Session 1 - Exercises

- 1. Download the notebook files from the github repository (https://github.com/AlexRogersCS/probabilistic_machine_learning). Either install the Python package from Anaconda (https://www.anaconda.com/products/individual) and PyMC3 (https://docs.pymc.io), or open them in Google Colab (https://colab.research.google.com).
- 2. Calculate by hand, and verifying in Python (by editing the probability.ipynb script as necessary) the following probabilities when two dice are rolled:
 - (a) $P(D_1 + D_2 = 6)$
 - (b) $P(D_1 + D_2 > 10)$
 - (c) $P(D_1 = 1, D_2 < 4)$
 - (d) $P(D_1 = 1 \mid D_1 + D_2 = 4)$
 - (e) $P(D_1 < 5 \mid D_1 + D_2 = 10)$
- 3. Use Bayes rule to answer each of these three settings:
 - (a) You are planning to go on a picnic but the morning is cloudy. This is bad as 50% of all rainy days start of cloudy. However, cloudy morning are common (about 40% of days start cloudy) and this is usually a dry month (only 3 out of 30 days, or 10% of days, tend to be rainy). What is the chance of rain during the day?
 - (b) Two production lines produce the same part. Line 1 produces 1,000 parts per week of which 100 are defective. Line 2 produces 2,000 parts per week of which 150 are defective. If you choose a part randomly from the stock what is the probability it is defective? If it is defective what is the probability it was produced by line 1?
 - (c) A robot tasked with patrolling an office building has a Lidar sensor to determine if any doors are open or closed. The sensor will successfully detect an open door 60% of the time. However, it will also mistake a closed door for open door 30% of the time. If half the doors in the office building are typically left open, and the robot's sensor detects that a particular door is open, what is the robot's belief state about this door?

Session 1 - Solutions

- 1. No solution needed.
- 2. (a) 5 / 36: probability=np.sum(total==6)/N_REPEATS
 - (b) 3 / 36: probability=np.sum(total>10)/N_REPEATS
 - (c) 3/36: probability=np.sum(np.logical_and(dice1==1,dice2<4))/N_REPEATS
 - (d) 12/36: probability=np.sum(np.logical_and(dice1==1,total==4))/np.sum(total==4)
 - (e) 12/36: probability=np.sum(np.logical_and(dice1<5,total==10))/np.sum(total==10)
- 3. (a) The information we know is P(Rain) = 0.1, P(Cloud|Rain) = 0.5, and P(Cloud) = 0.4. Applying Bayes rules gives P(Rain|Cloud) = 0.125.
 - (b) The information we know is $P(D|L_1) = 1/10$, $P(D|L_2) = 3/40$, $P(L_1) = 1/3$ and P(D) = 5/60. Applying Bayes rules gives $P(L_1|D) = 2/5$.
 - (c) The information we know is P(Open) = 0.5, P(Sensor Reading|Open) = 0.6, and P(Sensor Reading|Closed) = 0.3. Applying Bayes rules gives P(Open|Sensor Reading) = 2/3 = 0.67.