## 1- Genetic Algorithm for Continuous Optimization

#### Algorithm

- 1. **Initialize Population**: Randomly generate bitstrings representing potential solutions.
- 2. **Decode**: Convert bitstrings to continuous values within given bounds.
- 3. Evaluate: Calculate the fitness of each solution.
- 4. **Selection**: Select parents using tournament selection.
- 5. **Crossover**: Perform crossover between two parents to produce offspring.
- 6. Mutation: Apply random mutation on offspring.
- 7. **Repeat**: Repeat steps 4-6 for several generations.
- 8. Output: Return the best solution and its fitness.

```
from numpy.random import randint, rand

def objective(x): return sum(i**2 for i in x)

def decode(bounds, n_bits, bitstring):
    largest = 2**n_bits - 1
    return [bounds[i][0] + (int(".join(map(str, bitstring[i*n_bits:(i+1)*n_bits])), 2) / largest) * (bounds[i][1] - bounds[i][0]) for i in range(len(bounds))]

def selection(pop, scores, k=3):
    return min([pop[randint(len(pop))] for _ in range(k)], key=lambda p: scores[pop.index(p)])

def crossover(p1, p2, r_cross):
```

```
if rand() < r cross:
     pt = randint(1, len(p1)-1)
     return [p1[:pt] + p2[pt:], p2[:pt] + p1[pt:]]
  return [p1, p2]
def mutation(bitstring, r mut):
  for i in range(len(bitstring)):
     if rand() < r mut:
        bitstring[i] = 1 - bitstring[i]
def genetic algorithm(objective, bounds, n bits, n iter, n pop,
r cross, r mut):
  pop = [randint(0, 2, n_bits * len(bounds)).tolist() for _ in
range(n pop)]
  best, best eval = pop[0], objective(decode(bounds, n bits, pop[0]))
  for gen in range(n iter):
     scores = [objective(decode(bounds, n bits, p)) for p in pop]
     for i in range(n pop):
        if scores[i] < best_eval:
          best, best eval = pop[i], scores[i]
          print(f">iter {gen}, new best f({decode(bounds, n bits,
pop[i])}) = {scores[i]:.6f}")
     selected = [selection(pop, scores) for in range(n pop)]
     pop = [child for i in range(0, n pop, 2) for child in
crossover(selected[i], selected[i+1], r cross)]
     for c in pop: mutation(c, r_mut)
  return best, best eval
bounds = [[-5.0, 5.0], [-5.0, 5.0]]
```

```
n_iter, n_bits, n_pop, r_cross = 100, 16, 100, 0.9
r_mut = 1.0 / (n_bits * len(bounds))

best, score = genetic_algorithm(objective, bounds, n_bits, n_iter, n_pop, r_cross, r_mut)
decoded_best = decode(bounds, n_bits, best)
print(f"\nGenetic algorithm completed\nBest solution:
{decoded_best}\nFitness score: {score:.5f}")
```

### **OUTPUT**

```
>iter 0, new best f([-2.047271728515625, -1.97540283203125]) = 8.093538

>iter 0, new best f([0.15594482421875, -1.57745361328125]) = 2.512679

>iter 0, new best f([-0.55755615234375, -1.076812744140625]) = 1.470395
```

\_ \_

Genetic algorithm completed

Best solution: [-0.000152587890625, 0.0]

Fitness score: 0.00000

## 2 - Genetic Algorithm for Binary Optimization:

### Algorithm:

- 1. Initialize a population of random binary strings.
- 2. Evaluate fitness for each individual.
- 3. For each generation:
  - Select parents using tournament selection.
  - Crossover parents to produce offspring.
  - Mutate offspring.
  - o Evaluate new population's fitness.
- 4. Replace old population with new offspring.
- 5. Return the best solution and its fitness.

```
from numpy.random import randint, rand

def onemax(x): return -sum(x)

def selection(pop, scores, k=3):
    return min([pop[randint(len(pop))] for _ in range(k)], key=lambda p:
    scores[pop.index(p)])

def crossover(p1, p2, r_cross):
    if rand() < r_cross:
        pt = randint(1, len(p1)-1)
        return [p1[:pt] + p2[pt:], p2[:pt] + p1[pt:]]
    return [p1, p2]

def mutation(bitstring, r_mut):
    for i in range(len(bitstring)):
        if rand() < r_mut:
```

```
def genetic algorithm(objective, n bits, n iter, n pop, r cross, r mut):
  pop = [randint(0, 2, n bits).tolist() for in range(n pop)]
  best, best eval = pop[0], objective(pop[0])
  for gen in range(n iter):
     scores = [objective(c) for c in pop]
     for i in range(n pop):
       if scores[i] < best_eval:
          best, best eval = pop[i], scores[i]
          print(f">iter {gen}, new best f({pop[i]}) = {scores[i]:.3f}")
     selected = [selection(pop, scores) for in range(n pop)]
     pop = [child for i in range(0, n pop, 2) for child in
crossover(selected[i], selected[i+1], r cross)]
     for c in pop: mutation(c, r mut)
  return best, best eval
n iter, n bits, n pop, r cross = 100, 20, 100, 0.9
r_mut = 1.0 / float(n_bits)
print(f'Starting genetic algorithm\n')
best, score = genetic algorithm(onemax, n bits, n iter, n pop,
r cross, r mut)
print(f'\nGenetic algorithm completed\nBest solution: {best}\nFitness
score: {score:.5f}')
OUTPUT
>iter 0, new best f([1, 1, 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1])
= -14.000
```

bitstring[i] = 1 - bitstring[i]

```
>iter 0, new best f([1, 1, 1, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1])
= -16.000
```

= -17.000

= -18.000

= -19.000

= -20.000

Genetic algorithm completed

Fitness score: -20.00000

## 3 - Simulated Annealing:

### Algorithm:

- 1. Initialize a random starting point within bounds.
- Evaluate the initial solution.
- 3. Repeat for a given number of iterations:
  - Generate a candidate solution by perturbing the current solution.
  - Evaluate the candidate solution.
  - If the candidate is better than the best solution, update the best solution.
  - Calculate the temperature decay.
  - Metropolis criterion: If the candidate solution is worse, accept it based on the temperature and a random probability.
- 4. Return the best solution and its evaluation.

```
from numpy import asarray, exp
from numpy.random import randn, rand, seed

def objective(x): return x[0]**2

def simulated_annealing(objective, bounds, n_iter, step_size, temp):
    best = bounds[:, 0] + rand(len(bounds)) * (bounds[:, 1] - bounds[:, 0])
    best_eval = objective(best)
    curr, curr_eval = best, best_eval
    for i in range(1, n_iter+1):
        candidate = curr + randn(len(bounds)) * step_size
        candidate_eval = objective(candidate)
        if candidate_eval < best_eval:
        best, best_eval = candidate, candidate_eval
```

```
print(f'>iteration {i}: f({best}) = {best_eval:.5f}')
    diff, t = candidate_eval - curr_eval, temp / (i + 1)
    if diff < 0 or rand() < exp(-diff / t):
        curr, curr_eval = candidate, candidate_eval
    return best, best_eval

seed(1)
bounds = asarray([[-5.0, 5.0]])
best, score = simulated_annealing(objective, bounds, 1000, 0.1, 10)
print(f'\nBest solution: {best}\nFitness score: {score:.5f}')</pre>
```

#### OUTPUT

## Starting simulated annealing algorithm

```
>iteration 34: f([-0.78753544]) = 0.62021
>iteration 35: f([-0.76914239]) = 0.59158
>iteration 37: f([-0.68574854]) = 0.47025
>iteration 39: f([-0.64797564]) = 0.41987
>iteration 40: f([-0.58914623]) = 0.34709
>iteration 41: f([-0.55446029]) = 0.30743
>iteration 42: f([-0.41775702]) = 0.17452
>iteration 43: f([-0.35038542]) = 0.12277
>iteration 50: f([-0.15799045]) = 0.02496
```

# Simulated annealing completed

Best solution: [0.00013605]

Fitness score: 0.00000

# 4 - Ant Colony Optimization (ACO)

### Algorithm:

- 1. Initialize: Set initial pheromone levels and distances.
- 2. **Ant Movement**: Each ant picks a city based on pheromone and visibility. Repeat until all cities are visited.
- 3. **Compute Path Length**: Calculate the total distance of the ant's tour.
- 4. **Pheromone Update**: Update pheromone levels based on the tour quality.
- 5. **Iterate**: Repeat for a set number of iterations, finding the best tour.

```
import numpy as np
import networkx as nx
import matplotlib.pyplot as plt

def plot_graph(g, title="", highlight_edges=[]):
    pos = nx.get_node_attributes(g, "pos")
    plt.figure(figsize=(10, 10))
    nx.draw(g, pos=pos, with_labels=True, width=2)
    weights = nx.get_edge_attributes(g, "weight")
    nx.draw_networkx_edge_labels(g, pos, edge_labels=weights, label_pos=0.4)
    nx.draw_networkx_edges(g, pos, edgelist=highlight_edges, edge_color="r", width=3)
    plt.title(title)
    plt.show()

def zero_divide(a, b):
```

```
return np.divide(a, b, out=np.zeros like(a), where=b != 0)
class ACO TSP:
  def init (self, g, n ants=100, alpha=1, beta=5, Q=100, rho=0.6):
     self.q = q
     self.n nodes = len(q.nodes)
     self.visibility = zero divide(np.ones like(nx.to numpy array(g)),
nx.to numpy array(g))
     self.n ants = n ants
     self.alpha = alpha
     self.beta = beta
     self.Q = Q
     self.rho = rho
     self.phe trail = np.ones((self.n nodes, self.n nodes))
  def compute prob(self, visited):
     prob = self.phe trail**self.alpha * self.visibility**self.beta
     prob[:, list(visited)] = 0
     prob sum = prob.sum(-1, keepdims=True)
     return zero divide(prob, prob sum)
  def initialize(self):
     self.ant_pos = np.random.choice(list(self.g.nodes), self.n_ants)
  def path length(self, path):
     edge weights = nx.get edge attributes(self.g, "weight")
     return sum(edge weights[tuple(sorted(edge))] for edge in path)
  def ant tour(self, k):
     current = self.ant pos[k]
     visited = {current}
     path = []
```

```
while len(visited) < self.n nodes:
        prob = self.compute prob(visited)
       current = np.random.choice(self.n nodes, p=prob[current])
       visited.add(current)
        path.append((current, current))
     return path
  def update pheromone(self):
     d_phe_trail = np.zeros_like(self.phe_trail)
     for k in range(self.n ants):
        if len(self.paths[k]) == self.n nodes - 1:
          for i, j in self.paths[k]:
             d_phe_trail[i, j] = d_phe_trail[j, i] = self.Q /
self.path lengths[k]
     self.phe trail = self.rho * self.phe trail + d phe trail
  def run(self, n iter=50):
     self.initialize()
     for in range(n iter):
        self.paths = [self.ant_tour(k) for k in range(self.n_ants)]
       self.path lengths = [self.path length(path) for path in
self.paths]
       self.update_pheromone()
       print(f"Shortest Path Length: {min(self.path lengths)}")
  @property
  def min_path_length(self):
     return min(self.path lengths)
  @property
  def min_path(self):
     return self.paths[np.argmin(self.path_lengths)]
```

```
# Generate random weighted graph (Example)
def generate_random_weighted_graph(n, min_weight=1,
max_weight=10):
    G = nx.complete_graph(n)
    for u, v in G.edges:
        G[u][v]['weight'] = np.random.randint(min_weight, max_weight)
    return G

# Main Execution
np.random.seed(3)
g = generate_random_weighted_graph(10)
plot_graph(g, "Graph for TSP")

aco_tsp = ACO_TSP(g, n_ants=10, alpha=3, beta=5, Q=10, rho=0.1)
aco_tsp.run(n_iter=50)

plot_graph(g, "Shortest Path Found by ACO for TSP",
aco_tsp.min_path)
```

#### **OUTPUT - DIAGRAM**

## 5 - Particle Swarm Optimization (PSO)

Algorithm (Shortened):

- **1.** Initialize the swarm: Randomly initialize n particles with positions and velocities within the given bounds.
- Set hyperparameters: Choose dim (dimensions), minx (lower bound), maxx (upper bound), and optimization constants (w, c1, c2).
- **3.** Main loop: Repeat for max\_iter iterations:
  - For each particle, update its velocity based on its best position and the global best.
  - Update the particle's position and fitness.
  - If the new position is better than its previous best, update its best position.
  - If the particle's best fitness is better than the global best, update the global best.
- **4.** Return the global best position after max\_iter iterations.

```
import random
import sys

def fitness_sphere(position):
    return sum(x**2 for x in position)

class Particle:
    def __init__(self, fitness, dim, minx, maxx, seed):
        self.rnd = random.Random(seed)
        self.position = [self.rnd.uniform(minx, maxx) for _ in range(dim)]
        self.velocity = [self.rnd.uniform(minx, maxx) for _ in range(dim)]
        self.best_pos = self.position[:]
```

```
self.best fitness = fitness(self.position)
  def update velocity(self, global best pos, w, c1, c2):
     r1, r2 = self.rnd.random(), self.rnd.random()
     self.velocity = [
       w * v + c1 * r1 * (bp - p) + c2 * r2 * (qb - p)
       for v, bp, p, gb in zip(self.velocity, self.best pos, self.position,
global best pos)
     ]
  def update position(self, minx, maxx):
     self.position = [max(minx, min(p + v, maxx)) for p, v in
zip(self.position, self.velocity)]
     self.fitness = fitness sphere(self.position)
  def update best(self):
     if self.fitness < self.best_fitness:
        self.best_pos, self.best_fitness = self.position[:], self.fitness
def pso(fitness, max iter, n, dim, minx, maxx):
  w, c1, c2 = 0.729, 1.49445, 1.49445
  swarm = [Particle(fitness, dim, minx, maxx, i) for i in range(n)]
  global_best_pos = min(swarm, key=lambda p:
p.best fitness).best pos
  global best fitness = min(swarm, key=lambda p:
p.best fitness).best fitness
  for Iter in range(max iter):
     if Iter % 10 == 0 and Iter > 1:
        print(f"Iter = {Iter} best fitness = {global best fitness:.3f} Best
position: {[f'{x:.6f}' for x in global best pos]}")
```

```
for particle in swarm:
       particle.update velocity(global best pos, w, c1, c2)
       particle.update position(minx, maxx)
       particle.update best()
       if particle.best_fitness < global_best_fitness:
          global best pos, global best fitness = particle.best pos,
particle.best fitness
  return global best pos
# Driver code
dim, max_iter, num_particles = 3, 100, 50
print("\nStarting PSO algorithm\n")
best position = pso(fitness sphere, max iter, num particles, dim,
-10.0, 10.0)
print("\nPSO completed\n")
print("\nBest solution found:")
print([f"{x:.6f}" for x in best position])
fitnessVal = fitness sphere(best position)
print(f"fitness of best solution = {fitnessVal:.6f}")
OUTPUT
Starting PSO algorithm
Iter = 10 best fitness = 9.700 Best position: ['-2.963075', '-0.926583',
'0.248887'1
Iter = 20 best fitness = 9.700 Best position: ['-2.963075', '-0.926583',
'0.248887'1
Iter = 30 best fitness = 1.100 Best position: ['-0.411780', '-0.854872',
'0.446743']
```

```
Iter = 40 best fitness = 0.873 Best position: ['-0.417564', '-0.829184', '0.105651']
Iter = 50 best fitness = 0.855 Best position: ['-0.405815', '-0.829811', '0.036998']
```

Iter = 60 best fitness = 0.851 Best position: ['-0.403051', '-0.829691', '0.013340']

Iter = 70 best fitness = 0.850 Best position: ['-0.402990', '-0.829325', '0.015951']

Iter = 80 best fitness = 0.850 Best position: ['-0.402987', '-0.829222', '0.020165']

Iter = 90 best fitness = 0.850 Best position: ['-0.402987', '-0.829218', '0.020344']

## PSO completed

Best solution found:

 $\hbox{[$'$-0.402987', $'$-0.829218', $'0.020351']}$ 

fitness of best solution = 0.850415

## 6 - Gray Wolf Optimization (GWO)

### Initialize Population:

• Randomly initialize n grey wolves  $X_i$  within bounds [minx, maxx].

#### **Evaluate Fitness:**

- Calculate fitness for each wolf.
- Identify  $X_{\alpha}$ ,  $X_{\beta}$ , and  $X_{\gamma}$  (the top 3 best wolves).

### **Iterate** for T iterations:

- Update the coefficient  $a=2(1-\frac{t}{T})$ .
- For each wolf:
  - Update position using:

$$X_i = rac{X_lpha + X_eta + X_\gamma}{3} - A imes |C imes X_i - X_{best}|$$

Update fitness and select new best positions if applicable.

**Return**: Best solution ( $X_{\alpha}$ ) after T iterations.

## import random

```
# Sphere fitness function
def fitness_sphere(position):
    return sum(x**2 for x in position)
```

```
# Grey Wolf Optimization (GWO) class

def gwo(fitness, max_iter, n, dim, minx, maxx):

rnd = random.Random(0)

population = [wolf(fitness, dim, minx, maxx, i) for i in range(n)]
```

```
# Sort population based on fitness population.sort(key=lambda w: w.fitness)
```

```
alpha, beta, gamma = population[:3]
  for Iter in range(max iter):
     if Iter % 10 == 0 and Iter > 1:
        print(f"Iter = {Iter}, best fitness = {alpha.fitness:.3f}, Best
position = {[f'{x:.6f}' for x in alpha.position]}")
     a = 2 * (1 - Iter / max iter) # Linearly decrease a
     # Update each wolf's position
     for wolf in population:
       A, C = [a * (2 * rnd.random() - 1) for _ in range(3)], [2 *
rnd.random() for _ in range(3)]
       Xnew = [(alpha.position[i] - A[0] * abs(C[0] * alpha.position[i] -
wolf.position[i]) +
              beta.position[i] - A[1] * abs(C[1] * beta.position[i] -
wolf.position[i]) +
              gamma.position[i] - A[2] * abs(C[2] * gamma.position[i] -
wolf.position[i])) / 3
             for i in range(dim)]
       # Fitness of new position
       fnew = fitness(Xnew)
        if fnew < wolf.fitness:
          wolf.position, wolf.fitness = Xnew, fnew
     # Update alpha, beta, gamma
     population.sort(key=lambda w: w.fitness)
     alpha, beta, gamma = population[:3]
  return alpha.position
```

```
# Wolf class
class wolf:
  def init (self, fitness, dim, minx, maxx, seed):
     self.position = [random.uniform(minx, maxx) for in range(dim)]
     self.fitness = fitness(self.position)
# Driver code
dim = 3
fitness = fitness sphere
num particles = 10
max iter = 50
print('Starting graywolf algorithm\n')
best position = gwo(fitness, max iter, num particles, dim, -10.0, 10.0)
print('\nGraywolf algorithm completed\n')
print("\nBest solution found:")
print([f"{x:.6f}" for x in best position])
print(f"Fitness of best solution = {fitness(best_position):.6f}")
OUTPUT
Starting graywolf algorithm
Iter = 10, best fitness = 0.012, Best position = ['-0.044360', '0.084065',
'-0.050042']
Iter = 20, best fitness = 0.000, Best position = [-0.004129], [-0.005473],
'0.000494'1
Iter = 30, best fitness = 0.000, Best position = ['-0.001647', '0.001247',
'-0.000390'1
Iter = 40, best fitness = 0.000, Best position = [-0.000896], [0.001025],
'-0.000212'1
```

## Graywolf algorithm completed

Best solution found:

['-0.000871', '0.000903', '-0.000206']

Fitness of best solution = 0.000002

### 7 - Tabu Search

### **Shortest Tabu Search Algorithm:**

- 1. Initialize:
  - Generate an initial solution randomly.
  - Calculate its objective value.
- 2. Create Tabu List:
  - Generate all possible swap pairs (neighbors).
- 3. Main Loop:
  - For each iteration:
    - Evaluate neighbors (swap jobs).
    - Select best non-tabu or aspiration move.
    - Update best solution if improvement is found.
- 4. Update Tabu List:
  - Add the selected move to the tabu list with an expiration time.
- 5. **Repeat** until termination (e.g., max iterations or no improvement).
- 6. Output Best Solution.

import pandas as pd import random as rd from itertools import combinations

```
class TS:
  def init (self, path, seed, tabu tenure):
     self.instance dict = pd.read excel(path, names=['Job', 'weight',
"processing time". "due date"]. index col=0).to dict('index')
     self.seed = seed
     self.tabu tenure = tabu tenure
     self.initial solution = self. get initial solution()
     self.best solution, self.best obj value = self. tabu search()
  def get initial solution(self):
     solution = list(range(1, len(self.instance dict) + 1))
     rd.seed(self.seed)
     rd.shuffle(solution)
     return solution
  def obj fun(self, solution):
     t = obi value = 0
     for job in solution:
       C i = t + self.instance dict[job]["processing time"]
       T i = max(0, C i - self.instance dict[job]["due date"])
       obj value += self.instance dict[job]["weight"] * T i
       t = C i
     return obj_value
  def swap move(self, solution, i, j):
     solution = solution.copy()
     solution[solution.index(i)], solution[solution.index(j)] =
solution[solution.index(j)], solution[solution.index(i)]
     return solution
  def get tabu structure(self):
```

```
return {swap: {'tabu time': 0, 'move value': float('inf')} for swap in
combinations(self.instance dict.keys(), 2)}
  def tabu search(self):
    tabu structure = self. get tabu structure()
     best solution = self.initial solution
     best obj value = self. obj fun(best solution)
     current solution = best solution
    current obj value = best obj value
    iter count, terminate = 1, 0
     while terminate < 100:
       for move in tabu structure:
          candidate solution = self. swap move(current solution,
move[0], move[1])
         tabu structure[move]['move value'] =
self. obj fun(candidate solution)
       while True:
          best move = min(tabu structure, key=lambda x:
tabu structure[x]['move value'])
          move_value, tabu_time =
tabu_structure[best_move]["move_value"],
tabu structure[best move]["tabu time"]
          if tabu time < iter count:
            current solution = self. swap move(current solution,
best move[0], best move[1])
            current obj value = self. obj fun(current solution)
            if move value < best obj value:
```

```
best solution, best obj value = current solution,
current obj value
              terminate = 0
            else:
              terminate += 1
            tabu structure[best move]['tabu time'] = iter count +
self.tabu tenure
            iter count += 1
            break
         elif move value < best obj value:
            current_solution = self._swap_move(current_solution,
best move[0], best move[1])
            best solution = current solution
            best obj value = self. obj fun(current solution)
            terminate = 0
            iter count += 1
            break
         tabu structure[best move]["move value"] = float('inf')
    return best_solution, best_obj_value
print("Starting Tabu search\n")
test = TS(path="Instance 10.xlsx", seed=2012, tabu tenure=3)
OUTPUT
Starting Tabu search
Iteration 1: Best objvalue: 29.220000000000002
```

Iteration 2: Best\_objvalue: 21.62

. . .

Tabu search completed

Performed iterations: 110

Best found Solution: [3, 2, 1, 4, 8, 10, 5, 9, 7, 6], Objvalue:

13.2400000000000002