Backpropagation

白白传播

更有级的 梯枝下降

Gradient Descent

Network parameters $\theta = \{w_1, w_2, \dots, b_1, b_2, \dots\}$

Starting Parameters
$$\theta^0 \longrightarrow \theta^1 \longrightarrow \theta^2 \longrightarrow \dots$$

Parameters
$$\theta^0 \longrightarrow \theta^1 \longrightarrow \theta^2 \longrightarrow \dots$$

$$\nabla L(\theta)$$

$$= \begin{bmatrix} \partial L(\theta)/\partial w_1 \\ \partial L(\theta)/\partial w_2 \\ \vdots \\ \partial L(\theta)/\partial b_1 \\ \partial L(\theta)/\partial b_2 \\ \vdots \end{bmatrix}$$
Compute $\nabla L(\theta^0)$

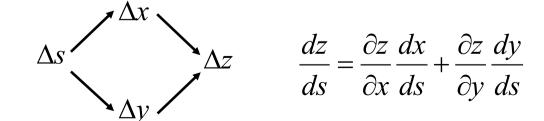
$$\theta^1 = \theta^0 - \eta \nabla L(\theta^0)$$

$$\theta^2 = \theta^1 - \eta \nabla L(\theta^1)$$
Millions of parameters
$$To compute the gradients efficiently, we use backpropagation.$$

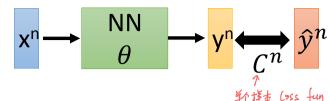
Chain Rule

Case 1
$$y = g(x)$$
 $z = h(y)$
$$\Delta x \to \Delta y \to \Delta z$$

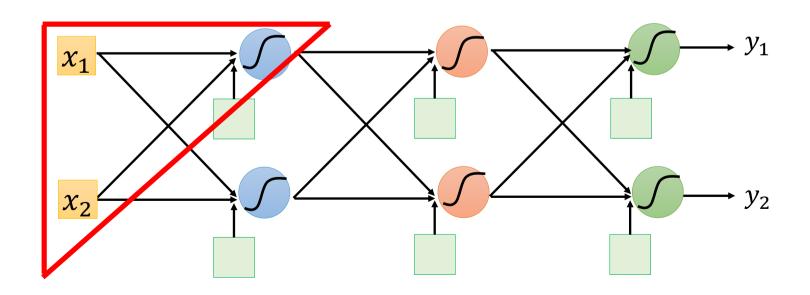
$$x = g(s)$$
 $y = h(s)$ $z = k(x, y)$



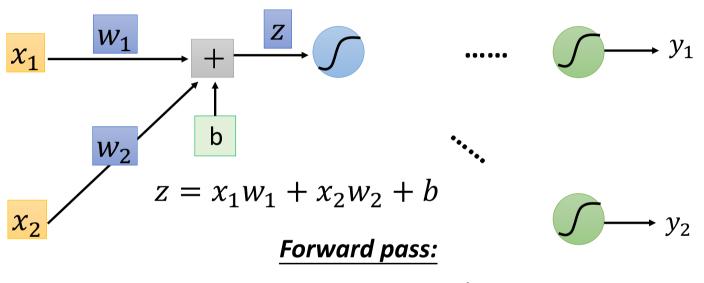
Backpropagation



$$L(\theta) = \sum_{n=1}^{N} C^{n}(\theta) \qquad \frac{\partial L(\theta)}{\partial w} = \sum_{n=1}^{N} \frac{\partial C^{n}(\theta)}{\partial w}$$



Backpropagation



$\frac{\partial C}{\partial w} = ? \frac{\partial z}{\partial w} \frac{\partial C}{\partial z}$ (Chain rule)

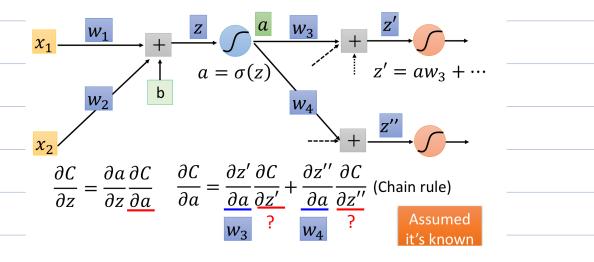
Compute $\partial z/\partial w$ for all parameters

Backward pass:

反向传播程解

受験できる。
$$\frac{\partial L(\theta)}{\partial w} = \sum_{n=1}^{N} \frac{\partial C^{n}(\theta)}{\partial w}$$

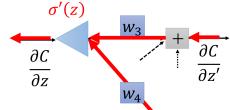
Compute $\partial C/\partial z$ for all activation function inputs z



直接长 可以, 根据复合运输出导链扩泛则, 后面分叉非常的假如从前往后军, 如归图, 欲求可以需要 是 为 知知, 但断东西又流在后面的东西。

反过来算

光前向传播, input (学),得到新节点的值,再反向传播, 购前面计算偏弱, 扁延后面的偏导, 例以从后往前算



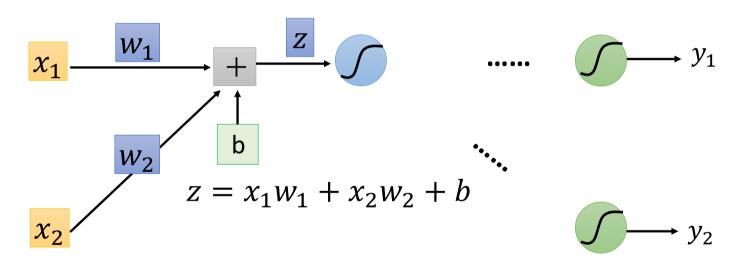
 $\overline{\partial z''}$

 $\sigma'(z)$ is a constant because z is already determined in the forward pass.

$$\frac{\partial C}{\partial z} = \sigma'(z) \left[w_3 \frac{\partial C}{\partial z'} + w_4 \frac{\partial C}{\partial z''} \right]$$

Backpropagation – Forward pass

Compute $\partial z/\partial w$ for all parameters



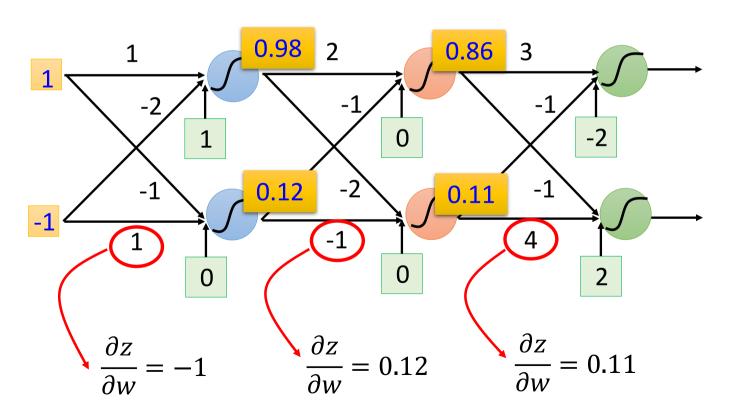
$$\frac{\partial z}{\partial w_1} = ? x_1$$

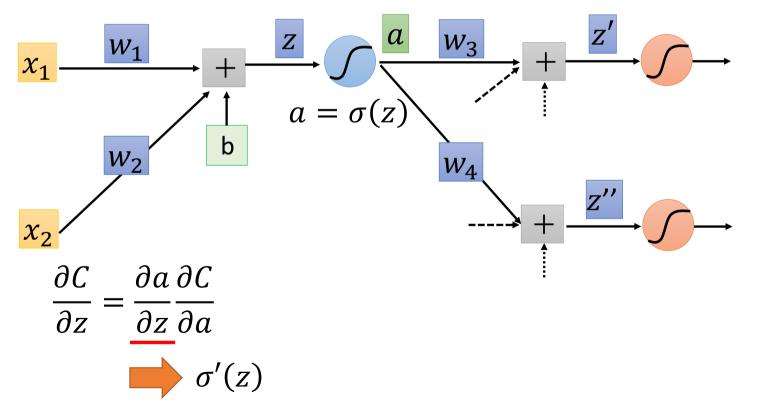
$$\frac{\partial z}{\partial w_2} = ? x_2$$

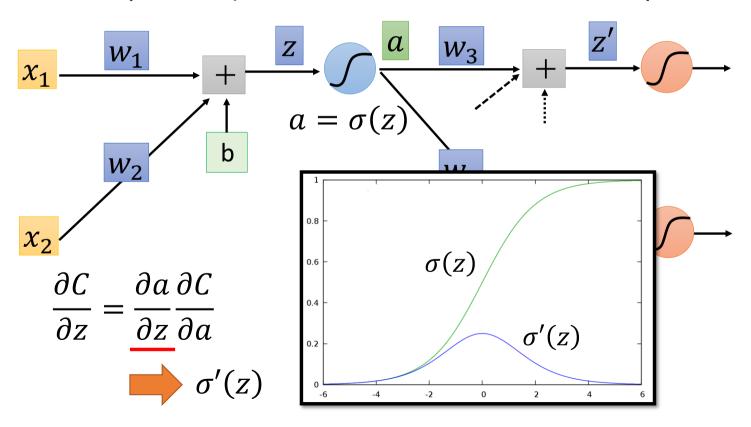
The value of the input connected by the weight

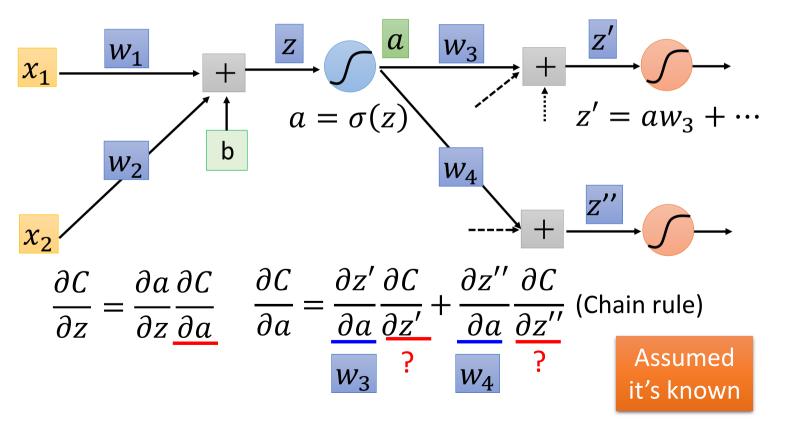
Backpropagation – Forward pass

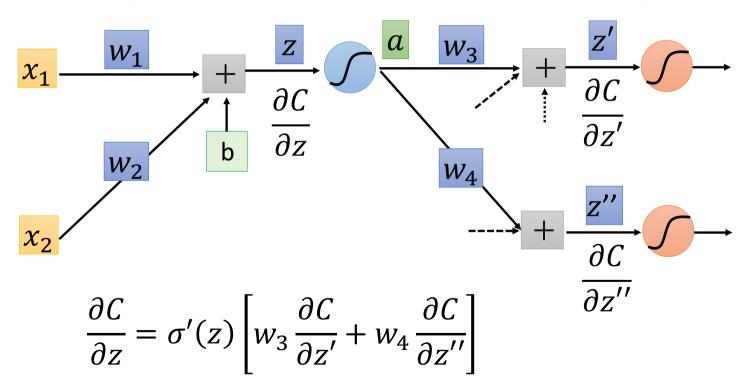
Compute $\partial z/\partial w$ for all parameters

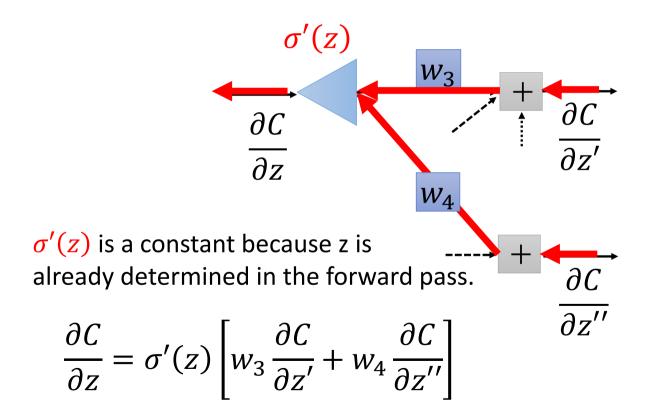


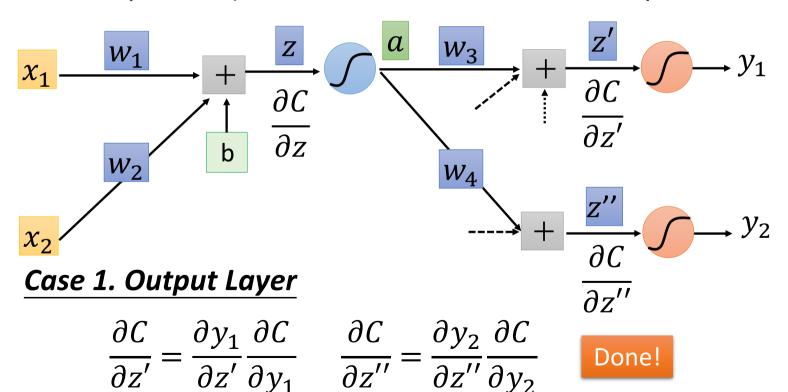






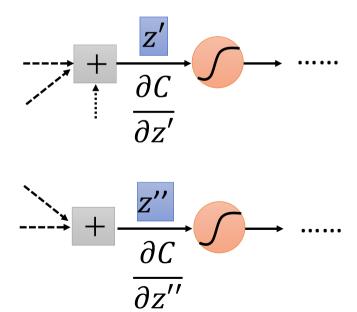






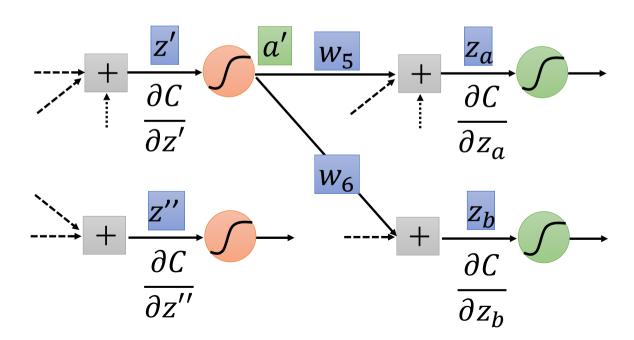
Compute $\partial C/\partial z$ for all activation function inputs z

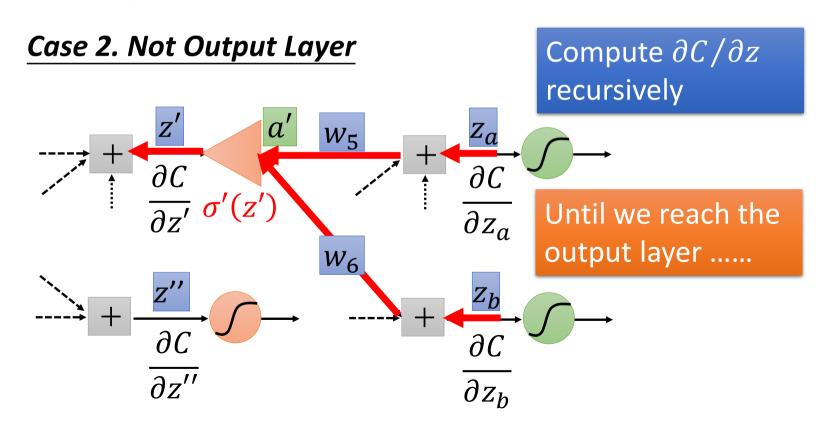
Case 2. Not Output Layer



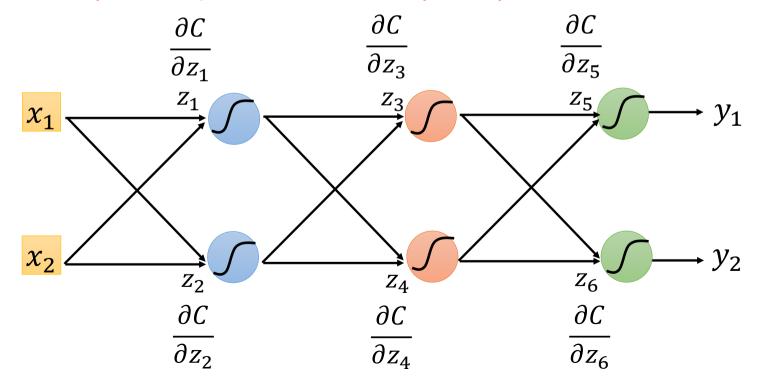
Compute $\partial C/\partial z$ for all activation function inputs z

Case 2. Not Output Layer

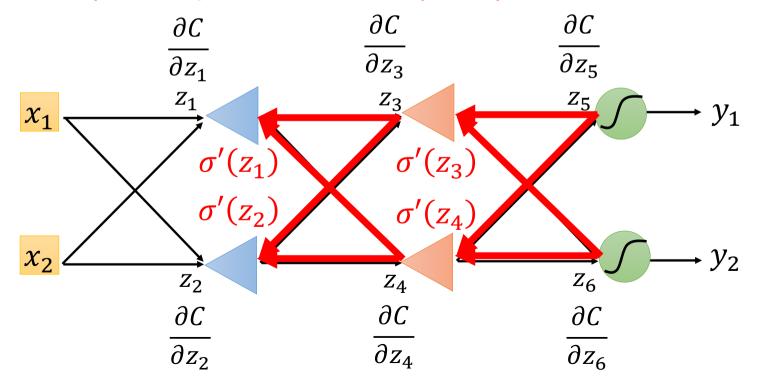




Compute $\partial C/\partial z$ for all activation function inputs z Compute $\partial C/\partial z$ from the output layer



Compute $\partial C/\partial z$ for all activation function inputs z Compute $\partial C/\partial z$ from the output layer



Backpropagation – Summary

