What does the sum of integers from 1 to n mean?# Natural numbers are positive numbers starting from 1. These can be written as: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10...

We want to write a program that takes a particular number and sums up all the numbers from 1 up until that number.

The illustration below explains the concept to help you understand.

sum input-**→**output (function)

3+2+1

output

input

function

2 of 3

input

numbers before it. It can be seen as follows:

 $\sum_{i=1}^{5} i$

 $=5+\sum_{i=1}^4 i$

 $=5+4+\sum_{i=1}^{3}$

 $=5+4+3+\sum_{i=1}^{2}$

=5+4+3+2+1

 $= n + (n-1) + \sum_{i=1}^{n-2}$

 $\sum_{i=1}^{n} i$

 $=n+\sum_{i=1}^{n-1}i$

Generic Mathematical Notation

 $= n + (n-1) + (n-2) \dots + 2 + 1$

class SummationClass {

else {

10

11

12

13

14

15

16

17 }

Run

Implementing the Code

if (num == 1) {

int input = 5;

int sum = sumAll(input);

Understanding the Code

an explanation of the above code:

Driver Method

defined as sum.

Recursive Method

positive integer input.

Recursive Case

recursive call.

 $n+\sum_{i=1}^{n-1}i$

Base Case

return num;

public static int sumAll(int num) {

return num + sumAll(num-1);

public static void main(String args[]) {

sum of all the numbers up to the value stored in the input.

• This method takes an integer, num, as the input argument.

Understanding through a Stack#

calls

calls

calls o

calls

calls

calls

calls

calls

calls (

calls

calls

calls

calls (

calls (

returns 3

returns 6

returns 10 d

returns 15 <

System.out.println("The sum of integers from 1 to " + input + " is: " + sum);

In the code above, the method sumAll is a recursive method, since it calls itself in the function body. Below is

• Inside the main method, we have defined the integer variable input on line 13. The code calculates the

• The method sumAll is called on line 14 and its return value is stored in an int variable, which is

• The System.out.println command on line 15 prints the answer when the sumAll method is called.

• The base case of the method is defined on **line 4** where the method will terminate and return num if the

• If the base case condition does not compute as true, the method enters the else block where it makes a

• This recursive call takes an input argument of num-1. The value returned from sumAll(num-1) is added

sumAll(5)

5+sumAll(4)

sumAll(5)

4+sumAll(3)

5+sumAll(4)

sumAll(5)

3+sumAll(2)

4+sumAll(3)

5+sumAll(4)

sumAll(5)

2+sumAll(1)

3+sumAll(2)

4+sumAll(3)

5+sumAll(4)

sumAll(5)

2+sumAll(1)

3+sumAll(2)

4+sumAll(3)

5+sumAll(4)

sumAll(5)

base case reached

2+sumAll(1)

3+sumAll(2)

4+sumAll(3)

5+sumAll(4)

sumAll(5)

3+sumAll(2)

4+sumAll(3)

5+sumAll(4)

sumAll(5)

4+sumAll(3)

5+sumAll(4)

sumAll(5)

5+sumAll(4)

sumAll(5)

sumAII(5)=15

Now that you have learned about computing the sum of integers from 1 to n using recursion, we will solve

another interesting mathematical problem using recursion, computing modulo.

top

top

top

top

top

top

top

top

top

to that number is equal to the sum of that number and all the numbers below it.

to the input argument, num, and returned. This is because, as discussed above, the sum of the integers up

num<=1 condition is met. This due to the fact that, if the num is 1, there are no integers less than 1; hence</pre>

the sum is 1. All the numbers including 0 and below are returned because they are considered an invalid

• The return type of this method is int since the sum of all the integers will be an integer.

1 of 3

function

The sum of all numbers up to a particular number is equal to the sum of that number and the sum of all the

output

3 of 3

Reset

1 of 11

2 of 11

3 of 11

4 of 11

5 of 11

6 of 11

7 of 11

8 of 11

9 of 11

10 of 11

11 of 11

Save