## Theory of Computation, Fall 2022 Assignment 7 Solutions

Q1. (20 pts) 
$$M_{\rightarrow}=(\{s,h\},\Sigma,\delta,s,\{h\}), \text{where } \delta(s,a)=(h,\rightarrow) \text{ for any } a\in\Sigma.$$

Q2. (50 pts) 
$$\begin{aligned} & M = (K, \Sigma, \delta, s, H) \\ & \bullet K = K_1 \cup K_2 \cup K_3 \cup \{h\} \\ & \bullet s = s_1 \\ & \bullet H = H_2 \cup H_3 \cup \{h\} \\ & \bullet \text{for } q \in K - H, \text{for each } c \in \Sigma \\ & \text{(i) If } q \in K_1 - H_1, \, \delta(q, c) = \delta_1(q, c) \\ & \text{(ii) If } q \in H_1, \, \delta(q, a) = (s_2, a), \delta(q, b) = (s_3, b), \delta(q, c) = (h, \to) \text{ for any } c \in \Sigma - \{a, b\} \\ & \text{(iii) If } q \in K_2 - H_2, \, \delta(q, c) = \delta_2(q, c) \\ & \text{(iiii) If } q \in K_3 - H_3, \, \delta(q, c) = \delta_3(q, c) \end{aligned}$$

Q3. (30 pts)

The Turing machine is shown as follows.

