Main

Fall2019-proj3-grp7

In your final repo, there should be an R markdown file that organizes all computational steps for evaluating your proposed Facial Expression Recognition framework.

This file is currently a template for running evaluation experiments. You should update it according to your codes but following precisely the same structure.

```
if(!require("EBImage")){
  source("https://bioconductor.org/biocLite.R")
  biocLite("EBImage")
}
if(!require("R.matlab")){
  install.packages("R.matlab")
if(!require("readxl")){
  install.packages("readxl")
if(!require("dplyr")){
  install.packages("dplyr")
}
if(!require("readxl")){
  install.packages("readxl")
}
if(!require("ggplot2")){
  install.packages("ggplot2")
}
if(!require("caret")){
  install.packages("caret")
}
if(!require("OpenImageR")){
  install.packages("OpenImageR")
if(!require("FSelectorRcpp")){
  install.packages("FSelectorRcpp")
}
if(!require("mlr")){
  install.packages("mlr")
if(!require("kernlab")){
  install.packages("kernlab")
}
```

```
if(!require("gbm")){
  install.packages("gbm")
}
if(!require("class")){
  install.packages("class")
}
if(!require("MASS")){
  install.packages("MASS")
if(!require("e1071")){
  install.packages("e1071")
library(R.matlab)
library(readxl)
library(dplyr)
library(EBImage)
library(ggplot2)
library(caret)
library(OpenImageR)
library(FSelectorRcpp)
library(mlr)
library(kernlab)
library(gbm)
library(class)
library("e1071")
library("MASS")
```

Step 0 set work directories, extract paths, summarize

```
set.seed(0)
# setwd("~/Desktop/5243/Project 3/fall2019-proj3-sec2--grp7-master/doc")
# here replace it with your own path or manually set it in RStudio to where this rmd file is located.
# use relative path for reproducibility
# setwd("../doc")
```

Provide directories for training images. Training images and Training fiducial points will be in different subfolders.

```
train_dir <- "../data/train_set/" # This will be modified for different data sets.
train_image_dir <- paste(train_dir, "images/", sep="")
train_pt_dir <- paste(train_dir, "points/", sep="")
train_label_path <- paste(train_dir, "label.csv", sep="")</pre>
```

Step 1: set up controls for evaluation experiments.

In this chunk, we have a set of controls for the evaluation experiments.

• (T/F) cross-validation on the training set

- (number) K, the number of CV folds
- (T/F) process features for training set
- (T/F) run evaluation on an independent test set
- (T/F) process features for test set

```
run.cv=TRUE # run cross-validation on the training set
K <- 5 # number of CV folds
run.feature.train=FALSE # process features for training set
run.test=TRUE # run evaluation on an independent test set
run.feature.test=TRUE # process features for test set
run.feature.test.test=FALSE # process features for test_test set</pre>
```

Using cross-validation or independent test set evaluation, we compare the performance of models with different specifications. In this Starter Code, we tune parameter k (number of neighbours) for KNN.

Step 2: import data and train-test split

```
#train-test split
info <- read.csv(train_label_path)
n <- nrow(info)
n_train <- round(n*(4/5), 0)
train_idx <- sample(info$Index, n_train, replace = F)
test_idx <- setdiff(info$Index,train_idx)</pre>
```

If you choose to extract features from images, such as using Gabor filter, R memory will exhaust all images are read together. The solution is to repeat reading a smaller batch(e.g 100) and process them.

```
n_files <- length(list.files(train_image_dir))

image_list <- list()
for(i in 1:100){
   image_list[[i]] <- readImage(pasteO(train_image_dir, sprintf("%04d", i), ".jpg"))
}</pre>
```

Fiducial points are stored in matlab format. In this step, we read them and store them in a list.

```
#function to read fiducial points
#input: index
#output: matrix of fiducial points corresponding to the index
readMat.matrix <- function(index){
    return(round(readMat(pasteO(train_pt_dir, sprintf("%04d", index), ".mat"))[[1]],0))
}
#load fiducial points
fiducial_pt_list <- lapply(1:n_files, readMat.matrix)
save(fiducial_pt_list, file=".../output/fiducial_pt_list.RData")</pre>
```

Step 3: feature selection

feature.R should be the wrapper for all your feature engineering functions and options. The function feature() should have options that correspond to different scenarios for your project and produces an R

object that contains features and responses that are required by all the models you are going to evaluate later.

- feature.R
- Input: list of images or fiducial point
- Output: an RData file that contains extracted features and corresponding responses

```
source("../lib/feature.R")
tm feature train <- NA
if(run.feature.train){
  ## Distance calculation
  tm_feature_train <- system.time(dat_train <- feature_train(fiducial_pt_list, train_idx))</pre>
  dat train <- cbind(dat train, as.factor(infosemotion idx[train idx]))</pre>
  colnames(dat_train)[dim(dat_train)[2]] <- "emotion_idx"</pre>
  dat_train <- as.data.frame(dat_train)</pre>
  colnames(dat_train)<-make.names(colnames(dat_train),unique=T)</pre>
  ## Normalize
  tm feature train <- tm feature train +
    system.time(dat_train_stand <- feature_normalization(dat_train[,c(-dim(dat_train)[2])]))
 dat_train_stand <- cbind(dat_train_stand,dat_train$emotion_idx)</pre>
 colnames(dat_train_stand)[dim(dat_train_stand)[2]] <- "emotion_idx"</pre>
  ## Feature selection
  tm feature train <- tm feature train +
    system.time(feature_name <- feature_selection(dat_train_stand, "emotion_idx"))</pre>
  dat_train_selected <- dat_train[,feature_name]</pre>
  ## Calculate size from all selected distance
  tm_feature_train <- tm_feature_train +</pre>
    system.time(dat_train_double <- feature_selection_size(dat_train_selected))</pre>
  ## Add manually selected feature
  tm_feature_train <- tm_feature_train +</pre>
    system.time(dat_train_ratio <- manually_feature(fiducial_pt_list, train_idx))</pre>
  dat_train_selected_stand <- cbind(dat_train_selected,dat_train_double,dat_train_ratio)</pre>
  dat train selected stand <- feature normalization(dat train selected stand)
  dat_train_selected_stand <- cbind(dat_train_selected_stand,dat_trainselection_idx)
  colnames(dat_train_selected_stand)[dim(dat_train_selected_stand)[2]] <- "emotion_idx"</pre>
}
tm_feature_test <- NA</pre>
if(run.feature.test){
  ## This is the result from test
  feature_name <- c("point.7.to.point.21", "point.10.to.point.13", "point.10.to.point.33",
                     "point.11.to.point.49", "point.12.to.point.55", "point.14.to.point.18",
                     "point.23.to.point.50", "point.34.to.point.46", "point.50.to.point.62",
                     "point.59.to.point.62")
  ## Distance Feature
  tm_feature_test <- system.time(dat_test <- feature_train(fiducial_pt_list, test_idx))</pre>
```

```
dat_test <- cbind(dat_test, as.factor(info$emotion_idx[test_idx]))</pre>
  colnames(dat_test)[dim(dat_test)[2]] <- "emotion_idx"</pre>
  dat_test <- as.data.frame(dat_test)</pre>
  colnames(dat_test) <-make.names(colnames(dat_test), unique=T)</pre>
  dat_test_selected <- dat_test[,feature_name]</pre>
  ## Size Feature
  tm feature test <- tm feature test +
    system.time(dat_test_double <- feature_selection_size(dat_test_selected))</pre>
  ## Add manually selected feature
  tm_feature_test <- tm_feature_test +</pre>
    system.time(dat_test_ratio <- manually_feature(fiducial_pt_list, test_idx))</pre>
  dat_test_selected_stand <- cbind(dat_test_selected,dat_test_double,dat_test_ratio)</pre>
  dat_test_selected_stand <- feature_normalization(dat_test_selected_stand)</pre>
  dat_test_selected_stand <- cbind(dat_test_selected_stand,dat_test$emotion_idx)</pre>
  colnames(dat_test_selected_stand)[dim(dat_test_selected_stand)[2]] <- "emotion_idx"</pre>
}
tm_feature_test_test <- NA</pre>
if(run.feature.test.test){
  test_test_idx = c(1:2500)
  ## This is the result from test
  feature_name <- c("point.7.to.point.21", "point.10.to.point.13", "point.10.to.point.33",
                     "point.11.to.point.49", "point.12.to.point.55", "point.14.to.point.18",
                     "point.23.to.point.50", "point.34.to.point.46", "point.50.to.point.62",
                     "point.59.to.point.62")
  ## Distance Feature
  tm_feature_test_test <- system.time(dat_test_test <- feature_train(fiducial_pt_list, test_test_idx))</pre>
  colnames(dat_test_test) <-make.names(colnames(dat_test_test), unique=T)</pre>
  dat_test_test_selected <- dat_test_test[,feature_name]</pre>
  ## Size Feature
  tm_feature_test_test <- tm_feature_test_test +</pre>
    system.time(dat_test_test_double <- feature_selection_size(dat_test_test_selected))</pre>
  ## Add manually selected feature
  tm_feature_test_test <- tm_feature_test_test +</pre>
    system.time(dat_test_test_ratio <- manually_feature(fiducial_pt_list, test_test_idx))</pre>
  dat_test_selected_stand_test <- cbind(dat_test_test_selected,dat_test_test_double,</pre>
                                     dat_test_test_ratio)
  dat_test_selected_stand_test <- feature_normalization(dat_test_selected_stand_test)</pre>
}
##save(dat_train_selected_stand, file="../output/feature_train.RData")
## Because feature train takes over 10 hours, we do not knit this part.
## The previous feature selection train is already included in the output file.
save(dat_test_selected_stand, file="../output/feature_test.RData")
```

```
##save(dat_test_selected_stand_test, file="../output/feature_test_test.RData")
```

Step 4: Train a classification model with training features and responses

```
load("../output/feature_train.RData")
dat_train_selected <- dat_train_selected_ratio_stand55
dat_test_selected <- dat_test_selected_stand</pre>
```

Call the train models and test models from library:

- 1. KNN
- 2. LDA
- 3. SVM with radial kernel (improved model)
- 4. GBM with tree stumps (baseline Model)

1. KNN

- Do model selection by choosing among different values of training model parameters.
- Choose the "best" parameter value
- Train accuracy:
- KNN: Run test on test images
- evaluation
- Summarize Running Time

2. LDA

• Train the model with the entire training set using the selected model (model parameter) via cross-validation.

```
source("../lib/train_lda.R")
tm_train=NA
tm_train <- system.time(fit_train <- train(dat_train_selected, par_best))
save(fit_train, file="../output/fit_train.RData")</pre>
```

• Train Accuracy:

```
source("../lib/test_lda.R")
tm_test=NA
if(run.test){
  pred_train <- test(fit_train, dat_train_selected)
}
accu <- mean(dat_train_selected$emotion_idx == pred_train)
accu</pre>
```

```
## [1] 0.533
```

• LDA: Run test on test images

```
source("../lib/test_lda.R")
tm_test=NA
if(run.test){
  load(file="../output/fit_train.RData")
  tm_test <- system.time(pred <- test(fit_train, dat_test_selected))
}</pre>
```

```
• evaluation
accu <- mean(dat_test_selected$emotion_idx == pred)</pre>
cat("The accuracy of model:", "is", accu*100, "%.\n")
## The accuracy of model: is 47.6 %.
library(caret)
confusionMatrix(pred, dat_test_selected$emotion_idx)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction 1
                                       9 10 11 12 13 14 15 16 17 18 19 20 21
                  2
                     3
                        4
                           5
                              6
                                 7
                                     8
           1 15
                  0
                                 3
                                     0
                                              0
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##
                                        0
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##
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           19
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                              0
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                                        0 0 0 0
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##
                        0
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##
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##
           21
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                                                                         3 12
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##
           22
               0
                  0
                     0
                        2
                           0
                              0
                                                          0
                                                             1
                                                                1
                                                                    0
             Reference
##
## Prediction 22
##
               0
           1
##
           2
               1
```

```
##
           3
               6
##
           4
               0
##
           5
               0
           6
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               8
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           7
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           9
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           12
               0
##
           13
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           14
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           15
               0
               2
##
           16
##
           17
               0
##
           18
               1
##
           19
               1
##
           20
               0
##
           21
               2
##
           22
               5
##
## Overall Statistics
##
##
                   Accuracy: 0.476
##
                     95% CI: (0.4315, 0.5208)
##
       No Information Rate: 0.062
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                      Kappa: 0.4512
##
##
    Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
##
                         Class: 1 Class: 2 Class: 3 Class: 4 Class: 5 Class: 6
                           0.5769
## Sensitivity
                                     0.6071
                                              0.5500
                                                        0.4000
                                                                  0.7500
                                                                           0.6190
## Specificity
                           0.9726
                                     0.9936
                                              0.9604
                                                        0.9853
                                                                  0.9917
                                                                           0.8894
## Pos Pred Value
                           0.5357
                                     0.8500
                                              0.3667
                                                        0.5882
                                                                  0.7895
                                                                           0.1970
## Neg Pred Value
                           0.9767
                                     0.9771
                                              0.9809
                                                        0.9689
                                                                  0.9896
                                                                           0.9816
## Prevalence
                                              0.0400
                                                        0.0500
                                                                  0.0400
                                                                           0.0420
                           0.0520
                                     0.0560
## Detection Rate
                                     0.0340
                                              0.0220
                                                        0.0200
                                                                  0.0300
                                                                           0.0260
                           0.0300
## Detection Prevalence
                           0.0560
                                     0.0400
                                              0.0600
                                                        0.0340
                                                                  0.0380
                                                                           0.1320
                                                                  0.8708
## Balanced Accuracy
                           0.7747
                                     0.8004
                                              0.7552
                                                        0.6926
                                                                           0.7542
##
                         Class: 7 Class: 8 Class: 9 Class: 10 Class: 11
                                     0.7143
                                              0.7500
                                                         0.4615
## Sensitivity
                           0.5652
                                                                    0.3478
## Specificity
                                     0.9916
                                              0.9814
                                                         0.9705
                                                                    0.9979
                           0.9811
## Pos Pred Value
                           0.5909
                                     0.7895
                                              0.5714
                                                         0.4615
                                                                    0.8889
## Neg Pred Value
                           0.9791
                                     0.9875
                                              0.9916
                                                         0.9705
                                                                    0.9695
## Prevalence
                           0.0460
                                     0.0420
                                              0.0320
                                                         0.0520
                                                                    0.0460
## Detection Rate
                           0.0260
                                     0.0300
                                              0.0240
                                                         0.0240
                                                                    0.0160
## Detection Prevalence
                           0.0440
                                     0.0380
                                              0.0420
                                                         0.0520
                                                                    0.0180
## Balanced Accuracy
                           0.7732
                                     0.8530
                                              0.8657
                                                         0.7160
                                                                    0.6729
##
                         Class: 12 Class: 13 Class: 14 Class: 15 Class: 16
## Sensitivity
                            0.4167
                                       0.1364
                                                 0.5909
                                                            0.4545
                                                                       0.7368
```

```
## Specificity
                            0.9748
                                      0.9686
                                                 0.9749
                                                           0.9833
                                                                      0.9813
## Pos Pred Value
                            0.4545
                                      0.1667
                                                 0.5200
                                                           0.5556
                                                                      0.6087
                                                           0.9751
## Neg Pred Value
                            0.9707
                                      0.9606
                                                 0.9811
                                                                      0.9895
## Prevalence
                            0.0480
                                                                      0.0380
                                      0.0440
                                                 0.0440
                                                           0.0440
## Detection Rate
                            0.0200
                                      0.0060
                                                 0.0260
                                                           0.0200
                                                                      0.0280
                            0.0440
                                      0.0360
## Detection Prevalence
                                                 0.0500
                                                           0.0360
                                                                      0.0460
## Balanced Accuracy
                            0.6957
                                      0.5525
                                                 0.7829
                                                           0.7189
                                                                      0.8591
##
                         Class: 17 Class: 18 Class: 19 Class: 20 Class: 21
## Sensitivity
                            0.2903
                                      0.4348
                                                 0.3571
                                                           0.2500
                                                                      0.5000
## Specificity
                            0.9765
                                      0.9748
                                                 0.9733
                                                           0.9832
                                                                      0.9601
## Pos Pred Value
                            0.4500
                                      0.4545
                                                 0.2778
                                                           0.4286
                                                                      0.3871
## Neg Pred Value
                                      0.9728
                                                 0.9813
                            0.9542
                                                           0.9630
                                                                      0.9744
## Prevalence
                            0.0620
                                      0.0460
                                                 0.0280
                                                           0.0480
                                                                      0.0480
                                      0.0200
                                                 0.0100
## Detection Rate
                            0.0180
                                                           0.0120
                                                                      0.0240
## Detection Prevalence
                            0.0400
                                      0.0440
                                                 0.0360
                                                           0.0280
                                                                      0.0620
## Balanced Accuracy
                            0.6334
                                      0.7048
                                                 0.6652
                                                           0.6166
                                                                      0.7300
##
                         Class: 22
## Sensitivity
                            0.1923
## Specificity
                            0.9852
## Pos Pred Value
                            0.4167
## Neg Pred Value
                            0.9570
## Prevalence
                            0.0520
## Detection Rate
                            0.0100
## Detection Prevalence
                            0.0240
## Balanced Accuracy
                            0.5888
```

Note that the accuracy is not high but is better than that of ramdom guess (4.5%).

• Summarize Running Time Prediction performance matters, so does the running times for constructing features and for training the model, especially when the computation resource is limited.

```
cat("Time for training model=", tm_train[1], "s \n")

## Time for training model= 0.077 s

cat("Time for testing model=", tm_test[1], "s \n")

## Time for testing model= 0.005 s
```

- 3. SVM (improved model)
 - Tune the SVM model with cross-validation:

```
##
## Parameter tuning of 'svm':
##
## - sampling method: 12-fold cross validation
##
## - best parameters:
  gamma cost
## 0.001
           35
##
## - best performance: 0.5394843
## - Detailed performance results:
##
     gamma cost
                    error dispersion
## 1 1e-05 30 0.7414899 0.01624426
## 2 1e-04
           30 0.5805437 0.03553754
## 3 1e-03 30 0.5409873 0.02619165
## 4 1e-02 30 0.5654865 0.03189845
## 5 1e-01 30 0.6474581 0.04071884
## 6 1e-05 35 0.7314918 0.01769932
## 7 1e-04 35 0.5765307 0.03410334
## 8 1e-03 35 0.5394843 0.02718324
## 9 1e-02 35 0.5714896 0.02705938
## 10 1e-01 35 0.6474581 0.04071884
## 11 1e-05 40 0.7164797 0.02016448
## 12 1e-04 40 0.5735156 0.03079428
## 13 1e-03 40 0.5414893 0.02932813
## 14 1e-02 40 0.5759986 0.02377225
## 15 1e-01 40 0.6474581 0.04071884
```

• Train the model

```
source("../lib/train_svm.R")
par_best=NULL
fit_train_final_svm <- train(dat_train_selected, tuned_parameters$best.parameters)
save(fit_train_final_svm, file="../output/fit_train_final.RData")</pre>
```

• Train accuracy:

```
source("../lib/test_svm.R")
load("../output/fit_train_final.RData")

if(run.test){
   pred_train <- test(fit_train_final_svm, dat_train_selected)
}

accu <- mean(dat_train_selected$emotion_idx == pred_train)
accu</pre>
```

[1] 0.5725

• SVM: Run test on test images

```
source("../lib/test_svm.R")
tm_test=NA
if(run.test){
 load(file="../output/fit_train.RData")
 tm_test <- system.time(pred <- test(fit_train_final_svm, dat_test_selected))</pre>
******** SVM: Run test_test on test images
source("../lib/test_svm.R")
tm_test=NA
if(run.test){
 load(file="../output/fit_train_final.RData")
 tm_test <- system.time(pred <- test(fit_train_final_svm, dat_test_selected))</pre>
}
  • evaluation
accu <- mean(dat_test_selected$emotion_idx == pred)</pre>
cat("The accuracy of model:", "is", accu*100, "%.\n")
## The accuracy of model: is 55 %.
library(caret)
confusionMatrix(pred, dat_test_selected$emotion_idx)
## Confusion Matrix and Statistics
##
##
            Reference
## Prediction 1
                 2
                    3
                      4
                         5
                            6
                               7
                                  8
                                    9 10 11 12 13 14 15 16 17 18 19 20 21
                    2
                                             0
##
          1 20
                 0
                            0
                               1
                                  0
                                     0
                                       0
                                          0
                                                1
                                                   0
                                                      0
          2
              0 23
                    0
                      0
                         0
                                       0
                                          0
                                             0
                                                0
                                                   0
                                                      0
##
                            0
                               0
                                  1
                                     1
                                                         0
                                                            0
                                                               0
                                                                 1
                                                                    0
                                                                       0
              2 0 13
##
          3
                      3
                         0
                            3
                               0
                                  0
                                     0
                                        1
                                          1
                                             0
                                                1
                                                   0
                                                      0
                                                         0
                                                              0
                                                                       0
##
          4
              0 0 2 15
                        0
                            0
                               0
                                  0 0 5 4 2
                                                8
                                                   0
                                                      0
                                                         0
                                                            Ω
                                                              0
          5
##
             0 0 0 0 17
                               0
                                  0 0 0 0 0
                                                0
                                                   0
                                                      0
                                                         0
          6
              0 0 0 1
                         0
                            7
                                  0 0
                                       1 1 0 3
                                                   0
                                                      0
                                                         2
##
                               1
                                                           Ω
                                                              0
                                                                       0
##
          7
              1
                 0
                    0
                         0
                            0
                               9
                                  0
                                     0
                                       0
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                                                                       0
          8
              0 2 0
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                         0
                            0
                               1 17
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                                       Ω
                                          Ω
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                                                            2
                                                              Λ
##
                                                                    1
##
          9
              0 3 0
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                               0
                                 1 14
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                                                      0
          10 0 0 1
                               0
                                  0 0 15
                                             2
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##
                      4
                         0
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          11
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                    0
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                                                      0
##
                      0
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          12 1 0 0 1
                         0
                            5 0
                                  0 0 0 2 13
                                                0
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##
##
          13 2 0 1 1
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                            2 0
                                  0 0 3 2
                                             3
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##
          14 0
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                                                0 17
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##
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          16 0 0 1 0
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                                                      0 14
##
                                                                       1
##
          17 0 0 0 0
                         0
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                               2
                                  2 0
                                       0 0 0
                                                0
                                                   1
                                                      0
                                                         0 13
                                                              1
##
          18 0
                 0
                    0
                      0
                         2
                            0
                               1
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                                       0 0 0
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                                                           4 13
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##
          19 0 0
                    0
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                               2 0 0 0 0 0
                                                0
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                                                         0
                                                              3
                                                                 2
                                                                    3
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                                                           1
##
          20 0
                 0
                    0
                      0
                         0 0 0
                                  0
                                    1
                                       0 0 0 0
                                                   0
                                                      0
                                                         0
                                                           5
          21 0
                      0 0 0 6 0 0
                                       0 0 1 0 0 0 1 0 1 3 4 10
##
                 0
                    0
```

```
##
           ##
             Reference
## Prediction 22
           1
               0
##
##
           2
               1
##
           3
               3
##
           4
               1
           5
##
              0
##
           6
               1
##
           7
              0
##
           8
               0
           9
               0
##
           10
              3
##
              2
##
           11
##
           12
              0
##
           13
              0
##
           14
              1
##
           15
              0
##
           16
              3
##
           17
               1
##
           18
              0
##
           19
              2
##
           20
              1
##
           21
##
           22
              6
## Overall Statistics
##
##
                  Accuracy: 0.55
                    95% CI: (0.5052, 0.5942)
##
##
      No Information Rate: 0.062
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa: 0.5283
##
##
   Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
##
                        Class: 1 Class: 2 Class: 3 Class: 4 Class: 5 Class: 6
## Sensitivity
                          0.7692
                                   0.8214
                                            0.6500
                                                     0.6000
                                                              0.8500
                                                                       0.3333
## Specificity
                          0.9895
                                   0.9915
                                            0.9688
                                                     0.9537
                                                              0.9896
                                                                       0.9791
## Pos Pred Value
                          0.8000
                                   0.8519
                                            0.4643
                                                     0.4054
                                                              0.7727
                                                                       0.4118
## Neg Pred Value
                                                     0.9784
                          0.9874
                                   0.9894
                                            0.9852
                                                              0.9937
                                                                       0.9710
## Prevalence
                                   0.0560
                                            0.0400
                                                     0.0500
                                                              0.0400
                                                                       0.0420
                          0.0520
## Detection Rate
                          0.0400
                                   0.0460
                                            0.0260
                                                     0.0300
                                                              0.0340
                                                                       0.0140
                                                     0.0740
## Detection Prevalence
                          0.0500
                                   0.0540
                                            0.0560
                                                              0.0440
                                                                       0.0340
## Balanced Accuracy
                                   0.9065
                                            0.8094
                                                                       0.6562
                          0.8793
                                                     0.7768
                                                              0.9198
##
                        Class: 7 Class: 8 Class: 9 Class: 10 Class: 11
## Sensitivity
                          0.3913
                                   0.8095
                                            0.8750
                                                      0.5769
                                                                0.3913
                                   0.9875
                                            0.9876
                                                      0.9557
                                                                0.9874
## Specificity
                          0.9979
## Pos Pred Value
                          0.9000
                                   0.7391
                                            0.7000
                                                      0.4167
                                                                0.6000
## Neg Pred Value
                          0.9714
                                   0.9916
                                            0.9958
                                                      0.9763
                                                                0.9711
## Prevalence
                          0.0460
                                   0.0420
                                            0.0320
                                                      0.0520
                                                                0.0460
```

```
## Detection Rate
                           0.0180
                                    0.0340
                                              0.0280
                                                        0.0300
                                                                  0.0180
                                             0.0400
## Detection Prevalence
                                                                  0.0300
                           0.0200
                                    0.0460
                                                        0.0720
## Balanced Accuracy
                           0.6946
                                    0.8985
                                             0.9313
                                                        0.7663
                                                                  0.6894
##
                         Class: 12 Class: 13 Class: 14 Class: 15 Class: 16
## Sensitivity
                            0.5417
                                      0.1818
                                                 0.7727
                                                           0.7273
                                                                      0.7368
## Specificity
                            0.9790
                                      0.9686
                                                0.9644
                                                           0.9854
                                                                      0.9834
## Pos Pred Value
                            0.5652
                                      0.2105
                                                0.5000
                                                           0.6957
                                                                      0.6364
## Neg Pred Value
                            0.9769
                                      0.9626
                                                0.9893
                                                           0.9874
                                                                      0.9895
## Prevalence
                            0.0480
                                      0.0440
                                                 0.0440
                                                           0.0440
                                                                      0.0380
## Detection Rate
                            0.0260
                                      0.0080
                                                0.0340
                                                           0.0320
                                                                      0.0280
## Detection Prevalence
                            0.0460
                                      0.0380
                                                 0.0680
                                                           0.0460
                                                                      0.0440
## Balanced Accuracy
                            0.7603
                                      0.5752
                                                 0.8686
                                                           0.8563
                                                                      0.8601
##
                         Class: 17 Class: 18 Class: 19 Class: 20 Class: 21
## Sensitivity
                            0.4194
                                      0.5652
                                                 0.1429
                                                           0.3333
                                                                      0.4167
## Specificity
                            0.9765
                                      0.9811
                                                 0.9733
                                                           0.9727
                                                                      0.9643
## Pos Pred Value
                            0.5417
                                      0.5909
                                                 0.1333
                                                           0.3810
                                                                      0.3704
## Neg Pred Value
                            0.9622
                                      0.9791
                                                0.9753
                                                           0.9666
                                                                      0.9704
## Prevalence
                            0.0620
                                      0.0460
                                                 0.0280
                                                           0.0480
                                                                      0.0480
## Detection Rate
                            0.0260
                                      0.0260
                                                0.0040
                                                           0.0160
                                                                      0.0200
## Detection Prevalence
                            0.0480
                                      0.0440
                                                 0.0300
                                                           0.0420
                                                                      0.0540
## Balanced Accuracy
                            0.6980
                                      0.7732
                                                0.5581
                                                           0.6530
                                                                      0.6905
##
                         Class: 22
## Sensitivity
                            0.2308
## Specificity
                            0.9916
## Pos Pred Value
                            0.6000
## Neg Pred Value
                            0.9592
## Prevalence
                            0.0520
## Detection Rate
                            0.0120
## Detection Prevalence
                            0.0200
## Balanced Accuracy
                            0.6112
```

Summarize Running Time

Prediction performance matters, so does the running times for constructing features and for training the model, especially when the computation resource is limited.

```
#cat("Time for constructing training features=", tm_feature_train[1], "s \n") #cat("Time for constructing testing features=", tm_feature_test[1], "s \n") cat("Time for training model=", tm_train[1], "s \n")
```

Time for training model= 259.809 s

```
cat("Time for testing model=", tm_test[1], "s \n")
```

Time for testing model= 0.119 s

- 4. GBM (Baseline Model)
 - Tune GBM.

```
hyper_grid <- expand.grid(</pre>
  shrinkage = c(.001, .01),
  interaction.depth = c(1, 3),
  n.minobsinnode = c(5, 10),
  bag.fraction = c(.65, .8),
  optimal_trees = 0,
                                    # a place to dump results
  min_RMSE = 0
                                    # a place to dump results
# randomize data
random_index <- sample(1:nrow(dat_train_selected), nrow(dat_train_selected))</pre>
random_train <- dat_train_selected[random_index, ]</pre>
# grid search
for(i in 1:nrow(hyper_grid)) {
  # reproducibility
  set.seed(123)
  # train model
  gbm.tune <- gbm(</pre>
    formula = emotion_idx~.,
    distribution = "multinomial",
    data = random_train,
    n.trees = 100,
    interaction.depth = hyper_grid$interaction.depth[i],
    shrinkage = hyper_grid$shrinkage[i],
    n.minobsinnode = hyper_grid$n.minobsinnode[i],
    bag.fraction = hyper_grid$bag.fraction[i],
    train.fraction = .75,
    n.cores = NULL, # will use all cores by default
    verbose = FALSE
  # add min training error and trees to grid
  hyper_grid$optimal_trees[i] <- which.min(gbm.tune$valid.error)
  hyper_grid$min_RMSE[i] <- sqrt(min(gbm.tune$valid.error))</pre>
hyper_grid %>%
  dplyr::arrange(min_RMSE) %>%
 head(10)
```

```
shrinkage interaction.depth n.minobsinnode bag.fraction optimal_trees
## 1
          0.010
                                                          0.65
                                                                          100
                                 3
                                               10
## 2
          0.010
                                 3
                                               10
                                                          0.80
                                                                          100
                                                5
## 3
          0.010
                                3
                                                          0.65
                                                                          100
## 4
          0.010
                                3
                                                5
                                                          0.80
                                                                          100
## 5
          0.010
                                               10
                                                          0.65
                                                                          100
                                1
## 6
          0.010
                                1
                                                5
                                                          0.65
                                                                          100
## 7
          0.010
                                1
                                               10
                                                          0.80
                                                                          100
## 8
        0.010
                                1
                                               5
                                                          0.80
                                                                          100
## 9
         0.001
                                3
                                               10
                                                          0.65
                                                                          100
```

```
## 10
         0.001
                               3
                                             5
                                                        0.65
                                                                       100
##
     min RMSE
## 1 1.487001
## 2 1.491959
## 3 1.492670
## 4 1.497072
## 5 1.581901
## 6 1.583199
## 7 1.583916
## 8 1.584736
## 9 1.690817
## 10 1.692194
```

• Train the model with the entire training set using the selected model (model parameter) via cross-validation.

```
source("../lib/train_gbm.R")
tm_train=NA
tm_train <- system.time(fit_train_baseline <- train(dat_train_selected, par = NULL))
save(fit_train_baseline, file="../output/fit_train_baseline_final.RData")</pre>
```

• Train Error:

```
source("../lib/test_gbm.R")
load("../output/fit_train_baseline_final.RData")

tm_test=NA
if(run.test){
   tm_test <- system.time(pred_train <- test(fit_train_baseline, dat_train_selected))
}

labels = colnames(pred_train)[apply(pred_train, 1, which.max)]
accu <- mean(dat_train_selected$emotion_idx == labels)
accu</pre>
```

[1] 0.7705

• GBM: Run test on test images

```
source("../lib/test_gbm.R")
tm_test=NA
if(run.test){
  load(file="../output/fit_train.RData")
  tm_test <- system.time(pred <- test(fit_train_baseline, dat_test_selected))
}</pre>
```

• GBM: Run test_test on test images

```
source("../lib/test_gbm.R")

tm_test_test=NA

if(run.feature.test.test){
  load(file="../output/fit_train_baseline_final.RData")
  tm_test <- system.time(pred <- test(fit_train_baseline, dat_test_selected))
}</pre>
```

evaluation

```
labels = colnames(pred)[apply(pred, 1, which.max)]
accu <- mean(dat_test_selected$emotion_idx == labels)</pre>
cat("The accuracy of model:", "is", accu*100, "%.\n")
## The accuracy of model: is 59.6 %.
library(caret)
confusionMatrix(as.factor(labels), dat_test_selected$emotion_idx)
## Warning in confusionMatrix.default(as.factor(labels),
## dat_test_selected$emotion_idx): Levels are not in the same order for
## reference and data. Refactoring data to match.
## Confusion Matrix and Statistics
##
              Reference
                                          9 10 11 12 13 14 15 16 17 18 19 20 21
## Prediction
                1
                   2
                             5
                                 6
               22
                                                    2
                                                        2
                                                           0
                   0
                       3
                                       0
                                          0
                                                 1
                                                              0
##
            1
                             0
                                 1
                                    0
                                              1
                                                                  1
            2
##
                0 19
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                                    0
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##
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##
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##
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##
            11
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##
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##
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##
            15
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##
##
              Reference
## Prediction 22
            1
                1
##
##
            2
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            3
                3
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##
            4
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##
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##
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##
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           17
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##
           18
           19
               3
##
##
           20
               0
##
           21
               5
##
           22
##
## Overall Statistics
##
##
                   Accuracy: 0.596
                     95% CI: (0.5515, 0.6393)
##
       No Information Rate: 0.062
##
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                      Kappa: 0.5766
##
    Mcnemar's Test P-Value : NA
##
##
## Statistics by Class:
##
                         Class: 1 Class: 2 Class: 3 Class: 4 Class: 5 Class: 6
##
                                                                  0.9000
## Sensitivity
                                     0.6786
                                               0.7000
                                                        0.6800
                                                                            0.4762
                           0.8462
## Specificity
                           0.9705
                                     0.9873
                                               0.9667
                                                        0.9811
                                                                  0.9958
                                                                            0.9833
## Pos Pred Value
                           0.6111
                                     0.7600
                                               0.4667
                                                        0.6538
                                                                  0.9000
                                                                            0.5556
                                     0.9811
## Neg Pred Value
                           0.9914
                                               0.9872
                                                        0.9831
                                                                  0.9958
                                                                            0.9772
## Prevalence
                           0.0520
                                     0.0560
                                               0.0400
                                                        0.0500
                                                                  0.0400
                                                                            0.0420
## Detection Rate
                                                                  0.0360
                           0.0440
                                     0.0380
                                               0.0280
                                                        0.0340
                                                                            0.0200
## Detection Prevalence
                           0.0720
                                     0.0500
                                               0.0600
                                                        0.0520
                                                                  0.0400
                                                                            0.0360
                                               0.8333
                                                                  0.9479
## Balanced Accuracy
                           0.9083
                                     0.8329
                                                        0.8305
                                                                            0.7297
##
                         Class: 7 Class: 8 Class: 9 Class: 10 Class: 11
## Sensitivity
                           0.6087
                                     0.7619
                                               0.6875
                                                         0.6154
                                                                    0.6087
## Specificity
                           0.9853
                                     0.9896
                                               0.9752
                                                         0.9684
                                                                    0.9832
## Pos Pred Value
                                               0.4783
                                                                    0.6364
                           0.6667
                                     0.7619
                                                         0.5161
## Neg Pred Value
                                     0.9896
                                               0.9895
                                                                    0.9812
                           0.9812
                                                         0.9787
## Prevalence
                           0.0460
                                     0.0420
                                               0.0320
                                                         0.0520
                                                                    0.0460
## Detection Rate
                           0.0280
                                     0.0320
                                               0.0220
                                                         0.0320
                                                                    0.0280
## Detection Prevalence
                           0.0420
                                     0.0420
                                               0.0460
                                                         0.0620
                                                                    0.0440
                                     0.8757
                                               0.8314
                                                         0.7919
## Balanced Accuracy
                           0.7970
                                                                    0.7960
##
                         Class: 12 Class: 13 Class: 14 Class: 15 Class: 16
## Sensitivity
                            0.4583
                                       0.2727
                                                  0.7727
                                                            0.6818
                                                                       0.7895
## Specificity
                                                  0.9791
                                                            0.9833
                            0.9832
                                       0.9937
                                                                       0.9834
## Pos Pred Value
                            0.5789
                                       0.6667
                                                  0.6296
                                                            0.6522
                                                                       0.6522
## Neg Pred Value
                            0.9730
                                       0.9674
                                                  0.9894
                                                            0.9853
                                                                       0.9916
## Prevalence
                                       0.0440
                                                  0.0440
                                                            0.0440
                            0.0480
                                                                       0.0380
## Detection Rate
                            0.0220
                                       0.0120
                                                  0.0340
                                                            0.0300
                                                                       0.0300
## Detection Prevalence
                            0.0380
                                       0.0180
                                                  0.0540
                                                            0.0460
                                                                       0.0460
## Balanced Accuracy
                            0.7208
                                       0.6332
                                                  0.8759
                                                            0.8325
                                                                       0.8864
```

```
##
                         Class: 17 Class: 18 Class: 19 Class: 20 Class: 21
## Sensitivity
                            0.4839
                                      0.5652
                                                 0.3571
                                                           0.5417
                                                                      0.4167
                            0.9872
                                      0.9832
                                                 0.9712
                                                           0.9664
## Specificity
                                                                      0.9664
## Pos Pred Value
                                      0.6190
                                                 0.2632
                                                                      0.3846
                            0.7143
                                                           0.4483
## Neg Pred Value
                            0.9666
                                      0.9791
                                                 0.9813
                                                           0.9766
                                                                      0.9705
## Prevalence
                            0.0620
                                      0.0460
                                                 0.0280
                                                           0.0480
                                                                      0.0480
## Detection Rate
                            0.0300
                                      0.0260
                                                 0.0100
                                                           0.0260
                                                                      0.0200
                                                 0.0380
## Detection Prevalence
                            0.0420
                                      0.0420
                                                           0.0580
                                                                      0.0520
## Balanced Accuracy
                            0.7355
                                      0.7742
                                                 0.6642
                                                           0.7540
                                                                      0.6915
##
                         Class: 22
## Sensitivity
                            0.2692
## Specificity
                            0.9937
## Pos Pred Value
                            0.7000
## Neg Pred Value
                            0.9612
## Prevalence
                            0.0520
## Detection Rate
                            0.0140
## Detection Prevalence
                            0.0200
## Balanced Accuracy
                            0.6315
```

###Reference

• Du, S., Tao, Y., & Martinez, A. M. (2014). Compound facial expressions of emotion. Proceedings of the National Academy of Sciences, 111(15), E1454-E1462.