Linear D.E

- > D.E is said to be linear if satisfies the following conditions
- 1. Dependent variable and it's desiratives occur first degree.
- 2. No term in the eq: that contains the product of dependent variable and it's derivatives)
- 3. No transcedental Punction with dependent variable.

$$\frac{dy}{dx} + P(x)y = Q(x)$$

Solution (1+x²)
$$\frac{dy}{dx} + 2xy = 4x²$$

Solution (1+x²) $\frac{dy}{dx} + \frac{2x}{(1+x²)} \cdot y = \frac{4x²}{(1+x²)}$, $P(x) = \frac{2x}{(1+x²)}$ $Q(x) = \frac{4x²}{(1+x²)}$

I.F. = $e^{\int \frac{2x}{(1+x²)} dx} = \frac{1}{1+x²} \cdot (1+x²) = 1+x²$
 $= 4 \int x^2 dx + c$
 $= 4 \int x^2 dx + c$
 $= 4 \int x^3 + c$
 $= 4 \int x^3 + c$
 $= 4 \int x^3 + c$
 $= 6 \int x^3 + c$
 $=$

Q- Find the general solution of (x2-9) dy +xy=0 $\frac{dy}{dx} + \frac{y}{y^2 - q}, y = 0 , P(x) = \frac{x}{x^2 - q} \quad Q(x) = 0$ IF= e = = = = = = = = = [x=q]/2 [x=q]/ y√x2-9 = ∫0. 15 dn+C y√2-9 = C > y = € , xy3 0€ x<-3 Initial-Value Problem Solve: (1) +y=x, y(0)=4 P(x)=1 Q(0)=x IF= e = ex yex = fx. exdx+c yex = xex- steak+c yer = re-ex+c y = x-1+cex - General solution y(0)=0-1+c=(0) 4 =-1+0

y = x+5=x-1 003

Bernoullis Differential Equation

It no or not them Linear of not then Bornoull's

$$\frac{1}{(1-n)} \frac{dz}{dx} + P(x)z = Q(x)$$

$$\frac{dz}{dx} + (1-n)P(x)z = (1-n)Q(x) + Unear D.E$$

Z. See'x =
$$\int see'x (-tan'n)dn + C$$

= $-\int tan'n \cdot sec'ndn + C$

id fam = See x

Z. Seàx =
$$-\frac{\tan^3x}{3}$$
 + C

$$y' = -\frac{1}{3} \frac{\tan^3x}{\cos^3x} + \frac{C}{\sec^3x}$$

$$y^{-1} = \frac{3c - tanin}{3secin}$$

in- Solve the following mitial value problem.

Worksheet #03

Linear and Bernoulli's D.E

1.
$$\frac{dy}{dx} + \frac{y}{x} = x^{3} - 3$$
 Am: $xy = \frac{x^{5}}{5} - 3\frac{x^{2}}{2} + c$

11.
$$\chi^2 dy + y(x+y) dx = 0$$
 Ans: $\frac{1}{xy} = -\frac{1}{2x^2} - c$

Ams: x Lny=xex-ex+c