

# K J Somaiya College of Engineering, Mumbai-77

(Autonomous College Affiliated to University of Mumbai)

Batch: Roll No.: 16010221025  
Experiment / assignment / tutorial No. 6  
Grade: AA / AB / BB / BC / CC / CD / DD

Signature of the Staff In-charge with date

**Title:** Coplanar Concurrent Force System

**CO3** Analyze applications of equilibrium using free body diagram

## Objective

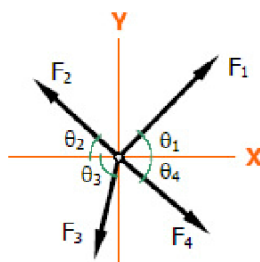
To verify the condition of equilibrium of a coplanar concurrent forces .

## Theory

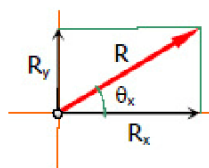
Resultant of a force system is a force or a couple that will have the same effect to the body, both in translation and rotation, if all the forces are removed and replaced by the resultant.

### **Resultant of Coplanar Concurrent Force System**

The lines of action of each force in coplanar concurrent force system are on the same plane. All of these forces meet at a common point, thus concurrent. In x-y plane, the resultant can be found by the following formulas:



=



$$\begin{aligned} R_x &= \sum F_x \\ R_y &= \sum F_y \\ R &= \sqrt{R_x^2 + R_y^2} \\ \tan \theta_x &= \frac{R_y}{R_x} \end{aligned}$$

## AIM:

To verify the condition of equilibrium of a coplanar concurrent system of forces and analyse the error if any.

**Department of Mechanical Engineering**

## K J Somaiya College of Engineering, Mumbai-77

(Autonomous College Affiliated to University of Mumbai)

### **APPARATUS:**

Universal force table, Weights and Spirit level.

### **Setup Diagram:**



### **PROCEDURE:**

1. Place the Universal force table on the firm platform.
2. Make the circular disc in horizontal position with the help of foot screws.
3. Put slotted weights to each hanger to these ends of strings passing over the pulleys.
4. Note the sum of slotted weights in each hanger and weight of hangers as five forces  $F_1$ ,  $F_2$ ,  $F_3$ ,  $F_4$  and  $F_5$ .
5. Measure the angles included between the two adjacent pulleys and note them as  $\theta_1$  to  $\theta_5$ .
6. Record these observations.

**Department of Mechanical Engineering**

## K J Somaiya College of Engineering, Mumbai-77

(Autonomous College Affiliated to University of Mumbai)

7. Repeat by changing any one or two pulley positions and take three sets of readings.
8. Draw force polygon.

### OBSERVATION TABLE:

Sr No	Forces					Angles					$\Sigma F_x$	$\Sigma F_y$
	F1	F2	F3	F4	F5	$\theta_1$	$\theta_2$	$\theta_3$	$\theta_4$	$\theta_5$		
1	3.43	1.96	3.43	2.94	2.45	0	65	142	213	292	0.007	0.015
2	2.5	2	2.5	2.5	3	0	65	129	199	280	-0.071	-0.012
3	2.5	2	2.5	3	2	0	65	143	214	292	-0.389	-0.215

### CALCULATION:

III reading :

$F_1 = 2.5 \text{ N}$	$\theta_1 = 0^\circ$
$F_2 = 2 \text{ N}$	$\theta_2 = 65^\circ$
$F_3 = 2.5 \text{ N}$	$\theta_3 = 143^\circ$
$F_4 = 3 \text{ N}$	$\theta_4 = 214^\circ$
$F_5 = 2 \text{ N}$	$\theta_5 = 292^\circ$

$$\therefore \Sigma F_x = F_1 \cos \theta_1 + F_2 \cos \theta_2 + F_3 \cos \theta_3 + F_4 \cos \theta_4 + F_5 \cos \theta_5$$

$$= 2.5(1) + 2 \cos 65^\circ + 2.5 \cos 143^\circ + 3 \cos 214^\circ + 2 \cos 292^\circ$$

$$\boxed{\Sigma F_x = -0.389 \text{ N}}$$
  

$$\therefore \Sigma F_y = F_1 \sin \theta_1 + F_2 \sin \theta_2 + F_3 \sin \theta_3 + F_4 \sin \theta_4 + F_5 \sin \theta_5$$

$$= 2.5 \sin 0^\circ + 2 \sin 65^\circ + 2.5 \sin 143^\circ + 3 \sin 214^\circ + 2 \sin 292^\circ$$

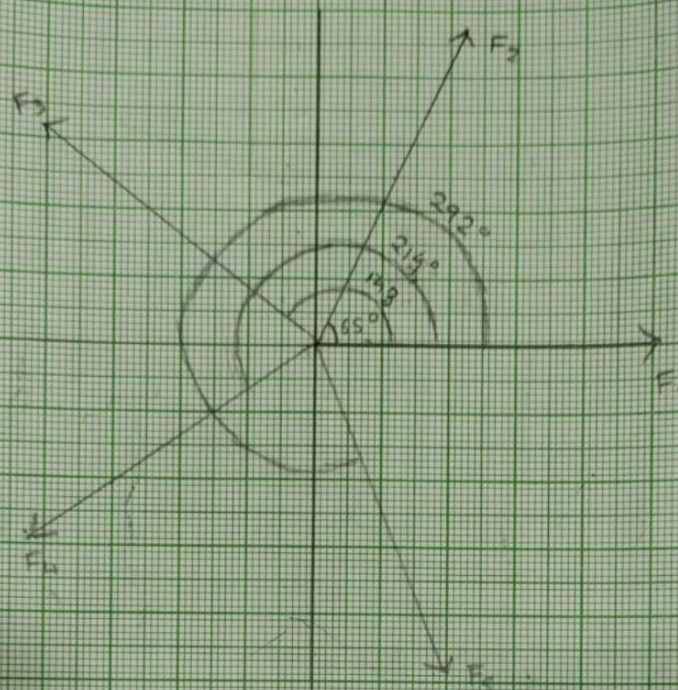
$$\boxed{\Sigma F_y = -0.215 \text{ N}}$$
  

$$\therefore R = \sqrt{\Sigma F_x^2 + \Sigma F_y^2} = \sqrt{(-0.389)^2 + (-0.215)^2}$$

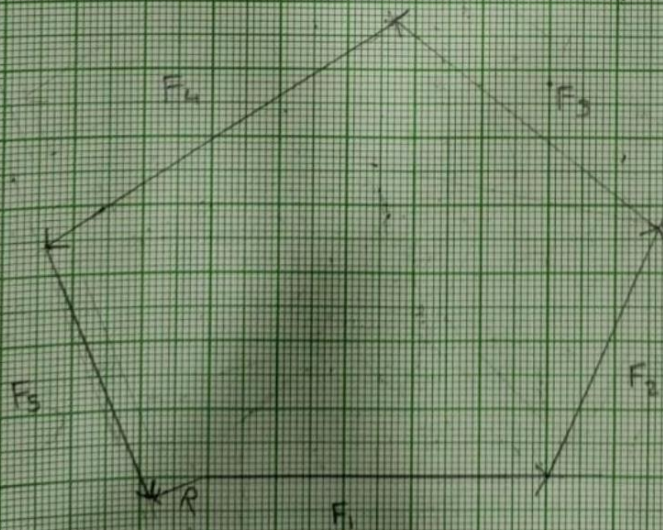
$$\boxed{R = 0.444 \text{ N}}$$

$$\theta = \tan^{-1} \left( \frac{-0.215}{-0.389} \right) = \boxed{208.8^\circ}$$





Scale :  
 $0.5 \text{ N} = 1 \text{ cm}$



Graph calculations:

$$\sum F_y = -0.4 \quad \sum F_x = -0.15$$

$$R = \sqrt{\sum F_x^2 + \sum F_y^2} = \boxed{0.427}$$

$$\theta = \tan^{-1} \left( \frac{-0.15}{-0.4} \right) = 180 + 20.55 = \boxed{200.55^\circ}$$

## **RESULT:**

**For Set 3:**

### **Analytical Results:**

$$\begin{aligned}\sum F_x &= -0.389 \text{ N} \\ \sum F_y &= -0.215 \text{ N} \\ R &= 0.444 \text{ N} \\ \theta &= 208.8^\circ\end{aligned}$$

### **Graphical Results:**

$$\begin{aligned}\sum F_x &= -0.4 \text{ N} \\ \sum F_y &= -0.15 \text{ N} \\ R &= 0.427 \text{ N} \\ \theta &= 200.55^\circ\end{aligned}$$

## **CONCLUSION:**

We experimented the condition of equilibrium of a coplanar concurrent system of forces.

**Signature of faculty in-charge**

**Department of Mechanical Engineering**