

Feedforward Neural Networks: Revisiting Word Vectors and Text Classification

COM6513 Natural Language Processing

Nikos Aletras

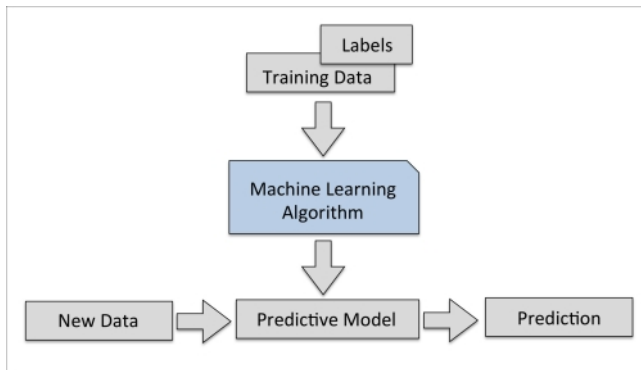
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Computer Science Department

Week 6
Spring 2021



In lecture 2...



Supervised ML

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- **Machine Learning Algorithm:** Logistic Regression
- Binary and Multi-class

Logistic Regression recap

- Compute the dot product z between the input vector \mathbf{x} and the weight vector \mathbf{w} , and add a bias term b (often ignored):

$$z = \mathbf{w} \cdot \mathbf{x} + b$$

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- Predict the class with the highest probability:

$$\hat{y} := \begin{cases} 0 & \text{if } P(y = 1|\mathbf{x}; \mathbf{w}) < 0.5 \\ 1 & \text{otherwise} \end{cases}$$

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- LR directly maps input to output and only captures linear relationships in the data

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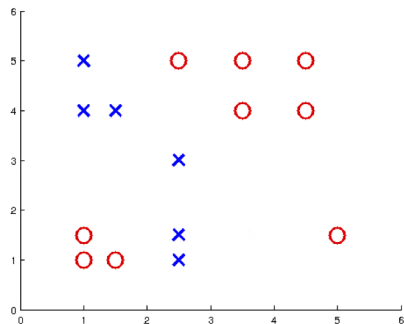
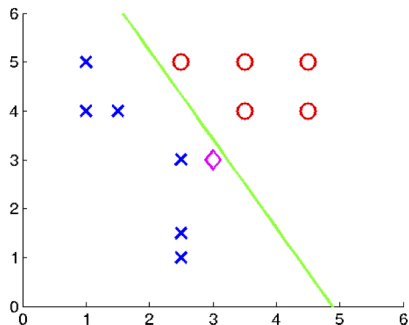
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- **Feedforward** neural networks or deep feedforward networks or multilayer perceptrons
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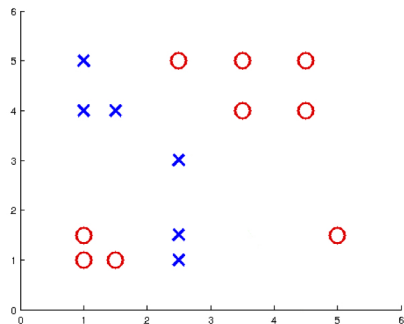
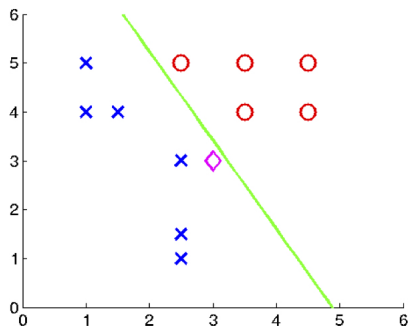
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- Pass input through a series of intermediate computations (**hidden layers**) to capture **non-linear relationships** a.k.a. **deep learning**
- Train with **SGD** and **Backpropagation** (for computing the gradients)
- NLP applications: word vectors and text classification

Limitations of linear models



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The righthand dataset is not linearly separable and cannot be learned with a linear model.

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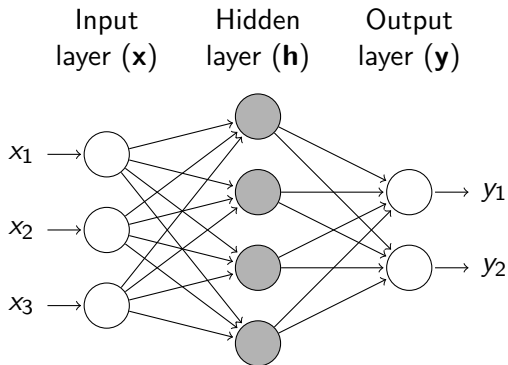
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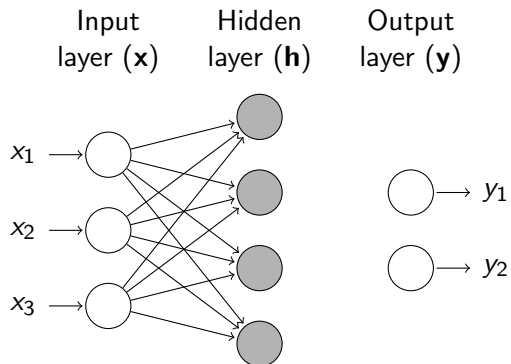
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- The final layer to obtain the prediction is called the **output** layer (e.g. sigmoid, softmax)

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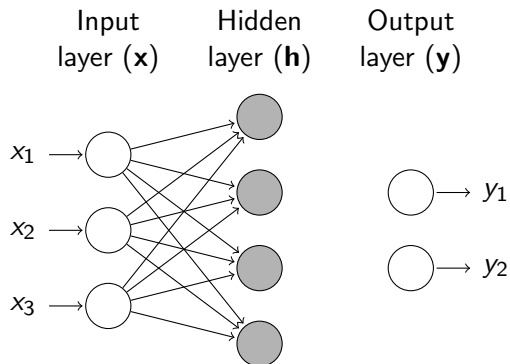


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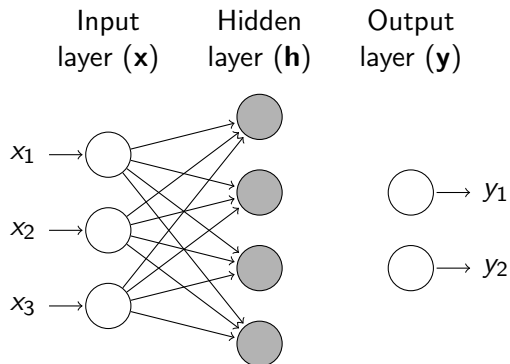
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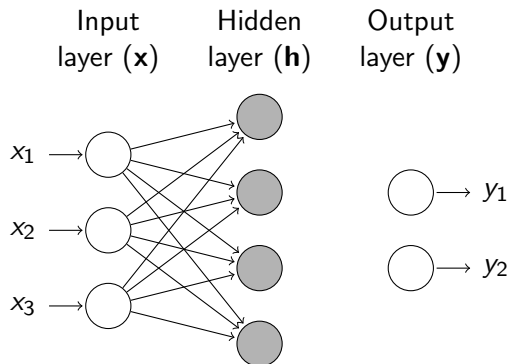


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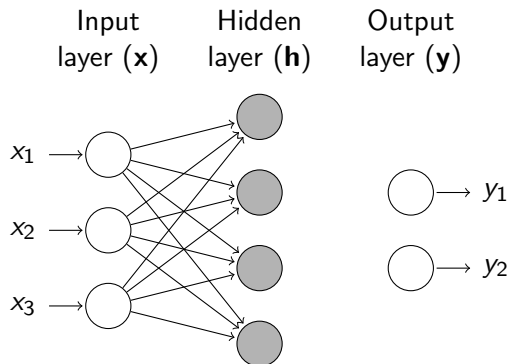
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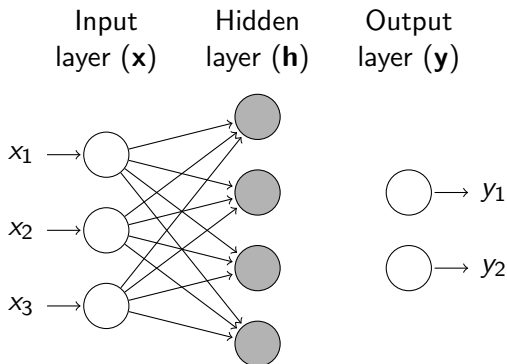
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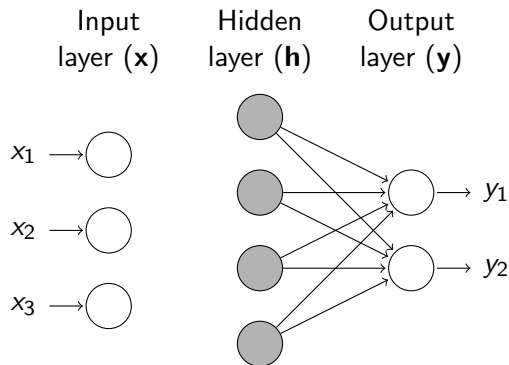


$$\begin{aligned}\mathbf{x} &\in \mathcal{R}^d, d = 3 \\ \mathbf{h} &= g(\mathbf{x}^T \mathbf{W}_h) \\ \mathbf{h} &\in \mathcal{R}^h, h = 4 \\ \mathbf{W}_h &\in \mathcal{R}^{d \times h}\end{aligned}$$

Extended to deeper architectures:

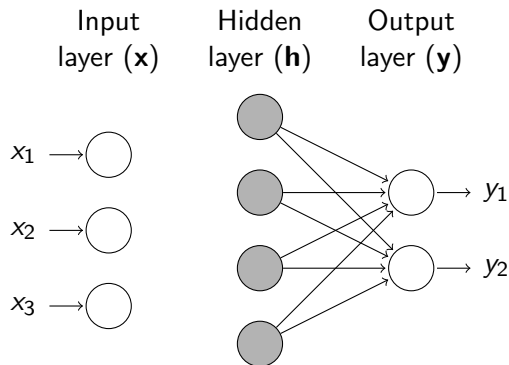
$$\mathbf{h}_i = g(\mathbf{h}_{i-1}^T \mathbf{W}_{h_i})$$

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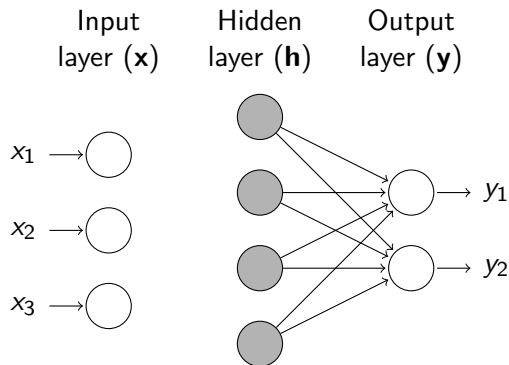
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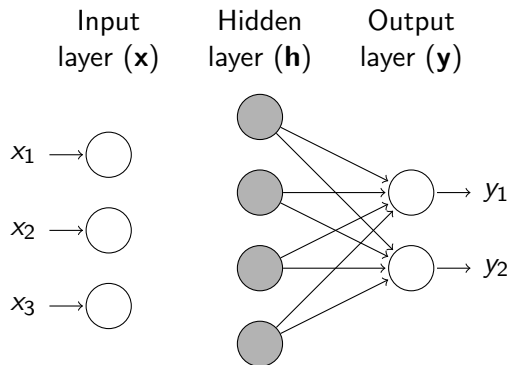
$$\mathbf{h} = g(\mathbf{x}^T \mathbf{W}_h)$$
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But what is $g(\cdot)$?

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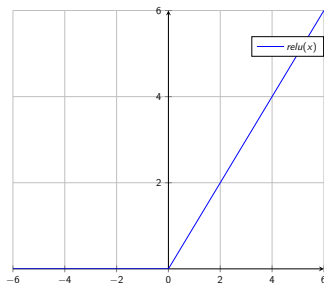
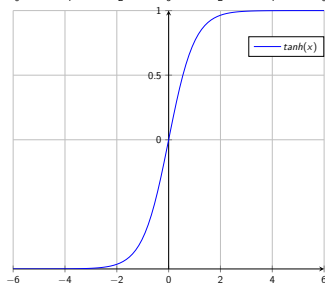
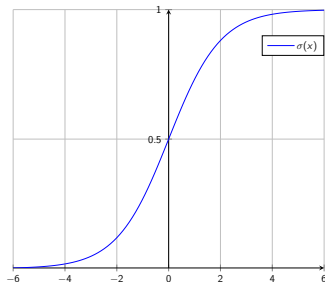
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- **Rectified Linear Unit (ReLU)**:

$$g(z) = \max(0, z)$$

- And many more...

Activation Functions



Training: Stochastic Gradient Descent (SGD) recap

Input: $D_{train} = \{(x_1, y_1) \dots (x_M, y_M)\}$, $D_{val} = \{(x_1, y_1) \dots (x_D, y_D)\}$,

learning rate η , epochs e , tolerance t

initialize \mathbf{w} with zeros

for each epoch e do

randomise order in D_{train}

for each (x_i, y_i) in D_{train} do

update $\mathbf{w} = \mathbf{w} - \eta \nabla_{\mathbf{w}} L(\mathbf{w}; x_i, y_i)$

monitor training and validation loss

if *previous validation loss – current validation loss; smaller than t*

break

return \mathbf{w}

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How to compute the gradient for the weights of the hidden layers?

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- **Forward Pass:** Compute and store all the output values of all the hidden units (for each hidden layer) and the output layer

Training: Backpropagation Algorithm

- **Forward Pass:** Compute and store all the output values of all the hidden units (for each hidden layer) and the output layer
- **Backward Pass:** Compute the gradients for the output and hidden layers with respect to the cost function L and update the weights for each layer

Training: SGD and Backpropagation

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initialise $W_i \in W = \{W_1, \dots, W_l\}$ for each layer (small random values)

for each epoch e **do**

randomise order in D_{train}

for each (x_i, y_i) *in* D_{train} **do**

layer_outputs = *forward_pass* $((x_i, y_i), W)$

$W = \text{backward_pass}((x_i, y_i), W, L, \text{layer_outputs})$

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for layer  $k = 1, \dots, l$  do  
     $\mathbf{z}_k \leftarrow \mathbf{W}_k \mathbf{h}_{k-1}$   
     $\mathbf{h}_k \leftarrow g(\mathbf{z})$   
end for
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$\mathbf{h}_k \leftarrow g(\mathbf{z})$

end for

Get prediction $\hat{\mathbf{y}} = \mathbf{h}_l$

Compute cross-entropy loss $L(\hat{\mathbf{y}}, \mathbf{y})$

return \mathbf{h}, \mathbf{z} for all layers

Backward Pass

Propagate the gradients backwards from the loss to the input layer (i.e. how each layer's output should change to reduce error):

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Convert the gradient on the layer's output (\mathbf{h}) into a gradient before the activation function (\mathbf{z}):

$$\mathbf{g} \leftarrow \nabla_{\mathbf{z}_k} L = \mathbf{g} \odot f'(\mathbf{z}_k) \quad (\odot \text{ element-wise, } f'(\cdot) \text{ deriv.})$$

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Update current weights:

$W_k \leftarrow W_k - \eta \nabla_{W_k} L$

end for

return W

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- **Dropout**: randomly ignore a percentage (e.g. 20% or 50%) of layer outputs during training:
 - Apply a random binary mask after the activation function, i.e. elementwise multiplication with vector containing 0s in random positions

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- How many layers?
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- How many layers?
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- Architecture engineering vs feature engineering
- Theory says that we can approximate any function with one hidden layer, practice says different architectures work well for different problems

Implementation tips

- Learning objective non-convex: initialisation matters
 - start with small non-zero values
 - random restarts to escape local optima
- Greater learning capacity makes overfitting more likely: regularise
- Many open libraries are available: PyTorch, Tensorflow, MxNet, Keras etc.

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- Lecture 1: word vectors by **counting** co-occurrences with context words
- **Instead**, use a feedforward network to **predict** a context word for a given word (and vice versa)
- **Word2Vec (Mikolov et al., 2013)** family, more recently supporting char n-grams (e.g. FastText)

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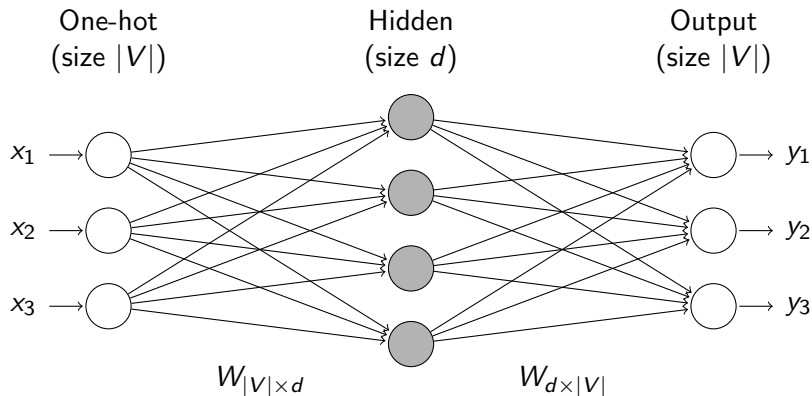
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- **Output:** softmax over the vocabulary to predict the correct context/target words respectively

Word2Vec Architecture



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- **Vector** of a word $x_i = W_i$, from the network weights
- Evaluation: standard approaches for word representation (see Lecture 1)
- Pre-trained word embeddings are widely re-used in other NLP tasks, i.e. transfer learning (more in Lecture 10)

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 - **Negative Sampling:** Update the weights for the positive word, plus the weights for a small number (5-20) other words that we want to output 0
 - **Subsampling frequent words** to decrease the number of training examples

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Applications: Text Classification

- **Approach 1:** Pass BOW vectors into a series of hidden layers (extending the LR model in Lecture 2)
- **Approach 2:** Pass one-hot word vectors through an **embedding layer** to obtain embeddings for each word in a document which are subsequently **concatenated (or added/averaged) and passed through a series of hidden layers**
- Approach 2 is more contemporary and usually the embedding layer is pre-trained (e.g. using Word2Vec) and is not updated during training

Bibliography

- Chapters 6-8 from Goodfellow et al.
- Sections 3-6 from Goldberg
-  ■ Tutorial on backprop by D. Stansbury
- Word2vec tutorial by Chris McCormick

Coming up next..

- Recurrent Networks and Neural Language Modelling