

$$1.1) 1 - 0.45 = \boxed{0.55}$$

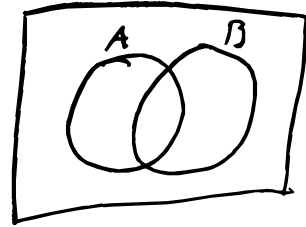
$$1.2) 0.5 + 0.2 - 0.55 = \boxed{0.15}$$

$$A \cup B = A + B - AB$$

$$AB = A + B - A \cup B$$

$$1.3) P(A \cap \bar{B}) = P(A) - P(A \cap B) = 0.5 - 0.15 = \boxed{0.35}$$

$$1.4) \boxed{\text{NO}}$$



$$2.1) \quad 1 - \left(\frac{1}{6}\right)^0 \left(\frac{5}{6}\right)^4 \approx 0.5177 = \frac{671}{1296}$$

$$2.2) \quad 1 - \left(\frac{1}{6}\right)^0 \left(\frac{5}{6}\right)^{20} \approx 0.9739$$

$$2.3) \quad p = 1 - \left(\frac{5}{6}\right)^n \quad n = \frac{\ln(1-p)}{\ln\left(\frac{5}{6}\right)} \quad p=0.9 \quad n \approx 12.63 = \underline{\underline{13}}$$

$$3) \quad P(3) + P(2) + P(1) \rightarrow \frac{1}{9} + \frac{2}{9} + \frac{1}{9} = \boxed{\frac{4}{9}}$$

$$P(E) = 2P(O)$$

$$2P(O) + P(O) = 1$$

$$P(O) = \frac{1}{3} \quad \text{each odd face } P = \frac{1}{9}$$

$$P(E) = \frac{2}{3} \quad \text{each even face } P = \frac{2}{9}$$

4.1) Total Books = $3+2+2+3 = 10$

$${}^{10}C_3 = \frac{10!}{3!7!} = \frac{10 \cdot 9 \cdot 8}{3 \cdot 2} = 10 \cdot 3 \cdot 4 = \boxed{120 \text{ ways}}$$

4.2) $\boxed{\frac{3}{20}}$

$$\frac{{}^3C_1 \cdot {}^2C_1 \cdot {}^3C_1}{120} = \frac{1 \cdot 1 \cdot 1}{120} = \frac{1}{120} = \frac{3}{20}$$

$$5.1) \frac{1}{3}P_A + \frac{1}{3}P_B + \frac{1}{3}P_C = \frac{0.002 + 0.02 + 0.001}{3} = \frac{23}{3000} \approx 0.007667$$

$$5.2) P(A|D) = \frac{P(D|A)P(A)}{P(D)} = \boxed{0.08696}$$

$$P(B|D) = \frac{P(D|B)P(B)}{P(D)} = \boxed{0.8696}$$

$$P(C|D) = \frac{P(D|C)P(C)}{P(D)} = \boxed{0.04348}$$

$$5.3) 0.5P_A + 0.1P_B + 0.4P_C = \boxed{0.0034}$$

$$5.4) P(A|D) = \frac{P(D|A)P(A)}{P(D)} = \boxed{0.2941}$$

$$P(B|D) = \boxed{0.5882}$$

$$P(C|D) = \boxed{0.1176}$$

$$6a) \frac{4}{52} = \boxed{\frac{1}{13}}$$

$$6b) \boxed{\frac{1}{52}}$$

$$6c) \frac{1}{52} + \frac{1}{52} = \boxed{\frac{1}{26}}$$

$$6d) \boxed{\frac{1}{2}}$$

$$7.1) P(H_1) = \frac{13}{52}$$

$$7.2) P(H_2) = \underbrace{\frac{13}{52} \cdot \frac{12}{51}}_{\downarrow} + \underbrace{\frac{39}{52} \cdot \frac{13}{51}}_{\downarrow} = \boxed{\frac{1}{4}}$$

Prob of 1st
draw being
heart

Prob of
1st draw
not being
heart