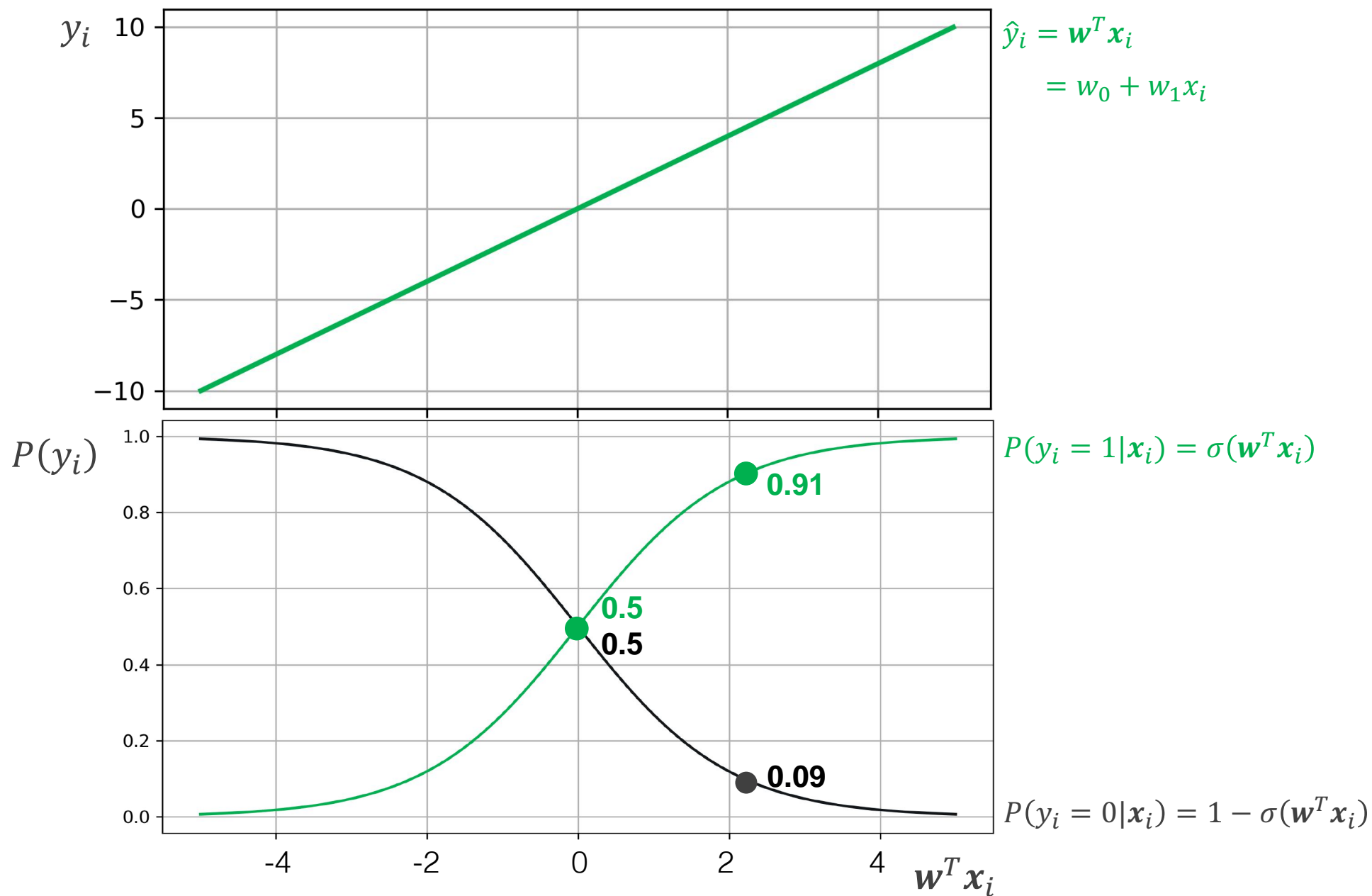


Evaluating Performance I

Linear Regression

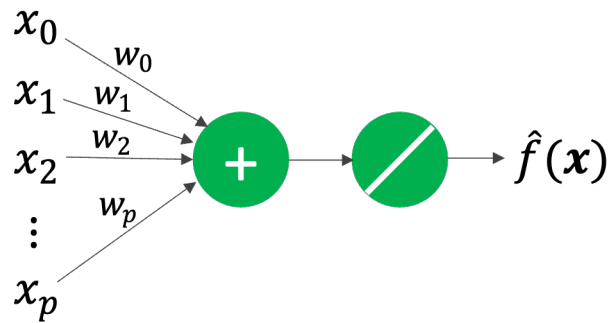
Logistic Regression



Linear Regression

Model

$$\hat{f}(\mathbf{x}) = \sum_{i=0}^p w_i x_i$$



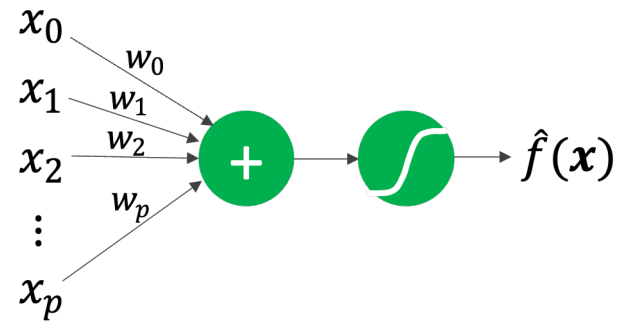
Resulting
output $\hat{f}(\mathbf{x})$

Estimate of the
target variable

Range of $\hat{f}(\mathbf{x})$ $-\infty < \hat{f}(\mathbf{x}) < \infty$

Logistic Regression

$$\hat{f}(\mathbf{x}) = \sigma \left(\sum_{i=0}^p w_i x_i \right)$$

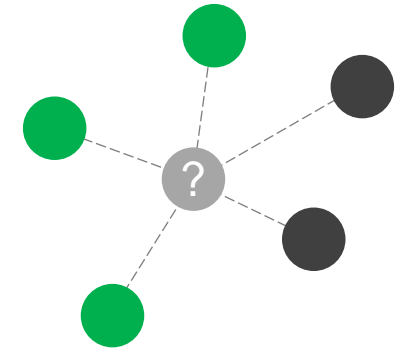


Probability of the
target being Class 1

$$0 < \hat{f}(\mathbf{x}) < 1$$

KNN Classification

$$\frac{\#\bullet}{k} \rightarrow \hat{f}(\mathbf{x})$$



Fraction of Class 1
neighbors

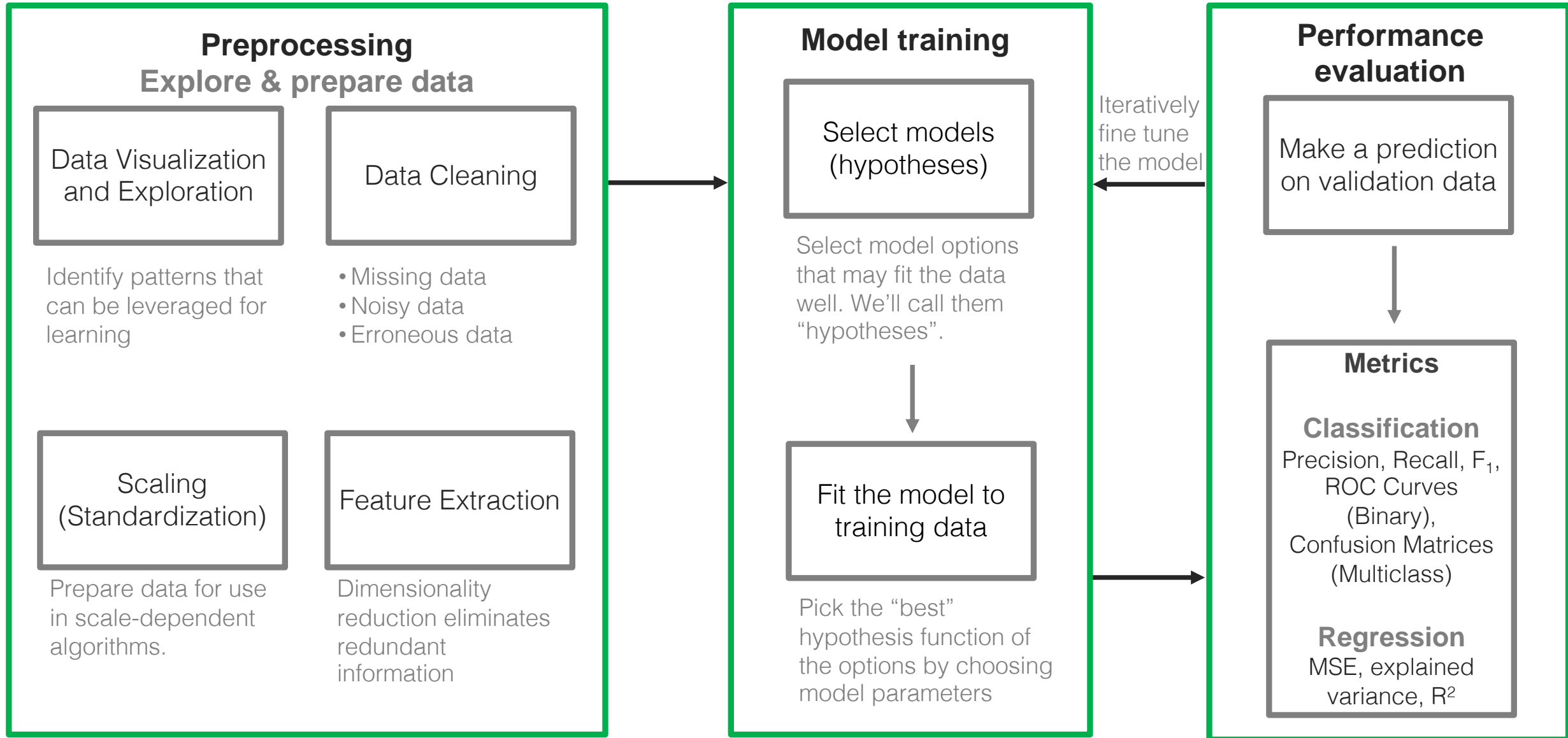
$$\hat{f}(\mathbf{x}) \in \left[0, \frac{1}{k}, \frac{2}{k}, \dots, \frac{k-1}{k}, 1\right]$$

Note these are **NOT** binary predictions!

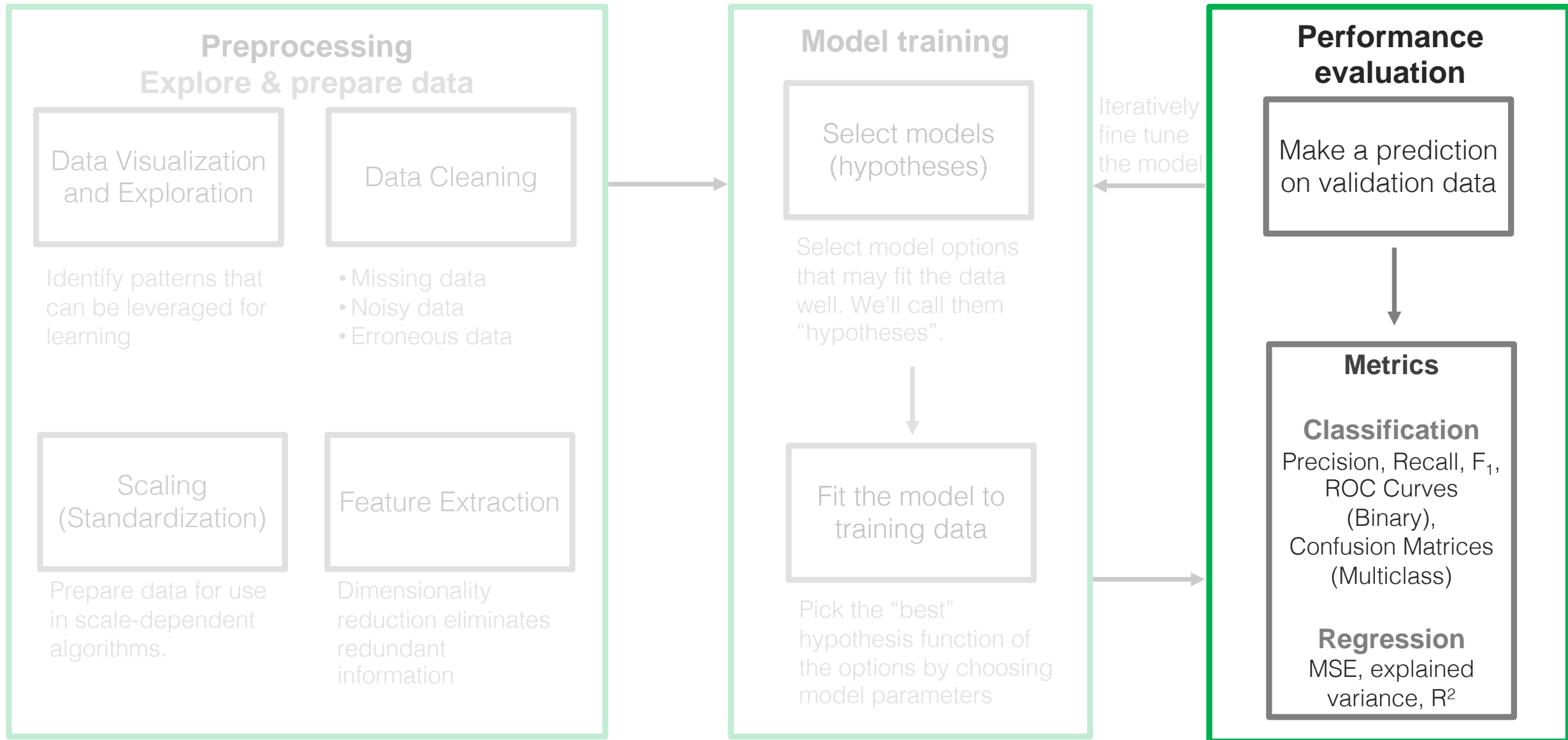
To create binary predictions, we need to
threshold these values (apply a decision rule)

These are confidence scores (which we may
interpret as class probabilities)

Supervised learning in practice



Supervised learning in practice



Performance evaluation overview

Metrics

(regression/classification metrics, ROC curves)

Quantify model performance

Today

Data resampling techniques

(Train/validation/test splits and cross validation)

Fairly evaluate generalization performance

Next Class

Modeling Considerations

Accuracy

Computational Efficiency

Interpretability

Accuracy

Supervised Learning Performance Evaluation

Regression

Classification

Binary

Multiclass

Receiver Operating
Characteristic (ROC)
curves

Confusion matrices

Common Metrics

- Mean squared error (MSE)
- Mean absolute error (MAE)
- R^2 , coefficient of determination

- Classification accuracy
- True positive rate
- False positive rate
- Precision
- F_1 Score
- Area under the ROC curve (AUC)

- Classification accuracy
- Micro-averaged F_1 Score
- Macro-averaged F_1 Score

Regression: Mean Squared Error

The mean squared error (MSE)

$$\text{MSE} = \frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2$$

Absolute measure of performance

One of the most widely used loss / cost functions
(**when in doubt - use this!**)

Regression: Mean **Absolute** Error

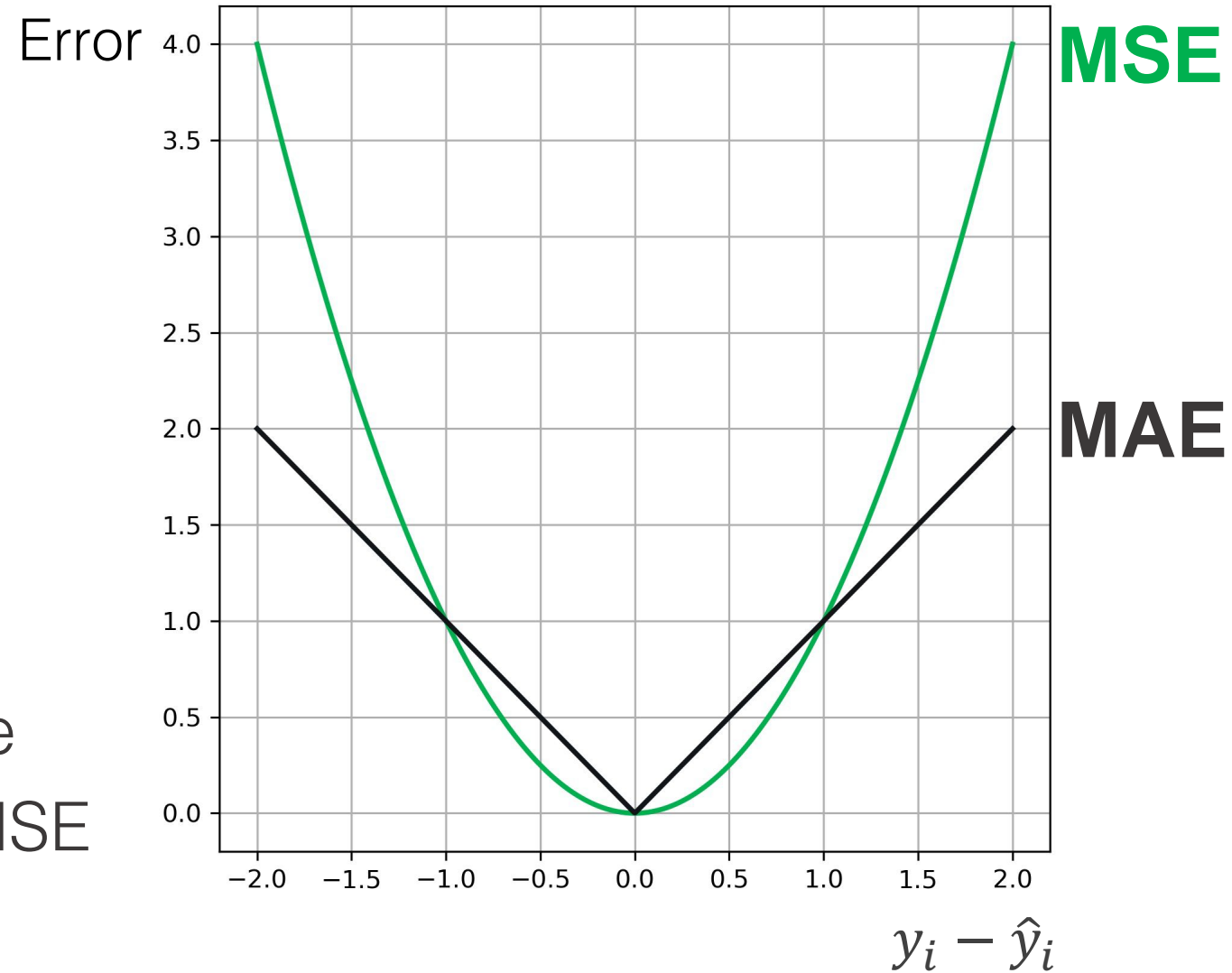
The mean absolute error (MAE)

$$\text{MAE} = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i|$$

Absolute measure of performance

Penalizes large errors less than MSE

(can be more robust to outliers)



Regression: R^2 Coefficient of determination

Proportion of the response variable variation explained by the model

Residual sum of squares
(variation in the residuals)

$$SS_{res} = \sum_{i=1}^N (y_i - \hat{y}_i)^2$$

Total sum of squares
(variation in the data)

$$SS_{tot} = \sum_{i=1}^N (y_i - \bar{y})^2$$

$$\bar{y} = \frac{1}{N} \sum_{i=1}^N y_i$$

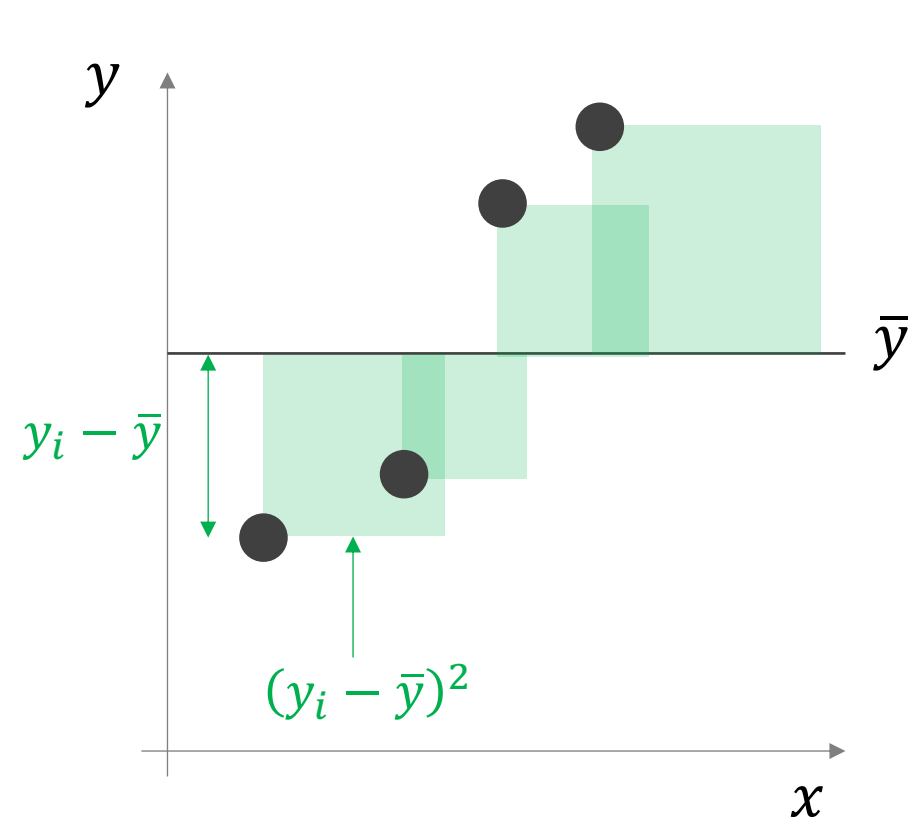
R-squared

$$R^2 = 1 - \frac{SS_{res}}{SS_{tot}}$$

Relative measure of performance

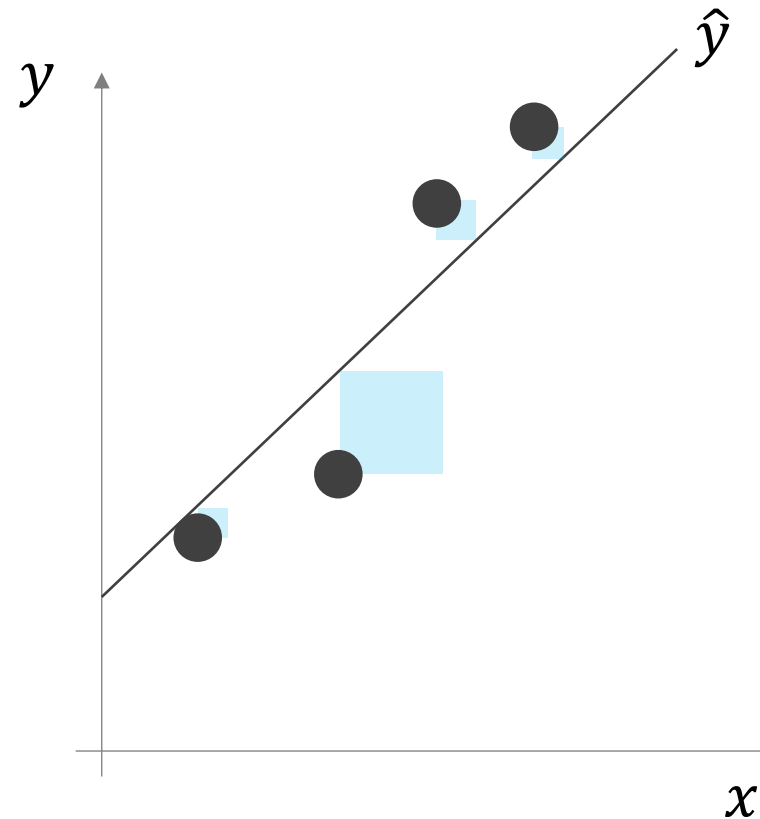
Regression: R^2 Coefficient of determination

Essentially compares performance to a model that predicts the mean of the target variable



Total sum of squares
(variation in the data)

$$SS_{tot} = \sum_{i=1}^N (y_i - \bar{y})^2 \quad \bar{y} = \frac{1}{N} \sum_{i=1}^N y_i$$



Residual sum of squares
(variation in the residuals)

$$SS_{res} = \sum_{i=1}^N (y_i - \hat{y}_i)^2$$

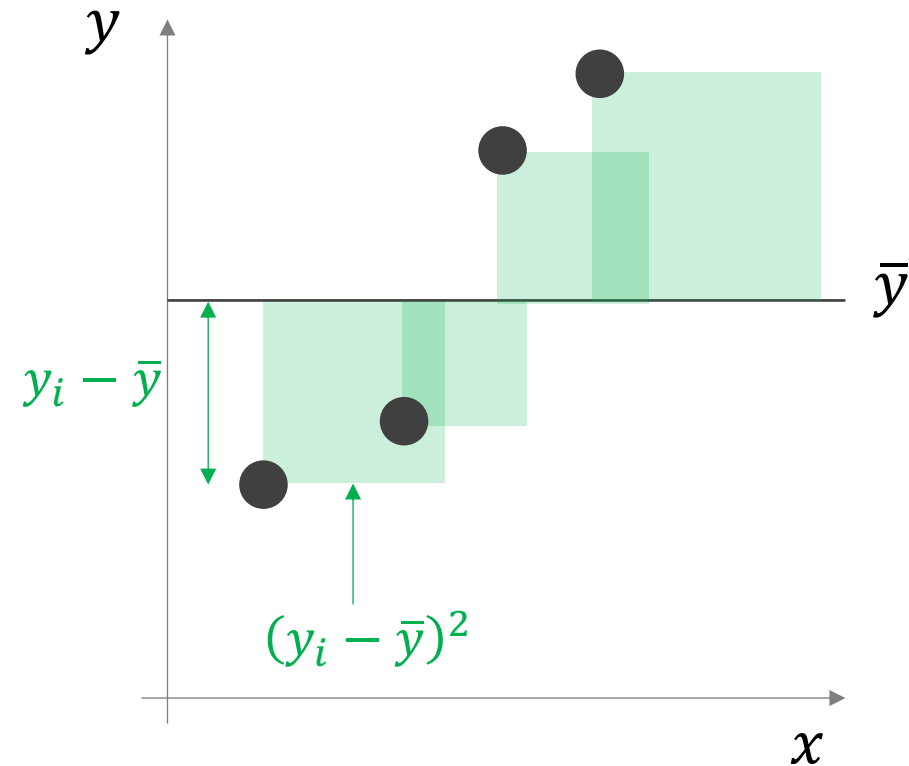
Relative measure
of performance
(relative to the
mean)

R-squared

$$R^2 = 1 - \frac{SS_{res}}{SS_{tot}}$$

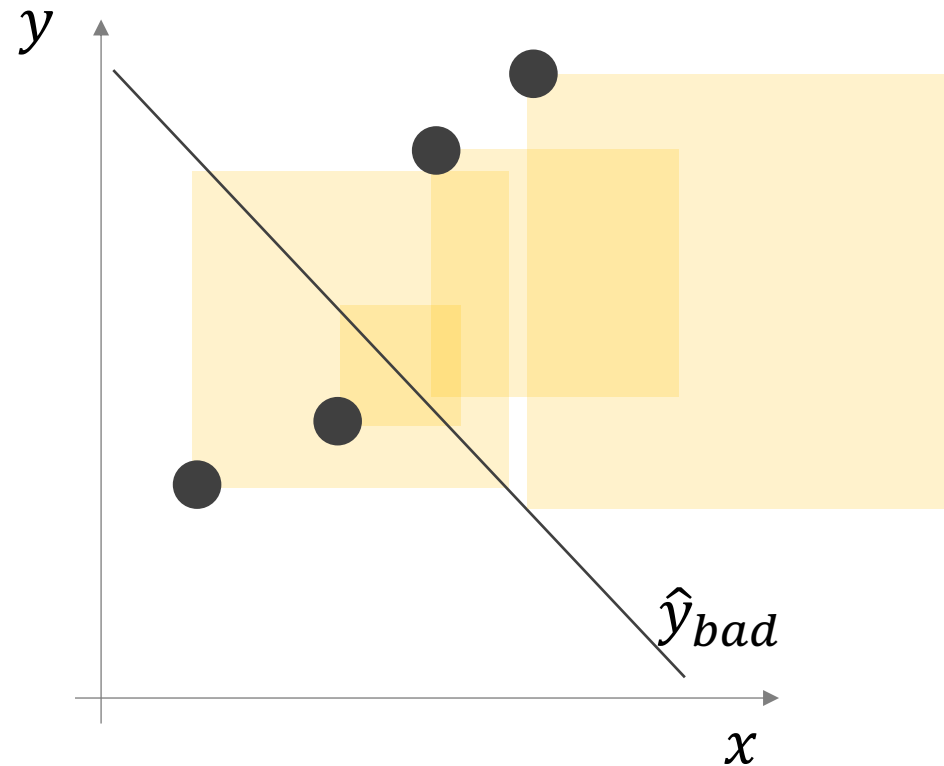
Regression: R^2 can be negative

Essentially compares performance to a model that predicts the mean of the target variable



Total sum of squares
(variation in the data)

$$SS_{tot} = \sum_{i=1}^N (y_i - \bar{y})^2 \quad \bar{y} = \frac{1}{N} \sum_{i=1}^N y_i$$



Residual sum of squares
(variation in the residuals)

$$SS_{res} = \sum_{i=1}^N (y_i - \hat{y}_i)^2$$

R-squared **can** be negative if the model is worse than just guessing the mean

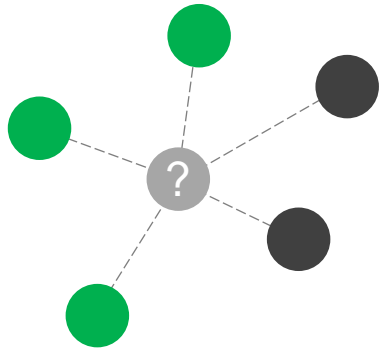
R-squared

$$R^2 = 1 - \frac{SS_{res}}{SS_{tot}}$$

Binary Classification

KNN Classification

$$\frac{\# \bullet}{k} \rightarrow \hat{f}(x)$$



Fraction of Class 1
neighbors

You input your training data into your KNN model

2 of the 3 nearest neighbors are Class 1, so we predict the class to be Class 1

What do we do if our training labels match that class? What if they don't?

Types of classification error

False Positive
(Type I error)



False Negative
(Type II error)

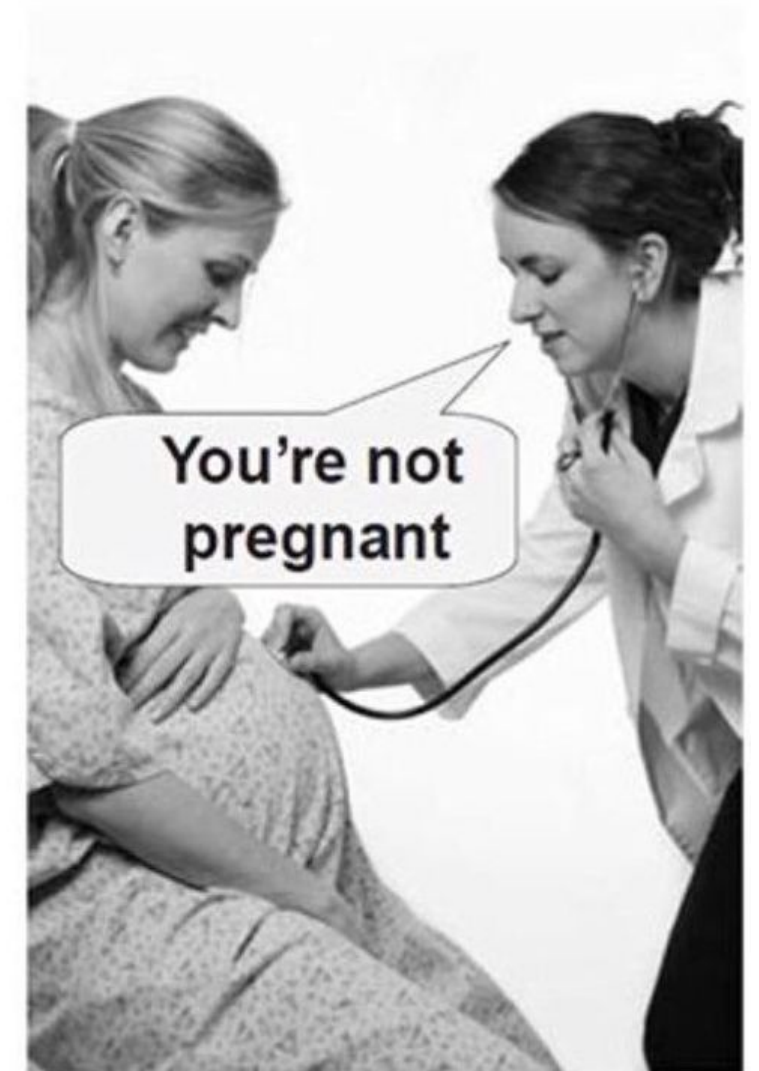
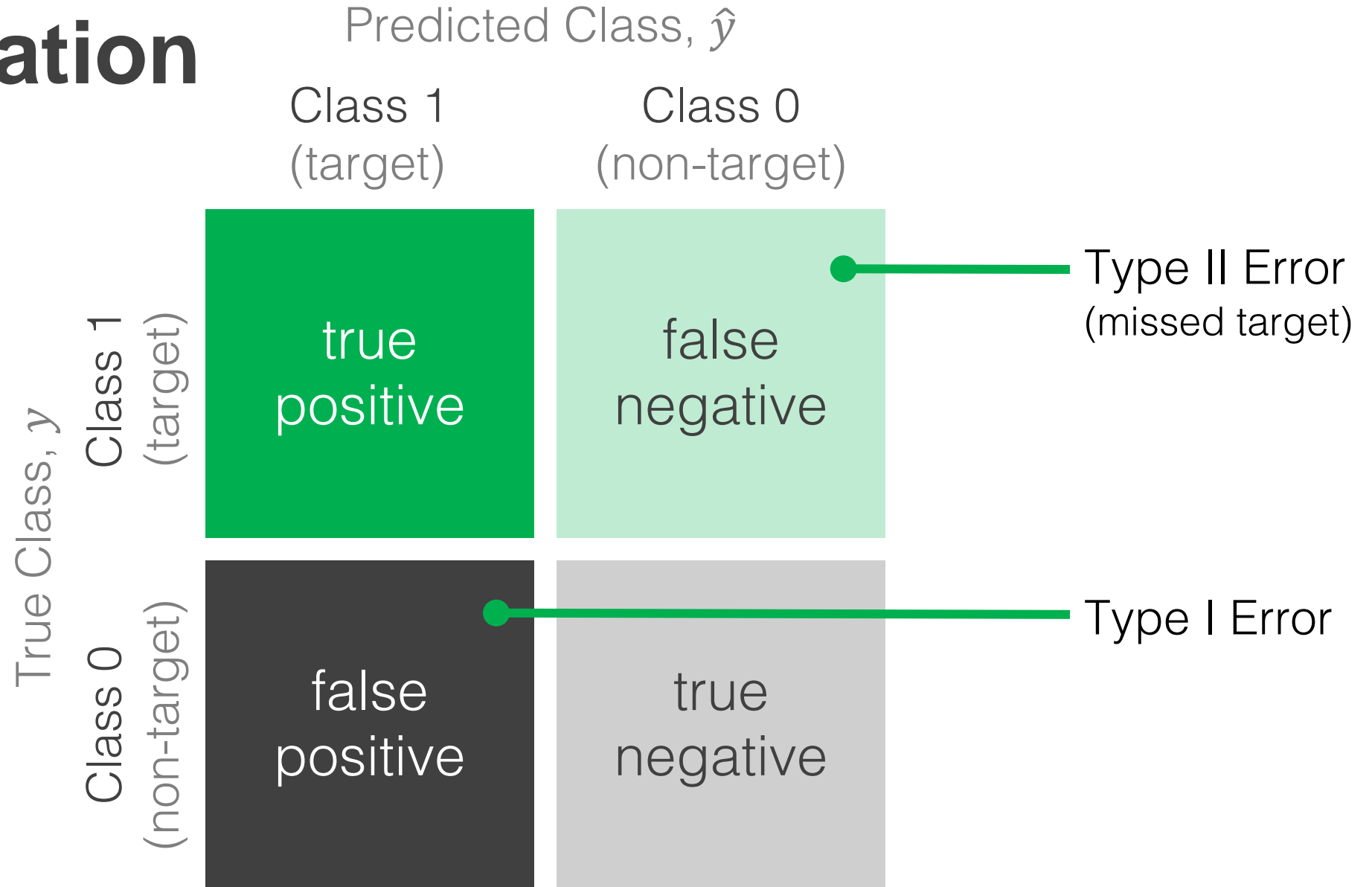


Image from: Ellis. *The Essential Guide to Effect Sizes*

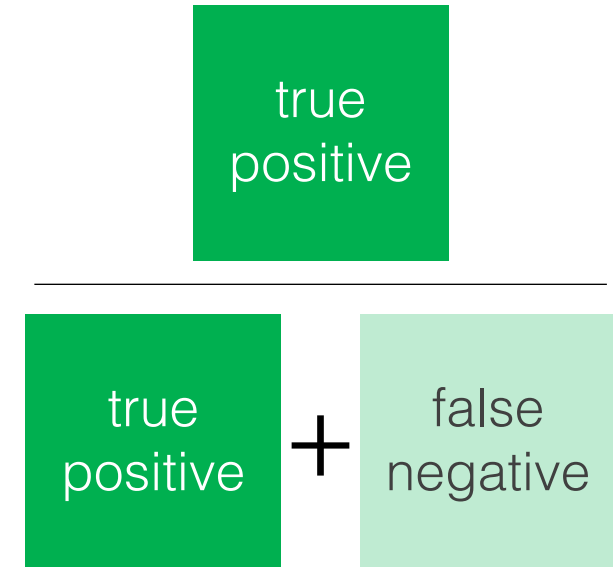
Binary Classification



Binary Classification

		Predicted Class, \hat{y}	
		Class 1 (target)	Class 0 (non-target)
True Class, y	Class 1 (target)	true positive	false negative
	Class 0 (non-target)	false positive	true negative

True positive rate
Probability of detection, p_D
Sensitivity
Recall

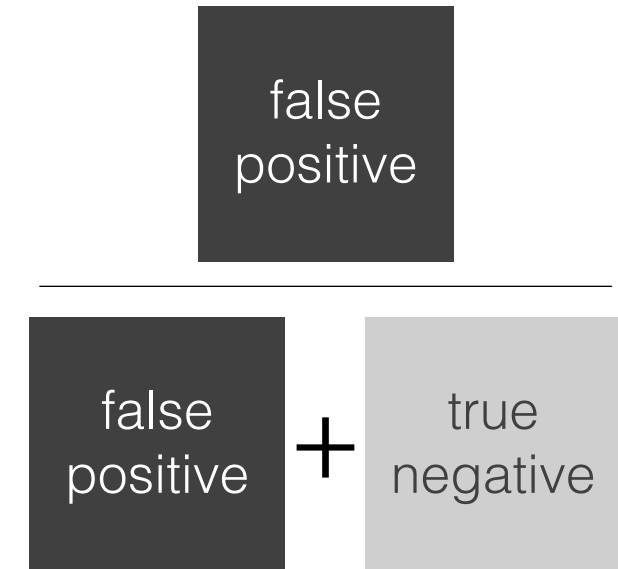


How many targets (Class 1) were correctly classified as targets?

Binary Classification

		Predicted Class, \hat{y}	
		Class 1 (target)	Class 0 (non-target)
True Class, y	Class 1 (target)	true positive	false negative
	Class 0 (non-target)	false positive	true negative

False positive rate
Probability of false alarm, p_{FA}



How many non-targets (Class 0) were incorrectly classified as targets?

Binary Classification

Predicted Class, \hat{y}

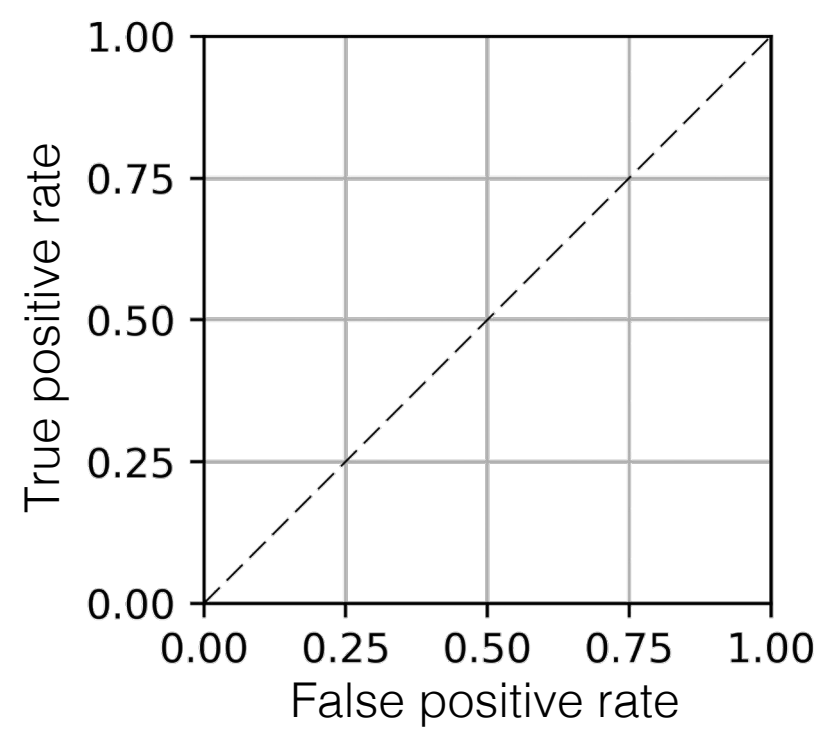
		Predicted Class, \hat{y}	
		Class 1 (target)	Class 0 (non-target)
True Class, y	Class 1 (target)	true positive	false negative
	Class 0 (non-target)	false positive	true negative

Precision

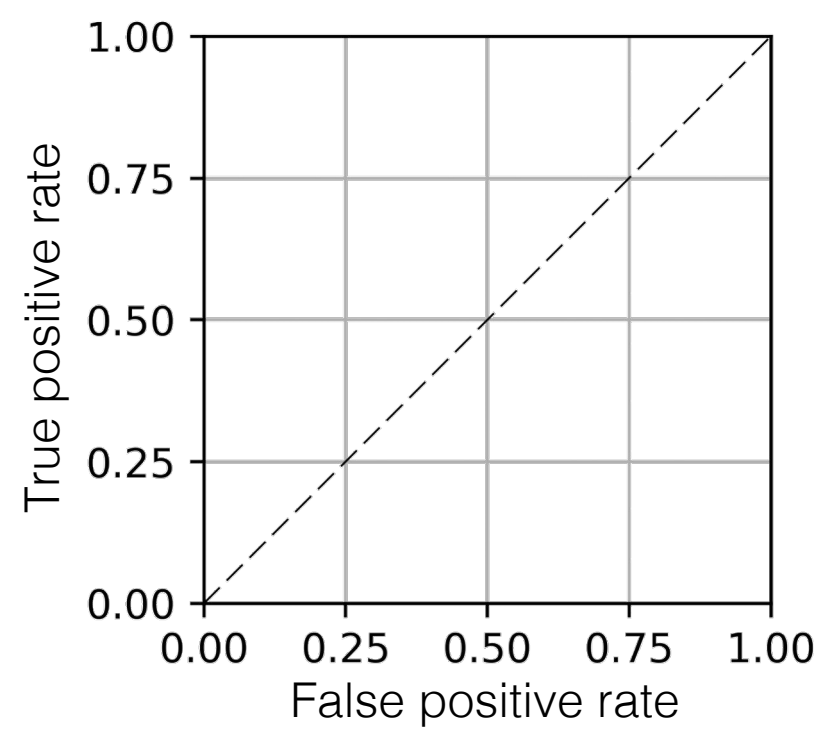
$$\frac{\text{true positive}}{\text{true positive} + \text{false positive}}$$

How many of the predicted targets are targets?

ROC Curves

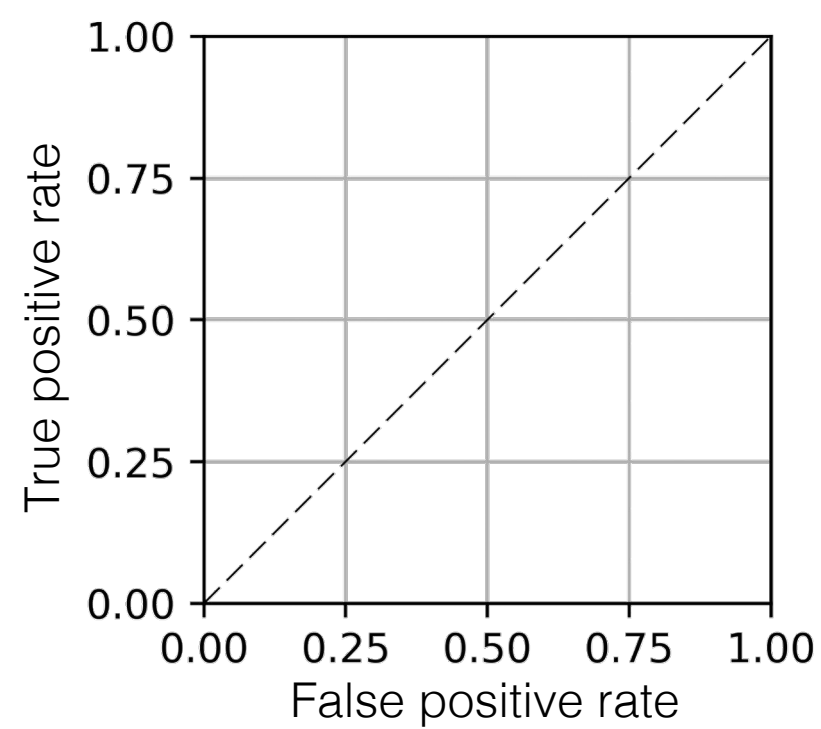


ROC Curves



True Class Label (y)	Classifier Confidence
1	1.40
1	0.95
0	0.80
1	0.60
0	-0.10

ROC Curves

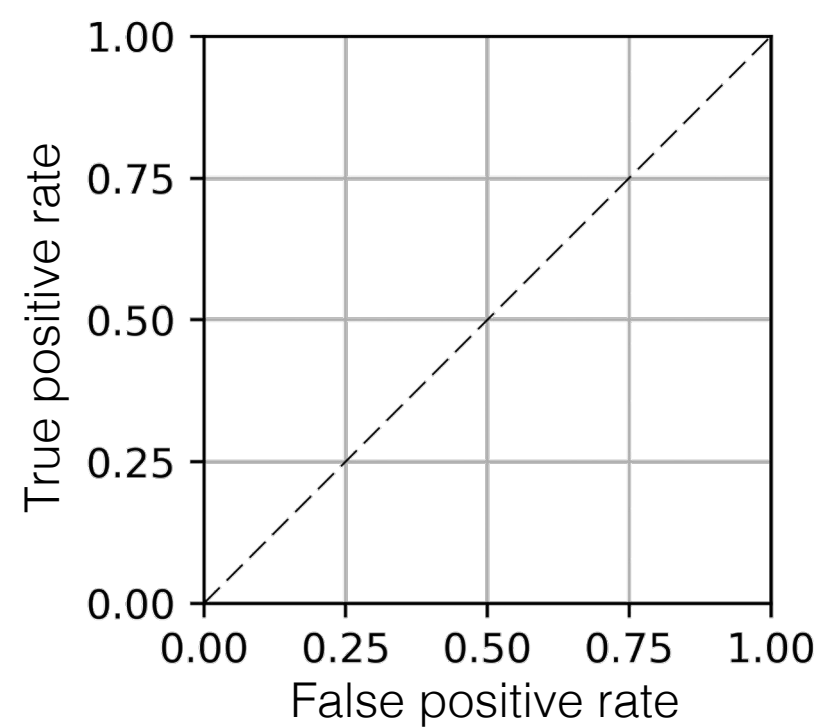


Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
?	1	1.40
?	1	0.95
?	0	0.80
?	1	0.60
?	0	-0.10

ROC Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$

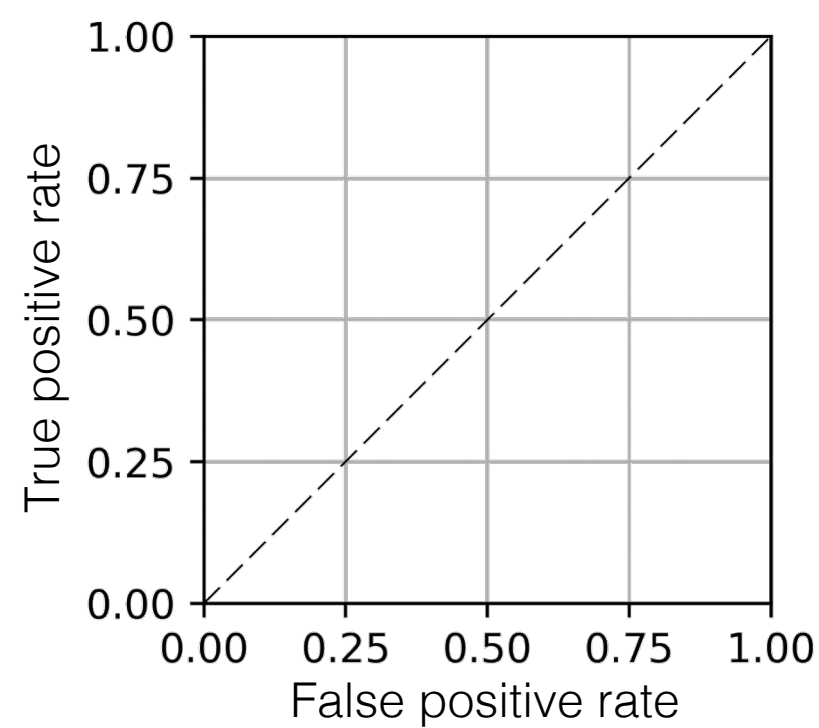


Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
?	1	1.40
?	1	0.95
?	0	0.80
?	1	0.60
?	0	-0.10

ROC Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



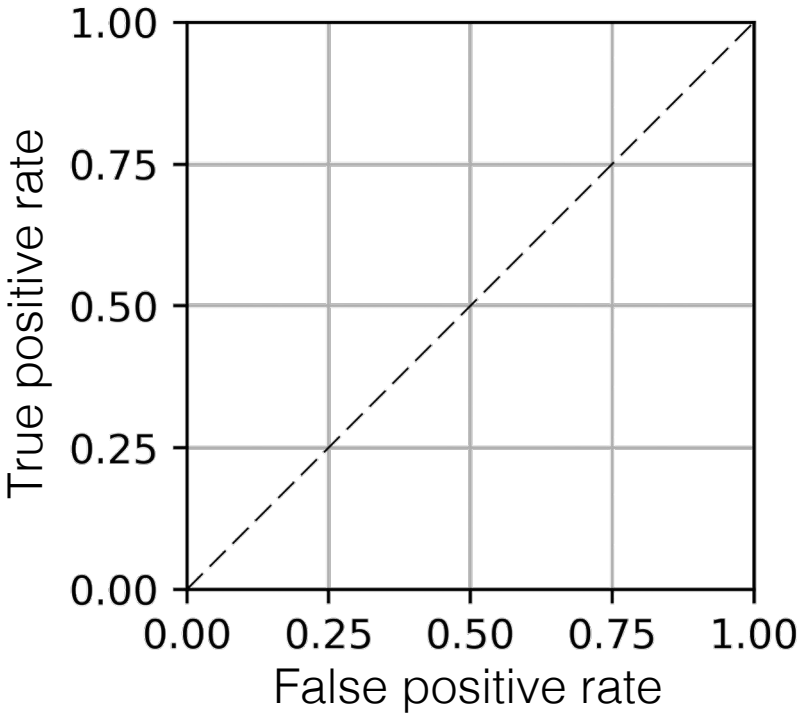
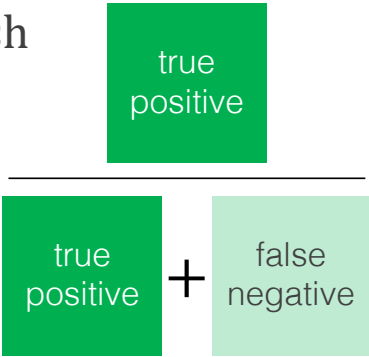
Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
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Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
?	1	1.40
?	1	0.95
?	0	0.80
?	1	0.60
?	0	-0.10

ROC Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
?	1	1.40
?	1	0.95
?	0	0.80
?	1	0.60
?	0	-0.10

Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
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ROC Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$

true
positive

false
positive

true
positive

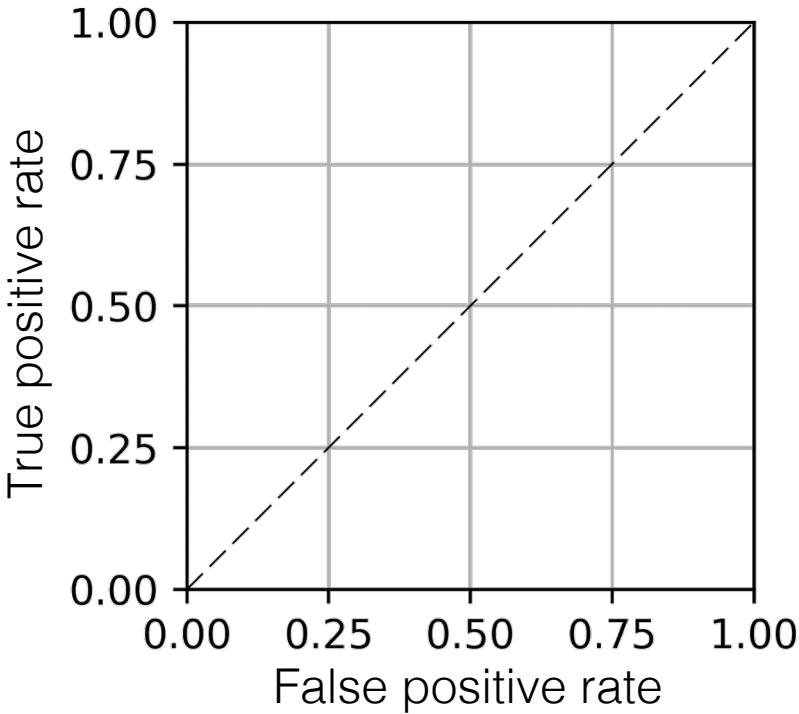
+

false
negative

false
positive

+

true
negative



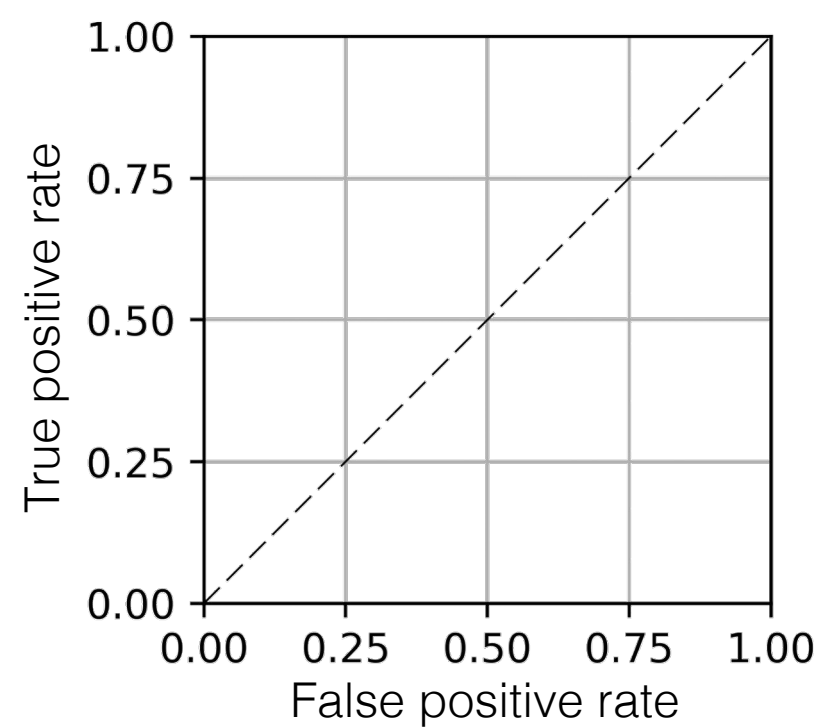
Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
?	1	1.40
?	1	0.95
?	0	0.80
?	1	0.60
?	0	-0.10

Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
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ROC Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



True Class Label (y)	Classifier Confidence
1	1.40
1	0.95
0	0.80
1	0.60
0	-0.10

true positive

false positive

true positive

false negative

false positive

true negative

Total Positives = 3

Total Negatives = 2

Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
-----------	------------------	--------------------	-------------------	---------------------

ROC Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$

true positive

false positive

true positive

+ false negative

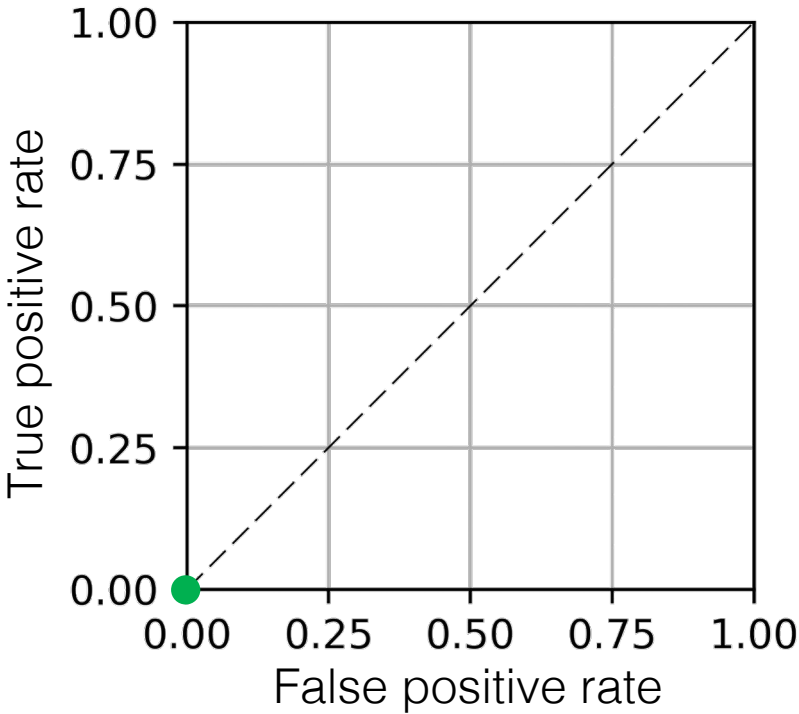
false positive

+ true negative

Total Positives = 3

Total Negatives = 2

Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
∞	0	0	0	0



Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
0	1	1.40
0	1	0.95
0	0	0.80
0	1	0.60
0	0	-0.10

ROC Curves

Classifier decision rule:
$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$

true positive

false positive

true positive

+

false negative

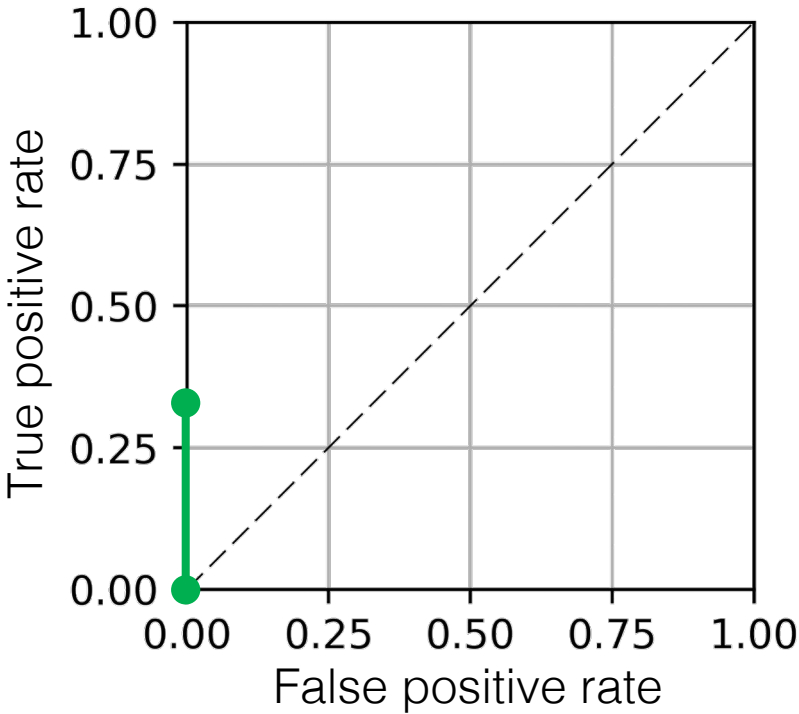
false positive

+

true negative

Total Positives = 3

Total Negatives = 2



Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
0	1	0.95
0	0	0.80
0	1	0.60
0	0	-0.10

Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
∞	0	0	0	0
1.0	1	0.333	0	0

ROC Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$

true positive

false positive

true positive

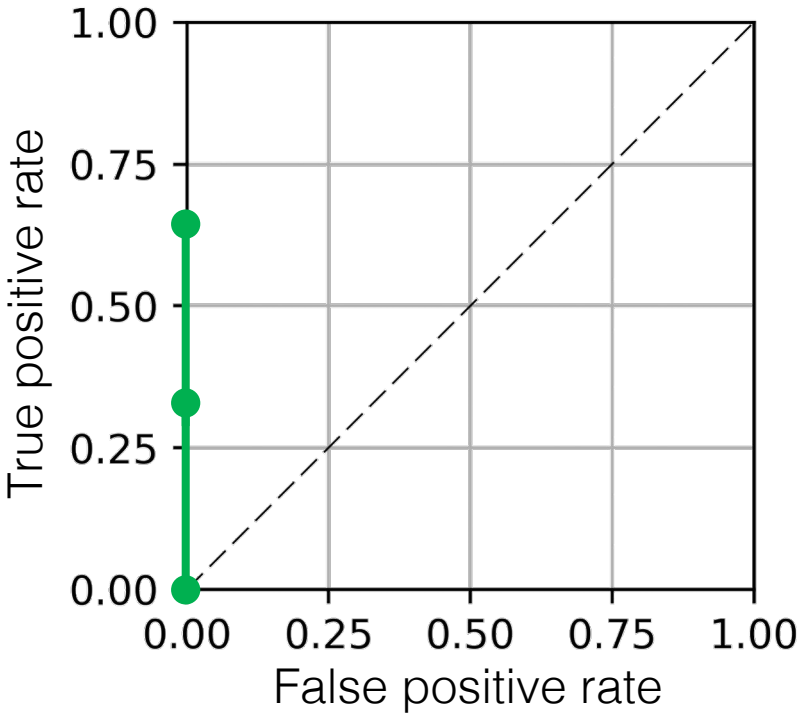
false negative

false positive

true negative

Total Positives = 3

Total Negatives = 2



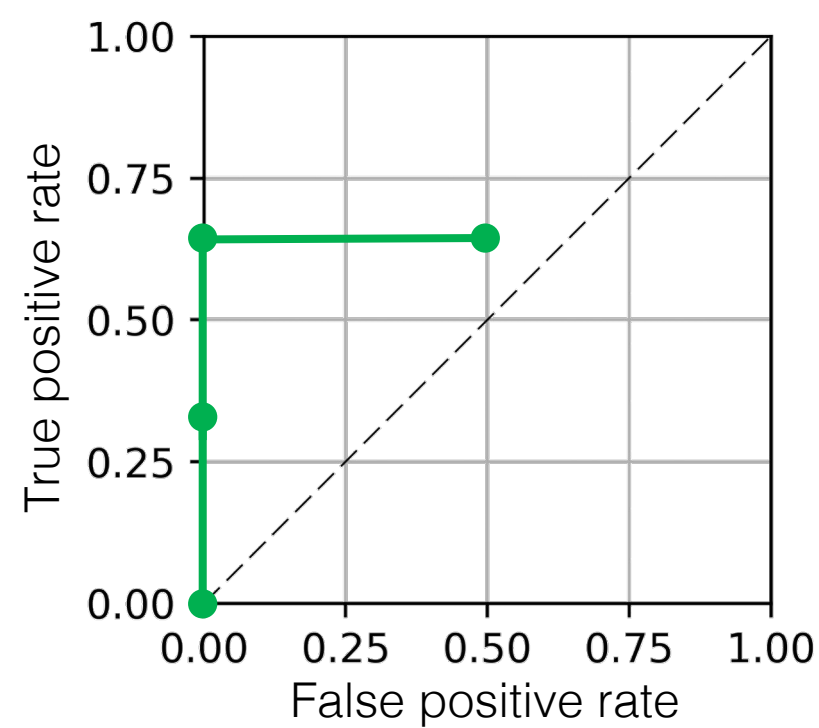
Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
1	1	0.95
0	0	0.80
0	1	0.60
0	0	-0.10

Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
∞	0	0	0	0
1.0	1	0.333	0	0
0.9	2	0.667	0	0

ROC Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



true
positive

false
positive

true
positive

+

false
negative

false
positive

+

true
negative

Total Positives = 3

Total Negatives = 2

Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
∞	0	0	0	0
1.0	1	0.333	0	0
0.9	2	0.667	0	0
0.7	2	0.667	1	0.5

Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
1	1	0.95
1	0	0.80
0	1	0.60
0	0	-0.10



ROC Curves

Classifier decision rule:

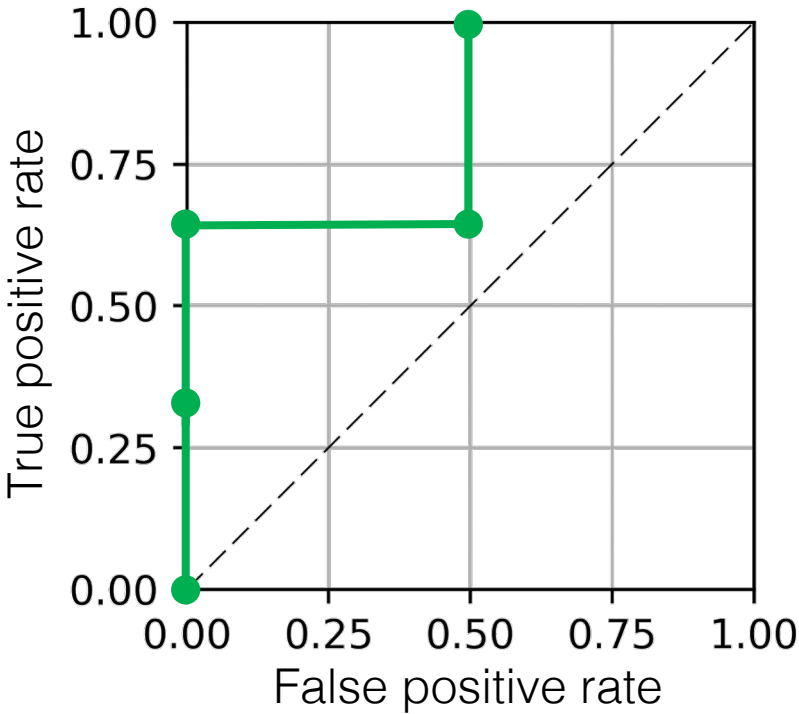
$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Total Positives = 3

Total Negatives = 2

Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
∞	0	0	0	0
1.0	1	0.333	0	0
0.9	2	0.667	0	0
0.7	2	0.667	1	0.5
0.0	3	1	1	0.5

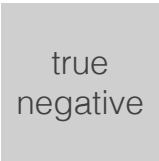
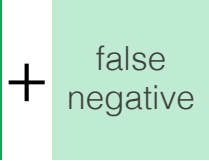


Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
1	1	0.95
1	0	0.80
1	1	0.60
0	0	-0.10

ROC Curves

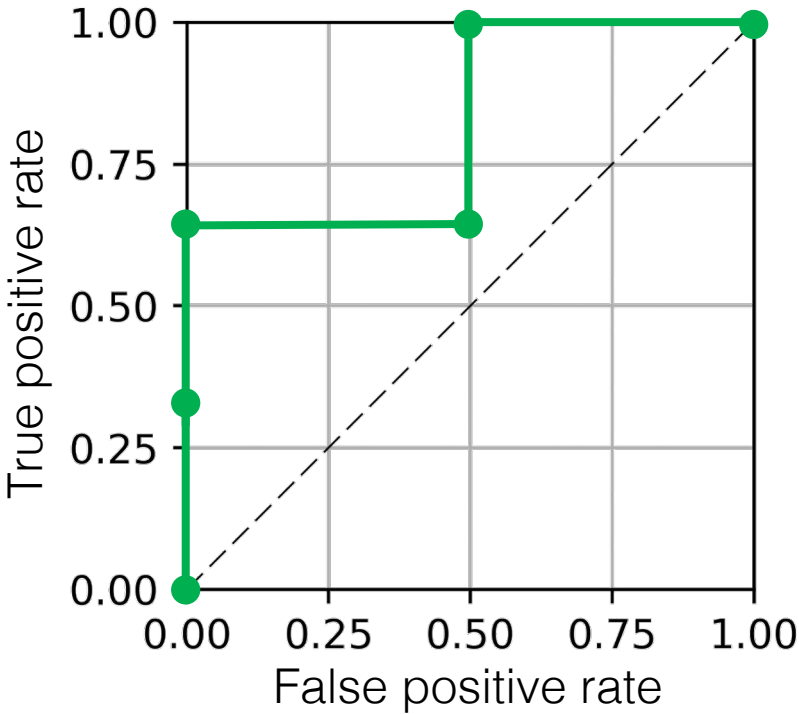
Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Total Positives = 3

Total Negatives = 2



Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
1	1	0.95
1	0	0.80
1	1	0.60
1	0	-0.10



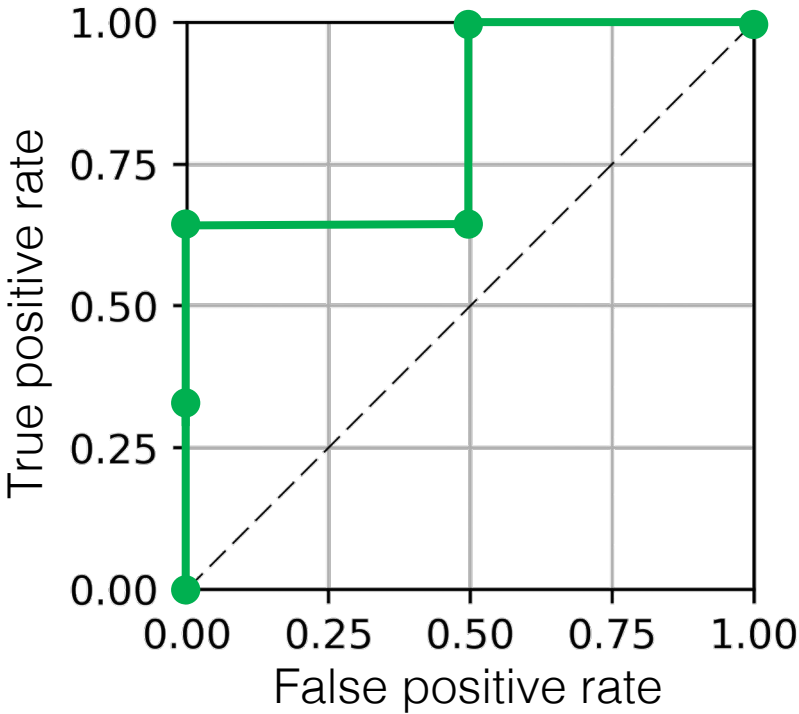
Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
∞	0	0	0	0
1.0	1	0.333	0	0
0.9	2	0.667	0	0
0.7	2	0.667	1	0.5
0.0	3	1	1	0.5
$-\infty$	3	1	2	1

ROC Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$

$$AUC = \left(\frac{2}{3}\right) \left(\frac{1}{2}\right) + (1) \left(\frac{1}{2}\right) = \frac{5}{6} \cong 0.833$$



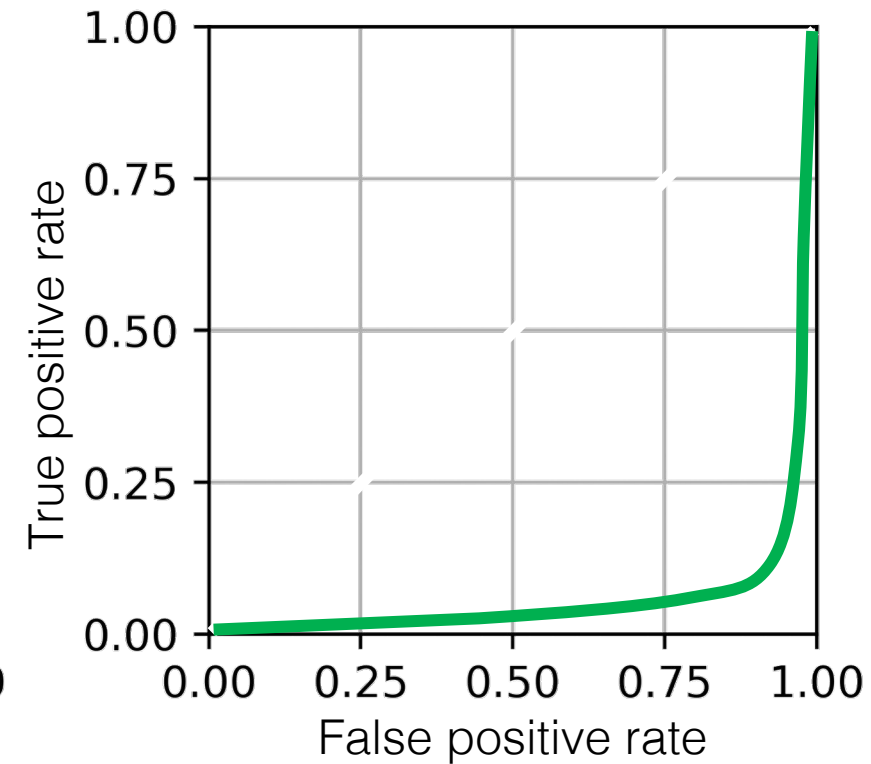
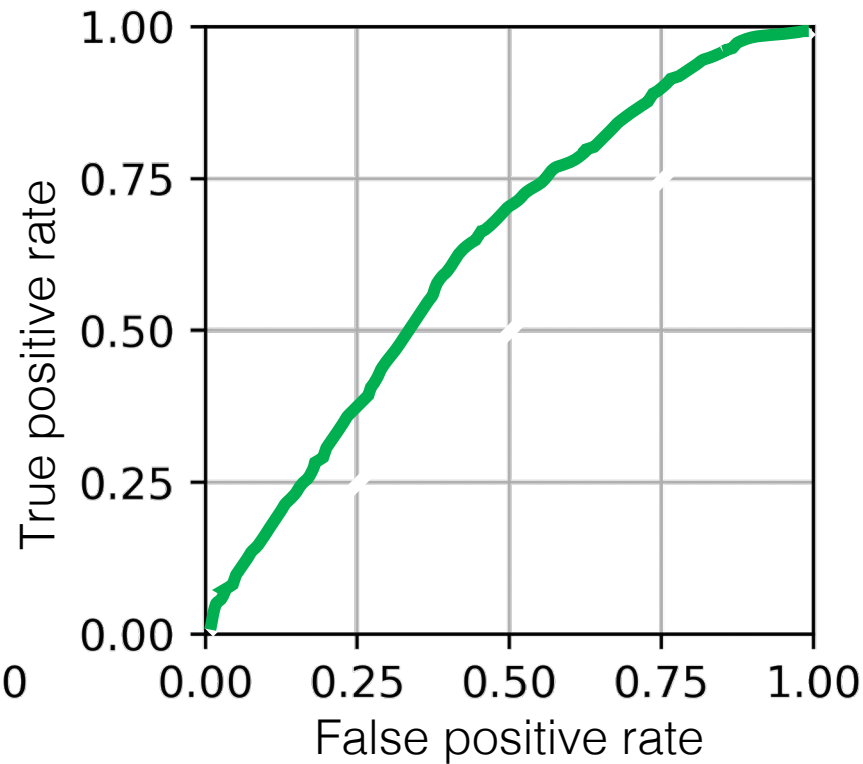
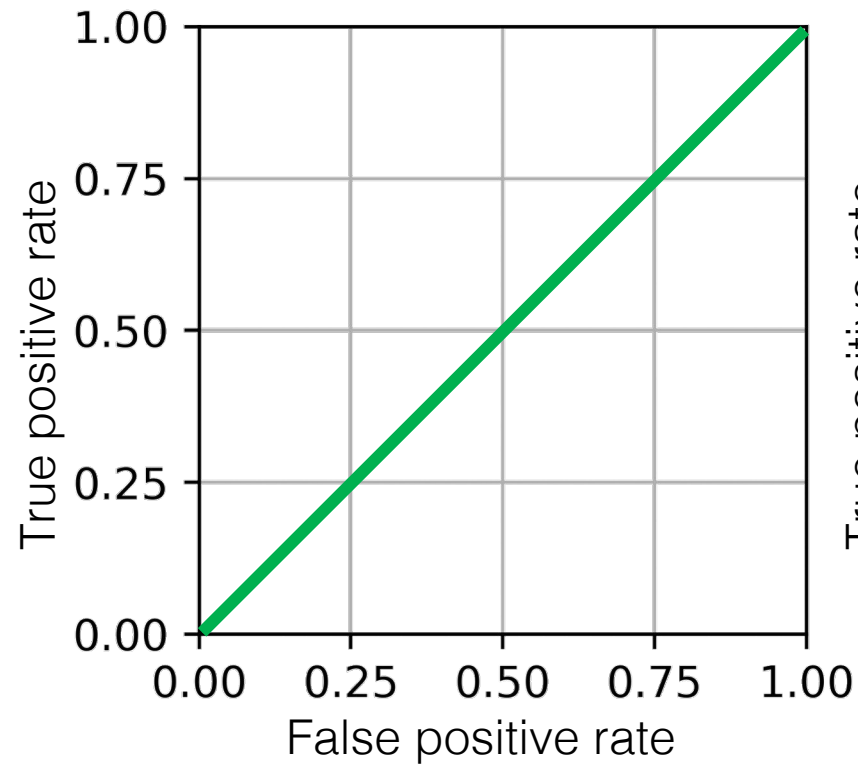
Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
1	1	0.95
1	0	0.80
1	1	0.60
1	0	-0.10

Total Positives = 3

Total Negatives = 2

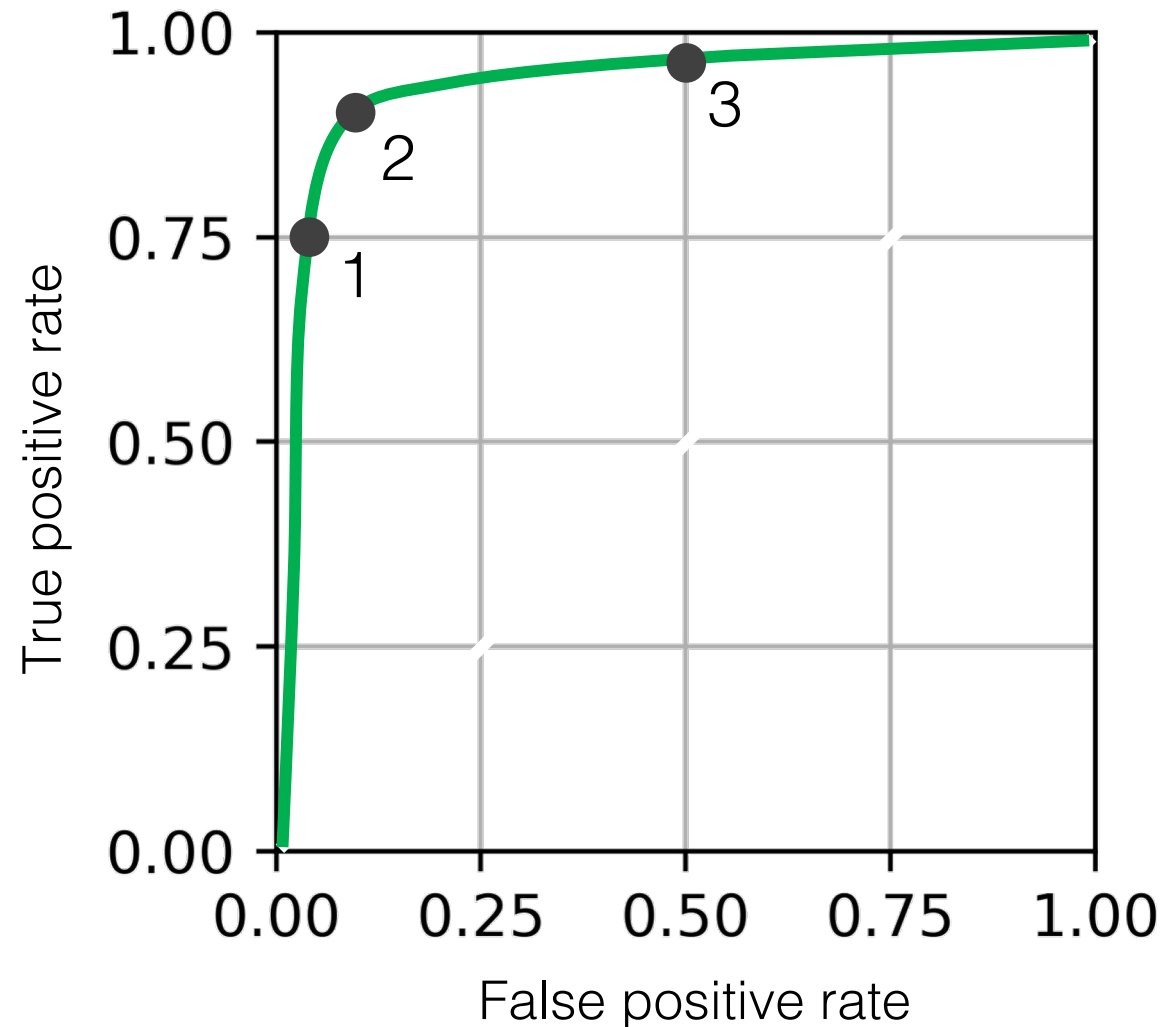
Threshold	# True Positives	True Positive Rate	# False Positives	False Positive Rate
∞	0	0	0	0
1.0	1	0.333	0	0
0.9	2	0.667	0	0
0.7	2	0.667	1	0.5
0.0	3	1	1	0.5
$-\infty$	3	1	2	1

ROC Curves: how do they compare?



The model represented by this ROC curve is the most discriminative (but usually predicts incorrectly)

ROC Curves: where do we operate?

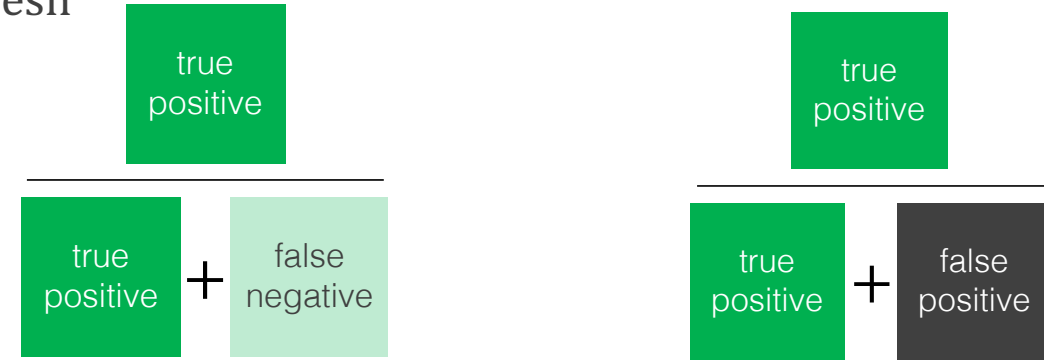


What does it mean to operate at a point on this curve?

PR Curves

Classifier decision rule:

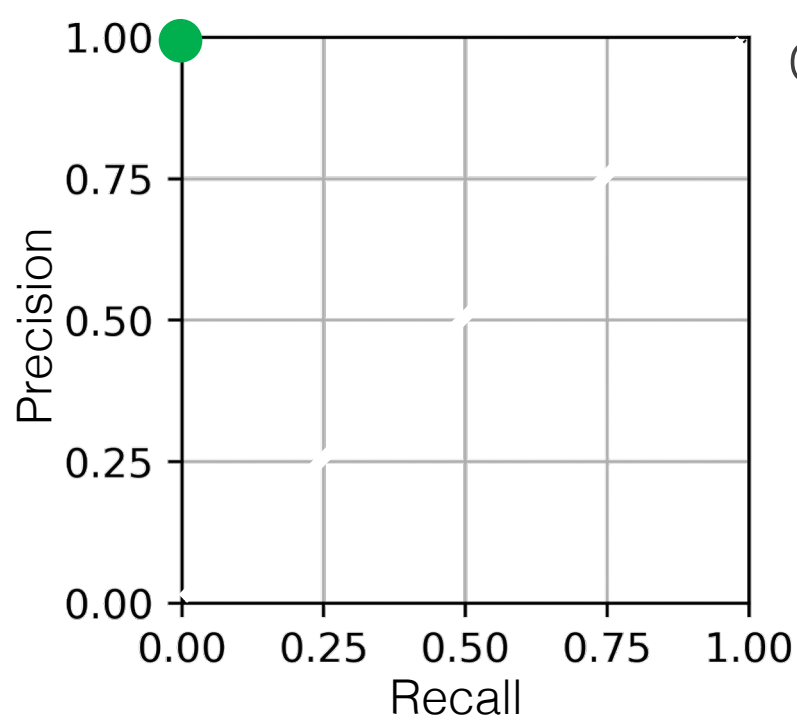
$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Total Positives = 3

Total Negatives = 2

Threshold	# True Positives	Recall	# Predicted Positive	Precision
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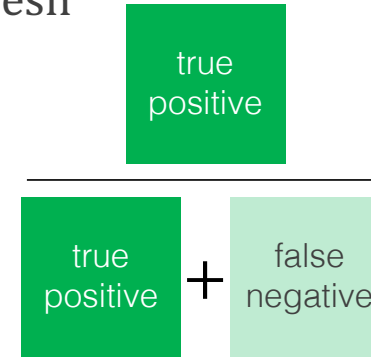
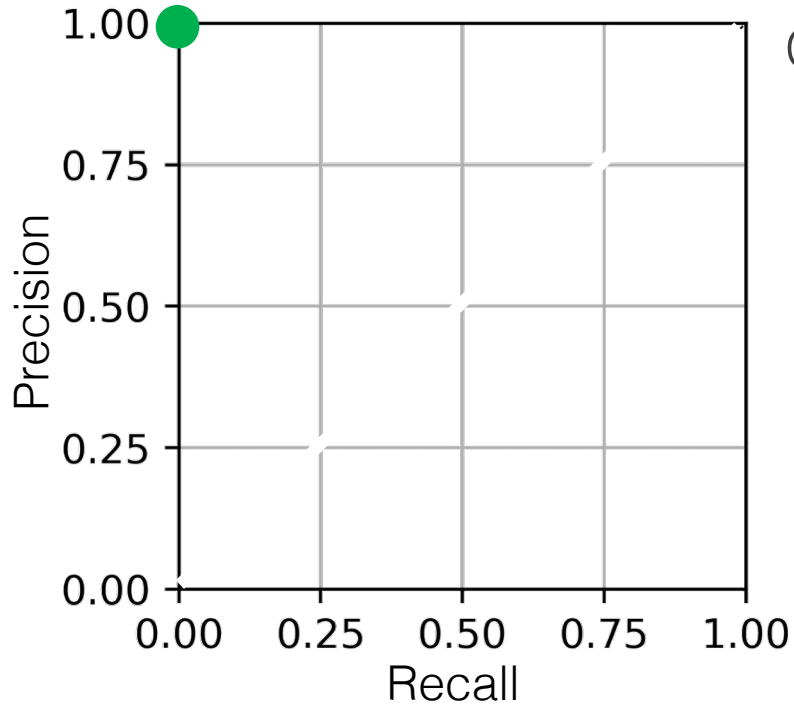


True Class Label (y)	Classifier Confidence
1	1.40
1	0.95
0	0.80
1	0.60
0	-0.10

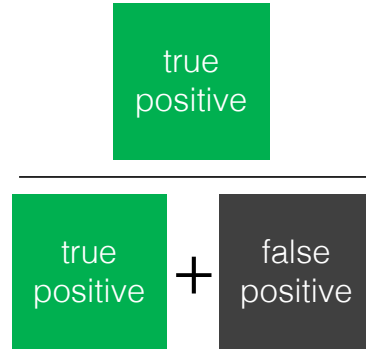
PR Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Total Positives = 3



Total Negatives = 2

Threshold	# True Positives	Recall	# Predicted Positive	Precision
∞	0	0	0	undefined

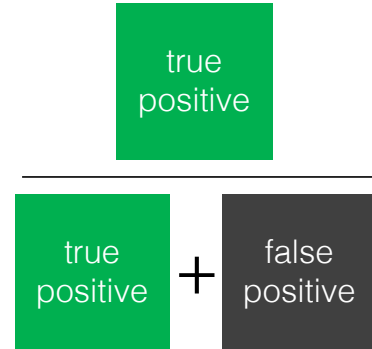
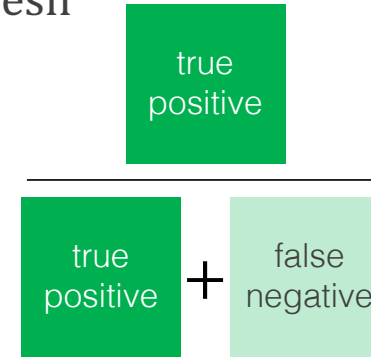
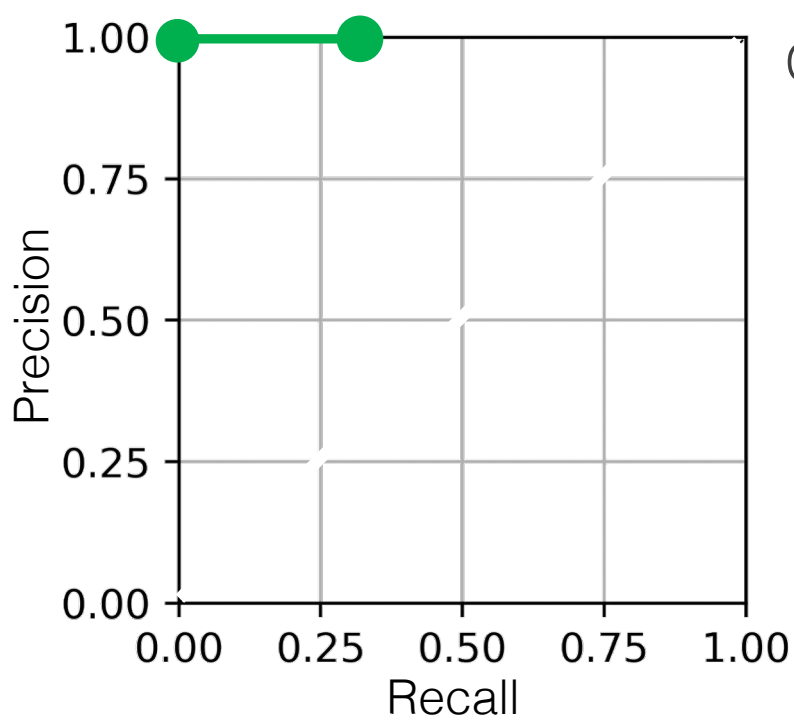


Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
0	1	1.40
0	1	0.95
0	0	0.80
0	1	0.60
0	0	-0.10

PR Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Total Positives = 3

Total Negatives = 2

Threshold	# True Positives	Recall	# Predicted Positive	Precision
∞	0	0	0	undefined
1.0	1	0.333	1	1

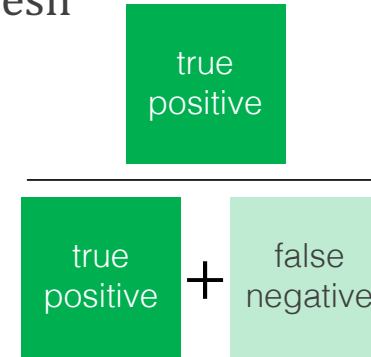
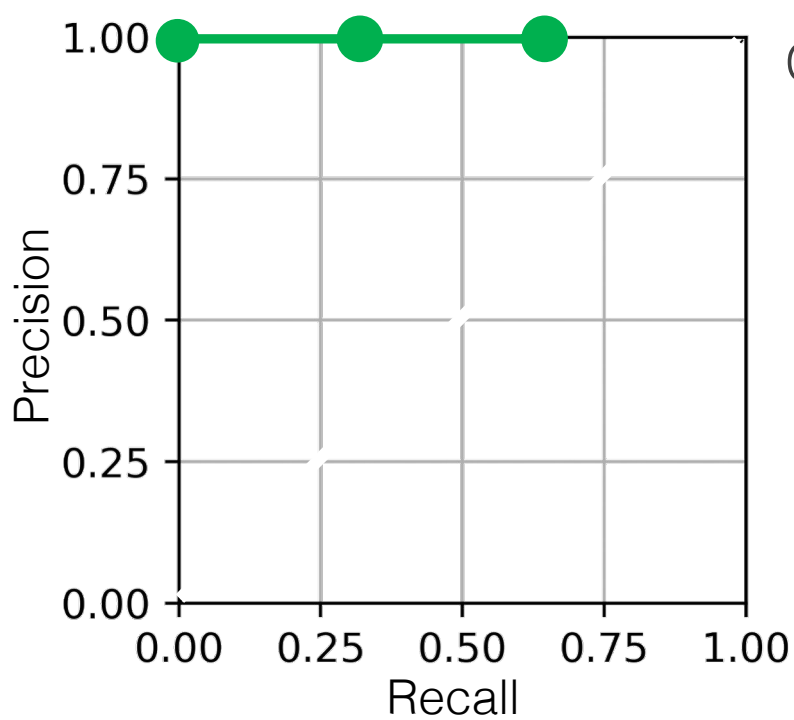
Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
0	1	0.95
0	0	0.80
0	1	0.60
0	0	-0.10



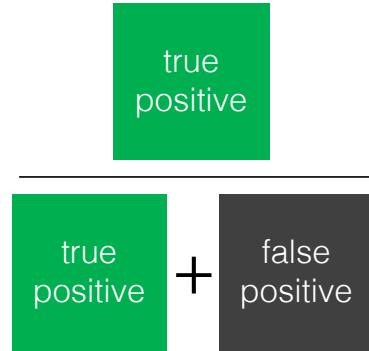
PR Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Total Positives = 3



Total Negatives = 2

Threshold	# True Positives	Recall	# Predicted Positive	Precision
∞	0	0	0	undefined
1.0	1	0.333	1	1
0.9	2	0.667	2	1

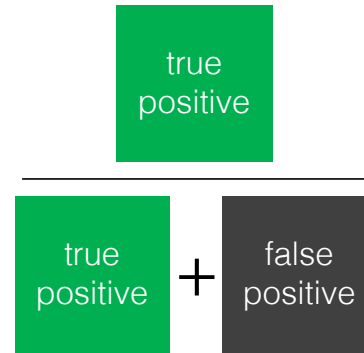
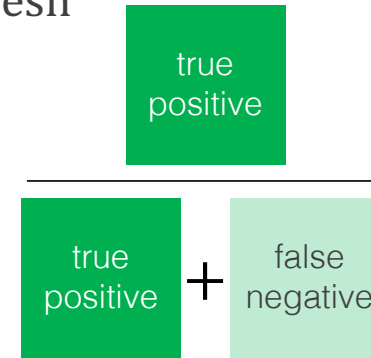
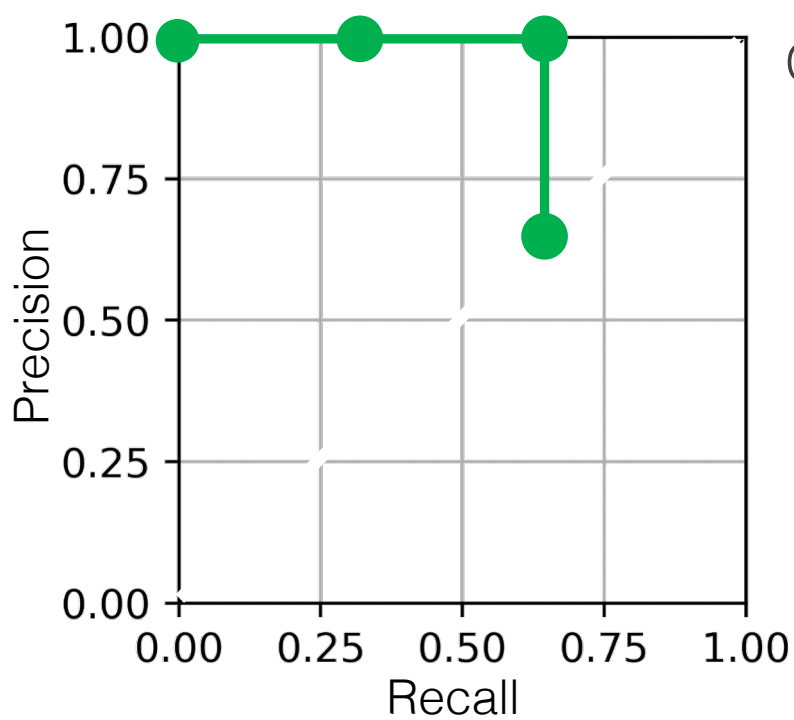
Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
1	1	0.95
0	0	0.80
0	1	0.60
0	0	-0.10



PR Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Total Positives = 3

Total Negatives = 2

Threshold	# True Positives	Recall	# Predicted Positive	Precision
∞	0	0	0	undefined
1.0	1	0.333	1	1
0.9	2	0.667	2	1
0.7	2	0.667	3	0.667

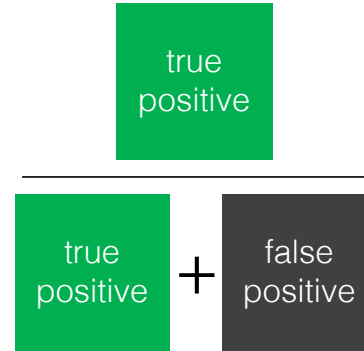
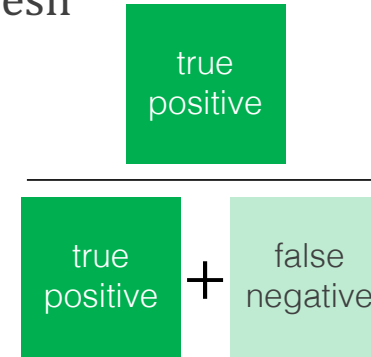
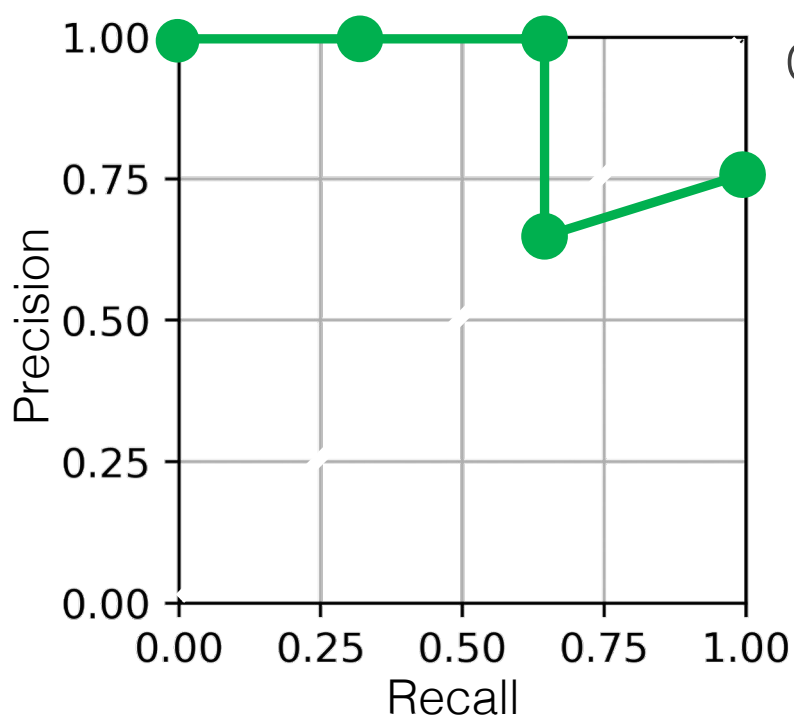


Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
1	1	0.95
1	0	0.80
0	1	0.60
0	0	-0.10

PR Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Total Positives = 3

Total Negatives = 2

Threshold	# True Positives	Recall	# Predicted Positive	Precision
∞	0	0	0	undefined
1.0	1	0.333	1	1
0.9	2	0.667	2	1
0.7	2	0.667	3	0.667
0.0	3	1	4	0.75

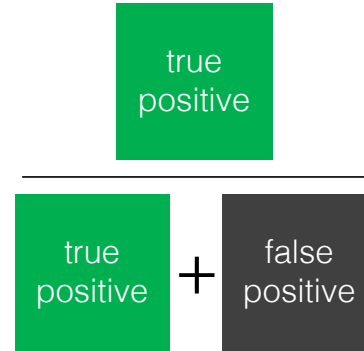
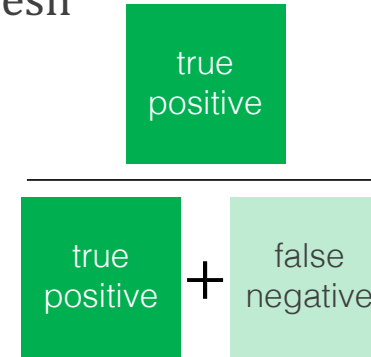
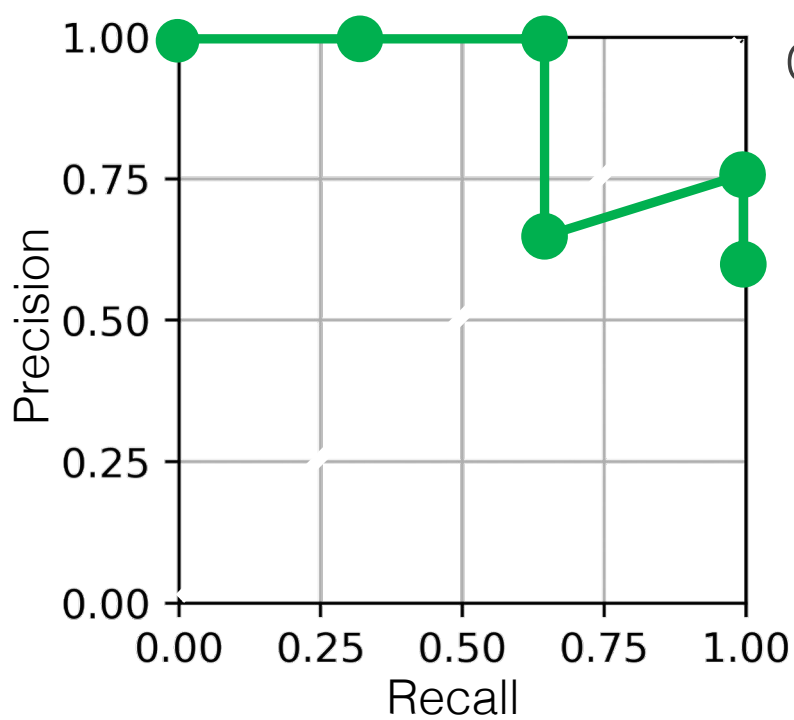
Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
1	1	0.95
1	0	0.80
1	1	0.60
0	0	-0.10



PR Curves

Classifier decision rule:

$$\hat{y} = \begin{cases} 1, & \text{confidence score} > \text{thresh} \\ 0, & \text{confidence score} \leq \text{thresh} \end{cases}$$



Total Positives = 3

Total Negatives = 2

Threshold	# True Positives	Recall	# Predicted Positive	Precision
∞	0	0	0	undefined
1.0	1	0.333	1	1
0.9	2	0.667	2	1
0.7	2	0.667	3	0.667
0.0	3	1	4	0.75
$-\infty$	3	1	5	0.6

Estimate (\hat{y})	True Class Label (y)	Classifier Confidence
1	1	1.40
1	1	0.95
1	0	0.80
1	1	0.60
1	0	-0.10



Be wary of overall accuracy as sole metric

Case study 1

i	y_i	\hat{y}_i
1	1	1
2	1	1
3	1	1
4	1	1
5	1	1
6	1	1
7	1	0
8	0	1
9	0	0
10	0	0
11	0	0
12	0	0
13	0	0
14	0	0
15	0	0

Overall classification accuracy = $13/15 = 0.87$

ROC Curves measure the tradeoff between...

A False positive rate = $1/8 = 0.13$

B True positive rate (Recall) = $6/7 = 0.86$

PR Curves measure the tradeoff between...

B True positive rate (Recall) = $6/7 = 0.86$

C Precision = $6/7 = 0.86$

A

false
positive

false
positive + true
negative

B

true
positive

true
positive + false
negative

C

true
positive

true
positive + false
positive

Case study 2

i	y_i	\hat{y}_i
1	1	1
2	1	1
3	1	0
4	1	0
5	0	0
6	0	0
7	0	0
8	0	0
9	0	0
10	0	0
11	0	0
12	0	0
13	0	0
14	0	0
15	0	0

Overall classification accuracy = $13/15 = 0.87$

ROC Curves measure the tradeoff between...

A False positive rate = $0/11 = 0$

B True positive rate (Recall) = $2/4 = 0.5$

PR Curves measure the tradeoff between...

B True positive rate (Recall) = $2/4 = 0.5$

C Precision = $2/2 = 1$

A

false
positive

false
positive + true
negative

B

true
positive

true
positive + false
negative

C

true
positive

true
positive + false
positive

Case study 3

i	y_i	\hat{y}_i
1	1	1
2	1	1
3	1	1
4	1	1
5	1	1
6	1	1
7	1	1
8	1	1
9	1	1
10	1	1
11	1	1
12	1	1
13	1	1
14	0	1
15	0	1

Overall classification accuracy = $13/15 = 0.87$

ROC Curves measure the tradeoff between...

A False positive rate = $2/2 = 1$

B True positive rate (Recall) = $13/13 = 1$

PR Curves measure the tradeoff between...

B True positive rate (Recall) = $13/13 = 1$

C Precision = $13/15 = 0.87$

A

false
positive

false
positive + true
negative

B

true
positive

true
positive + false
negative

C

true
positive

true
positive + false
positive

Multiclass Classification: Confusion Matrix

		Predicted Class, \hat{y}			No. samples from class ↓
		Class 1	Class 2	Class 3	
True Class, y	Class 1	190	8	2	[200]
	Class 2	1	5	4	[10]
	Class 3	24	24	25	[73]

confusion matrix with number of samples

Multiclass Classification: Confusion Matrix

		Predicted Class, \hat{y}			No. samples from class ↓ [200]
		Class 1	Class 2	Class 3	
True Class, y	Class 1	190	8	2	[10]
	Class 2	1	5	4	
	Class 3	24	24	25	

confusion matrix with number of samples

		Predicted Class, \hat{y}			[200]
		Class 1	Class 2	Class 3	
True Class, y	Class 1	0.95	0.04	0.01	[10]
	Class 2	0.10	0.50	0.40	
	Class 3	0.33	0.33	0.34	

confusion matrix with probabilities

F₁-score

$$F_1 = 2 \frac{1}{\frac{1}{\text{recall}} + \frac{1}{\text{precision}}}$$

Harmonic mean of
precision and recall

$$= 2 \frac{\text{precision} \cdot \text{recall}}{\text{precision} + \text{recall}}$$

Generally:

$$F_\beta = (1 + \beta^2) \frac{\text{precision} \cdot \text{recall}}{\beta^2 \cdot \text{precision} + \text{recall}}$$

β controls the relative
weight of precision/recall

Multiclass F_1

Micro-average: Calculate precision and recall metrics globally by counting the total true positives, false negatives, and false positives
(average for the whole dataset)

Macro-average: Use the average precision and recall for each class label
(average of class-averages)

Computational Efficiency

Measure of how an algorithm's run time (or space requirements) grow as the input size grows

Complexity of making predictions with kNN

(compare an unseen sample to the training samples)

Assume we have $n = 10,000$, $p = 2$

The Euclidean distance between $\begin{bmatrix} x_{1,1} \\ x_{1,2} \end{bmatrix}$ and $\begin{bmatrix} x_{2,1} \\ x_{2,2} \end{bmatrix}$ can be measured as:

$$\sqrt{(x_{2,1} - x_{1,1})^2 + (x_{2,2} - x_{1,2})^2}$$

That's two (p) distinct sets of operations dependent on the data

We repeat that n times – once for each sample in the training dataset

$$O(np)$$

Computational Efficiency

Training time efficiency?

Test time efficiency?

How do each change with the size of our data?

Interpretability

Transparency (can I tell how the model works)

- **Simulatability**: can I contemplate the whole model at once?
- **Decomposability**: is there an intuitive explanation for each part of the model?
(e.g. all patients with diastolic blood pressure over 150)

Explainability (post-hoc explanations)

Visualization, local explanations, explanations by example

(e.g. this tumor is classified as malignant because to the model it looks a lot like these other tumors)

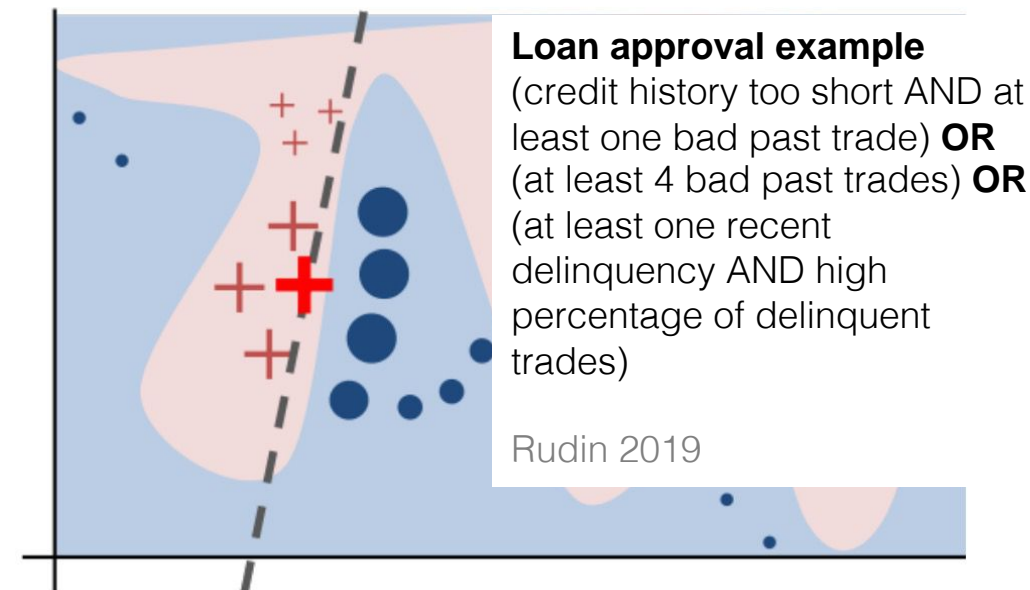
Lipton, Zachary C. "The Mythos of Model Interpretability: In Machine Learning, the Concept of Interpretability Is Both Important and Slippery." Queue 16, no. 3 (2018): 31–57.

Recidivism prediction algorithm

Performance as good as a black box model with 130+ factors;
might include socio-economic info; expensive (software license);
within software used in US justice system

IF	age between 18–20 and sex is male	THEN predict arrest (within 2 years)
ELSE IF	age between 21–23 and 2–3 prior offences	THEN predict arrest
ELSE IF	more than three priors	THEN predict arrest
ELSE	predict no arrest	

Rudin, Cynthia. "Stop Explaining Black Box Machine Learning Models for High Stakes Decisions and Use Interpretable Models Instead." Nature Machine Intelligence 1, no. 5 (2019): 206–15.



Ribeiro, Marco Tulio, Sameer Singh, and Carlos Guestrin. "Model-Agnostic Interpretability of Machine Learning." ArXiv Preprint ArXiv:1606.05386, 2016.