What does the sum of integers from 1 to n mean?#

Natural numbers are positive numbers starting from 1. These can be written as:

```
1, 2, 3, 4, 5, 6, 7, 8, 9, 10...
```

We want to write a program that takes a particular number and sums up all the numbers from 1 up until that number.

The illustration below explains the concept to help you understand.

```
input sum (function)

1 of 3
```

The sum of all numbers up to a particular number is equal to the sum of that number and the sum of all the numbers before it. It can be seen as follows:

```
\sum_{i=1}^{5} i
= 5 + \sum_{i=1}^{4} i
= 5 + 4 + \sum_{i=1}^{3}
= 5 + 4 + 3 + \sum_{i=1}^{2}
.
.
.
.
.
.
```

$\sum_{i=1}^n i$

Generic Mathematical Notation

class SummationClass {

Implementing the Code

```
public static int sumAll(int num) {
    if (num == 1) {
        return num;
    }
    else {
        return num + sumAll(num-1);
    }
}

public static void main( String args[] ) {
    int input = 5;
    int sum = sumAll(input);
    System.out.println("The sum of integers from 1 to " + input + " is: " + sum);
}

Run

Save Reset []

Understanding the Code #
```

an explanation of the above code:

Inside the main method, we have defined the integer variable input on line 13. The code calculates the

In the code above, the method sumAll is a recursive method, since it calls itself in the function body. Below is

sum of all the numbers up to the value stored in the input. The method sumAll is called on line 14 and its return value is stored in an int variable, which is

Recursive Method

Base Case

- defined as sum.
 The System.out.println command on line 15 prints the answer when the sumAll method is called.
- The return type of this method is int since the sum of all the integers will be an integer.
- The base case of the method is defined on **line 4** where the method will terminate and return num if the num<=1 condition is met. This due to the fact that, if the num is 1, there are no integers less than 1; hence

the sum is 1. All the numbers including 0 and below are returned because they are considered an invalid positive integer input.

• This method takes an integer, num, as the input argument.

If the base case condition does not compute as true, the method enters the else block where it makes a recursive call.
 This recursive call takes an input argument of num-1. The value returned from sumAll(num-1) is added

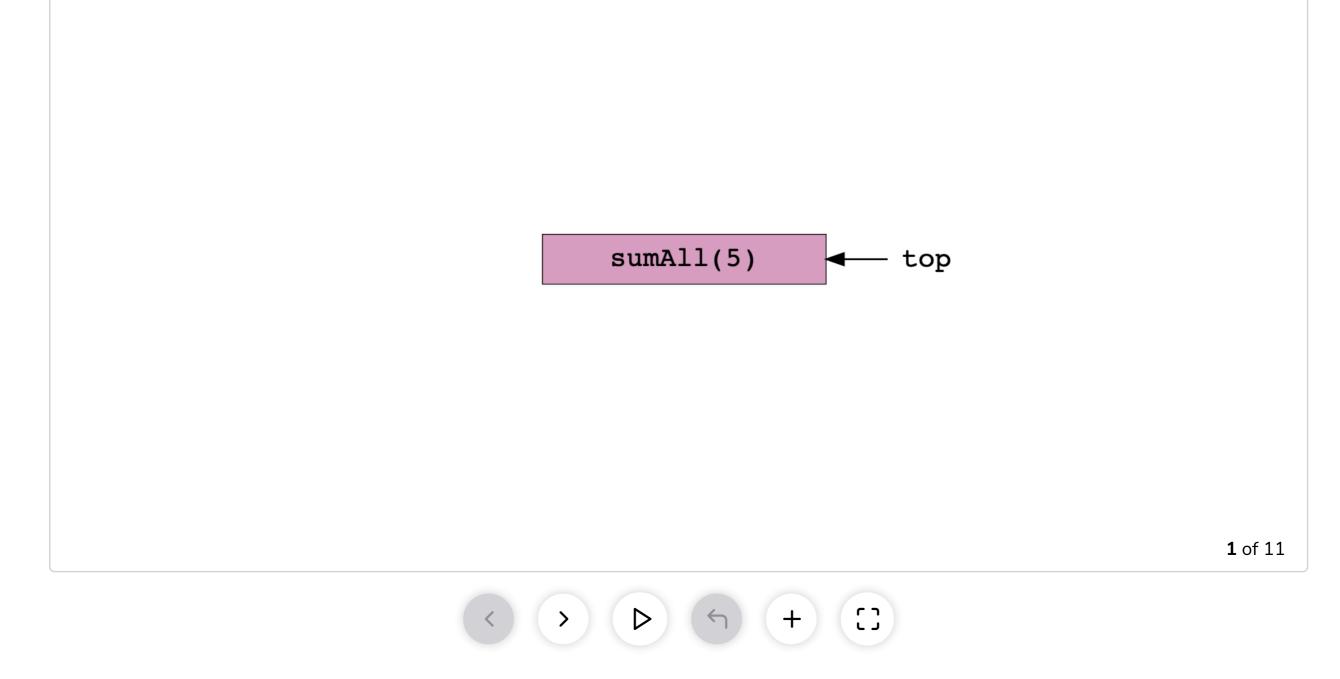
to the input argument, num, and returned. This is because, as discussed above, the sum of the integers up

to that number is equal to the sum of that number and all the numbers below it.

$$n+\sum_{i=1}^{n-1}i$$

Recursive Case

Understanding through a Stack



Now that you have learned about computing the sum of integers from 1 to n using recursion, we will solve another interesting mathematical problem using recursion, computing modulo.