

Chapter 5

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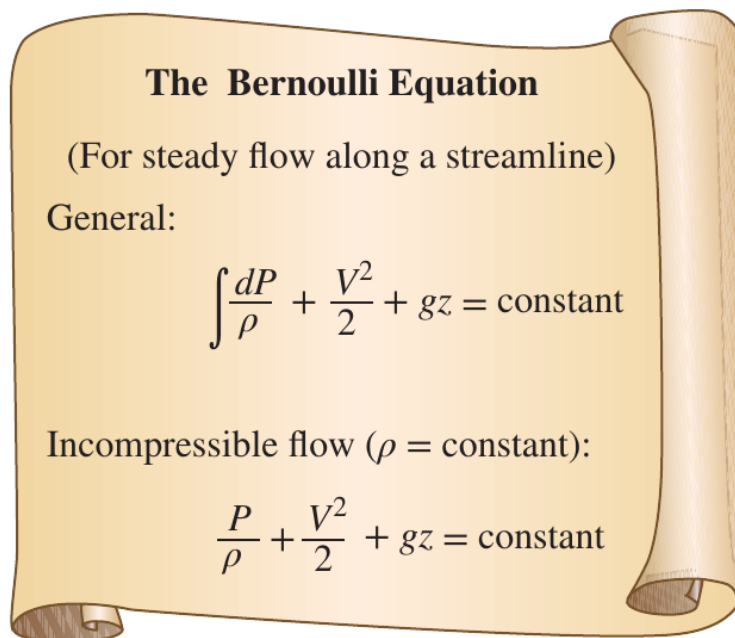
5-1 Conversion of Mass

- **Mass and Flow Rate:** $\dot{m} = \rho \dot{V}$
- **Mass Balance:** $\sum_{in} \dot{m} = \sum_{out} \dot{m}$
- **Incompressible Flow:** $\dot{V}_1 = \dot{V}_2 \Rightarrow v_1 A_1 = v_2 A_2$

5-2 The Bernoulli Equation

The **Bernoulli Equation** is an approximate relation between pressure, velocity, and elevation, and is valid in regions of steady, incompressible flow where net frictional forces are negligible

$$\frac{P_1}{\rho} + \frac{V_1^2}{2} + gz_1 = \frac{P_2}{\rho} + \frac{V_2^2}{2} + gz_2$$



5-3 Energy Analysis of Steady Flows

$$\dot{m} \left(\frac{P_1}{\rho} + \alpha_1 \frac{V_1^2}{2} + gz_1 \right) + \dot{W}_{\text{pump},u} = \dot{m} \left(\frac{P_2}{\rho} + \alpha_2 \frac{V_2^2}{2} + gz_2 \right) + \dot{W}_{\text{turbine},e} + E_{\text{mech,loss}}$$

- α : the kinetic energy correction factor
- $\dot{W}_{\text{pump},u}$: the useful energy that the pump delivered
- $\dot{W}_{\text{turbine},e}$: the energy used by turbine

- $E_{\text{mech,loss}}$: the mechanical energy that lost