# Data-analysis and Retrieval Top-k searching

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May 10, 2023

#### Top-k queries

An example top-k query:

```
SELECT * FROM UsedCars
WHERE brand = 'BMW' OR brand = 'Mercedes'
ORDER BY 8*price + 2*mileage
LIMIT 20
```

General characteristics:

We order resulting tuples according to some function f and are interested in a limit set of tuples containing extreme values of f.

#### Top-k queries

Another example: similarity matching in image databases.

Given a certain image qim:

```
SELECT im.id FROM Images im
WHERE date >= '01.01.2016'
ORDER BY DESC
     0.5*ColorSim(qim, im) + 0.5*TextureSim(qim, im)
LIMIT 10
```

## Top-k query processing

A naive approach to top-k query processing:

- Process the basic structure of the query (before the ORDER)
- Do the sorting based on the function f
- Scan the first k tuples from the resulting table

So in general, finding a top-10 might require processing 10,000 or  $10^6$  or  $10^9$  tuples.

Can we do better?



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Can we do better?

Yes, we can!

(But there are some conditions)



# Top-k query processing: monotonicity

- We require that *f* is monotone
- In our examples, we suppose f is monotonic non-decreasing  $^1$
- Intuition: if you increase the value one of the parameters of f and keep the others constant, f will not decrease.
- Definition: suppose f has n parameters. For each  $i \in [1..n]$  we require that for all  $x_1, x_2, ..., x_n$  and  $y_i$ :  $x_i < y_i \implies f(x_1, x_2, ..., x_i, ..., x_n) \le f(x_1, x_2, ..., y_i, ..., x_n)$

 $<sup>^1</sup>$ Of course, with some adaptations, we could also apply the algorithms if f is monotonic non-increasing.

## Top-k algorithms

- We will look at two algorithms by Fagin e.a.
- We suppose that we access the data columns through lists
- TA: Threshold Algorithm sorted access and random access to each list
- NRA: No Random Access algorithm sorted access to each list, but no random access

## Top-k: lists representing function parameters

We represent the attributes which are arguments of f by separate lists. Remember that we suppose f has to be maximized and is monotonic non-decreasing. The values of lists A and B each have a known minimum (in our case 0).

Example: the table below has sorted access to both A and B.

oid	Α	В	С
001	4	7	
002	2	8	l
003	3	1	

For TA and NRA, it is represented as:

oid	Α
001	4
003	3
002	2

oid	В
002	8
001	7
003	1

#### Top-k: lists in a relational context

- If we have an RDBMS with a classical, record oriented architecture, we can realize sorted access by creating a B-tree index on each column that acts as a list.
- Caveat: note that you cannot manipulate the B-tree directly.
   You are forced to simulate the manipulation of the B-tree using SQL-queries.
- If we have a main-memory RDBMS with column stores, sorted access can by obtained by efficient internal sorting techniques.
- Random access based on oid can be realized either by an index structure or by a (duplicate) list sorted on oid.

Basic approach: in each round of the algorithm, one new value from each list is inspected, starting at the top. Suppose f = A + B.

oid	Α
001	4
003	3
002	2

oid	В
002	8
001	7
003	1

We keep track of the following variables:

Max-A: maximum value of A to be found in following rounds (4)

Max-B: maximum value of B to be found in following rounds (8)

Threshold T: maximum value of f to be found in next rounds (12)

Buffer: known [oid, f] tuples: [001, 11], [002, 10]

Partial top-k: still empty (why?)



Intermezzo 1: TA (four rounds)

OID	Α
4	100
1	90
6	80
5	70
2	40
3	30

OID	В
6	100
5	90
1	70
3	50
4	30
2	20

ROUND	1	2	3	4
Max-A	100			
Max_B	100			
Treshold	200			
Buffer	[4:130]			
	[4:130] [6:180]			
Top-k				

OID	Α
4	100
1	90
6	80
5	70
2	40
3	30

OID	В
6	100
5	90
1	70
3	50
4	30
2	20

ROUND	1	2	3	4
Max-A	100	90		
Max_B	100	90		
Treshold	200	180		
Buffer	[4:130] [6:180]	[4:130] *[6:180] [1:160] [5:160]		
Top-k		[6:180]		

## NRA: No random access algorithm

Basic approach: in each round of the algorithm, one new value from each list is inspected, starting at the top, but now we cannot find the corresponding oid in the other list quickly.

oid	Α
001	4
003	3
002	2

oid	В
002	8
001	7
003	1

We keep track of the following variables:

Max-A: maximum value of A to be found in next rounds (4)

Max-B: maximum value of B to be found in next rounds (8)

Threshold T: maximum value of f to be found in next rounds (12)

Buffer: known [oid, f] tuples: [001, 4 - 12], [002, 8 - 12]

Partial top-k: still empty (why?)



#### NRA: No random access algorithm

Intermezzo 2: NRA (four rounds)

# NRA: No Random Access Algorithm

OID	Α
4	90
1	90
6	40
5	30
2	20
3	10

OID	В
6	100
5	40
1	40
4	30
3	20
2	10

ROUND	1	2	3	4
Max-A	90			
Max_B	100			
Treshold	190			
Buffer	[4: 90 - 190]		1	
(changing!)	[6: 100 - 190]			
Top-k				

# NRA: No Random Access Algorithm

OID	Α
4	90
1	90
6	40
5	30
2	20
3	10

OID	В
6	100
5	40
1	40
4	30
3	20
2	10

ROUND	1	2	3	4
Max-A	90	90		
Max_B	100	40		
Treshold	190	130		
Buffer	[4: 90 - 190]	[4: 90 - 130]		
(changing!)	[6: 100 - 190]	[6: 100 - 190]		
		[1: 90 - 130]		
		[5: 40 - 130]		
Top-k				

#### Top-k: more advanced approaches

We have seen top-k query processing on single tables. More complications rise when the query involves a join of several tables.

The reference below describes an approach where top-k processing is fully integrated with classical relational query optimization.

#### https:

//cs.uwaterloo.ca/~ilyas/papers/ilyassigmod05.pdf

#### Top-k: epilog

- In 2013, Nick Schuiling and Maarten van Duren implemented these algorithms on top of MonetDB, a main-memory column store RDBMS developed at the CWI. They realized huge performance gains on TPC/H benchmarks.
- You are invited to apply smart top-k algorithms in Lab 1.