

<i>qu.</i>	<i>Use</i>	<i>Key</i>	<i>Code</i>	<i>ITEM</i>
145	Web2	C	A 1	921
<ul style="list-style-type: none"> <li><math>x^2 + 10x - 24 = 0</math></li> <li><math>(x + 12)(x - 2) = 0</math></li> <li><math>x = -12, x = 2</math></li> </ul>				
146	Web2	C	A 2	996
<ul style="list-style-type: none"> <li><math>\log_6 2x = 1 \Rightarrow x = 3</math></li> <li><math>\log_6 2x = 0 \Rightarrow 2x = 1</math></li> <li><math>(\bullet) x = \frac{1}{2}</math></li> </ul>				
147	Web2	B	A 3	919
<ul style="list-style-type: none"> <li><math>(b, 3) \rightarrow (b, -3)</math></li> <li><i>so B</i></li> </ul>				
148	Web2	B	A 4	55
<ul style="list-style-type: none"> <li><math>f(2x)</math></li> <li><math>(2x)^2 + 1</math></li> <li><math>(\bullet) 4x^2 + 1</math></li> </ul>				
149	Web2	B	A 5	925
<ul style="list-style-type: none"> <li><math>2p = -8 \Rightarrow p = -4</math></li> <li><math>p^2 + q = 7 \Rightarrow q = -9</math></li> </ul>				
150	Web2	D	A 6	1235
<ul style="list-style-type: none"> <li><math>\sin\left(x - \frac{\pi}{6}\right) = 1 \Rightarrow x = \frac{2\pi}{3} \text{ so (1)}\checkmark</math></li> <li><math>y_{\max} = 3 \times 1 + 5 = 8 \text{ so (2)}\checkmark</math></li> </ul>				
151	Web2	D	A 7	9
<ul style="list-style-type: none"> <li><math>(0, 0) \Rightarrow \text{not } C</math></li> <li><math>(1, -2) \Rightarrow C \text{ or } D</math></li> <li><math>(\bullet) D</math></li> </ul>				
152	Web2	B	A 10	2001
<ul style="list-style-type: none"> <li><math>u_2 = 0.4 \times 50 + 5 = 25</math></li> <li><math>u_3 = 0.4 \times 25 + 5 = 15</math></li> <li><math>u_4 = 0.4 \times 15 + 5 = 11</math></li> <li><math>u_5 = 0.4 \times 11 + 5 = 9.4</math></li> </ul>				
153	Web2	D	A 11	1074
<ul style="list-style-type: none"> <li><math>u_{k+1} = 3u_k - 2 = 13</math></li> <li><math>u_{k+2} = 3u_{k+1} - 2 = 37</math></li> </ul>				
154	Web2	C	A 12	1109
<ul style="list-style-type: none"> <li><math>-1 &lt; p - 1 &lt; 1</math></li> <li><math>0 &lt; p &lt; 2</math></li> </ul>				

<i>qu.</i>	<i>Use</i>	<i>Key</i>	<i>Code</i>	<i>ITEM</i>
155	Web2	A	A 13	929
<ul style="list-style-type: none"> <li><math>L = -0.7L + 21</math></li> <li><math>L = \frac{21}{1.7}</math></li> <li><math>(\bullet) L = \frac{210}{17}</math></li> </ul>				
156	Web2	C	A 15	1001
<ul style="list-style-type: none"> <li><math>y = k(x + 2)(x - 4)</math></li> <li><math>-1 = k(6 + 2)(6 - 4)</math></li> <li><math>(\bullet) k = -\frac{1}{16}</math></li> </ul>				
157	Web2	D	A 16	930
<ul style="list-style-type: none"> <li><math>(x + 2)(2x - 3) &gt; 0</math></li> <li><math>x = 0 \text{ is false}</math></li> <li><math>(\bullet) x &lt; -2, x &gt; \frac{3}{2}</math></li> </ul>				
158	Web2	A	A 17	1163
<ul style="list-style-type: none"> <li><math>\begin{pmatrix} 0 \\ -3 \end{pmatrix} \text{ on } f \Rightarrow \text{cuts } x\text{-axis twice}</math></li> <li><math>b^2 - 4ac &gt; 0</math></li> </ul>				
159	Web2	D	A 18	1003
<ul style="list-style-type: none"> <li><math>b^2 - 4ac = 0</math></li> <li><math>16 - (-24k) = 0</math></li> <li><math>(\bullet) k = -\frac{2}{3}</math></li> </ul>				
160	Web2	A	A 19	1076
<ul style="list-style-type: none"> <li><math>y = k(x + 3)(x - 1)(x - 2)</math></li> <li><math>12 = 6k</math></li> <li><math>(\bullet) k = 2</math></li> </ul>				
161	Web2	B	A 21	91
<ul style="list-style-type: none"> <li><math>(-5)^3 + 4 \times (-5)^2 - 5k - 10 = 0</math></li> <li><math>-125 + 100 - 10 = 5k</math></li> <li><math>(\bullet) k = -7</math></li> </ul>				
162	Web2	C	A 23	1902
<ul style="list-style-type: none"> <li><math>x = -\frac{2}{3}y - \frac{7}{3}</math></li> <li><math>y = 3\left(-\frac{2}{3}y - \frac{7}{3}\right)^2 + 4\left(-\frac{2}{3}y - \frac{7}{3}\right) - 7</math></li> </ul>				
163	Web2	C	A 28	24
<ul style="list-style-type: none"> <li><math>\log_9 9^{\frac{3}{2}}</math></li> <li><math>\frac{3}{2} \log_9 9</math></li> </ul>				

<i>qu.</i>	<i>Use</i>	<i>Key</i>	<i>Code</i>	<i>ITEM</i>
164	Web2	D	A 31	339
<ul style="list-style-type: none"> <li><math>64 = y^{\frac{2}{3}}</math></li> <li><math>8 = y^{\frac{1}{3}}</math></li> <li><math>(\bullet) y = 512</math></li> </ul>				
165	Web2	A	A 32	1251
<ul style="list-style-type: none"> <li><math>\log_4 8q = 1</math></li> <li><math>8q = 4</math></li> <li><math>(\bullet) q = \frac{1}{2}</math></li> </ul>				
166	Web2	A	A 33	2034
<ul style="list-style-type: none"> <li><math>y = 100x^3</math></li> <li><math>\log_{10} y = \log_{10}(100x^3)</math></li> <li><math>\log_{10} y = \log_{10} 100 + \log_{10} x^3</math></li> <li><math>(\bullet) \log_{10} y = 2 + 3\log_{10} x</math></li> </ul>				
167	Web2	C	C 1	307
<ul style="list-style-type: none"> <li><math>f'(x) = 12x^2</math></li> <li><math>f'(2) = 12 \times 4</math></li> <li><math>(\bullet) f'(2) = 48</math></li> </ul>				
168	Web2	A	C 2	1008
<ul style="list-style-type: none"> <li><math>\bullet \frac{dy}{dx} = \frac{1}{4}x^{-\frac{3}{4}} + \frac{1}{2}x^{-\frac{3}{2}}</math></li> </ul>				
169	Web2	D	C 3	30
<ul style="list-style-type: none"> <li><math>f(x) = x^{-2}</math></li> <li><math>f'(x) = -2x^{-3}</math></li> <li><math>(\bullet) f'(x) = -\frac{2}{x^3}</math></li> </ul>				
170	Web2	A	C 4	968
<ul style="list-style-type: none"> <li><math>\frac{dy}{dx} = 3x^2 + 4x</math></li> <li><math>\frac{dy}{dx}_{x=1} = 3 \times 1 + 4 \times 1 = 7</math></li> </ul>				
171	Web2	A	C 6	1011
<ul style="list-style-type: none"> <li><math>\frac{dv}{dt} = 2t + 2</math></li> <li><math>t = 3 \Rightarrow \frac{dv}{dt} = 8</math></li> </ul>				
172	Web2	B	C 7	366
<ul style="list-style-type: none"> <li><math>f'(x) = -4x^{-3}</math></li> <li><math>-\frac{4}{x^3} &gt; 0</math></li> <li><math>x^3 \text{ is neg., } x \text{ is neg.}</math></li> </ul>				

qu.	Use	Key	Code	ITEM
173	Web2	D	C 8	330
<ul style="list-style-type: none"> <li>stationary pts at <math>f'(x) = 0</math></li> <li><math>x(x+2) = 0</math></li> <li>(•) <math>x = 0, x = -2</math></li> </ul>				
174	Web2	B	C 12	942
<ul style="list-style-type: none"> <li><math>f(x) = 2x^3 - x^{-1} + c</math></li> </ul>				
175	Web2	C	C 13	248
<ul style="list-style-type: none"> <li><math>y = \left[ \frac{3}{7} x^{\frac{7}{3}} \right]_{-1}^1</math></li> <li><math>y = \left( \frac{3}{7} \times 1^{\frac{7}{3}} \right) - \left( \frac{3}{7} \times (-1)^{\frac{7}{3}} \right)</math></li> <li><math>y = \frac{3}{7} - \left( -\frac{3}{7} \right) = \frac{6}{7}</math></li> </ul>				
176	Web2	A	C 14	115
<ul style="list-style-type: none"> <li><math>f'(x) = x^{-4}</math></li> <li><math>f(x) = -\frac{1}{3}x^{-3}</math></li> <li>(•) <math>f(x) = -\frac{1}{3x^3} + c</math></li> </ul>				
177	Web2	D	C 15	2039
<ul style="list-style-type: none"> <li><math>I = \left[ 12x + \frac{1}{4}x^4 \right]_0^2</math></li> <li><math>= (24 + 4) - 0</math></li> <li><math>= 28</math></li> </ul>				
178	Web2	A	C 17	208
<ul style="list-style-type: none"> <li><math>\sin x = \cos x</math></li> <li><math>x = \frac{\pi}{4}</math></li> <li><math>\int_0^{\frac{\pi}{4}} \sin x \, dx + \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \cos x \, dx</math></li> </ul>				
179	Web2	A	C 18	1071
<ul style="list-style-type: none"> <li>know to integrate</li> <li><math>y = \frac{1}{3}x^3 - 2x^2 + c</math></li> </ul>				
180	Web2	A	C 20	85
<ul style="list-style-type: none"> <li><math>\frac{dy}{dx} = -\sin x</math></li> <li>gradient <math>= -\sin \frac{\pi}{2}</math></li> <li>(•) gradient <math>= -1</math></li> </ul>				
181	Web2	C	C 21	1094
<ul style="list-style-type: none"> <li><math>f'(x) = 3(x^4 + 2x)^2 \times \dots</math></li> <li><math>f'(x) = \dots \times (4x^3 + 2)</math></li> <li>(•) <math>f'(x) = 3(4x^3 + 2)(x^4 + 2x)^2</math></li> </ul>				

qu.	Use	Key	Code	ITEM
182	Web2	C	C 22	320
<ul style="list-style-type: none"> <li><math>y = \frac{1}{4}(2x+1)^4 \times \dots</math></li> <li><math>y = \dots \times \frac{1}{2}</math></li> <li>(•) <math>y = \frac{1}{8}(2x+1)^4 + c</math></li> </ul>				
183	Web2	B	C 23	98
<ul style="list-style-type: none"> <li><math>I = -\cos 3x \times \dots</math></li> <li><math>I = \dots \times \frac{1}{3}</math></li> <li>(•) <math>I = -\frac{1}{3}\cos 3x + c</math></li> </ul>				
184	Web2	C	G 1	1045
<ul style="list-style-type: none"> <li><math>PQ = \sqrt{(-2-3)^2 + (3-5)^2 + (1-2)^2}</math></li> <li><math>PQ = \sqrt{30}</math></li> </ul>				
185	Web2	B	G 2	86
<ul style="list-style-type: none"> <li><math>m_{AB} = \frac{8-0}{0-(-4)} = 2</math></li> <li><math>m_{AC} = \frac{8-(-4)}{0-p} = -\frac{12}{p}</math></li> <li><math>-2p = 12 \dots p = -6</math></li> </ul>				
186	Web2	A	G 3	129
<ul style="list-style-type: none"> <li><math>m = \frac{-2-4}{1-(-3)} = -\frac{3}{2}</math></li> <li><math>y-4 = -\frac{3}{2}(x+3)</math></li> <li><math>2y-8 = -3x-9</math></li> <li><math>3x+2y+1=0</math></li> </ul>				
187	Web2	D	G 5	976
<ul style="list-style-type: none"> <li><math>y = -\frac{3}{5}x + \frac{8}{5}</math> AND <math>m = -\frac{3}{5}</math></li> <li><math>m_{\perp} = \frac{5}{3}</math></li> </ul>				
188	Web2	A	G 7	1048
<ul style="list-style-type: none"> <li><math>m_{\perp \text{ to } ST} = \frac{1}{2}</math></li> <li><math>y-8 = \frac{1}{2}(x-6)</math></li> <li>(•) <math>y = \frac{1}{2}x + 5</math></li> </ul>				
189	Web2	D	G 9	144
<ul style="list-style-type: none"> <li><math>x^2 + y^2 - 4x - 3y + \frac{1}{3} = 0</math></li> <li><math>C = (2, 1\frac{1}{2})</math></li> </ul>				

qu.	Use	Key	Code	ITEM
190	Web2	C	G 10	970
<ul style="list-style-type: none"> <li>centre(P) = (2, -3)</li> <li>radius(Q) = 4</li> <li>(•) <math>(x-2)^2 + (y+3)^2 = 16</math></li> </ul>				
191	Web2	C	G 11	1061
<ul style="list-style-type: none"> <li><math>m_{oc} = \frac{4}{3}</math></li> <li><math>m_{tgt} = -\frac{3}{4}</math></li> <li>(•) <math>y = -\frac{3}{4}x</math></li> </ul>				
192	Web2	A	G 12	2083
<ul style="list-style-type: none"> <li><math>(2y+5)^2 + y^2</math></li> <li><math>-6(2y+5) - 3y - 5 = 0</math></li> <li><math>5y^2 + 5y - 10 = 0</math></li> </ul>				
193	Web2	D	G 16	52
<ul style="list-style-type: none"> <li><math>\overrightarrow{PQ} = \begin{pmatrix} -6 \\ -4 \\ 4 \end{pmatrix}</math></li> <li><math> \overrightarrow{PQ}  = \sqrt{36 + 16 + 16} = \sqrt{68}</math></li> </ul>				
194	Web2	A	G 17	1185
<ul style="list-style-type: none"> <li><math>\overrightarrow{PQ} = \begin{pmatrix} 3 \\ 1 \\ 1 \end{pmatrix}</math>      <math>\overrightarrow{RS} = \begin{pmatrix} 9 \\ 3 \\ 3 \end{pmatrix}</math></li> <li>(•) <math>R = (1, 4, 2)</math> so <math>S = (10, 7, 5)</math></li> </ul>				
195	Web2	C	G 18	165
<ul style="list-style-type: none"> <li><math>\left(\frac{6}{7}\right)^2 + \left(-\frac{3}{7}\right)^2 + z^2 = 1</math></li> <li><math>z^2 = \frac{4}{49}</math>      (•) <math>z = \pm \frac{2}{7}</math></li> </ul>				
196	Web2	D	G 19	956
<ul style="list-style-type: none"> <li><math>\frac{2}{5} = \frac{-4}{p}</math></li> <li><math>2p = -20, p = -10</math></li> </ul>				
197	Web2	D	G 20	35
<ul style="list-style-type: none"> <li><math>x = \frac{1}{2}(2v - 3u)</math></li> <li><math>x = \frac{1}{2} \left[ \begin{pmatrix} 4 \\ -8 \\ 0 \end{pmatrix} - \begin{pmatrix} 3 \\ 0 \\ 3 \end{pmatrix} \right]</math>      (•) <math>x = \begin{pmatrix} \frac{1}{2} \\ -4 \\ -\frac{3}{2} \end{pmatrix}</math></li> </ul>				

qu. Use Key Code ITEM  
198 Web2 B G 21 1033

$$\begin{aligned} \bullet \vec{NP} &= \frac{1}{4} \vec{NL} \\ \bullet \vec{NL} &= -\mathbf{u} + \mathbf{v} \\ (\bullet) \vec{NP} &= \frac{1}{4}(-\mathbf{u} + \mathbf{v}) \end{aligned}$$

199 Web2 D G 22 1137

200 Web2 A G 24 1138

$$\begin{aligned} \bullet \vec{PX} &= \begin{pmatrix} -15 \\ -25 \\ -20 \end{pmatrix} = 5 \begin{pmatrix} -3 \\ -5 \\ -4 \end{pmatrix} \\ \bullet \vec{XQ} &= \begin{pmatrix} -6 \\ -10 \\ -8 \end{pmatrix} = 2 \begin{pmatrix} -3 \\ -5 \\ -4 \end{pmatrix} \quad (\bullet) \text{ ratio} = 5:2 \end{aligned}$$

201 Web2 B G 25 1035

$$\begin{aligned} \bullet \vec{KL} &= \begin{pmatrix} 10 \\ 0 \\ -10 \end{pmatrix} \quad \bullet \vec{KP} = \begin{pmatrix} 4 \\ 0 \\ -4 \end{pmatrix} \\ (\bullet) K &= (-1, 0, 4) \text{ so } P = (3, 0, 0) \end{aligned}$$

202 Web2 C G 26 1036

$$\begin{aligned} \bullet \mathbf{r} \cdot \mathbf{s} &= |\mathbf{r}| |\mathbf{s}| \cos 45^\circ \\ \bullet \mathbf{r} \cdot \mathbf{s} &= 1 \times \sqrt{2} \times \frac{1}{\sqrt{2}} \\ (\bullet) \mathbf{r} \cdot \mathbf{s} &= 1 \end{aligned}$$

203 Web2 A G 27 1059

$$\begin{aligned} \bullet \begin{pmatrix} g \\ 3 \\ 2 \end{pmatrix} \cdot \begin{pmatrix} 5 \\ -4 \\ -g \end{pmatrix} &= 0 \\ \bullet 5g - 12 - 2g &= 0 \quad (\bullet) g = 4 \end{aligned}$$

204 Web2 A G 28 983

$$\begin{aligned} \bullet \cos t^\circ &= \frac{\sqrt{3}}{\sqrt{2} \times \sqrt{2}} = \frac{\sqrt{3}}{2} \\ \bullet t &= 30 \end{aligned}$$

205 Web2 B G 29 1039

$$\begin{aligned} \bullet \mathbf{i} \cdot \mathbf{i} + 2\mathbf{i} \cdot \mathbf{j} - \mathbf{i} \cdot \mathbf{k} \\ \bullet |\mathbf{i}|^2 + 0 + 0 \\ (\bullet) 1 \end{aligned}$$

206 Web2 B T 1 68

$$\begin{aligned} \bullet 2t - \frac{\pi}{4} &= \frac{\pi}{2} \\ \bullet 2t &= \frac{3\pi}{4} \quad (\bullet) t = \frac{3\pi}{8} \end{aligned}$$

qu. Use Key Code ITEM  
207 Web2 A T 3 1143

$$\begin{aligned} \bullet -\frac{1}{2} \dots\dots \\ \bullet \dots\dots -\frac{1}{2} &= -1 \end{aligned}$$

208 Web2 B T 4 974

$$\begin{aligned} \bullet \max/\min &= \pm 3 \text{ so } A \text{ or } B \\ \bullet x = \pi, y = 3 \sin \frac{\pi}{2} &= 3 \text{ so } B \end{aligned}$$

209 Web2 B T 5 7

$$\begin{aligned} \bullet \min \left( 1 - \cos \left( t - \frac{\pi}{3} \right) \right) \\ \text{when } \cos \left( t - \frac{\pi}{3} \right) \text{ is max} \\ \bullet \cos \left( t - \frac{\pi}{3} \right) = 1 \quad (\bullet) t = \frac{\pi}{3} \end{aligned}$$

210 Web2 A T 7 1150

$$\begin{aligned} \bullet \sin x &= \frac{1}{\sqrt{2}} \text{ or } -\frac{1}{\sqrt{2}} \\ \bullet x = \frac{\pi}{4} \text{ or no sol. so } A \end{aligned}$$

211 Web2 B T 8 34

$$\begin{aligned} \bullet \cos 45 \cos 30 + \sin 45 \sin 30 \\ \bullet \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \cdot \frac{1}{2} \\ \frac{\sqrt{3} + 1}{2\sqrt{2}} \end{aligned}$$

212 Web2 B T 9 216

$$\begin{aligned} \bullet \sin 2x &= 2 \sin x \cos x \\ \bullet \cos x &= \sqrt{1 - k^2} \\ (\bullet) \sin 2x &= 2k\sqrt{1 - k^2} \end{aligned}$$

213 Web2 D T 12 1196

$$\begin{aligned} \bullet k^2 &= 3 + 1, k = 2 \\ \bullet \tan a^\circ &= \frac{1}{\sqrt{3}}, a = 30 \end{aligned}$$

214 Web2 B T 13 42

$$\begin{aligned} \bullet k \sin a &= 2, k \cos a = -3 \\ \bullet \tan a &= -\frac{2}{3} \end{aligned}$$

145

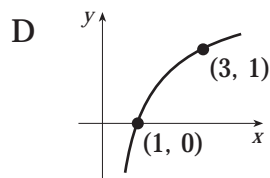
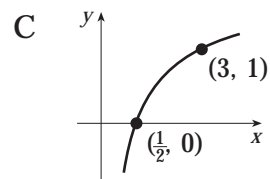
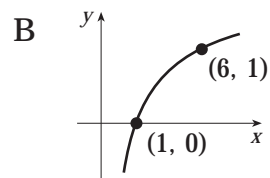
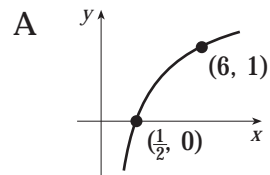
$$y = \frac{1}{x^2 + 10x - 24}.$$

For what values of  $x$  is  $y$  undefined?

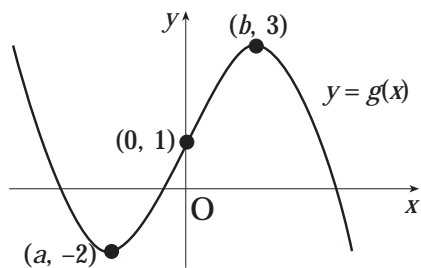
- A  $x = -6$  and  $x = 4$
- B  $x = -2$  and  $x = 12$
- C  $x = 2$  and  $x = -12$
- D  $x = 6$  and  $x = -4$

146

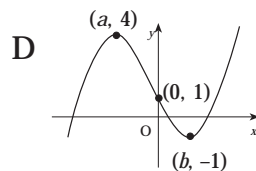
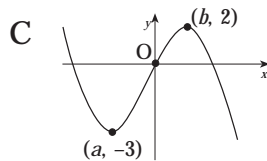
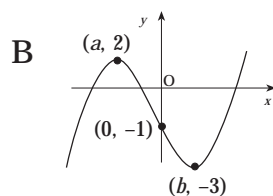
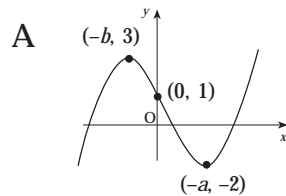
Which of the following sketches shows part of the graph of  $y = \log_6 2x$  ?



The diagram shows the graph of  $y = g(x)$ .



Which diagram below shows the graph of  $y = -g(x)$ ?



$f$  and  $g$  are functions defined by  $f(x) = x^2 + 1$  and  $g(x) = 2x$ , where  $x$  is a real number.

Find an expression for  $f(g(x))$ .

- A  $f(g(x)) = 2x^2 + 2$   
 B  $f(g(x)) = 4x^2 + 1$   
 C  $f(g(x)) = 2x^3 + 1$   
 D  $f(g(x)) = 2x^3 + 2x$

149

When  $x^2 - 8x + 7$  is written in the form  $(x + p)^2 + q$ , what is the value of  $q$ ?

- A  $-57$
- B  $-9$
- C  $7$
- D  $23$

150

Here are two statements about the graph of  $y = 3\sin\left(x - \frac{\pi}{6}\right) + 5$  for  $0 \leq x \leq 2\pi$ :

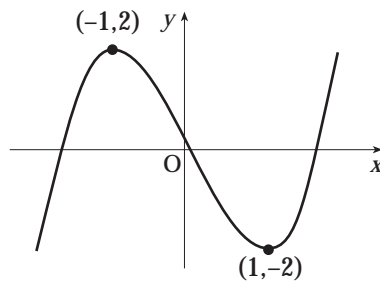
- (1) the maximum occurs when  $x = \frac{2\pi}{3}$
- (2) the maximum value of the function is 8.

Which of the following is true?

- A only statement (1) is correct
- B only statement (2) is correct
- C neither statement is correct
- D both statements are correct

151

The diagram shows the sketch of a cubic function  $f$  with turning points at  $(-1, 2)$  and  $(1, -2)$ . Which of the following is most likely to be  $f(x)$ ?



- A  $x^3 - x$
- B  $-x^3 + 3x$
- C  $-x^3 - 3x^2 - x + 3$
- D  $x^3 - 3x$

152

A sequence is defined by the recurrence relation

$$u_{n+1} = 0.4u_n + 5, \quad u_1 = 50.$$

What is the smallest value of  $n$  for which  $u_n < 11$ ?

- A  $n = 3$
- B  $n = 5$
- C  $n = 7$
- D  $n = 9$

**153**

The terms of a sequence satisfy the recurrence relation  $u_{n+1} = 3u_n - 2$ .

If  $u_k = 5$ , what is the value of  $u_{k+2}$  ?

- A  $\frac{7}{3}$
- B 7
- C 13
- D 37

**154**

A sequence is defined by the recurrence relation

$$u_{n+1} = (p-1)u_n + 3 \text{ with } u_0 = 12.$$

For what values of  $p$  does this sequence have a limit?

- A  $0 \leq p \leq 2$  only
- B  $-1 \leq p \leq 1$  only
- C  $0 < p < 2$  only
- D  $-1 < p < 1$  only

**155**

A sequence is defined by the recurrence relation  $u_{n+1} = -0.7u_n + 21$  with  $u_0 = 10$ .

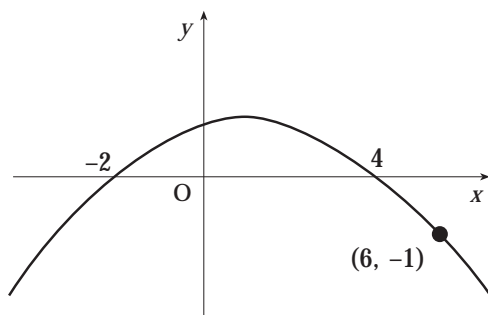
What is the limit of this sequence?

- A  $\frac{210}{17}$
- B  $\frac{210}{13}$
- C 30
- D 70

**156**

The diagram shows part of the graph of a quadratic function.

The equation of the graph is of the form  $y = k(x-l)(x-m)$ .



What is the value of  $k$  ?

- A -9
- B -2
- C  $-\frac{1}{16}$
- D  $-\frac{1}{8}$

**157**

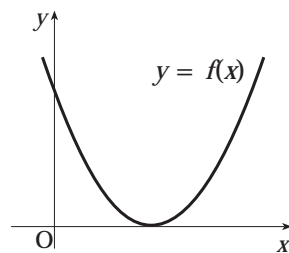
For what range of values of  $x$  is  $2x^2 + x - 6 > 0$ ?

- A  $x < -\frac{3}{2}$  or  $x > 2$
- B  $-\frac{3}{2} < x < 2$
- C  $-2 < x < \frac{3}{2}$
- D  $x < -2$  or  $x > \frac{3}{2}$

**158**

The diagram shows part of the graph of a parabola  $y = f(x)$  which touches the  $x$ -axis as shown.

The function  $g$  is given by  $g(x) = f(x) - 3$ .



Which of the following describes the value of the discriminant of  $g$ ?

- A discriminant  $> 0$
- B discriminant  $= 0$
- C discriminant  $< 0$
- D discriminant = any real number

**159**

The roots of the equation  $kx^2 + 4x - 6 = 0$  are equal.

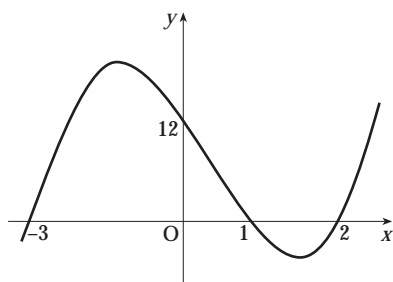
What is the value of  $k$ ?

- A  $-9$
- B  $-\frac{1}{6}$
- C  $-\frac{1}{3}$
- D  $-\frac{2}{3}$



160

The diagram shows part of the graph of a cubic function  $f$ .



What is the equation of the graph?

- A  $y = 2(x-1)(x-2)(x+3)$
- B  $y = -2(x+1)(x+2)(x-3)$
- C  $y = 12(x-1)(x-2)(x+3)$
- D  $y = 12(x+1)(x+2)(x-3)$

161

If  $x+5$  is a factor of the polynomial  $x^3 + 4x^2 + kx - 10$  what is the value of  $k$ ?

- A  $-3$
- B  $-7$
- C  $-35$
- D  $-43$

162

The line with equation  $3x + 2y + 7 = 0$  intersects the parabola with equation  $y = 3x^2 + 4x - 7$  at two points, P and Q.

Which of the following equations can be solved to find the coordinates of P and Q?

- A  $y = 3(2y+7)^2 + 4(2y+7) - 7$
- B  $y = 3(-2y-7)^2 + 4(-2y-7) - 7$
- C  $y = 3\left(-\frac{2}{3}y - \frac{7}{3}\right)^2 + 4\left(-\frac{2}{3}y - \frac{7}{3}\right) - 7$
- D  $y = 3\left(\frac{2}{3}y + \frac{7}{3}\right)^2 + 4\left(\frac{2}{3}y + \frac{7}{3}\right) - 7$

163

What is the exact value of  $\log_9 27$ ?

- A  $\frac{1}{3}$
- B  $\frac{2}{3}$
- C  $\frac{3}{2}$
- D  $3$

**164**

Given that  $\log_y 64 = \frac{2}{3}$ , find the value of  $y$ .

- A 24
- B 96
- C 256
- D 512

**165**

Given that  $\log_4 8 + \log_4 q = 1$ , what is the value of  $q$ ?

- A  $\frac{1}{2}$
- B  $\frac{1}{32}$
- C  $\frac{1}{8}$
- D 2

**166**

A graph is drawn of  $\log_{10} y$  against  $\log_{10} x$  where  $y = 100x^3$ .  
What is the equation of the graph?

- A  $\log_{10} y = 3\log_{10} x + 2$
- B  $\log_{10} y = 100\log_{10} x$
- C  $\log_{10} y = 300(\log_{10} x)^2$
- D  $\log_{10} y = 300\log_{10} x$

**167**

Given that  $f(x) = 4x^3 + 5$ , find the value of  $f'(2)$ .

- A 21
- B 26
- C 48
- D 53

**168**

What is the derivative, with respect to  $x$ , of  $x^{\frac{1}{4}} - x^{-\frac{1}{2}}$ ?

- A  $\frac{1}{4}x^{-\frac{3}{4}} + \frac{1}{2}x^{-\frac{3}{2}}$
- B  $\frac{1}{4}x^{-\frac{3}{4}} - \frac{1}{2}x^{-\frac{3}{2}}$
- C  $\frac{1}{4}x^{-\frac{1}{4}} + \frac{1}{2}x^{-\frac{3}{2}}$
- D  $\frac{1}{4}x^{\frac{1}{4}} + \frac{1}{2}x^{-\frac{1}{2}}$

**169**

If  $f(x) = \frac{1}{x^2}$  and  $x \neq 0$ , find  $f'(x)$ .

- A  $\frac{1}{2x}$
- B  $\frac{2}{x}$
- C  $-\frac{1}{x^3}$
- D  $-\frac{2}{x^3}$

**170**

A curve has equation  $y = x^3 + 2x^2 + 5$ .

What is the gradient of the curve at the point where  $x = 1$ ?

- A 7
- B 8
- C 10
- D 12

**171**

The speed,  $v$  m/s, at time  $t$  seconds is given by  $v(t) = t^2 + 2t$ .

What is the rate of change of speed when  $t = 3$ ?

- A  $8 \text{ m/s}^2$
- B  $12 \text{ m/s}^2$
- C  $15 \text{ m/s}^2$
- D  $18 \text{ m/s}^2$

**172**

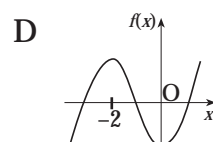
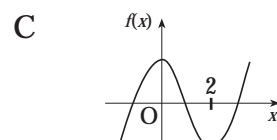
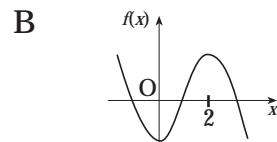
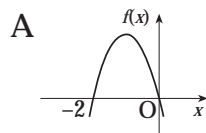
Find the values of  $x$  for which the graph of the

function  $f(x) = \frac{2}{x^2}, x \neq 0$ , has a positive gradient.

- A all possible values
- B  $x < 0$  only
- C  $x > 0$  only
- D  $x^3 < 4$  only

173

Which of the following graphs could be part of the graph of a function  $f$  such that  $f'(x) = x(x + 2)$ ?



174

If  $f(x) = \int (6x^2 + x^{-2}) \, dx$ , then find  $f(x)$ .

- A  $18x^3 - x^{-1} + c$
- B  $2x^3 - x^{-1} + c$
- C  $12x - 2x^{-3} + c$
- D  $2x^3 - \frac{1}{3}x^{-3} + c$

175

Find  $\int_{-1}^1 \left( \frac{4}{x^3} \right) \, dx$ .

- A 0
- B  $\frac{3}{7}$
- C  $\frac{6}{7}$
- D  $\frac{10}{3}$

176

Find  $\int \left( \frac{1}{x^4} \right) dx$ .

- A  $-\frac{1}{3x^3} + c$   
 B  $-\frac{3}{x^3} + c$   
 C  $-\frac{1}{5x^5} + c$   
 D  $\frac{5}{x^5} + c$

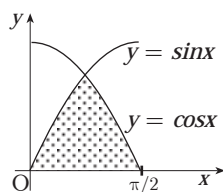
177

What is the value of  $\int_0^2 (12 + x^3) dx$  ?

- A 8  
 B 12  
 C 16  
 D 28

178

The diagram shows the curves with equations

 $y = \sin x$  and  $y = \cos x$  for  $0 \leq x \leq \frac{\pi}{2}$ .

Find an expression for the shaded area.

- A  $\int_0^{\frac{\pi}{4}} \sin x \, dx + \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \cos x \, dx$   
 B  $\int_0^{\frac{\pi}{2}} (\cos x - \sin x) \, dx$   
 C  $\int_0^{\frac{\pi}{2}} (\sin x - \cos x) \, dx$   
 D  $\int_0^{\frac{\pi}{2}} (\sin x + \cos x) \, dx$

179

If  $\frac{dy}{dx} = x^2 - 4x$ , express  $y$  in terms of  $x$ .

- A  $y = \frac{1}{3}x^3 - 2x^2 + c$   
 B  $y = 2x - 4 + c$   
 C  $y = x^2 - 4x + c$   
 D  $y = x^3 - 4x^2 + c$

**180**

A curve has equation  $y = \cos x$ .

What is the gradient of the curve at the point where  $x = \frac{\pi}{2}$  ?

- A  $-1$
- B  $-\frac{\pi}{4}$
- C  $0$
- D  $1$

**181**

What is the derivative, with respect to  $x$ , of  $(x^4 + 2x)^3$  ?

- A  $3(4x^3 + 2)^2$
- B  $\frac{1}{4}(\frac{1}{5}x^5 + x^2)^4$
- C  $3(x^4 + 2x)^2(4x^3 + 2)$
- D  $\frac{1}{4}(x^4 + 2x)^4(\frac{1}{5}x^5 + x^2)$

**182**

Find  $\int (2x+1)^3 dx$  .

- A  $\frac{1}{4}(2x+1)^4 + c$
- B  $\frac{1}{2}(2x+1)^4 + c$
- C  $\frac{1}{8}(2x+1)^4 + c$
- D  $(x^2 + x)^3 + c$

**183**

Find  $\int (\sin 3x) dx$  .

- A  $-\cos 3x + c$
- B  $-\frac{1}{3}\cos 3x + c$
- C  $\frac{1}{3}\cos 3x + c$
- D  $3\cos 3x + c$

**184**

R and T are the points  $(-2, 3, 1)$  and  $(3, 5, 2)$  respectively.

What is the length of the line RT ?

- A  $\sqrt{6}$
- B  $\sqrt{24}$
- C  $\sqrt{30}$
- D  $\sqrt{74}$

**185**

The straight line joining the points A(0,8) and B(-4,0) passes through the point C( $p$ , -4).

What is the value of  $p$  ?

- A      -8
- B      -6
- C      -2
- D      6

**186**

Find the equation of the line passing through the points with coordinates (1,-2) and (-3,4).

- A       $3x + 2y + 1 = 0$
- B       $3x - 2y - 7 = 0$
- C       $2x + 3y + 4 = 0$
- D       $2x - 3y - 8 = 0$

**187**

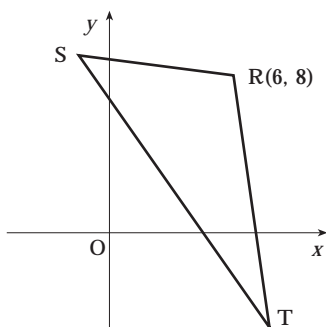
A line L has equation  $3x + 5y - 8 = 0$ .

What is the gradient of a line perpendicular to line L?

- A       $-\frac{3}{5}$
- B       $-\frac{1}{3}$
- C       $\frac{3}{5}$
- D       $\frac{5}{3}$

**188**

In triangle RST, R has coordinates (6, 8) and the gradient of ST is -2.



What is the equation of the altitude through R ?

- A       $y = \frac{1}{2}x + 5$
- B       $y = -2x + 20$
- C       $y = \frac{1}{2}x + 2$
- D       $y = -2x + 22$

**189**

What are the coordinates of the centre of the circle with equation  $3x^2 + 3y^2 - 12x - 9y + 1 = 0$  ?

- A (12, 9)
- B  $(6, 4\frac{1}{2})$
- C (4, 3)
- D  $(2, 1\frac{1}{2})$

**190**

Circle P has equation  $x^2 + y^2 - 4x + 6y - 1 = 0$ .

Circle Q has equation  $(x + 1)^2 + (y - 1)^2 = 16$ .

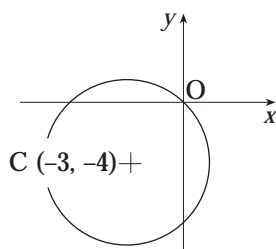
Circle R has the same centre as circle P and the same radius as circle Q.

What is the equation of circle R?

- A  $(x + 2)^2 + (y - 3)^2 = 4$
- B  $(x - 2)^2 + (y + 3)^2 = 4$
- C  $(x - 2)^2 + (y + 3)^2 = 16$
- D  $(x + 2)^2 + (y - 3)^2 = 16$

**191**

A circle, centre  $C(-3, -4)$ , passes through the origin.



What is the equation of the tangent to the circle at the origin ?

- A  $y = \frac{4}{3}$
- B  $y = \frac{3}{4}x$
- C  $y = -\frac{3}{4}x$
- D  $y = -\frac{4}{3}x$

**192**

The line with equation  $x = 2y + 5$  and the circle with equation

$x^2 + y^2 - 6x - 3y - 5 = 0$  intersect at the points P and Q.

Which of the following equations will give the  $y$ -coordinates of P and Q ?

- A  $5y^2 + 5y - 10 = 0$
- B  $y^2 - 5y - 10 = 0$
- C  $2y^2 - 9y - 5 = 0$
- D  $y^2 - 13y - 30 = 0$



**193**

P is the point  $(4, 3, -1)$  and Q is  $(-2, -1, 3)$ .  
What is the length of PQ ?

- A  $\sqrt{6}$
- B  $\sqrt{12}$
- C  $\sqrt{24}$
- D  $\sqrt{68}$

**194**

P, Q and R have coordinates  $(1, 2, -1)$ ,  $(4, 3, 0)$  and  $(1, 4, 2)$  respectively.  
If  $\overrightarrow{RS} = 3\overrightarrow{PQ}$ , what are the coordinates of S ?

- A  $(10, 7, 5)$
- B  $(19, 19, -1)$
- C  $(-10, -7, -5)$
- D  $(-8, -5, -1)$

**195**

$\mathbf{a}$  has components  $\begin{pmatrix} \frac{6}{7} \\ -\frac{3}{7} \\ z \end{pmatrix}$ . If  $\mathbf{a}$  is a unit vector find the values of  $z$ .

- A  $\pm \frac{4}{7}$
- B  $\pm \frac{3}{7}$
- C  $\pm \frac{2}{7}$
- D  $\pm \frac{1}{7}$

**196**

Vectors  $\mathbf{u} = 2\mathbf{i} - 4\mathbf{j} - 8\mathbf{k}$  and  $\mathbf{v} = 5\mathbf{i} + p\mathbf{j} - 20\mathbf{k}$  are parallel.  
What is the value of  $p$ ?

- A 10
- B -1
- C -7
- D -10

197

$\mathbf{u}$  and  $\mathbf{v}$  have components  $\begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$  and  $\begin{pmatrix} 2 \\ -4 \\ 0 \end{pmatrix}$  respectively.

If  $3(\mathbf{x} + \mathbf{u}) = 2\mathbf{v} + \mathbf{x}$ , find the components of  $\mathbf{x}$ .

A  $\begin{pmatrix} 1 \\ -8 \\ -3 \end{pmatrix}$

B  $\begin{pmatrix} \frac{3}{2} \\ -4 \\ -\frac{1}{2} \end{pmatrix}$

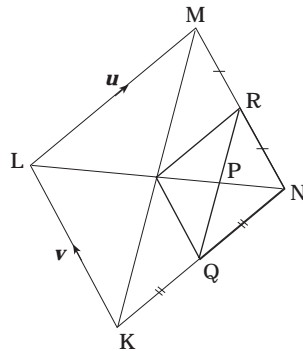
C  $\begin{pmatrix} \frac{1}{2} \\ -4 \\ -\frac{1}{2} \end{pmatrix}$

D  $\begin{pmatrix} \frac{1}{2} \\ -4 \\ -\frac{3}{2} \end{pmatrix}$

198

KLMN is a parallelogram as shown in the diagram.

Q is the midpoint of KN and R is the midpoint of MN.



If  $\overrightarrow{LM} = \mathbf{u}$  and  $\overrightarrow{KL} = \mathbf{v}$ , find an expression for  $\overrightarrow{NP}$ .

A  $\overrightarrow{NP} = -\frac{1}{4}(\mathbf{u} + \mathbf{v})$

B  $\overrightarrow{NP} = \frac{1}{4}(\mathbf{v} - \mathbf{u})$

C  $\overrightarrow{NP} = \frac{1}{4}(\mathbf{u} - \mathbf{v})$

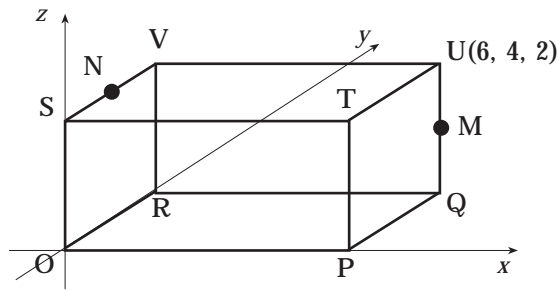
D  $\overrightarrow{NP} = \frac{1}{4}(\mathbf{u} + \mathbf{v})$

199

The diagram shows a cuboid OPQRSTUV.

The coordinates of U are (6, 4, 2).

M and N are the midpoints of UQ and SV .



What are the components of  $\overrightarrow{MN}$  ?

A  $\begin{pmatrix} 6 \\ 2 \\ -1 \end{pmatrix}$

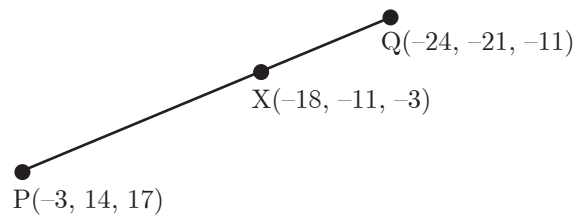
B  $\begin{pmatrix} -6 \\ 1 \\ -2 \end{pmatrix}$

C  $\begin{pmatrix} 1 \\ -6 \\ -2 \end{pmatrix}$

D  $\begin{pmatrix} -6 \\ -2 \\ -1 \end{pmatrix}$

200

P, X and Q are collinear points with coordinates as shown in the diagram.



In what ratio does X divide PQ ?

A 5 : 2

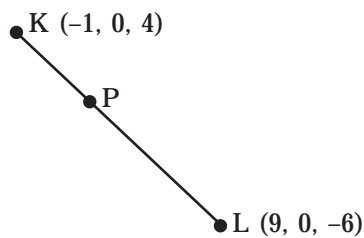
B 5 : 7

C 2 : 7

D 2 : 5

201

K and L have coordinates  $(-1, 0, 4)$  and  $(9, 0, -6)$  as shown in the diagram.  
P divides KL in the ratio 2:3.

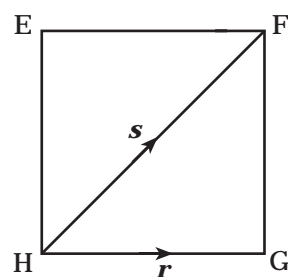


What are the coordinates of P?

- A  $(5, 0, -2)$
- B  $(3, 0, 0)$
- C  $\left(\frac{16}{5}, 0, -\frac{4}{5}\right)$
- D  $(4, 0, -4)$

202

EFGH is a square of side 1 unit as shown in the diagram.  
 $\overrightarrow{HG} = \mathbf{r}$  and  $\overrightarrow{HF} = \mathbf{s}$ .



What is the value of  $\mathbf{r} \cdot \mathbf{s}$ ?

- A  $\frac{1}{\sqrt{2}}$
- B  $\sqrt{\frac{2}{3}}$
- C 1
- D 2

203

Vectors  $\mathbf{u}$  and  $\mathbf{v}$  are defined by  $\mathbf{u} = \begin{pmatrix} g \\ 3 \\ 2 \end{pmatrix}$  and  $\mathbf{v} = \begin{pmatrix} 5 \\ -4 \\ -g \end{pmatrix}$ .

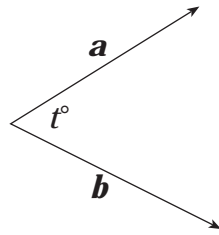
If  $\mathbf{u}$  and  $\mathbf{v}$  are perpendicular, what is the value of  $g$ ?

- A 4
- B  $\frac{13}{3}$
- C -4
- D  $\frac{12}{7}$

204

The diagram shows two vectors,  $\mathbf{a}$  and  $\mathbf{b}$ , inclined at angle of  $t^\circ$ .

$$|\mathbf{a}| = |\mathbf{b}| = \sqrt{2} \text{ units and } \mathbf{a} \cdot \mathbf{b} = \sqrt{3}$$

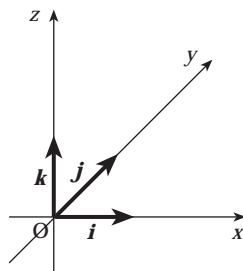


What is the value of  $t$  ?

- A 30
- B 45
- C 60
- D 90

205

The diagram shows three unit vectors,  $\mathbf{i}$ ,  $\mathbf{j}$  and  $\mathbf{k}$ .



What is the value of  $\mathbf{i} \cdot (\mathbf{i} + 2\mathbf{j} - \mathbf{k})$  ?

- A 0
- B 1
- C 2
- D 4

206

For  $0 \leq x \leq \pi$ , the maximum value of  $\sin\left(2x - \frac{\pi}{4}\right)$  occurs when  $x = t$ .

What is the value of  $t$  ?

- A  $\frac{\pi}{8}$
- B  $\frac{3\pi}{8}$
- C  $\frac{\pi}{2}$
- D  $\frac{3\pi}{4}$

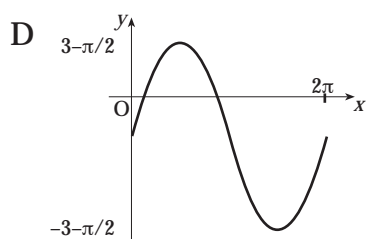
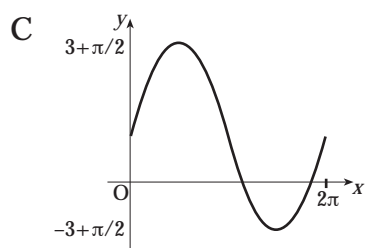
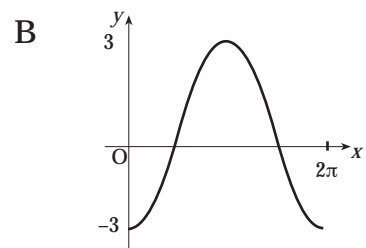
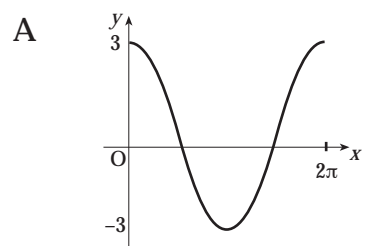
207

What is the exact value of  $\sin\left(\frac{7\pi}{6}\right) - \sin\left(\frac{5\pi}{6}\right)$  ?

- A  $-1$
- B  $-\sqrt{3}$
- C  $\frac{\sqrt{3}}{2}$
- D  $0$

208

Which of the sketches below shows the graph with equation  $y = 3\sin\left(x - \frac{\pi}{2}\right)$ ?



**209**

A minimum value of  $1 - \cos\left(x - \frac{\pi}{3}\right)$  occurs when  $x = t$ , where  $0 \leq t \leq \frac{3\pi}{2}$ .

What is the value of  $t$  ?

- A 0
- B  $\frac{\pi}{3}$
- C  $\pi$
- D  $\frac{4\pi}{3}$

**210**

What is the solution to the equation  $2\sin^2 x = 1$

in the interval  $0 \leq x < \frac{\pi}{2}$  ?

- A  $\frac{\pi}{4}$
- B  $\sqrt{\frac{\pi}{6}}$
- C  $\frac{\pi}{6}$
- D  $\frac{\pi}{3}$

**211**

What is the value of  $\cos(45^\circ - 30^\circ)$  ?

- A  $\frac{\sqrt{3}-1}{2\sqrt{2}}$
- B  $\frac{\sqrt{3}+1}{2\sqrt{2}}$
- C  $\frac{\sqrt{3}-1}{2}$
- D  $\frac{\sqrt{2}-\sqrt{3}}{2}$

**212**

Given that  $\sin x = k$ , where  $0 \leq x < \frac{\pi}{2}$ , find an expression for  $\sin 2x$  .

- A  $\sin 2x = 2k$
- B  $\sin 2x = 2k\sqrt{1-k^2}$
- C  $\sin 2x = 2k\sqrt{1+k^2}$
- D  $\sin 2x = 2k^2 - 1$

**213**

$k$  and  $a$  are given by  $k \cos a^\circ = \sqrt{3}$  and  $k \sin a^\circ = 1$   
 where  $k > 0$  and  $0 \leq a < 90$ .

What are the values of  $k$  and  $a$  ?

	$k$	$a$
A	4	60
B	4	30
C	2	60
D	2	30

**214**

$2 \sin x - 3 \cos x$  is expressed in the form  $k \cos x \cos a + k \sin x \sin a$   
 where  $k$  and  $a$  are constants and  $0 \leq a \leq 2\pi$ .

What is the value of  $\tan a$  ?

- A  $-\frac{3}{2}$
- B  $-\frac{2}{3}$
- C  $\frac{2}{3}$
- D  $\frac{3}{2}$