

Econometrics I

Lecture 5: Extended Example: The Wage Equation

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Mincerian Regression

- Recall the Mincerian regression (wage equation):

$$\ln wage_i = \beta_0 + \beta_{ed} Education_i + \beta_{exp} Experience_i + \beta_{Fem} Female_i + \cdots + \varepsilon_i$$

- Let's revisit estimating this with the Cornwell and Rupert (NLSY) data.

Process the data

```
suppressMessages(library(tidyverse))
suppressMessages(library(fixest))

# first, the Cornwell and Rupert regression
data <- read.csv('./cornwell-rupert.csv') %>% mutate(EXP2 = EXP^2)

# see counts of each education level

data2<-data %>% mutate(ED_LEVEL=cut(ED,c(0,8,11,12,15,16,17),
                                     labels = c("NOHS", "SOMEHS", "HS", "SOMECOL","COL","POST"),
                                     right=TRUE))

|
# check that we did it correctly
table(data$ED,data2$ED_LEVEL)
```

Baseline Results

```
reg_1 <- feols(LWAGE ~ ED + EXP + EXP2 + WKS + OCC + SOUTH + SMSA
+ MS + UNION + FEM, data = data)

# dropping the constant
reg_2 <- feols(LWAGE ~ -1 + i(ED_LEVEL) + EXP + EXP2 + WKS + OCC + SOUTH + SMSA
+ MS + UNION + FEM, data = data2)

# not dropping the constant -- which category is omitted?
reg_3 <- feols(LWAGE ~ 1+ i(ED_LEVEL) + EXP + EXP2 + WKS + OCC + SOUTH + SMSA
+ MS + UNION + FEM, data = data2)

# change the omitted category -- how do coefficients change?
reg_4 <- feols(LWAGE ~ 1+ i(ED_LEVEL,ref="COL") + EXP + EXP2 + WKS + OCC + SOUTH + SMSA
+ MS + UNION + FEM, data = data2)
etable(list(reg_1,reg_2,reg_3,reg_4))
```

Note on interpreting effects with log dependent variable:

Intrepreting coefficients for $\log(y_i) \approx 1 + \beta$:

- $\exp(-.3892) = .6826$
- $\exp(.05654) = 1.057$

Dependent Variable:	LWAGE			
Model:	(1)	(2)	(3)	(4)
<i>Variables</i>				
Constant	5.245*** (0.0717)		5.655*** (0.0634)	6.161*** (0.0597)
ED	0.0565*** (0.0026)			
EXP	0.0404*** (0.0022)	0.0410*** (0.0022)	0.0410*** (0.0022)	0.0410*** (0.0022)
EXP2	-0.0007*** (4.78×10^{-5})	-0.0007*** (4.8×10^{-5})	-0.0007*** (4.8×10^{-5})	-0.0007*** (4.8×10^{-5})
WKS	0.0045*** (0.0011)	0.0046*** (0.0011)	0.0046*** (0.0011)	0.0046*** (0.0011)
OCC	-0.1405*** (0.0147)	-0.1386*** (0.0151)	-0.1386*** (0.0151)	-0.1386*** (0.0151)
SOUTH	-0.0721*** (0.0125)	-0.0762*** (0.0126)	-0.0762*** (0.0126)	-0.0762*** (0.0126)
SMSA	0.1390*** (0.0121)	0.1436*** (0.0121)	0.1436*** (0.0121)	0.1436*** (0.0121)
MS	0.0674*** (0.0206)	0.0692*** (0.0207)	0.0692*** (0.0207)	0.0692*** (0.0207)
UNION	0.0901*** (0.0129)	0.0940*** (0.0130)	0.0940*** (0.0130)	0.0940*** (0.0130)
FEM	-0.3892*** (0.0252)	-0.3819*** (0.0253)	-0.3819*** (0.0253)	-0.3819*** (0.0253)
ED_LEVEL = NOHS		5.655*** (0.0634)		-0.5066*** (0.0284)
ED_LEVEL = SOMEHS		5.795*** (0.0624)	0.1400*** (0.0249)	-0.3666*** (0.0236)
ED_LEVEL = HS		5.903*** (0.0609)	0.2482*** (0.0229)	-0.2584*** (0.0194)
ED_LEVEL = SOMECOL		5.991*** (0.0610)	0.3364*** (0.0268)	-0.1702*** (0.0206)
ED_LEVEL = COL		6.161*** (0.0597)	0.5066*** (0.0284)	
ED_LEVEL = POST		6.188*** (0.0589)	0.5337*** (0.0295)	0.0271 (0.0213)
<i>Fit statistics</i>				
Observations	4,165	4,165	4,165	4,165
R ²	0.41826	0.41724	0.41738	0.41738

Heuristic Policies

- ▶ These are methods aiming to give a good but not necessarily optimal solution to a problem.
- ▶ There exist a number of such policies for bandit problems.
- ▶ Greedy policy:
 - choose arm with greatest expected reward
 - ignores variability in prior distribution
 - quite good for Bernoulli bandits, but less effective for normal bandits

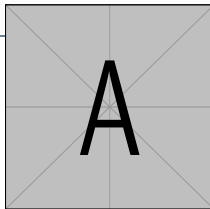


Figure 1: *

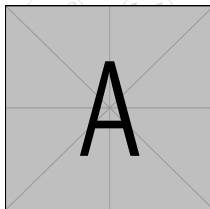


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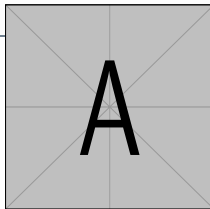


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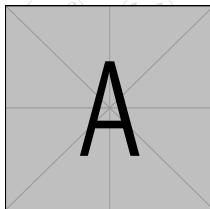


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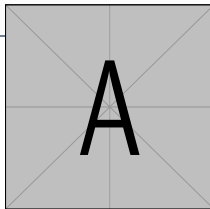


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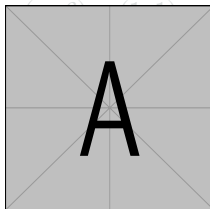


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$$(\alpha, \beta) = (6, 5)$$

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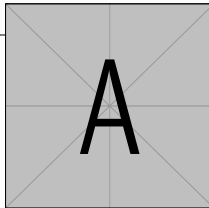


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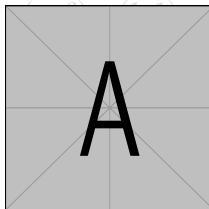


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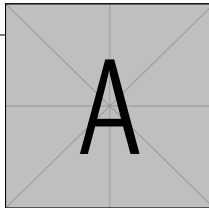


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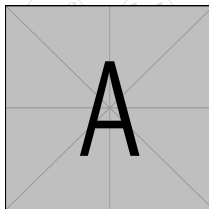


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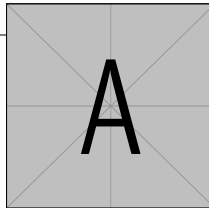


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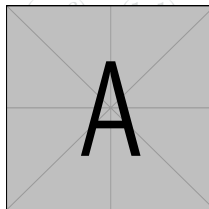


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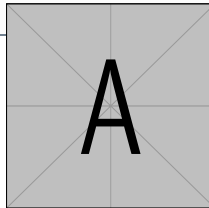


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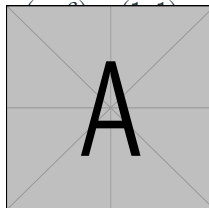


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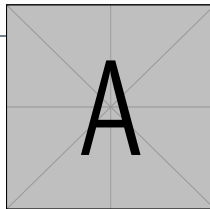


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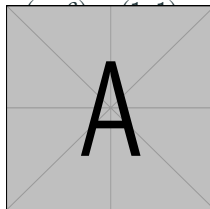


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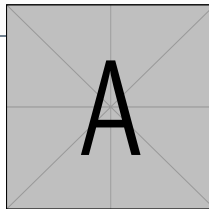


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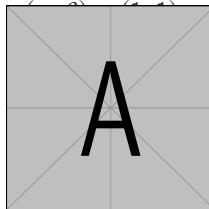


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⇒ play this arm

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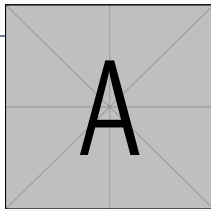


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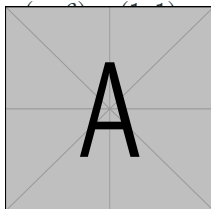


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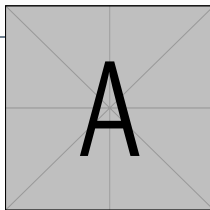


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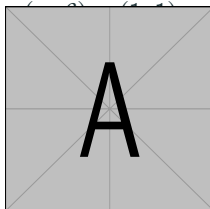


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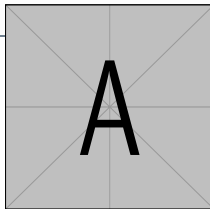


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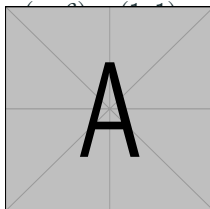


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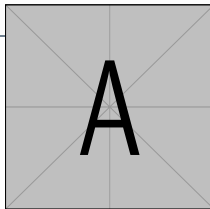


Figure 1: *

\Rightarrow play this arm
with probability ε

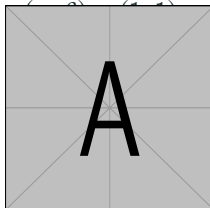


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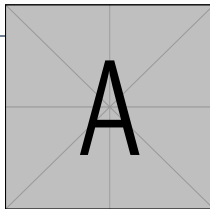


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\Rightarrow play this arm
with probability $\varepsilon \Rightarrow$

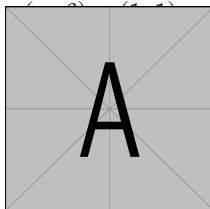


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play this arm with
probability $1 - \varepsilon$

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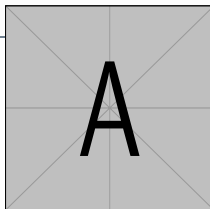


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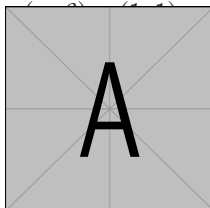


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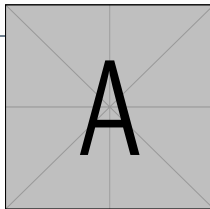


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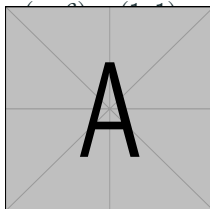


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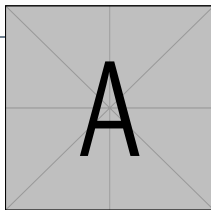


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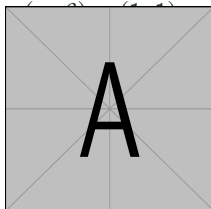


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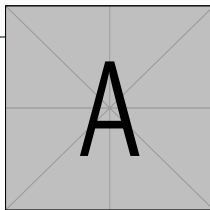


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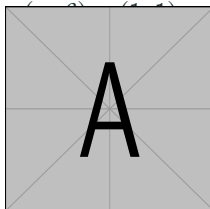


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