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# **3RD SEM** **DMS EL**

CALCULATION OF NO. OF ONTO FUNCTIONS





# INTRODUCTION

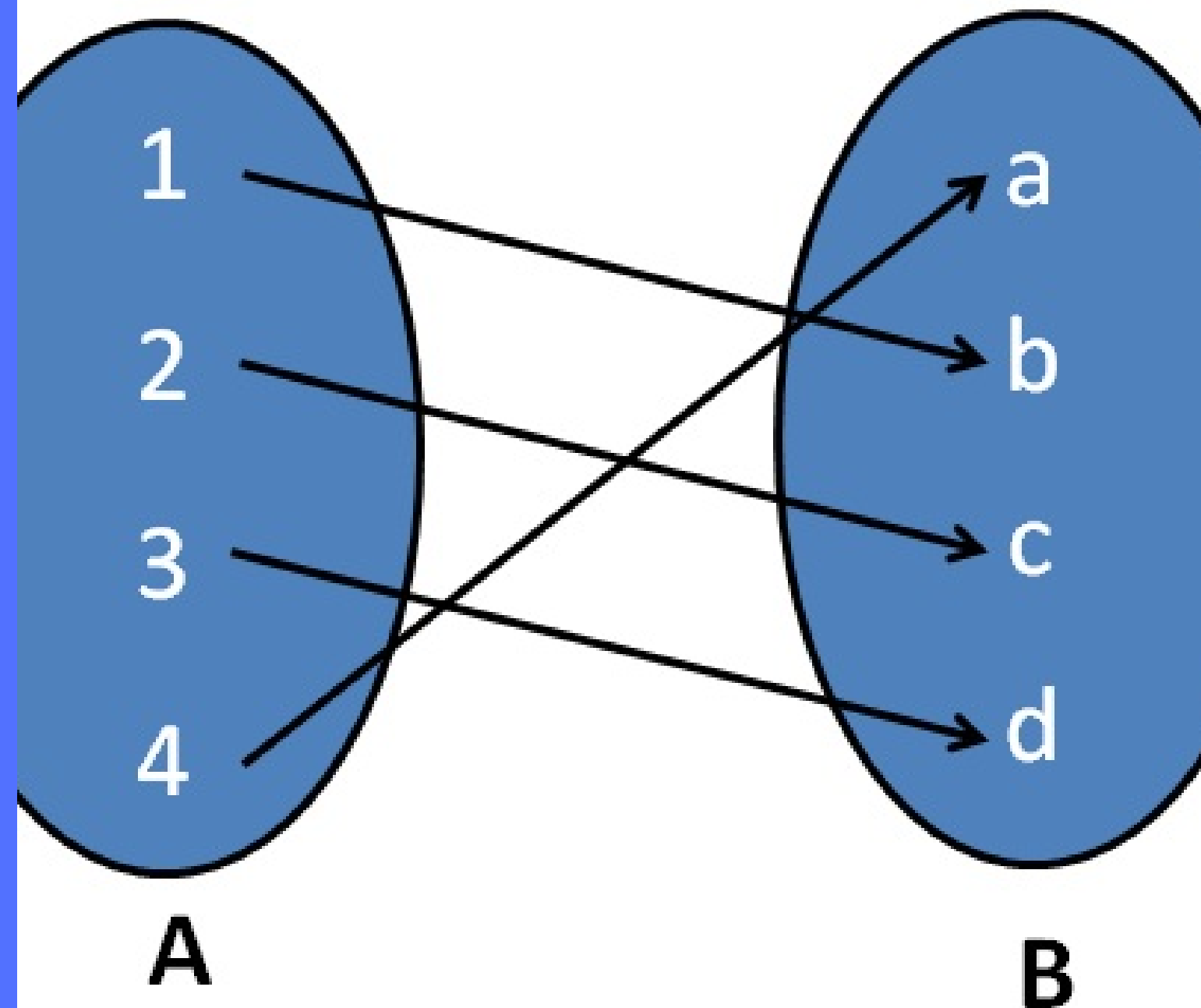
WHAT IS AN ONTO FUNCTION?



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# DEFINITION

A SURJECTIVE (ONTO) FUNCTION IS A FUNCTION  $F$  SUCH THAT EVERY ELEMENT  $Y$  CAN BE MAPPED FROM ELEMENT  $X$  SO THAT  $F(X) = Y$ .



- Range = Co-Domain
- Every *element of the function's codomain is the image of at least one element of its domain.*

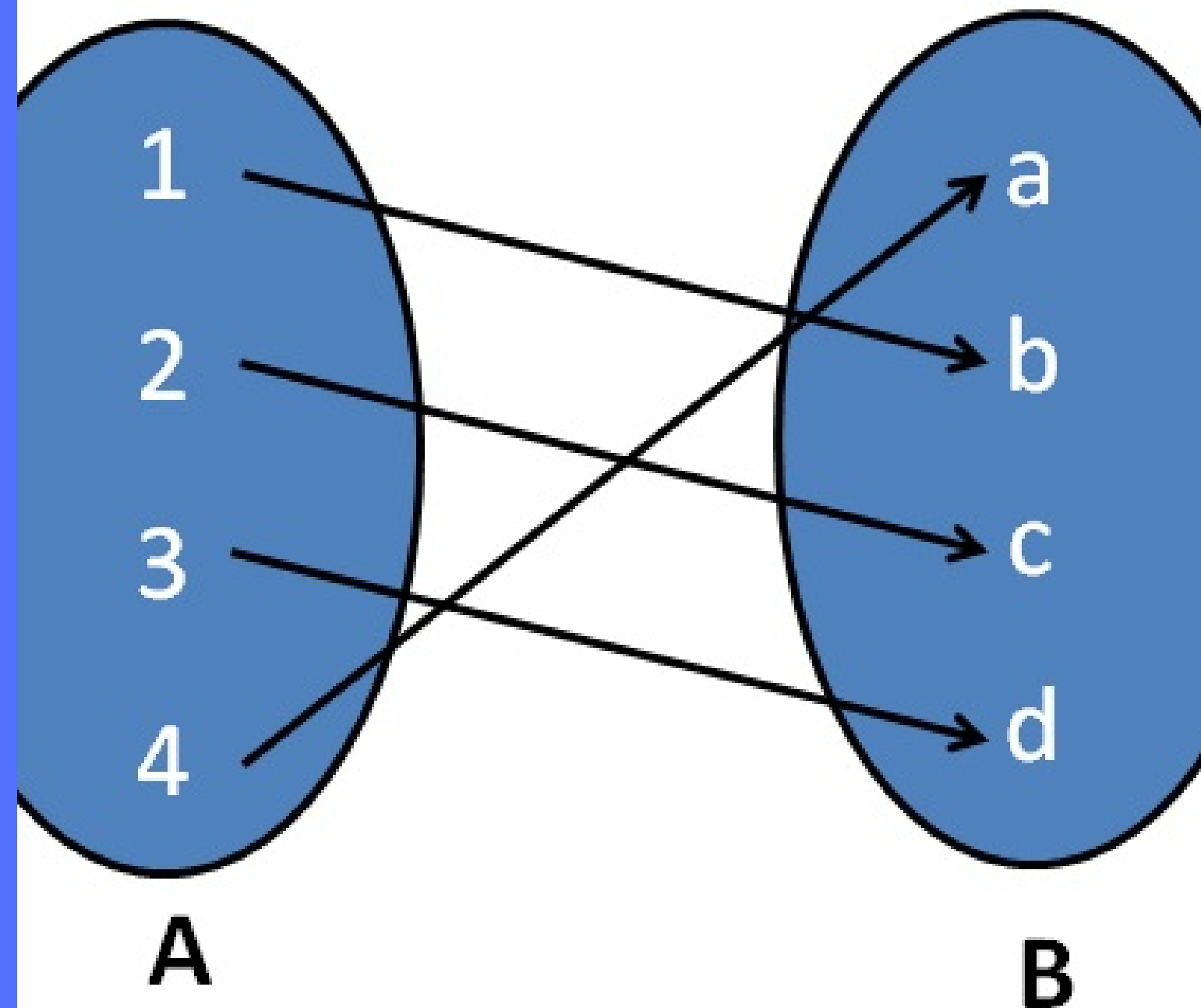
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# FORMULA

IF A SET A HAS M ELEMENTS AND SET B HAS N ELEMENTS, THEN THE NUMBER OF ONTO FUNCTIONS FROM A TO B =

$$N^M - {}^NC_1(N-1)^M + {}^NC_2(N-2)^M - {}^NC_3(N-3)^M + \dots - {}^NC_{N-1}(1)^M$$

(M ≥ N ONLY)



- Range = Co-Domain
- Every *element of the function's codomain is the image of at least one element of its domain.*

# CODE

*PYTHON PROGRAM EXPLANATION*



1

## ITERTOOLS LIBRARY

*To generate combinations with repetitions for the set B.*

2

## FACTORIAL & C(N, R) FUNCTIONS

*To find the number of onto functions from set A to set B.*

```
from itertools import product
```

```
def fact(n):  
    """Returns the factorial of n.  
    """
```

```
    if n <= 1:  
        return 1  
    return n * fact(n - 1)
```

```
def nCr(n, r):  
    """Returns C(n, r)  
    """  
  
    return (fact(n) / (fact(r) * fact(n - r)))
```

1

## CHECKING M AND N

First checks if the no. of elements in set A ( $=m$ ) is greater than equal to no. of elements in set B ( $=n$ ), i.e.,  $m \geq n$ .

2

## COMPUTING NO. OF ONTO FUNCTIONS

The no. of onto functions is computed by incorporating the formula showed before and storing the value in **num\_onto** variable.

3

## STORE ALL ONTO FUNCTIONS

All possible onto functions are stored in a list named **onto** which is calculated using **product** function from the **itertools** library.

```
def calculate_onto(A, B):
    """Calculate the number of onto functions from A to B.
    """

    # Calculate the number of onto functions from A to B
    m = len(A)
    n = len(B)
    if m < n:
        print("There are no onto functions from A to B.")
        return 0, []
    num_onto = 0
    for k in range(0, n): # 0 to n-1
        num_onto += ((-1)**k) * nCr(n, n-k) * ((n-k)**m)

    # List all of the onto functions from A to B
    onto = []
    for b in product(B, repeat=m): # Combinations with repetition
        if len(set(b)) == n: # b contains all elements of B (range = co-domain)
            onto.append(dict(zip(A, b)))

    # product here generates all possible combinations
    # of elements in set B with length m.
    # Eg: B = {1, 2}, m = 3
    # product(B, repeat=m)
    # = {(1, 1, 1), (1, 1, 2), (1, 2, 1), (1, 2, 2),
    # (2, 1, 1), (2, 1, 2), (2, 2, 1), (2, 2, 2)}

    return int(num_onto), onto
```

# EXAMPLES

## Default

FOR THE SETS:

$S = \{1, 2, 3, 4\}$

$T = \{'A', 'B', 'C'\}$

Number of onto functions from A to B:  
All of the onto functions from A to B:

```
1: {1: 'b', 2: 'b', 3: 'c', 4: 'a'}
2: {1: 'b', 2: 'b', 3: 'a', 4: 'c'}
3: {1: 'b', 2: 'c', 3: 'b', 4: 'a'}
4: {1: 'b', 2: 'c', 3: 'c', 4: 'a'}
5: {1: 'b', 2: 'c', 3: 'a', 4: 'b'}
6: {1: 'b', 2: 'c', 3: 'a', 4: 'c'}
7: {1: 'b', 2: 'c', 3: 'a', 4: 'a'}
8: {1: 'b', 2: 'a', 3: 'b', 4: 'c'}
9: {1: 'b', 2: 'a', 3: 'c', 4: 'b'}
10: {1: 'b', 2: 'a', 3: 'c', 4: 'c'}
11: {1: 'b', 2: 'a', 3: 'c', 4: 'a'}
12: {1: 'b', 2: 'a', 3: 'a', 4: 'c'}
13: {1: 'c', 2: 'b', 3: 'b', 4: 'a'}
14: {1: 'c', 2: 'b', 3: 'c', 4: 'a'}
15: {1: 'c', 2: 'b', 3: 'a', 4: 'b'}
16: {1: 'c', 2: 'b', 3: 'a', 4: 'c'}
17: {1: 'c', 2: 'b', 3: 'a', 4: 'a'}
18: {1: 'c', 2: 'c', 3: 'b', 4: 'a'}
19: {1: 'c', 2: 'c', 3: 'a', 4: 'b'}
20: {1: 'c', 2: 'a', 3: 'b', 4: 'b'}
21: {1: 'c', 2: 'a', 3: 'b', 4: 'c'}
22: {1: 'c', 2: 'a', 3: 'b', 4: 'a'}
23: {1: 'c', 2: 'a', 3: 'c', 4: 'b'}
24: {1: 'c', 2: 'a', 3: 'a', 4: 'b'}
25: {1: 'a', 2: 'b', 3: 'b', 4: 'c'}
26: {1: 'a', 2: 'b', 3: 'c', 4: 'b'}
27: {1: 'a', 2: 'b', 3: 'c', 4: 'c'}
28: {1: 'a', 2: 'b', 3: 'c', 4: 'a'}
29: {1: 'a', 2: 'b', 3: 'a', 4: 'c'}
30: {1: 'a', 2: 'c', 3: 'b', 4: 'b'}
31: {1: 'a', 2: 'c', 3: 'b', 4: 'c'}
32: {1: 'a', 2: 'c', 3: 'b', 4: 'a'}
33: {1: 'a', 2: 'c', 3: 'c', 4: 'b'}
34: {1: 'a', 2: 'c', 3: 'a', 4: 'b'}
35: {1: 'a', 2: 'a', 3: 'b', 4: 'c'}
36: {1: 'a', 2: 'a', 3: 'c', 4: 'b'}
```

## Custom

$S = \{1, 2, 3\}$

$T = \{A, B\}$

Try with your own sets of integers!

Enter a set A of integers separated by spaces:

1 2 3

Enter a set B of characters separated by spaces:

a b

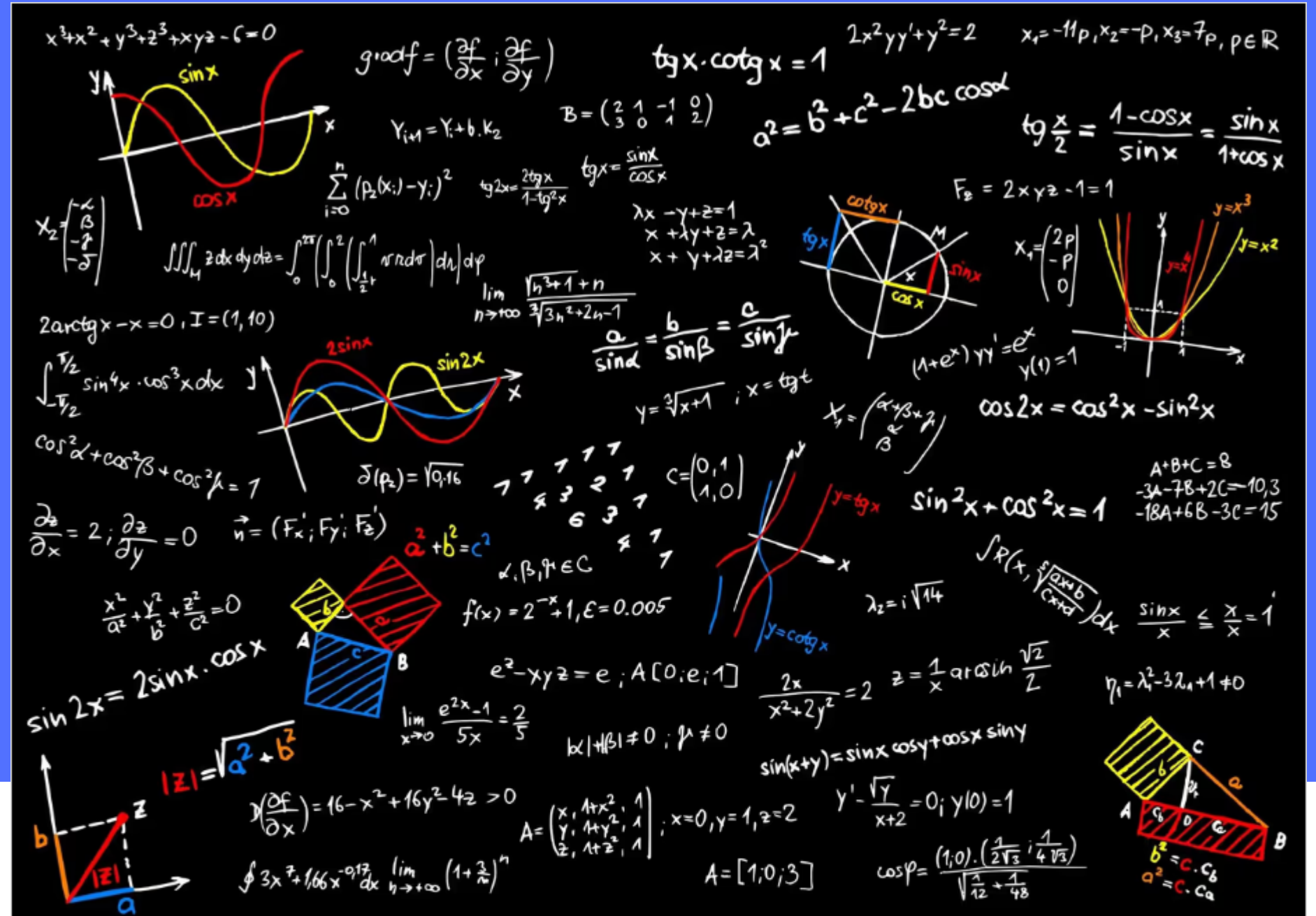
Number of onto functions from A to B: 6

All of the onto functions from A to B:

```
1: {1: 'b', 2: 'b', 3: 'a'}
2: {1: 'b', 2: 'a', 3: 'b'}
3: {1: 'b', 2: 'a', 3: 'a'}
4: {1: 'a', 2: 'b', 3: 'b'}
5: {1: 'a', 2: 'b', 3: 'a'}
6: {1: 'a', 2: 'a', 3: 'b'}
```



# CODEBASE LINK



### Hardvan/DMS-EL-Onto-Functions

Contribute to Hardvan/DMS-EL-Onto-Functions development by creating an account on GitHub.



## LINK TO THE CODE FILE



**THANK YOU**