# STAT512 Team4

**COVID-19 Infection and Death Cases in Indiana** 

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# Introduction

COVID: Dec. 2019

economics

infections

deaths

Masks: Jul. 2020-Apr. 2021

Vaccine: Dec. 2020

Booster: Aug. 2021









# Introduction

### 2-Dose Vaccine

 Study has shown an efficacy of 95% against infection.



### **Booster**

 Study has shown an efficacy of 96 % against severe illness and death.



### **Masks**

 Study has shown that masks block 80%-90% of virus.





# Introduction

- Efficacy: measured in lab
- Effectiveness: social study
- Effectiveness of Vaccine, Booster, Mask
- Confirmatory Study
- Weekly Data
- Indiana



### Source of Variables

- All data comes from Centers for Disease Control and Prevention. 6 continuous variables and 1 categorical variables are in the dataset.
- Continuous variables are Total Vaccine,
   First Dose, Complete Series, Booster,
   Infection, and Death.
- •Categorical variable is Mask.
- All 6 continuous variables record data in Indiana.

### **Data Cleaning**

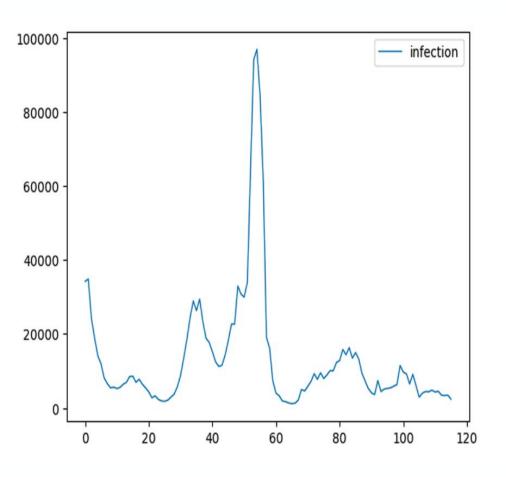
• The original vaccine data is the total number of administered vaccines per day.

• To match the unit of infection and death variables, we calculate the weekly total vaccine number by summing up every day's vaccine in one week.

• In order to eliminate outliers, we delete all the data containing 0.



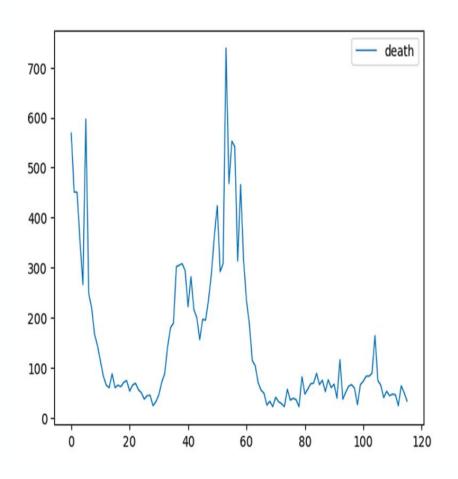




- Infection records the weekly infection cases in Indiana from December 31, 2020 to March 29, 2023.
- As vaccine takes 1-2 week to take effect, we postpone the infection cases two weeks to correspond to the effective vaccine.

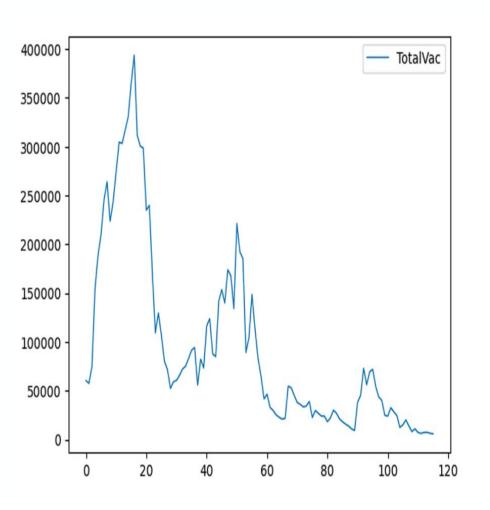






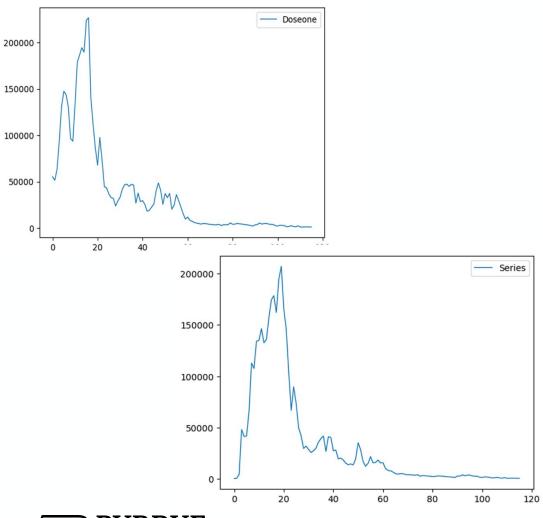
- Death records the weekly death cases in Indiana from December 31, 2020 to March 29, 2023.
- Similar to Infection variables, we postpone the death cases by two weeks to correspond to the effective vaccine.





- Total Vaccine is the total number of administered vaccines per week in Indiana, which includes the first dose, second dose, and both first and second booster.
- Different providers like Pfizer-BioNTech, Moderna, Novavax, and Johnson & Johnson.
- CDC's data may overestimate the total number of vaccines.



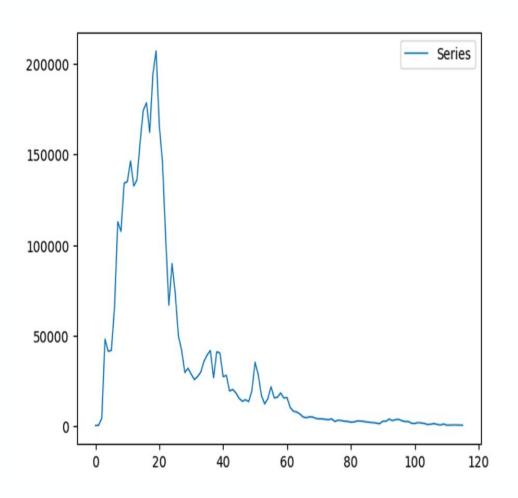


- The Doseone and Series are the total number of the first-dose vaccine and second dose in Indiana per week from different providers.
- CDC's data may overestimate the total number of first dose vaccine but underestimate the total number of second dose vaccine.



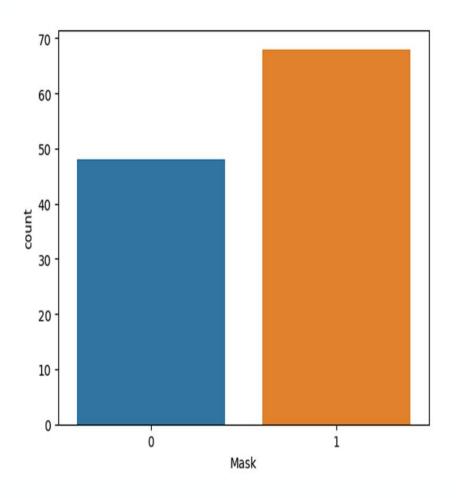


### Variable Description



 Booster is the total number of first booster dose vaccines in Indiana per week from different providers.





- The mask is the categorical variable which includes 0 and 1.
- If Mask is 0, it means the mask mandate policy ended in Indiana. If Mask is 1, it means the mask mandate policy was still activated.
- The mask mandate policy required everyone over the age of 8 to wear a mask both indoors and outside wherever social distancing is not possible since July 27, 2020. The mask mandate ended on April 6, 2021. (IN gov, July 27)



1. Do complete series have significant impact on infected cases, given death cases and first dose?

H0: beta3 = 0 given beta2 and beta5 Ha: beta3 is not 0 given beta2 and

beta5

Reduced model: Y = beta0 + beta5(X5) + beta2(X2)

Full model: Y = beta0 + beta5(X5) + beta2(X2) + beta3(X3)

2. Do complete series and first dose have the same impact on infected cases, given death cases?

H0: beta2 = beta3 = betanew Ha: beta2 is not equal to beta3

Reduced model: Y = beta0 + betanew(X2 + X3) + beta5(X5)

Full model: Y = beta0 + beta2(X2) + beta3(X3) + beta5(X5)





X2: first dose

X3: complete series

X5: death cases

Y: infection cases

Shapiro-Wilk normality test

data: res

W = 0.85227, p-value = 2.153e-09

studentized Breusch-Pagan test

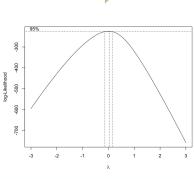
data: model

BP = 35.205, df = 3, p-value = 1.103e-07

Normal Q-Q Plot 40000 Sample Quantiles -20000 Theoretical Quantiles

Log transformation on X, Box-cox transformation on  $Y(\lambda = 0.0303)$ 





Shapiro-Wilk normality test

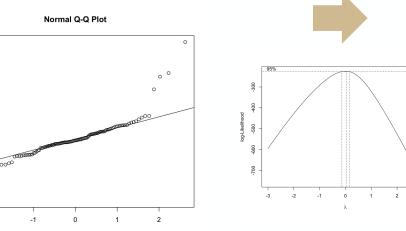
residuals(modelNew)

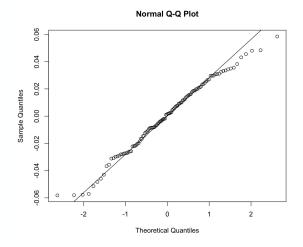
W = 0.98693, p-value = 0.327

studentized Breusch-Pagan test

data: modelNew

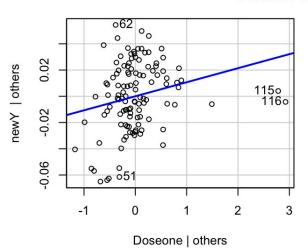
BP = 7.5565, df = 3, p-value = 0.05612

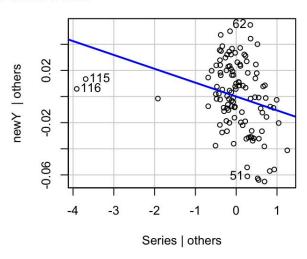


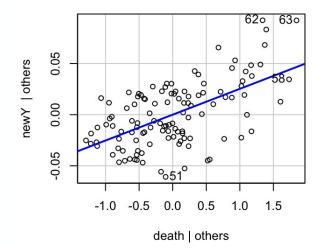












All marginal effects of the predictors are significant.

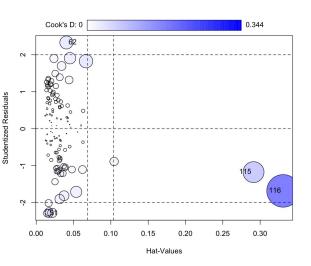


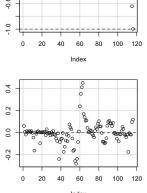
dfbetas Plots

```
> sum(abs(rstudent(modelNew)) > 2)
[1] 0
> infl = lm.influence(modelNew)$hat
> length(which(infl[] > 2 * (4 / 116)))
[1] 3
```

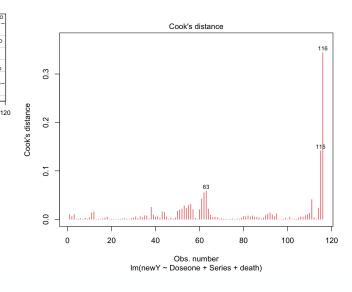
```
> sum(d[which(abs(d[, 2]) > 1 & abs(d[, 3]) > 1 & abs(d[, 4]) > 1)])
[1] 0
> length(dff[dff > 1])
[1] 0
> sum(Cooksdistance > minor)
[1] 0
> sum(Cooksdistance > major)
[1] 0
```

### O Y outliers, 3 x outliers

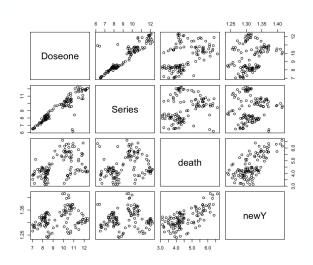


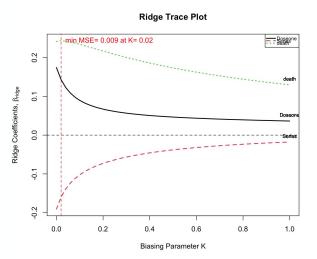


### No influential points









> VIF(Im(Doseone~Series+death, new))

[1] 7.283964

> VIF(Im(Series~Doseone+death, new))

[1] 6.085945

> VIF(Im(death~Doseone+Series, new))

[1] 1.531526

|          | Doseone | Series  | death   |
|----------|---------|---------|---------|
| k=0      | 7.28396 | 6.08595 | 1.53153 |
| k = 0.02 | 4.65084 | 3.95688 | 1.31869 |
| k = 0.04 | 3.25454 | 2.82358 | 1.18521 |
| k = 0.06 | 2.42528 | 2.14714 | 1.08976 |
| k = 0.08 | 1.89220 | 1.70962 | 1.01549 |
| k=0.1    | 1.52885 | 1.40920 | 0.95437 |
| k=0.12   | 1.26971 | 1.19316 | 0.90216 |
| k=0.14   | 1.07811 | 1.03194 | 0.85640 |
| k=0.16   | 0.93221 | 0.90792 | 0.81555 |
| k=0.18   | 0.81835 | 0.81007 | 0.77862 |

**Multicollinearity** 



**Ridge Regression** 



```
Call:
                                                            lmridge.default(formula = newY ~ Doseone + Series + death, data = new,
lm(formula = newY ~ Doseone + Series + death, data = new)
                                                                K = 0.14
Residuals:
     Min
                     Median
                                                            Coefficients: for Ridge parameter K= 0.14
-0.058194 -0.018880 0.001447 0.019094 0.058479
                                                                     Estimate Estimate (Sc) StdErr (Sc) t-value (Sc) Pr(>|t|)
                                                            Intercept
                                                                      1,2066
                                                                                  0.3447
                                                                                            0.3763
                                                                                                       0.9162 0.3615
                                                                                                               0.0053 **
                                                                      0.0048
                                                                                  0.0779
                                                                                            0.0274
                                                                                                       2.8452
                                                            Doseone
Coefficients:
                                                            Series
                                                                      -0.0049
                                                                                 -0.0879
                                                                                            0.0268
                                                                                                       -3.2780
                                                                                                               0.0014 **
            Estimate Std. Error t value Pr(>|t|)
                                                                                                               <2e-16 ***
                                                            death
                                                                      0.0238
                                                                                  0.2272
                                                                                            0.0244
                                                                                                       9.3040
                      0.016614 71.998 < 2e-16 ***
(Intercept) 1.196178
Doseone
            0.010701
                      0.004322 2.476 0.01478 *
                                                            Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
                      0.003580 -2.964 0.00371 **
            -0.010609
Series
death
            0.025270
                      0.003377 7.483 1.77e-11 ***
                                                            Ridge Summary
                                                                   R2
                                                                         adj-R2
                                                                                DF ridge
                                                                                                       AIC
                                                                                                                 BIC
                                                                        0.36610
                                                                                 2.13765 38.30602 -841.63815 -284.33547
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
                                                            Ridge minimum MSE= 0.02213321 at K= 0.14
                                                            P-value for F-test (2.13765, 113.4471) = 5.317365e-14
Residual standard error: 0.02608 on 112 degrees of freedom
                              Adjusted R-squared: 0.4991
Multiple R-squared: 0.5122,
F-statistic: 39.19 on 3 and 112 DF, p-value: < 2.2e-16
BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS
                                                                   BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS
Based on 100 bootstrap replicates
                                                                   Based on 100 bootstrap replicates
CALL:
                                                                   CALL:
boot.ci(boot.out = modelrid, type = "perc", index = 2) boot.ci(boot.out = modelrid, type = "perc", index = 3)
                                                                   Intervals:
Intervals:
                                                                               Percentile
                                                                   Level
Level
            Percentile
                                                                          (-0.0067, -0.0030)
      ( 0.0022, 0.0077 )
                                                                   95%
                                                                   Calculations and Intervals on Original Scale
Calculations and Intervals on Original Scale
                                                                   Some percentile intervals may be unstable
Some percentile intervals may be unstable
```

- beta2 > 0 ???
- 1. The amount of data is insufficient and limited to the state of Indiana.
- 2. It is uncertain whether a two-week delay is enough for the first dose to manifest.
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- Covid-19 virus is notorious for its fast mutation, so it may be the case that the virus has already mutated by the time that dose one is taken.

> FS = MSR / MSE

>FS

[1] 7.627347

> af(1 - 0.05, reduced\$df.residual full\$df.residual, full\$df.residual)

[1] 3.925834

> p = 1 - pf(FS, reduced\$df.residual full\$df.residual, full\$df.residual)

> p

[1] 0.006720598

> FS = MSR/MSE

>FS

[1] 8.78373

> qf(0.95,

reduced\$df.residual-full\$df.residual, full\$df.residual)

[1] 3.925834

> p =

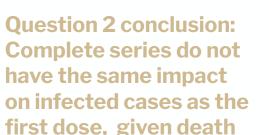
1-pf(FS,reduced\$df.residual-full\$df.resi dual, full\$df.residual)

> p

[1] 0.003713453

**Ouestion 1 conclusion: Complete series has** significant impact on infected cases, given death cases and first dose.





cases.



A full series of Covid-19 vaccines can restrict the infection rate. which may indirectly prove that a full series vaccination is able to increase the immunity to Covid-19.





### K-fold Cross Validation

nvmax RMSE Rsquared MAE RMSESD RsquaredSD MAESD 4 0.02722844 0.487252 0.02208553 0.002404326 0.1818767 0.002062165

The model behaves stably across different data and has good predictive power





Does complete series have the same impact as the booster shot with the first dose and death cases in the model?

X2: first dose

X3: complete series

X4: booster

X5: death cases

Y: infection cases

Ho: beta3 = beta4

Reduced Model: Y = beta2X2+betanew(X3+X4)+beta5X5

Ha: beta3 ≠ beta4

Full Model: Y = beta2X2+beta3X3+beta4X4+beta5X5

```
call:
lm(formula = y \sim x2 + x3 + x4 + x5)
Residuals:
  Min
         10 Median 30
                           Max
-27566 -3442 -722 4634 43276
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -107.21121 1538.69340 -0.070 0.944632
x2
             x3
            -1.09480 0.22240 -4.923 4.75e-06 ***
           -0.04840 0.04735 -1.022 0.309829
x5
           111.78220 11.09195 10.078 1.03e-15 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 9634 on 77 degrees of freedom
Multiple R-squared: 0.7536, Adjusted R-squared: 0.7408
F-statistic: 58.87 on 4 and 77 DF, p-value: < 2.2e-16
```



Does complete series have the same impact as the booster shot with the first dose and death cases in the model?

- BP test
- Shapiro test
- qq plot
- outlier

- non constant error variance
- non normal error
- 6 outliers

```
> # Check Variance Constancy
> bptest(covidFull.mod)

studentized Breusch-Pagan test

data: covidFull.mod
BP = 23.856, df = 4, p-value = 8.538e-05

> # Check Variance Normality
> shapiro.test(residuals(covidFull.mod))

Shapiro-Wilk normality test

data: residuals(covidFull.mod)
W = 0.89307, p-value = 4.981e-06

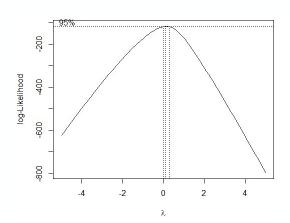
> # Check Outlier
> data$outlier <- abs(rstudent(covidFull.mod)) > 2
> sum(data$outlier)
[1] 6
```

# Normal Q-Q Plot Sample Consulting Service Consulti



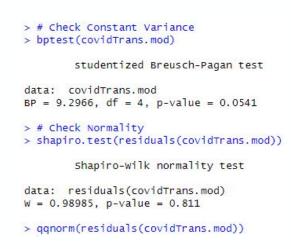
Does complete series have the same impact as the booster shot with the first dose and death cases in the model?

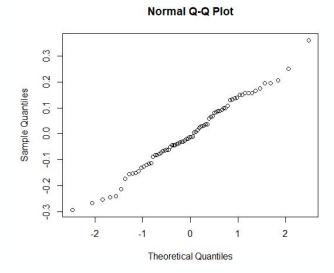
- X Transformation
- Box-Cox Y Transformation
- BP test
- Shapiro test
- qq plot



### After transformation:

- constant error variance
- normal error



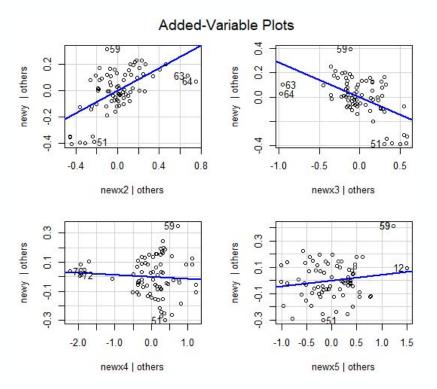


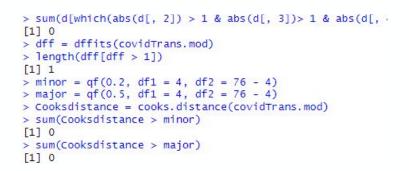


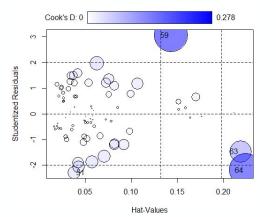
Does complete series have the same impact as the booster shot with the first dose and death cases in the model?

- Added Variable Plots
- DFBETAS, DFFITS, Cook's Distance

- no 0 marginal effect
- few influential points









Does complete series have the same impact as the booster shot with the first dose and death cases in the model?

- pairs plot
- VIF

50000

150000

- no 0 marginal effect
- few influential points

```
> VIF(lm(Doseone~Series+Booster+death, data=data))
[1] 9.202451
> VIF(lm(Series~Doseone+Booster+death, data=data))
[1] 7.146584
> VIF(lm(Booster~Doseone+Series+death, data=data))
[1] 2.143072
> VIF(lm(death~Doseone+Series+Booster, data=data))
[1] 2.385914
```



20000 40000

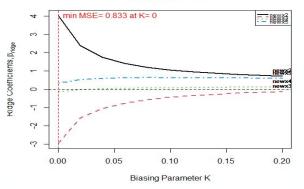
Does complete series have the same impact as the booster shot with the first dose and death cases in the model?

Ridge Regression

multicollinearity removed

```
> vif(Ridge.mod)
         newx2
                  newx3
                          newx4
k=0
      23.34991 16.96300 3.08289 2.96793
k=0.02 7.77698 6.19320 2.60475 2.33742
k=0.04 3.99406 3.49207 2.26019 2.02151
k=0.06 2.49969 2.37503 1.98702 1.79395
k=0.08 1.75025 1.78400 1.76388 1.61221
       1.31640 1.42205 1.57839 1.46094
k=0.12 1.03997 1.17829 1.42217 1.33226
k=0.14 0.85136 1.00301 1.28921 1.22129
k=0.16 0.71594 0.87088 1.17498 1.12460
k=0.18 0.61479 0.76772 1.07606 1.03969
       0.53683 0.68496 0.98978 0.96462
```

### **Ridge Trace Plot**



```
> summary(covidRidge.mod)
call:
lmridge.default(formula = newy ~ newx2 + newx3 + newx4 + newx5,
    data = newdata, K = 0.12)
Coefficients: for Ridge parameter K= 0.12
          Estimate Estimate (Sc) StdErr (Sc) t-value (Sc) Pr(>|t|)
                         -6.4575
                                      2.6821
                                                  -2.4076 0.0186
Intercept
          1.4229
                         0.9483
            0.1015
                                      0.1570
newx2
                                                   6.0422
                                                           <2e-16
newx3
           -0.0337
                         -0.3469
                                      0.1671
                                                  -2.0763
                                                           0.0414
            0.0085
                         0.0924
                                      0.1835
                                                   0.5035
                                                           0.6161
newx4
newx5
           0.0845
                         0.6244
                                      0.1776
                                                   3.5148
                                                           0.0008
Intercept *
newx2
newx3
newx4
newx5
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Ridge Summary
                       DF ridge
               adj-R2
                                        F
             0.40960
                         2.53802
                                 24.81952 -282.57748
Ridge minimum MSE= 16.43541 at K= 0.12
P-value for F-test ( 2.53802 , 72.86528 ) = 3.333628e-10
```

0.95-CI beta3 (-0.68, -0.01) 0.95-CI beta4 (-0.36, 0.37)



Does complete series have the same impact as the booster shot with the first dose and death cases in the model?

F test

Do not have the same effect

Test Statistic: 24.1499 Critical Value: 3.9758



Does complete series have the same impact as the booster shot with the first dose and death cases in the model?

K-fold Cross Validation

Small RMSE



Does the number of vaccines have the same impact on the number of death cases before and after the mask mandate was lifted in Indiana?

 $X_1$ : The number of vaccines

 $X_2$ : Mask mandate

When  $X_2 = 0$ ,  $E(Y) = \beta_0 + \beta_1 X_1$ ; When  $X_2 = 1$ ,  $E(Y) = (\beta_0 + \beta_2) + (\beta_1 + \beta_3) X_1$ 

Y: The number of death cases

 $H_0: \beta_3 = 0 \ H_a: \beta_3 \neq 0$ 

Reduced Model:  $Y_i = \beta_0 + \beta_1 X_1 + \beta_2 X_2$ 

Full Model:  $Y_i = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_1 X_2$ 





### **Constant Variance**

### **Normality**

studentized Breusch-Pagan test

Shapiro-Wilk normality test

data: model

$$BP = 19.313$$
,  $df = 3$ ,  $p$ -value = 0.0002355

### Non-constant variance & violation of normality

**Log Transformation On X** 



**Box-cox Transformation on Y** 

### **Rechecking constant variance & normality**

studentized Breusch-Pagan test

data: newModel

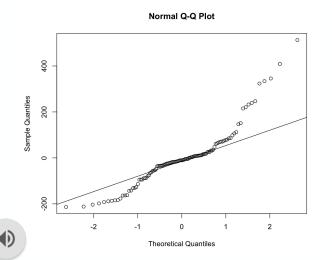
$$BP = 16.304$$
,  $df = 3$ ,  $p$ -value = 0.0009825

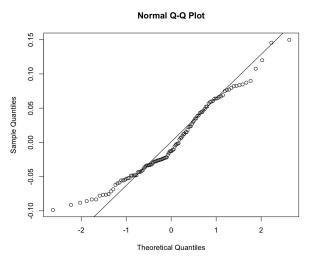
Shapiro-Wilk normality test

data: residuals(newModel)

W = 0.88327, p-value = 4.516e-08

### There is an improvement on non-constant variance and normality







Does the number of vaccines have the same impact on the number of death cases before and after the mask mandate was lifted in Indiana?

 $X_1$ : The number of vaccines

 $X_2$ : Mask mandate

When 
$$X_2 = 0$$
,  $E(Y) = \beta_0 + \beta_1 X_1$ ; When  $X_2 = 1$ ,  $E(Y) = (\beta_0 + \beta_2) + (\beta_1 + \beta_3) X_1$ 

> anova(newModel)

Y: The number of death cases

$$H_0: \beta_3 = 0 \ H_a: \beta_3 \neq 0$$

Reduced Model:  $Y_i = \beta_0 + \beta_1 X_1 + \beta_2 X_2$ 

Full Model:  $Y_i = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_1 X_2$ 

According to OLS model, the interaction factor between two parameters is **insignificant**.

```
PURDUE UNIVERSITY.
```

```
Analysis of Variance Table

Response: death

Df Sum Sq Mean Sq F value Pr(>F)

TotalVac 1 0.09824 0.098235 31.1020 1.718e-07 ***
factor(Mask) 1 0.07482 0.074823 23.6896 3.737e-06 ***

TotalVac:factor(Mask) 1 0.00057 0.000566 0.1793 0.6728

Residuals 112 0.35375 0.003158

---

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

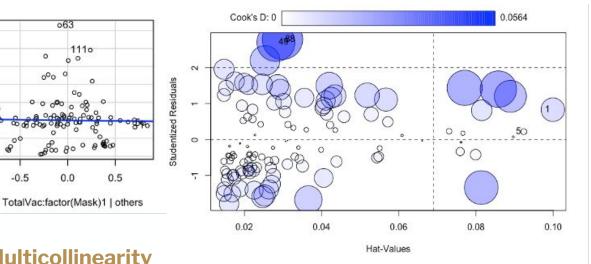
### Added-Variable Plots 630 400 1110 death | others death | others 200 0 -200 -1.0 -0.50.0 0.5 -0.080.04 TotalVac | others factor(Mask)1 | others Cook's D: 0 063

### **Marginal Effect**

Total number of vaccines and interaction factor don't provide much additional information.

### X and Y Outliers

Both X and Y have no obvious outliers.



**Multicollinearity** 

TotalVac 5.803335

-0.5

death | others

factor(Mask) TotalVac:factor(Mask) 224.744249 268.974980

Have multicollinearity issue, but it's expected



### Improve multicollinearity by Ridge Regression

```
> vif(RModel) # 0.06
        TotalVac factor(Mask)1 TotalVac:factor(Mask)1
         5.80334
                       224.74425
                                                 268.97498
k=0
k=0.02 2.11490
                         2.56865
                                                    2.66031
k=0.04 1.87480
                         1.14226
                                                    0.99427
k=0.06 1.68544
                         0.80927
                                                    0.63227
k=0.08 1.52610
                         0.66171
                                                    0.48709
k=0.1
         1.38974
                         0.57399
                                                    0.40919
k=0.12 1.27187
                         0.51299
                                                    0.35968
> summary(RModel)
Call:
lmridge.default(formula = death ~ TotalVac + TotalVac * factor(Mask),
    data = data, K = 0.06)
Coefficients: for Ridge parameter K= 0.06
                    Estimate Estimate (Sc) StdErr (Sc) t-value (Sc) Pr(>|t|)
Intercept
                      0.3492
                                   1.8637
                                             0.8494
                                                         2.1943
                                                                 0.0303 *
TotalVac
                     -0.0009
                                  -0.0104
                                             0.0724
                                                        -0.1441
                                                                 0.8857
```

-0.2010

-0.1961

-0.0379

From Ridge Regression model, we find that the parameter: total number of vaccines doesn't play an significant role in the model.

0.0502

0.0443

-4.0081

-4.4234

0.0001 \*\*\*

<2e-16 \*\*\*



factor(Mask)1

TotalVac:factor(Mask)1 -0.0032

### **Bootstrapping**

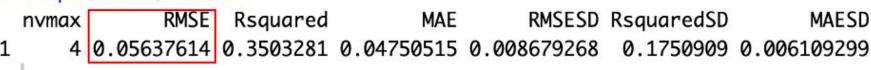
The 95% CI of X1 is [-0.0136, 0.0109]

The 95% CI of X2 is [-0.0602, -0.0160]

The 95% CI of the interaction factor between X1 and X2 is [-0.0042, -0.0019].

### **K-Fold Validation**

> step.model1\$results



RMSE=0.056376 means the model can make a good prediction.

### **Conclusion:**

- 1. The number of death cases were lower before the mask mandate was lifted.
- 2. Total number of vaccines isn't significant when it's in the same model with the categorial parameter mask mandate.



### Nature of Study

In this project, we use linear regression models to determine how factors including the first dose of vaccine, the complete series of vaccines (second dose), the booster, the total number of vaccines people take, and the categorical factor like whether the mask mandate was lifted in Indiana affects the number of infections and the number of deaths.

Our study is a confirmatory observational study



An evidence review of face masks against COVID-19





January 11, 2021 118 (4) e2014564118 https://doi.org/10.1073/pnas.2014564118

### **Expectations**

- A reduction in the number of infections after people take the first dose of COVID-19 vaccine, and continuous reduction when people take the second dose.
- 2. Booster can further reduce the number of infections in Indiana.
- See the same effect of vaccines before and after the mask mandate was lifted which can further confirm that vaccines do have a strong effectiveness in preventing COVID-19 even when people didn't wear a mask.
- 4. Through wearing masks and getting vaccinated, we also expected to see a much lower number of death cases.

All our models have very strong predictive ability, but not all our expectations are reached.



### Pros & Cons

### **Pros**

- 1. The database of our project is **up-to-date** since the pandemic just happened in the last three years.
- 2. The project can be meaningful since the pandemic is not completely over.
- We learn how to deal with real-world data which is much problematic than database we used in homeworks.

### Cons

- 1. The scale of research questions can't be handled by relatively small database.
- 2. Not all violations of data such as non-constant variance and normality were solved in our model.
- 3. Project wasn't planned well. We didn't set aside more time for emergency.





Next step

The scale of research questions can't be handled by relatively small database

Scale up current database

Expanding our research from Indiana to the United States

Extending the time of data from several weeks to years





# Thank You

