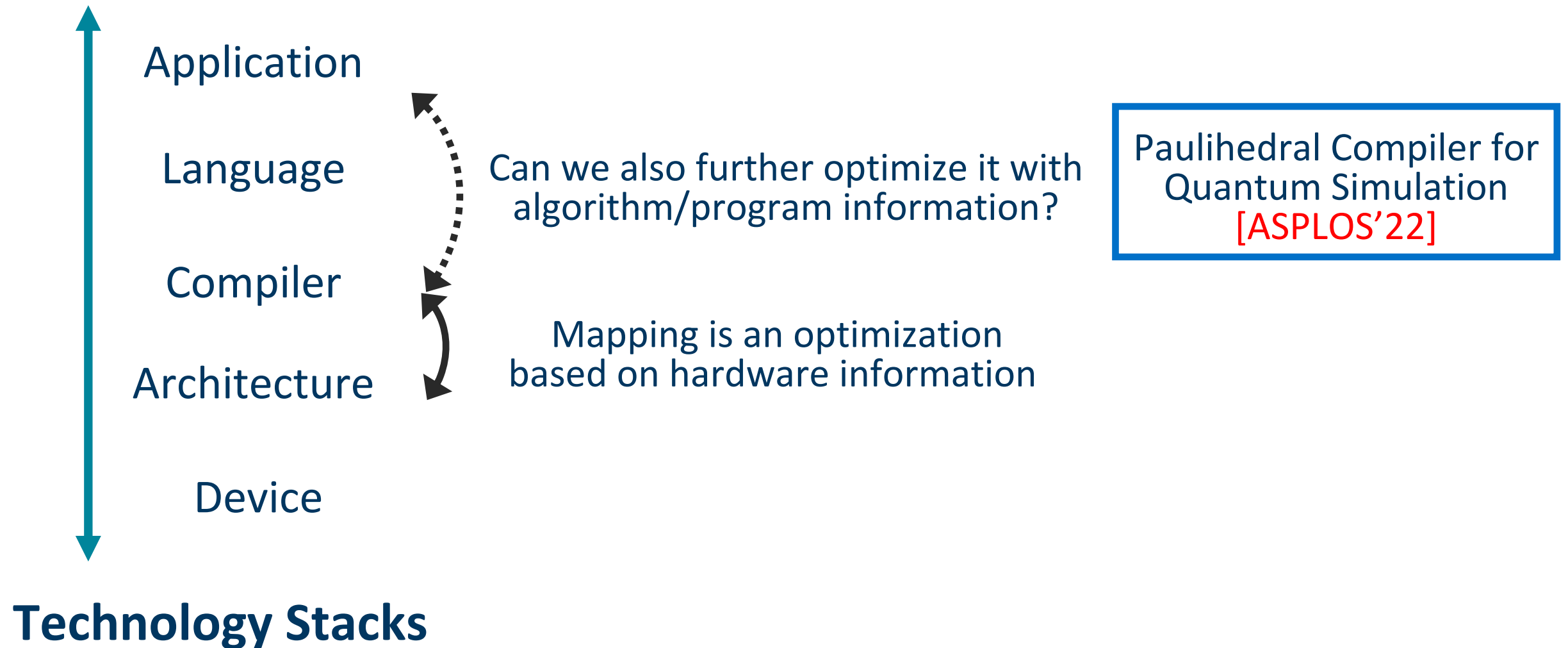


Quantum  
Compiler  
Optimization



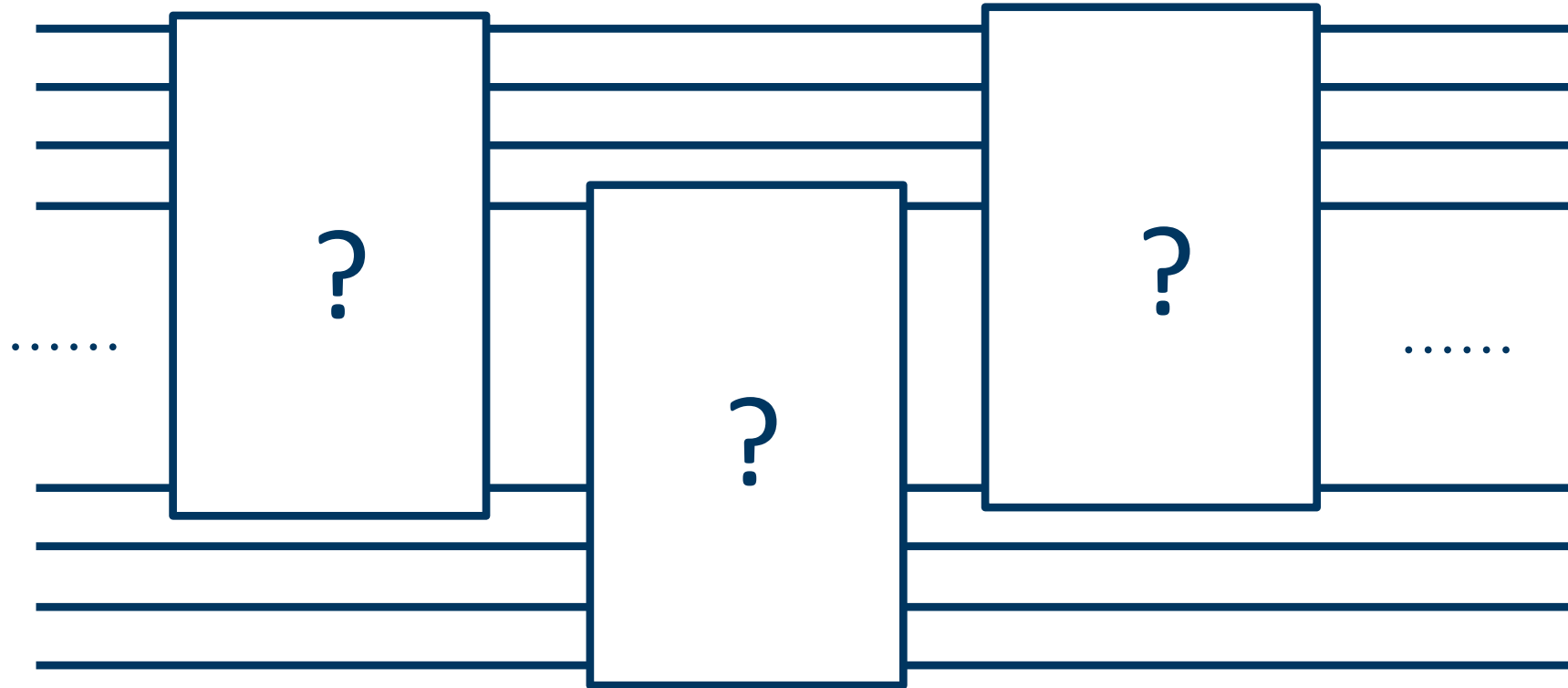
hardware-compatible  
quantum program

# Going Further



# Challenge

- How to extract algorithmic information from the program





# Challenge

- Gate matrix size grows exponentially



2x2 matrices



4x4 matrices



8x8 matrices

**n-qubit gate**

**$2^n \times 2^n$  matrices**

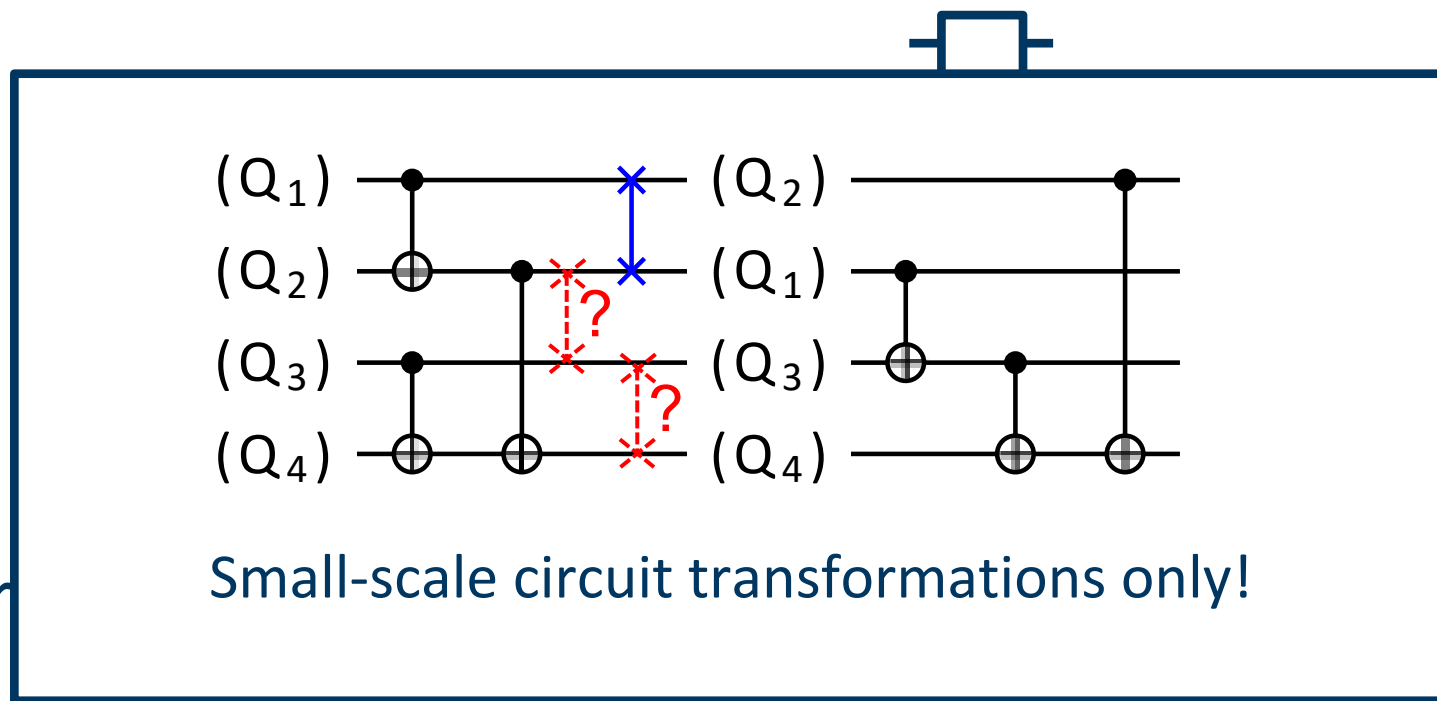
- Hard to reason about, analyze, synthesize, decompose

# Challenge

- Gate matrix size grows exponentially



- Hard to r



trices

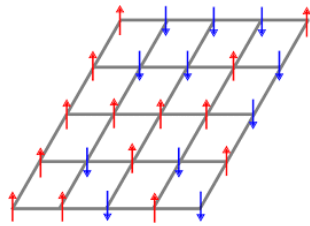
$2^n$  matrices

pose

# Opportunities at High-Level

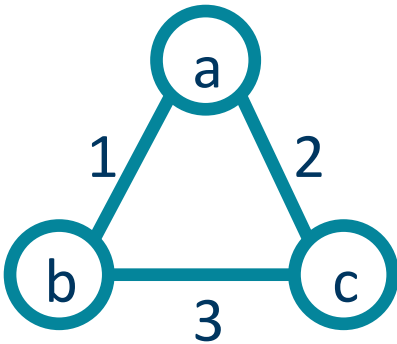
- More abstract compact form? Yes
- Simulation is widely used in quantum algorithm design

Simulation



$$H = -\sum J_{ij} Z_i Z_j - \mu \sum h_j Z_j$$

Graph Cut



$$H = \frac{1}{2} (Z_a Z_b - I) + \frac{2}{2} (Z_a Z_c - I) + \frac{3}{2} (Z_b Z_c - I)$$

And many more

# Quantum Simulation Kernel

- A widely-used subroutine

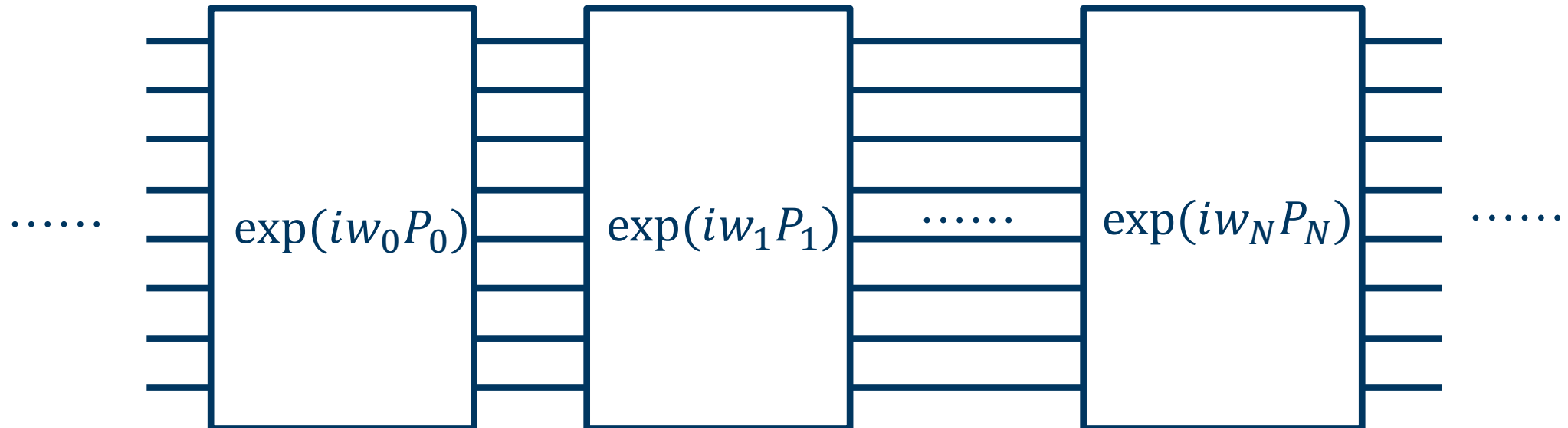
$$\exp(iHt)$$

$$H = \sum_i w_i P_i, P_i \text{ is a Pauli string, } w_i \in \mathbb{R} \text{ is weight}$$

$$P = \sigma_{n-1} \sigma_{n-2} \dots \sigma_0$$

$$\sigma_i = X | Y | Z | I$$

$$P = Y_4 Z_3 I_2 X_1 Z_0$$



# Tree Structure

- The program pattern

$$\exp(iwZ_3Z_2Z_1Z_0)$$

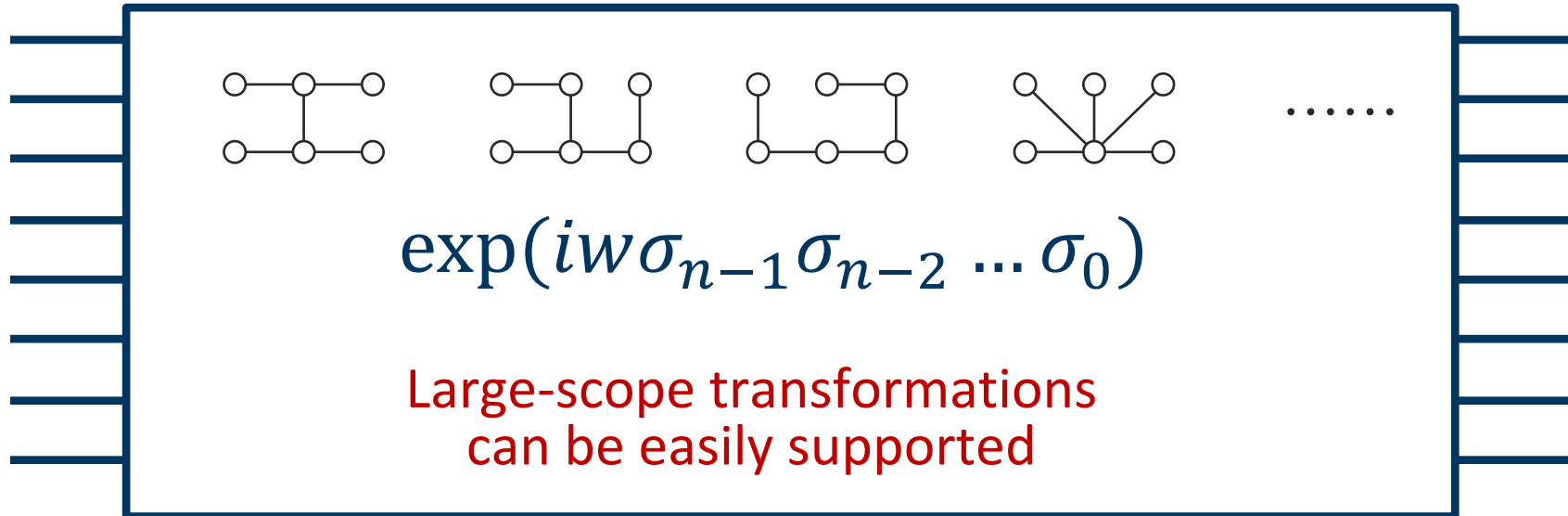
q0  
q1

q2

q3

q0

All these  
equivalents  
have a t

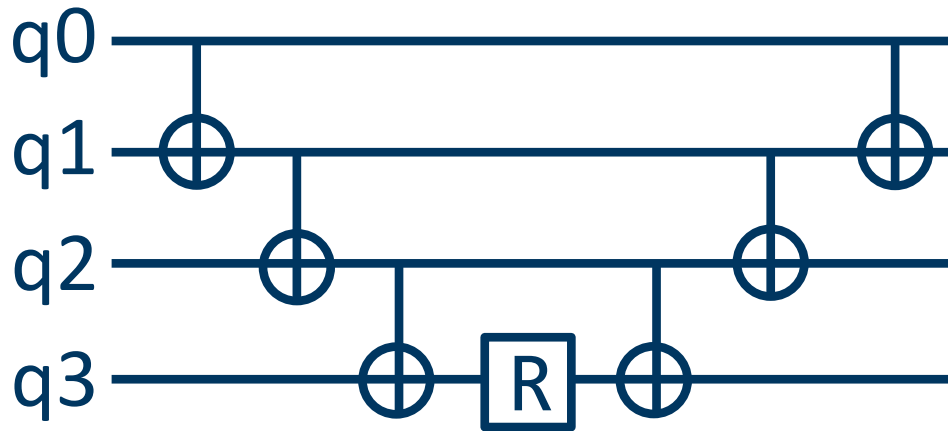


q0  
q1  
q3  
q2



# Conventional Compilation

- Find SWAP in gate sequence  $\exp(iwZ_3Z_2Z_1Z_0)$



CNOT q0, q1

CNOT q1, q2

CNOT q2, q3



SWAP q1, ...

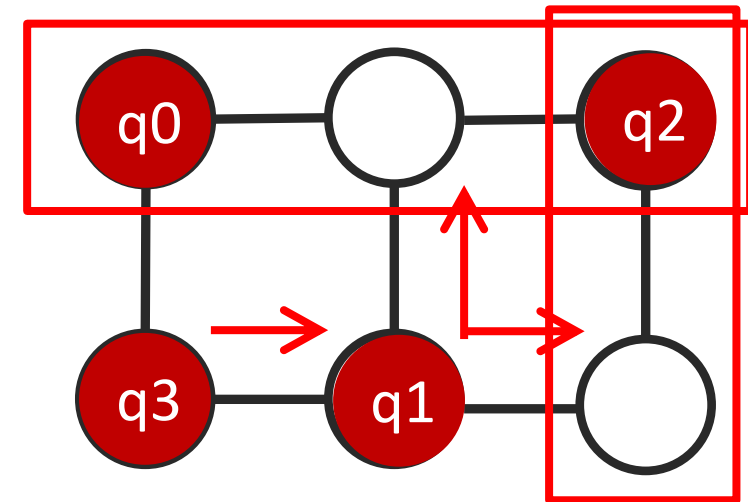
CNOT q0, q1

CNOT q1, q2

SWAP q3, ...

SWAP q3, ...

CNOT q2, q3



# Paulihedral Compilation

- Leverage high-level information

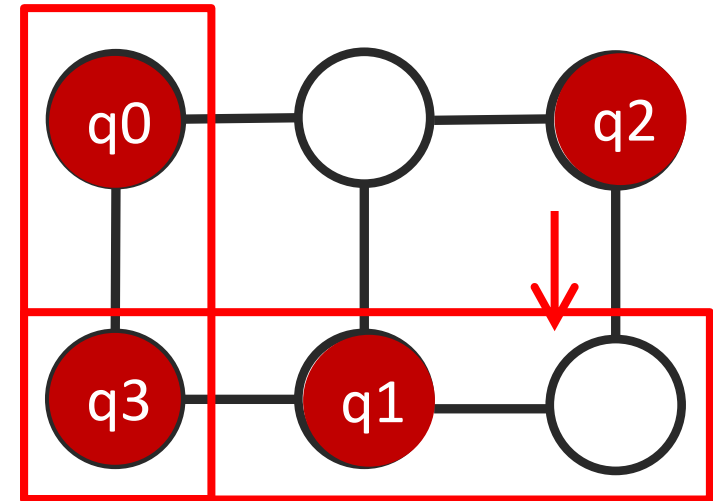
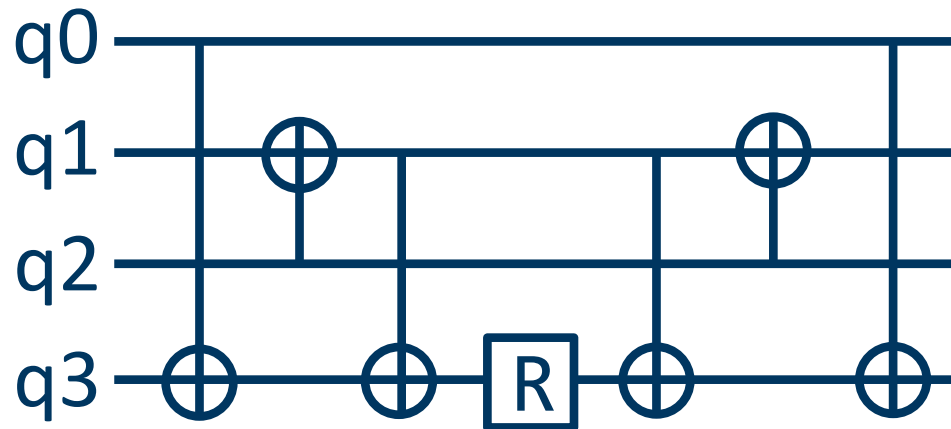
$\exp(iwZ_3Z_2Z_1Z_0) \longrightarrow$

SWAP q2, ...

CNOT q0, q3

CNOT q2, q1

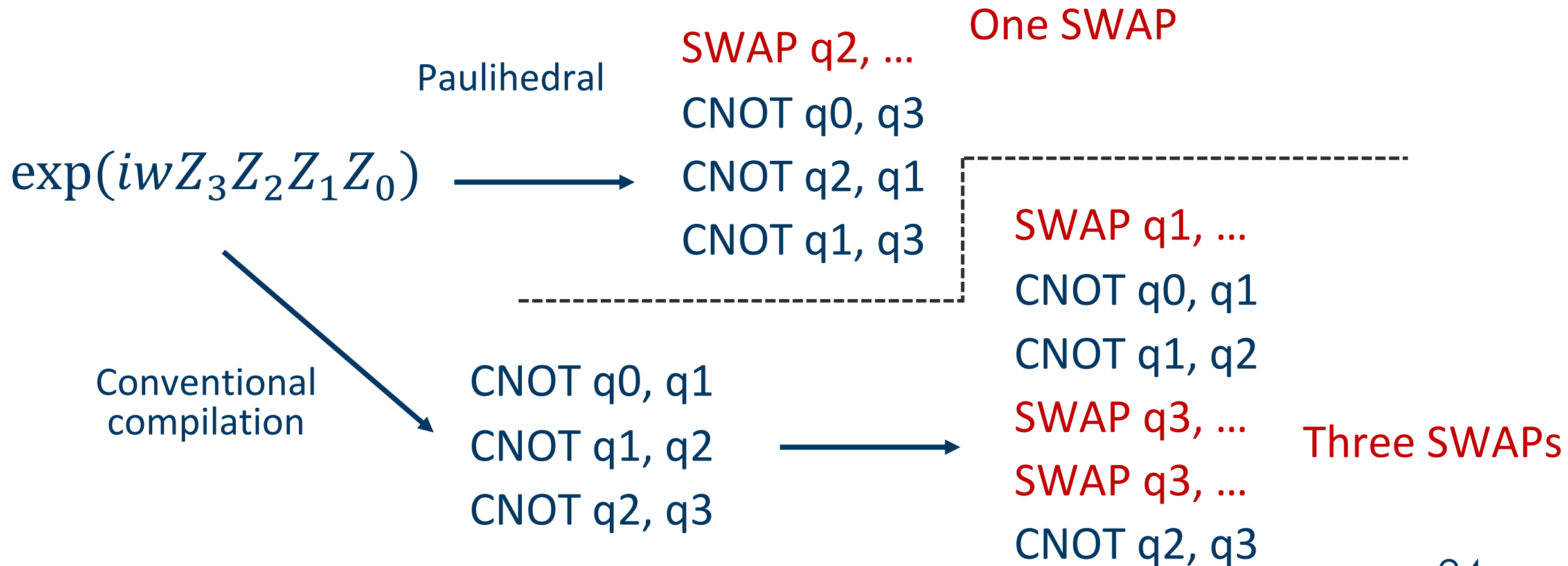
CNOT q1, q3



Find a tree embedding, then  
generate the CNOT tree

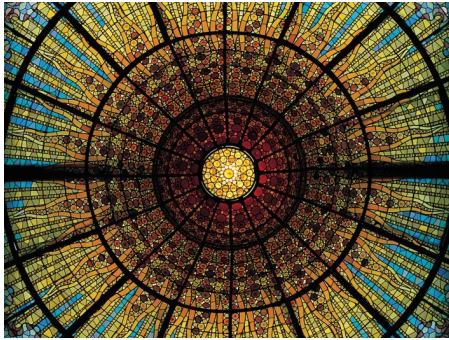
# Comparison

- Significant SWAP overhead reduction



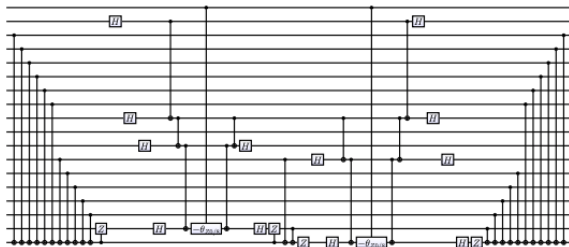


# Moreover



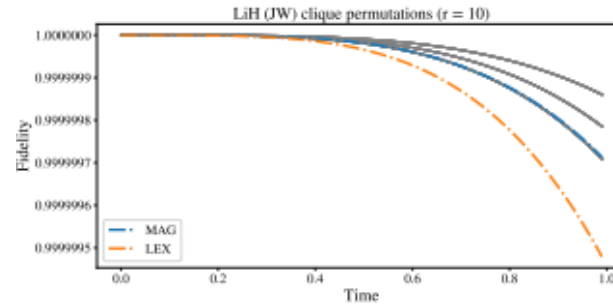
[Livio, 2012]

symmetry preserving



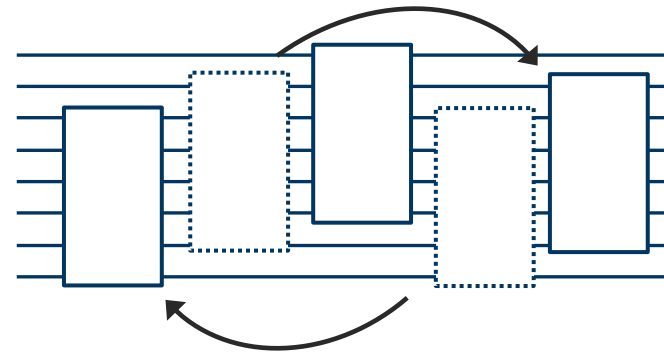
[Hastings et al. 2015]

more gate cancellation



[Gui et al. 2019]

error mitigation

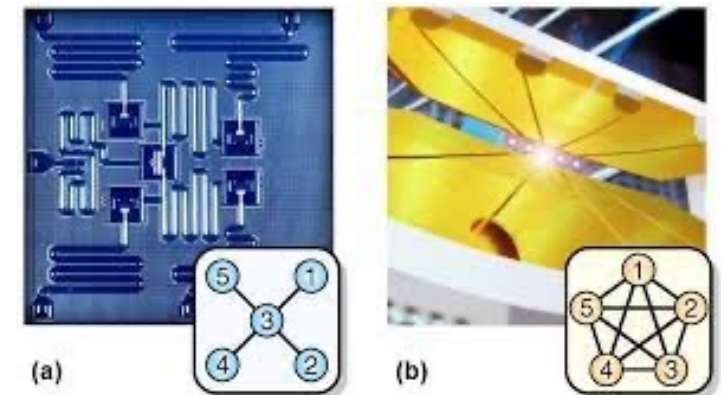


large-scale scheduling

$$\begin{aligned}(a_2^\dagger a_0 - a_0^\dagger a_2) &= \frac{i}{2}(X_2 Z_1 Y_0 - Y_2 Z_1 X_0) \\ (a_3^\dagger a_1 - a_1^\dagger a_3) &= \frac{i}{2}(X_3 Z_2 Y_1 - Y_3 Z_2 X_1) \\ (a_3^\dagger a_2^\dagger a_1 a_0 - a_0^\dagger a_1^\dagger a_2 a_3) &= \\ &\frac{i}{8}(X_3 Y_2 X_1 X_0 + Y_3 X_2 X_1 X_0 + Y_3 Y_2 Y_1 X_0 + Y_3 Y_2 X_1 Y_0 \\ &\quad - X_3 X_2 Y_1 X_0 - X_3 X_2 X_1 Y_0 - Y_3 X_2 Y_1 Y_0 - X_3 Y_2 Y_1 Y_0).\end{aligned}$$

[McArdle et al. 2020]

parameter sharing



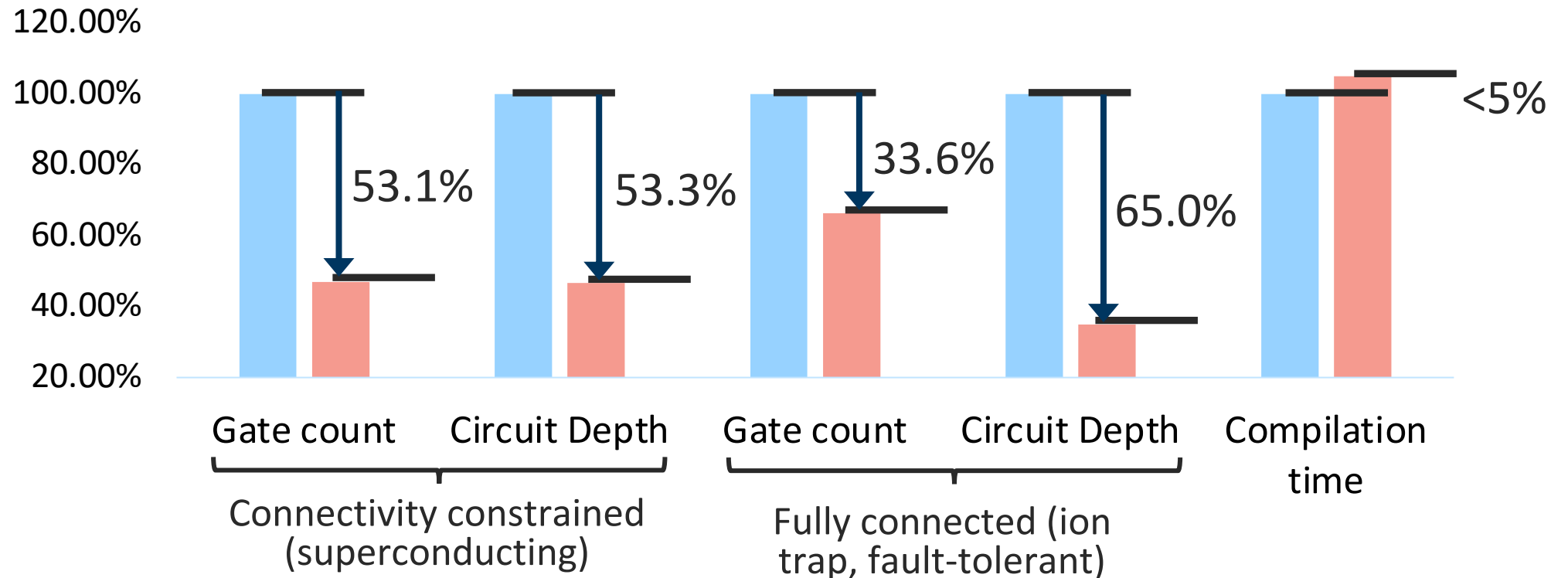
[Linke et al. 2017]

different backends

Please see paper for details

# Evaluation

- Benchmarks: molecule/Ising/Heisenberg/random Hamiltonian, UCCSD/QAOA graph ansatz

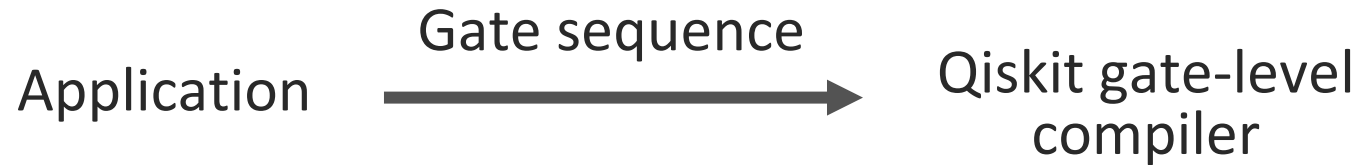


gate count -> number of instructions  
circuit depth -> length of critical path (time)

■  $t|ket\rangle$  ■ Paulihedral

# Changes in Qiskit Infrastructure

Before:



After:



More high-level optimizations are incoming!

# High-Level Optimization in QEC

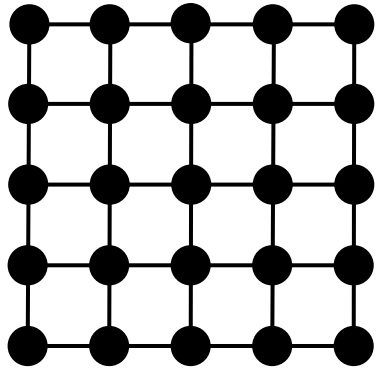
- Quantum hardware, e.g., superconducting quantum devices, is noisy.

IBM Washington. CNOT error:  $\sim 1\%$ ; 70 CNOT, fidelity  $< 50\%$ .

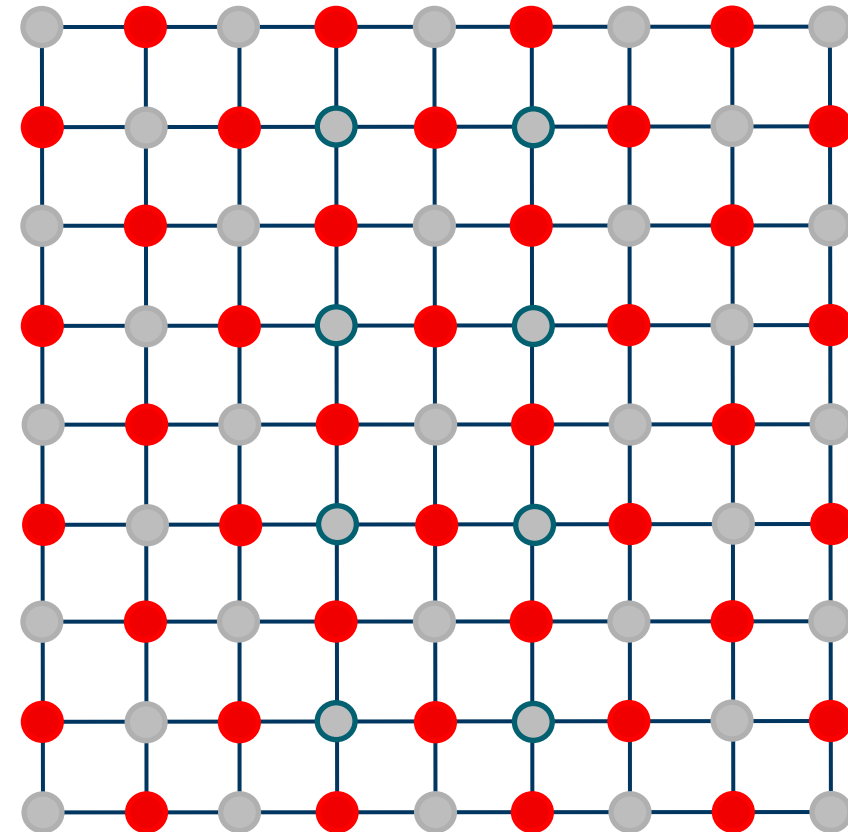
- Quantum error correction (QEC) is important for future, fault-tolerant quantum computing.
- Surface code is among the best QEC codes, with great error correction capability and mild resource requirement.

# How Does Surface Code Work?

- It composes physical qubits in 2-D lattice with high error into a logic qubit with less error.

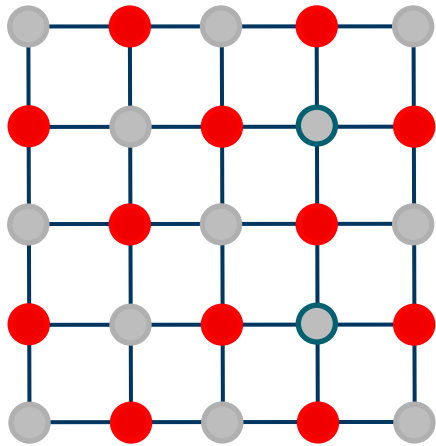


**Coupling graph** for  
Physical Qubits in  
2-D lattice Space

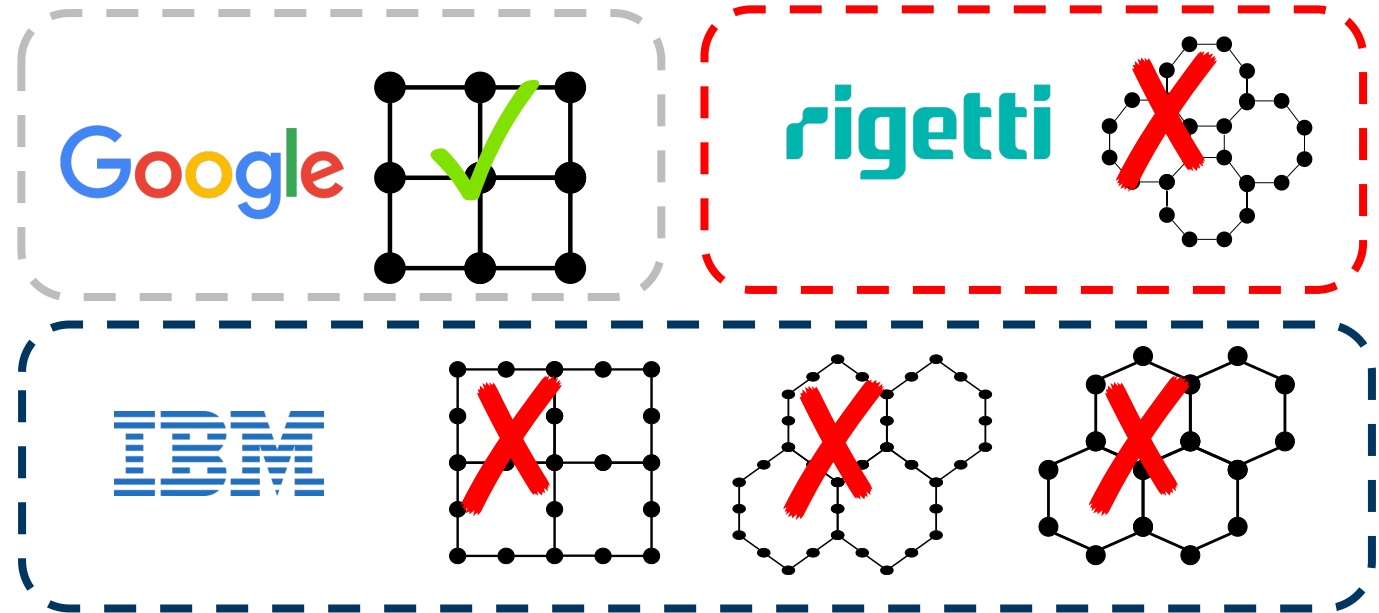


• Freedom:  $13 - 12 = 1$

# Mismatch between Surface Code and Sparse Architectures



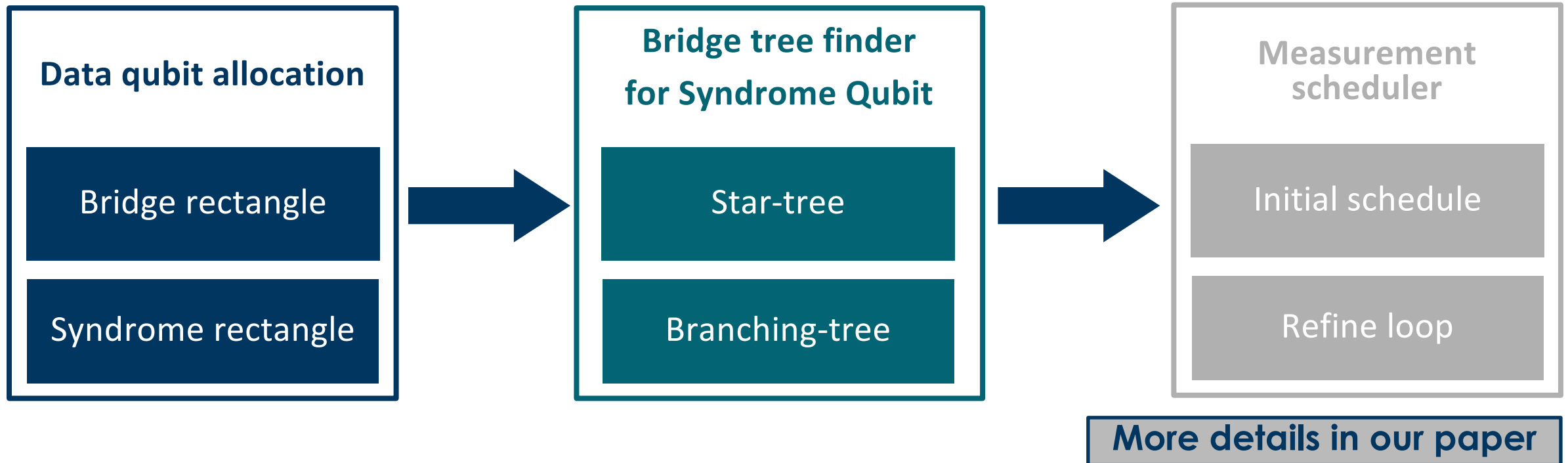
Surface Code



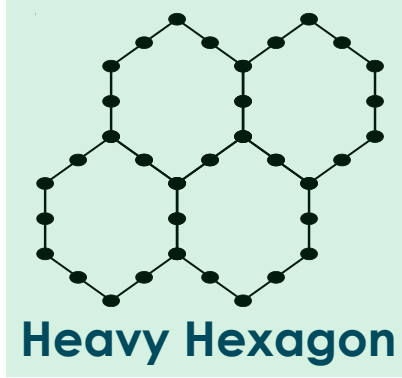
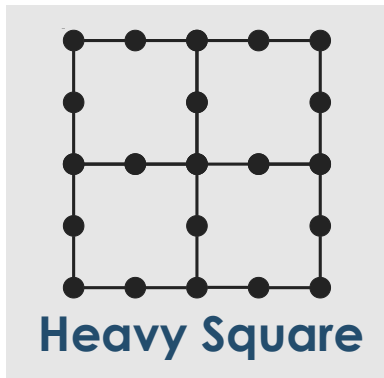
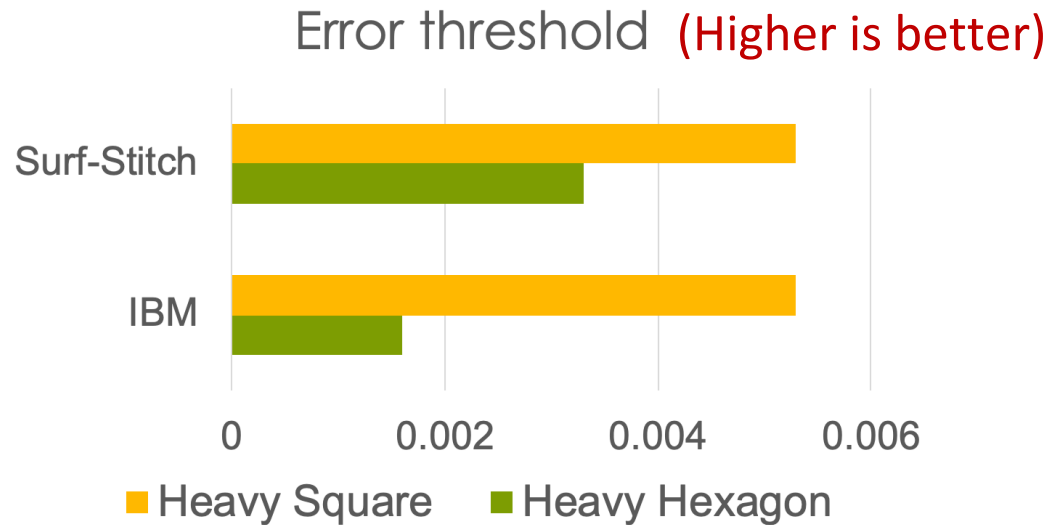
Some recent study **manually** designed **new** QEC codes tailored for these **sparse** architecture.

# Our Surf-Stitch Compiler: Overview [ISCA'22]

- We can systematically solve the mismatch: 1) Good abstraction (**Stablizer**); 2) Knowledge of **beneficial and legal transformations**; 3) An efficient search scheme.
- Compilation flow surface code to *different sparse quantum architectures*



# Performance



## Key Observation:

Our automatically generated QEC code is comparable or even better than IBM's **manually designed** QEC codes tailored for the sparse architectures.

## Our Key Insight:

Automatic compiler framework is more efficient to tap the large design space of QEC design when the problem is properly **abstracted**.

More results in our paper



# High-Level Operator in Program Testing

- Projection-Based Runtime Assertion for Quantum Program Testing and Debugging [OOPSLA'20]



# Quantum Programming

- Quantum programming is error-prone for programmers living in the classical world

Wrong sign on teleportation.qasm when  $X, Z == [1, 1] \neq$



vsoftco opened this issue on 24 Aug · 0 comments



vsoftco commented on 24 Aug · edited ▾

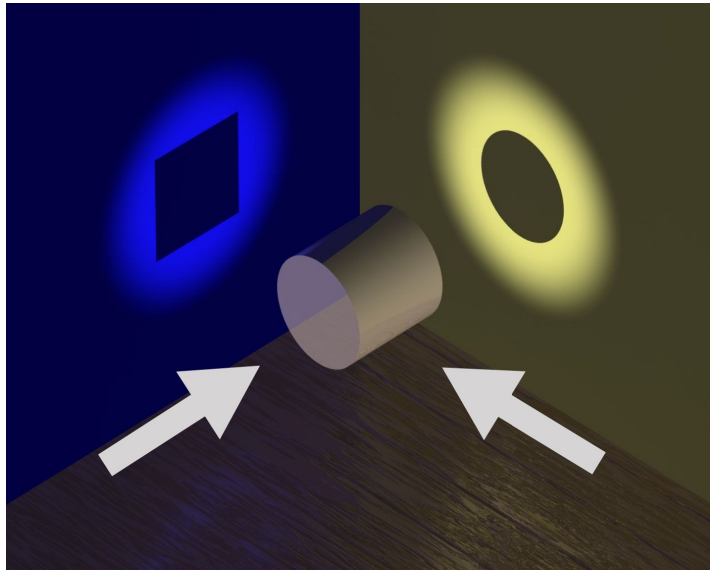


X and Z corrections should be interchanged, otherwise we get a MINUS (-) global phase when the final measurement result is [1, 1]. Proposed fix in [#48](#).

Quantum teleportation - quantum 'Hello World'  
Bug in the quantum 'Hello World'

# Test a Quantum State

- Existing approaches

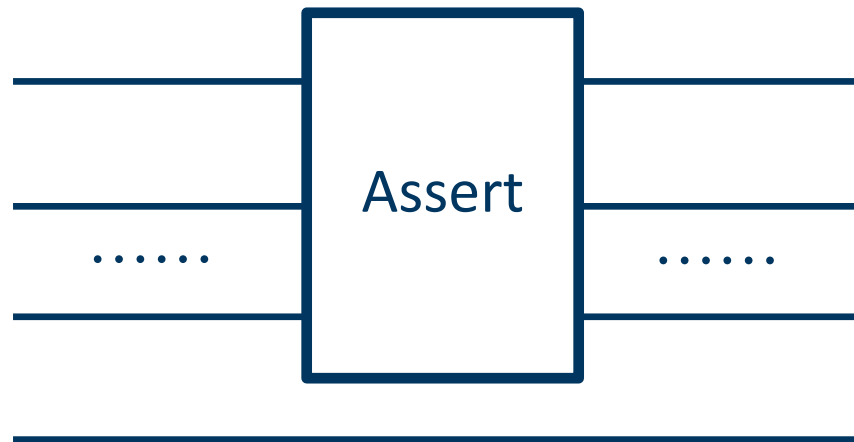


Quantum State Tomography

- a protocol to fully characterize any state
- very **expensive** – in a nutshell, observe a quantum state from many dimensions, repeated state preparation and measurement many times

# Test a Quantum State

- Existing approaches



Quantum Program Assertion

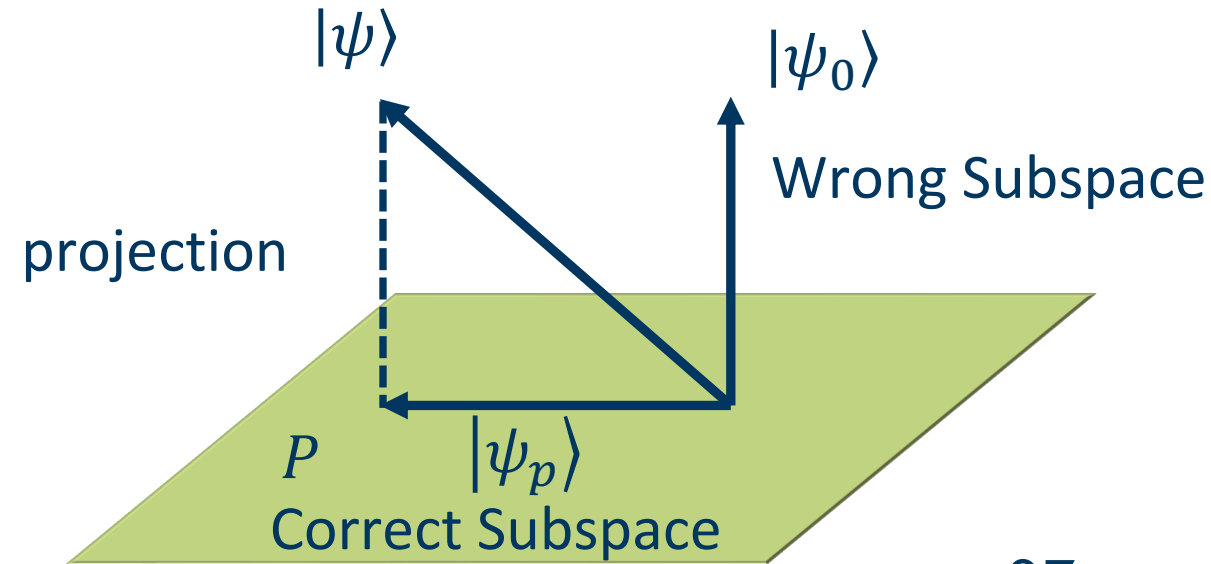
- describe a quantum state property using classical languages

$$\begin{array}{l} |1010 \dots 0101\rangle \\ |++ + \dots + +\rangle \\ |000 \dots 00\rangle + |111 \dots 11\rangle \end{array}$$

- poor expressive power**
- direct measurement will usually destroy the tested state

# Our Objective

- We hope to develop quantum **assertions** for testing and debugging:
  - **Strong expressive power**: specify complex quantum state properties
  - **Efficient checking**: efficiently quantum computers
- We select **Projection** for both needs.
- **Subspaces as predicates**

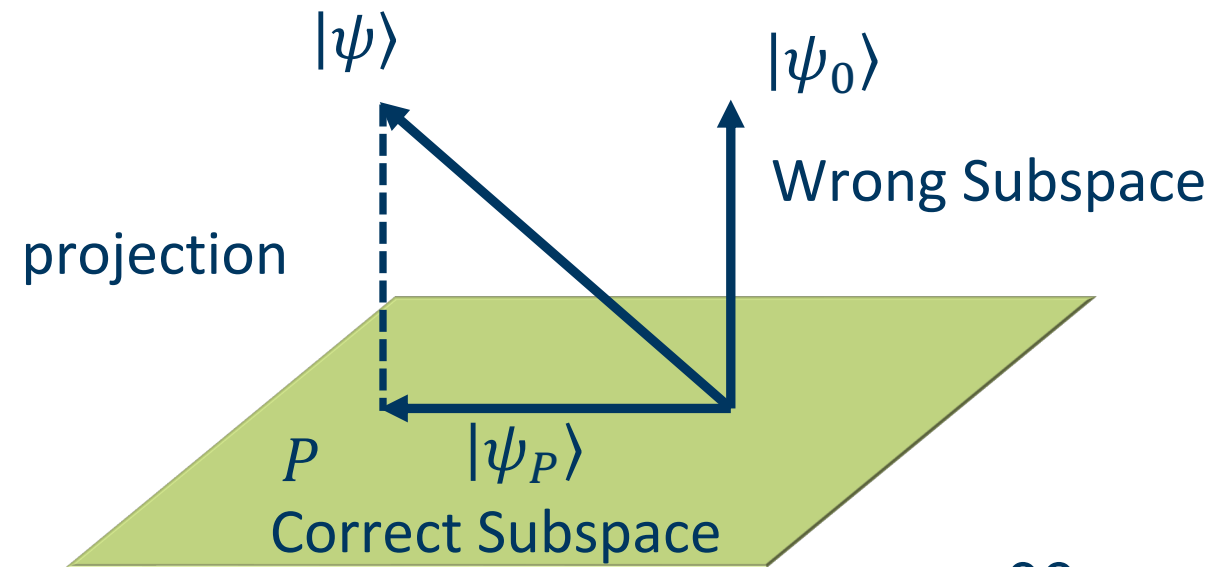


# Expression Power

- Projections allows to specify subspaces of any dimensions (rank of projection)

Example 1:  $P = |00\rangle\langle 00|$ , Subspace:  $\{|00\rangle\}$  (rank 1)

Example 2:  $P = |00\rangle\langle 00| + |11\rangle\langle 11|$ , Subspace:  $\{|00\rangle, |11\rangle\}$  (rank 2)



# Expression Power

- Projections allows to specify subspaces of any dimensions (rank of projection)

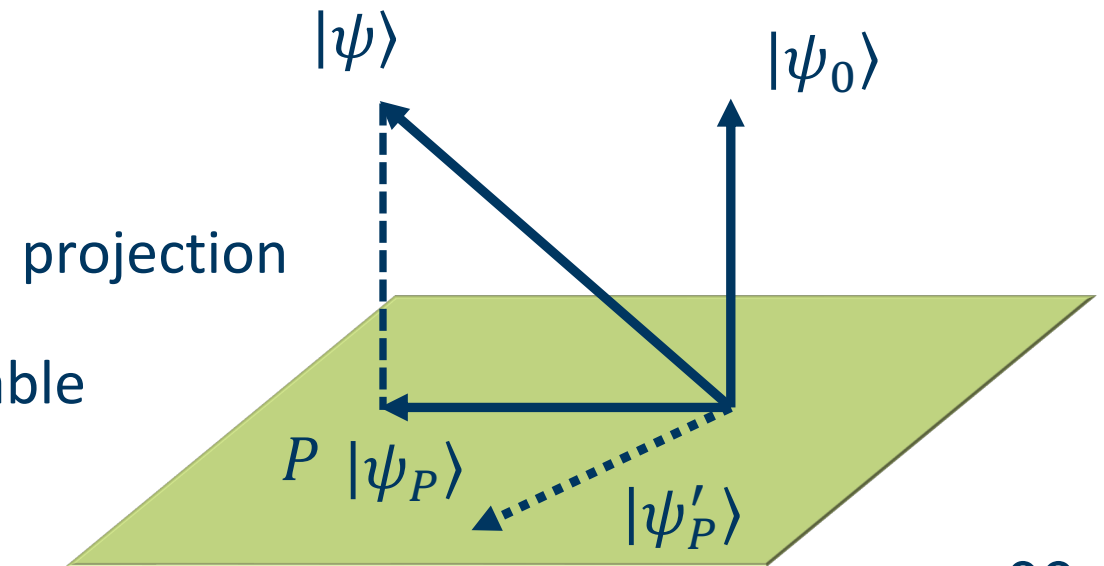
Example 1:  $P = |00\rangle\langle 00|$ , Subspace:  $\{|00\rangle\}$  (rank 1)

Example 2:  $P = |00\rangle\langle 00| + |11\rangle\langle 11|$ , Subspace:  $\{|00\rangle, |11\rangle\}$  (rank 2)

- **Caveat:** indistinguishable states

Because we are not doing tomography  
 $|\psi_P\rangle$  and  $|\psi'_P\rangle$  are indistinguishable

---> A sweet point, which will  
allow efficient checking

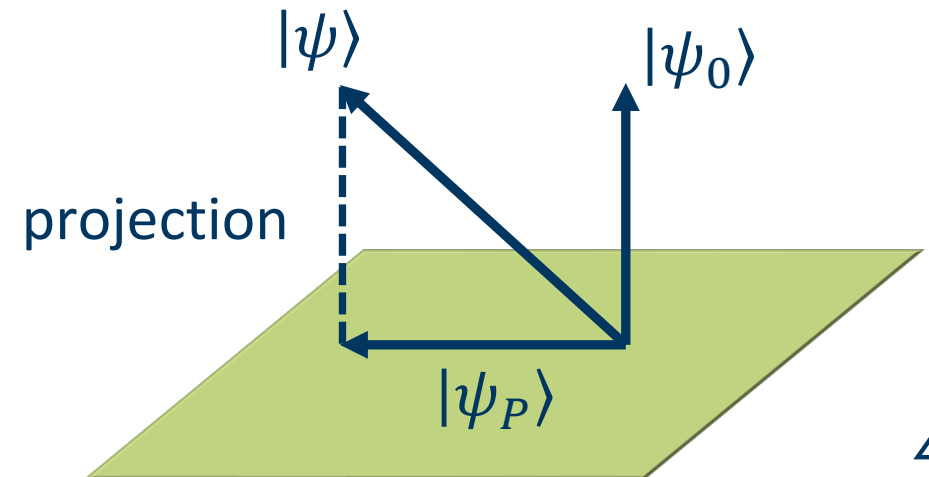


# Efficient Checking

- Turn characterization into determination (sound approximation)  
Whether in a subspace is much easier to check
- Projective measurement may preserve the measured state

$$P|\psi_P\rangle = |\psi_P\rangle$$

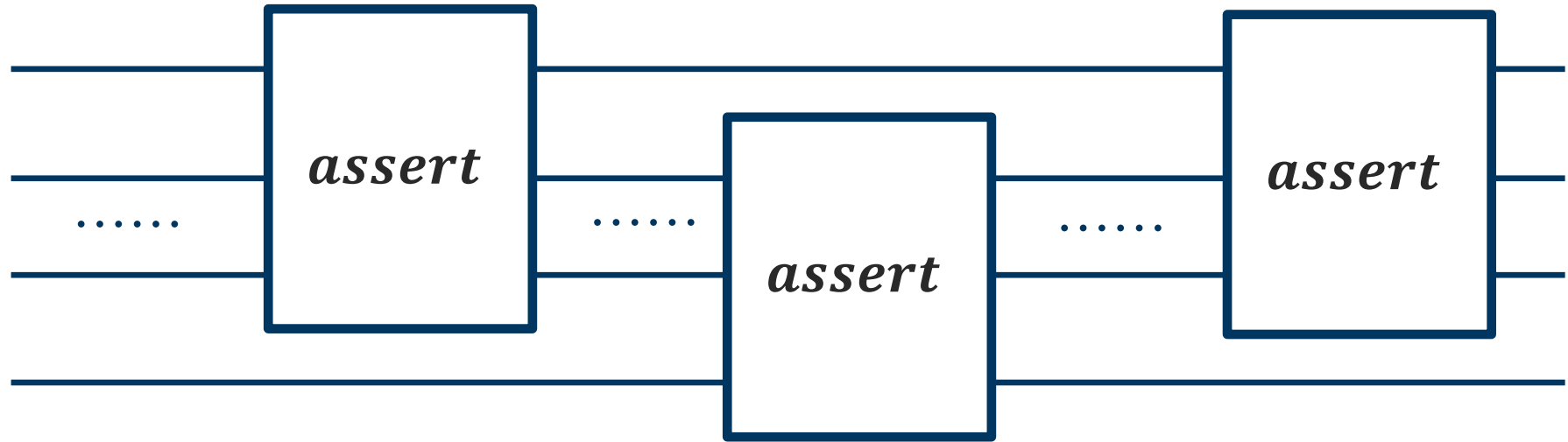
Allowing follow-up execution





# Projection-Based Assertion

- Language primitive  $\text{assert}(\bar{q}; P)$ , where  $P$  is a projection and  $\bar{q}$  is a set of qubits



- $M_P = \{M_{true} = P, M_{false} = I - P\}$

If true, continue

If false, abort and report

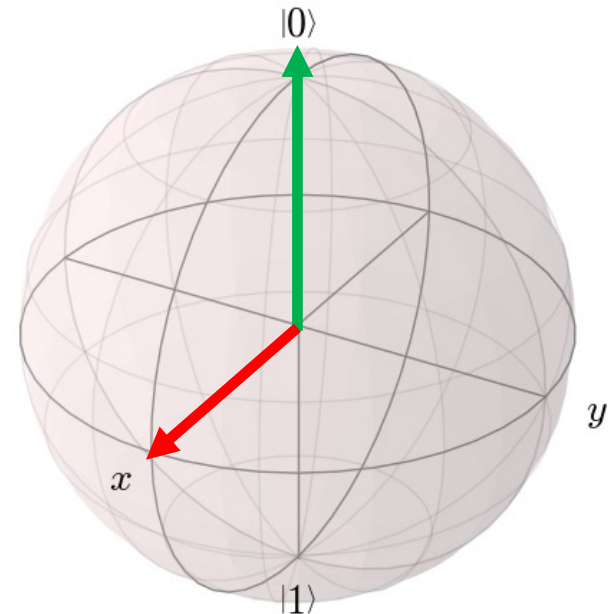
# Practical Implementation Issues

- $M_P = \{M_{true} = P, M_{false} = I - P\}$ , this constructed measurement may not be directly executable on a quantum computer.
- Two key constraints:
  - Limited measurement basis**
  - Dimension (rank) mismatch**

# Limited Measurement Basis

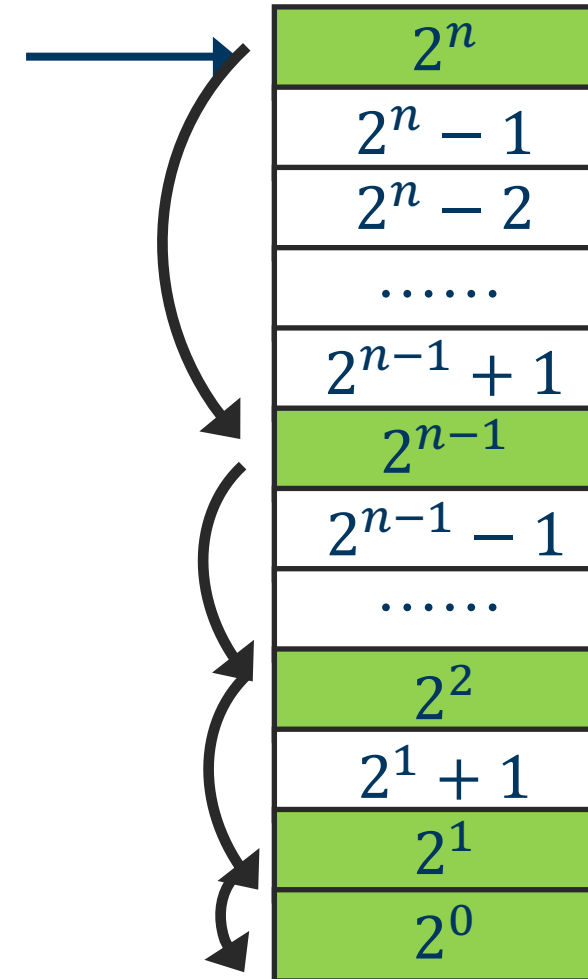
- Most physical quantum computers only support direct projective measurement along the computational basis  $\{|0\rangle, |1\rangle\}$
- $M_P = \{M_{true} = |0\rangle\langle 0|, M_{false} = |1\rangle\langle 1|\}$  😊
- $M_P = \{M_{true} = |+\rangle\langle +|, M_{false} = |-\rangle\langle -|\}$  😞

$$|+\rangle = \frac{|0\rangle + |1\rangle}{\sqrt{2}}, |-\rangle = \frac{|0\rangle - |1\rangle}{\sqrt{2}}$$



# Dimension Mismatch

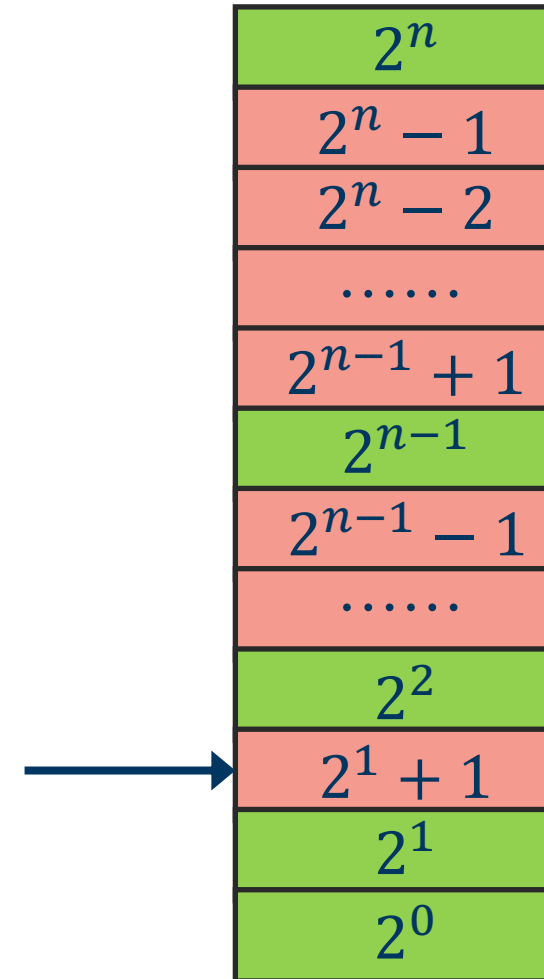
- $2^n$ -dimensional space for  $n$  qubits
- Measure one qubit, the space is reduced by half,  $2^{n-1}$ -dimensional space
- We can only measure an integer number of qubits
- Only support rank  $P \in \{2^{n-1}, 2^{n-2}, \dots, 2^0\}$



All possible ranks

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- Only support rank  $P \in \{2^{n-1}, 2^{n-2}, \dots, 2^0\}$
- $P = |00\rangle\langle 00| + |01\rangle\langle 01| + |11\rangle\langle 11|$  😞

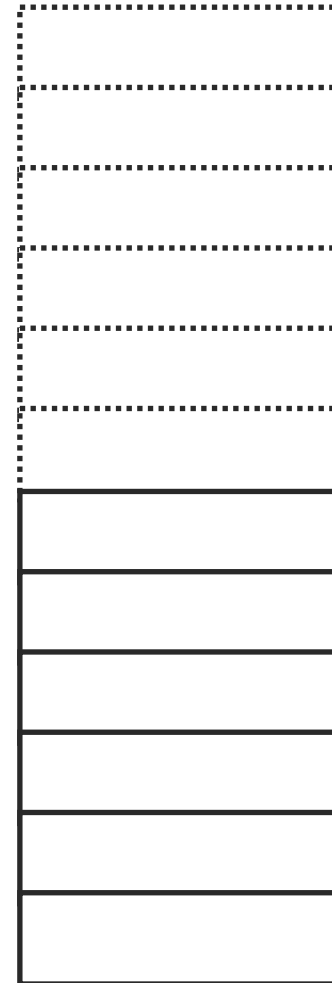


All possible ranks

# Assertion Compilation Flow

- We propose a compilation flow
  1. Control the dimension using **ancilla qubit**

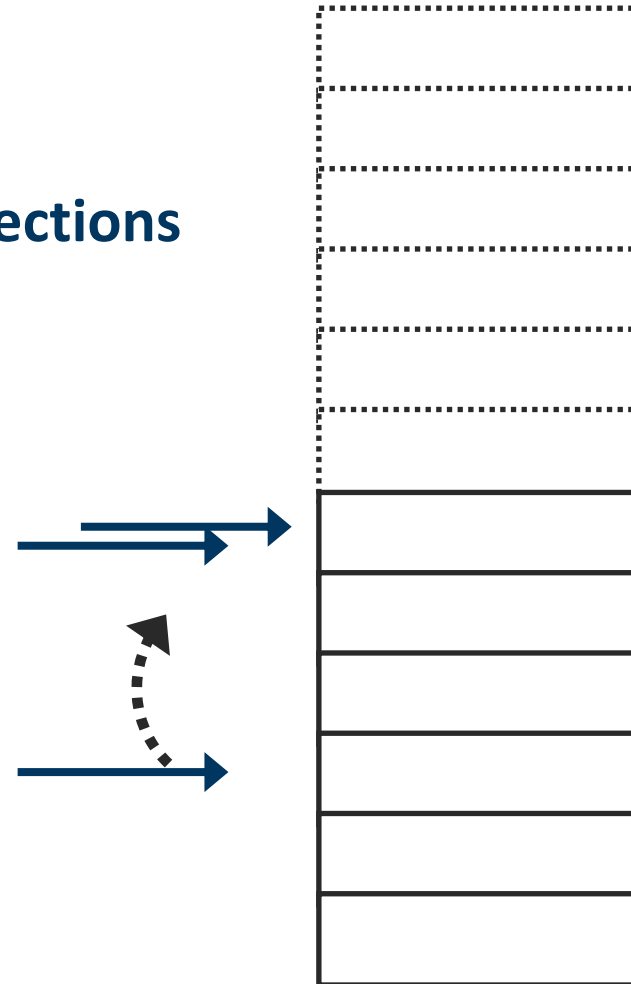
larger state  
space



# Assertion Compilation Flow

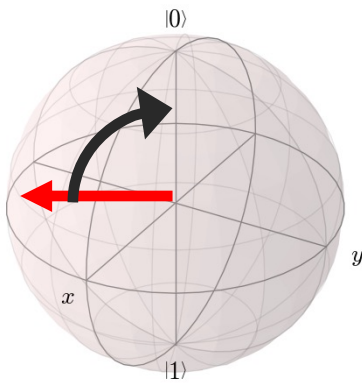
- We propose a compilation flow
  1. Control the dimension using **ancilla qubit** and **intersection of larger projections**

Change the relative position

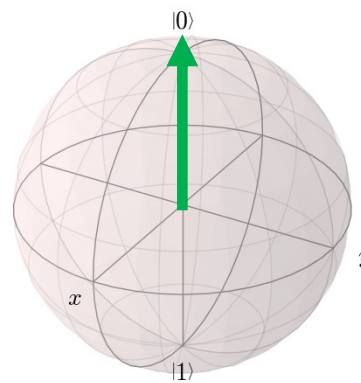


# Assertion Compilation Flow

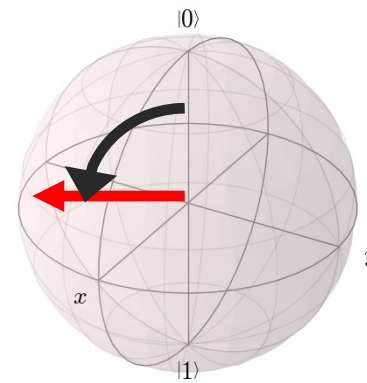
- We propose a compilation flow
  1. Control the dimension using **ancilla qubit** and **intersection of larger projections**
  2. Tune the measurement basis with **unitary transformations**



rotate



measure



rotate back



# Assertion Compilation Flow

- We propose a compilation flow
  1. Control the dimension using **ancilla qubit** and **intersection of larger projections**
  2. Tune the measurement basis with **unitary transformations**
- Making all projection-based assertion physically executable
- More details (statistical efficiency proof, example, etc.) can be found in our paper

# Error Mitigation

## Assertions as Error Mitigation

- One point calculation of energy, no variational loop
- Experiment A : no verification
- Experiment B : runtime verification of 3 symmetries
- Despite the increased circuit depth the error is halved!

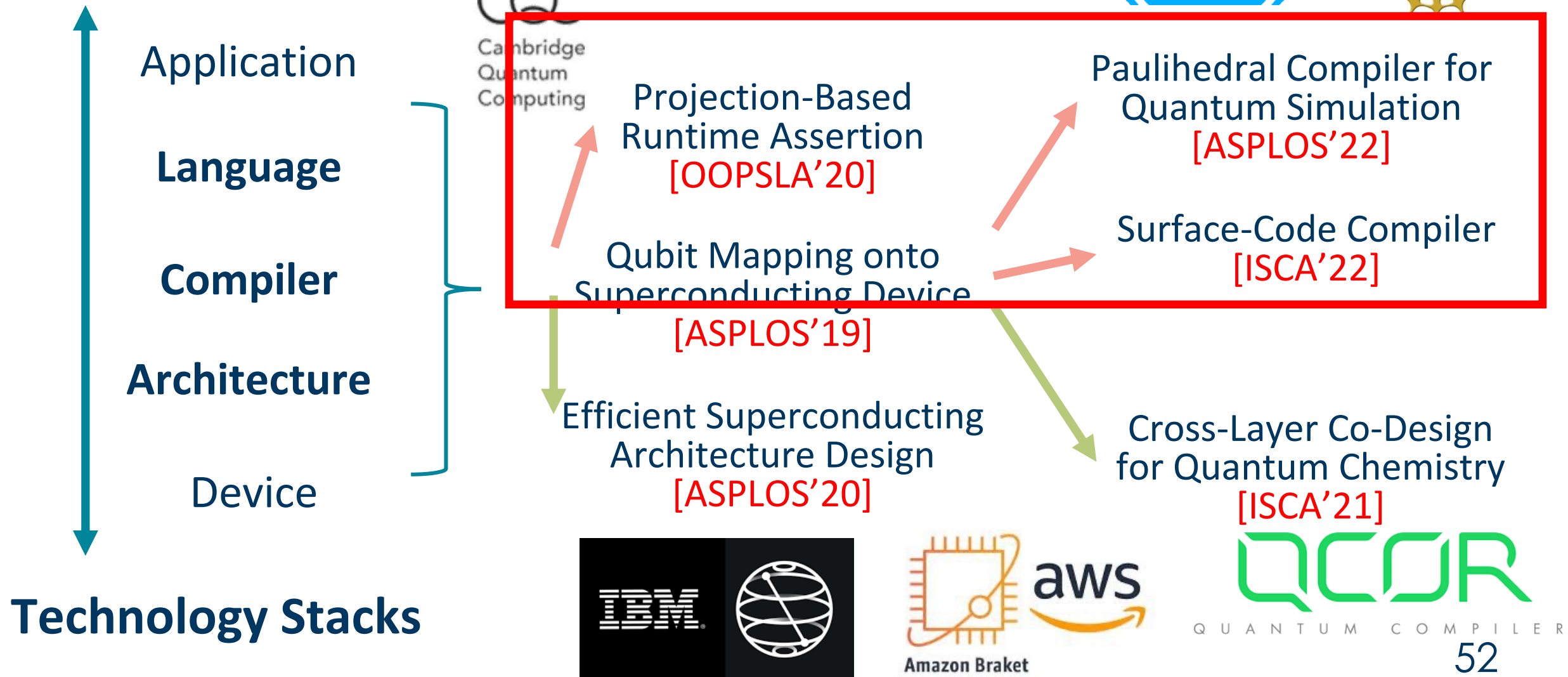
	Circuit size (CX gates)	Energy (Ha)	Error
No verification	15	-1.1032	0.1321
<b>Mid-circuit verification</b>	25	<b>-1.1738</b>	<b>0.0615</b>
Exact	-	-1.2353	-

Projection-based deployed in molecule simulation experiments  
Reduce simulation error by 50%

# Take Home Message

- High-level information is very useful
- Reconstructing high-level semantics from quantum assembly is hard
- Enhance your software with build-in high-level operators
- Design corresponding compilation/transformation

# Q & A



# Thank You!