

CH_3

Hooke's Law

$$\sigma = E\varepsilon$$

- E : the modulus of elasticity of Youngs' modulus, which has the stress units

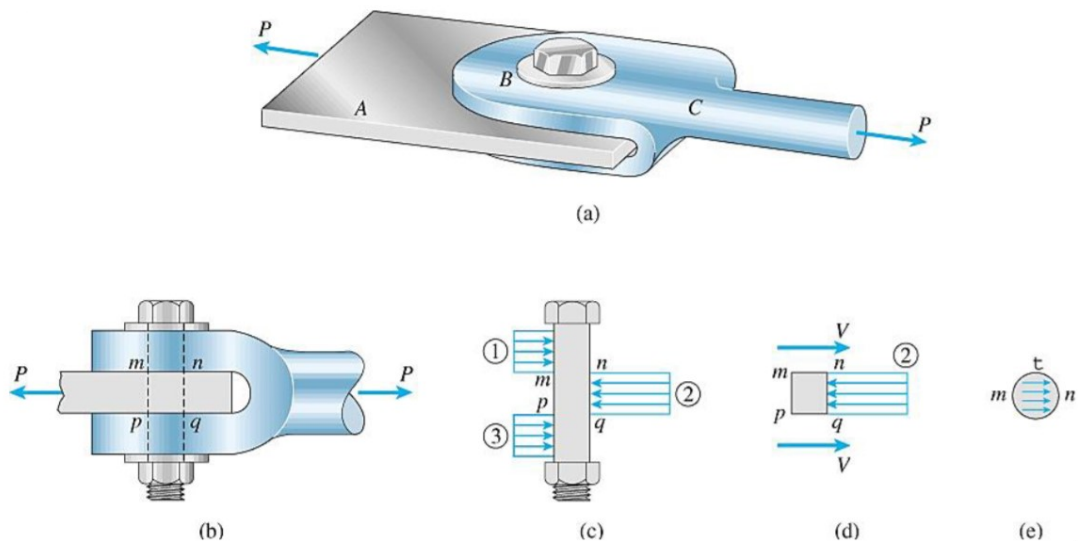
Poisson Ratio

$$\nu = -\frac{\varepsilon'}{\varepsilon}$$

- ν : Poisson Ratio
- ε : axial strain
- ε' : lateral strain

Shear Stress

the stress component that act in the plane of the sectioned area



Average Bearing Stress

$$\sigma_b = \frac{F_b}{A_b}$$

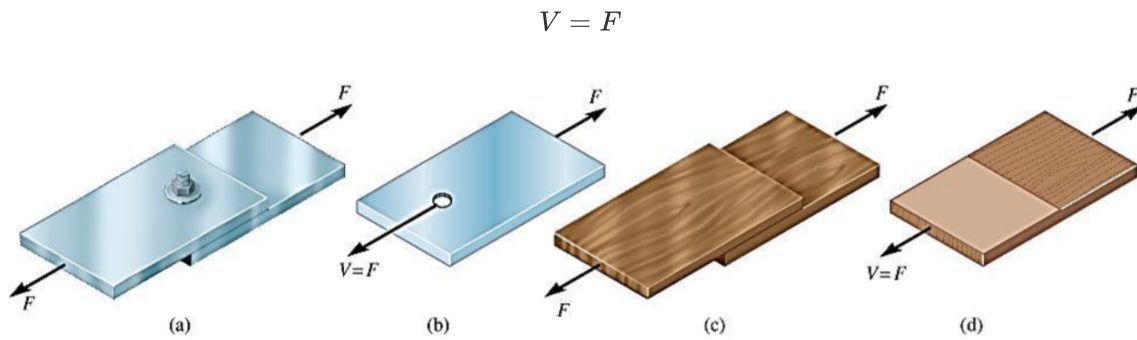
- F_b : bearing force
- A_b : bearing area

Average Shear Stress at Section

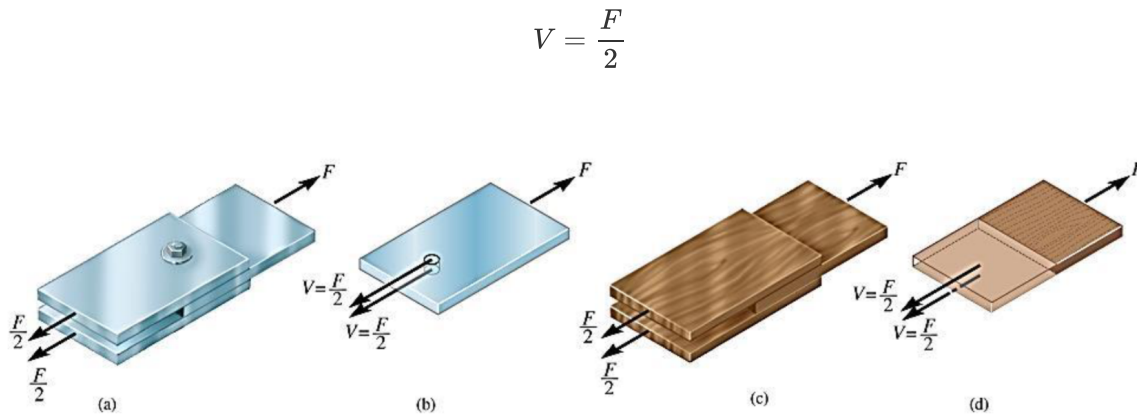
$$\tau_{aver} = \frac{V}{A}$$

- V : internal shear force at section determined from equations of equilibrium
- A : area of section

Single Shear



Double Shear



- Positive strain is when the angle between two positive faces is reduced
- Negative strain is when the angle between two positive faces is increased

Hooke's Law for Shear

$$\tau = G\gamma$$

$$G = \frac{E}{2(1 + \nu)}$$

- G : shear modulus of elasticity

Allowable Stresses and Allowance Loads

When designing a structural member or mechanical element, the design interest is **strength**, that is the *capacity of the object to support or transmit loads*

- factor of safety (F.S.)

$$n = \frac{\text{Actual Strength}}{\text{Required Strength}}$$

- allowable strength

$$\sigma_{\text{allow}} = \frac{\sigma_Y}{n_1}$$

$$\tau_{\text{allow}} = \frac{\tau_Y}{n_2}$$

- σ_Y and τ_Y are yield stresses
- n_1 and n_2 are the corresponding factors of safety.

Design for Axial Loads and Direct Shear

- determine the area of section subjected to a normal force

$$A = \frac{P}{\sigma_{\text{allow}}}$$

- determine the area of section subjected to a shear force

$$A = \frac{V}{\tau_{\text{allow}}}$$