

Determine if the following multistep method for approximating the solution to the IVP $y' = f(t, y)$, $a \leq t \leq b$, $y(a) = \alpha$ is stable:

$$w_{i+1} = 2w_{i-1} - w_i + \frac{h}{2}[5f(t_i, w_i) + f(t_{i-1}, w_{i-1})]$$

For above Equation, $m=2$, $a_0=2$, $a_1=-1$

then $P(\lambda) = \lambda^2 + \lambda - 2 = 0$ \Leftarrow Use Def 5.22

$$(\lambda + 2)(\lambda - 1) = 0$$

$$\lambda_1 = 1, \lambda_2 = -2$$

$$\Rightarrow |\lambda_1| = 1, |\lambda_2| = 2 > 1$$

\Rightarrow Doesn't Satisfy Root Condition as $|\lambda_2| > 1$

\Rightarrow By Def 5.23, This method is *unstable*