Labs
Machine Learning Course
Fall 2020

EPFL

School of Computer and Communication Sciences
Nicolas Flammarion & Martin Jaggi
www.epfl.ch/labs/mlo/machine-learning-cs-433

Problem Set 12, Dec 3, 2020 (Theory Questions SVD)

Goals. The goal of this exercise is to

- familiarize yourself with the theory related to SVD.
- have time to discuss Project 2 with the assistants and teammates.

1 Theory Questions

Problem 1 (How to compute U and S efficiently):

In class, we saw that solving the eigenvector/value problem for the matrix XX^{\top} gives us a way to compute U and S. But in some instances $D\gg N$. In those cases, is there a way to accomplish this computation more efficiently?

Problem 2 (Positive semi-definite):

Show that if \boldsymbol{X} is a $N \times N$ symmetric matrix then the SVD has the form $\boldsymbol{U}\boldsymbol{S}\boldsymbol{U}^{\top}$, where \boldsymbol{U} is a $N \times N$ unitary matrix and \boldsymbol{S} is a $N \times N$ diagonal matrix with non-necessarily positive entries. Show that if \boldsymbol{X} is positive semi-definite, then all entries of \boldsymbol{S} are non-negative.