2016-2017 学年 第二学期 《通信原理与系统》课程设计报告

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(一) 课程设计题目

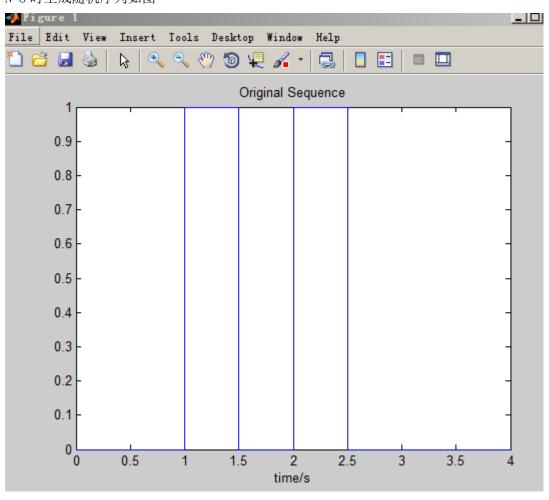
- 标准题目:选择两种波形,s1(t),s2(t),进行匹配滤波或者最优相关接收,画出各个部分的波形。
- 扩展题目:加入高斯白噪声,进行信噪比、门限对 Pe 的分析。

(二) 课程设计仿真结果与讨论

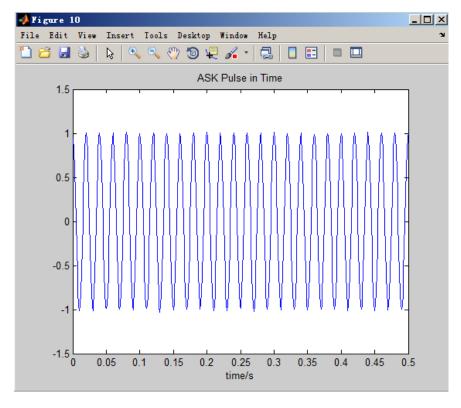
1、仿真实验

I. ASK

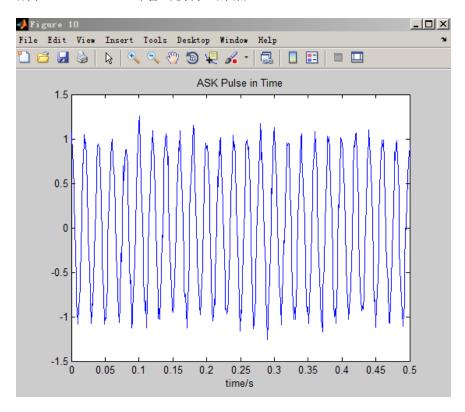
取采样频率 1000Hz,载波频率 50Hz. N 即随机序列码元数可调。为便于观察,先取 N=8 N=8 时生成随机序列如图



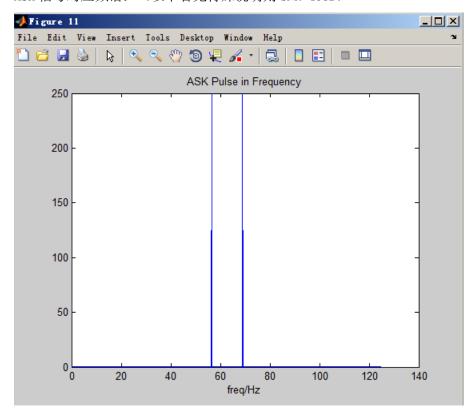
ASK 载波信号(SNR=40dB,信噪比很大,几乎看不出噪声的存在)



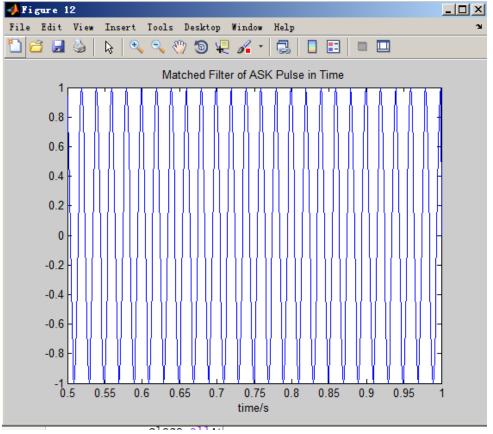
减小至 SNR=20dB, 可看出较明显的噪声

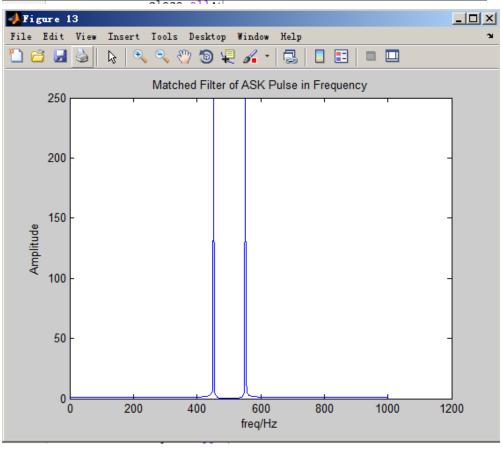


ASK 信号对应频谱: (以下若无特殊说明则 SNR=40dB)

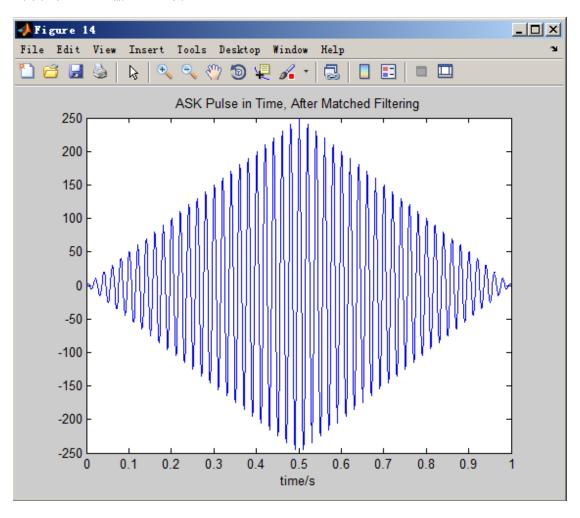


匹配滤波器的时域冲激响应函数与频谱:

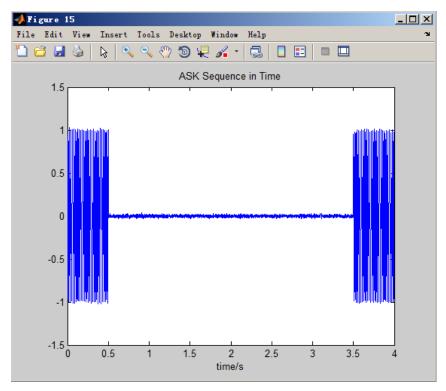




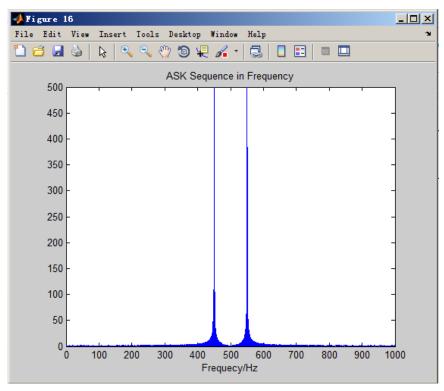
当单个脉冲通过匹配滤波器后,得到下图波形。可观察到信号幅度在 0.5s 即信号结束处达到最大值(也是输出 SNR 最大处)



对此前生成的随机序列进行调制,于是得到 ASK 序列,如图

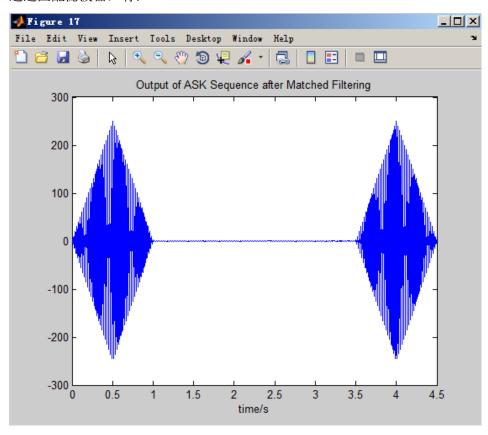


其频谱:

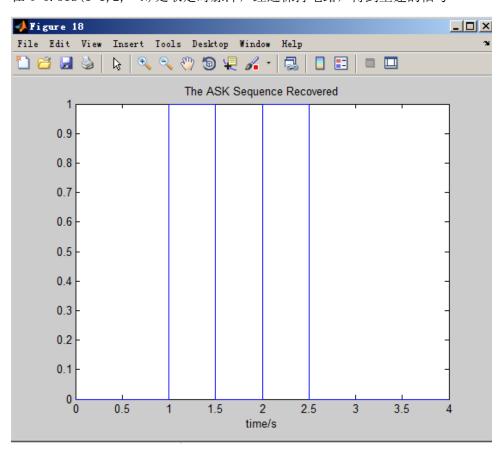


能观察到不明显的旁瓣(离散谱信号)

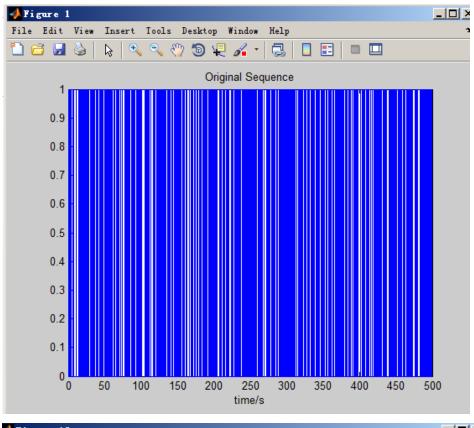
通过匹配滤波器,有:

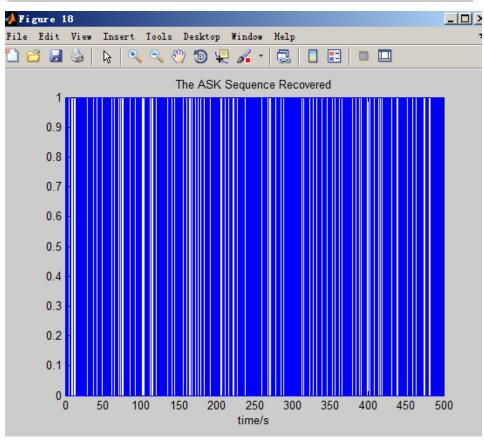


在 t=0.5is(i=1,2,···N)处取定时脉冲,经过保持电路,得到重建的信号



该信号与原信号一致。在放大到 N=1000 的序列里,依旧如此:





II. Linear Frequency Modulation

在信息对抗原理课上学到线性调频脉冲压缩(LFM)调制,常用于雷达,通过脉冲压缩调制,将长脉冲所含的大能量压缩进长度相对短的脉冲中(在雷达中意味着可以获得较大能量又能保持短脉冲的距离分辨率),获得大时宽带宽积信号,具有发射功率峰值低的优点(对于雷达而言意味着截获概率降低)。用于通信系统,可获得相对更高的信息传送速率,降低对发送机的功率要求。

线性调频脉冲信号类似 ASK 调制,包络也是宽度 τ 的矩形脉冲,但信号的载频随时间线性变化,其瞬时角频率如(1.1)

$$\omega_i = \omega_0 + \mu t \tag{1.1}$$

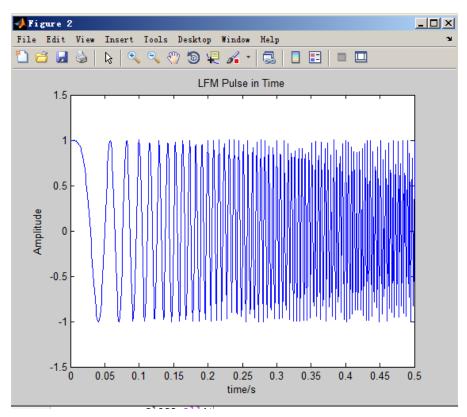
其带宽 B 的表达式如(1.2)

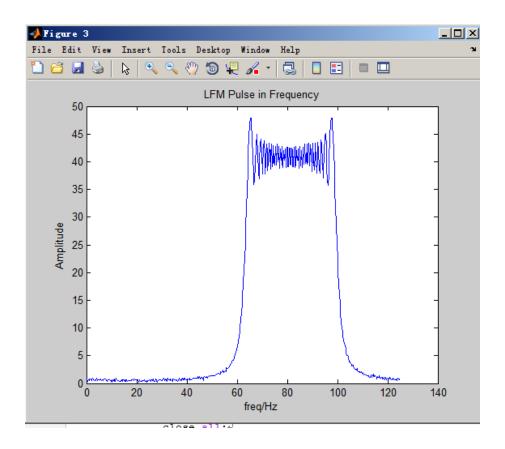
$$B = \frac{\mu \tau}{2\pi} \tag{1.2}$$

即,LFM 脉冲的时域表达式为:

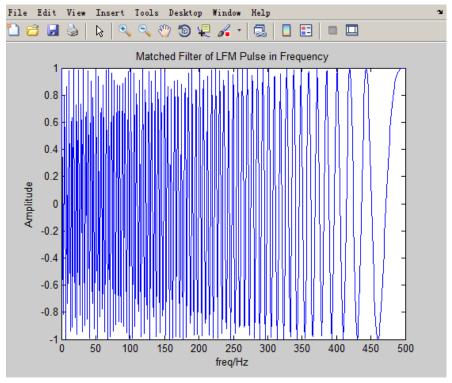
$$s(t) = Arect(\frac{t}{\tau})\cos(\omega_0 t + \frac{1}{2}\mu t^2)$$
 (1.3)

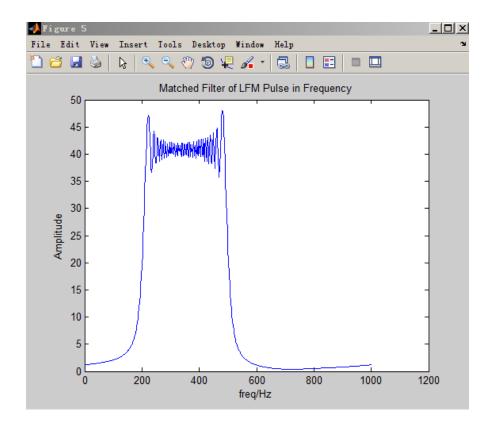
单个 LFM 脉冲的时域、频域图如下 (SNR40dB):



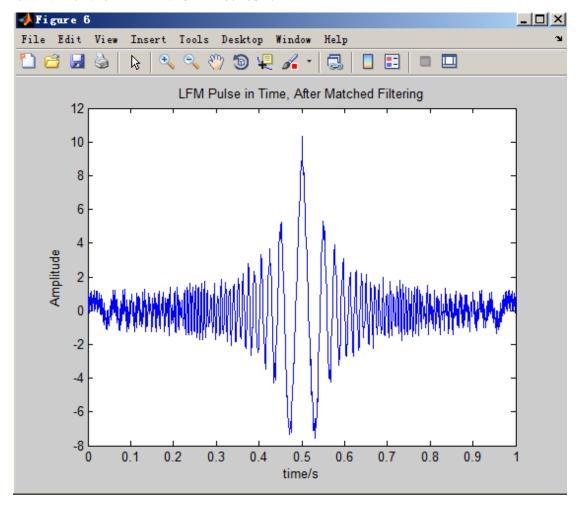


其对应的匹配滤波器时域、频域:

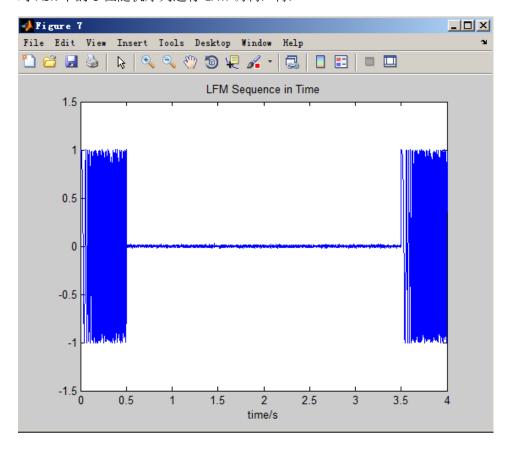




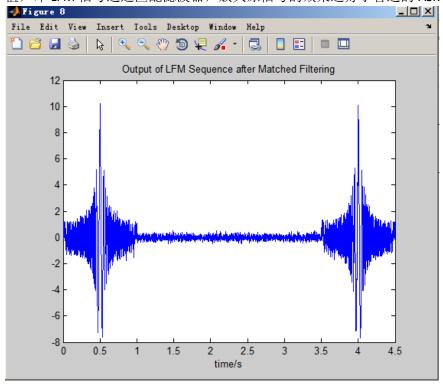
单独的一个脉冲通过匹配滤波器,得到波形:



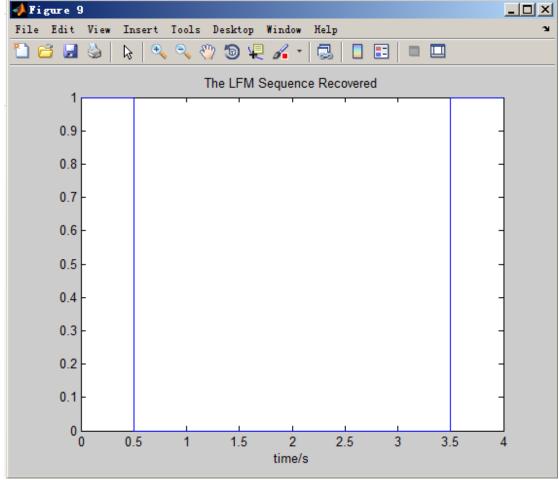
对 ASK 中的 8 位随机序列进行 LFM 调制,得:



将该信号通过匹配滤波器,得到匹配滤波后的波形如图,可观察到每个信号结束处明显的峰值,即 LFM 信号通过匹配滤波器,放大原信号的效果远好于普通的 ASK



对其进行定时脉冲抽样和保持,重建得到接收到的信号: 📣 Figure 9 File Edit View Insert Tools Desktop Window Help



与原输入信号相同。

2、仿真结果讨论

I. Pe:

在 SNR=0 时,由于没有噪声干扰, n_0 始终=0,所以不论 ASK 或 LFM,由 (1.4) 计算出来的 Pe 都等于0,解调出的码型一定等于原码型。

$$P_e = \frac{1}{2} \operatorname{erfc}(\sqrt{\frac{E(1-\rho)}{2n_0}})$$
 (1.4)

在有噪声干扰时,运行程序(取 N=1000, SNR=40dB),有:

ThresholdLFM =

PeLFM =

0

ThresholdASK =

5.0619

PeASK =

3.8721e-06

可见,同为对原信号进行幅度上的调制(1 为脉冲, 0 为无信号)LFM 的绝对阈值较高(但归一化阈值取的是相同的)。由于初始设置的 SNR 较小(40dB),二者皆有很小的 Pe, 而 LFM 更佳。调整初始设置的 SNR 至 20dB, 得二者误码率

PeLFM =

PeASK =

7.8270e-04

依旧可见,LFM 的误码率优于 ASK-但随着输入的 SNR 减小,二者输出的误码率均有增大。说明噪声可以增大误码率,故在实际通信中应尽量提高解调器输入端的 SNR 以减少差错。

II. 关于匹配滤波:

观察 ASK, FSK 的单脉冲波形,可见,匹配滤波器 $h(t) = K \times s(t_0 - t)$ 可以实现使输入信号在 t_0 处达到最大值,且此最大值数倍于输入信号本身的幅度,换言之,匹配滤波可以在很大程 度上改善接收机的信噪比。但它会使输入信号波形产生严重失真。

附: 源程序代码

close all;

PulseDuration=0.5;% 0.5s per code element fs=1000;%Sampling Frequency: 1000 points/s fc=50;%Carrier Frequency. Due to Nyquist Theroem,fc<500Hz SNR=40;%SNR in dB numCodeElement=PulseDuration*fs;%Number of samples within a pulse N=8;%Length of Random Sequence K=1;%Coefficient of the matched filter

TimeDuration=PulseDuration*N;%Total Time Duration
nofPulseDuration=1:PulseDuration*fs;%n sequence of a pulse
nofTimeDuration=1:TimeDuration*fs;%n sequence of the whole plot

% Random Sequence Generation: a random sequence with the length of N Gate=0.5;% threshold of the sequence. In this Sequence P(0)=Gate, P(1)=1-Gate)

```
OriginalSignal=unifrnd(0,1,1,N);
Sequence=ones(1,N);
for n=1:N
   if OriginalSignal(n)>=Gate
      Sequence (n) = 1;
   else
      Sequence (n) = 0;
   end
end
SignalSource=rectpulse(Sequence,numCodeElement); %%Rectangular pulse
shaping, with numCodeElement(PulseDuration*fs) samples per pulse
plot(nofTimeDuration/fs,SignalSource);
title('Original Sequence');
xlabel('time/s');
%%%%% Linear Frequency Modulation
a=1;%Amplitude of LFM Pulse
B=0.3; %Bandwidth of the LFM pulse
miu=B/(2*length(nofPulseDuration));
lfm=a*exp(j*(2*pi*fc*nofPulseDuration+2*pi*miu*nofPulseDuration.*nofP
ulseDuration));% LFM of a pulse
lfmwithNoise=awqn(lfm,SNR); %with White Gaussian Noise added
figure,plot(nofPulseDuration/fs,real(lfmwithNoise));%a Linear
Frequency Modulation (LFM) pulse in time
title('LFM Pulse in Time');
xlabel('time/s');ylabel('Amplitude');
LFM=fftshift(fft(lfmwithNoise)); % LFM pulse in Frequency
figure, plot (nofPulseDuration/TimeDuration, abs (LFM));
title('LFM Pulse in Frequency');
xlabel('freq/Hz');ylabel('Amplitude');
% Matched filter of LFM
nTimeDelay=1;
nt0=nTimeDelay+length(lfm);
nofMatchedFilter=nt0-nofPulseDuration;
hLFM=K*lfm(nofMatchedFilter); %reversed part of the matched filter
hLFM=[zeros(1,nTimeDelay) hLFM]; % matched filter with a beginning of a
delay of TimeDelay/fs
figure, plot(linspace(1, PulseDuration, length(hLFM)), real(hLFM)); % match
ed filter in time
title('Matched Filter of LFM Pulse in Time');
xlabel('time/s');ylabel('Amplitude');
```

```
HLFM=fftshift(fft(hLFM));
figure,plot((1:length(HLFM))/PulseDuration,abs(HLFM));%matched filter
in frequency
% n transforming into w (or f?): frequency=n*(2pi/N)*(fs/2pi),
N=TimeDuration*fs
title('Matched Filter of LFM Pulse in Frequency');
xlabel('freq/Hz');ylabel('Amplitude');
%Signal output of one pulse, after matched filtering
yLFM=conv(hLFM,lfmwithNoise);
tofyLFM=1:length(yLFM);
figure,plot(tofyLFM/fs,real(yLFM));%Signal output in time
title('LFM Pulse in Time, After Matched Filtering');
xlabel('time/s');ylabel('Amplitude');
%Linear phase modulation of the random sequence given above
SignalmodulatedbyLFM=zeros(1,TimeDuration*fs);
   for n1=0:(N-1)
       for n2=1:(PulseDuration*fs)
SignalmodulatedbyLFM(PulseDuration*fs*n1+n2)=SignalSource(PulseDurati
on*fs*n1+n2)*lfm(n2);
      end
   end
SignalmodulatedbyLFM=awgn(SignalmodulatedbyLFM,SNR);
figure,plot(nofTimeDuration/fs,real(SignalmodulatedbyLFM));
title('LFM Sequence in Time');
xlabel('time/s');
%LFM modulated signal passing through its corresponding matched filter
ySignalmodulatedbyLFM=conv(SignalmodulatedbyLFM, hLFM);
nofySignalmodulatedbyLFM=1:length(ySignalmodulatedbyLFM);
figure,plot(nofySignalmodulatedbyLFM/fs,real(ySignalmodulatedbyLFM));
title('Output of LFM Sequence after Matched Filtering');
xlabel('time/s');
%Recovery
ThresholdLFM=(0.5*a+a/(2*SNR)*log((1-Gate)/Gate))*max(ySignalmodulate)
dbyLFM)
tofRecovery=1:N;
LFMRecovery=zeros(1,N);
for Samples=1:N
LFMRecovery(Samples) = ySignalmodulatedbyLFM(PulseDuration*fs*Samples);
```

```
if LFMRecovery(Samples)>ThresholdLFM
      LFMRecovery (Samples) =1;
   else
      LFMRecovery(Samples)=0;
   end
end
LFMRecovered=rectpulse(LFMRecovery, numCodeElement);
figure,plot(nofTimeDuration/fs,LFMRecovered)
title('The LFM Sequence Recovered')
xlabel('time/s')
sumoflfm=0;
for n=1:length(lfm)
   sumoflem=sumoflem+real(lem(n))*real(lem(n));
end
N0=sumoflfm/(10.^(SNR/10));
SNRLFM=2*0.5*a*a*PulseDuration*fs/N0;
PeLFM=0.5*erfc(sqrt(SNRLFM/4))
% ASK
a=1; %Amplitude of ASK=1;
carrier=a*cos(2*pi*fc*nofPulseDuration/fs);% the carrier signal of ASK
carrierwithNoise=awqn(carrier, SNR); % with White Gaussian Noise added
figure,plot(nofPulseDuration/fs,real(carrierwithNoise)); % an ASK pulse
in time
title('ASK Pulse in Time');
xlabel('time/s');
ASKPulse=fftshift(fft(carrierwithNoise)); %LFM pulse in Frequency
figure, plot (nofPulseDuration/TimeDuration, abs (ASKPulse));
title('ASK Pulse in Frequency');
xlabel('freq/Hz');
% Matched filter
nTimeDelay=1;
nt0=nTimeDelay+length(carrier);
nofMatchedFilterASK=nt0-nofPulseDuration;
hASK=K*carrier(nofMatchedFilterASK); %reversed part of the matched filter
hASK=[zeros(1,nTimeDelay) hASK]; % matched filter with a beginning of a
delay of TimeDelay/fs
figure, plot(linspace(1, PulseDuration, length(hASK)), real(hASK)); % match
ed filter in time
title('Matched Filter of ASK Pulse in Time');
xlabel('time/s');
```

```
HASK=fftshift(fft(hASK));
figure,plot((1:length(HASK))/PulseDuration,abs(HASK));%matched filter
in frequency
% n transforming into w (or f?): frequency=n*(2pi/N)*(fs/2pi),
N=TimeDuration*fs
title('Matched Filter of ASK Pulse in Frequency');
xlabel('freq/Hz');ylabel('Amplitude');
%Signal output of one pulse, after matched filtering
yASK=conv(hASK, carrierwithNoise);
tofyASK=1:length(yASK);
figure,plot(tofyASK/fs,real(yASK));%Signal output in time
title('ASK Pulse in Time, After Matched Filtering');
xlabel('time/s');
SignalModulatedbyASK=zeros(1,TimeDuration*fs);
   for n1=0:(N-1)
      for n2=1:(PulseDuration*fs)
SignalModulatedbyASK(PulseDuration*fs*n1+n2)=SignalSource(PulseDurati
on*fs*n1+n2)*carrier(n2);
      end
   end
SignalModulatedbyASK=awgn(SignalModulatedbyASK,SNR);
figure,plot(nofTimeDuration/fs,real(SignalModulatedbyASK));
title('ASK Sequence in Time');
xlabel('time/s');
SIGNALASK=fftshift(fft(SignalModulatedbyASK));
figure, plot (nofTimeDuration/TimeDuration, abs (SIGNALASK));
title('ASK Sequence in Frequency');
xlabel('Frequecy/Hz');
%ASK modulated signal passing through its corresponding matched filter
ySignalmodulatedbyASK=conv(SignalModulatedbyASK, hASK);
nofySignalmodulatedbyASK=1:length(ySignalmodulatedbyASK);
figure,plot(nofySignalmodulatedbyASK/fs,real(ySignalmodulatedbyASK));
title('Output of ASK Sequence after Matched Filtering');
xlabel('time/s');
%Recovery of ASK Signal
ThresholdASK=(0.5*a+a/(2*SNR)*log((1-Gate)/Gate))*max(ySignalmodulate)
dbyASK)
```

```
tofRecovery=1:N;
ASKRecovery=zeros(1,N);
for Samples=1:N
ASKRecovery(Samples) = ySignalmodulatedbyASK(PulseDuration*fs*Samples);
   if ASKRecovery(Samples)>ThresholdASK
      ASKRecovery(Samples)=1;
   else
      ASKRecovery(Samples)=0;
   end
end
ASKRecovered=rectpulse(ASKRecovery,numCodeElement);
figure, plot (nofTimeDuration/fs, ASKRecovered)
title('The ASK Sequence Recovered')
xlabel('time/s')
PeASK=0.5*erfc(sqrt(SNR/4))
close all;
PulseDuration=0.5;% 0.5s per code element
fs=1000; %Sampling Frequency: 1000 points/s
fc=50; %Carrier Frequency. Due to Nyquist Theroem, fc<500Hz
SNR=40;%SNR in dB
numCodeElement=PulseDuration*fs;%Number of samples within a pulse
N=8; %Length of Random Sequence
K=1; %Coefficient of the matched filter
TimeDuration=PulseDuration*N;%Total Time Duration
nofPulseDuration=1:PulseDuration*fs;%n sequence of a pulse
nofTimeDuration=1:TimeDuration*fs;%n sequence of the whole plot
% Random Sequence Generation: a random sequence with the length of N
Gate=0.5; threshold of the sequence. In this Sequence P(0)=Gate,
P(1)=1-Gate
OriginalSignal=unifrnd(0,1,1,N);
Sequence=ones(1,N);
for n=1:N
   if OriginalSignal(n)>=Gate
      Sequence (n) = 1;
      Sequence (n) = 0;
   end
SignalSource=rectpulse(Sequence,numCodeElement);%%Rectangular pulse
```

```
shaping, with numCodeElement(PulseDuration*fs) samples per pulse
plot(nofTimeDuration/fs, SignalSource);
title('Original Sequence');
xlabel('time/s');
%%%%% Linear Frequency Modulation
a=1;%Amplitude of LFM Pulse
B=0.3; %Bandwidth of the LFM pulse
miu=B/(2*length(nofPulseDuration));
lfm=a*exp(j*(2*pi*fc*nofPulseDuration+2*pi*miu*nofPulseDuration.*nofP
ulseDuration));% LFM of a pulse
lfmwithNoise=awgn(lfm,SNR); %with White Gaussian Noise added
figure,plot(nofPulseDuration/fs,real(lfmwithNoise));%a Linear
Frequency Modulation (LFM) pulse in time
title('LFM Pulse in Time');
xlabel('time/s');ylabel('Amplitude');
LFM=fftshift(fft(lfmwithNoise));%LFM pulse in Frequency
figure, plot (nofPulseDuration/TimeDuration, abs (LFM));
title('LFM Pulse in Frequency');
xlabel('freq/Hz');ylabel('Amplitude');
% Matched filter of LFM
nTimeDelay=1;
nt0=nTimeDelay+length(lfm);
nofMatchedFilter=1:length(lfm);
nofMatchedFilter=nt0-nofPulseDuration;
hLFM=K*lfm(nofMatchedFilter); %reversed part of the matched filter
hLFM=[zeros(1,nTimeDelay) hLFM]; % matched filter with a beginning of a
delay of TimeDelay/fs
figure,plot(linspace(1,PulseDuration,length(hLFM)),real(fliplr((hLFM)
)));
title('Matched Filter of LFM Pulse in Time');
xlabel('time/s');ylabel('Amplitude');
HLFM=fftshift(fft(hLFM));
figure, plot((1:length(HLFM))/PulseDuration, abs(HLFM)); %matched filter
in frequency
% n transforming into w (or f?): frequency=n*(2pi/N)*(fs/2pi),
N=TimeDuration*fs
title('Matched Filter of LFM Pulse in Frequency');
xlabel('freq/Hz');ylabel('Amplitude');
%Signal output of one pulse, after matched filtering
```

```
yLFM=conv(hLFM,lfmwithNoise);
tofyLFM=1:length(yLFM);
figure,plot(tofyLFM/fs,real(yLFM));%Signal output in time
title('LFM Pulse in Time, After Matched Filtering');
xlabel('time/s');ylabel('Amplitude');
%Linear phase modulation of the random sequence given above
SignalmodulatedbyLFM=zeros(1,TimeDuration*fs);
        for n1=0:(N-1)
                for n2=1:(PulseDuration*fs)
{\tt Signal modulated by LFM (Pulse Duration*fs*n1+n2) = Signal Source (
on*fs*n1+n2)*lfm(n2);
                end
        end
SignalmodulatedbyLFM=awgn(SignalmodulatedbyLFM,SNR);
figure,plot(nofTimeDuration/fs,real(SignalmodulatedbyLFM));
title('LFM Sequence in Time');
xlabel('time/s');
%LFM modulated signal passing through its corresponding matched filter
ySignalmodulatedbyLFM=conv(SignalmodulatedbyLFM, hLFM);
nofySignalmodulatedbyLFM=1:length(ySignalmodulatedbyLFM);
figure,plot(nofySignalmodulatedbyLFM/fs,real(ySignalmodulatedbyLFM));
title('Output of LFM Sequence after Matched Filtering');
xlabel('time/s');
%Recovery
ThresholdLFM=abs((0.5*a+a/(2*SNR)*log((1-Gate)/Gate))*max(ySignalmodu
latedbyLFM))
tofRecovery=1:N;
LFMRecovery=zeros(1,N);
for Samples=1:N
LFMRecovery(Samples) = ySignalmodulatedbyLFM(PulseDuration*fs*Samples);
        if LFMRecovery(Samples)>ThresholdLFM
                LFMRecovery(Samples)=1;
        else
                LFMRecovery(Samples)=0;
        end
end
LFMRecovered=rectpulse(LFMRecovery, numCodeElement);
figure,plot(nofTimeDuration/fs,LFMRecovered)
title('The LFM Sequence Recovered')
```

```
xlabel('time/s')
sumoflfm=0;
for n=1:length(lfm)
   sumoflem=sumoflem+real(lem(n))*real(lem(n));
N0=sumoflfm/(10.^(SNR/10));
SNRLFM=2*0.5*a*a*PulseDuration*fs/N0;
PeLFM=0.5*erfc(sqrt(SNRLFM/4))
a=1;%Amplitude of ASK=1;
carrier=a*cos(2*pi*fc*nofPulseDuration/fs);% the carrier signal of ASK
carrierwithNoise=awgn(carrier, SNR); % with White Gaussian Noise added
figure,plot(nofPulseDuration/fs,real(carrierwithNoise)); % an ASK pulse
in time
title('ASK Pulse in Time');
xlabel('time/s');
ASKPulse=fftshift(fft(carrierwithNoise)); %LFM pulse in Frequency
figure, plot (nofPulseDuration/TimeDuration, abs (ASKPulse));
title('ASK Pulse in Frequency');
xlabel('freq/Hz');
%%%Matched filter
nTimeDelay=1;
nt0=nTimeDelay+length(carrier);
nofMatchedFilterASK=nt0-nofPulseDuration;
hASK=K*carrier(nofMatchedFilterASK); %reversed part of the matched filter
hASK=[zeros(1,nTimeDelay) hASK]; % matched filter with a beginning of a
delay of TimeDelay/fs
figure, plot(linspace(1, PulseDuration, length(hASK)), real(hASK)); % match
ed filter in time
title('Matched Filter of ASK Pulse in Time');
xlabel('time/s');
HASK=fftshift(fft(hASK));
figure, plot((1:length(HASK))/PulseDuration, abs(HASK)); % matched filter
in frequency
%n transforming into w (or f?): frequency=n*(2pi/N)*(fs/2pi),
N=TimeDuration*fs
title('Matched Filter of ASK Pulse in Frequency');
xlabel('freq/Hz');ylabel('Amplitude');
%Signal output of one pulse, after matched filtering
```

```
yASK=conv(hASK, carrierwithNoise);
tofyASK=1:length(yASK);
figure,plot(tofyASK/fs,real(yASK));%Signal output in time
title('ASK Pulse in Time, After Matched Filtering');
xlabel('time/s');
SignalModulatedbyASK=zeros(1,TimeDuration*fs);
   for n1=0:(N-1)
      for n2=1:(PulseDuration*fs)
SignalModulatedbyASK(PulseDuration*fs*n1+n2)=SignalSource(PulseDurati
on*fs*n1+n2)*carrier(n2);
      end
   end
SignalModulatedbyASK=awgn(SignalModulatedbyASK,SNR);
figure,plot(nofTimeDuration/fs, real(SignalModulatedbyASK));
title('ASK Sequence in Time');
xlabel('time/s');
SIGNALASK=fftshift(fft(SignalModulatedbyASK));
figure, plot (nofTimeDuration/TimeDuration, abs (SIGNALASK));
title('ASK Sequence in Frequency');
xlabel('Frequecy/Hz');
%%%ASK modulated signal passing through its corresponding matched filter
ySignalmodulatedbyASK=conv(SignalModulatedbyASK, hASK);
nofySignalmodulatedbyASK=1:length(ySignalmodulatedbyASK);
figure,plot(nofySignalmodulatedbyASK/fs,real(ySignalmodulatedbyASK));
title('Output of ASK Sequence after Matched Filtering');
xlabel('time/s');
%%%Recovery of ASK Signal
ThresholdASK=(0.5*a+a/(2*SNR)*log((1-Gate)/Gate))*max(ySignalmodulate)
dbyASK)
tofRecovery=1:N;
ASKRecovery=zeros(1,N);
for Samples=1:N
ASKRecovery(Samples) = ySignalmodulatedbyASK(PulseDuration*fs*Samples);
   if ASKRecovery(Samples)>ThresholdASK
      ASKRecovery(Samples)=1;
   else
      ASKRecovery(Samples)=0;
   end
```

end

```
ASKRecovered=rectpulse(ASKRecovery, numCodeElement);
figure,plot(nofTimeDuration/fs, ASKRecovered)
title('The ASK Sequence Recovered')
xlabel('time/s')
%
% sumofask=0;
% for n=1:length(lfm)
% sumofask=sumofask+real(ask(n))*real(ask(n));
% end
% NO=sumofask/(10.^(SNR/10));
PeASK=0.5*erfc(sqrt(SNR/4))
```