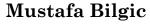
# CS 480 – Introduction to Artificial Intelligence

TOPIC: ADVERSARIAL SEARCH AND GAMES

CHAPTER: 5





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### ADVERSARIAL SEARCH

- A multiagent and competitive environment
- Agents are trying to maximize their utilities at the expense of other agents' utilities
- o Zero-sum games, where the sum of the utilities in the end is constant
  - E.g., win = +1, loss = -1, tie = 0
- Games with abstract descriptions attracted the attention of AI researchers quite a bit
  - The states are relatively easy to represent, limited number of actions, precise rules, expected outcomes, etc. E.g., chess, checkers, backgammon
  - Physical games, except soccer, has not attracted much attention

    (11. Austin Peter)

### CHAPTER 5 V.S. CHAPTER 3

### • Chapter 3:

• Goal-based agent, where the path to the goal is optimized

# SA

### • Chapter 5:

• Utility-based agent, where the expected utility in the end is optimized

MA

Computation

### GAMES ARE PRETTY HARD TO SOLVE

- For example, chess
  - Average branching factor: ~30
  - If a game lasts 40 moves per player
    - Search tree depth is 80
    - Number of nodes:  $30^{80} \approx 10^{118}$
    - Number of estimated atoms in the universe: 10<sup>80</sup>
  - You still must make a decision before you can calculate the optimal move



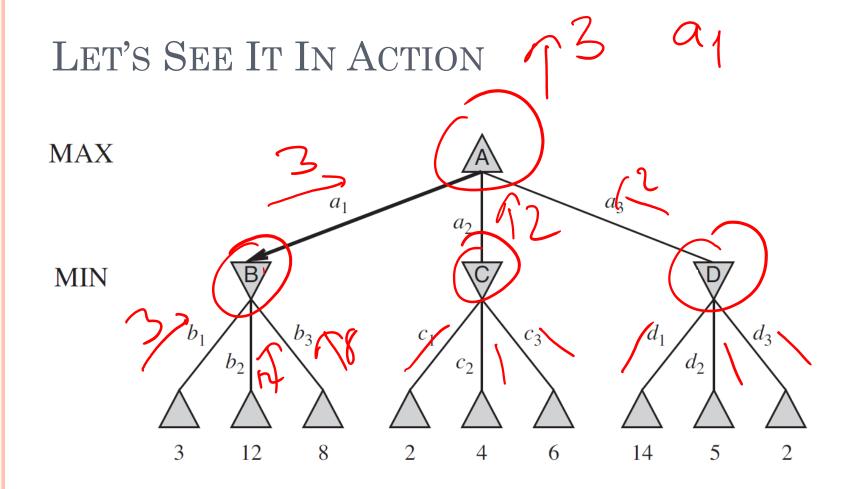
#### GAME DEFINITION

- $\circ$   $S_0$ : The initial state
- $\circ$  *Player*(s): Which player's turn in state s
- $\circ$  *Action(s)*: The set of legal moves in state s
- $\circ$  Result(s, a): The transition model
- $\circ$  *Terminal-test(s)*: Is the game over
- Utility(s, p): The utility of player p in state s
- Two players: MAX and MIN. MAX moves first

1+9+9.8+ GAME TREE - TIC-TAC-TOE MAX(x)MIN (o) MAX(x)What is the number of ХО ХО X O X terminal nodes? MIN (o) TERMINAL Utility

# OPTIMAL STRATEGY

- Maximize utility
- An optimal strategy leads to outcomes at least as good as any other strategy when one is playing on *infallible* opponent
  - What if the opponent is not playing optimally?
- The minimax algorithm



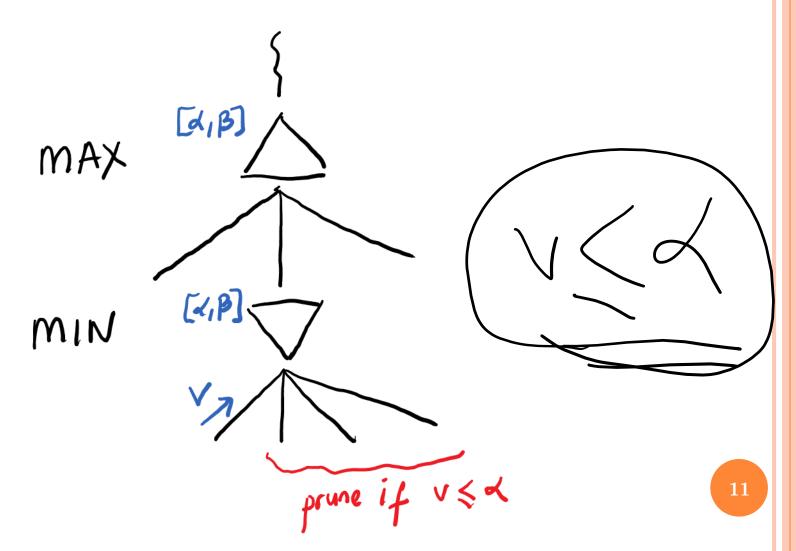
### TIME AND SPACE COMPLEXITY

- The minimax algorithm is a <u>depth-first search</u> algorithm
  - Space: O(bm)
  - Time:  $O(b^m)$
- o Can we do better?

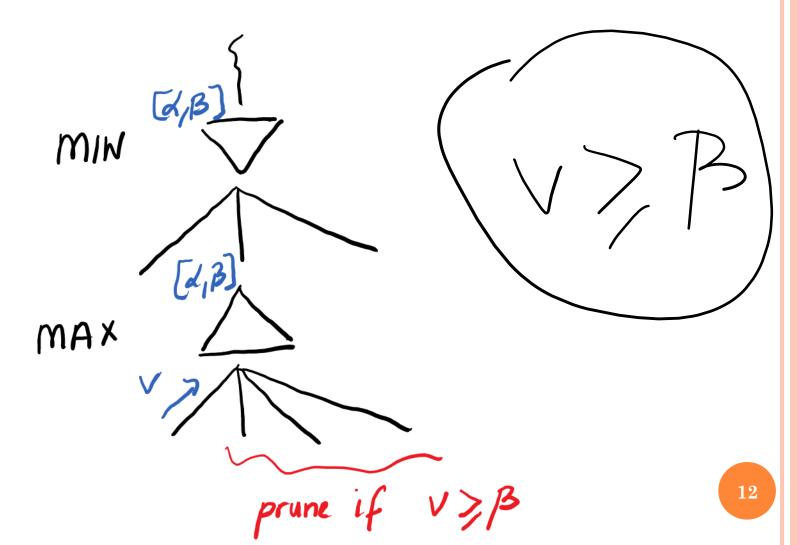
#### ALPHA-BETA PRUNING

- Keep lower and upper bounds ( $\alpha$ ,  $\beta$ )
- $\circ$  MAX updates the lower bound  $\alpha$
- MIN updates the upper bound  $\beta$
- Both pass the current bounds to their children
- MIN( $\alpha$ ,  $\beta$ ) prunes if  $v \le \alpha$ ; MAX already has a better choice  $\alpha$
- MAX( $\alpha(\beta)$ ) prunes if  $v \ge \beta$ ; MIN already has a better choice  $\beta$

# EXAMPLE: MIN PRUNES



# EXAMPLE: MAX PRUNES



### ALPHA-BETA PRUNING ALGORITHM

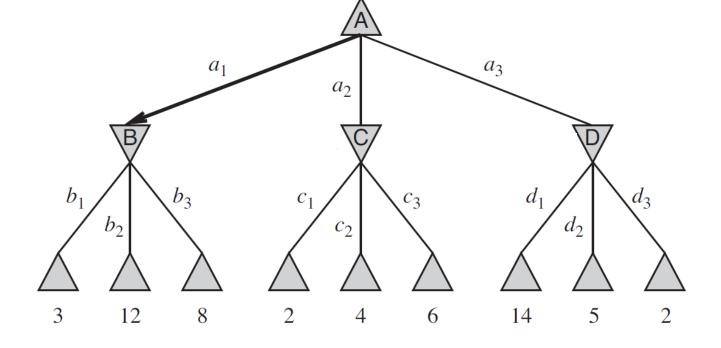
```
function ALPHA-BETA-SEARCH(state) returns an action
   v \leftarrow \text{MAX-VALUE}(state, -\infty, +\infty)
  return the action in ACTIONS(state) with value v
function MAX-VALUE(state, \alpha, \beta) returns a utility value
  if TERMINAL-TEST(state) then return UTILITY(state)
   v \leftarrow -\infty
  for each a in ACTIONS(state) do
     v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a), \alpha, \beta))
     if v \geq \beta then return v
     \alpha \leftarrow \text{MAX}(\alpha, v)
  return v
function MIN-VALUE(state, \alpha, \beta) returns a utility value
  if TERMINAL-TEST(state) then return UTILITY(state)
   v \leftarrow +\infty
  for each a in ACTIONS(state) do
     v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a), \alpha, \beta))
     if v < \alpha then return v
     \beta \leftarrow \text{MIN}(\beta, v)
  return v
```

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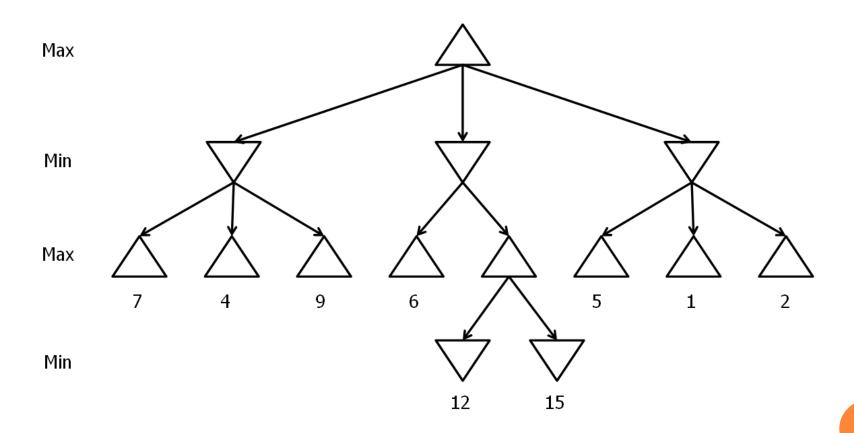
# ALPHA-BETA PRUNING



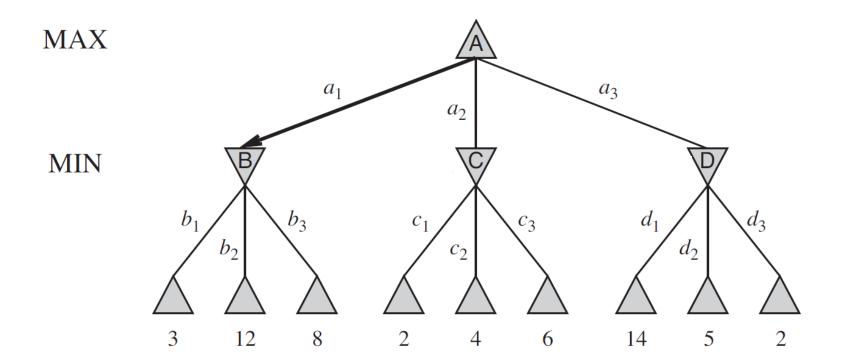
MIN



## Alpha-Beta Pruning – Another Example



# Alpha-Beta Pruning (Figure 5.7)

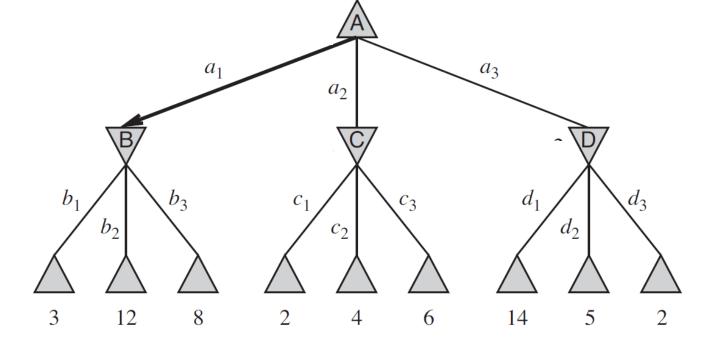


Can we do better?

# Move Ordering

MAX

MIN



What if we re-order these?

#### STILL

- To be able to prune, the alpha-beta algorithm has to visit some of the leaf nodes
  - Of course, this is not practical for most games
- A solution: early cut-off
  - How can we do this? Remember, the utility function is defined for the terminal states.

(m) -> Termine

Sterk

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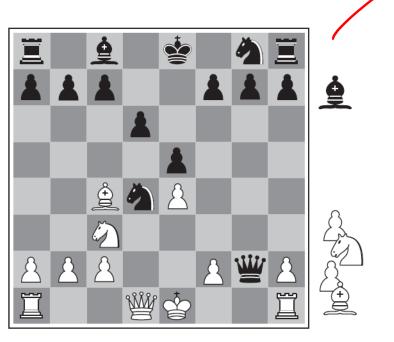
## HEURISTIC EVALUATION FUNCTIONS

- An estimate of the utility is returned rather than the actual utility
- Define features and a weighted feature combination function
  - e.g., EVAL(s) =  $w_1 f_1(s) + w_2 f_2(s) + ... + w_n f_n(s)$
- Chess
  - Pawn: 1, Knight or bishop: 3, rook: 5, queen: 9

## HEURISTIC EVALUATION FUNCTIONS

- Just like in Chapter 3, heuristic functions are not part of the problem description
  - It takes additional <u>expertise</u> and learning to devise useful heuristic functions
- They are not very easy to define

# LINEAR COMBINATION FAILS





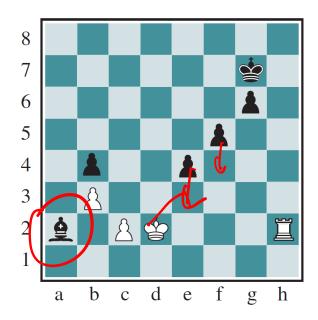


## CUTTING-OFF IS NOT TRIVIAL

- A simple depth limit will not work
  - Cut-off at positions that are quiescent
    - Positions in which a drastic change is unlikely to happen
- Horizon effect
  - A serious damage is unavoidable but the search delays it by making little sacrifices
    - The little sacrifices are unnecessary as the serious damage is unavoidable but a depth-limited search cannot see it

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### HORIZON EFFECT



**Figure 5.9** The horizon effect. With Black to move, the black bishop is surely doomed. But Black can forestall that event by checking the white king with its pawns, encouraging the king to capture the pawns. This pushes the inevitable loss of the bishop over the horizon, and thus the pawn sacrifices are seen by the search algorithm as good moves rather than bad ones.

#### SEARCH V.S. LOOKUP

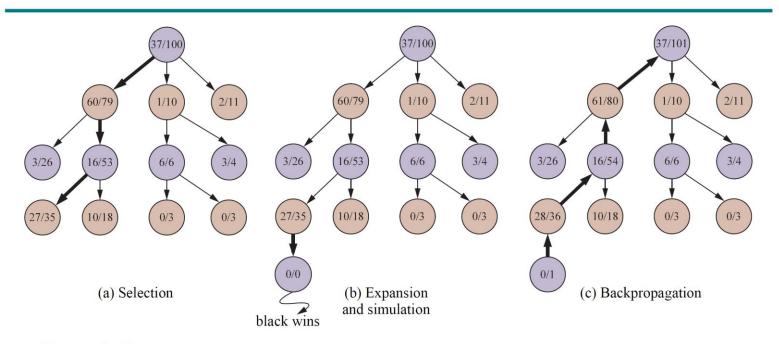
- Opening of a game
  - A depth-limited search is unlikely to help
  - Human expertise and learning from previous games for opening moves
- Ending a game
  - When very few pieces are left, the number of possible states is not many; rather than a depth-limited search, look-up a winning strategy

#### MONTE-CARLO TREE SEARCH

```
function Monte-Carlo-Tree-Search(state) returns an action
tree \leftarrow \text{Node}(state)
while Is-Time-Remaining() do
leaf \leftarrow \text{Select}(tree)
child \leftarrow \text{Expand}(leaf)
result \leftarrow \text{Simulate}(child)
Back-Propagate(result, child)
return the move in Actions(state) whose node has highest number of playouts
```

**Figure 5.11** The Monte Carlo tree search algorithm. A game tree, *tree*, is initialized, and then we repeat a cycle of SELECT / EXPAND / SIMULATE / BACK-PROPAGATE until we run out of time, and return the move that led to the node with the highest number of playouts.

#### MONTE-CARLO TREE SEARCH



**Figure 5.10** One iteration of the process of choosing a move with Monte Carlo tree search (MCTS) using the upper confidence bounds applied to trees (UCT) selection metric, shown after 100 iterations have already been done. In (a) we select moves, all the way down the tree, ending at the leaf node marked 27/35 (for 27 wins for black out of 35 playouts). In (b) we expand the selected node and do a simulation (playout), which ends in a win for black. In (c), the results of the simulation are back-propagated up the tree.

# So Far

- Deterministic
- Fully-observable

### STOCHASTIC GAMES

- An element of chance, such as dice
- Modify the search tree and the minimax algorithm:
  - Include a chance node, that leads to all possible outcomes
  - Rather than computing utilities, compute expected utilities

## PARTIALLY OBSERVABLE GAMES

- The current state is only partially observable
- Model what is not observed
- Examples
  - Card games
  - Battleships
  - Kriegspiel

# HISTORICAL NOTES

#### Algorithms

- 1912 Minimax
- 1956-1961 Alpha-beta pruning
- 1987 Monte Carlo tree search

#### Games

- Chess
  - 1982 Master status
  - 1990 International master status
  - 1997 Defeated Gary Kasparov, the world champion
  - 2017 AlphaZero defeated Stockfish
- Checkers
  - 1960s learned from self-play using reinforcement learning
  - 2007 The game is fully solved

## HISTORICAL NOTES

#### • Games (continued)

- Go
  - 1970 Visual pattern recognition for Go was proposed
  - 1993 Monte-Carlo tree search for Go
  - 1994 reinforcement learning for Go
  - 2001 neural networks for Go
  - 2016 AlphaGo put all these ideas together
- Backgammon
  - 1980s first computer programs for Backgammon
  - 1995 TD-Gammon neural networks and self-play able to play at world champion level
- Poker
  - 2015 Optimal strategy was developed (using game theory)
  - 2017 Computers beat world champions
- StarCraft II
  - 2019 AlphaStar defeats expert players
    - Discussion whether programs have unfair advantage in action speed