

Sequence Model and Recurrent Neural Network (RNN)

Changchong Sheng

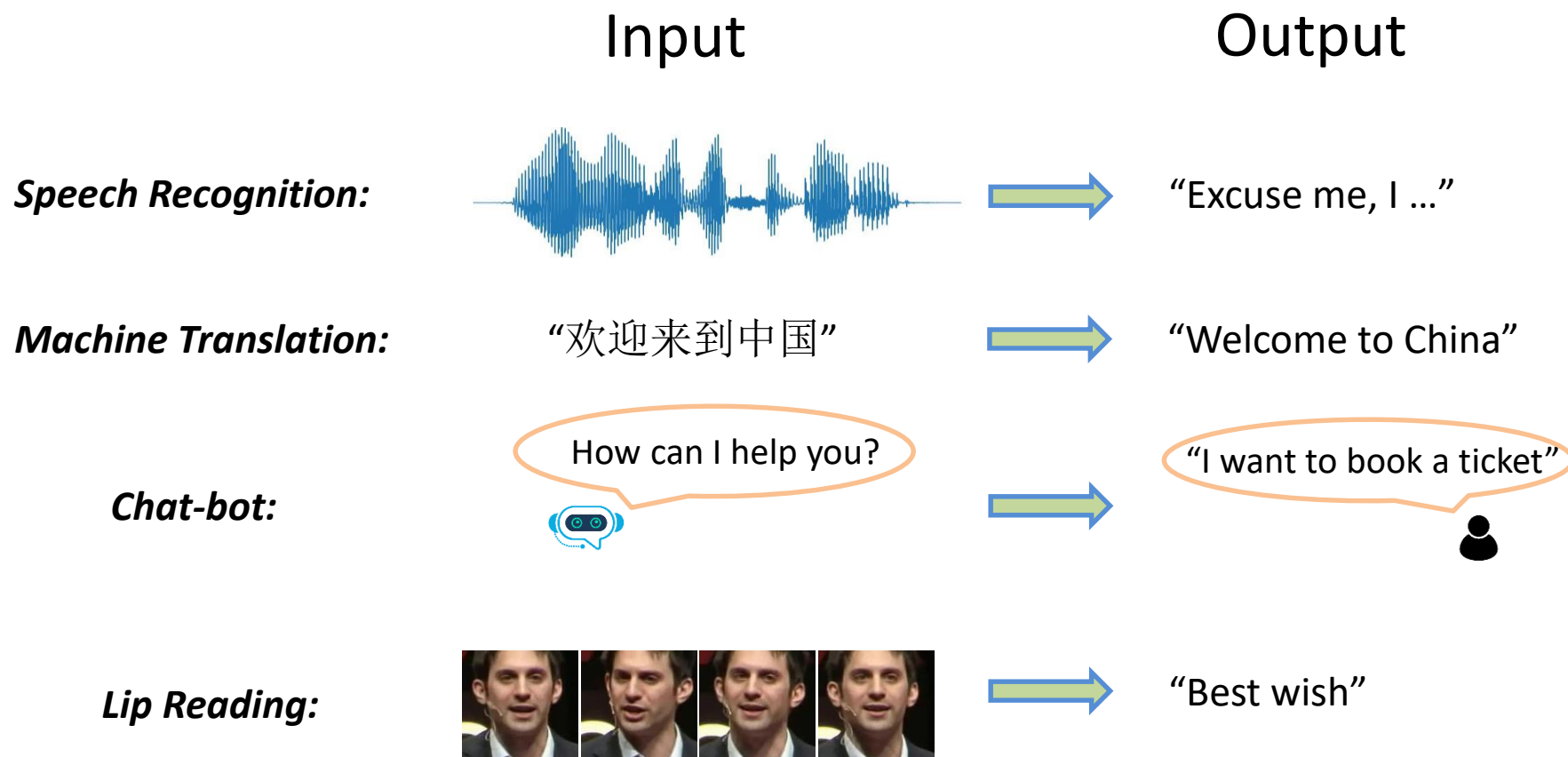
Outline

This lecture introduces sequence model. The goal is to know how RNN and LSTM work, have an idea of their applications.

- Why sequence model?
- Why RNN?
- Basic RNN
- LSTM
- Applications
- Attention mechanism
- Self-attention based models

Why Sequence Model ?

➤ Some Example Tasks:



Why Sequence Model ?

➤ Some Example Tasks:

Input

Output

Music Generation:

\emptyset



Image Captioning:



"A Woman is running"

Sentiment Classification:

"This movie
is terrible"



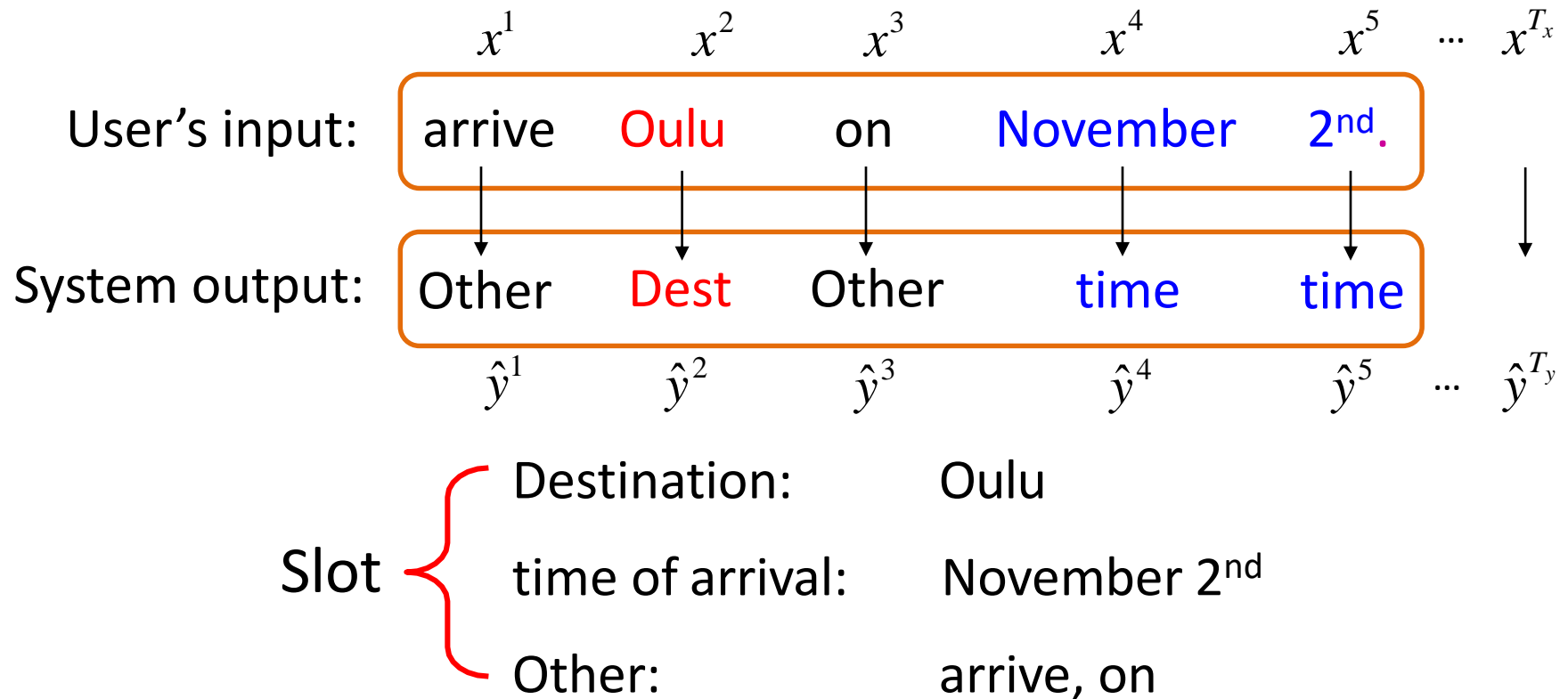
Activity Recognition:



HighJump

Why RNN?

- Slot Filling: Ticket booking system



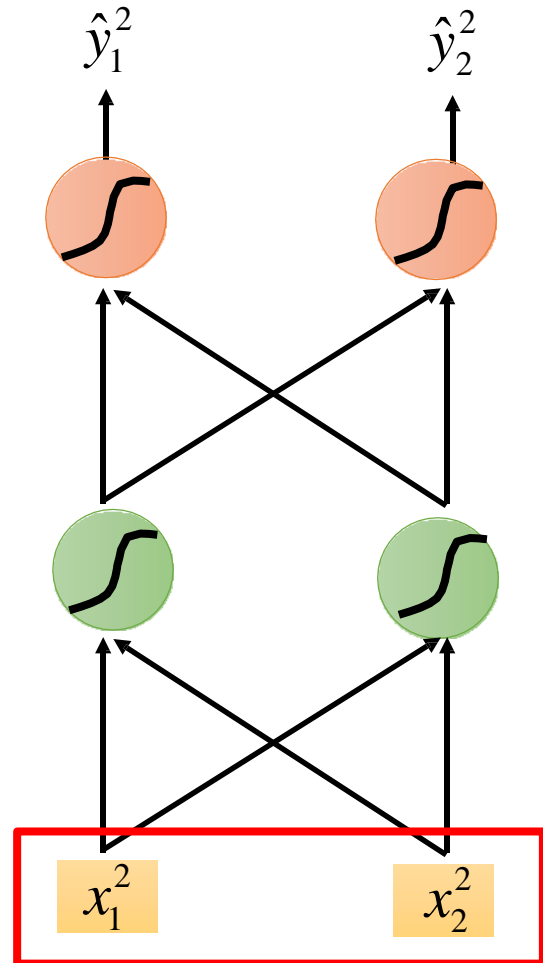
Why RNN?

Solving slot filling by
Feedforward network?

Input: a word

(Each word is represented
as a vector)

Oulu



One-hot encoding

How to represent each word as a vector?

One-hot Encoding lexicon = {apple, bag, cat, dog, elephant}

The vector is lexicon size.

Each dimension corresponds to a word in the lexicon

The dimension for the word is 1, and others are 0

apple = [1 0 0 0 0]

bag = [0 1 0 0 0]

cat = [0 0 1 0 0]

dog = [0 0 0 1 0]

elephant = [0 0 0 0 1]

Why RNN?

Solving slot filling by
Feedforward network?

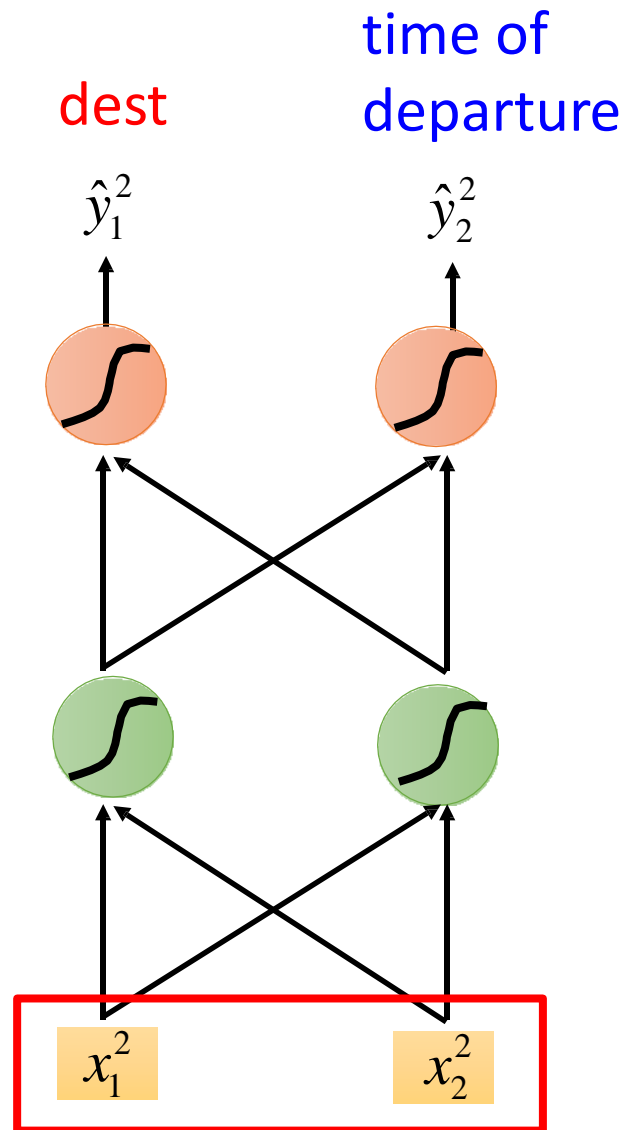
Input: a word

(Each word is represented
as a vector)

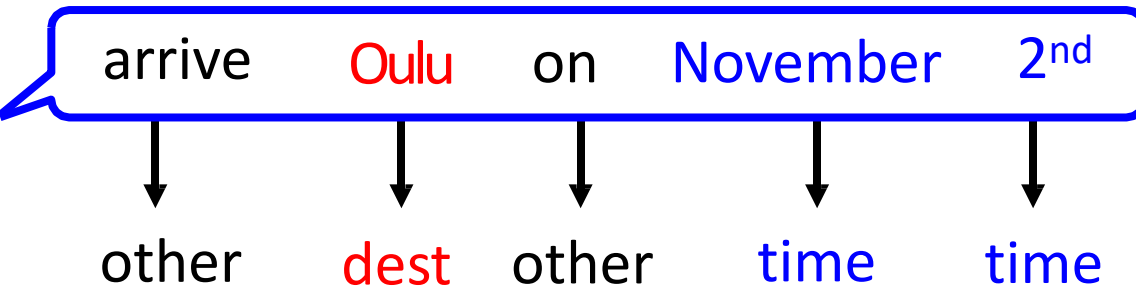
Output:

Probability distribution that
the input word belonging to
the slots

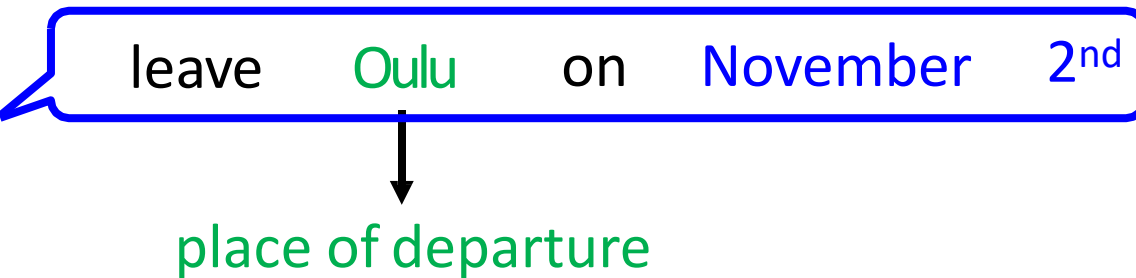
Oulu



Why RNN?

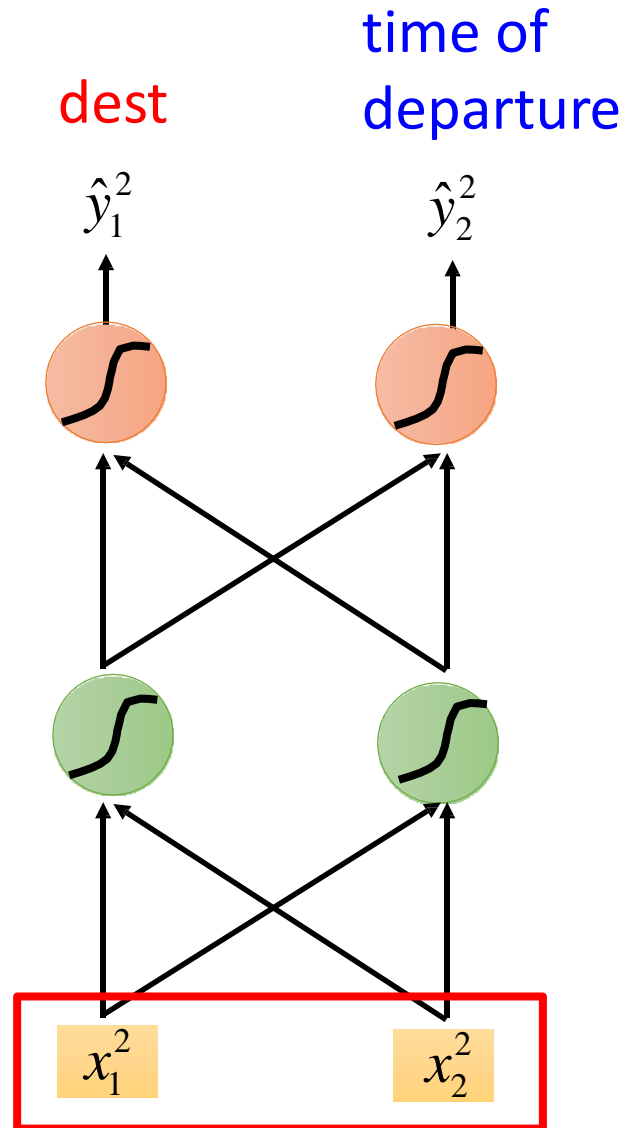


Problem?



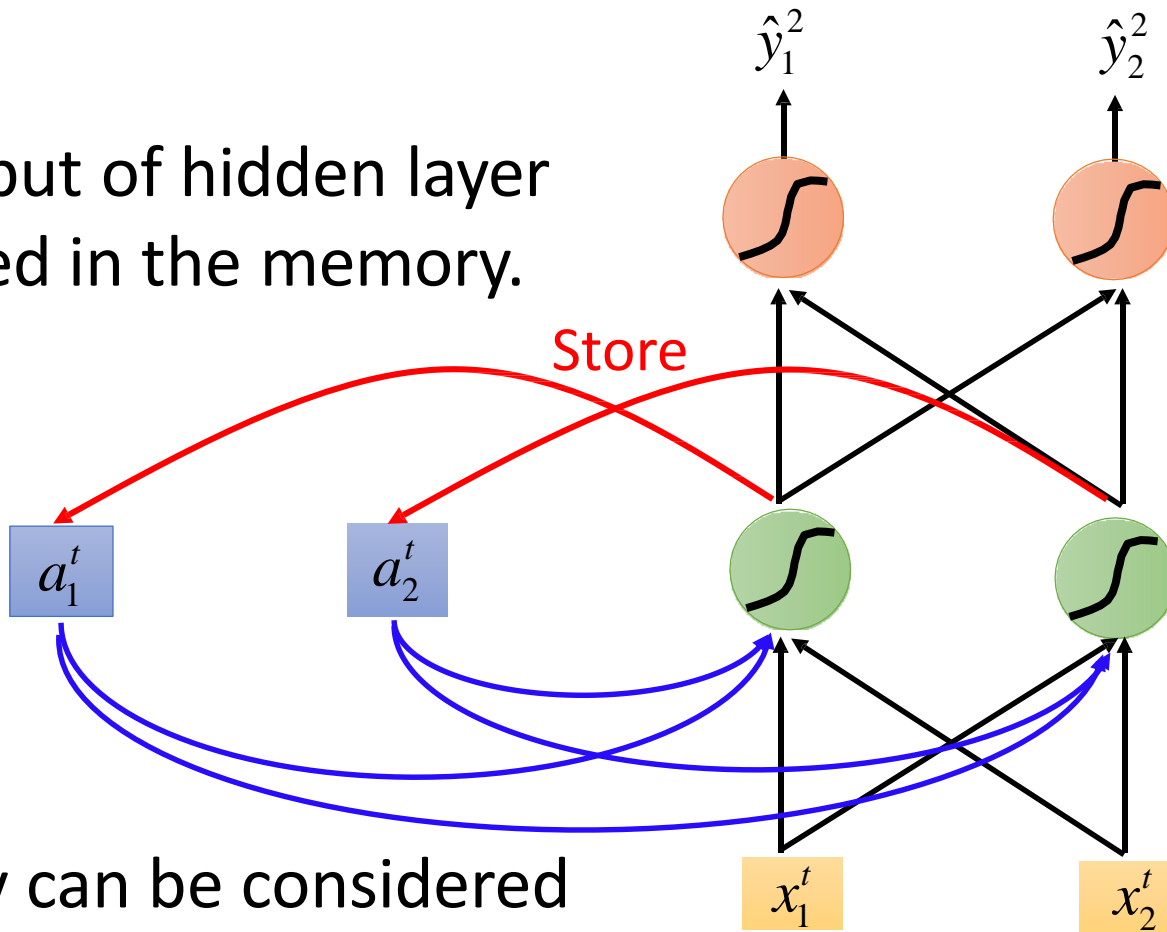
Neural network
needs memory!

Oulu



Recurrent Neural Network (RNN)

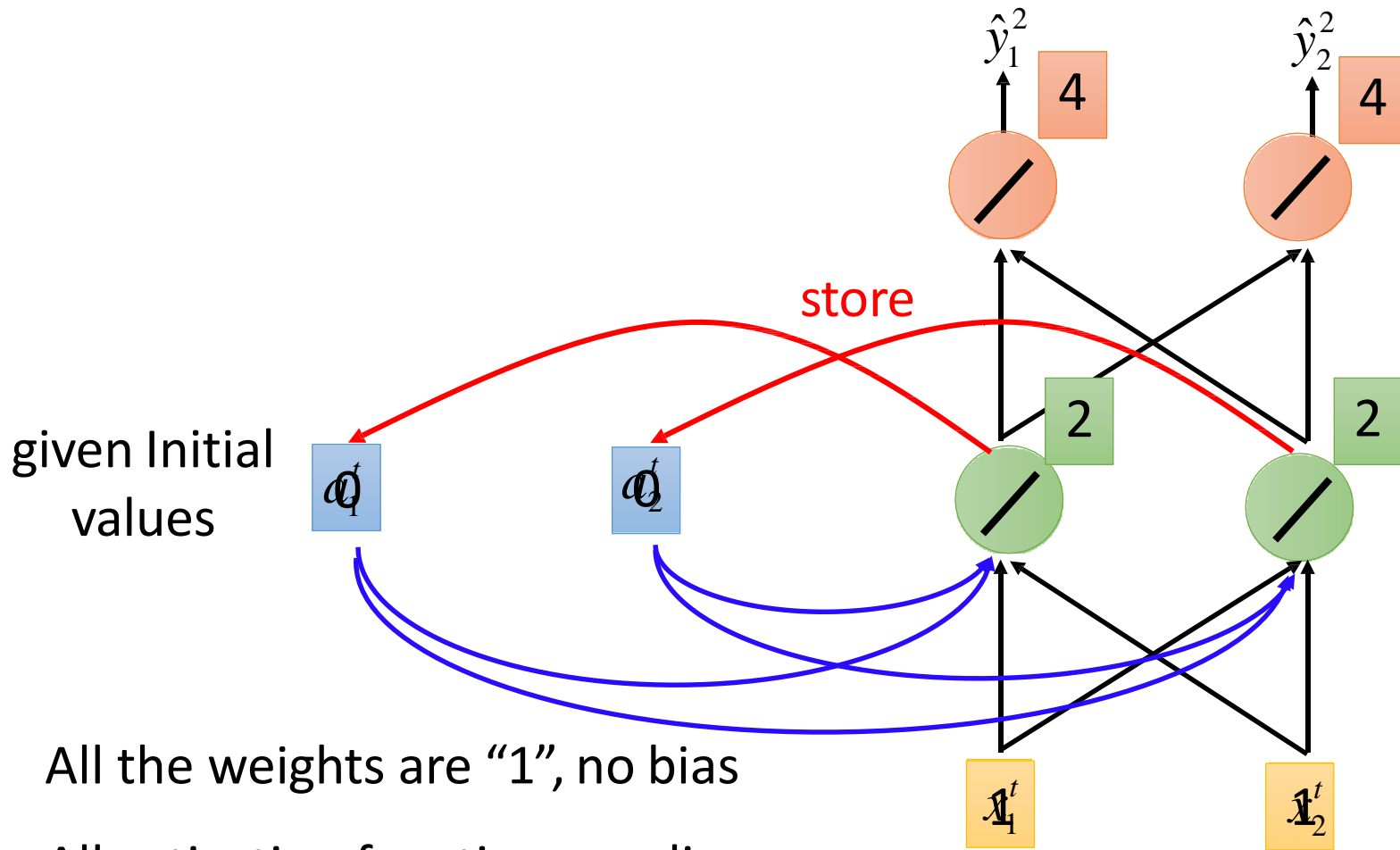
The output of hidden layer are stored in the memory.



Memory can be considered as another input.

Example

Input sequence: $\begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 2 \\ 2 \end{bmatrix} \dots$
output sequence: $\begin{bmatrix} 4 \\ 4 \end{bmatrix}$



All the weights are "1", no bias

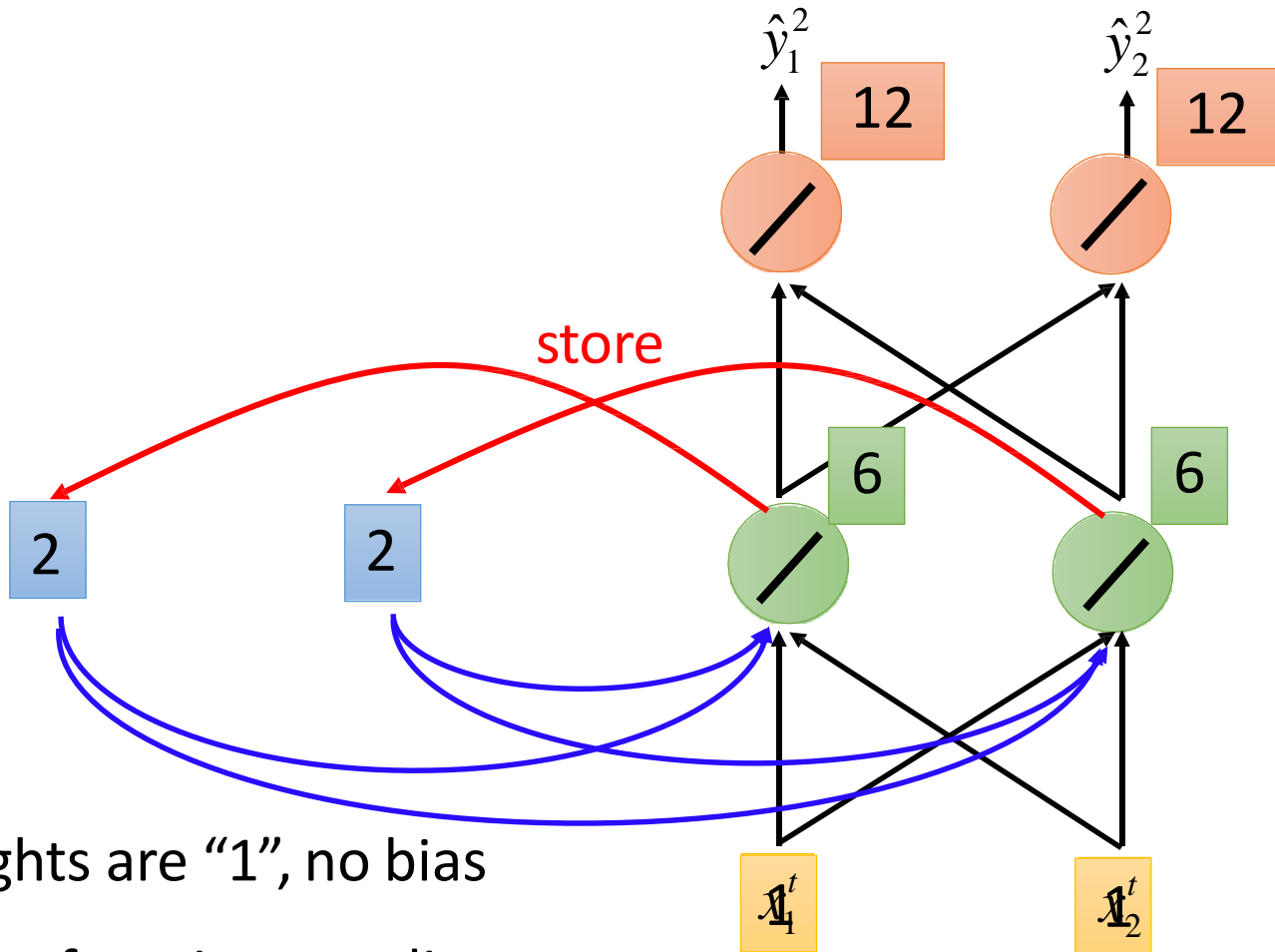
All activation functions are linear

time: 1

Example

Input sequence: $\begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 2 \\ 2 \end{bmatrix} \dots$

output sequence: $\begin{bmatrix} 4 \\ 4 \end{bmatrix} \begin{bmatrix} 12 \\ 12 \end{bmatrix}$



All the weights are "1", no bias

All activation functions are linear

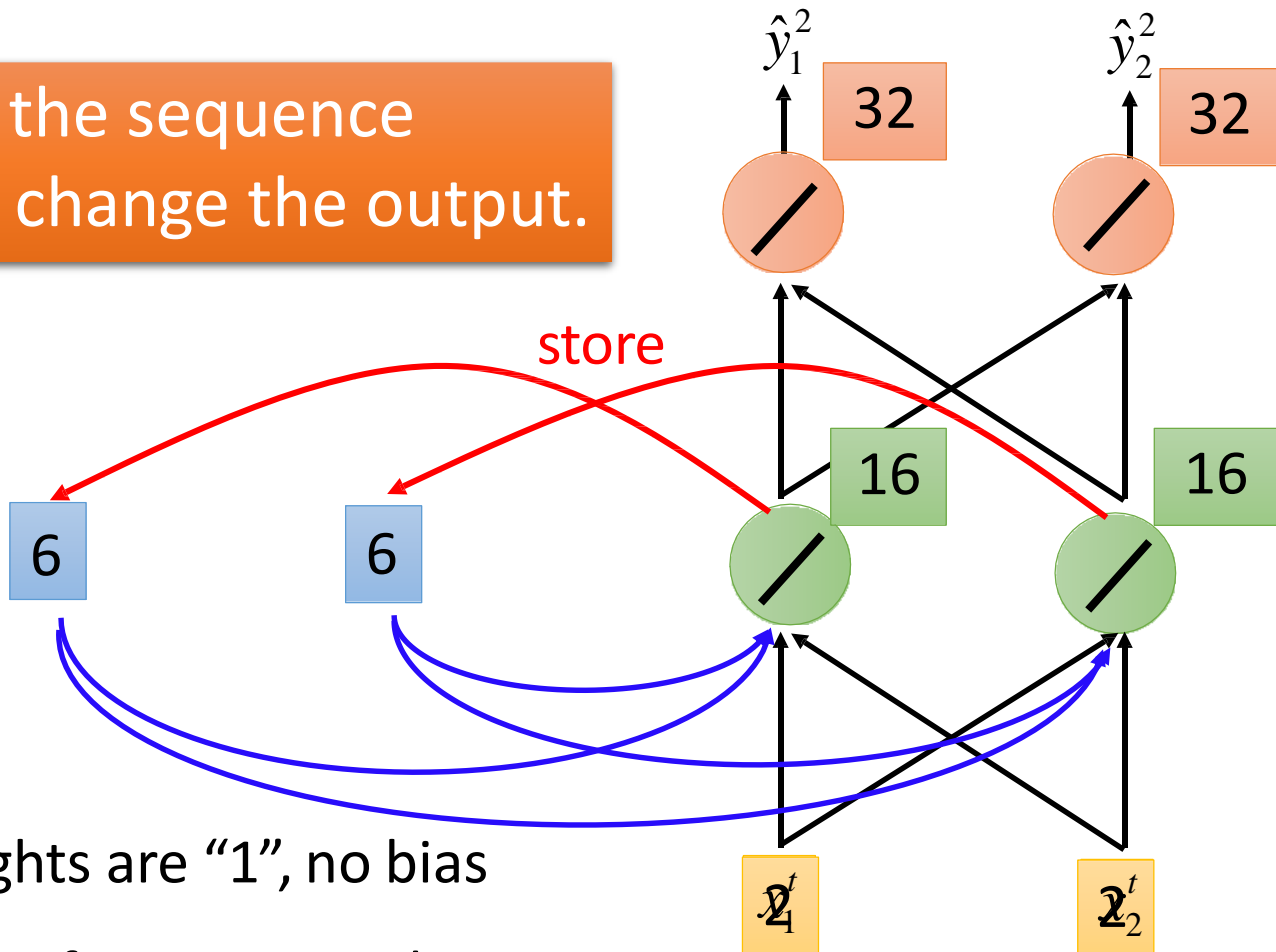
time: 2

Example

Input sequence: $\begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 2 \\ 2 \end{bmatrix} \dots$

output sequence: $\begin{bmatrix} 4 \\ 4 \end{bmatrix} \begin{bmatrix} 12 \\ 12 \end{bmatrix} \begin{bmatrix} 32 \\ 32 \end{bmatrix} \dots$

Changing the sequence order will change the output.



All the weights are "1", no bias

All activation functions are linear

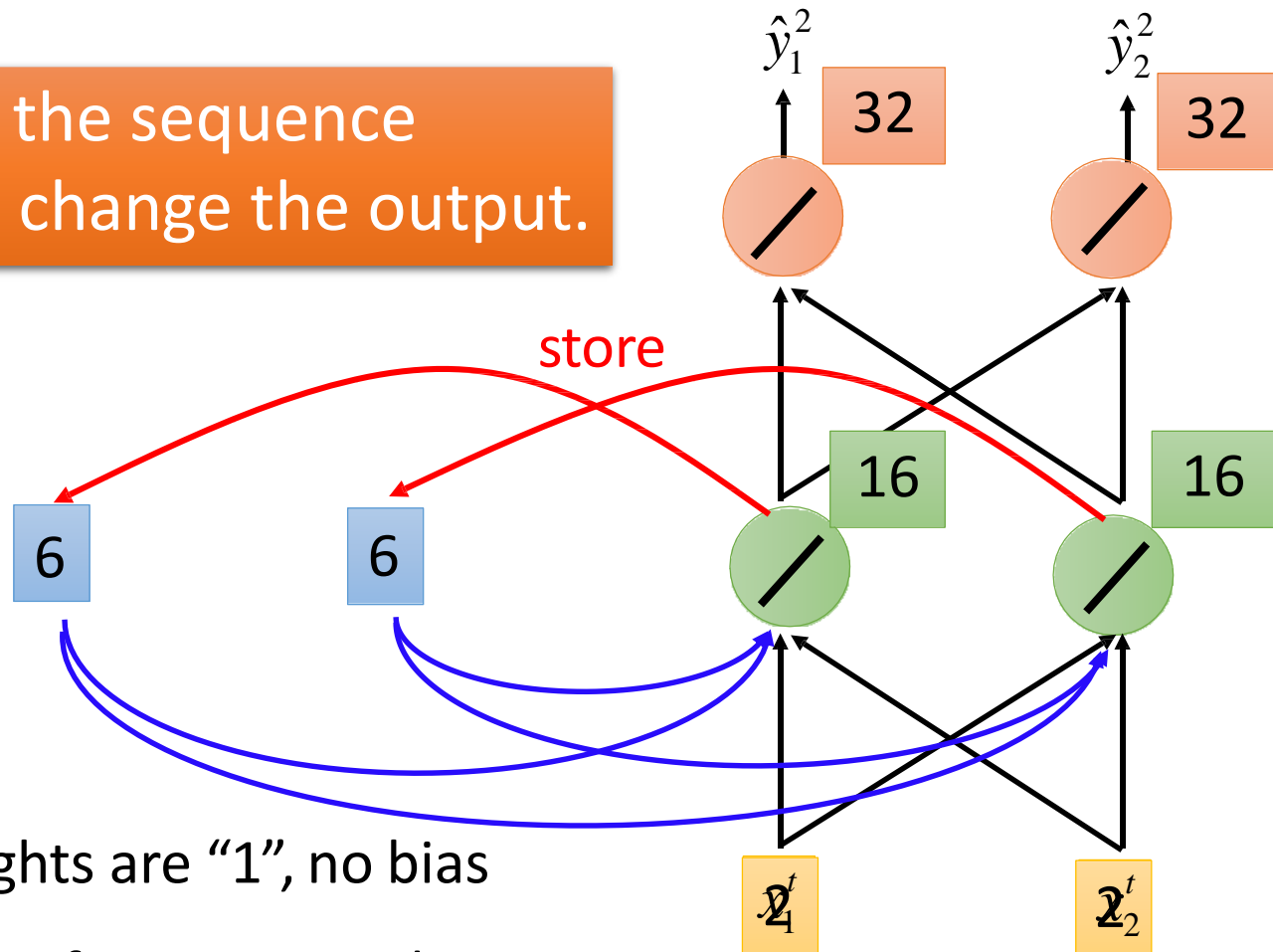
time: 3

Example

Input sequence: $\begin{bmatrix} 2 \\ 2 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \dots$

output sequence: $\begin{bmatrix} 8 \\ 8 \end{bmatrix} \begin{bmatrix} 20 \\ 20 \end{bmatrix} \begin{bmatrix} 44 \\ 44 \end{bmatrix} \dots$

Changing the sequence order will change the output.



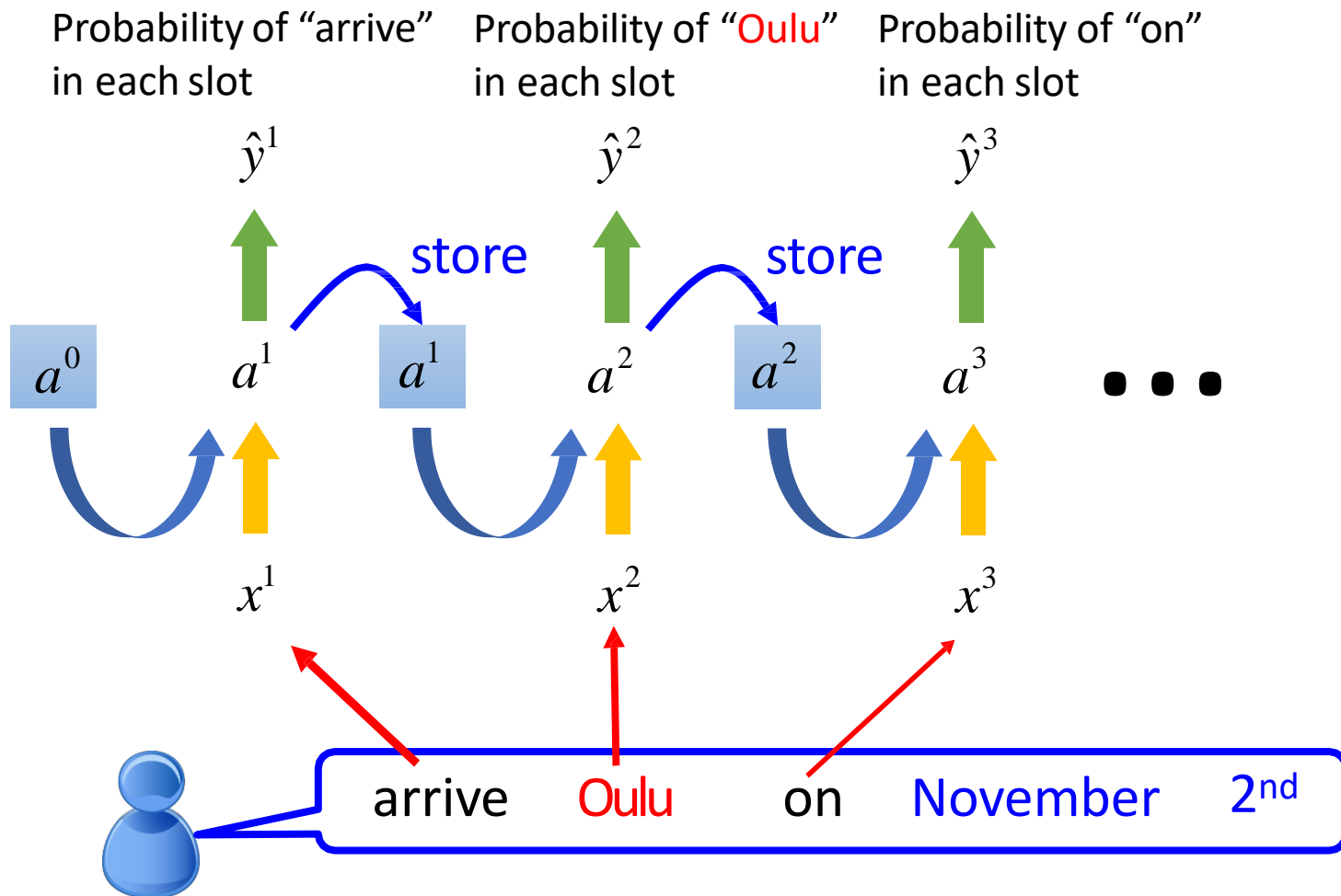
All the weights are "1", no bias

All activation functions are linear

time: 3

RNN

The same network is used again and again.



RNN

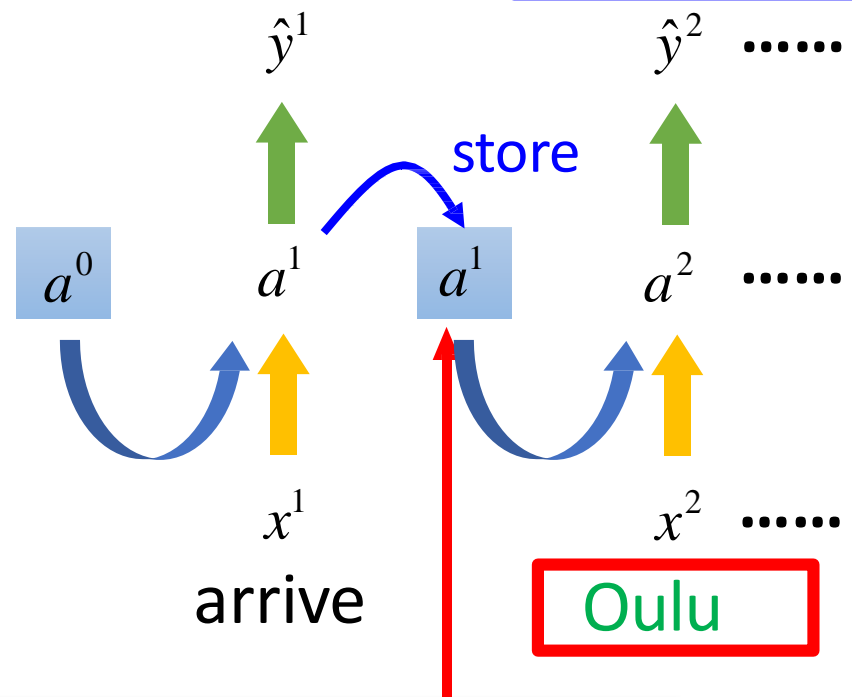
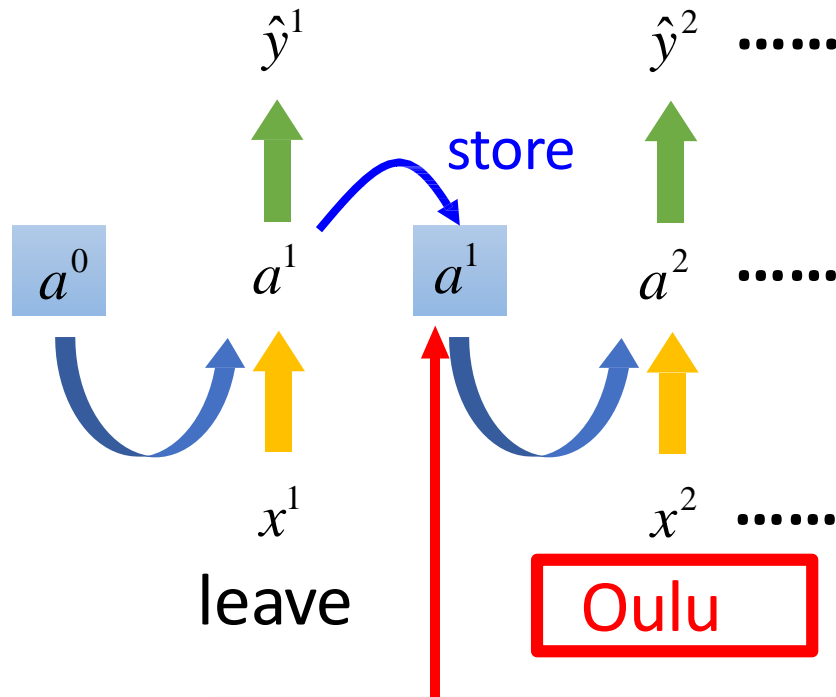
Different

Prob of “leave”
in each slot

Prob of “**Oulu**”
in each slot

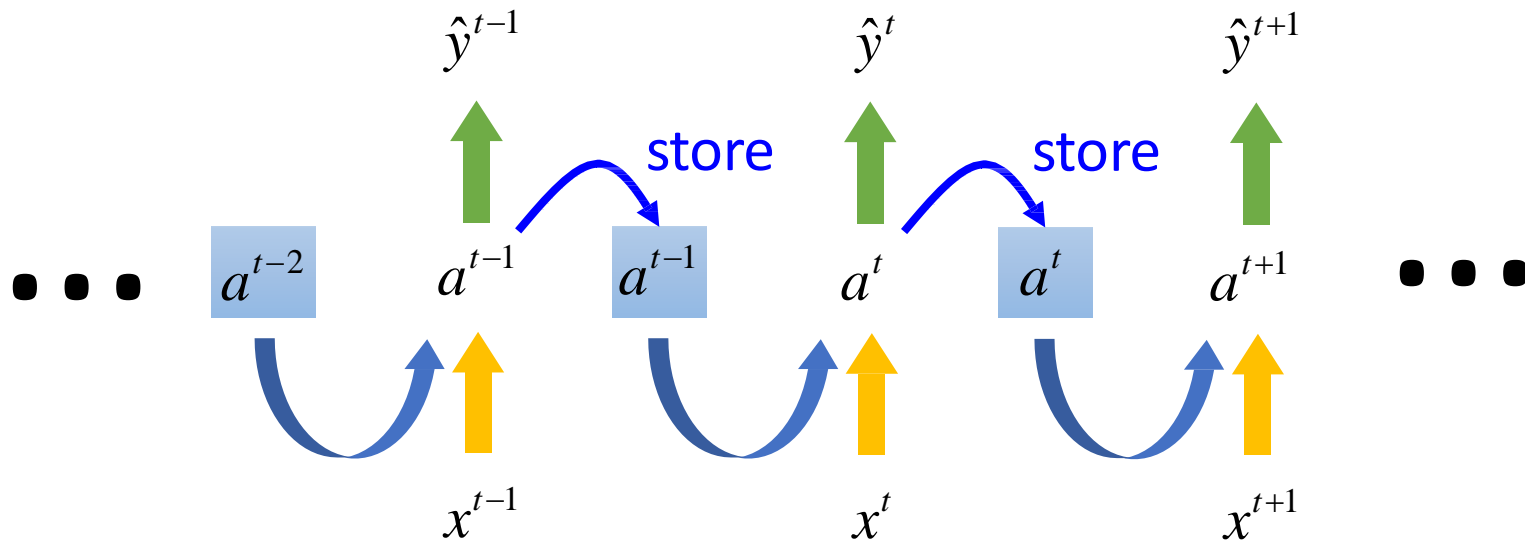
Prob of “arrive”
in each slot

Prob of “**Oulu**”
in each slot



The values stored in the memory is different.

RNN Training



Forward Propagation:

$$a^t = g(w_{aa}a^{t-1} + w_{ax}x^t + b_a)$$

$$\hat{y}^t = g(w_{ya}a^t + b_y)$$

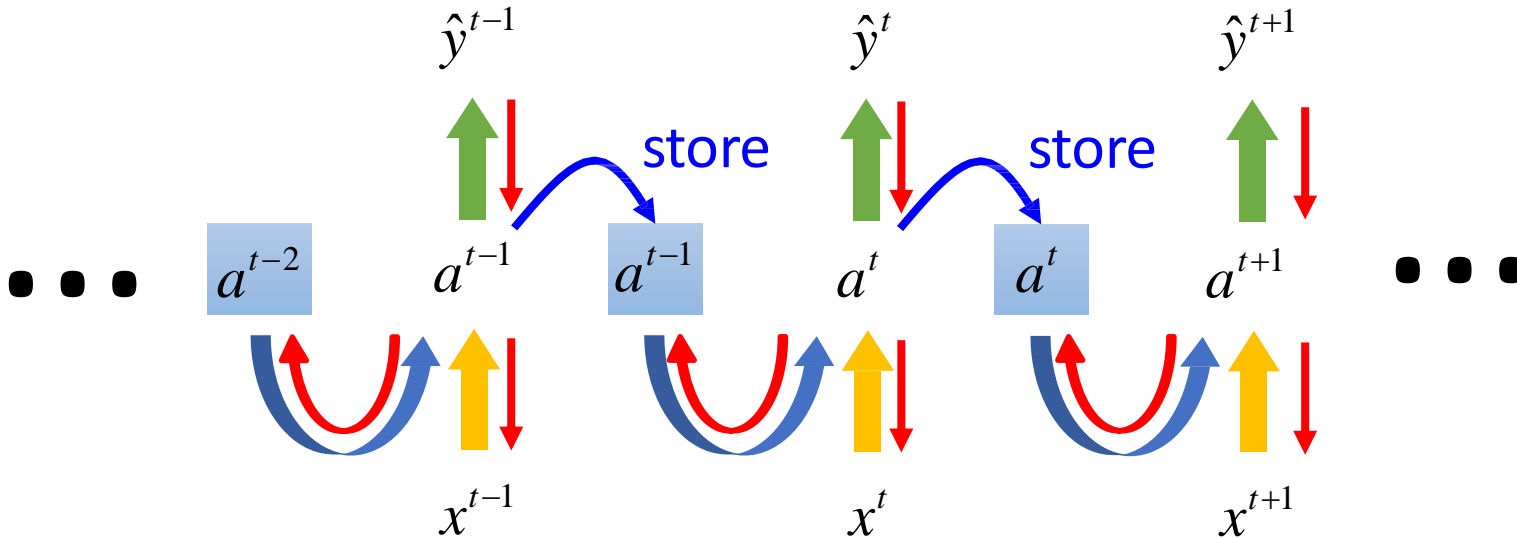


$$a^t = g(w_a[a^{t-1}, x^t] + b_a)$$

$$\hat{y}^t = g(w_ya^t + b_y)$$

RNN Training

Backpropagation
through time (BPTT)



Back Propagation: $w_a \leftarrow w_a - \alpha \frac{\partial L}{\partial w_a}$ α : learning rate (3)

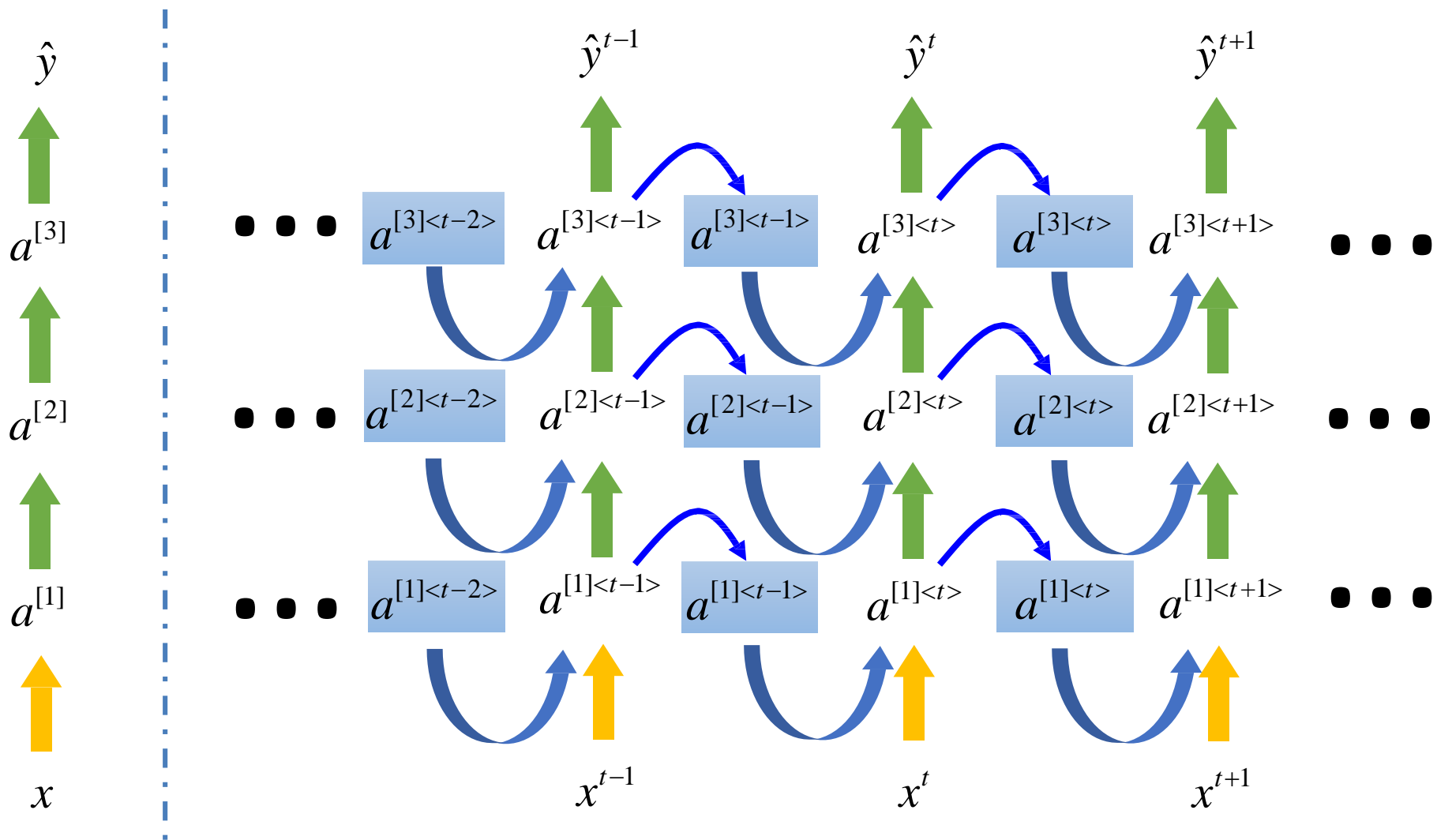
$$L^t(\hat{y}^t, y^t) = -y^t \log \hat{y}^t \quad (1)$$

$$L = \sum_{t=1}^{T_y} L^t(\hat{y}^t, y^t) \quad (2)$$

$$\frac{\partial L}{\partial w_a} = \sum_{t=1}^{T_y} \frac{\partial L^t}{\partial w_a} \quad (4)$$

$$\frac{\partial L^t}{\partial w_a} = \sum_{k=1}^t \frac{\partial L^t}{\partial \hat{y}^t} \frac{\partial \hat{y}^t}{\partial a^t} \frac{\partial a^t}{\partial a^k} \frac{\partial a^k}{\partial w_a} \quad (5)$$

Deep RNN



Bidirectional RNN (BRNN)

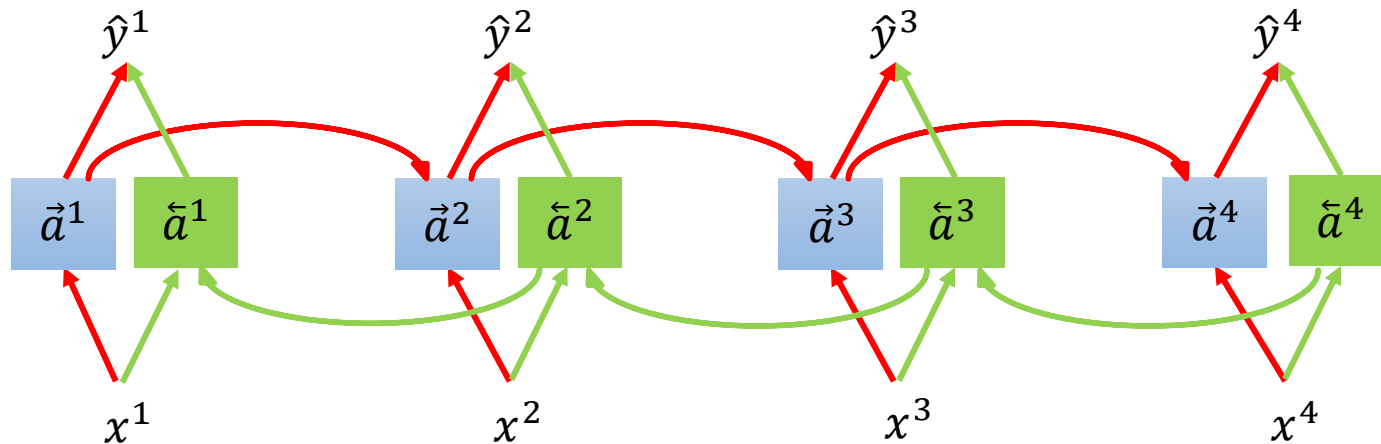


Beijing, the capital of China, I will arrive there on November 2nd.



Beijing, the capital of China, I will leave there on November 2nd.

Bidirectional RNN



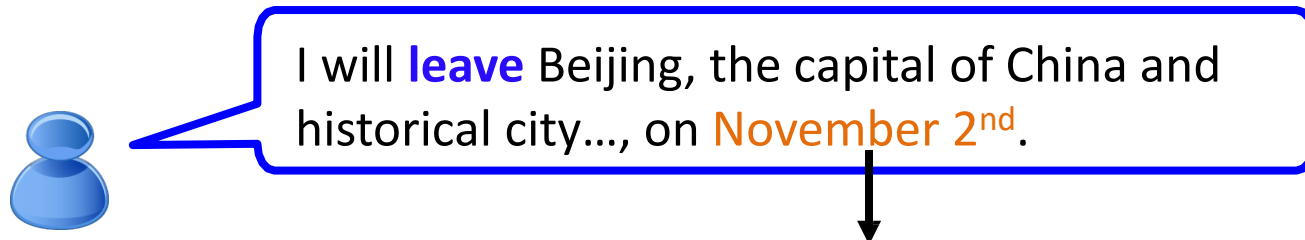
Advantage: take into account information from the past and from the future.

Disadvantage: need the entire sequence of data before you can make predictions anywhere

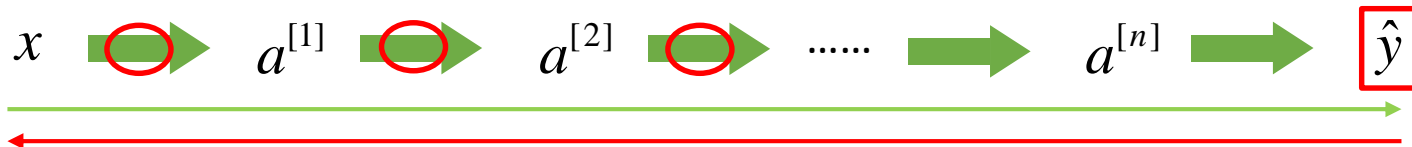
Vanishing gradients with RNNs



Time of arrival



Time of departure



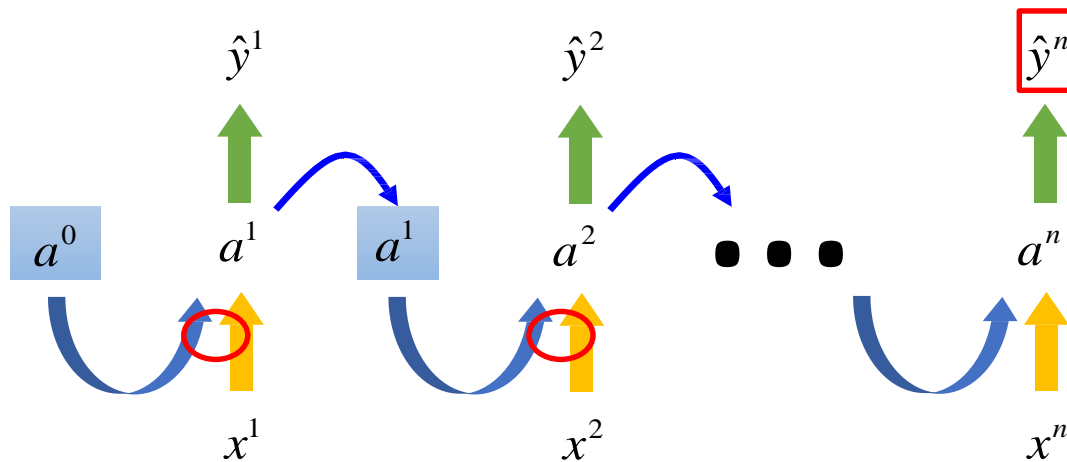
Vanishing gradients with RNNs



I will **arrive** Beijing, the capital of China and historical city, on November 2nd.



I will **leave** Beijing, the capital of China and historical city, on November 2nd.

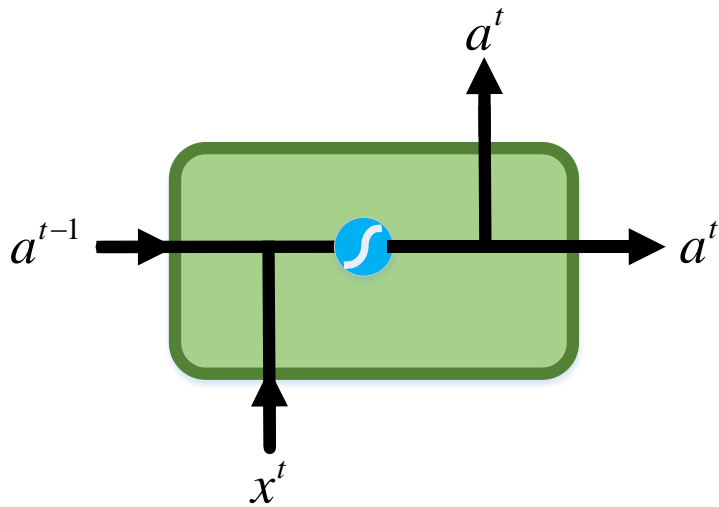


Exploding gradients?

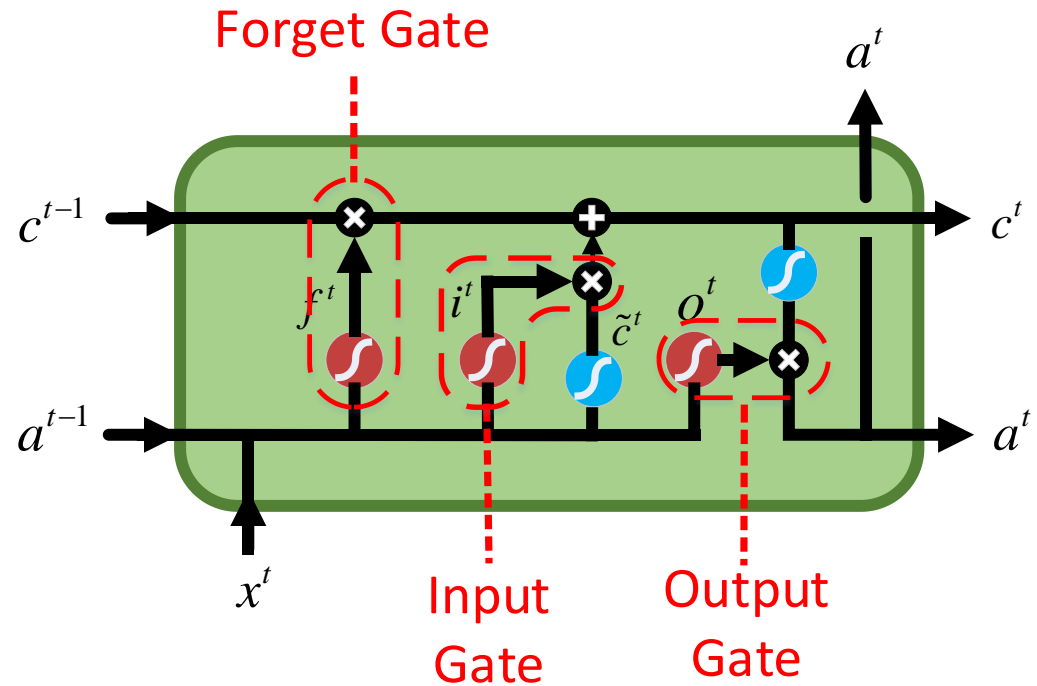
gradient clipping 

Long Short-term Memory (LSTM)

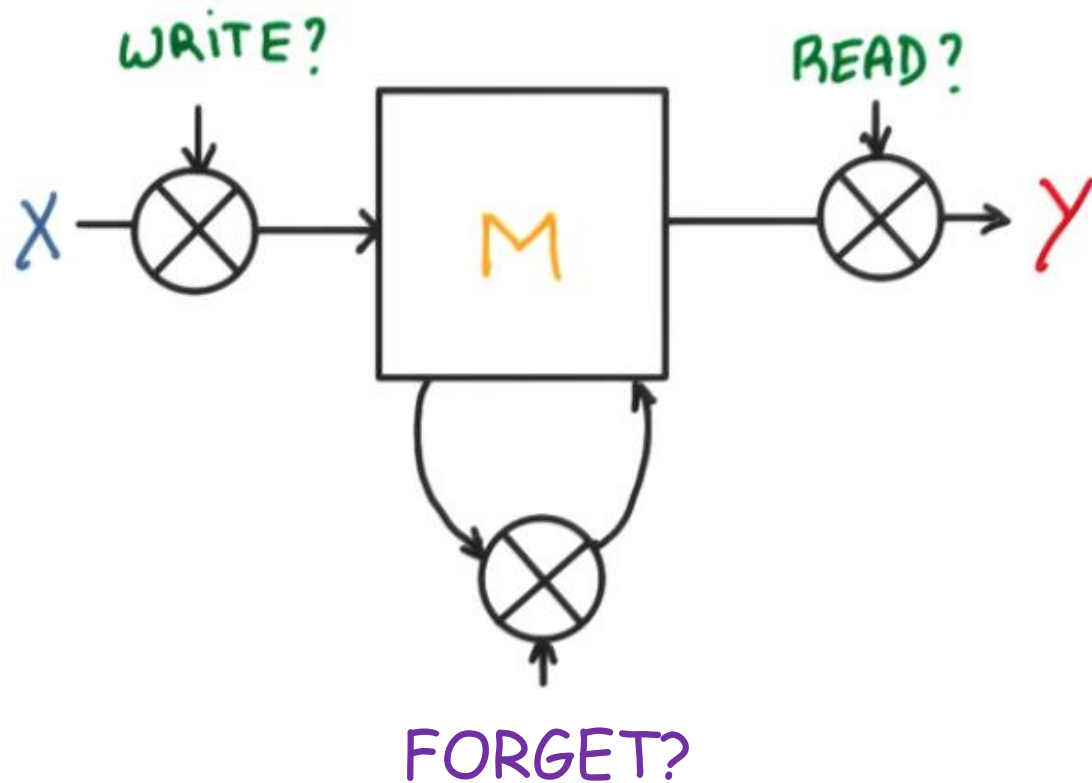
Basic RNN unit



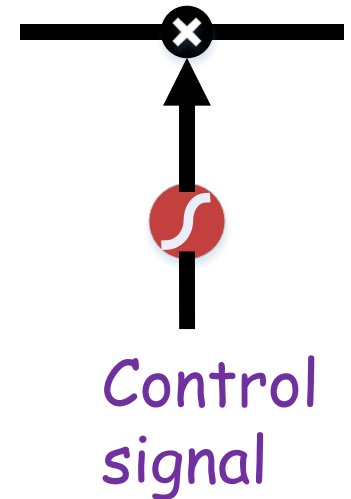
LSTM Unit



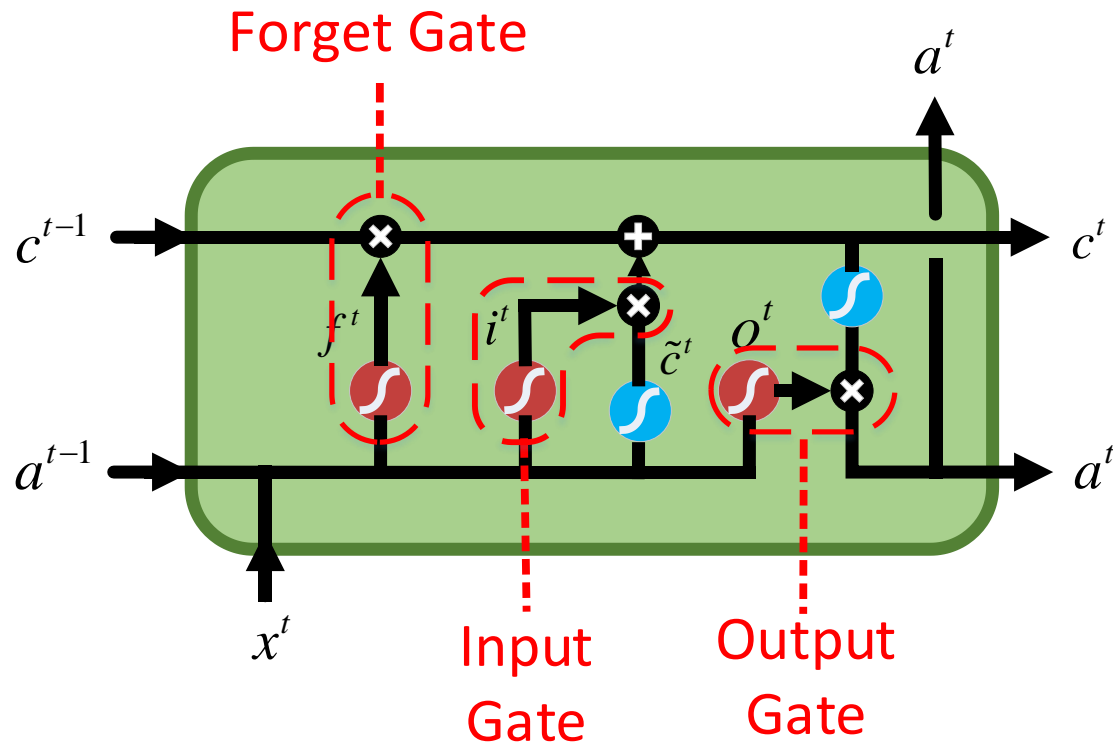
Long Short-term Memory (LSTM)



Gate Unit:



Long Short-term Memory (LSTM)




 sigmoid

 tanh

 pointwise
multiplication

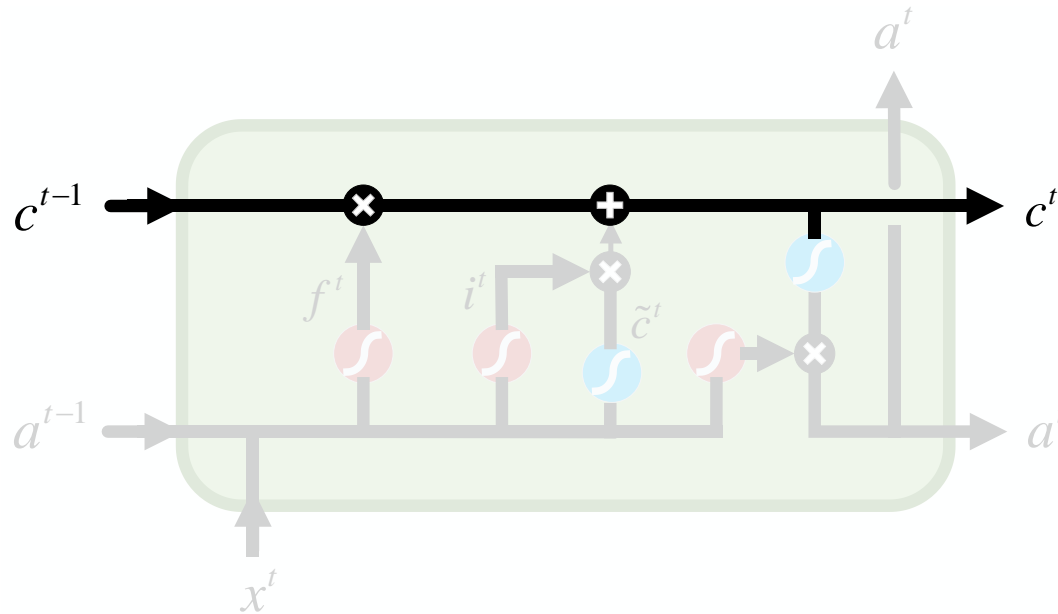
 pointwise
addition

 Concentrate

 Copy

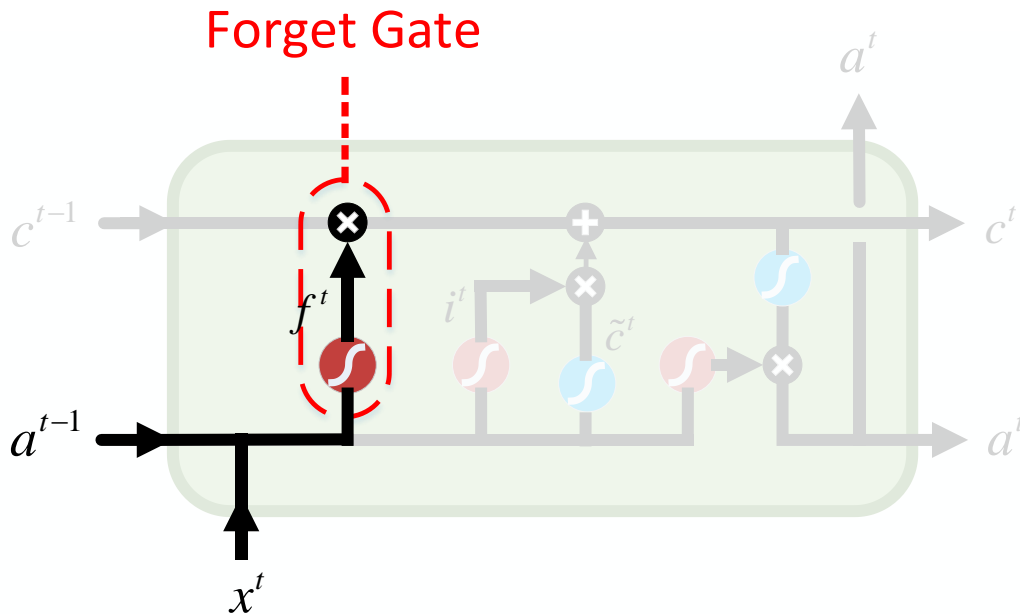
Long Short-term Memory (LSTM)

Memory Cell State:



Long Short-term Memory (LSTM)

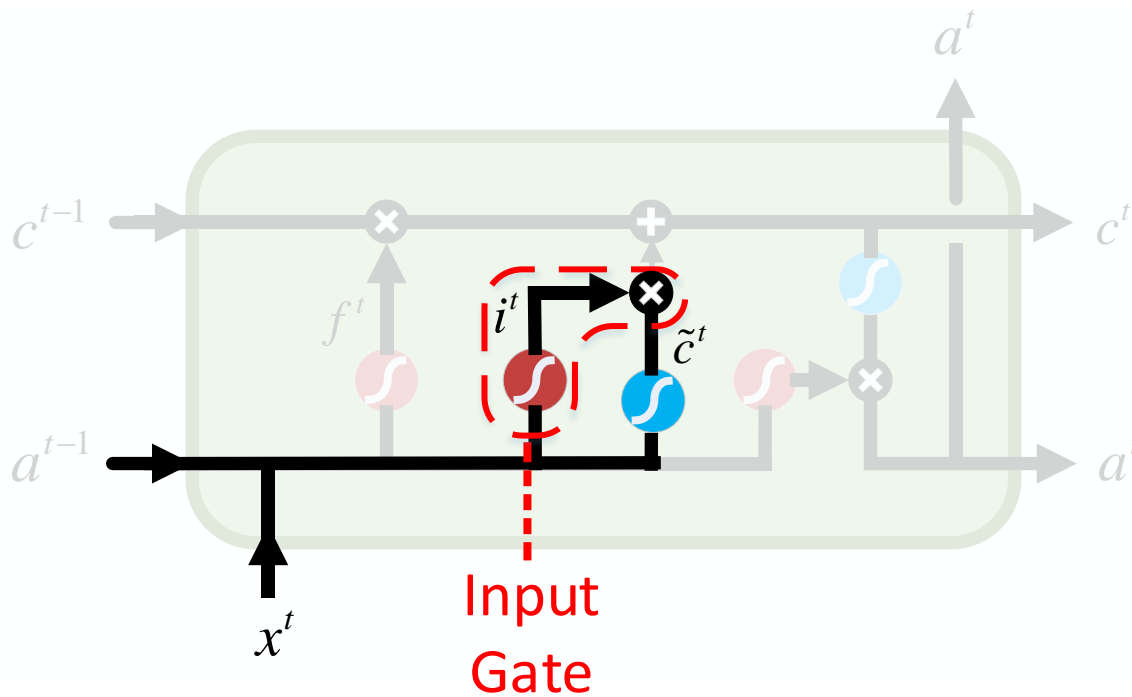
Step 1:



$$f^t = \sigma(w_f[a^{t-1}, x^t] + b_f)$$

Long Short-term Memory (LSTM)

Step 2:

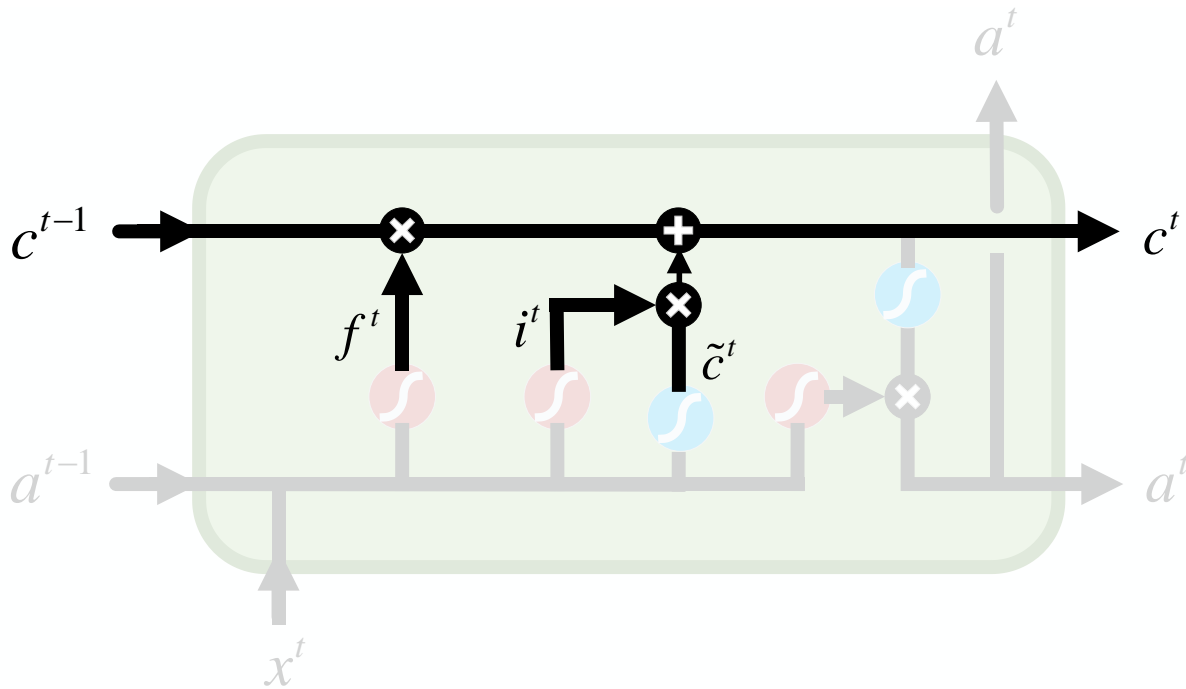


$$i^t = \sigma(w_i[a^{t-1}, x^t] + b_i)$$

$$\tilde{c}^t = \tanh(w_c[a^{t-1}, x^t] + b_c)$$

Long Short-term Memory (LSTM)

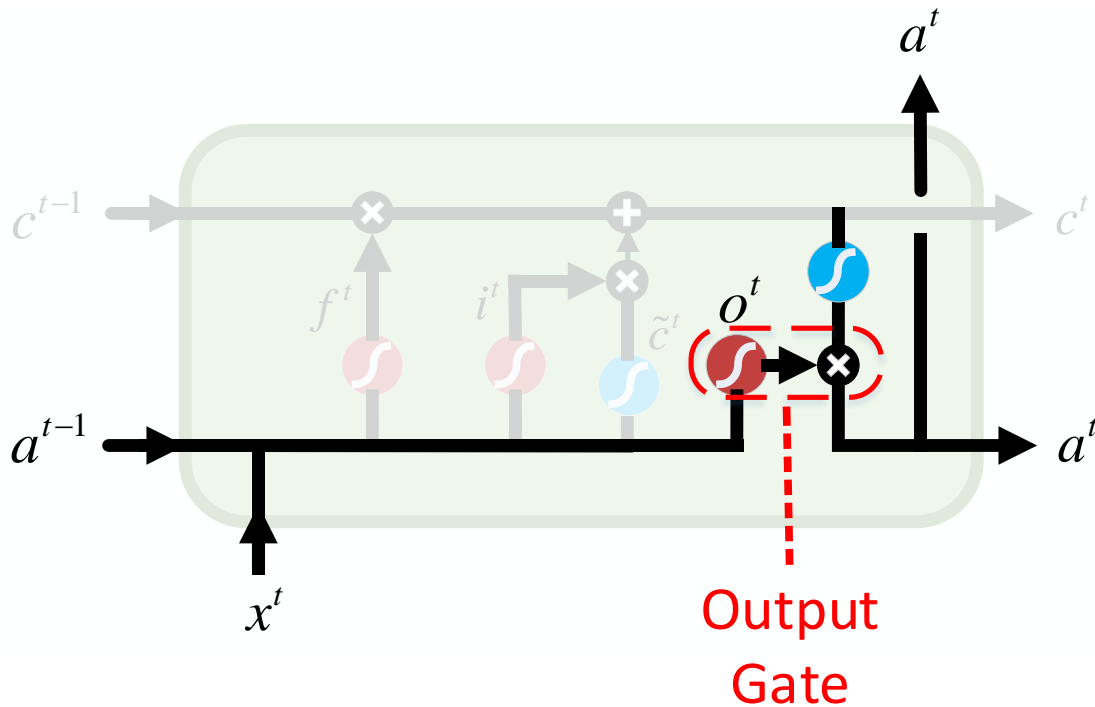
Step 3:



$$c^t = f^t * c^{t-1} + i^t * \tilde{c}^t$$

Long Short-term Memory (LSTM)

Step 4:

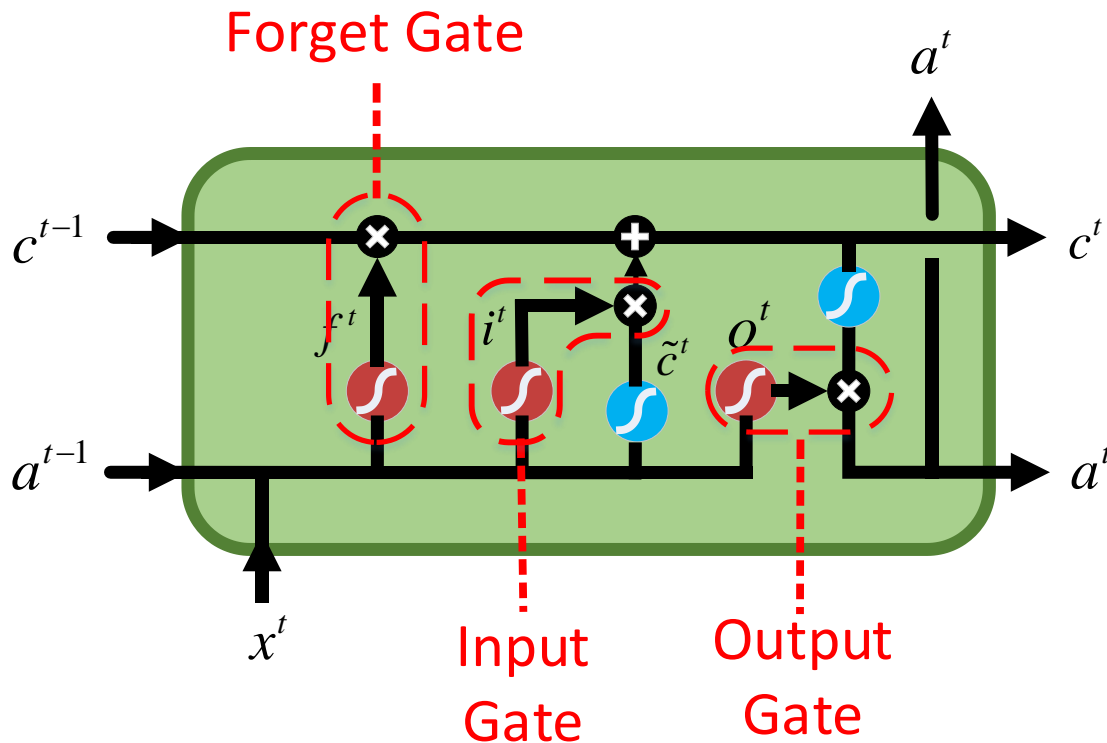


$$o^t = \sigma(w_o[a^{t-1}, x^t] + b_o)$$

$$a^t = o^t * \tanh(c^t)$$

Long Short-term Memory (LSTM)

Overall:



$$f^t = \sigma(w_f[a^{t-1}, x^t] + b_f)$$

$$i^t = \sigma(w_i[a^{t-1}, x^t] + b_i)$$

$$\tilde{c}^t = \tanh(w_c[a^{t-1}, x^t] + b_c)$$

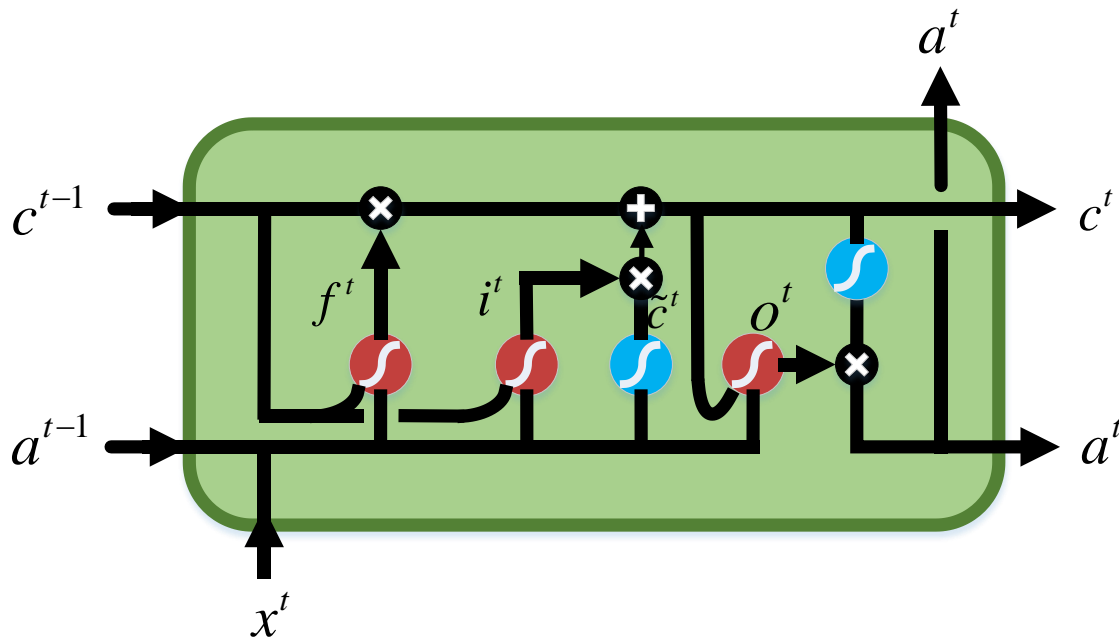
$$c^t = f^t * c^{t-1} + i^t * \tilde{c}^t$$

$$o^t = \sigma(w_o[a^{t-1}, x^t] + b_o)$$

$$a^t = o^t * \tanh(c^t)$$

Long Short-term Memory (LSTM)

Some Variants of LSTM :



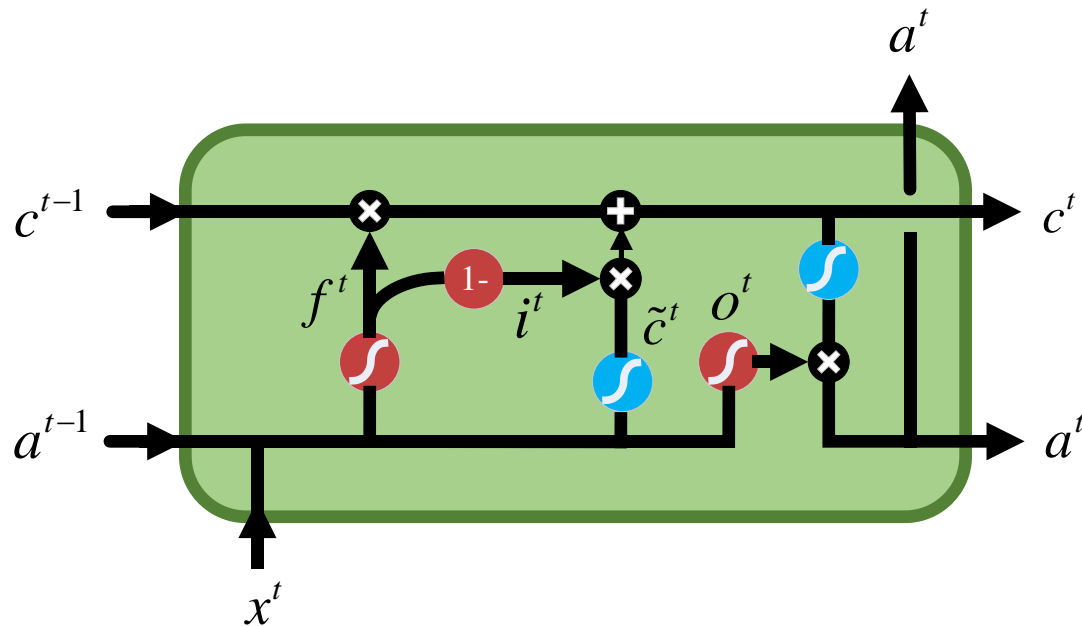
$$f^t = \sigma(w_f[c^{t-1}, a^{t-1}, x^t] + b_f)$$

$$i^t = \sigma(w_i[c^{t-1}, a^{t-1}, x^t] + b_i)$$

$$o^t = \sigma(w_o[c^t, a^{t-1}, x^t] + b_o)$$

Long Short-term Memory (LSTM)

Some Variants of LSTM:

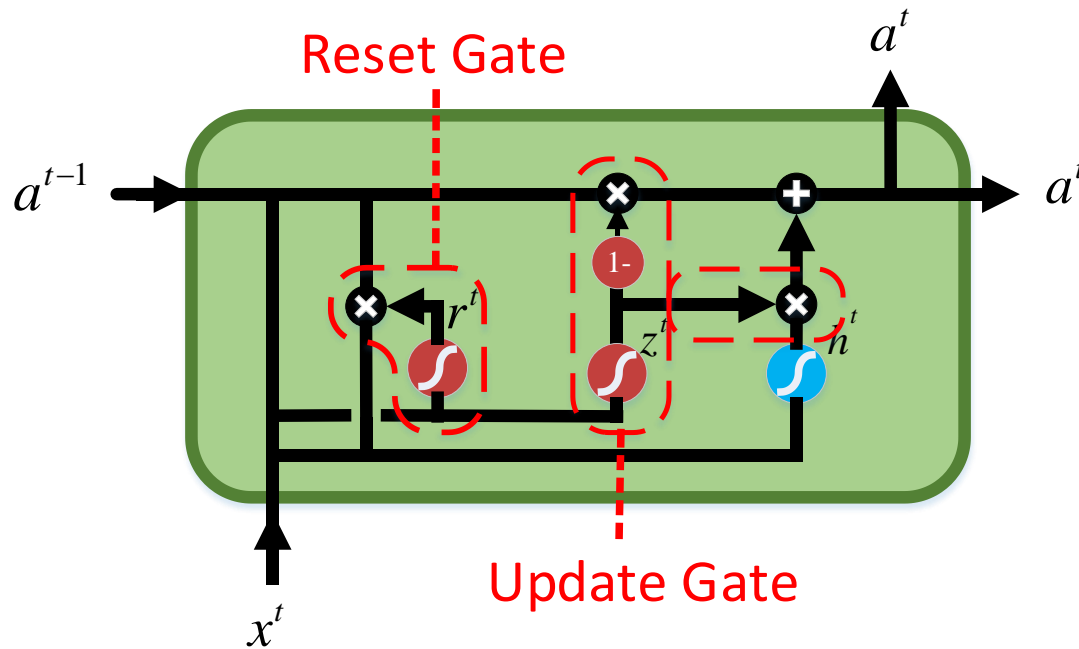


$$f^t = \sigma(w_f[c^{t-1}, a^{t-1}, x^t] + b_f)$$

$$i^t = 1 - f^t$$

$$c^t = f^t * c^{t-1} + (1 - f^t) * \tilde{c}^t$$

Gated Recurrent Unit (GRU)



$$z^t = \sigma(w_z[a^{t-1}, x^t])$$

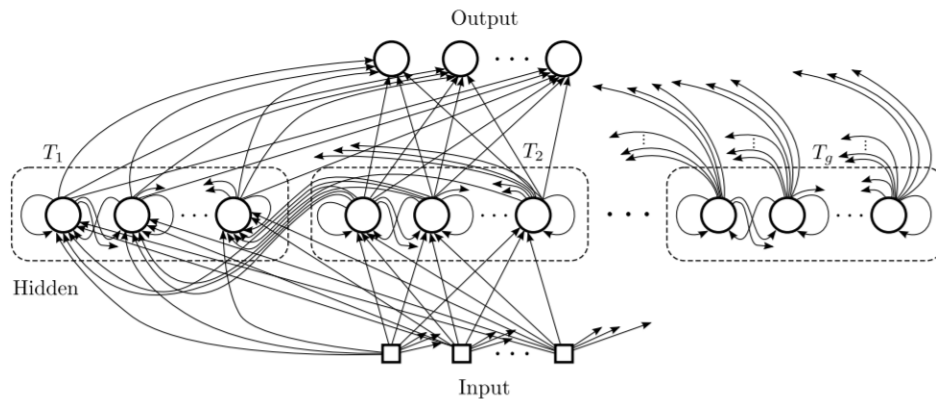
$$r^t = \sigma(w_r[a^{t-1}, x^t])$$

$$\tilde{a}^t = \tanh(w_{\tilde{a}}[r^t * a^{t-1}, x^t])$$

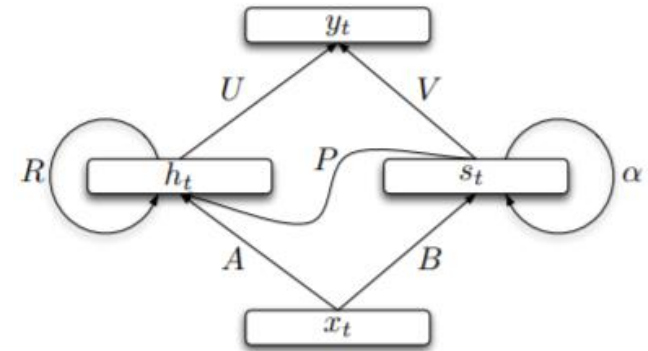
$$a^t = (1 - z^t) * a^{t-1} + z^t * \tilde{a}^t$$

Other variants of RNN

Clockwise RNN:



Structurally Constrained Recurrent Network(SCRN):



[1] Koutnik J, Greff K, Gomez F, et al. A clockwork rnn. arXiv preprint arXiv:1402.3511, 2014.

[2] Mikolov T, Joulin A, Chopra S, et al. Learning longer memory in recurrent neural networks. arXiv preprint arXiv:1412.7753, 2014.

RNN, LSTM, GRU in Pytorch

```
nn.RNN(input_size=512,hidden_size=1024,num_layers=3,  
        bias=False, batch_first=True, dropout=0.1, bidirectional=True)  
nn.LSTM(input_size=512,hidden_size=1024,num_layers=3,  
        bias=False, batch_first=True, dropout=0.1, bidirectional=True)  
nn.GRU(input_size=512,hidden_size=1024,num_layers=3,  
        bias=False, batch_first=True, dropout=0.1, bidirectional=True)
```

Main Arguments:

input_size: the dimension of x^t

hidden_size: the dimension of a^t and c^t

num_layers: number of recurrent layers

bias: the layer use bias or not

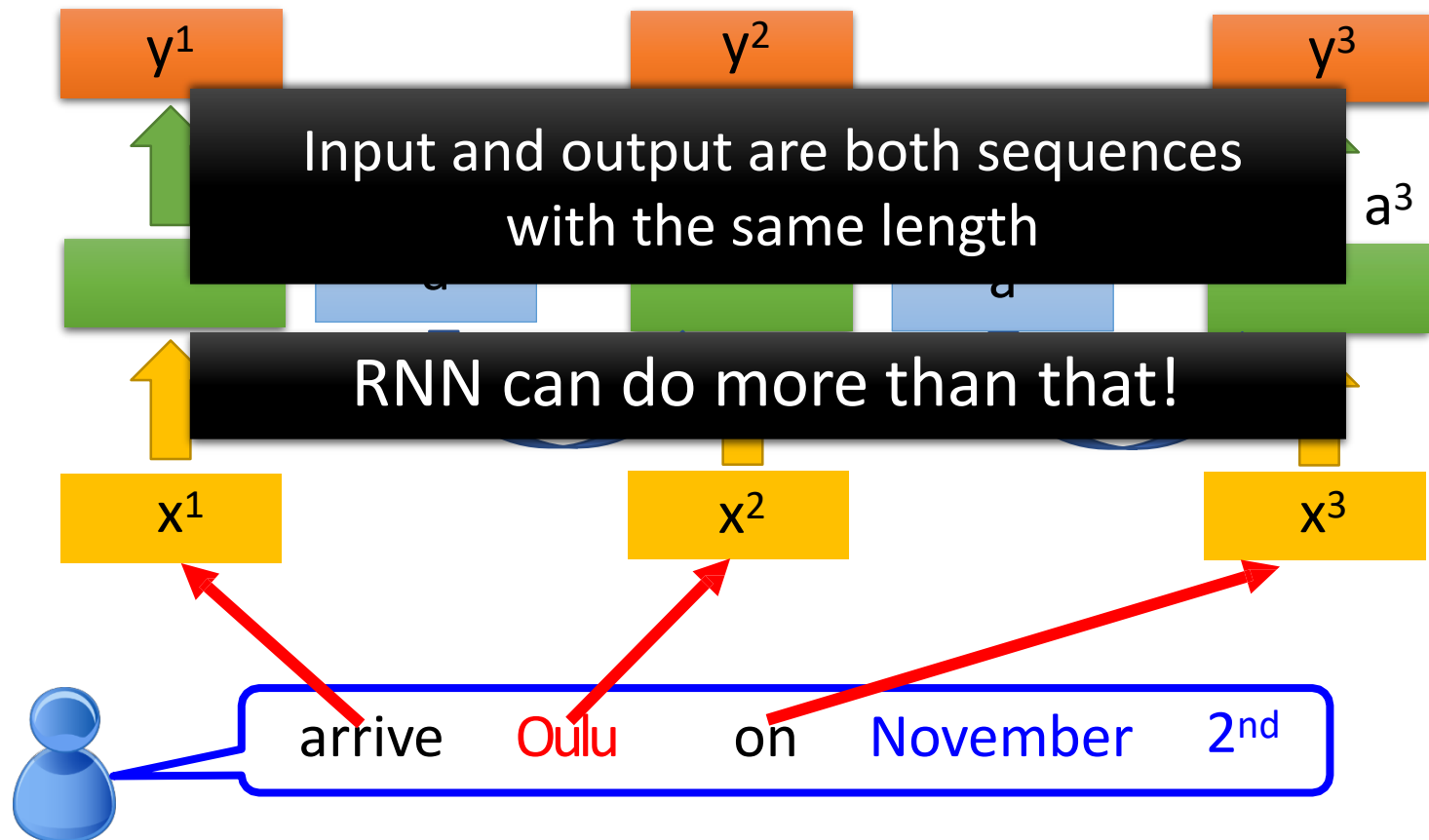
bidirectional: unidirectional or bidirectional

More Applications

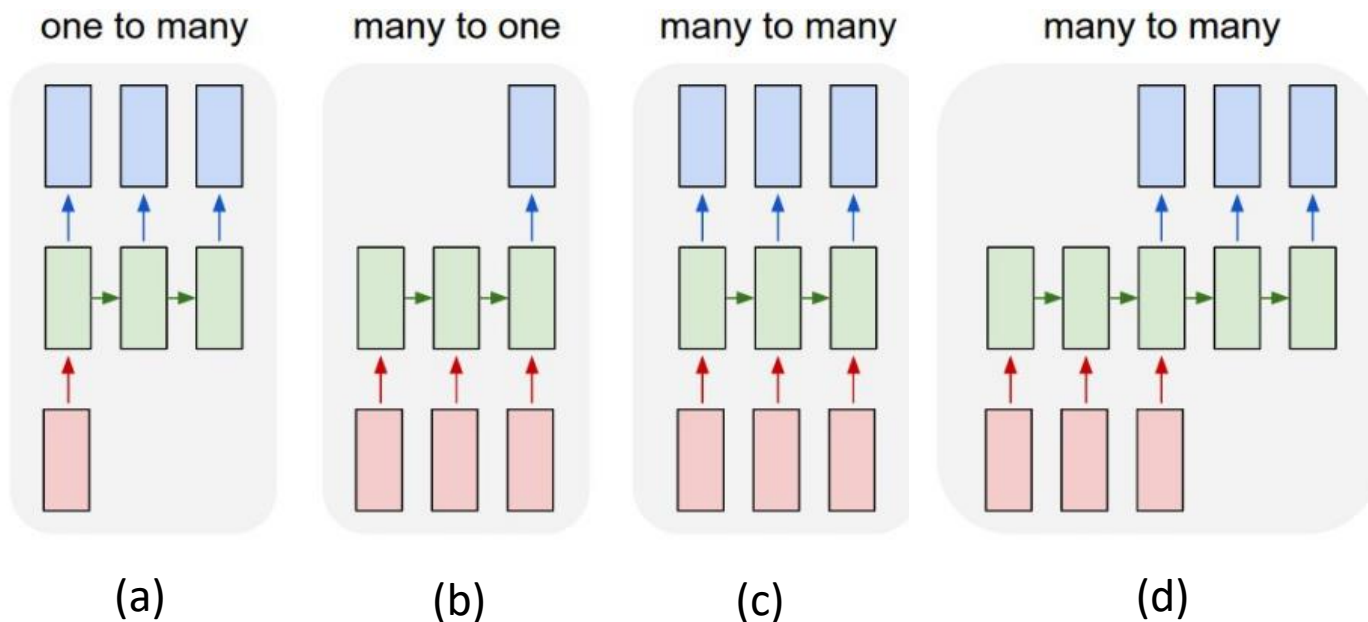
Probability of
“arrive” in each slot

Probability of
“**Oulu**” in each slot

Probability of
“on” in each slot



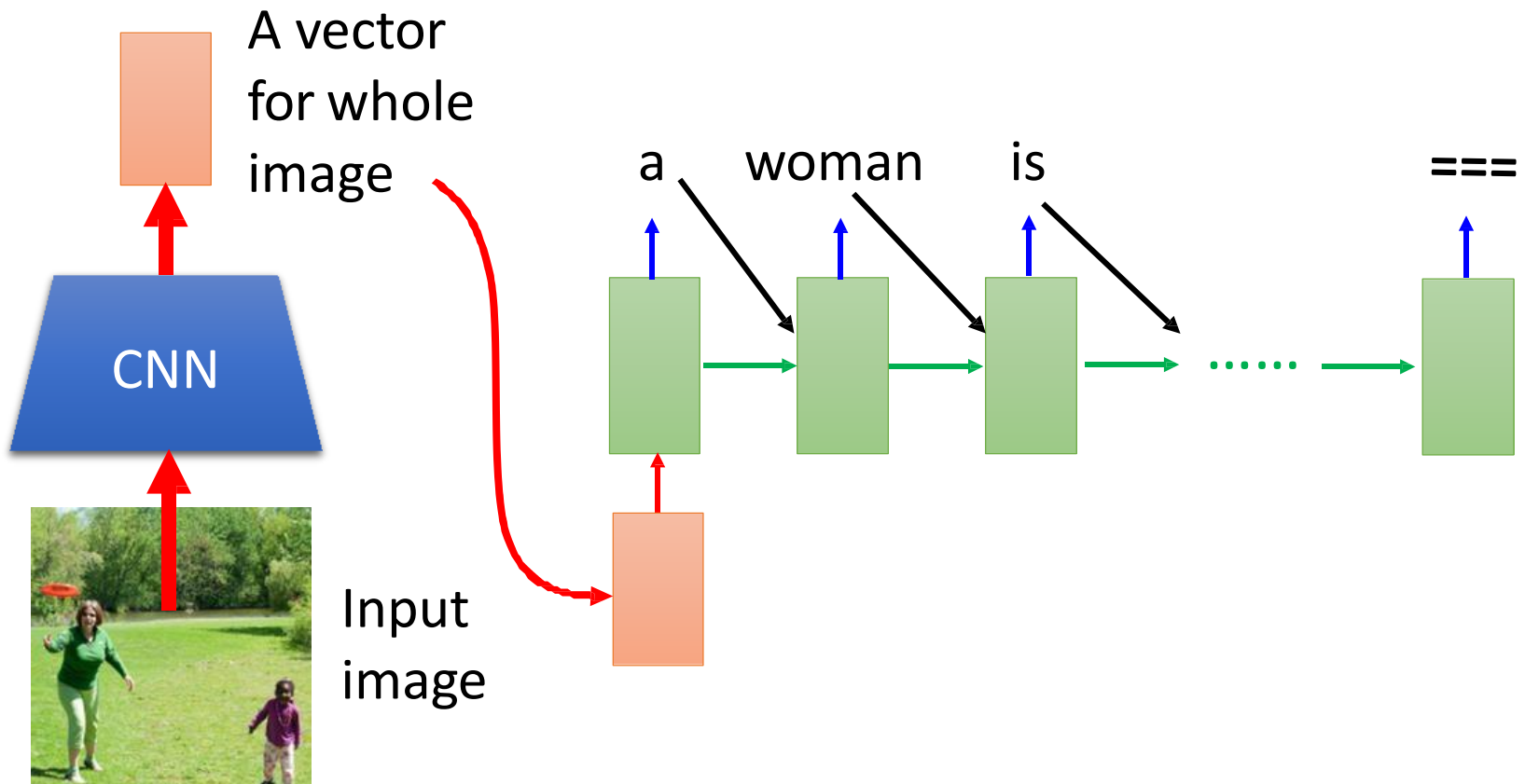
Applications



(a) Sequence output (e.g. image captioning). **(b)** Sequence input (e.g. sentiment analysis). **(c)** Syncd sequence input and output (e.g. speech recognition) **(d)** Sequence input and sequence output (e.g. Machine Translation).

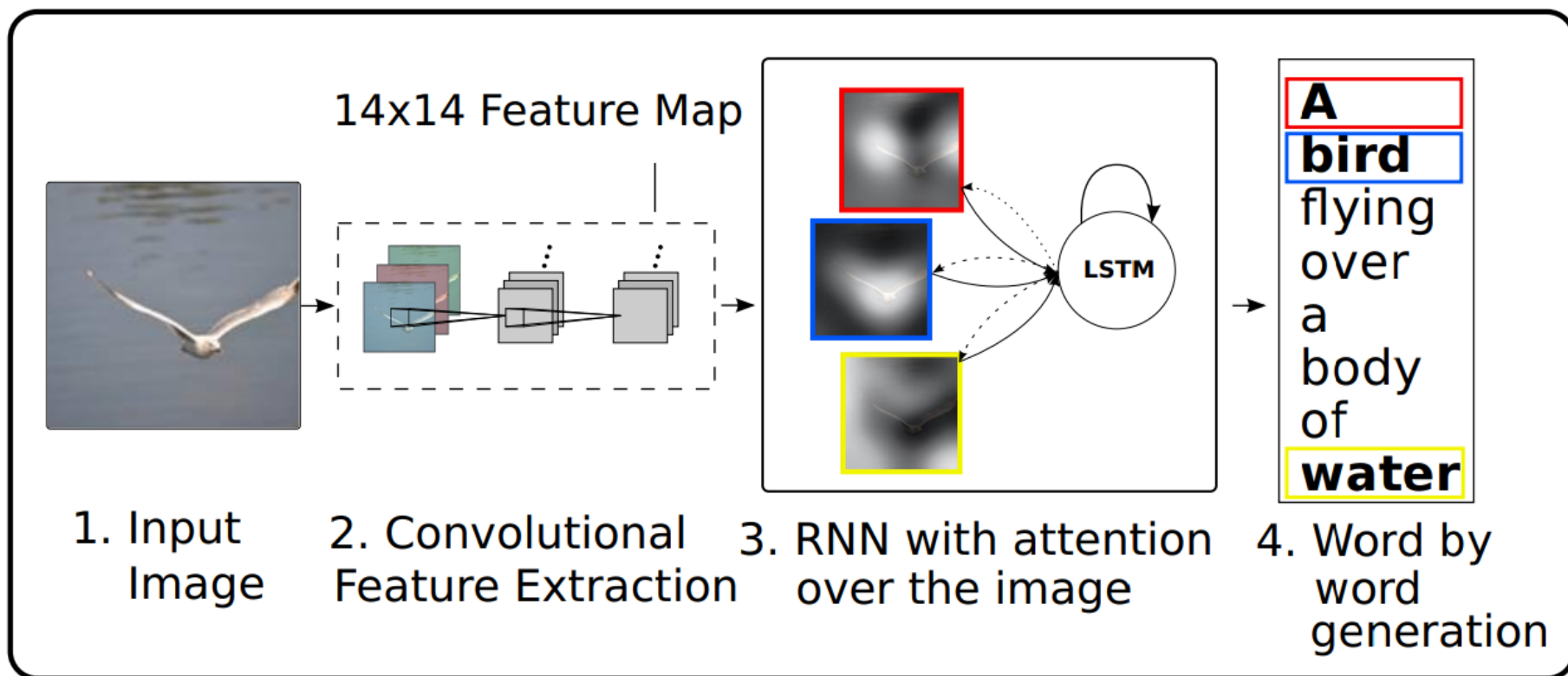
One to Many (Image Captioning)

- Input an image, but output a sequence of words



One to Many (Image Captioning)

- Input an image, but output a sequence of words



One to Many (Image Captioning)

- Reference paper list:

[1] Xu K, Ba J, Kiros R, et al. Show, attend and tell: Neural image caption generation with visual attention. ICML 2015.

[2] Karpathy A, Fei-Fei L. Deep visual-semantic alignments for generating image descriptions. CVPR 2015.

[3] You Q, Jin H, Wang Z, et al. Image captioning with semantic attention. CVPR 2016.

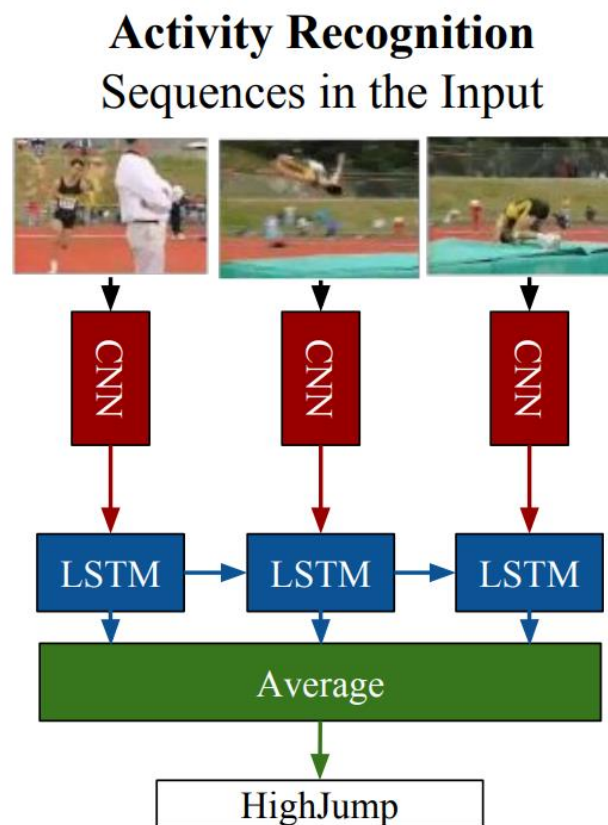
[4] Gan Z, Gan C, He X, et al. Semantic compositional networks for visual captioning. CVPR 2017.

[5] Anderson P, He X, Buehler C, et al. Bottom-up and top-down attention for image captioning and visual question answering. CVPR 2018.

[6] Dai B, Fidler S, Lin D. A neural compositional paradigm for image captioning. NIPS 2018.

Many to One (Video Classification)

- Input an video, but output a class score



Many to One (Video Classification)

- Input an video, but output class scores

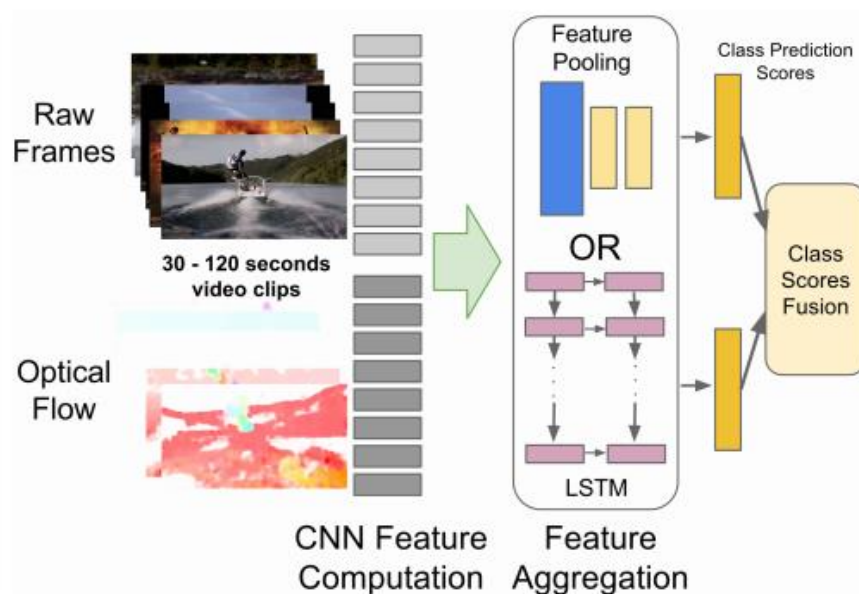


Figure 1: Overview of our approach.

Many to One (Video Classification)

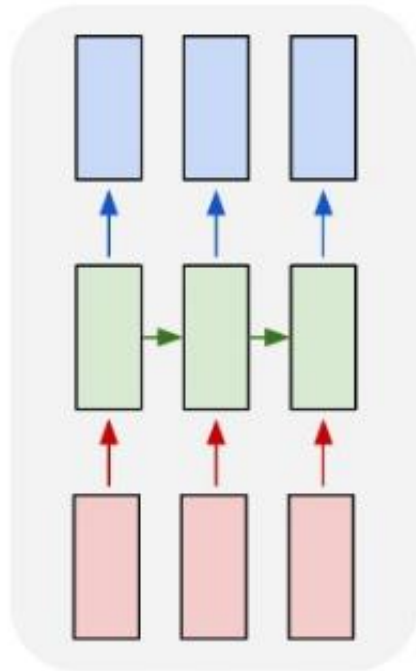
- Reference paper list:

- [1] Donahue J, Anne Hendricks L, Guadarrama S, et al. Long-term recurrent convolutional networks for visual recognition and description. CVPR 2015.
- [2] Yue-Hei Ng J, Hausknecht M, Vijayanarasimhan S, et al. Beyond short snippets: Deep networks for video classification. CVPR 2015.
- [3] Simonyan K, Zisserman A. Two-stream convolutional networks for action recognition. NIPS 2015.
- [4] Feichtenhofer C, Pinz A, Zisserman A. Convolutional two-stream network fusion for video action recognition. CVPR 2016.
- [5] Wang L, Xiong Y, Wang Z, et al. Temporal segment networks: Towards good practices for deep action recognition. ECCV 2016.
- [6] Xu H, Das A, Saenko K. R-c3d: Region convolutional 3d network for temporal activity detection. ICCV 2017.

Many to Many (Synced)

- Both input and output are sequences, **Synchronizing in temporal.**
- Output sequence is shorter or the same length as input sequence.

many to many



Same length: slot filling

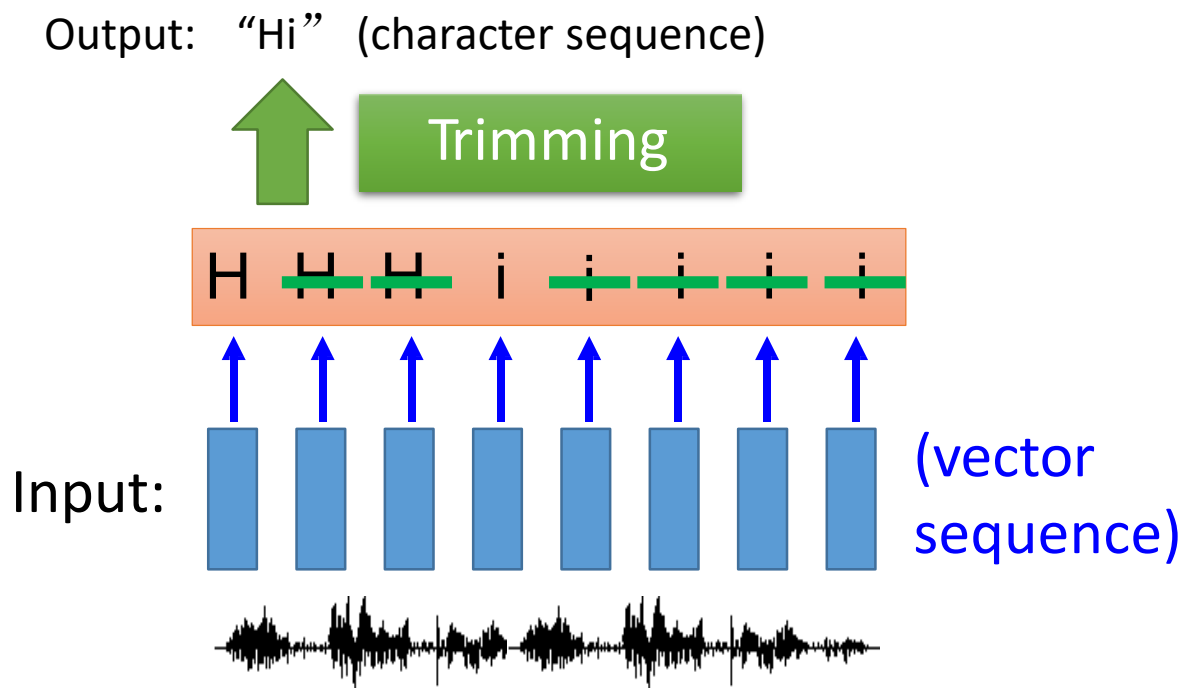
different length: speech recognition

Many to Many (Speech Recognition)

- Both input and output are both sequences, **but the output is shorter.**

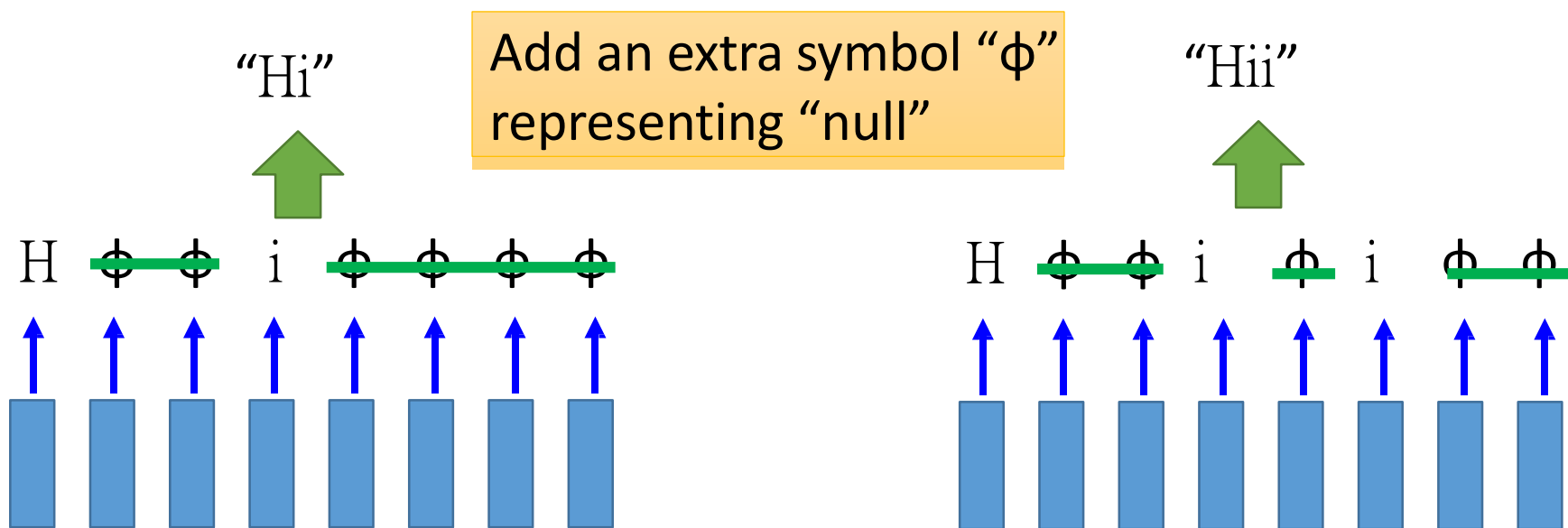
Problem?

“Helo”, Why can’t
it be “Hello”



Many to Many (Speech Recognition)

- Both input and output are both sequences, **but the output is shorter.**
- Connectionist Temporal Classification (CTC)



Many to Many (Speech Recognition)

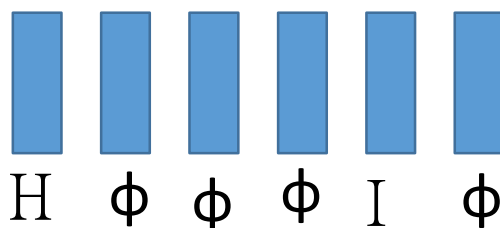
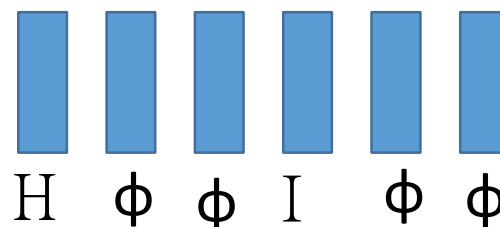
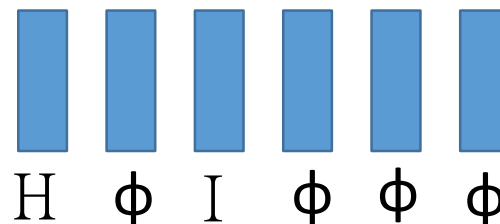
- CTC: Training

Acoustic
Features:



Label: H I

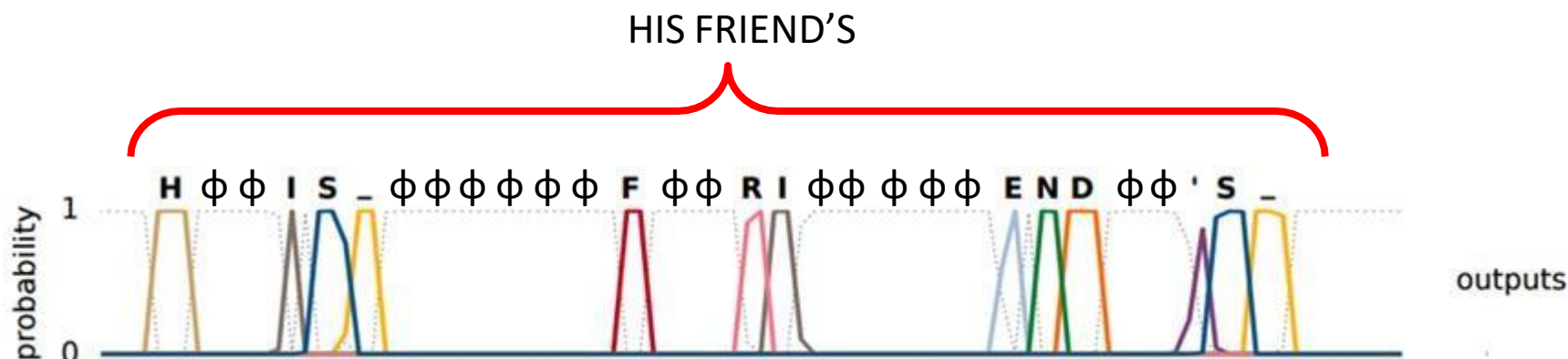
All possible alignments
are considered as correct.



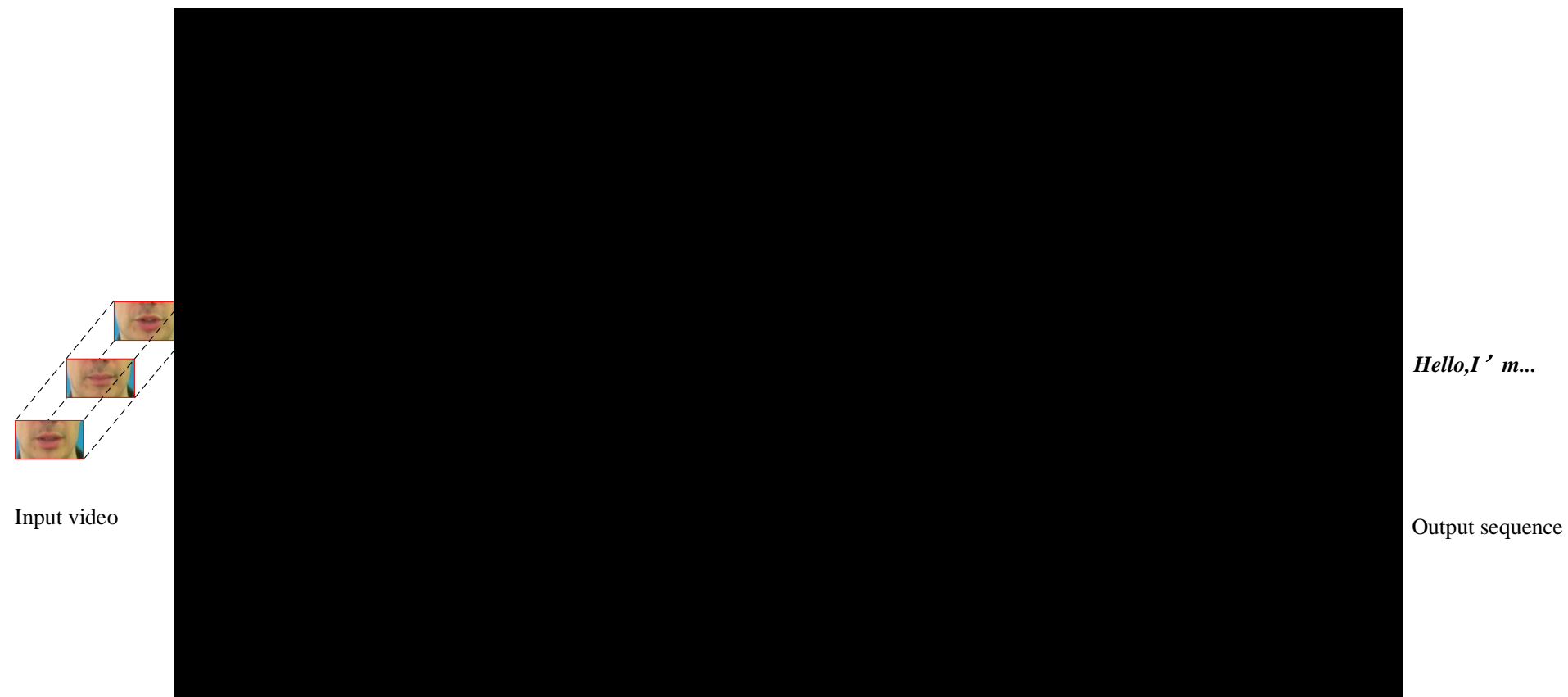
⋮

Many to Many (Speech Recognition)

- CTC: example



Many to Many (Lip Reading)



Many to Many (Lip Reading)

Method	Unseen Speakers		Overlapped Speakers	
	CER	WER	CER	WER
Hearing-Impaired Person (avg)	—	47.7%	—	—
Baseline-LSTM	38.4%	52.8%	15.2%	26.3%
Baseline-2D	16.2%	26.7%	4.3%	11.6%
Baseline-NoLM	6.7%	13.6%	2.0%	5.6%
LipNet	6.4%	11.4%	1.9%	4.8%

Many to Many (Lip Reading)

- Reference paper list:

[1] Assael Y M, Shillingford B, Whiteson S, et al. Lipnet: End-to-end sentence-level lipreading. arXiv:1611.01599, 2016.

[2] Chung J S, Senior A, Vinyals O, et al. Lip reading sentences in the wild. CVPR 2017.

[3] Stafylakis T, Tzimiropoulos G. Combining residual networks with LSTMs for lipreading. arXiv:1703.04105, 2017.

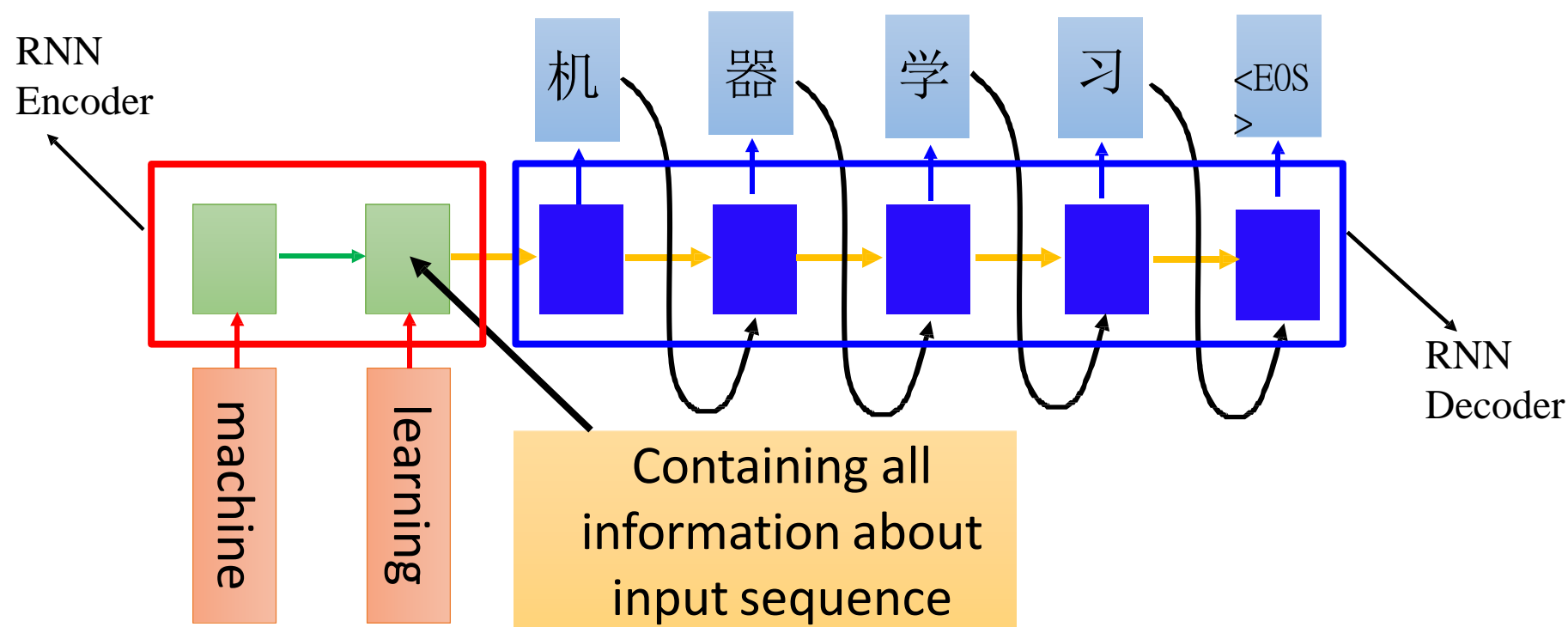
[4] Afouras T, Chung J S, Senior A, et al. Deep audio-visual speech recognition. IEEE TPAMI, 2018.

[5] Shillingford B, Assael Y, Hoffman M W, et al. Large-scale visual speech recognition. arXiv:1807.05162, 2018.

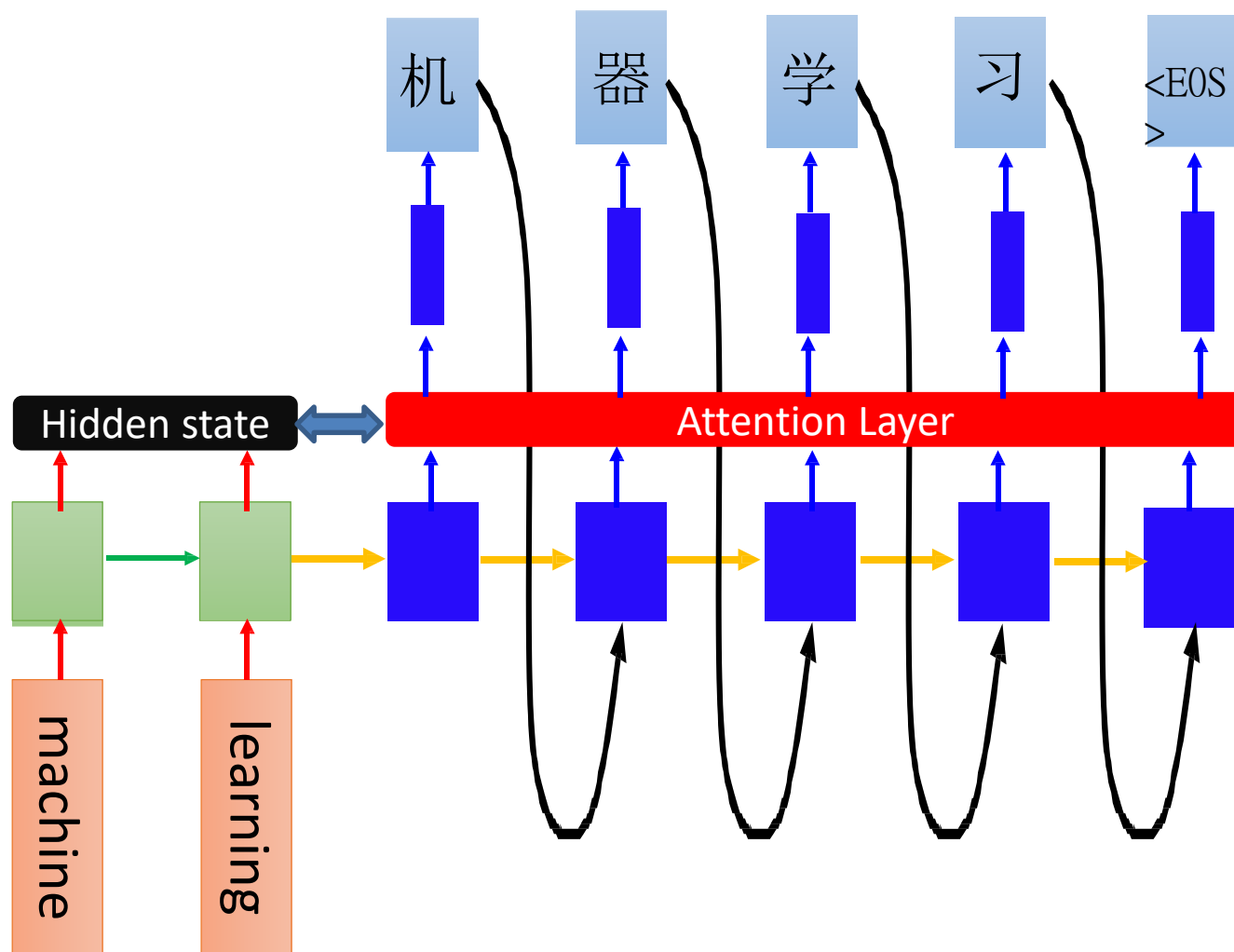
[6] Zhang X, Cheng F, Wang S. Spatio-Temporal Fusion based Convolutional Sequence Learning for Lip Reading. ICCV 2019.

Many to Many (Seq2seq)

- Both input and output are both sequences **with different lengths**. → **Sequence to sequence learning**
 - E.g. **Machine Translation** (machine learning → 机器学习)

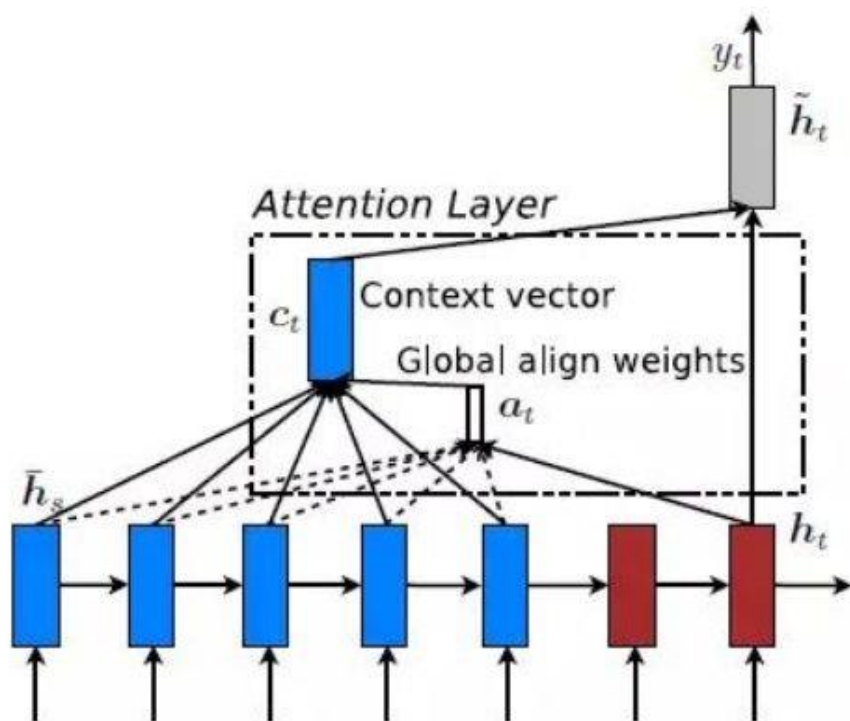


Many to Many (Seq2seq-Att)



Many to Many (Seq2seq-Att)

- Attention layer:



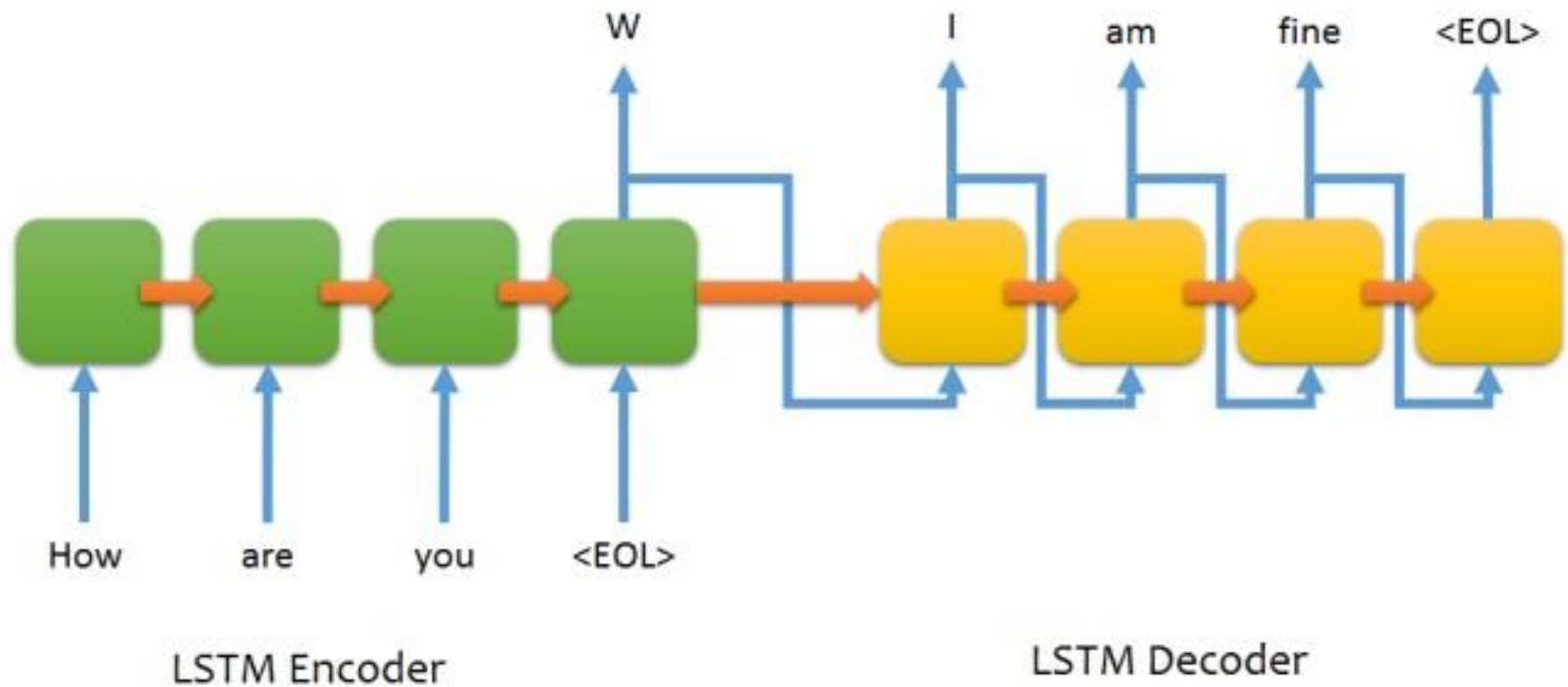
$$\alpha_{ts} = \frac{\exp(\text{score}(h_t, \bar{h}_s))}{\sum_{s'=1}^S \exp(\text{score}(h_t, \bar{h}_{s'}))}$$

Attention weight

$$c_t = \sum_s \alpha_{ts} \bar{h}_s$$

Context vector

Demo: Chat-bot



Demo: Visual Question Answering



What is the mustache
made of?

AI System

bananas

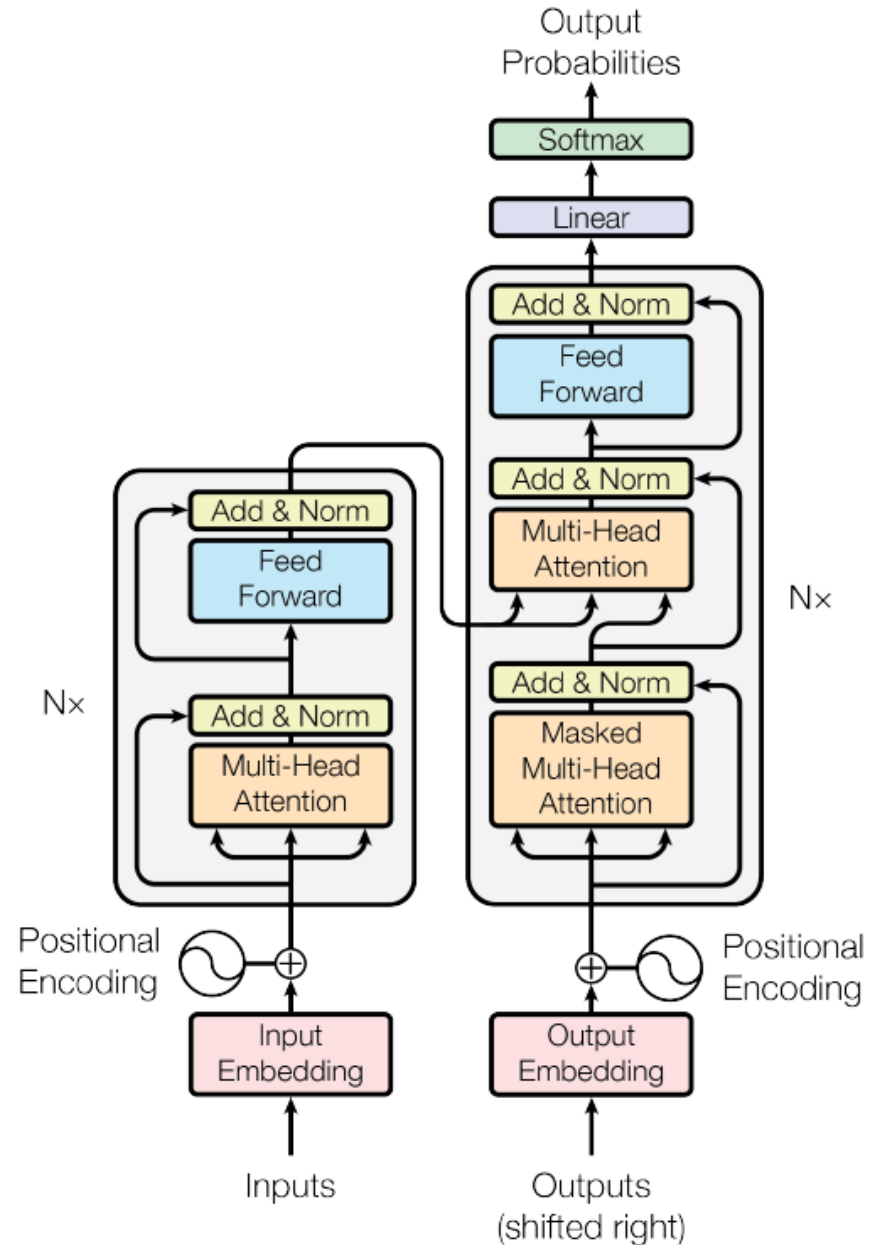
source: <http://visualqa.org/>

Some drawbacks of RNN

- Memory cost
- Can't train in parallel
- Short-term dependency

Beyond RNN

Transformer



Thank you!