

# Lab 7 - Tree

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## #A

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### Description

Given the in-order and post-order of a binary tree. You need to find the pre-order.

### Input

in-order.

post-order.

### Output

pre-order.

### Sample Test Data

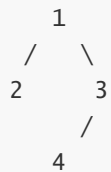
#### Input #1

```
2143
2431
```

#### Output #1

```
1234
```

#### Tips:



### Data Limit

Each node is represented by a single character. the character is a digit or a uppercase or lowercase letter. (i.e. [0-9a-zA-Z])

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## #B

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### Description

You are given a **tree** with  $N$  vertices.

An edge connects Vertices  $a$  and  $b$  and has a length of  $c$ .

You are also given  $Q$  queries and an integer  $R$ . In the  $i$ -th query:

find the length of the shortest path from Vertex  $x_i$  to Vertex  $y_i$  via Vertex  $R$ .

(Hint: what is the shortest path in a tree? Don't think it's complicated.)

### Input

$N$

$N-1$  lines, each line is:  $a\ b\ c$

$Q\ R$

$Q$  lines, each line is:  $x_i\ y_i$

### Output

$Q$  lines, each line is a length of the shortest path.

### Sample Test Data

#### Input #1

```
5
1 2 1
1 3 1
2 4 1
3 5 1
3 1
2 4
2 3
4 5
```

#### Output #1

```
3
2
4
```

#### Input #2

```
10
1 2 1000000000
2 3 1000000000
3 4 1000000000
4 5 1000000000
5 6 1000000000
6 7 1000000000
7 8 1000000000
8 9 1000000000
9 10 1000000000
1 1
9 10
```

### Output #2

```
17000000000
```

### Input #3

```
7
1 2 1
1 3 3
1 4 5
1 5 7
1 6 9
1 7 11
3 2
1 3
4 5
6 7
```

### Output #3

```
5
14
22
```

## Data Limit

$$3 \leq N \leq 100000$$

$$1 \leq Q \leq 100000$$

$$x_i \neq y_i, x_i \neq R, y_i \neq R$$

$$1 \leq c \leq 10^9$$

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# #C

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## Description

You are given a **tree** with  $N$  vertices.

An edge connects Vertices  $a$  and  $b$  and has a length of 1.

You need to find a vertex such that the sum of the shortest distances from all vertices to it is the minimum.

If multiple vertices meet the requirements, use the one with the lowest number.

(Hint: the vertex is called "centroid". It has some properties. You can easily find more information about it online.)

## Input

$N$

$N-1$  lines, each line is:  $a\ b$ , representing an edge.

## Output

A line, two integers.

The first is the vertex.

The second is the sum of the shortest distances from all vertices to it.

## Sample Test Data

### Input #1

```
4
1 2
2 3
3 4
```

### Output #1

```
2 4
```

## Data Limit

$2 \leq N \leq 100000$

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## #D

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### Description

A text has  $n$  kinds of characters, you need to encode the characters in binary. The encoding of one kind of character cannot be a prefix of another.

The number of occurrences of the  $i$ -th character is  $a_i$  how to make its final text encoding length minimum. In the case of ensuring the minimum length of the final text encoding, how to make the longest character encoding minimum ?

### Input

$n$

$n$  lines, each line:  $a_i$

### Output

The minimum length of the text after encoding.

In the case of ensuring the minimum length of the final encoding, the minimum longest character encoding.

### Sample Test Data

#### Input #1

```
6
1
5
7
9
1
6
```

#### Output #1

```
67
4
```

### Data Limit

$$1 \leq n \leq 100000$$

$$1 \leq a_i \leq 10^9$$

### Hint

`priority_queue` in C++ or `PriorityQueue` in Java may help you.

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# #E

## Description

You are given a **tree** with  $N$  vertices.

Each vertex has an initial value 0.

An edge  $e_i$  connects Vertices  $a_{e_i}$  and  $b_{e_i}$ .

You are also given  $Q$  queries. In the  $i$ -th query:

You are given integers:  $opt, e_i, x$ .

if  $opt=1$ : for each Vertex  $v$  reachable from Vertex  $a_{e_i}$  without visiting Vertex  $b_{e_i}$  by traversing edges, the value of  $v$  increases by  $x$ .

if  $opt=2$ : for each Vertex  $v$  reachable from Vertex  $b_{e_i}$  without visiting Vertex  $a_{e_i}$  by traversing edges, the value of  $v$  increases by  $x$ .

## Input

$N$

$N-1$  lines, each line is:  $a_{e_i} b_{e_i}$

$Q$

$Q$  lines, each line is:  $opt e_i x$

## Output

The value of each vertex at the end, in the order of  $1 \sim n$  vertex.

## Sample Test Data

### Input #1

```
5
1 2
2 3
2 4
4 5
4
1 1 1
1 4 10
2 1 100
2 2 1000
```

### Output #1

```
11
110
1110
110
100
```

## Tips

```
1
/e1
2
/e2 \e3
3    4
      \e4
      5
```

In the first query, we add 1 to Vertex 1.

In the second query, we add 10 to Vertex 1,2,3,4

In the third query, we add 100 to Vertex 2,3,4,5.

In the fourth query, we add 1000 to Vertex 3.

## Input #2

```
7
2 1
2 3
4 2
4 5
6 1
3 7
7
2 2 1
1 3 2
2 2 4
1 6 8
1 3 16
2 4 32
2 1 64
```

## Output #2

```
72
8
13
26
58
72
5
```

## Input #3

```
11
2 1
1 3
3 4
5 2
1 6
```

```
1 7
5 8
3 9
3 10
11 4
10
2 6 688
1 10 856
1 8 680
1 8 182
2 2 452
2 4 183
2 6 518
1 3 612
2 6 339
2 3 206
```

### output #3

```
1657
1657
2109
1703
1474
1657
3202
1474
1247
2109
2559
```

## Data Limit

$$2 \leq N \leq 200000$$

$$1 \leq Q \leq 200000$$

$$1 \leq x \leq 10^9$$

## Hint

Maybe you can save time by making some markers to tell you that an adding was performed instead of actually doing it.

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