PROJECT 1: Implementing Algorithms

Submitted by:

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Both screenshots:

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1 GROUP MEMBER:

2 ABIOLA GODO

4
```

```
student@Abiola: ~/Desktop
                                                              Q ≡
student@Abiola:~/Desktop$ make
g++ .c disks_test .cpp
g++ disks_test.o -o disk
student@Abiola:~/Desktop$ g++ disks_test.cpp
student@Abiola:~/Desktop$ ./a.out
disk_state still works: passed, score 1/1
sorted_disks still works: passed, score 1/1
disk_state::is_initialized: passed, score 3/3
disk state::is sorted: passed, score 3/3
alternate, n=4: passed, score 1/1 alternate, n=3: passed, score 1/1
alternate, other values: Passed score 1/1
lawnmower, n=4: passed, score 1/1
lawnmower, n=3: passed, score 1/1
lawnmower, other values: passed, score 1/1
TOTAL SCORE = 14/14
```

Following is a pseudocode of the Lawnmower Algorithm for the given problem.

Algorithm1: Lawnmower Algorithm

Input: $n \leftarrow a$ positive integer n

 $L \leftarrow$ a list of 2n disks of alternating colors dark-light, starting with dark

Output: L' \leftarrow a list of 2n disks, the first n disks are dark, the next n disks are light

 $m \leftarrow$ an integer representing the number of swaps required

```
1.
     m \leftarrow 0
2.
     L'←L
3.
     For i = 1, 2, ..., n/2:
4.
               For j = 1, 2, ..., 2n - 1:
                      If L'[j] == white and L'[j+1] == black
5.
6.
                              swap(L'[j], L'[j+1])
7.
                              m := m + 1
8.
                      End If
9.
               End For
               For j = 2n, 2n - 1, ..., 2:
10.
                      If L'[j-1] == white and L'[j] == black
11.
12.
                               swap(L'[j-1], L'[j])
                              m := m + 1
13.
                       End If
14.
               End For
15.
16.
       End For
     Return L', m
17.
```

Complexity Analysis of the Lawnmower Algorithm:

Here the first loop (line 3) takes n/2 iterations. Inside the first loop, there are two more loops (line 4, line 10). Both of them take 2n-1 iterations. The contents inside those loops have complexity of O(1).

So the total complexity becomes:

```
(n/2) * ((2n-1) + (2n-1))
=> (n/2) * (4n-2)
=> n * (2n-1)
=> 2n^2 - n
```

So we can say that the complexity of the Lawnmower Algorithm is $O(n^2)$.

Following is a pseudocode of the Alternate Algorithm for the given problem.

Algorithm2: Alternate Algorithm

Input: $n \leftarrow a$ positive integer n

 $L \leftarrow$ a list of 2n disks of alternating colors dark-light, starting with dark

Output: L' \leftarrow a list of 2n disks, the first n disks are dark, the next n disks are light

 $m \leftarrow$ an integer representing the number of swaps required

```
1.
     m \leftarrow 0
2.
     L'←L
3.
     For i = 1, 2, ..., n:
               If i \% 2 == 1
4.
5.
                      For j = 1, 3, ..., 2n - 1:
                              If L'[j] == white and L'[j+1] == black
6.
7.
                                      swap(L'[j], L'[j+1])
                                      m := m + 1
8.
9.
                              End If
10.
                      End For
               End If
11.
12.
               Else
13.
                      For j = 2, 4, ..., 2n - 2:
14.
                              If L'[j] == white and L'[j+1] == black
15.
                                      swap(L'[j], L'[j+1])
                                      m := m + 1
16.
                              End If
17.
18.
                      End For
               End Else
19.
20.
       End For
21.
     Return L', m
```

Complexity Analysis of the Alternate Algorithm:

Here the first loop (line 3) takes n iterations. Inside the first loop, there are two more loops (line 5, line 13). Both of them take n and n - 1 iterations correspondingly. The contents inside those loops have complexity of O(1).

So the total complexity becomes:

```
n * (n + (n - 1))
=> n * (2n - 1)
=> 2n^2 - n
```

So we can say that the complexity of the Alternate Algorithm is $O(n^2)$.