# Quizzes of TTK4225 - Systems Theory, Autumn 2020

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Can we have  $BA \neq \mathbf{0}$  even if  $AB = \mathbf{0}$ ?

Which is more correct to say among these two options?

- a matrix defines a specific linear transformation
- 2 a matrix defines a specific linear transformation from a specific basis into another
- the first
- the second
- they are equivalent
- I don't know

Assume that a LTI system admits a rational transfer function with two distinct zeros and three distinct poles. Then the associated minimal state space system realizing that transfer function has its state update matrix . . .

- diagonalizable
- diagonalizable if there are no poles-zeros cancellations
- non-diagonalizable
- I don't know

If the state update matrix of a LTI system is diagonalizable then the system is controllable

- true
- false
- it depends
- I don't know

Consier a generic matrix  $A \in \mathbb{R}^{n \times n}$ , and its characteristic polynomial, i.e., the scalars  $\alpha_0, \alpha_1, \dots, \alpha_{n-1}$  such that

$$A^n = -\alpha_{n-1}A^{n-1} - \ldots - \alpha_1A - \alpha_0I$$

and forming the polynomial

$$s^{n} + \alpha_{n-1}s^{n-1} + \ldots + \alpha_{1}s + \alpha_{0}.$$

Then the characteristic polynomial is the lowest order polynomial that is nullified by A. I.e., there are no other scalars  $\beta_0, \beta_1, \dots, \beta_{m-1}$  with m < n such that

$$A^{m} = -\beta_{m-1}A^{m-1} - \dots - \beta_{1}A - \beta_{0}I$$

- true
- false
- it depends
- 4 I don't know

Compute  $e^{At}$  with

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

Compute  $e^{At}$  with

$$A = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Consider the autonomous system

$$\begin{cases} \dot{x} = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} x \\ y = \begin{bmatrix} 1 & 0 & 1 \end{bmatrix} x \end{cases}$$

Compute y(t) assuming that the initial condition for the system is

$$\boldsymbol{x}_0 = \begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix}$$

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#### Consider the system

$$\begin{cases} \dot{\boldsymbol{x}} = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \boldsymbol{x} + \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \boldsymbol{u} \\ \boldsymbol{y} = \begin{bmatrix} 1 & 0 & 1 \end{bmatrix} \boldsymbol{x} \end{cases}$$

- Compute its step response;
- ② say how the step response would change if B was  $[0,0,1]^T$ ;
- lacksquare say how the step response would change if C was [1,0,0].

Consider the system

$$\begin{cases} \dot{\boldsymbol{x}} = \begin{bmatrix} 1 & 3 & 5 \\ 2 & 1 & 0 \\ 0 & 1 & 2 \end{bmatrix} \boldsymbol{x} + \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \boldsymbol{u} \\ \boldsymbol{y} = \begin{bmatrix} 1 & 0 & 1 \end{bmatrix} \boldsymbol{x} \end{cases}$$

How may one do to compute its step response?

Compute  $e^{At}$  with

$$A = \begin{bmatrix} 0 & 1 \\ -k & -f \end{bmatrix}$$

Assume that a system is s.t. its state update matrix A is s.t.  $A^m = \mathbf{0}$  for some m. How does this help computing the forced response of the system?