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In-Class Problems

1. Calculate the Class Balanced Accuracy for the confusion matrix below.
2. Calculate the Balanced Accuracy for the confusion matrix below.

		True/Actual		
		Cat (🐱)	Fish (🐟)	Hen (🐔)
Predicted	Cat (🐱)	4	6	3
	Fish (🐟)	1	2	0
	Hen (🐔)	1	2	6

3. Calculate the distance in feature space (d) between the 2 iris dataset samples below.
4. Using SMOTE Oversampling with RN = 0.5, synthesize a sample of Iris-setosa between these 2 samples.

sample	sepal-length	sepal-width	petal-length	petal-width	class
real (r)	5.1	3.5	1.4	0.2	Iris-setosa
nearest neighbor (n)	4.9	3	1.4	0.2	Iris-setosa

5. Calculate the centroid in feature space of the 3 iris dataset samples below.

sepal-length	sepal-width	petal-length	petal-width	class
5.1	3.5	1.4	0.2	Iris-setosa
4.9	3	1.4	0.2	Iris-setosa
4.7	3.2	1.3	0.2	Iris-setosa

1. Calculate the Class Balanced Accuracy for the confusion matrix below.

$$P(\text{Cat}) = 4 / (4+6+3) = 4/13$$

$$P(\text{Fish}) = 2 / 3$$

$$P(\text{Hen}) = 6 / 9 = 2 / 3$$

$$R(\text{Cat}) = 4 / 6 = 2 / 3$$

$$R(\text{Fish}) = 2 / 10 = 1 / 5$$

$$R(\text{Hen}) = 6 / 9 = 2 / 3$$

$$\text{Min}(P(\text{Cat}), R(\text{Cat})) = 4 / 13$$

$$\text{Min}(P(\text{Fish}), R(\text{Fish})) = 1 / 5$$

$$\text{Min}(P(\text{Hen}), R(\text{Hen})) = 2 / 3$$

$$\text{Class Balanced Accuracy} = ((4/13) + (1/5) + (2/3)) / 3 = 39.15\%$$

2. Calculate the Balanced Accuracy for the confusion matrix below.

$$R(\text{Cat}) = 4 / 6 = 2 / 3$$

$$R(\text{Fish}) = 2 / 10 = 1 / 5$$

$$R(\text{Hen}) = 6 / 9 = 2 / 3$$

$$\text{Specificity}(\text{Cat}) = (2 + 2 + 6) / ((2 + 2 + 6) + (6 + 3)) = 10 / 19$$

$$\text{Specificity}(\text{Fish}) = 14 / (14 + 1) = 14 / 15$$

$$\text{Specificity}(\text{Hen}) = (4 + 6 + 1 + 2) / ((4 + 6 + 1 + 2) + (1 + 2)) = 13 / 16$$

$$\text{Avg}(R(\text{Cat}), \text{Specificity}(\text{Cat})) = 34 / 57$$

$$\text{Avg}(R(\text{Fish}), \text{Specificity}(\text{Fish})) = 17 / 30$$

$$\text{Avg}(R(\text{Hen}), \text{Specificity}(\text{Hen})) = 71 / 96$$

$$\text{Balanced Accuracy} = (34/57 + 17/30 + 71/96) / 3 = 63.32\%$$

3. Calculate the distance in feature space (d) between the 2 iris dataset samples below.

$$d = \sqrt{(5.1 - 4.9)^2 + (3.5 - 3)^2 + (1.4 - 1.4)^2 + (0.2 - 0.2)^2} = 0.539$$

4. Using SMOTE Oversampling with $RN = 0.5$, synthesize a sample of Iris-sesota between these 2 samples.

Synthetic sample = $(5.1 + 0.5(4.9-5.1)), (3.5 + 0.5(3-3.5)), (1.4 + 0.5(1.4-1.4)), (0.2+0.5(0.2-0.2))$

Sepal-length: 5

Sepal-width: 3.25

Petal-length: 1.4

Petal-width: 0.2

5. Calculate the centroid in feature space of the 3 iris dataset samples below.

$[\text{mean}(5.1, 4.9, 4.7), \text{mean}(3.5, 3, 3.2), \text{mean}(1.4, 1.4, 1.3), \text{mean}(0.2, 0.2, 0.2)] = [4.9, 3.23, 1.36, 0.2]$