

✔ Congratulations! You passed!

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1. Suppose a MAC system (S, V) is used to protect files in a file system

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by appending a MAC tag to each file. The MAC signing algorithm S is applied to the file contents and nothing else. What tampering attacks are not prevented by this system?

- ☒ Changing the last modification time of a file.
- ☐ Replacing the contents of a file with the concatenation of two files on the file system.
- ☐ Changing the first byte of the file contents.
- ☐ Replacing the tag and contents of one file with the tag and contents of a file from another computer protected by the same MAC system, but a different key.

✔ Correct

The MAC signing algorithm is only applied to the file contents and does not protect the file meta data.

2. Let (S, V) be a secure MAC defined over (K, M, T) where $M = \{0, 1\}^n$ and $T = \{0, 1\}^{128}$. That is, the key space is K , message space is $\{0, 1\}^n$, and tag space is $\{0, 1\}^{128}$.

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Which of the following is a secure MAC: (as usual, we use \parallel to denote string concatenation)

- ☐ $S'(k, m) = S(k, m[0, \dots, n-2] \parallel 0)$ and
 $V'(k, m, t) = V(k, m[0, \dots, n-2] \parallel 0, t)$
- ☒ $S'(k, m) = S(k, m \parallel m)$ and
 $V'(k, m, t) = V(k, m \parallel m, t)$.

✔ Correct

a forger for (S', V') gives a forger for (S, V) .

- ☒ $S'((k_1, k_2), m) = (S(k_1, m), S(k_2, m))$ and
 $V'((k_1, k_2), m, (t_1, t_2)) = [V(k_1, m, t_1) \text{ and } V(k_2, m, t_2)]$
(i.e., $V'((k_1, k_2), m, (t_1, t_2))$ outputs "1" if both t_1 and t_2 are valid tags)

✓ **Correct**

a forger for (S', V') gives a forger for (S, V) .

☐ $S'(k, m) = S(k, m)$ and

$$V'(k, m, t) = \begin{cases} V(k, m, t) & \text{if } m \neq 0^n \\ "1" & \text{otherwise} \end{cases}$$

☒ $S'(k, m) = [t \leftarrow S(k, m), \text{output } (t, t)]$ and

$$V'(k, m, (t_1, t_2)) = \begin{cases} V(k, m, t_1) & \text{if } t_1 = t_2 \\ "0" & \text{otherwise} \end{cases}$$

(i.e., $V'(k, m, (t_1, t_2))$ only outputs "1"

if t_1 and t_2 are equal and valid)

✓ **Correct**

a forger for (S', V') gives a forger for (S, V) .

☐ $S'(k, m) = S(k, m \oplus m)$ and

$$V'(k, m, t) = V(k, m \oplus m, t)$$

3. Recall that the ECBC-MAC uses a fixed IV (in the lecture we simply set the IV to 0).

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Suppose instead we chose a random IV for every message being signed and include the IV in the tag. In other words, $S(k, m) := (r, \text{ECBC}_r(k, m))$

where $\text{ECBC}_r(k, m)$ refers to the ECBC function using r as

the IV. The verification algorithm V given key k , message m ,

and tag (r, t) outputs "1" if $t = \text{ECBC}_r(k, m)$ and outputs

"0" otherwise.

The resulting MAC system is insecure.

An attacker can query for the tag of the 1-block message m

and obtain the tag (r, t) . He can then generate the following

existential forgery: (we assume that the underlying block cipher operates on n -bit blocks)

☒ The tag $(r \oplus m, t)$ is a valid tag for the 1-block message 0^n .

☐ The tag $(r \oplus t, r)$ is a valid tag for the 1-block message 0^n .

☐ The tag $(m \oplus t, r)$ is a valid tag for the 1-block message 0^n .

☐ The tag $(r, t \oplus r)$ is a valid tag for the 1-block message 0^n .

✓ **Correct**

The CBC chain initiated with the IV $r \oplus m$ and applied

to the message 0^n will produce exactly the same output as the CBC chain initiated with the IV r and applied to the message m . Therefore, the tag $(r \oplus m, t)$ is a valid existential forgery for the message 0 .

4. Suppose Alice is broadcasting packets to 6 recipients

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B_1, \dots, B_6 . Privacy is not important but integrity is.

In other words, each of B_1, \dots, B_6 should be assured that the packets he is receiving were sent by Alice.

Alice decides to use a MAC. Suppose Alice and B_1, \dots, B_6 all share a secret key k . Alice computes a tag for every packet she sends using key k . Each user B_i verifies the tag when receiving the packet and drops the packet if the tag is invalid.

Alice notices that this scheme is insecure because user B_1 can use the key k to send packets with a valid tag to users B_2, \dots, B_6 and they will all be fooled into thinking that these packets are from Alice.

Instead, Alice sets up a set of 4 secret keys $S = \{k_1, \dots, k_4\}$.

She gives each user B_i some subset $S_i \subseteq S$ of the keys. When Alice transmits a packet she appends 4 tags to it by computing the tag with each of her 4 keys. When user B_i receives a packet he accepts it as valid only if all tags corresponding

to his keys in S_i are valid. For example, if user B_1 is given keys $\{k_1, k_2\}$ he will accept an incoming packet only if the first and second tags are valid. Note that B_1 cannot validate the 3rd and 4th tags because he does not have k_3 or k_4 .

How should Alice assign keys to the 6 users so that no single user can forge packets on behalf of Alice and fool some other user?

☒ $S_1 = \{k_1, k_2\}, S_2 = \{k_1, k_3\}, S_3 = \{k_1, k_4\}, S_4 = \{k_2, k_3\}, S_5 = \{k_2, k_4\}, S_6 = \{k_3, k_4\}$

☒ Correct

Every user can only generate tags with the two keys he has.

Since no set S_i is contained in another set S_j , no user i can fool a user j into accepting a message sent by i .

- ☐ $S_1 = \{k_1, k_2\}, S_2 = \{k_1, k_3\}, S_3 = \{k_1, k_4\}, S_4 = \{k_2, k_3, k_4\}, S_5 = \{k_2, k_3\}, S_6 = \{k_3, k_4\}$
- ☐ $S_1 = \{k_1, k_2\}, S_2 = \{k_1, k_3, k_4\}, S_3 = \{k_1, k_4\}, S_4 = \{k_2, k_3\}, S_5 = \{k_2, k_3, k_4\}, S_6 = \{k_3, k_4\}$
- ☐ $S_1 = \{k_1, k_2\}, S_2 = \{k_2, k_3\}, S_3 = \{k_3, k_4\}, S_4 = \{k_1, k_3\}, S_5 = \{k_1, k_2\}, S_6 = \{k_1, k_4\}$

5. Consider the encrypted CBC MAC built from AES. Suppose we

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compute the tag for a long message m comprising of n AES blocks.

Let m' be the n -block message obtained from m by flipping the

last bit of m (i.e. if the last bit of m is b then the last bit

of m' is $b \oplus 1$). How many calls to AES would it take

to compute the tag for m' from the tag for m and the MAC key? (in this question please ignore message padding and simply assume that the message length is always a multiple of the AES block size)

☐ n

☒ 4

☐ 5

☐ 6

☒ Correct

You would decrypt the final CBC MAC encryption step done using k_2 ,

the decrypt the last CBC MAC encryption step done using k_1 ,

flip the last bit of the result, and re-apply the two encryptions.

6. Let $H : M \rightarrow T$ be a collision resistant hash function.

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Which of the following is collision resistant:

(as usual, we use \parallel to denote string concatenation)

☐ $H'(m) = H(m)[0, \dots, 31]$

(i.e. output the first 32 bits of the hash)

☐ $H'(m) = H(m) \oplus H(m)$

☒ $H'(m) = H(H(m))$

☒ Correct

a collision finder for H' gives a collision finder for H .

☐ $H'(m) = H(0)$

☒ $H'(m) = H(m \parallel m)$

☒ **Correct**

a collision finder for H' gives a collision finder for H .

☒ $H'(m) = H(m) \parallel H(0)$

☒ **Correct**

a collision finder for H' gives a collision finder for H .

☐ $H'(m) = H(m) \oplus H(m \oplus 1^{|m|})$

(where $m \oplus 1^{|m|}$ is the complement of m)

7. Suppose H_1 and H_2 are collision resistant

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hash functions mapping inputs in a set M to $\{0, 1\}^{256}$.

Our goal is to show that the function $H_2(H_1(m))$ is also

collision resistant. We prove the contra-positive:

suppose $H_2(H_1(\cdot))$ is not collision resistant, that is, we are

given $x \neq y$ such that $H_2(H_1(x)) = H_2(H_1(y))$.

We build a collision for either H_1 or for H_2 .

This will prove that if H_1 and H_2 are collision resistant

then so is $H_2(H_1(\cdot))$. Which of the following must be true:

☒ Either x, y are a collision for H_1 or

$H_1(x), H_1(y)$ are a collision for H_2 .

☐ Either $x, H_1(y)$ are a collision for H_2 or

$H_2(x), y$ are a collision for H_1 .

☐ Either x, y are a collision for H_2 or

$H_1(x), H_1(y)$ are a collision for H_1 .

☐ Either $H_2(x), H_2(y)$ are a collision for H_1 or

x, y are a collision for H_2 .

☒ **Correct**

If $H_2(H_1(x)) = H_2(H_1(y))$ then

either $H_1(x) = H_1(y)$ and $x \neq y$, thereby giving us

a collision on H_1 . Or $H_1(x) \neq H_1(y)$ but

$H_2(H_1(x)) = H_2(H_1(y))$ giving us a collision on H_2 .

Either way we obtain a collision on H_1 or H_2 as required.

8. In this question you are asked to find a collision for the compression function:

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$$f_1(x, y) = \text{AES}(y, x) \oplus y,$$

where $\text{AES}(x, y)$ is the AES-128 encryption of y under key x .

Your goal is to find two distinct pairs (x_1, y_1) and (x_2, y_2) such that $f_1(x_1, y_1) = f_1(x_2, y_2)$.

Which of the following methods finds the required (x_1, y_1) and (x_2, y_2) ?

☐ Choose x_1, y_1, x_2 arbitrarily (with $x_1 \neq x_2$) and let $v := \text{AES}(y_1, x_1)$.

$$\text{Set } y_2 = \text{AES}^{-1}(x_2, v \oplus y_1 \oplus x_2)$$

☐ Choose x_1, y_1, y_2 arbitrarily (with $y_1 \neq y_2$) and let $v := \text{AES}(y_1, x_1)$.

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☐ Choose x_1, y_1, y_2 arbitrarily (with $y_1 \neq y_2$) and let $v := \text{AES}(y_1, x_1)$.

$$\text{Set } x_2 = \text{AES}^{-1}(y_2, v \oplus y_2)$$

☒ **Correct**

You got it !

9. Repeat the previous question, but now to find a collision for the compression function $f_2(x, y) = \text{AES}(x, x) \oplus y$.

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Which of the following methods finds the required (x_1, y_1) and (x_2, y_2) ?

☒ Choose x_1, x_2, y_1 arbitrarily (with $x_1 \neq x_2$) and set

$$y_2 = y_1 \oplus \text{AES}(x_1, x_1) \oplus \text{AES}(x_2, x_2)$$

☐ Choose x_1, x_2, y_1 arbitrarily (with $x_1 \neq x_2$) and set

$$y_2 = \text{AES}(x_1, x_1) \oplus \text{AES}(x_2, x_2)$$

☐ Choose x_1, x_2, y_1 arbitrarily (with $x_1 \neq x_2$) and set

$$y_2 = y_1 \oplus x_1 \oplus \text{AES}(x_2, x_2)$$

☐ Choose x_1, x_2, y_1 arbitrarily (with $x_1 \neq x_2$) and set

$$y_2 = y_1 \oplus \text{AES}(x_1, x_1)$$

☒ **Correct**

Awesome!

10. Let $H : M \rightarrow T$ be a random hash function where $|M| \gg |T|$ (i.e. the size of M is much larger than the size of T).

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In lecture we showed

that finding a collision on H can be done with $O(|T|^{1/2})$

random samples of H . How many random samples would it take

until we obtain a three way collision, namely distinct strings x, y, z

in M such that $H(x) = H(y) = H(z)$?

☒ $O(|T|^{2/3})$

☐ $O(|T|^{1/2})$

☐ $O(|T|)$

☐ $O(|T|^{1/3})$

☒ **Correct**

An informal argument for this is as follows: suppose we

collect n random samples. The number of triples among the n

samples is n choose 3 which is $O(n^3)$. For a particular

triple x, y, z to be a 3-way collision we need $H(x) = H(y)$

and $H(x) = H(z)$. Since each one of these two events happens

with probability $1/|T|$ (assuming H behaves like a random

function) the probability that a particular triple is a 3-way

collision is $O(1/|T|^2)$. Using the union bound, the probability

that some triple is a 3-way collision is $O(n^3/|T|^2)$ and since

we want this probability to be close to 1, the bound on n

follows.