Homework 4

Computation Camp

Due August 30, 2023

Submit Link: https://classroom.github.com/a/I74glvkM (https://classroom.github.com/a/I74glvkM)

Question 1 - Change-Making:

Write a function to solve the following problem using dynamic programming:

Given a value N, if we want to make change for N cents, and we have an infinite supply of each $S=\{S1,S2,\ldots,S_m\}$ valued coins, how many ways can we make the change? The order of the coins does not matter. For example, if N=10 and $S=\{2,5,3,6\}$, there are five solutions.

Hint: All solutions can be divided into the set of solutions that contain at least one of the m th coin and those that do not.

Question 2 - Rod-Cutting:

Write a function to solve the following problem using dynamic programming:

Given a rod of length n inches and an array ${\bf P}$ of prices that contains prices of all pieces of size $s \le n$, determine the maximum value obtainable by cutting up the rod in even inch increments and selling the pieces. For example, if rod is 8 inches and the piece length values are given by ${\bf P}=\{1,5,8,9,10,17,17,20\}$, then the maximum obtainable value is 22 by cutting pieces of length 6 and 2.

Hint: Call the function V(n) the maximum value obtainable for a rod of length n. Then

$$V(n) = \max_{c \in \{0,1,\dots n-1\}} \{m{P}[c] + V(n-c)\}$$

Question 3 - Knapsack:

Write a function to solve the following problem using dynamic programming:

Given weights ${m W}$ and values ${m V}$ of n items, put these items in a knapsack of capacity C to get the maximum total value in the knapsack. As an example, if ${m W}=\{10,20,30\}$ and ${m V}=\{60,100,120\}$ and C=50, then the maximum value is 220, obtained by selecting the second and third item. Bonus: argue that this problem is a generalization of the problem in Question 2.

Hint: Possible subsets of items can be split up into including the nth item or not including the nth item.

Question 4 (optional - more of an encouragement than an actual assignment)

Write down an economic problem that interests you specifically and express it as a dynamic programming problem. Solve the problem on your computer and report things about the results that you find interesting - this could be plots of decision rules, simulated results of agents solving the problem, or whatever else comes to mind.