

## Clustering with k-Means

**Objective:** Improve and evaluate the k-Means clustering implementation.

### 1. Dataset Preparation:

- Generate a synthetic dataset using **make\_blobs** from **sklearn.datasets** with 300 samples, 3 centers, and a cluster standard deviation of 1.5.
- Visualize the generated dataset using matplotlib or seaborn.

### 2. Algorithm Implementation:

- Modify the **random\_centroids** function to ensure that the initial centroids are chosen more effectively. Hint: Consider using the **k-means++** initialization method.
- Implement a function to visualize the clustering results, displaying data points colored according to their cluster assignments and marking centroids.

### 3. Evaluation:

- Run the k-Means algorithm on the generated dataset with  $k=3$  and  $\text{max\_iter}=300$ .
- Plot the SSE (Sum of Squared Errors) over iterations to observe the convergence.
- Evaluate the effect of changing the **k** value on the clustering result and SSE. Test with  $k=2, 3, 4$ , and  $5$ .