

TE 461 Marking Scheme

Title: Computer Applications and Project Design(TE 461) - Marking Scheme

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Question 1

The filter's transfer function characteristics,

$$H(\omega) = \frac{\frac{1}{j\omega C}}{R + \frac{1}{j\omega C}} = \frac{1}{1 + j\omega CR}$$

$$\text{And, } |H(\omega)| = \left[\frac{1}{1 + (\omega CR)^2} \right]^{\frac{1}{2}}$$

$$\text{Therefore, } |H(\omega)|^2 = \frac{1}{1 + (2\pi f CR)^2} = \frac{1}{1 + \left(\frac{f}{f_0}\right)^2}$$

$$\text{Where, } f_0 = \frac{1}{2\pi CR}$$

1. The output power spectral density becomes

$$G_{no}(f) = |H(\omega)|^2 G_{no}(f) = \frac{1}{1 + \left(\frac{f}{f_0}\right)^2} \cdot \frac{N_0}{2}$$

The average noise power is found by integrating $G_{no}(f)$,

$$P_n = \int_{-\infty}^{\infty} G_{no}(f) df = \frac{N_0}{2} \int_{-\infty}^{\infty} \frac{1}{1 + \left(\frac{f}{f_0}\right)^2}$$

$$\text{Let } \tan \theta = \frac{f}{f_0}, \quad f = f_0 \tan \theta, \quad \frac{df}{d\theta} = f_0 \sec^2 \theta, \quad df = f_0 \sec^2 \theta$$

$$P_n = \frac{N_0}{2} \int_{-\pi/2}^{\pi/2} \frac{1}{1 + \tan^2 \theta} \cdot f \sec^2 \theta d\theta$$

$$P_n = \frac{N_0}{2} f_0 \int_{-\pi/2}^{\pi/2} \frac{1}{1 + \tan^2 \theta} \cdot \sec^2 \theta d\theta$$

$$P_n = \frac{N_0}{2} f_0 \int_{-\pi/2}^{\pi/2} df$$

$$P_n = \frac{N_0}{2} \cdot f_0 \cdot \left[\frac{\pi}{2} + \frac{\pi}{2} \right]$$

$$P_n = \frac{N_0}{2} \pi f_0$$