Problem 2

January 20, 2023

1 Imports

```
[]: import numpy as np
import matplotlib.pyplot as plt
import os
from functools import partial
import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler

plt.rcParams['figure.figsize'] = (10.0, 7.0)
plt.rcParams["font.size"] = 16
plt.rcParams["font.family"] = "Serif"
```

```
[]: DATA_DIR = 'data'
SAVE_DIR = "plots"
```

2 The Problems

The problems we need to solve are:

Housing Price Prediction Problem. Suppose 'Mr. X' is planning to buy a house in Delhi and wants to predict the price of the house given some features like number of bedrooms, number of bathrooms, area of the house, etc. The file 'prob2data.csv' contains a training set of housing prices in Delhi.

- 1. Read the excel file using pandas and perform data cleaning. Remove 1st column 'id' which may not be necessary here. Perform mean normalization of features.
- 2. Write a Python code to perform multivariate regression to predict the house price. Consider all 5 columns ('bedrooms',...,'yr built') as features. Implement batch gradient descent for optimization of weights.
- 3. Predict the house price using the model, for 4 bedrooms, 2.5 bathrooms, 2570 sq. feet area, 2 floors, 2005 yr. built, and state the difference between the model prediction and actual value (Rs. 719000). Show in % error.

2.1 The Approach

We'll be using pandas along with the BatchGradientDescent class which we have implemented in GD.py to solve the problem. For more details on how the class is implemented please see the notebook corresponding to the first problem.

2.1.1 Formulation of the Problem

Here, we give a formal formulation of the problem.

The hypothesis function is:

$$\hat{y} = h(\mathbf{w}, b) = h(\theta) = \mathbf{w}^T \mathbf{x} + b$$

with $\mathbf{w} = [w_1, w_2, w_3, w_4, w_5]$ are the weights and $\mathbf{x} = [x_1, x_2, x_3, x_4, x_5]$ are the input features.

For the loss function, we'll use the mean squared error loss function:

$$J(\hat{y}, \mathbf{y}) = \frac{1}{2m} \sum_{i=1}^{m} (\hat{y}^{(i)} - y^{(i)})^2$$

We are using a factor of 2 instead of 1 to make the derivatives simpler.

The gradient descent algorithm is:

$$\mathbf{w} := \mathbf{w} - \alpha \frac{\partial J}{\partial \mathbf{w}} b := b - \alpha \frac{\partial J}{\partial b}$$

Where α is the learning rate.

The partial derivatives can easily be calculated as:

$$\frac{\partial J}{\partial \mathbf{w}} = \frac{1}{m} \sum_{i=1}^{m} (\hat{y}^{(i)} - y^{(i)}) \mathbf{x}^{(i)} \frac{\partial J}{\partial b} = \frac{1}{m} \sum_{i=1}^{m} (\hat{y}^{(i)} - y^{(i)})$$

We can include the bias term in the input features \mathbf{x} by adding a column of 1's to the input features. This way, the partial derivatives calculated are the same while the update equations are simpler. We have:

$$\mathbf{w} := \mathbf{w} - \alpha \frac{\partial J}{\partial \mathbf{w}}$$

3 Solving the Second Problem

3.1 Problem 2.1

3.1.1 Loading Data

```
[ ]: df = pd.read_csv(os.path.join(DATA_DIR, 'prob2data.csv'))
    df.head()
```

[]:	id	price	bedrooms	bathrooms	sqft_living	floors	<pre>yr_built</pre>
0	7129300520	221900.0	3	1.00	1180	1.0	1955
1	6414100192	538000.0	3	2.25	2570	2.0	1951
2	5631500400	180000.0	2	1.00	770	1.0	1933
3	2487200875	604000.0	4	3.00	1960	1.0	1965
4	1954400510	510000.0	3	2.00	1680	1.0	1987

Let's have a look at the dataframe.

[]: df.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 21613 entries, 0 to 21612

Data columns (total 7 columns):

#	Column	Non-Null Count	Dtype
0	id	21613 non-null	int64
1	price	21613 non-null	float64
2	bedrooms	21613 non-null	int64
3	bathrooms	21613 non-null	float64
4	sqft_living	21613 non-null	int64
5	floors	21613 non-null	float64
6	<pre>yr_built</pre>	21613 non-null	int64

dtypes: float64(3), int64(4)

memory usage: 1.2 MB

So, there are not null values. Also, all the features are integres, so we don't need to do any conversion.

3.1.2 Removing the ID Column

```
[]: df.drop("id", axis=1, inplace=True)
df.head()
```

```
[]:
           price
                  bedrooms
                             bathrooms
                                        sqft_living
                                                      floors
                                                               yr_built
     0 221900.0
                          3
                                  1.00
                                                1180
                                                         1.0
                                                                   1955
     1 538000.0
                          3
                                  2.25
                                                2570
                                                         2.0
                                                                   1951
     2 180000.0
                          2
                                  1.00
                                                 770
                                                         1.0
                                                                   1933
     3 604000.0
                          4
                                  3.00
                                                1960
                                                         1.0
                                                                   1965
     4 510000.0
                          3
                                  2.00
                                                1680
                                                         1.0
                                                                   1987
```

3.1.3 Mean Normalization

Let's seperate the features and the target variable.

```
[]: X = df.drop("price", axis=1).values
y = df["price"].values
```

```
[]: col_means = X.mean()
col_maxes = X.max()
col_mins = X.min()

X = (X - col_means) / (col_maxes - col_mins)
```

3.2 Problem 2.2

We will be using the code written previously to erform multivariate regression to predict the house price. Please see the notebook for problem 1 for more detail.

We will use the BatchGradientDescent class.

Let's create the X feature matrix and y target vector.

We'll be doing train test split (no dev set) to gauge the performance of the model.

```
[]: np.random.seed(42)
    ratio = 0.8
    ids = np.arange(X.shape[0])
    np.random.shuffle(ids)
    train_ids = ids[:int(ratio * X.shape[0])]
    test_ids = ids[int(ratio * X.shape[0]):]
    X_train, y_train = X[train_ids], y[train_ids]
    X_test, y_test = X[test_ids], y[test_ids]
    X_train.shape, X_test.shape, y_train.shape, y_test.shape
```

```
[]: ((17290, 5), (4323, 5), (17290,), (4323,))
```

```
[]: X_train.max(), X_train.min()
```

[]: (0.9400607861153099, -0.059939213884690146)

While training, we'll use the tol feature of the BatchGradientDescent. We'll stop training if the tol becomes less than 10^{-6} .

```
[]: from GD import BatchGradientDescent bgd = BatchGradientDescent(tol=1e-6)
```

```
[]: np.random.seed(42)
bgd.fit(X_train, y_train, learning_rate=0.1, epochs=10000, verbose=0)
```

```
Converged at epoch 7458 ] 74.6%
```

Loss: 35262808669.764084

Let's see what is the mean error made by the model.

```
[]: y_pred_train = bgd.predict(X_train)
y_pred_test = bgd.predict(X_test)
rmse_train = np.sqrt(np.sum(((y_pred_train - y_train)**2))/len(y_train))
rmse_test = np.sqrt(np.sum(((y_pred_test - y_test)**2))/len(y_test))
print(f"Train RMSE: {rmse_train}")
print(f"Test RMSE: {rmse_test}")
```

Train RMSE: 265566.4642507701 Test RMSE: 245161.23828483588

```
[]: print(y.mean())
```

540182.1587933188

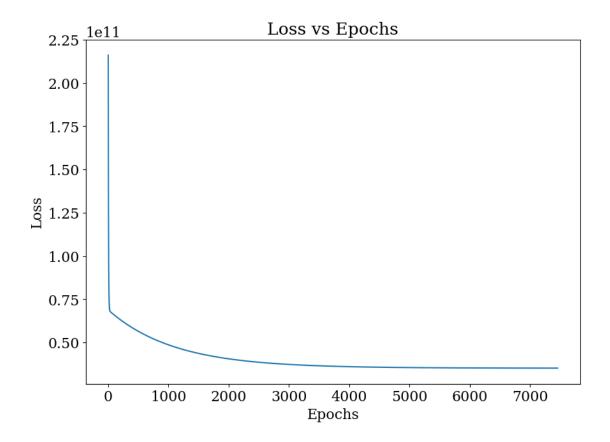
The model is performing good enough. Considering the fact that it assumes a linear relationship between the features and the target variable, it is doing a good job.

Let's also plot the loss with epochs.

```
fig, ax = plt.subplots()

epochs = np.arange(1, len(bgd._losses)+1)
ax.plot(epochs, bgd._losses)

ax.set_xlabel("Epochs")
ax.set_ylabel("Loss")
ax.set_title("Loss vs Epochs")
plt.savefig(os.path.join(SAVE_DIR, "0201.png"));
```



We can see that the loss is not decreasing that much after epoch 1000 or so.

3.3 Problem 2.3

Let's create a vector with the given features:

Correct Price: 719000 => Predicted Price: 675790

Absolute Error: 43210 Percentage Error: 6.01% So, the model gives about 6% error.