# System Performance Analysis Under Correlated Shadow Fading

#### DISSERTATION

Submitted in Partial Fulfillment of the Requirements for the Degree of

DOCTOR OF PHILOSOPHY (Electrical Engineering)

at the

NEW YORK UNIVERSITY
TANDON SCHOOL OF ENGINEERING

by

Tingting Lu

May 2017

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# VITA

Sanjay Goyal was born \*\*\*\*\*.

To \*\*\*\*\*.

# ACKNOWLEDGEMENT

First and foremost I would like to thank \*\*\*\*\*\*

### ABSTRACT

#### TITLE OF YOUR DISSERTATION

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# Contents

1	Intr	oducti	ion	1
	1.1	Challe	enge, Motivation and Our Approach	1
		1.1.1	Next Generation Cellular Network	1
		1.1.2	Correlated Shadow Fading Models	4
		1.1.3	Transmission Control Protocol (TCP)	8
	1.2	Disser	tation Outline	11
<b>2</b>	Coc	perati	ve Communication to Mitigate Correlated Shadow Fad-	-
	ing			13
	2.1	Backg	round	14
	2.2	Correl	ated Shadow Fading	18
		2.2.1	Correlated Outage Field	19
	2.3	Syster	m Model	21
		2.3.1	Cooperative Communication Scheme	22
	2.4	Outag	ge Probability Analysis	24
		2.4.1	Outage Probability of the Cooperative Communication Sys-	
			tem	24
	2.5	Simula	ation and Performance Evaluation	27
		251	Rolay Placement	27

		2.5.2 Simulation Configuration	27
		2.5.3 Simulation Results and Analysis	27
	2.6	Conclusions and Future Work	35
3	Sys	tem Performance Analysis under Exponential Correlated Shade	ow
	Fad	ling	36
	3.1	Background	37
	3.2	Channel Model with Correlated Shadow Fading	40
	3.3	Markov Chain Model	43
	3.4	Analysis of Outage Behavior	46
	3.5	Simulation Results	47
	3.6	Conclusions	49
4	$\mathbf{Titl}$	le of Chapter 2	51
5	Tra	Insport Layer Protocols for 5G	<b>52</b>
	5.1	Introduction	53
	5.2	Related Work	54
		5.2.1 mmWave Channel	54
		5.2.2 Explicit Congestion Notification (ECN)	55
		5.2.3 Remy	56
	5.3	Legacy TCP Performance on Mimic 5G Channel	57
	5.4	Congestion Detection Algorithm	58
		5.4.1 Network Topology	61
		5 4 9 Data Collection	62
		5.4.2 Data Collection	-
		5.4.2 Data Collection	64

	٠
37	1
	1

	xi
6 Conclusion	69
Appendices	70
$\mathbf{A}$	71
A.1 Title of Appendix A	71
В	72
B.1 Title of Appendix B	72

# List of Figures

1.1	(a) Shadowing autocorrelation for a mobile user, (b) Shadowing	
	cross-correlation for a mobile user	5
1.2	Generic geometry of shadowing autocorrelation and cross-correlation	6
2.1	Cooperative Communication Example	15
2.2	Correlated Shadowing Fields for Increasing Resolutions (The disk	
	area is the generated correlated shadowing field and the color of the	
	areas refers to the normalized standard deviation which is $S_i/\sigma_s(\vec{r_i})$	18
2.3	Correlated Outage Fields (Dark areas are outage areas while white	
	areas are non-outage areas)	20
2.4	System Model and Three Different Relay Placements	21
2.5	Theoretical and Simulated Outage Probability for Mode $1 \dots$	28
2.6	Best Channel Condition between MS and BS or Relays of Mode	
	1 (Dashed arrow demonstrates the channel condition that satisfies	
	the SNR requirement	29
2.7	Best Channel Condition between MS and BS or Relays of Mode	
	2 (Dashed arrow demonstrates the channel condition that satisfies	
	the SNR requirement	29

2.8	Best Channel Condition between MS and BS or Relays of Mode	
	3 (Dashed arrow demonstrates the channel condition that satisfies	
	the SNR requirement	30
2.9	Cumulative Distribution Function of Outage Duration of Mode 1	
	(with Rayleigh fading)	30
2.10	Cumulative Distribution Function of Outage Duration of Mode 2	
	(with Rayleigh fading)	31
2.11	Cumulative Distribution Function of Outage Duration of Mode 3	
	(with Rayleigh fading) $\ \ldots \ \ldots \ \ldots \ \ldots \ \ldots \ \ldots$	31
2.12	Outage Frequency of Three Modes with Different Relay Densities	33
3.1	An example of building blockage	38
3.2	(a) A typical exponential correlated shadow fading field in a $50m\times$	
	50m area. The color bar denotes the value of the shadow fading in	
	dB. (b) A single cell model with a MS moving on a fixed trajec-	
	tory. (c) A locally generated correlated shadowing field for a fixed	
	trajectory from point a to point b	41
3.3	Probabilities of outage duration greater than $L$	50
5.1	GENI Topology for Performance Evaluation	57
5.2	CWND Dynamics Given Exponentially On-Off Channel Behavior	59
5.3	Throughput Dynamics Given Exponentially On-Off Channel Be-	
	havior	59
5.4	CWND Dynamics Given Uniformly On-Off Channel Behavior	60
5.5	Throughput Dynamics Given Uniformly On-Off Channel Behavior	60
5.6	Network Topology	61
5.7	NS2 TCP Trace Format	62

	XIV
5.8 Queue Length Dynamics (Cubic)	62
5.9 ROC curve of Logistic Regression Classifier	65
5.11 Decision Tree (max_depth = 3, min_samples_leaf = 100000)	66

# List of Tables

2.1	Simulation Configuration Parameters	28
3.1	Simulation Configuration Parameters	48
5.1	Simulation Parameters	63
5.2	Simulation Parameters	67

# Chapter 1

# Introduction

# 1.1 Challenge, Motivation and Our Approach

The remarkable success of cellular wireless communication technologies make it possible for smartphones to be widely used. Meanwhile, the rapid increase of use of smartphones generate dramatical demand increase for capacity in mobile broadband communications every year. With the severe spectrum shortage in conventional cellular bands, the underutilized millimeter wave (mmWave) frequency spectrum has been considered as a key component to address the bandwidth deficiency in the next generation wireless communication network.

#### 1.1.1 Next Generation Cellular Network

There are fundamental differences between current cellular communication system and mmWave communication system, in terms of high propagation loss, low delay and sensitivity to blockage. These characteristics of mmWave channel result in tough challenges to fully exploit its potential. Fading phenomena can substantially affect the performance of a wireless communication system. In general,

fading can be divided into two categories: large-scale fading and small-scale fading. Small-scale fading is caused by multipath propagation. Large-scale fading, which is also known as shadow fading, is caused by obstacles in the propagation path. Electromagnetic waves have weak ability to diffract around obstacles with a size significantly larger than its wavelength. High frequency mmWave has small wavelength, which makes it more sensitive to blockage caused by small size obstacles like buildings, trees and even nearby pedestrians or vehicles. Therefore, shadow fading has significant impact on the performance of the next generation wireless communication system. Shadow fading can cause significant received power loss. We can conclude from what we have stated above that mmWave channel can be severely vulnerable to shadowing resulting in outages, rapidly changing channel conditions and intermittent connectivity.

Shadow fading is an important factor to be considered when analyzing the system performance. In most cases, shadow fading is assumed to be temporally and spatially independent to simplify the analysis of the system performance. Obviously this is not the real scenario, especially for next generation wireless communication network. For mmWave communication networks, the cell size will become mush smaller than current LTE cell size due to high propagation pathloss. When cell size becomes relatively comparable with obstacles that cause shadow fading, shadow fading cannot be considered as spatially independent. Due to the aforementioned characteristics of mmWave channel and next generation wireless communication network, this thesis focuses on investigating the system performance under correlated shadow fading. Since there is no consensus on standard mmWave channel, we study the system performance under correlated shadow fading of the legacy cellular spectrum frequency and suggest it can be applied to mmWave channel in the future.

At first, we choose distance-angle correlation model for shadow fading and investigate the correlated shadow fading problem in a single-cell cellular network. We find that correlated shadow fading could lead to correlated outage and long outage durations. To mitigate shadow fading, relays are deployed. The performance of three different relay deployments with different relay densities are investigated. Theoretical analysis and simulations of outage performance are given to compare between different relay placement scenarios. This work illustrate that uniformly spaced relays perform better than the randomly spaced, due to the randomness of relay deployment. Single-cell model is not suitable for analyzing next generation wireless communication networks. Therefore, extending the investigation to multi-cell network is necessary. The disadvantage of the distance-angle correlation model is that it scales with cell size when considering denser network. This is not realistic since the obstacle size will not scale with the cell size. Due to this feature, we choose to use exponential correlation model when we study multi-cell network.

Exponential correlation model has been widely used by researchers. Considering a single-cell model, exponentially correlated shadow fading can be modeled as a first-order autoregressive process. Given this feature, a first-order Markov chain model is developed and validated. The Markov chain model is constructed by partitioning the entire shadow fading range into a finite number of intervals. The state transition matrix of the Markov chain is derived from the joint probability distribution of correlated log-normal shadow fading. Based on the proposed Markov chain model, the frequency and duration of outage near the edge of a single cell can be analyzed. To validate the Markov chain model, correlated Gaussian random fields are simulated to analyze the outage frequency and durations due to correlated shadow fading. Comparing the simulation results with the Markov

chain model results, we conclude that the proposed Markov chain model is an efficient way to describe the channel variations, and the user experienced outage behavior of the channel. This Markov chain model can not be extended to multi-cell system because of the existing of interference from other base stations (BSs). To further investigate the performance of multi-cell system, we run simulation for different BS densities. Two scenarios are investigated: MU connecting to the nearest BS and MU connecting to the BS with strongest signal. We calculate signal-to-noise-and-interference ratio (SINR) for the mobile user (MU) with regard to different scenarios. Outage probability and outage duration can be generated from the SINR result. We conclude that increasing BS densities can decrease outage probability when MU is connected to the nearest BS. Outage duration will decrease when increasing the BS density in both cases.

Regarding higher layer performance, an ethernet channel with high capacity, low delay and periodic on-off behavior is used to mimic the mmWave channel. Existing TCP congestion control protocols are tested on this channel. Both throughputs and the variation of congestion windows are showed with regard to different channel behaviors. A data-driven fast congestion prediction algorithm is proposed based on the idea of Explicit Congestion Notification (ECN). This fast congestion prediction algorithm can be utilized to design next generation transport layer protocols.

### 1.1.2 Correlated Shadow Fading Models

In most cases, shadow fading is modeled as an independent log-normal distribution [1] with a standard deviation derived from empirical measurements. An independent log-normal shadowing model is used widely when shadow fading can-

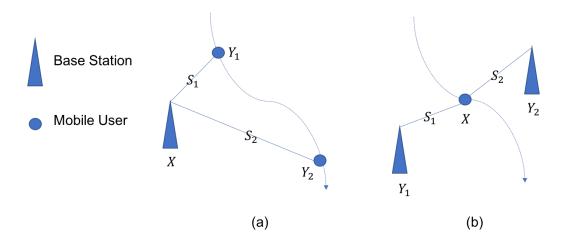


Figure 1.1: (a) Shadowing autocorrelation for a mobile user, (b) Shadowing cross-correlation for a mobile user

not be ignored. But this model fails to capture the spatial correlations in shadow fading, which has been proved to be not negligible in [2], [3] and [4]. There already exist several models for shadow fading correlation. In [5], the author elaborated different correlation models, investigated their feasibility and presented the physical plausibility of each model. Correlations can be divided into two categories: autocorrelation and cross-correlation as in Figure 1.1. Autocorrelation is the correlation between two receivers receiving signal from the same transmitting node. Cross-correlation considers two transmitting nodes transmitted to the same receiver. Autocorrelation and cross-correlation are symmetric in mathematical sense and can be investigated in the same manner.

Autocorrelation and cross-correlation models can be described as in Figure 1.2. There are N points  $Y_1, \dots, Y_N$ .  $S_i$  is the logarithm of the power attenuation due to shadowing on each path  $\vec{r_i}$ .  $\mathbb{E}\{S_i\} = 0$  since shadow fading has correlated log-normal distribution. The log-variance of shadow fading can be characterized as

$$\sigma_i^2 = VAR\{S_i\} = \sigma_S^2(\vec{r_i}) \tag{1.1}$$

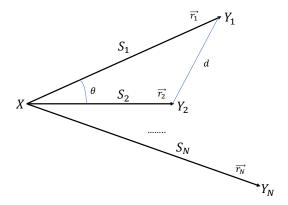


Figure 1.2: Generic geometry of shadowing autocorrelation and cross-correlation

This variance is considered as constant after a certain distance [6].

The correlation coefficients can be defined as

$$\rho_{i,j} = \mathbb{E}\{S_i S_j\} / \sigma_i \sigma_j = h(\vec{r_i}, \vec{r_j}), i \neq j$$

$$\rho_{i,i} = 1.$$
(1.2)

The following properties will be held:

- $\bullet \ -1 \le h(\vec{r_i}, \vec{r_j}) \le 1$
- $\bullet \ h(\vec{r_i}, \vec{r_j}) = h(\vec{r_j}, \vec{r_i})$

The correlation matrix of  $\mathbf{S} = [S_1, \dots, S_N]$  is:

$$\mathbf{K} = \begin{bmatrix} \sigma_1^2 & \sigma_1 \sigma_2 \rho_{1,2} & \cdots & \sigma_1 \sigma_N \rho_{1,N} \\ \sigma_1 \sigma_2 \rho_{1,2} & \sigma_2^2 & \cdots & \sigma_2 \sigma_N \rho_{2,N} \\ \vdots & \ddots & \ddots & \vdots \\ \sigma_1 \sigma_N \rho_{1,N} & \sigma_2 \sigma_N \rho_{2,N} & \cdots & 1 \end{bmatrix} . \tag{1.3}$$

For **K** to be a valid covariance matrix, it is necessary that **K** is positive semidefinite (psd).

By grouping the measurements along one variable in several ways, h can be expressed as a function of a single variable in the following three forms:

- absolute distance (between  $Y_1$  and  $Y_2$ ):  $d = ||\vec{r_1} \vec{r_2}||$ .
- angle of arrival separation:  $\theta = |\angle \vec{r_1} \angle \vec{r_2}| \in [0^\circ, 180^\circ]$
- arrival distance ratio (in decibels):  $R = |10 \log_{10} r_1/r_2| = (10/\ln 10) |\ln r_1 \ln r_2|$

A correlation model needs to satisfy as many as the following criteria to become a precise model:

- $h(\vec{r_i}, \vec{r_j}) \approx 1$  for  $\vec{r_i} \approx \vec{r_j}$ .
- $h(\vec{r_i}, \vec{r_j}) \ll 1 \text{ for } ||\vec{r_i} \vec{r_j}|| \gg 0.$
- h should be a nonincreasing function in  $\theta$ , R and d.
- h should be nonnegative.
- h should be small for large  $\theta$  and approach zero for  $\theta \approx 180^{\circ}$ , and  $r_1$  and  $r_2$  large.
- Continuity: a small change in  $\vec{r_i}$  should result in small change in  $h(\vec{r_i}, \vec{r_j})$ .
- Correlation should not depend on d only.

Considering the above criteria, the author of [5] recommended a correlated shadow fading model with distance and angle in [7] and provided a fast simulation method

to generate the correlated shadowing field. We use this model to analyze singlecell system performance and discuss how cooperative communication can help to mitigate shadow fading.

After investigating the single cell system, we want to analyze the multi-cell system performance. The aforementioned distance-angle model does not match this scenario. The correlation coefficient is a piecewise linear function of  $\theta$  and R. When the cell size scales,  $\theta$  and R remain the same, which means the correlation between two different positions also scales. Since the size of obstacles which generate shadow fading does not change with cell size, this model violate the physical characteristics of shadow fading. Exponentially correlated shadow fading is the most widely used model. To investigate the multi-cell system performance with correlated shadow fading, we choose the exponential correlation model. Exponential correlation model can be modeled as a Markov chain model in the single-cell case. This Markov model can be used to simplify the analysis of system performance. However, this Markov model cannot be used to analyze the performance of multi-cell system due to the existing of interference. Simulations are run to study the outage probability and outage duration of the multi-cell system given different network topologies.

## 1.1.3 Transmission Control Protocol (TCP)

TCP is the transport layer protocol that provides reliable connection-oriented and in-order service to applications [8]. TCP uses Error Control, Flow Control and Congestion Control to achieve this. When incoming traffic demand to the network exceeds its capacity, congestion happens and propagates to other connected networks. Congestions in network can generate long delay and high packet loss rate.

mmWave cellular network will be unstable and switching between Line-Of-Sight (LOS) and Non-Line-Of-Sight (NLOS) states frequently due to shadow fading. This behavior determines that mmWave cellular network is prone to congestion. Therefore, design an efficient congestion control protocol is necessary for next generation wireless communication network. There are two points to implement congestion control: end-to-end TCP congestion control and queuing discipline in the routers inside the network. In this thesis, we will focus on end-to-end TCP congestion control. Legacy TCP uses slow start, congestion avoidance, and fast retransmit/fast recovery to adapt to congestion in the routers. The sender maintains two variables for congestion control: a congestion window size (cwnd), which upper bounds the sender rate, and a slow start threshold (ssthresh), which determines how the sender rate is increased. Initially, cwnd increases exponentially until it reaches ssthresh. After that, cwnd increases roughly linearly. When congestion occurs, cwnd is reduced to 1 segment to avoid segment loss.

TCP relies on implicit signals received from receiver or timer time out to learn the state of the network. There are two ways in which TCP can detect packet loss:

- Timer time out: For each sent TCP segment, the sender expects to receive an acknowledgement (ACK) from the receiver within some period of time. If the ACK to a particular segment is not received by the sender before timer time out, the segment is considered to be lost.
- Duplicated ACKs: If the receiver received out of order data segment, it cannot acknowledge the out of order segment. Instead, it will acknowledge the last contiguous segment it has received prior to the lost segment. Upon the reception of the duplicate ACKs, the sender is informed about the lost

of the segment.

Both the above methods requires sender to wait for a period of time before start retransmission (timer time out or duplicate ACKs).

Considering the characteristics of mmWave channel, legacy TCP is not necessary to be a good choice for next generation networks. The slow start will be too conservative for senders to fully utilize the channel capacity. Since low delay mmWave channel switch between LOS and NLOS fast and frequently, time out and duplicate ACKs might not indicate the network condition precisely due to the long waiting time. To investigate the existing TCP performance on mmWave-like channel, we used high capacity ethernet channel with periodical on-off behavior to mimic the mmWave channel. TCP throughput of NewReno and Cubic are tested on this channel.

There are also some non-TCP congestion control techniques including Random Early Detection (RED), Explicit Congestion Notification (ECN) and so on. After investigating the legacy TCP performance on a mimic mmWave channel, we proposed an end-user TCP congestion prediction algorithm based on ECN. The key idea of ECN is to mark packets as congestion experienced when the routing queue is longer than a threshold instead of dropping them. When the receiver receives the marked packet, it response with a marked ACK to inform the sender that congestion may happen in the router. TCP senders can adjust their rate of transmission based on its own congestion avoidance algorithm. Inspired by ECN, we proposed a data driven virtual ECN algorithm to predict network congestions without involving routers or receivers.

#### 1.2 Dissertation Outline

This thesis is organized as follows. In Chapter 2, we introduce distance-angle correlated shadow fading model and investigate the system performance of a single cell cellular network. We explain that the correlated shadow fading could lead to correlated outage and long outage durations. To mitigate the shadow fading, relays are deployed to work cooperatively with the BS. The performance of three different relay deployments with different relay densities are discussed. Theoretical analysis and simulations of outage performance are given to compare between different relay placement scenarios.

In Chapter 3, the most widely used shadow fading correlation model: exponential correlation model is introduced. A Markov chain model is constructed for the spatially exponentially correlated shadow fading. This model can be used to analyze the outage behavior for a single cell system. We demonstrated that a well designed Markov chain model with an appropriate number of states corresponding to the standard deviation of the shadow fading is indeed a powerful tool to study system performance.

In Chapter 4, we extend the system performance analysis under exponentially correlated shadow fading from single-cell system to multi-cell system. We compare two different BS layout: Grid Layout and Random Layout and conclude that Grid Layout performs better than Random Layout. System performance are investigated in terms of outage probability and outage duration given different BS density and connection strategies.

In Chapter 5, we investigate the performance of legacy TCP on mimic mmWave channel. The result suggests that legacy TCP is not well designed for next generation network. We proposed a data driven machine learning congestion detection

algorithm. The algorithm can predict network congestion with high precision when network topology does not change dramatically. Future fast reacting congestion control algorithm can be designed based on this algorithm.

Chapter 6 concludes the thesis and discuss some future research directions.

# Chapter 2

# Cooperative Communication to Mitigate Correlated Shadow Fading

In a cellular network, connections between the Base Station (BS) and Mobile Stations (MS) may fail when the channel is in a deep fade. Shadow fading is large-scale fading which can cause significant received power loss for a wide area. This will lead to lost connections and/or packet loss which is harmful to mobile users, especially to those who are using real-time applications such as video conferencing. Cooperative communication is an efficient way to reduce outage and provide better Quality of Service (QoS) support for delay sensitive applications. A third station, which is often referred as a relay, can be used to forward signals between the BS and the MS. This chapter focuses on a study of the performance of relay deployments under correlated shadow fading. We consider the downlink direction in a single cell deployment, for which the shadowing effect is modeled as an angle and distance based correlated shadowing. The received signal-to-noise ratio (SNR) is then calculated by assuming jointly Gaussian shadow fading at the MS. Simulation results show channel variations over time with fixed user speed under

different relay deployments. These results demonstrate that a modest number of relays can improve the performance of real-time applications significantly.

# 2.1 Background

In a cellular communication system, the connection between the base station and a mobile station may be dropped when the mobile enters a deeply shadowed area. Shadow fading due to buildings, mountains or even trees significantly reduces the power of the received signal. In most cases, shadow fading is assumed to be temporally and spatially independent [9]. In [10] and [11], the effects of correlated shadowing in connectivity is demonstrated, which indicates that reliable connectivity will be much more difficult to maintain than indicated by independent fading shadow models. In a cellular system, for a downlink, the transmitter is a Base Station (BS) and the receiver is a Mobile Station (MS). For real-time applications (e.g. video conferencing), which require high bandwidth and are delay sensitive, the session may get dropped. In general, within a speed limit, the faster the MS moves, the more frequently the channel condition changes and the higher the connection loss frequency. The focus of this paper is to study channel variations due to correlated shadow fading, and provide a solution to reduce the frequency and duration of dropped connections by employing relays when the MS is moving.

Cooperative communication has been proven to be an efficient way to mitigate fast fading and increase the robustness of data connections [12,13]. However, cooperative communication can also efficiently maintain the connection whenever the channel condition experiences a sudden deterioration due to shadow fading by switching to different relays. Figure 3.1 is an example of cooperative commu-



Figure 2.1: Cooperative Communication Example

nication where relays and BS are placed on the top of buildings. In this case, when the MS moves to the area behind a tall building, with a high probability the signal transmitted from the BS will be obstructed by the building, and consequently the MS will encounter deep shadow fading. The channel between BS and MS will degrade and data rate will drop suddenly. In the worst case scenario, the connection with the BS may be totally lost. To combat this effect and enhance the signal received by the MS in this case, relays can be deployed on the top of tall buildings to relay the signals from the BS to MS to maintain good channel conditions between the BS and MS.

Cooperative communication has been a topic of research for several years. Madan et al. [14] studied multi-user spatial diversity in a shadow-fading environment. Other work [15–17], studied relay selection and cooperative relaying over different fading channels in different systems. Patwari et al. [18] studied relay placement in realistic deployments and confirmed that Rayleigh fading alone is not an appropriate assumption for evaluating network performance in a real deployment. In [19, 20], the authors analyzed outage probability and its duration with cooperative relaying. In an 4G-LTE network, which is strongly resilient to multipath fading, shadow fading becomes the most important fading factor [9]. Given the presence of relays, the channel variation experienced by an MS in an

environment with correlated shadow fading is still an open problem. In this paper, we analyze this problem in a single cell, and give insights on how relays could mitigate shadow fading. We will derive the critical relay density that can guarantee a certain QoS between the BS and an MS.

In most cases, shadow fading is modeled as an independent log-normal distribution [1] with a standard deviation derived from empirical measurements. An independent log-normal shadowing model is used widely when shadow fading cannot be ignored. In the log-normal shadowing model, the path loss  $\psi$  is assumed random, with a log-normal distribution given by

$$p(\psi) = \frac{\xi}{\sqrt{2\pi}\sigma_{\psi_{dB}}\psi} exp\left[-\frac{(10\log_{10}\psi - \mu_{\psi_{dB}})^2}{2\sigma_{\psi_{dB}}^2}\right], \psi > 0,$$
 (2.1)

where  $\xi = 10/\ln 10$ ,  $\mu_{\psi_{dB}}$  is the mean of  $\psi_{dB} = 10 \log_{10} \psi$  and  $\sigma_{\psi_{dB}}$  is the standard deviation of  $\psi_{dB}$ . The distribution of the dB value of  $\psi$  is Gaussian with mean  $\mu_{\psi_{dB}}$ , standard deviation  $\sigma_{\psi_{dB}}$  and is given by:

$$p(\psi_{dB}) = \frac{1}{\sqrt{2\pi}\sigma_{\psi_{dB}}} exp\left[-\frac{(\psi_{dB} - \mu_{\psi_{dB}})^2}{2\sigma_{\psi_{dB}}^2}\right].$$
 (2.2)

The above model fails to capture the spatial correlations in shadow fading. Empirical measurements show that shadowing has significant correlations in realistic scenarios that can affect system performance [2]. Considering the distribution of obstructions and the speed of the MS, a realistic channel propagation model should incorporate correlated shadow fading. Szyszkowicz et al. [5] presented a review and analysis of the feasibility of different correlated shadowing models.

In cooperative communications, relays help the BS to maintain the connection with the MS. Different cooperative schemes can be used by relays. Typically there

are two schemes: Amplify-and-Forward (AF), Decode-and-Forward (DF) [21]. In the AF mode, relays amplify the noisy signal received from the source and forward to the MS. In the DF mode, relays decode the signal received from the BS, then encode it and forward the coded signals to the MS. In this paper, we assume that DF scheme is used by relays.

Given a fixed placement of BS and a fixed moving trajectory for the MS, the efficient placement of relays to maintain the connection between BS and MS and the resulting reduction of the MS's outage probability under correlated shadow fading is the main focus of this paper. The key contributions of this paper are summarized below.

- An analysis of the relationship between correlated shadow fading and correlated outage events.
- Show how relays help mitigate correlated shadow fading. Correlated outage fields with and without relaying are given and compared.
- Analyze the performance of three different relay deployment schemes with different relay densities. The performance includes computing the best channel gain and the resulting change in outage probabilities. We also compare the advantages and disadvantages of different relay deployments.

The paper is organized as follows: Section 2.2 presents the correlated shadow fading model that is used in this paper and the resultant correlated outage. Section 2.3 presents the system model with three different relay deployments. Section 2.4 gives theoretical analysis of how relays mitigate shadow fading and reduce outage probability. Section 2.5 presents the simulation setup and analyzes the simulation results of different relay deployments. Section 2.6 summarizes the paper.

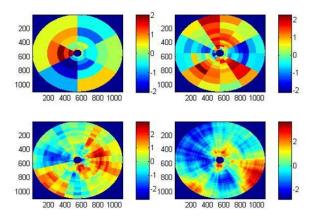


Figure 2.2: Correlated Shadowing Fields for Increasing Resolutions (The disk area is the generated correlated shadowing field and the color of the areas refers to the normalized standard deviation which is  $S_i/\sigma_s(\vec{r_i})$ )

# 2.2 Correlated Shadow Fading

As stated in the introduction, empirical measurements show that there exist different patterns of correlations between the shadowing. The independent log-normal shadow fading model, while very useful for static MS performance analysis, cannot reflect the correlation of shadow fading between different locations. In this section, we will give a brief introduction of shadow fading models, including the model used in this paper. There is no single mathematical model which captures all different categories of correlation [5]. In this paper, we use the correlated shadow fading model which incorporates the angular and distance correlations of shadow fading [7]. In [7], the author states that correlation in shadowing is indispensable for the analysis of interference of large networks and gives a time-efficient fast shadowing fields generation algorithm. The algorithm generates a correlated shadowing field  $\vec{S}$ , which gives shadow fading factor  $\vec{s_i}$  for each path  $\vec{r_i}$ 

with a correlation matrix

$$\mathbf{K}_{N\times N} = [\sigma_s(\vec{r_i})\sigma_s(\vec{r_i})h(\vec{r_i}\vec{r_j})], \tag{2.3}$$

where N paths interfere with path  $\vec{r_i}$  and  $\mathbf{E}\{S_i^2|\vec{r_i}\} = \sigma_s^2(\vec{r_i})$ . This model assumes that in the correlation matrix, h is separable with respect to the angle of arrival

$$\theta = |\angle \vec{r_i} - \angle \vec{r_i}| \in [0^\circ, 180^\circ], \tag{2.4}$$

and the arrival distance ratio

$$R = |10\log_{10} r_i/r_j| = \frac{10}{\ln 10} |\ln r_i - \ln r_j|, \qquad (2.5)$$

$$h(\vec{r_i}, \vec{r_j}) = \max\{1 - \theta/\theta_0, 0\} \cdot \max\{1 - R/R_0, 0\}.$$
 (2.6)

Following the fast shadowing field generation algorithm, we generate shadowing fields with different values of tuneable parameters. The shadowing fields are shown in Figure 2.2 with increasing resolutions. Four circular correlated shadowing fields are generated. The shadowing fields are similar to those generated in [7].

## 2.2.1 Correlated Outage Field

Given a correlated shadowing field, the outage events at different locations are also correlated. Here we analyze correlated outage events under correlated shadow fading and later give an example. In the spatial correlation of outage events, without considering Rayleigh fading, path loss is considered as constant at a fixed time point. Based on the correlated shadowing field we can generate a correlated outage field. Let G denotes total channel gain, PL denotes path loss,

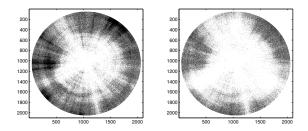


Figure 2.3: Correlated Outage Fields (Dark areas are outage areas while white areas are non-outage areas)

and S denotes shadow fading factor, we then have:

$$G = PL * S \tag{2.7}$$

For two different positions, the correlation coefficient of the two total channel gains is of the following form:

$$\rho_{1,2} = \frac{E[G_1 G_2]}{\sqrt{(Var(G_1)Var(G_2))}}.$$
(2.8)

where  $G_1 = PL_1 * S_1$  and  $G_2 = PL_2 * S_2$ . At a fixed time point, temporal correlation is neglected and only spatial correlation is considered, then  $PL_1$ ,  $PL_2$  can be assumed to be constants, which means that  $E[PL_1] = PL_1$ ,  $E[PL_2] = PL_2$ . Based on this assumption, we have

$$E[G_1G_2] = PL_1PL_2E[S_1S_2], (2.9)$$

$$Var(G_1) = PL_1^2 Var(S_1),$$
 (2.10)

$$Var(G_2) = PL_2^2 Var(S_2),$$
 (2.11)

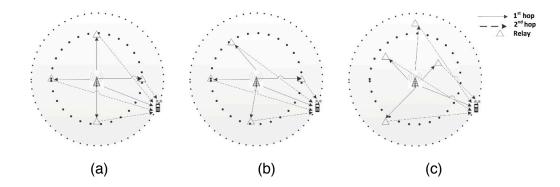


Figure 2.4: System Model and Three Different Relay Placements

Based on (2.9), (2.10) and (2.11), it is straightforward to rewrite (2.8) as:

$$\rho_{1,2} = \frac{E[S_1 S_2]}{\sqrt{Var(S_1)Var(S_2)}} = \rho_{S_1,S_2}.$$
(2.12)

The channel gain has a spatial correlation coefficient as shown above. Based on the result above, a correlated channel gain field can be generated. Given a proper threshold  $\gamma$ , the correlated outage field can be generated as in Figure 2.3. On the left, a correlated outage field without relaying is shown while the correlated outage field with relaying (3 relays uniformly placed on a circle near the edge) is given on the right. The black color indicates outage areas. In the next section we will present the methodology that helped us generate the results with relays.

#### 2.3 System Model

Since most of the key aspects of the problem can be studied in a single cell, we consider a single cell cellular deployment, where the BS is located at the center of the cell. Figure 2.4 shows the system model that is used in this paper. Several relays are placed in the cell and an MS is moving at a particular speed along the circumference at the cell edge. We picked this trajectory since it is the most

challenging path given the combination of shadowing and path loss. We consider three relay deployment modes. From left to right in Figure 2.4, (a) is the mode where relays are placed uniformly on a circle near the cell edge; (b) is relays that are randomly spaced on a circle near the cell edge; (c) is relays placed randomly in the cell. By varying relay densities in the above three different models we can analyze which combination of relay density and relay placement can meet the required QoS.

#### 2.3.1 Cooperative Communication Scheme

In this system, the BS and relays work cooperatively to try to guarantee that the MS has sufficient received power either from the BS or from relays with high probability. There are two main cooperative communication schemes: Amplify-and-Forward, and Decode-and-Forward. In this paper, we assume that relays use the Decode-and-Forward scheme. The cooperative communication system works in the following manner:

- First Hop: BS broadcasts signals to both relays and MS. If MS receives and decodes the signals transmitted by the BS successfully, there is no need for relays to repeat the transmission. If not, relays which successfully decode the signals will participate in the second hop retransmission. This mode of operation will require some signaling overhead, which is not addressed in this paper. Relays which cannot decode the received signal successfully, will not participate in the second hop.
- Second Hop: Among all relays which participate in the second hop, the one that has the best channel gain between the relay and MS will be chosen (this can be done by centralized control or using information from pilot signals).

This relay will encode the signals again and send the coded bits to the MS.

The received signal in a link  $(S \to D)$  between the source and destination is given by:

$$y_D = G_{SD}x_S + n_D. (2.13)$$

where  $x_S$  is the signal transmitted by the source and  $y_D$  is the signal received by the destination.  $n_D \sim \mathcal{CN}(0, N_0)$  is additive white Gaussian noise.  $G_{SD}$  is the channel gain from source to destination including path loss and shadow fading.  $SNR \triangleq P * G_{SD}^2/N_0$ , is the end-to-end received signal-to-noise ratio (SNR) and P is the transmitted power. The destination successfully receives the signals if no outage event happens, i.e.,  $\log_2(1 + SNR) \geq R$ , where R is the required data rate. From the definition of SNR, no outage event happens as long as  $SNR > \gamma$ , where  $\gamma = 2^R - 1$ . In the first hop, relays that can successfully decode the signals transmitted from the BS is a subset  $\mathcal{R}_n$  of N relays defined by:

$$\mathcal{R}_n \triangleq \{i : \log_2(1 + \text{SNR}_{S-i}) \ge R\},\tag{2.14}$$

where  $SNR_{S-i}$  is the received signal-to-noise ratio from BS to relay i and  $n \in \{0, 1, \dots, 2^N\}$ . In the first hop, the relay can successfully decode the BS signals if  $SNR_{S-i} > \gamma$ . The indices of all relays which are able to successfully decode BS signals form a set  $\mathcal{R}_n$ . In the second hop, the selected best relay j is the relay in  $\mathcal{R}_n$  that has the maximum SNR among all relays in  $\mathcal{R}_n$ , i.e.,  $j = \arg\max_{i \in \mathcal{R}_n} \{SNR_{i-D}\}$ , where  $SNR_{i-D}$  denotes the SNR from the ith relay to the destination MS. The BS to MS SNR is denoted by  $SNR_{S-D}$ . The SNR is determined by distance related path loss and large-scale correlated shadow fading.

#### 2.4 Outage Probability Analysis

Due to the variations of the channel gain caused by shadow fading and path loss of the propagation environment, if the end-to-end channel capacity is below the transmission rate, an outage occurs and the information packets are lost. The outage probability is an important performance measurement of the communication system. In this section, the expression for outage probability is derived.

# 2.4.1 Outage Probability of the Cooperative Communication System

If an MS cannot directly receive the signal from the BS and none of the relays can decode the BS signal, or if the MS has a bad channel with all relays which successfully decode the BS signal, then an outage event will take place. The probability that an MS cannot receive signals directly from the BS successfully is given below:

$$P_{out_0} = P[SNR_{S-D} < \gamma], \tag{2.15}$$

Under the assumption that an MS cannot successfully receive signals from the BS, the outage event happens in the first hop if no relay can receive the signal from the BS successfully, which means  $\mathcal{R}_0 = \phi$ . Based on this assumption we have:

$$P_{out_1} = \max_{i=1,\dots,N} P[SNR_{S-i} < \gamma]. \tag{2.16}$$

If the outage does not happen in the first hop, then the outage event may happen in the second hop with probability:

$$P_{out_2} = \sum_{n=1,\dots,2^N} P[SNR_{j-D} < \gamma | \mathcal{R}_n] P[\mathcal{R}_n], \qquad (2.17)$$

where j is the index of the relay which has the best channel gain between it and the MS. So the outage probability of the system is

$$P_{out_S} = P_{out_0} * (P_{out_1} + (1 - P_{out_1}) * P_{out_2}). \tag{2.18}$$

The probability density function (pdf) of shadow fading S given L correlated fading branches is

$$f_{\mathbf{S}}(\mathbf{s}) = \frac{\lambda^{L}}{\sqrt{2\pi} |\mathbf{K}_{L \times L}|^{1/2} \prod_{i=1}^{L} s_{i}} \cdot \exp(-\frac{1}{2} (10 \log_{10} \mathbf{s} - \bar{\mathbf{s}})^{T} \mathbf{K}_{L \times L}^{-1} (10 \log_{10} \mathbf{s} - \bar{\mathbf{s}})),$$
(2.19)

where  $\lambda = 10/\ln 10$  and  $\bar{\phantom{a}}$  is the average shadow fading which is normally 0.  $\mathbf{K}_{L\times L}$  is the correlation matrix which is defined in (2.3). Let  $\theta_i = \frac{10\log_{10} s_i - \mu_i}{\sqrt{2}\sigma_i}$ , and doing a change of variables gives us the pdf of  $\boldsymbol{\Theta}$  as follows:

$$f_{\mathbf{\Theta}}(`) = \frac{1}{\pi^{(L/2)|\mathbf{\Sigma}|^{1/2}}} \exp(-\mathbf{\Theta}^T \mathbf{\Sigma}^{-1} \mathbf{\Theta}), \tag{2.20}$$

where  $\Sigma$  is the correlation coefficient matrix which is

$$\begin{bmatrix} 1 & h_{1,2} & \cdots & h_{1,L} \\ \vdots & \ddots & \ddots & \vdots \\ h_{L,1} & h_{L,2} & \cdots & 1 \end{bmatrix}. \tag{2.21}$$

Since SNR=  $PL+S-N_0$  in dB, SNR>  $\gamma$  means  $S > \gamma - PL + N_0$ . Given  $S_0 = \phi$ , and letting  $\gamma_{ai}$  denote the shadow fading threshold for the *i*th relay in the *a*th hop and where a = 0, 1, 2, where the 0th hop is the direct transmission from BS to MS, we then have

$$P_{out_1} = \underbrace{\int_{-\infty}^{+\infty} \cdots \int_{-\infty}^{+\infty}}_{i=1,\dots,N} \prod g_0(\gamma_{1i}) f(\mathbf{s_1}) d\mathbf{s_1}. \tag{2.22}$$

For  $n = 1, \dots, 2^N$ , the outage probability for the second hop is

$$P_{out_2} = \sum_{n=1,\dots,2^N} \underbrace{\int_{-\infty}^{+\infty} \dots \int_{-\infty}^{+\infty}}_{i=1,\dots,N} \prod g_n(\gamma_{1i}) f(\mathbf{s_1}) d\mathbf{s_1}$$

$$\cdot \underbrace{\int_{-\infty}^{+\infty} \dots \int_{-\infty}^{+\infty}}_{i \in \mathcal{R}} \prod g_n(\gamma_{2i}) f(\mathbf{s_2}) d\mathbf{s_2}, \tag{2.23}$$

where  $\mathbf{s_1}$  is the correlated shadow fading in the first hop,  $\mathbf{s_2}$  is the correlated shadow fading in the second hop, u is a step function and

$$g_n(\gamma_{ai}) = \left\{ \begin{array}{cc} u(\gamma_{ai}) & i \in \mathcal{R}_n \\ 1 - u(\gamma_{ai}) & i \notin \mathcal{R}_n \end{array} \right.$$
 (2.24)

Due to the random nature of propagation environment,  $P_{out_0}$  is beyond our control. Therefore, to reduce the outage probability, we need to reduce  $P_{out_1}$  and  $P_{out_2}$ . Relays at proper positions with sufficient density can reduce the outage probability. Comparing different relay placements and finding the appropriate relay density to guarantee the outage probability requirement is the main issue that we will consider next.

#### 2.5 Simulation and Performance Evaluation

To study which relay placement yields the best system performance i.e., the lowest outage probability for continuous real-time applications that we assume to be running on an MS moving at the cell edge (for the given cooperative communication scheme), we set up simulations and compare performance for different relay placements.

#### 2.5.1 Relay Placement

Different relay placements as shown in Figure 2.4 are studied and compared in this section.

- Mode 1: Relays are uniformly spaced on a circle near the cell edge.
- Mode 2: Relays are randomly spaced on a circle near the cell edge.
- Mode 3: Relays are randomly placed in the cell.

#### 2.5.2 Simulation Configuration

In this paper, the Okumura-Hata model [22] is used to estimate the path loss. The values of parameters that are used in the simulation are shown in Table 3.1. In Mode 1 and Mode 2, the radius of the circle where relays are placed (near the edge) is 700m.

#### 2.5.3 Simulation Results and Analysis

In this section, numerical analysis and simulation results are presented. The best channel condition that the user can get from either BS or relay is simulated to demonstrate the improvement of the received signal strength at the MS.

Table 2.1: Simulation Configuration Parameters

Okumura-Hata Model	BS Height: $100m$
	Relay Height: 10m
	MS Height: 1.5m
	$R_0:6$
Correlated Shadow Fading	$\theta_0:\pi/3$
	$d_{min}:50m$
Relay Placements	Three Modes with Density:
	2,4,6,8,10,12
Cell Size	R:1000m
MS Moving Speed	v:10m/s
Radio Frequency	f:900MHz
BS Transmission Power	P:26dbm
SNR Requirement	8dB

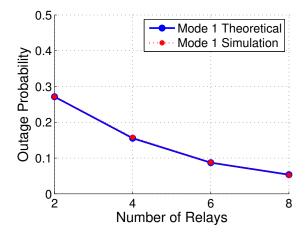


Figure 2.5: Theoretical and Simulated Outage Probability for Mode 1  $\,$ 

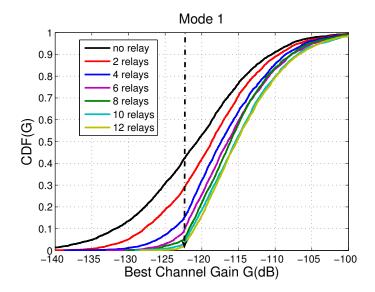


Figure 2.6: Best Channel Condition between MS and BS or Relays of Mode 1 (Dashed arrow demonstrates the channel condition that satisfies the SNR requirement.

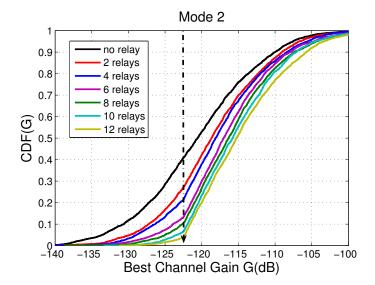


Figure 2.7: Best Channel Condition between MS and BS or Relays of Mode 2 (Dashed arrow demonstrates the channel condition that satisfies the SNR requirement.

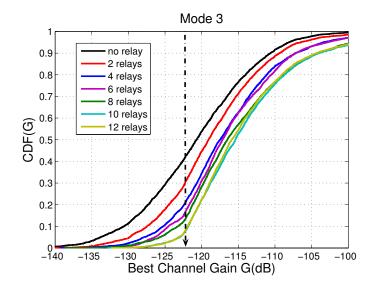


Figure 2.8: Best Channel Condition between MS and BS or Relays of Mode 3 (Dashed arrow demonstrates the channel condition that satisfies the SNR requirement.

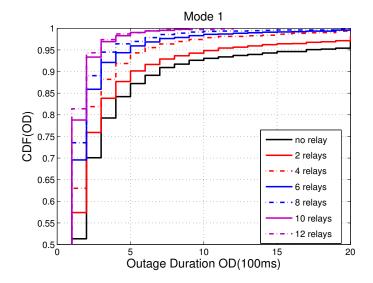


Figure 2.9: Cumulative Distribution Function of Outage Duration of Mode 1 (with Rayleigh fading)

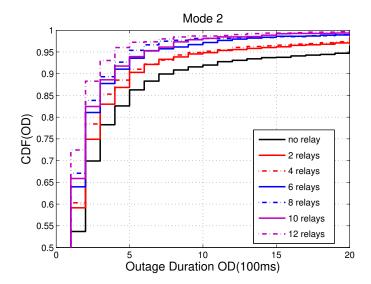


Figure 2.10: Cumulative Distribution Function of Outage Duration of Mode 2 (with Rayleigh fading)

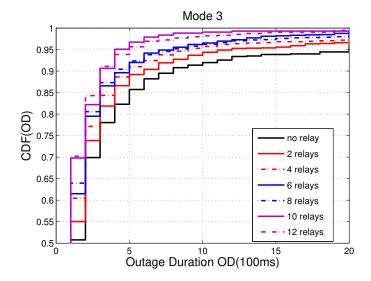


Figure 2.11: Cumulative Distribution Function of Outage Duration of Mode 3 (with Rayleigh fading)

The outage probabilities and durations are shown to indicate the potential user experience improvement when using a real-time application.

First, numerical analysis and simulation results of outage probabilities in Mode 1 is shown in Figure 2.5. The numerical analysis has high computational complexity and is difficult to apply to outage duration analysis. Therefore a simulation is necessary to study the system. Considering the computational complexity, to show that our simulation is validated by analysis, partial comparison between numerical analysis and simulation results is shown in Figure 2.5, which indicates that our simulation code is correct and can be used to study the system.

Second, we simulate the distribution of the best channel gain for the channel between the MS and BS or relays. Figure 2.6, 2.7 and 2.8 plot the distribution of the user channel gain of the three different relay deployment modes and 6 different relay densities. As shown in the figure, the intersection of the dashed arrow and the cumulative distribution function (cdf) plots indicates that as relay density increases, the percentage of outages reduces. The dashed arrow points to 122.5dBwhich is the lowest channel gain to guarantee the SNR to be above 8dB, in which case 16-QAM with 1/2 code rate will still work. Considering the power constraints, the complexity and cost of placing relays and received SNR requirements, finding a proper relay density is very important. Beyond a certain relay density, increasing the relay density will not give significant additional performance improvement. In all modes, it is shown that relays can mitigate the shadow fading efficiently. For example, in the Mode 1 case, 10 relays can improve the performance by reducing the probability of outage by 40% compared to the no relay case. To compare the results across the three different modes, we take the 10 relay case as an example. For this case, Mode 1 has an outage probability 3% less than Mode 2 and 10% less than Mode 3. In addition, we compare the three different modes from the

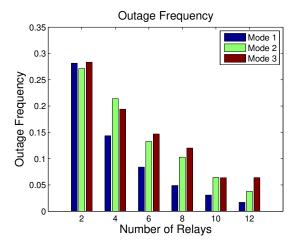


Figure 2.12: Outage Frequency of Three Modes with Different Relay Densities

outage frequency point of view. Outage frequency is defined as

$$f_{outage} = \frac{\text{Total Number of Outage Points}}{\text{Total Number of Simulation Points}}.$$
 (2.25)

Figure 2.12 shows the result of outage frequency of the three different modes and different relay densities. From this result, we can see that Mode 1 performs better than Mode 2 and Mode 3. This is due to the randomness of the relay deployment, which works against outage prevention for this model. In some cases Mode 3 performs better than Mode 2. This occurs when most of the relays in Mode 2 are placed in deep shadow areas and are therefore ineffective. The ideal relay deployment scheme would place relays at the edge of a deep fading area so that relays can successfully receive signals from the BS. On the average, random placement (Mode 3) is the worst choice among the three cases in our simulation.

For real-time applications, outage duration and outage frequency are both very important factors from the user experience point of view. Long outage duration and high outage frequency will lead to poor delay performance or even loss of packets. Figure 2.12 indicates that higher relay density will result in lower outage

frequency. Next we investigate the outage duration experienced by the MS with different relay deployments. Outage duration performance is given in Figure ??, which shows the cumulative distribution functions for outage durations for all three different modes. Here, we just show the distribution of outage duration from 100ms to 2s (100ms is the smallest simulation time period). Under the SNR requirement given as 8dB, it is shown that as the relay density increases, the probability of long outage duration decreases quickly. In Mode 1, with 4 relays, the probability of outage duration longer than 400ms is less than 10%. In Mode 2 and Mode 3, to achieve this, 6 and 8 relays are needed, respectively. For real-time video conferencing, the largest tolerable delay is around 200ms. Our results indicate that in Mode 1 we do not need more than 6 relays to guarantee the probability of outage duration larger than 200ms to be less than 15%. In Mode 2 and Mode 3 more than 12 relays are needed to achieve this objective. Since we put the SNR requirement as 8dB, which guarantees a small bit error rate (BER) of 16-QAM, the relay density needs to be high. If we reduce the SNR requirement and change the modulation, it is possible that the probability of outage duration longer than 200ms will become smaller or even close to 0. If there is no relay in the cell and an MS enters into a deep fading area, then due to correlated shadow fading, this outage duration will last for a long time. The longest outage duration in our simulation is 10s with no relay. From Figure 2.9, 2.10 and 2.11 we can observe that the probability of an outage duration greater than 2s is approximately 5% without relaying. Comparing the no relay case with the 6 relays case in Mode 1, it is shown that relays efficiently reduce the lengthy outages which are caused by deep shadow fading, with the probability of outage duration greater than 2s reduced to less than 1%. All these results indicate that relays can mitigate the deleterious effects of correlated shadow fading efficiently.

#### 2.6 Conclusions and Future Work

In this paper, we investigate the correlated shadow fading problem in a single cell cellular network and shows that it could lead to correlated outage and long outage durations. A correlated outage field is presented in the paper. To mitigate shadow fading, relays can be deployed. The performance of three different relay deployments with different relay densities are studied. Theoretical analysis and simulations of outage performance are given to compare between different relay placement scenarios. Through these simulation, we showed that uniformly spaced relays perform better than the randomly spaced, due to the randomness of relay deployment. In future work, we will consider more realistic relay placements, where they have good channels to the base station. We also plan to extend our analytic work to build a model that can predict the impact of shadow fading in a mobile environment to different parameter settings.

# Chapter 3

# System Performance Analysis under Exponential Correlated Shadow Fading

Shadow fading has been proven to be a significant contributor to channel variations in wireless communication. In most cases shadow fading is assumed to have a log-normal fading distribution to model the loss at a certain location. However, in a mobile network, it is also important to know how shadow fading is correlated both in space and in time, which can greatly affect application layer behavior and service quality. This chapter is an attempt to characterize shadow fading so as to accurately study its impact on the application layer quality of service. If the correlation is strong over time and space, shadow fading can result in a long outage. In this chapter, we assume shadow fading is exponentially correlated in space. To study correlated shadow fading and its resultant outage durations, a first-order Markov chain model is developed and validated. The Markov chain model is constructed by partitioning the entire shadow fading range

into a finite number of intervals. The state transition matrix of the Markov chain is derived from the joint probability distribution of correlated log-normal shadow fading. Based on the proposed Markov chain model, the frequency and duration of outage near the edge of a single cell is analyzed. To validate the Markov chain model, correlated Gaussian random fields are simulated to analyze the outage frequency and durations due to correlated shadow fading. Comparing the simulation results with the Markov chain model results, we can conclude that the proposed Markov chain model is an efficient way to describe the channel variations, and the user experienced outage behavior of the channel.

#### 3.1 Background

In the past few decades, fading in wireless communication systems has been studied extensively in the literature. Fading phenomena can substantially affect the performance of a wireless communication system. In general, fading can be divided into two categories: large-scale fading and small-scale fading. A signal transmitted from source to destination will experience both large-scale and small-scale fading. Small-scale fading is caused by multipath propagation. Large-scale fading, which is also known as shadow fading, is caused by obstacles (trees, buildings, etc.) in the propagation path. Shadow fading is approximated by an independent log-normal distribution [9] in most cases. Researchers have also shown that shadow fading is spatially correlated at different positions on the propagation path [23], [24]. The spatial correlation of shadow fading is important when studying the quality of service of a mobile system since it will result in long-lasting outage durations, which will deteriorate the performance of the applications running on the network. For example, in Figure 3.1, the user is moving behind a row

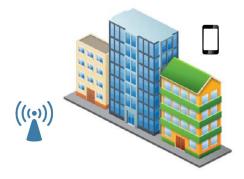


Figure 3.1: An example of building blockage.

of tall buildings which block the signals from the base station. These tall buildings result in deep shadow fading, and the shadow fading of different positions behind these buildings are closely correlated.

The spatial correlation of shadow fading has been investigated by numerous researchers. Based on empirical measurements, different autocorrelation models have been proposed for different scenarios and radio frequencies [23, 25, 26]. Szyszkowicz et al. [5] studied shadow fading correlation models and investigated the feasibility of all these models. Among all these models, the analytical model proposed by Gudmundson [23] based on empirical measurements of 900MHz frequency is the one which is widely used in channel estimation. This model shows that shadow fading can be modeled as a first-order autoregressive process AR(1), which indicates a spatial exponential decaying autocorrelation function. Given this model, we propose a Markov chain model that can be constructed to capture the variation of shadow fading. The Markov chain models can in turn be used to accurately model the impact of shadow fading on higher layer protocols and applications. Since the shadow fading statistically follows a log-normal distribution, we can divide the entire range of shadow fading, which is  $[-\infty, +\infty]$  into a finite number of intervals. Each interval is considered as a state of the Markov chain

model. When the shadow fading falls in a particular interval, it is assigned to be in this particular state. The number of intervals (states) defines the granularity of the Markov chain model. The higher the number of states, the higher the precision in modeling the shadow fading. Correlated log-normal shadow fading has different variances with regard to different scenarios. For example, urban and suburban areas have different standard deviations based on empirical measurements. Different standard deviations of the log-normal shadow fading will result in different state transition matrices of the Markov chain model.

Outage events happen when the channel state is poor, and the received signals are not strong enough for the receiver to decode. Outage probability and the length of outage duration are important performance measurements of a wireless communication system over fading channels. Considering the applications which require low latency where buffer size is small, a long outage duration will drop the connection and lower the quality of service. To study the outage behavior of a communication system under correlated shadow fading, a well designed Markov chain model is a powerful tool. With a Markov chain model, the channel state in the next user position can be estimated from the current channel state given the current user position. Therefore, the system performance can be evaluated efficiently. Fading is a significant factor which causes dramatic channel state variations. Correlated shadow fading will result in long-lasting outage durations which is harmful to delay-sensitive real-time application and result in loss of quality of service. The Markov chain model can be used to analyze the probability distribution of outage events. The distribution and behavior of outage events will provide us the necessary information to improve wireless communication systems further. For example, efficient cooperative communication schemes can be designed to mitigate the outage behavior.

The main focus of this chapter is how to design a first-order Markov chain model to reflect the spatial correlation of shadow fading, and the study of outage behavior of a single cell wireless communication system given correlated shadow fading. The key contributions of this chapter are summarized below.

- Constructed a Markov chain model based on correlated shadow fading.
- Analyzed the outage frequency and outage duration of a single cell wireless communication system over correlated shadow fading.

The remaining sections of this chapter are organized as follows. The channel model with spatial correlated shadow fading is described in Section 3.2. Section 3.3 shows how to construct the Markov chain model from the correlated shadow fading. Analysis of outage behavior is demonstrated in Section 3.4. Simulation to validate the Markov chain model is illustrated in Section 3.5. Section 3.6 summarizes and concludes the chapter.

# 3.2 Channel Model with Correlated Shadow Fading

To simplify the problem, we consider a single 4G LTE cell without any intercell interference in Figure 3.2(b). Due to the high bandwidth of OFDM systems, LTE networks are more resilient to frequency selective fading [9], therefore in this paper small-scale fading is ignored and shadow fading becomes the most important fading factor. There is a Base Station(BS) at the center of the cell. A Mobile Station (MS) is moving on a certain trajectory within the cell. The received signal

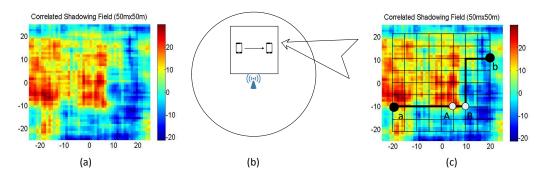


Figure 3.2: (a) A typical exponential correlated shadow fading field in a  $50m \times 50m$  area. The color bar denotes the value of the shadow fading in dB. (b) A single cell model with a MS moving on a fixed trajectory. (c) A locally generated correlated shadowing field for a fixed trajectory from point a to point b.

on a link  $(S \to D)$  between source and destination is given by:

$$y_D = G_{SD}x_S + n_D. (3.1)$$

where  $x_S$  is the signal transmitted by the source and  $y_D$  is the signal received by the destination.  $n_D \sim \mathcal{CN}(0, N_0)$  is additive white Gaussian noise.  $G_{SD}$ is the channel gain from source to destination including path loss and shadow fading.  $\text{SNR} \triangleq P*G_{SD}^2/N_0$ , is the end-to-end received signal-to-noise ratio (SNR). The destination successfully receives the signals if no outage event happens, i.e.,  $\log_2(1+\text{SNR}) \geq R$ , where R is the required data rate. From the definition of SNR, no outage event happens as long as  $G_{SD}^2 > \beta$ , where  $\beta = \frac{(2^R-1)*N_0}{P}$ . Therefore the channel gain from transmitter to receiver determines if an outage will occur.

Here we rewrite the channel gain in the following form:  $G_{dB} = PL(d) + S$ , where  $G_{dB}$  is  $G_{SD}$  in dB, PL denotes the propagation pathloss in dB, d is the distance from BS to MS and S denotes shadow fading factor. In most cases, shadow fading is modeled as an independent log-normal distribution [1] with a standard deviation derived from empirical measurements. In this model, the probability

distribution of pathloss  $G_{dB}$  is given by:

$$p(G_{dB}) = \frac{1}{\sqrt{2\pi}\sigma_{G_{dB}}} exp\left[-\frac{(G_{dB} - \mu_{G_{dB}})^2}{2\sigma_{G_{dB}}^2}\right].$$
(3.2)

where  $\mu_{G_{dB}}$  is the average pathloss which is equal to PL(d) and  $\sigma_{G_{dB}}$  denotes the standard deviation of pathloss. Since shadow fading is the only fading factor that is considered here,  $\sigma_{G_{dB}}$  is determined by the standard deviation of shadow fading. This model fails to capture the spatial correlations in shadow fading. For examples, in Figure 3.2(c), shadow fading factors of two close positions A and B, which are  $S_A$  and  $S_B$ , are not independent but correlated to each other. Empirical measurements showed that shadowing has significant correlations in several realistic scenarios and the correlated shadow fading can affect system performance [2]. Among all models derived from empirical measurements for correlated shadow fading, exponentially decaying correlation [23] is widely used. In this paper, we choose this model to do further analysis. Figure 3.2(a) is an example of exponentially correlated shadowing field which is generated from the Graziano model [2]. This figure shows a  $50 \times 50m^2$  shadow fading area and illustrates that deep shadowing area is clustered and correlated (the blue area).

In Figure 3.2(c), the entire space is discretized. The MS moves on the lattice as shown. A and B are two neighbouring points. Assume the shadow fading (in dB) is  $N(0, \sigma^2)$  where  $\sigma$  is the standard deviation, the spatial correlation between  $S_A$  and  $S_B$  will be given by

$$\rho_{A,B} = \frac{E[S_A S_B]}{\sigma^2} = e^{-\frac{d_{A,B}}{d_0}} \tag{3.3}$$

where  $d_{A,B}$  is the distance between A and B,  $d_0$  denotes the de-correlation distance

[27], which means if the distance between two points are substantially greater than  $d_0$ , the two shadow fading will be independent to each other.  $d_0$  is determined by the environment, therefore urban and suburban areas have different de-correlation distances. An exponential correlation implies the shadow fading samples can be written as an AR(1) process as follows [28]:

$$S_B = \rho S_A + (1 - \rho) n_A \tag{3.4}$$

where  $n_A$  denotes the channel noise at A. From this we conclude that the next channel state can be determined from the current channel state and the distance MS moves.

#### 3.3 Markov Chain Model

In this section, we will construct a Markov chain model for exponential correlated shadow fading. First of all, we will discretize the space. In Figure 3.2(c), the space was partitioned into unit square spaces of  $5 \times 5m^2$  (This granularity is used to describe the Markov chain model while in the simulation we uses a finer granularity). The MS moves on the lattices from point to point, the distance between each two neighboring points are considered as a unit distance  $\delta d$ . We prove that shadow fading factors of any two points that can be connected by a trajectory having jointly Gaussian distribution.

**Lemma 1.** Exponential correlated shadow fading factors of any two points that can be connected by a trajectory have a jointly Gaussian distribution.

*Proof.* Suppose the two points are a and b, since there exists a trajectory connecting a and b like in Figure 3.2(c), we can assume there are n positions on this

trajectory  $(t_1, t_2, \ldots, t_n)$ . Then follow equation (3.4), we have the following:

$$S_{b} = \rho S_{t_{n}} + (1 - \rho) n_{t_{n}}$$

$$= \rho(\rho S_{t_{n-1}} + (1 - \rho) n_{t_{n-1}}) + (1 - \rho) n_{t_{n}}$$

$$= \dots$$

$$= \rho^{n} S_{t_{1}} + \sum_{i=1}^{n} \rho^{n-i} (1 - \rho) n_{t_{i}}$$

$$= \rho^{n+1} S_{a} + \rho (1 - \rho) n_{a} + \sum_{i=1}^{n} \rho^{n-i} (1 - \rho) n_{t_{i}}$$
(3.5)

Let  $X = \alpha S_a + \beta S_b$ , from equation 3.5, the following can be derived:

$$X = \alpha S_a + \beta (\rho^{n+1} S_a + \rho (1 - \rho) n_a + \sum_{i=1}^n \rho^{n-i} (1 - \rho) n_{t_i})$$
 (3.6)

Since  $S_a$ ,  $n_{t_i}$  and  $n_a$  are all independent and Gaussian random variables, we conclude that X is also Gaussian, which implies that  $S_a$  and  $S_b$  are jointly Gaussian.

Given the above conclusion, a Markov chain model can be constructed as follows:

- Divide the entire shadow fading range  $[-\infty, +\infty]$  into a finite number of intervals  $\{[-\infty, S_0], [S_0, S_1], \dots, [S_N, +\infty]\}$ . Each interval represents a state of the Markov chain model.
- Derive the state transition matrix of the Markov chain model from the probability distribution of the correlated shadow fading.
- Derive the steady-state probability from the state transition matrix of the Markov chain model.

To derive the state transition matrix of the Markov chain model, we first investigate the probability density function of the correlated shadow fading. Since we have discretized the entire space into unit distances, here the state transition probability from point A to point B will be defined and used to calculate the state transition matrix of the Markov chain. Since  $S_A$  and  $S_B$  are jointly Gaussian with a correlated coefficient  $\rho_0$ , according to [29], we have

$$f_{S_A|S_B=s_B}(s_A) = \frac{f_{S_A,S_B}(s_A, s_B)}{f_{S_B}(s_B)}$$

$$= \frac{1}{\sigma_A \sqrt{2\pi(1-\rho_0^2)}} \exp\left\{-\frac{(s_A - (\mu_A + \sigma_A \rho_0(s_B - \mu_B)/\sigma_B))}{2\sigma_A^2(1-\rho_0^2)}\right\}$$
(3.7)

where  $\mu_A$  and  $\mu_B$  are expectations of log-normal shadow fading  $S_A$  and  $S_B$ , which is typically set to 0, while  $\sigma_A$  and  $\sigma_B$  are standard deviations, which are assumed to be equal to  $\sigma_0$ . Based on these assumptions, we can rewrite the equation as follows:

$$f_{S_A|S_B=s_B}(s_A) = \frac{1}{\sigma_0 \sqrt{2\pi(1-\rho_0^2)}} \exp\{-\frac{s_A - \rho_0 s_B}{2\sigma_0^2(1-\rho_0^2)}\}$$
(3.8)

Assume there are N states of the Markov chain model  $ST_1, ST_2, \dots, ST_N$  where  $ST_i$  corresponds to the interval  $(S_{i-1}, S_i]$ . Then we have the state transition probability as follows:

$$P_{i,j} = P(S_A \in ST_j | S_B \in ST_i)$$

$$= \frac{P(S_A \in ST_j, S_B \in ST_i)}{P(S_B \in ST_i)}$$

$$= \frac{\int_{S_{i-1}}^{S_i} (\int_{S_{j-1}}^{S_j} f_{(S_A | S_B = s_B}(s_A) ds_A) f(s_B) ds_B}{\int_{S_{i-1}}^{S_i} f(s_B) ds_B}$$
(3.9)

From equation (3.9), the state transition matrix of the Markov chain can be derived. The steady-state transition matrix can be determined by P.

#### 3.4 Analysis of Outage Behavior

In this section we analyze the outage behavior of the communication system using the Markov chain model of correlated shadow fading. The outage duration of a system is a significant factor influencing system performance. Given a fixed mobile trajectory, the Markov chain model described in Section 3.3 provides an efficient way to study the outage events. In Figure 3.2(c), a fixed trajectory is given from point a to b through several intermediate points. Considering two consecutive points A and B, we have  $G_A = PL_A(d_A) + S_A$  and  $G_B = PL_B(d_B) + S_B$  in dB. The probability that A and B are both in an outage area can be written as:

$$P(G_A < \gamma, G_B < \gamma)$$

$$= P(S_A < \gamma - PL_A(d_A), S_B < \gamma - PL_B(d_B))$$
(3.10)

If  $S_A < \gamma - PL_A(d_A) \in ST_i$  and  $S_B < \gamma - PL_B(d_B) \in ST_j$ , we can infer that, to avoid outage, the lower bound of the shadow fading factor  $S_A$  is in state  $ST_i$  and for  $S_B$  is in state  $ST_j$ . State  $ST_i$  and  $ST_j$  are called lower bound states. Based on this approximation, the above probability can be written as:

$$P(G_A < \gamma, G_B < \gamma) = \sum_{m=0}^{i} \sum_{n=0}^{j} P(ST_m) \bullet P(ST_m, ST_n)$$
 (3.11)

where  $P(ST_m)$  is the probability that  $S_A$  is in the range of  $ST_m$  which can be calculated from the Gaussian distribution.  $P(ST_m, ST_n)$  can be found from the state transition matrix. Following this, the probability of an outage duration of

$$P = \begin{bmatrix} 0.5580 & 0.3627 & 0.0757 & 0.0036 & 3.5243 \times 10^{-5} & 0 & 0 & 0 \\ 0.1587 & 0.4404 & 0.3359 & 0.0624 & 0.0026 & 2.3466 \times 10^{-5} & 0 & 0 \\ 0.0184 & 0.1788 & 0.4546 & 0.2980 & 0.0484 & 0.0018 & 1.4485 \times 10^{-5} & 0 \\ 0.0007 & 0.0258 & 0.2165 & 0.4624 & 0.2573 & 0.0361 & 0.0012 & 8.4341 \times 10^{-6} \\ 8.4341 \times 10^{-6} & 0.0012 & 0.0361 & 0.2573 & 0.4624 & 0.2165 & 0.0258 & 0.0007 \\ 0 & 1.4485 \times 10^{-5} & 0.0018 & 0.0484 & 0.2980 & 0.4546 & 0.1788 & 0.0184 \\ 0 & 0 & 2.3466 \times 10^{-5} & 0.0026 & 0.0623 & 0.3359 & 0.4404 & 0.1587 \\ 0 & 0 & 0 & 3.5243 \times 10^{-5} & 0.0036 & 0.0757 & 0.3627 & 0.5580 \end{bmatrix}$$

length l > L can be derived in below:

$$P(G_1 < \gamma, \dots, G_L < \gamma) =$$

$$\sum_{m_1=0}^{M_1} \dots \sum_{m_L=0}^{M_L} P(ST_{m_1}) \bullet P(ST_{m_1}, ST_{m_2})$$

$$\bullet \dots \bullet P(ST_{m_{L-1}}, ST_{m_L})$$
(3.12)

where  $M_i$ ,  $i \in \{1, ..., L\}$  are corresponding lower bound states of each position on the trajectory.

#### 3.5 Simulation Results

In this section, we employ Monte-Carlo simulation to validate our Markov chain model. To start the simulation, a large number of correlated shadowing fields are generated. As shown in Figure 3.2(b) and (c), instead of generating shadowing fields for the entire cell, we pick up a MS trajectory and generated shadowing fields that covers that trajectory. In this paper, we choose the urban environment as the case to study. In this case, the shadow fading and Markov chain parameters are set as in Table 3.1. The standard deviation of shadow fading is chosen to be 8dB following [5]. The number of states of the Markov chain is set to be  $3 * \sigma_0/n * 2 + 2$ , where n = 1, 3, 8 is the size of each range (state) in dB except the two above  $3\sigma_0$ . n in this case represents different granularities in the

Okumura-Hata Model	BS Height: 100m
	MS Height: $1m$
	De-Correlation Distance $d_0$ : 20 $m$
	Standard Deviation $\sigma_0$ : $8dB$
Correlated Shadow Fading	Number of States:
Markov Chain Model	50, 18, 8
	$(3*\sigma_0/n*2+2, n=1,3,8)$
MS Trajectory	Unit Distance $\delta d$ : 1m
Shadowing Field	$50 \times 50m^2$
Radio Frequency	f:1024MHz
BS Transmission Power	P:30dbm
SNR Requirement	10dB

Table 3.1: Simulation Configuration Parameters

area of  $[-3\sigma_0, 3\sigma_0]$ . The state transition matrices are calculated with regard to each n. For example, when n = 8, the states of the Markov chain model are:

$$[(-\infty, -24], (-24, -16], (-16, -8], (-8, 0],$$

$$[0, 8], [8, 16), [16, 24), [24, +\infty)]$$
(3.14)

and the state transition matrix is given in (3.13).

To validate our Markov chain models, the probability distributions of outage durations corresponding to MS trajectories of length l>1m up to l>9m are studied given different number of states. Since there is a trade-off between the number of states and the complexity of the simulation computation, the simulated results also provide us information about the proper granularity of the Markov chain model to most accurately approximate the real channel. The simulation also confirms that correlated shadow fading indeed can cause long-lasting outage durations. In our simulation, the MS moves on a straight track which is around 900m away from the BS. Let l denote the outage duration in meters, Figure 3.3 shows the probability of l>L. Comparing the two cases: with and without

correlation, we can conclude that correlated shadow fading can result in severe long-lasting outage durations. Take L=5 for example, the correlated case gives P(l>L)=12%, while in the non-correlated case the probability is around 0%. This illustrates the correlation between shadow fading cannot be neglected in mobility models. The MS speed is approximately the same as pedestrian speed which is 1m/s (Since the edge length of the lattice is 1m, the MS moves one grid (unit distance) every second). Assuming this, the user will experience an outage of more than 9 seconds with a probability of 7%.

To find out the proper number of states of the Markov chain model, three different Markov chain models with different number of states are tested. Basically we divide the  $[-3\sigma_0, 3\sigma_0]$  area with different granularity, which is represented by n = 1, 3, 8. When n = 1, the interval  $ST_i$  except  $(-\infty, S_0]$  and  $[S_N, +\infty)$  is 1dB. The results showed in Figure 3.3 indicates that when n = 1, the curve is close to the correlation curve, which means that the Markov chain model becomes a good approximation of the channel to study the outage behavior of the system. Generally, more Markov states lead to more precise models. When the interval  $[S_i, S_j]$  becomes relatively large with regarding  $\sigma_0$ , the Markov chain model will fail to be a useful tool to study the outage behavior of the system. For example, in Figure 3.3, when n = 8, P(l > 1) is almost twice the correct P(l > 1). The prediction of the outage behavior of the system is not precise and useful anymore.

#### 3.6 Conclusions

In this chapter we investigated how shadow fading at different positions in a cellular network is correlated. In an environment where the correlation is high,

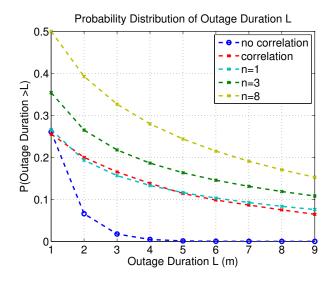


Figure 3.3: Probabilities of outage duration greater than L.

shadow fading will result in long-lasting outage durations which can lead to a significant deterioration in system performance. To model spatially correlated shadow fading we divided the entire range of shadow fading into a finite number of intervals. A Markov chain model is then constructed, where each interval becomes a state of the Markov chain model. This model can be used to analyze the outage behavior at the application layer. We demonstrated that a well designed Markov chain model with an appropriate number of states corresponding to the standard deviation of the shadow fading is indeed a powerful tool to study system performance.

Chapter 4

Title of Chapter 2

## Chapter 5

## Transport Layer Protocols for 5G

The rapid increase of use of smartphones generate dramatical demand increase for capacity in mobile broadband communications every year. The wireless carriers and researchers are motivated to explore the underutilized millimeter wave (mm-wave) frequency spectrum for next generation (Fifth Generation) broadband cellular communication networks. Fifth generation (5G) mm-wave communication system will provide high speed, high capacity wireless communication networks to users. Meanwhile, 5G mm-wave channel is sensitive to obstructions, which result in high fluctuations. Legacy transmission control protocols (TCP) might not work properly with the new channel. Therefore, we first investigate the performance of legacy TCP on 5G mm-wave channel. The result shows that 5G mm-wave channel requires a fast congestion detection scheme and an aggressive recovery scheme. In this chapter, we focus on fast congestion detection scheme and present a new end-to-end TCP congestion detection scheme for high speed network: Virtual Explicit Congestion Notification (Virtual ECN), which makes the design of fast reacting congestion control to be promising.

#### 5.1 Introduction

Mm-wave channel provides tremendous amount of capacity and relatively low delay while it suffers high propagation loss and sensitivity to blockage. Simulations and measurements showed that the capacity gain is significant comparing with current cellular systems in [30, 31]. The last hop wireless channel capacity is not a bottleneck problem anymore. Meanwhile, mm-wave channels are prone to variations due to the blockage from walls, trees, or even human body [32– 34. This feature brings frequent capacity variations to the channel. Typically, the channel switches periodically between Line-of-Sight and Non-Line-of-Sight. The upper layer channel provided by mmWave communication network is not standardized yet. But generally, researchers agreed that 5G mmWave channel will provide high capacity and low latency with frequent fluctuation. For 5G mm-wave wireless communication network, the legacy TCP congestion control might not work well due to the conservative slow congestion detection and loss recovery. Our investigation on legacy TCP with mimic 5G mm-wave channel confirms this. Therefore designing a new TCP congestion control scheme without involving any intermediate network device is necessary. In this chapter, we are addressing the initial step to design such scheme: design an end-to-end fast data driven congestion detection algorithm.

In recent years, several promising TCP congestion control protocols are developed: BIC TCP [35], CUBIC TCP [36], Compound TCP [37], etc. Most of these TCP congestion control schemes rely on three duplicated ACKs or Time Out to detect the congestion and packet loss. This means TCP needs to wait for at least 3 ACKs or time out timer before entering into recovery mode or slow start mode. The slow congestion detection will deteriorate the network performance for a high

capacity, low latency and high variation mmWave channel. First, for high capacity link, during this time interval, more congestion and packet loss might occur and cause high payoff to recover from the loss. Second, for a high variation network whose link capacity is fluctuate significantly, the slow congestion detection scheme might provide out of date information of the congestion status, which makes the TCP congestion control protocol extremely conservative.

This chapter is organized as follows: Section 5.2 gives the related work on TCP congestion control and mm-wave channel. Motivations to design this scheme is demonstrated in this section. In section 5.3, we investigated the legacy TCP congestion control scheme performance on mimic 5G channel, for both NewReno and Cubic. Section 5.4 demonstrates our design of the fast end-to-end congestion detection scheme in detail including network simulation setup, data process and congestion prediction. Section 5.5 summarize the chapter and propose future work can be accomplished based on this scheme.

#### 5.2 Related Work

In this section, we present the related work on mm-wave channel modeling and data driven TCP congestion control.

#### 5.2.1 mmWave Channel

In [38] [39], research on the feasibility of using mmWave to provide wireless communication service are presented. In [30], researchers investigated the mmWave propagation loss, penetration loss, interference etc. The author provided a detailed statistical mmWave channel model based on outdoor measurement. This model shows that mmWave system can provide an order of magnitude increase in capacity. The probabilities of outage and non-outage are provided. Coverage design technology and beam-forming scheme are studied in [40] [41], which convince us that mmWave can be used for future wireless communication network design. Although mmWave channel can provide high capacity and low latency, it has a challenging issue: mmWave is sensitive to the obstructions like buildings, trees and even nearby pedestrian or vehicles. These obstructions may cause sudden, short and severe channel downgrade. How to react fast to the channel fluctuations and fully utilize the channel capacity is the main issue for TCP congestion control protocol design. This paper focus on solving this problem from end user perspective.

#### 5.2.2 Explicit Congestion Notification (ECN)

Legacy TCP congestion control protocols considered duplicate ACKs as indication of congestion. With the addition of active queue management and ECN [42] to the network infrastructure, routers are capable to detect congestion before queue overflows. An additional Congestion Experienced (CE) byte is added to the IP header of the packet to support this function. Routers running RED queue management can mark the CE code point with certain probability when the average queue length is between minimal threshold and maximal threshold. When the average queue length exceeds the maximal threshold, all upcoming packets' CE byte will be marked with probability 1. The packet with CE marked will be sent to the receiver. When the receiver received the packet, it will piggyback an ACK with CE marked to notify the sender that there is congestion in the router. No extra traffic will be generated to overload the network. The sender will reduce the congestion window to avoid queue overflows and packet loss. Using ECN to

detect congestion requires the participation of routers and waiting for receiver's feedback. To mimic the congestion detection using ECN without involving any network devices and waiting for any feedback, we developed end user congestion prediction scheme called Virtual ECN.

#### 5.2.3 Remy

Remy [43] is proposed by Keith Winstein in 2013. It designed congestioncontrol schemes based on prior knowledge of the network and the traffic model. It was the first computer generated congestion control protocol. A RemyCC tracks just three state variables of the end user:

- An exponentially-weighted moving average (EWMA) of the inter-arrival time between new ACKs received (ack ewma).
- An EWMA of the time between TCP sender timestamps reflected in those ACKs (send ewma).
- The ratio between the most recent RTT and the minimum RTT seen during the current connection (rtt\_ratio).

The algorithm does not require the support from any intermediate network devices. The end user can adjust its sending speed following the pre-generated algorithm based on the above mentioned data. This indicates these three variables together might reflect the congestion state of the network.

Remy convinced us that designing a data driven congestion detection algorithm using end user data is possible. Since ECN gives the accurate information of whether there is congestion in the network or not, we decide to use end user data to predict ECN, thereby detect the congestion. The main contribution of this

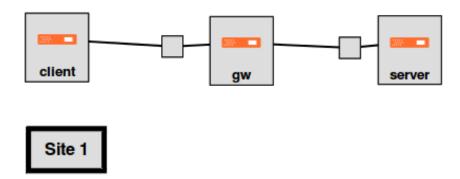


Figure 5.1: GENI Topology for Performance Evaluation

chapter is developing a data driven fast congestion detection algorithm (within one ACK inter-arrival time) using the end user data without support from receiver or router or other network devices.

## 5.3 Legacy TCP Performance on Mimic 5G Channel

Since Ethernet has similar capacity with mm-wave channel, we use Ethernet with periodic on-off behavior to mimic the mm-wave channel. We test two existing TCP congestion control protocol: NewReno and Cubic on the mimic 5G channel. In the GENI Portal, a three-node line topology with a server, a middle box and a client was set up as in Figure 5.1. Two different channel behavior are investigated: uniformly distributed on-off period and exponentially distributed on-off period. Congestion window size (CWND) and throughput are recorded to analyze the performance as in Figure 5.2, 5.3, 5.4 and 5.5. The channel capacity is set to be 1Gbps. In both cases, NewReno performance is deteriorated

significantly due to the frequent off period. Figure 5.2, 5.4 showed every time off period happened, slow start will follow. The throughput is as low as 200Mbps, which is 1/5 of the full capacity. Compare with NewReno, from Figure 5.2, 5.4 we conclude that Cubic is more aggressive than NewReno. When channel recovers from off period to on period, Cubic will increase the CWND faster to utilize the channel capacity. When channel off time is at the level of 10ms, cubic even didn't notice there is a channel lost. Instead, it behaves as congestion happened in the network and reduce the CWND. When the on time period is long enough as in the exponentially on-off period case, Cubic can still reach the upper limit of CWND and achieve full throughput as in Figure 5.3, while NewReno needs more time to recover. In the uniformly distributed on-off period case, the channel lost happened before Cubic fully recovered as in Figure 5.4. It shows that the CWND has a descending trend and the throughput decreases as time goes on. Based on the aforementioned observation, we conclude that even Cubic will not achieve high throughput if the channel switch between LOS (on) and NLOS (off) with a high frequency. Therefore, an aggressive congestion control protocol is necessary for the 5G network. In the following sections, we will focus on the initial step of design this protocol: develop a fast end-user congestion prediction scheme.

### 5.4 Congestion Detection Algorithm

In this section, the design of the fast congestion detection algorithm is illustrated in detail. The key idea is to predict the congestion in network within one inter-arrival time of ACKs from the end user data. The data which can be collected from end user includes packet sending time, ACK arriving time and the Round-Trip-Time (RTT) calculated from these two time stamps. To collect these

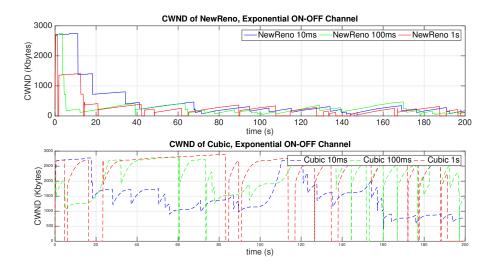


Figure 5.2: CWND Dynamics Given Exponentially On-Off Channel Behavior

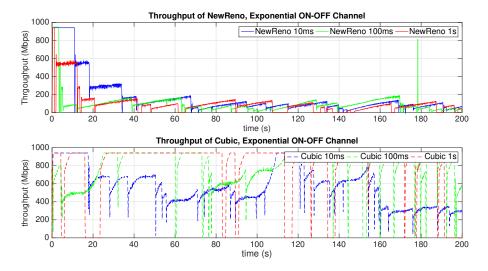


Figure 5.3: Throughput Dynamics Given Exponentially On-Off Channel Behavior

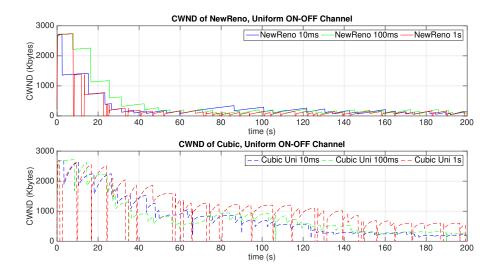


Figure 5.4: CWND Dynamics Given Uniformly On-Off Channel Behavior

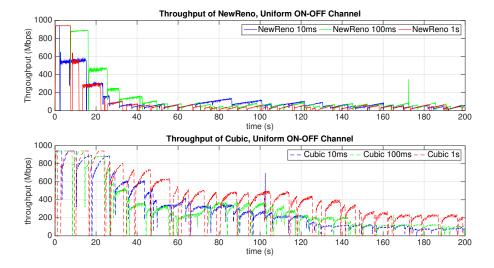


Figure 5.5: Throughput Dynamics Given Uniformly On-Off Channel Behavior

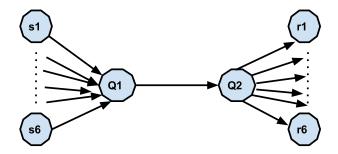


Figure 5.6: Network Topology

data for a particular network topology, we did simulations using discrete event based Network Simulator 2 (NS2).

### 5.4.1 Network Topology

A typical dumbbell model is studied here. The network topology is as in Figure 5.6. There are 6 TCP traffic senders and 6 receivers, sender i send data to receiver i through the bottleneck link  $Q1 \rightarrow Q2$ . Both Q1 and Q2 maintain a DropTail Queue. The queue limit is set to be the bandwidth-delay product to ensure the full utilization of the link capacity.

Congestion happens when the occupied queue length exceeds the threshold T on the arriving of the incoming packet. To generate traces with congestion identifiers, we mark every packet as Congestion Experienced in the queue when the queue length is greater than T. Typical NS2 TCP traces [44] are collected for future data processing as in Figure 5.7.

From the trace format we can identify the packet sending time, arriving time, packet size, unique ID, etc. Matching the packet unique ID, RTT can be calculated from packet sending time and corresponding ACK receiving time. For each unique packet, if congestion happens upon its arriving, the unique ID was recorded to be

```
event
     time
                                flags
   enqueue
            (at queue)
                                   src addr : node.port (3.0)
   dequeue
            (at
               queue)
                                   dst addr : node.port
                                                        (0.0)
d : drop
        r 1.3556 3 2 ack 40 ----- 1 3.0 0.0 15 201
          1.3556 2 0 ack 40 ----- 1
          1.3556 2 0 ack 40 ----- 1 3.0 0.0 15 201
        r 1.35576 0 2 tcp 1000 ----- 1 0.0 3.0 29 199
        + 1.35576 2 3 tcp 1000 ----- 1 0.0 3.0 29 199
        d 1.35576 2 3 tcp 1000 -----
          1.356 1 2 cbr 1000 ----- 2 1.0 3.1 157 207
          1.356 1 2 cbr 1000 ----- 2 1.0 3.1 157 207
```

Figure 5.7: NS2 TCP Trace Format

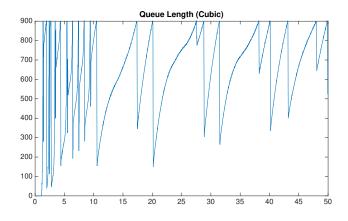


Figure 5.8: Queue Length Dynamics (Cubic)

congestion experienced.

The drop tail queue behavior is displayed as follows. Figure 5.8 shows how queue changes when traffic sources are running Cubic TCP with UDP competing traffic. In this case, when queue length is greater than 450 packets, the incoming packets will be marked as congestion experienced.

#### 5.4.2 Data Collection

Without losing generality of the analysis, we simulated amount of different traffic scenarios to collect end user data. We investigated following scenarios:

Access Link Capacity 1Gbps
BottleNeck Link Capacity 1Gbps
Access Link Delay 5ms
BottleNeck Link Delay 10ms
Queue Capacity Delay-Bandwidth Product

Table 5.1: Simulation Parameters

- Scenario 1: All traffic sources are running TCP NewReno with stationary bottleneck link capacity.
- Scenario 2: All traffic sources are running TCP Cubic with stationary bottleneck link capacity.
- Scenario 3: One half of traffic sources are running TCP NewReno while the other half are running UDP with stationary bottleneck link capacity.
- Scenario 4: One half of traffic sources are running TCP Cubic while the other half are running UDP with stationary bottleneck link capacity.
- Scenario 5: Repeat scenario 1 and 2 for a periodically On-Off bottleneck link.

The bottleneck link for those scenarios is link  $Q1 \rightarrow Q2$ . Detailed simulation parameters are showed in TABLE 5.1.

The data which is available from end user are packet sending time  $t_s$  and ACK receiving time  $t_r$ . From these two timestamps, we can calculate packet sending interval  $T_{s_i} = t_{s_i} - t_{s_{i-1}}$ , ACK inter-arrival time  $T_{r_i} = t_{r_i} - t_{r_{i-1}}$  and Round Trip Time (RTT)  $RTT_i = t_{s_i} - t_{r_i}$ . From the above three available time intervals, we develop 5 features that are used in the congestion prediction algorithm.

• Sending time interval between two consecutive packets  $T_{s_i}$ .

- Receiving time interval between two consecutive ACKs  $T_{r_i}$ .
- An exponentially-weighted moving average (EWMA) of  $T_{s_i}$  (send\_ewma).
- An EWMA of  $T_{r_i}$  (ack\_ewma).
- The ratio between the most recent RTT and the minimum RTT seen during the entire connection period (rtt ratio).

These above five features constructed the feature set to train the machine learning algorithm and predict the congestion.

### 5.4.3 Congestion Prediction

Each sample of the data collected from above five scenarios includes five features and a congestion identifier: Virtual ECN (0 stands for no congestion, 1 stands for congestion). The problem to be solved is a binary classification problem: train an algorithm to classify the sample data into two categories: congestion experienced and no congestion. First we run Logistic Regression, a popular binary classification algorithm, on the sample data. The area under ROC is 0.89 as showed in Figure. 5.9. The performance of Logistic Regression is good (0.80-0.90). The decision boundary is  $-2.31936102*f_1 - 33.36046689*f_2 - 12.65365902*f_3 - 15.29961927*f_4 + 2.0344486*f_5 - 2.69202498 = 0$ , where  $f_1, f_2, f_3, f_4, f_5$  are the five corresponding features.

Next we applied Decision Tree algorithm and regulated the maximum depth of the tree to be 5 and the minimum samples in each leaf node to be 10000 to avoid overfitting. Figure. 5.10a gives the ROC curve of Decision Tree Classifier. The area under ROC curve is 0.98. This indicates excellent (0.90 - 1) prediction result. The feature importance are given as [0.011703, 0.00085, 0.000000, 0.03985,

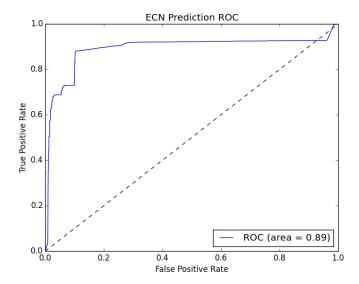
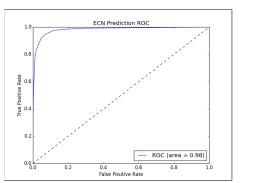
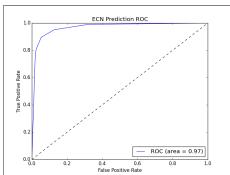


Figure 5.9: ROC curve of Logistic Regression Classifier

0.94760] for  $[T_{s_i}, T_{r_i}, \text{ send\_ewma, receive\_ewma, rtt\_ratio}]$ , from which we can conclude that rtt\\_ratio is the most important feature to predict congestion.





(a) ROC curve of Decision Tree Classifier (max\_depth = 5, min\_samples\_leaf = fier (max\_depth = 3, min\_samples\_leaf = 10000)

Further we changed the maximum depth to 3 and minimum samples of each leaf node to 100000, the ROC is displayed in Figure. 5.10b. The feature importance becomes [0, 0, 0, 0, 1]. This indicates the decision tree is doing the binary classification merely based on rtt\_ratio. All other features are not contributed to the binary classification process. The decision tree is showed in Figure. 5.11. In

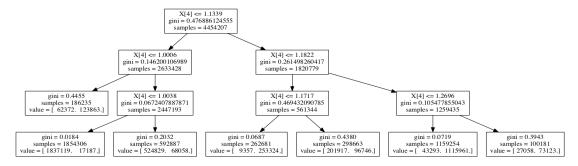
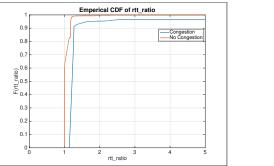
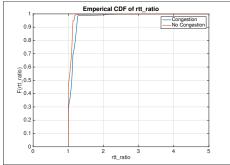


Figure 5.11: Decision Tree (max depth = 3, min samples leaf = 100000)

Figure. 5.11, X[4] is rtt\_ratio, the first layer is classified by this feature. The cumulative density function (CDF) of rtt\_ratio is given in Figure. 5.12a. The blue line is the CDF curve of rtt\_ratio when congestion experienced while the red line is when congestion not experienced. Take 1.2 as an example, the probability of rtt\_ratio to be less than 1.13 is 82% when there is no congestion. However, that probability is approximately 0% when congestion experienced. This is consistent with the result of feature importance generated from Decision Tree algorithm.





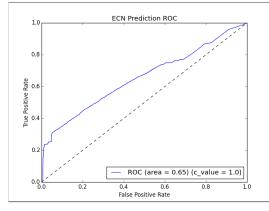
(a) CDF of rtt\_ratio with Same Propaga- (b) CDF of rtt\_ratio with Different Proption Delay

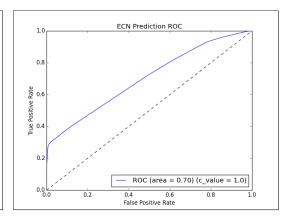
The above results are generated from a network with fixed propagation delay. To study how this prediction algorithm works when network condition changes, we investigated Scenario 1 and 2 with variations of propagation delay. We simulated networks with access delay and queue capacity as in TABLE 5.2. The Logistic Regression algorithm generated the ROC curve as in Figure. 5.13a. The area under

Table 5.2: Simulation Parameters

Access Link Delay	5ms, 10ms, 20ms
BottleNeck Link Delay	10 ms, 20 ms, 40 ms
Queue Capacity	Delay-Bandwidth Product

ROC curve is 0.654497, which indicates poor performance (0.60-0.70). The decision boundary is  $-0.46605323*f_1-7.33485574*f_2-0.34620622*f_3-1.41154115*$  $f_4 + 5.20171832 * f_5 - 5.53557771 = 0$ . The coefficient of each feature follows the same pattern as before. Decision Tree classifier is then applied to the collected dataset. The ROC curve is as in Figure. 5.13b. The area under ROC curve is 0.701188, which is on the boundary of poor performance. The feature importance is [0.000955787581, 0.000389816495, 0.00489484823, 0.0636899225, 0.930069625]. This is consistent with the previous result that rtt ratio is the most important feature. Those two figures indicates that when network condition changes, the predictability of congestion from the aforementioned five features decreases. Figure. 5.12b shows the CDF of rtt ratio with different link propagation delay. The figure indicates near 30% overlap of the CDF curve of Congestion Experience packet and No Congestion packet. This again verifies the prediction results.





(a) ROC curve of Logistic Regression Clas- (b) ROC curve of Decision Tree Classifier sifier with Different Propagation Delay

with Different Propagation Delay

### 5.5 Chapter Summary

In this chapter, we proposed a data driven machine learning congestion detection algorithm. Datasets are collected using NS2 for a dumbbell model with five different traffic scenarios. Five features are formatted from end user data. When the network condition is not changing, which means the propagation delay of each link is stable, our algorithm can detect congestion with high precision from the five features. In contrast, if the network condition changes, the algorithm fails to work. In both cases, rtt\_ratio is the most important feature to predict congestion. Other four features are less useful when doing the binary classification. The area under ROC curve is consistent with the CDF of rtt\_ratio. For stable network, a fast reacting congestion control algorithm can be designed based on our congestion detection algorithm for 5G mmWave communication network.

Chapter 6

Conclusion

## Appendices

## Appendix A

### A.1 Title of Appendix A

# Appendix B

B.1 Title of Appendix B

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